

Department of Computer Science and Engineering,
University of Dhaka

Computer Graphics (CSE 4103)

Lecture 6

Basic Raster Graphics Algorithm for Drawing 2D Primitives



Clipping Line

Last Classes

1. *Incremental Line-drawing Algorithm*
2. *Mid-point Algorithm for Line-drawing*
 - i) *In only one Octant*
 - ii) *In all 8 octants*
 - iii) *8-way Symmetry*
 - iv) *Tangent Independent mid-point line drawing algorithm*
3. *Mid-point Algorithm for drawing Circle*
4. *Mid-point Algorithm for drawing Ellipse*

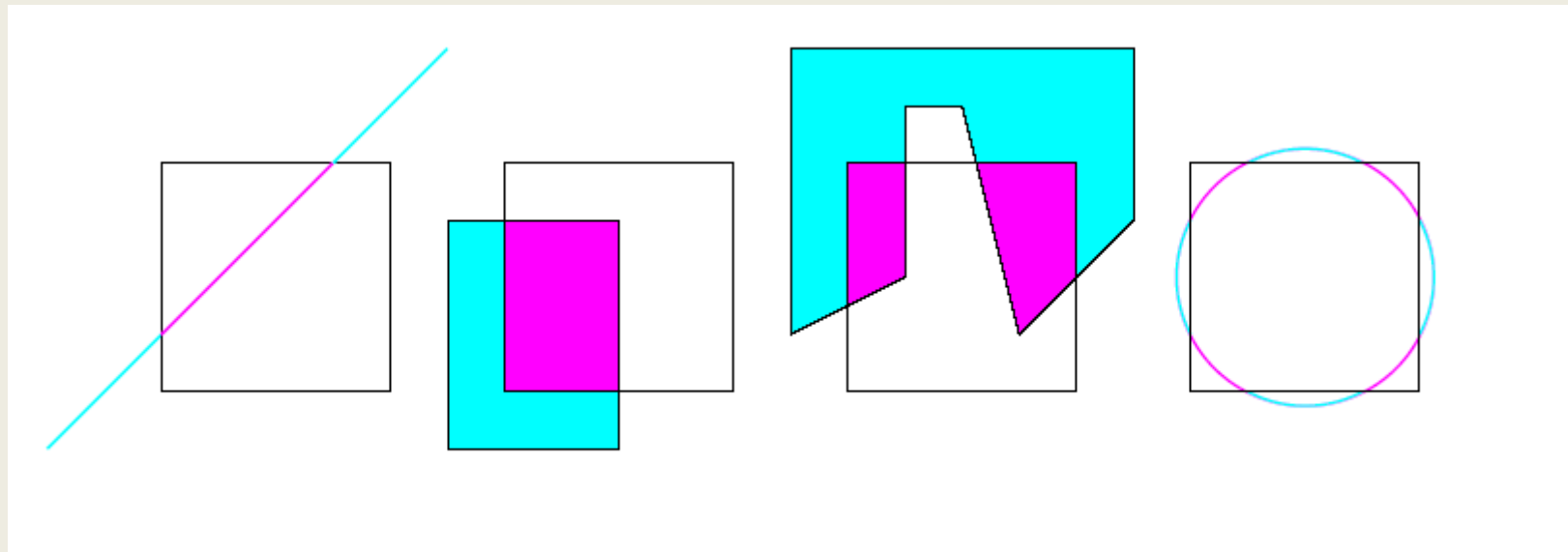
This Class

1. *Clipping lines using*
 - a) *Cohen-Sutherland Algorithm*
 - b) *Cyrus-Beck Algorithm*

What is Clipping

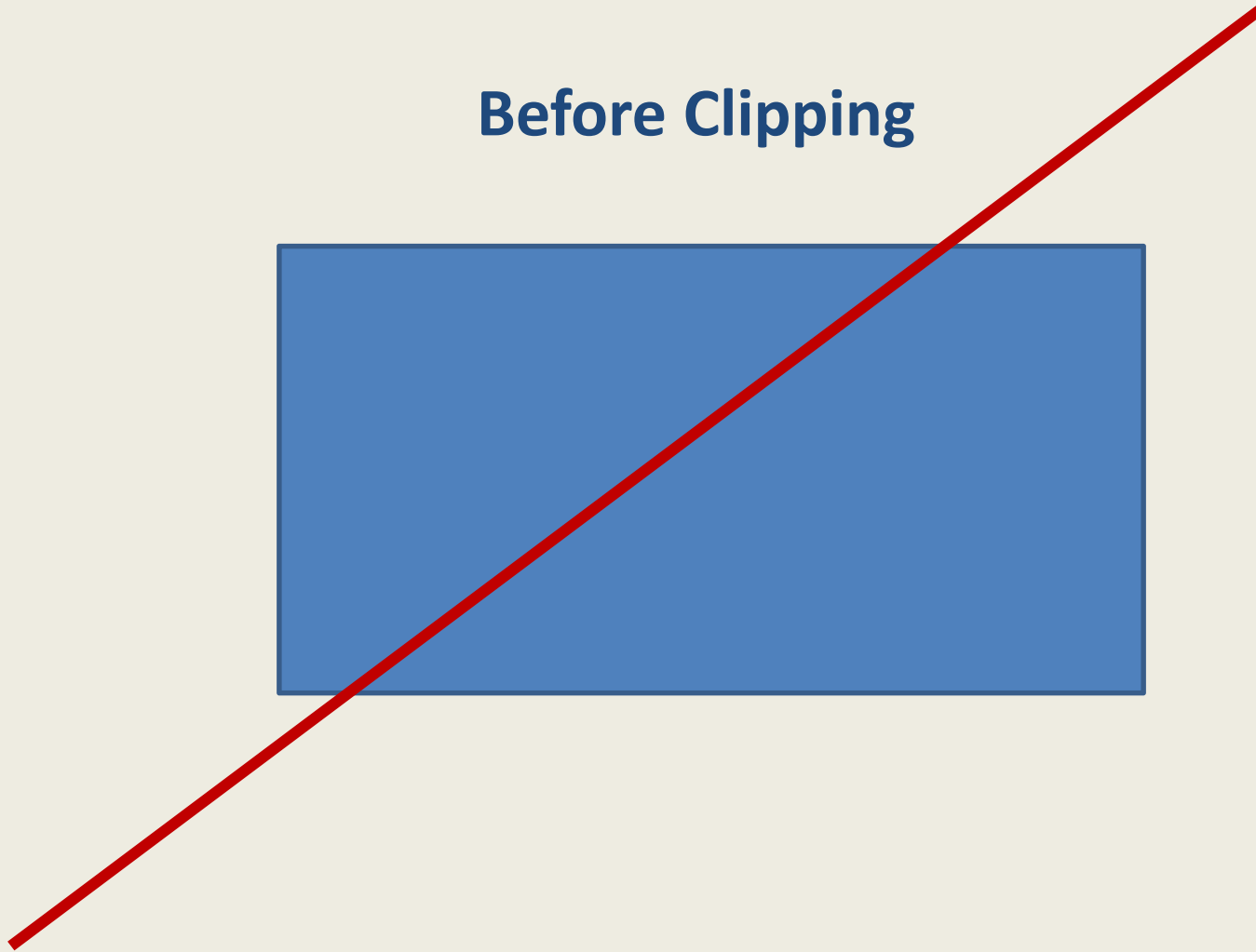
From Computer Graphic's context, Clipping “is a method to selectively enable or disable rendering operations within a defined region of interest”^[Wiki].

In general, Clipping is a technique to trimming down a given primitive with respect to an object.



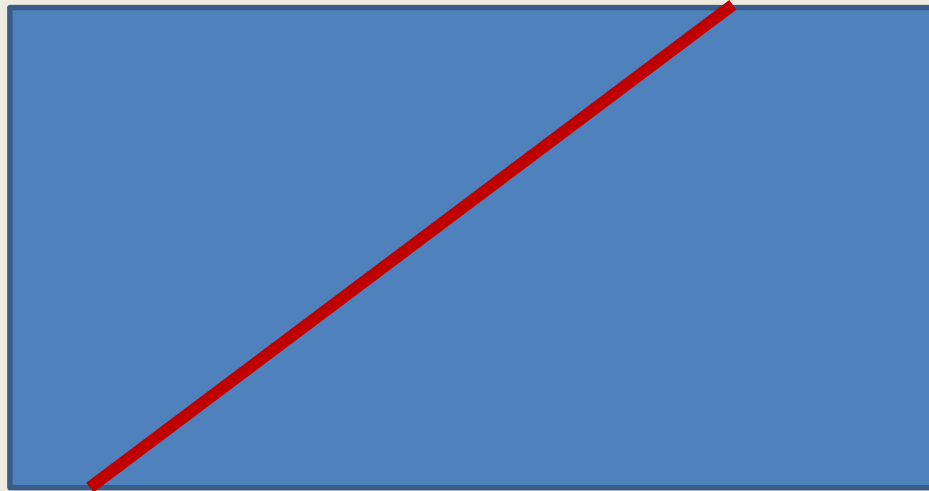
What is Clipping..

Before Clipping

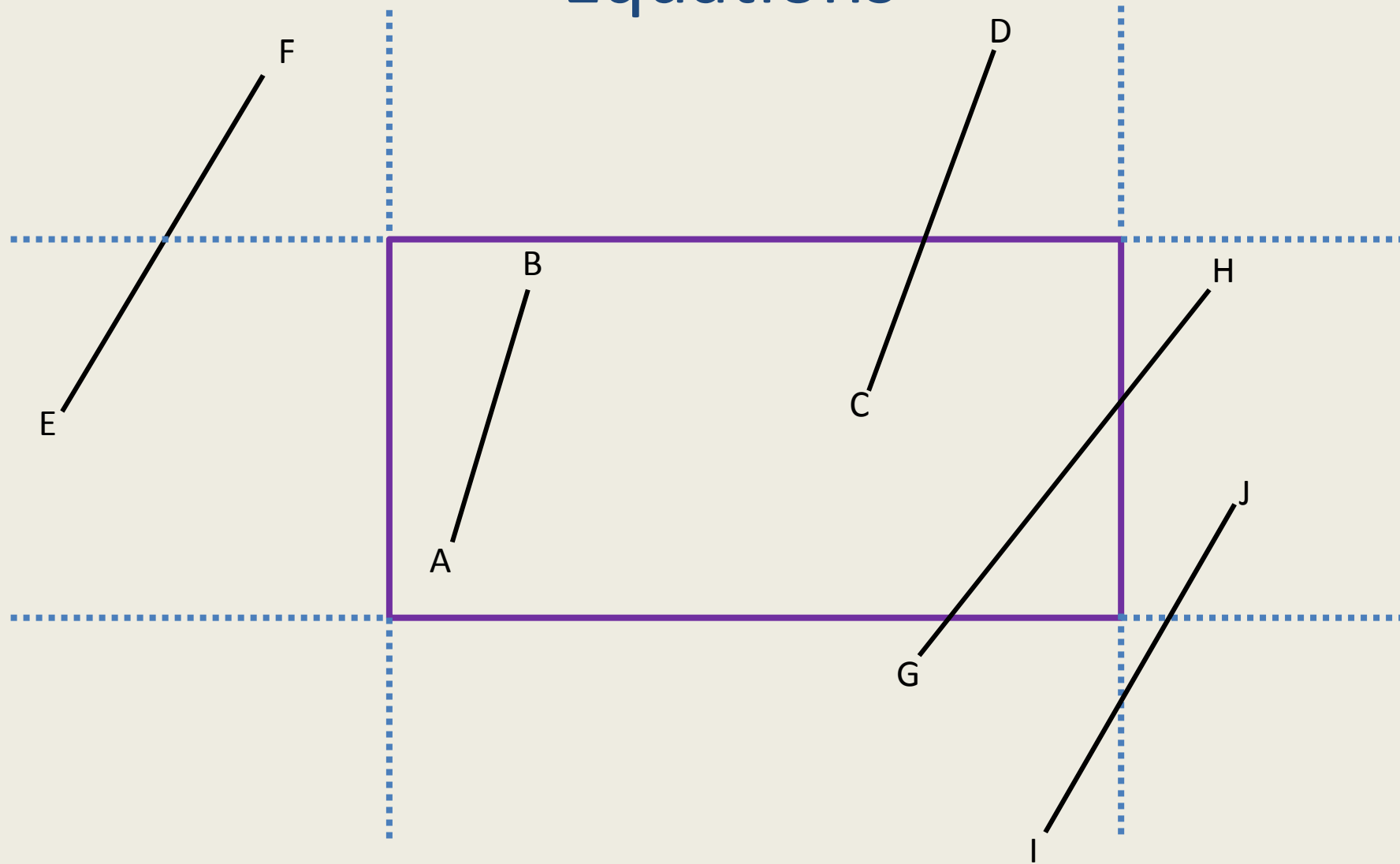


What is Clipping..

After Clipping



Clipping Lines by Solving Simultaneous Equations



Clipping Lines by Solving Simultaneous Equations..

Input: Coordinates of Lines, Four corners of rectangle $\{(x_{\min}, y_{\min}) (x_{\max}, y_{\max})\}$

Output: Clipped lines with respect to given rectangle

Step 1. **For** every line segment

Step 2: **If** the line is trivially accepted, do nothing

Step 3: **else** convert the line segment to equation of line (EL)

Step 4. consider the edges to equation of lines (EE)

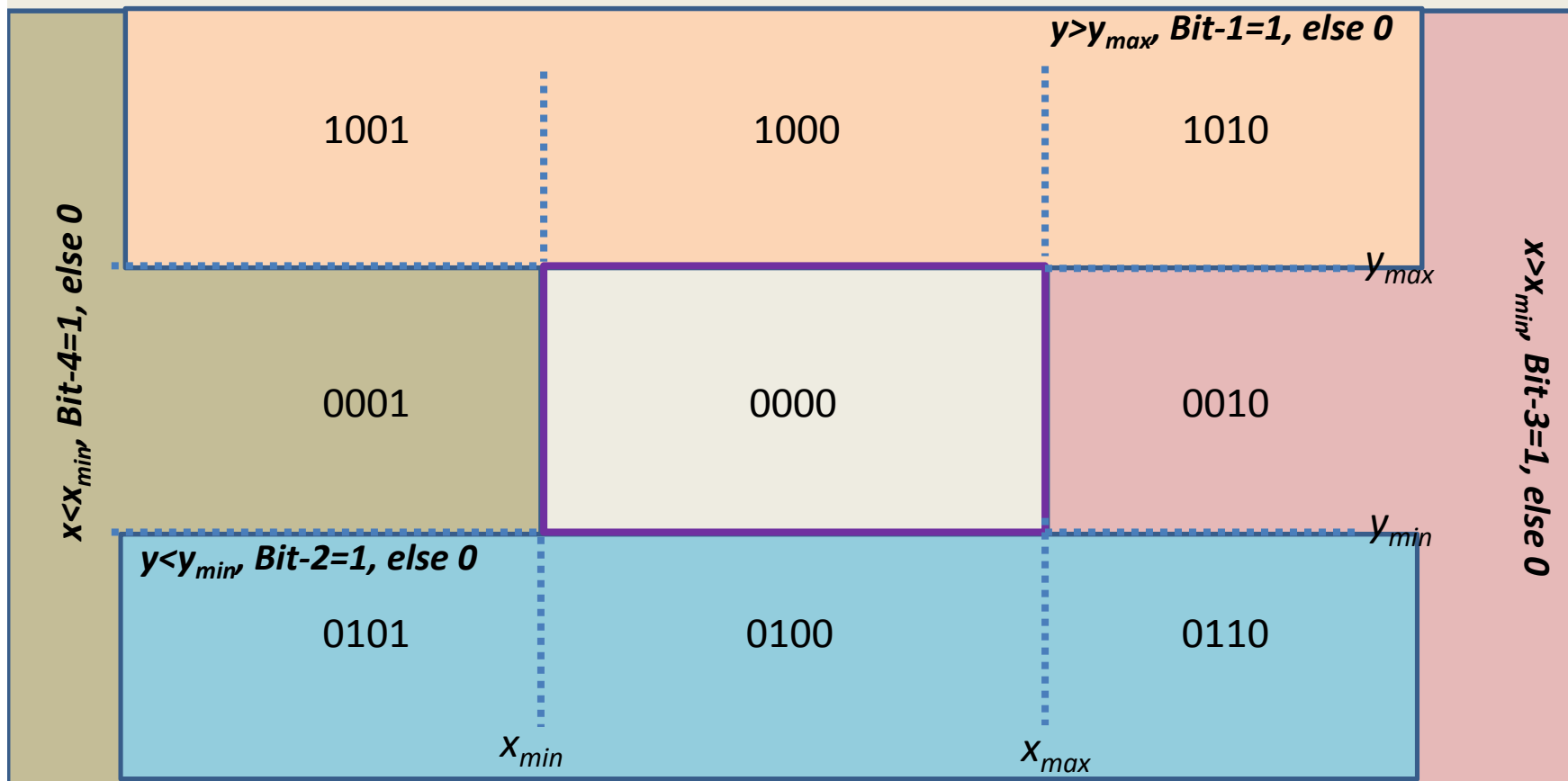
Step 5. consider every pair or (EL, EE_j)

Step 6. find the intersecting point between (EL, EE_j)

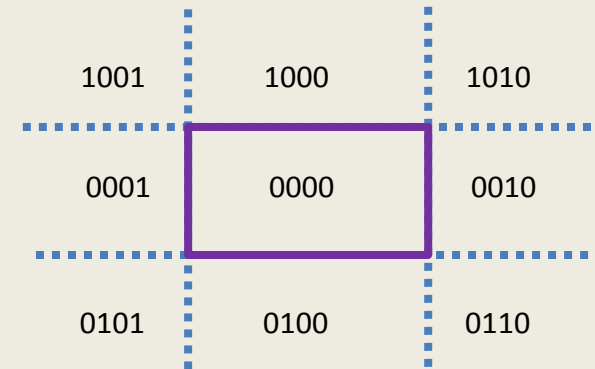
Step 7. validate the intersecting point with respect to $\{(x_{\min}, y_{\min}) (x_{\max}, y_{\max})\}$

Cohen-Sutherland Algorithm

- Divide viewplane into regions defined by viewport edges
- Assign each region a 4-bit outcode:

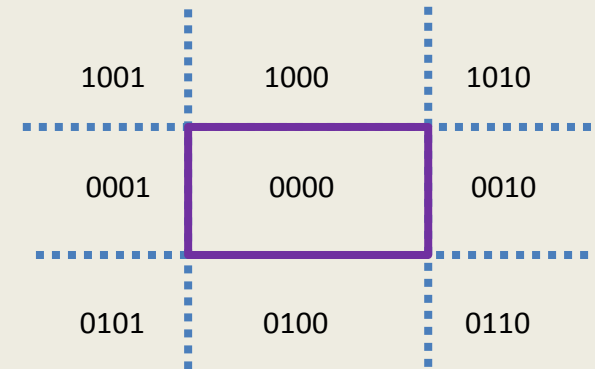


Cohen-Sutherland Algorithm..



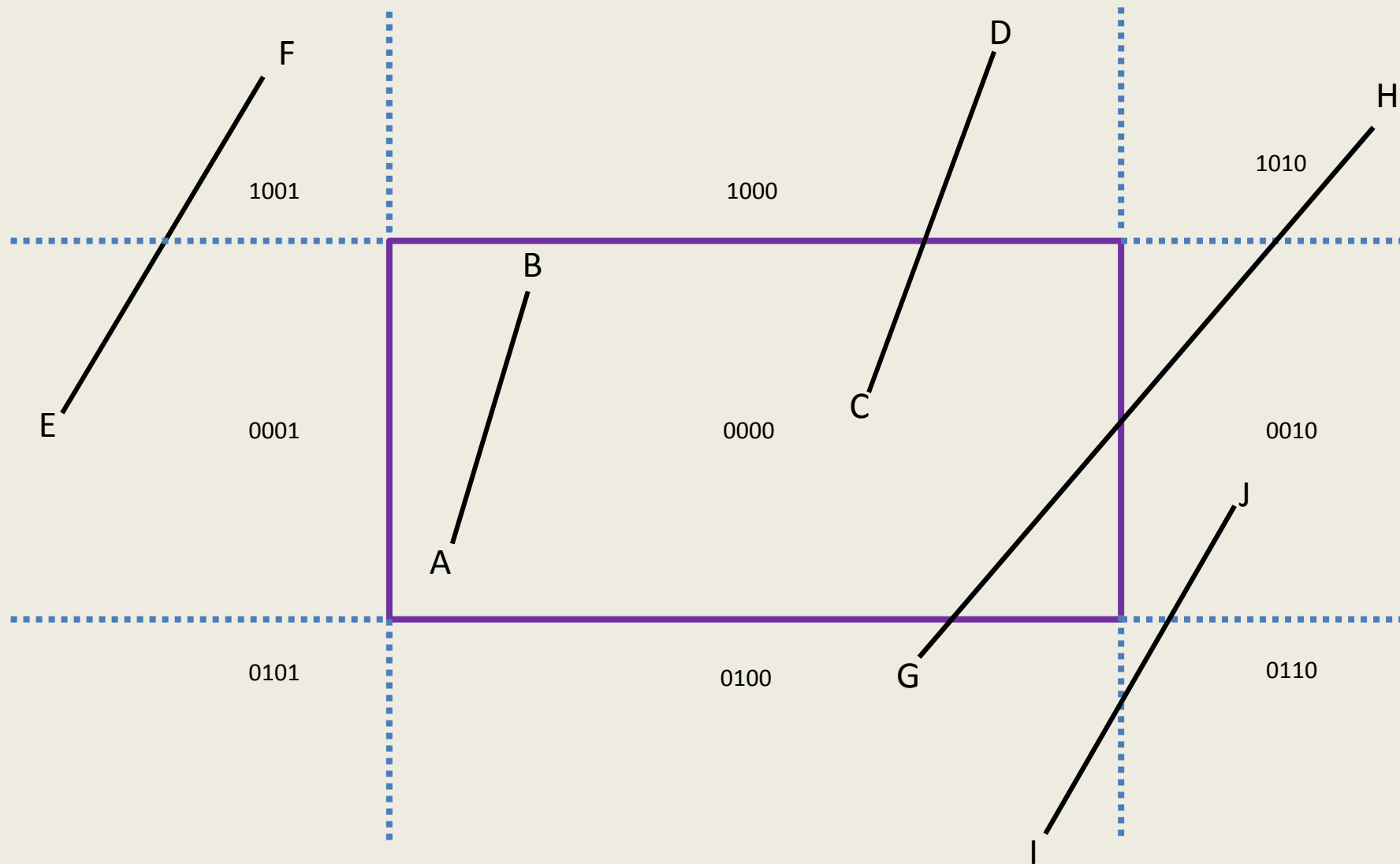
1. Check for trivial accept (both endpoints are in, i.e., outcode for both endpoints are 0000)
2. Check whether it line segment is trivially reject
 - (Trivially reject condition: Bit-wise AND of two outcode should be non-zero)
3. If line can be neither trivially accepted or trivially rejected, then split in two at a clip edge and iterate the same process.

Cohen-Sutherland Algorithm..

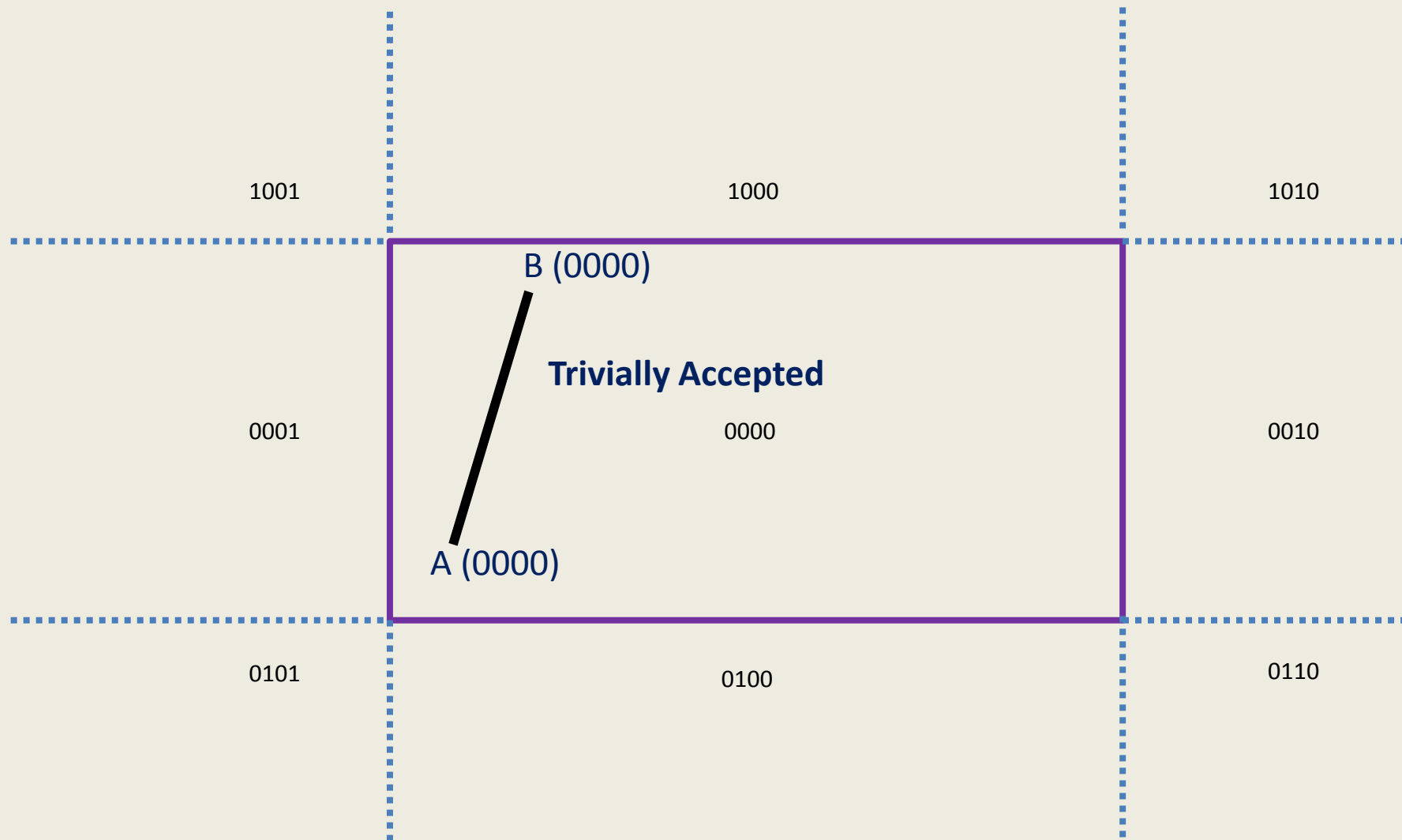


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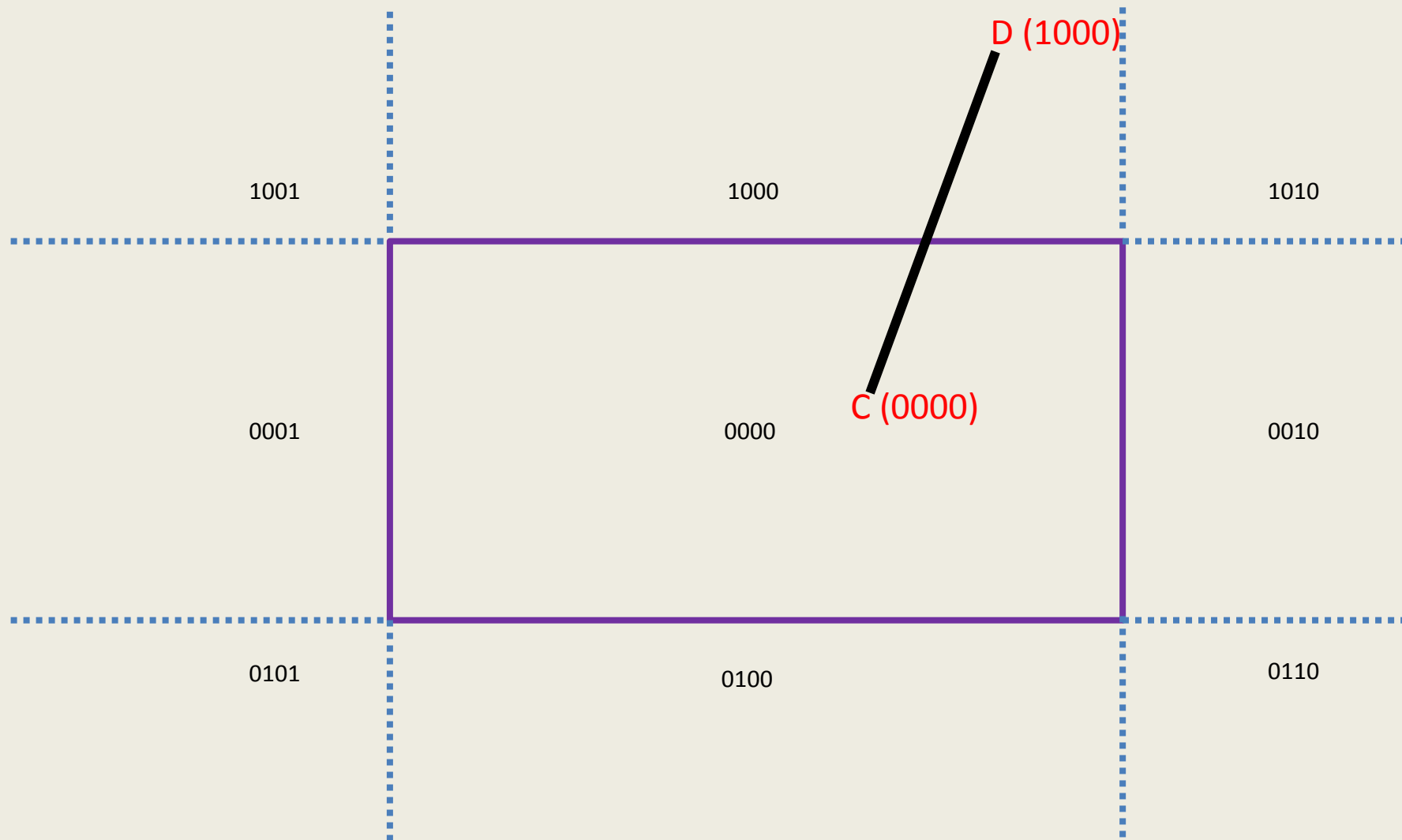
Cohen-Sutherland Algorithm..



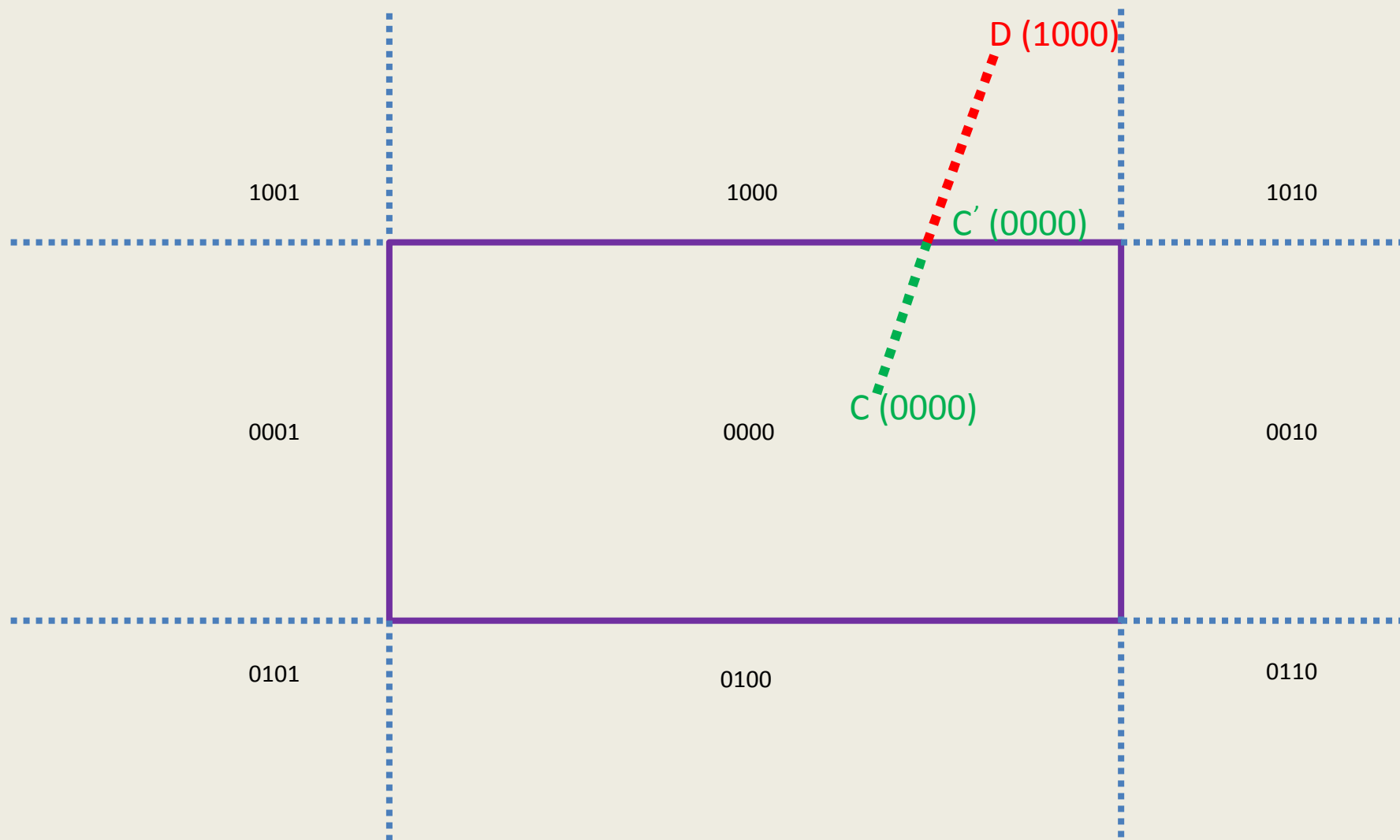
Cohen-Sutherland Algorithm..



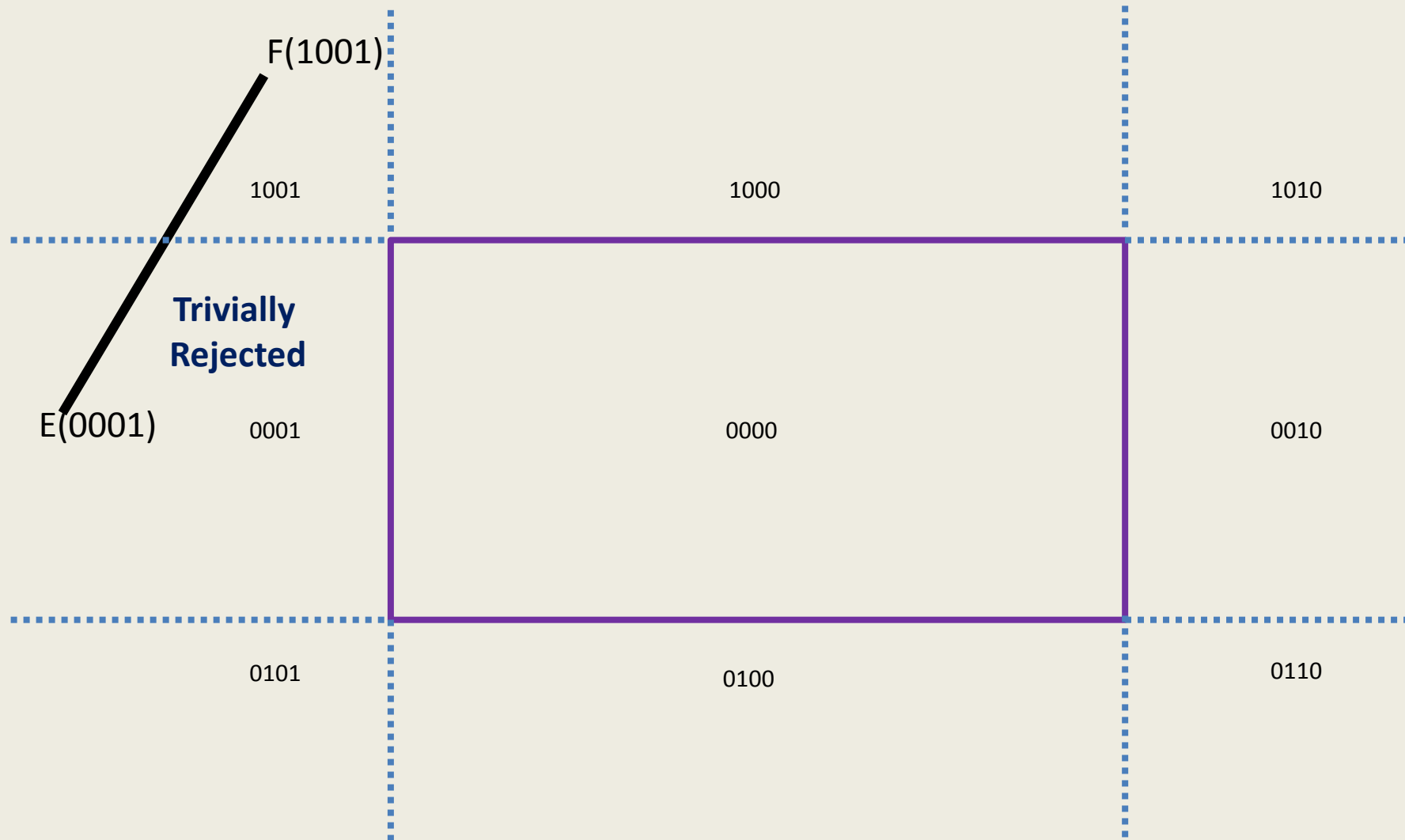
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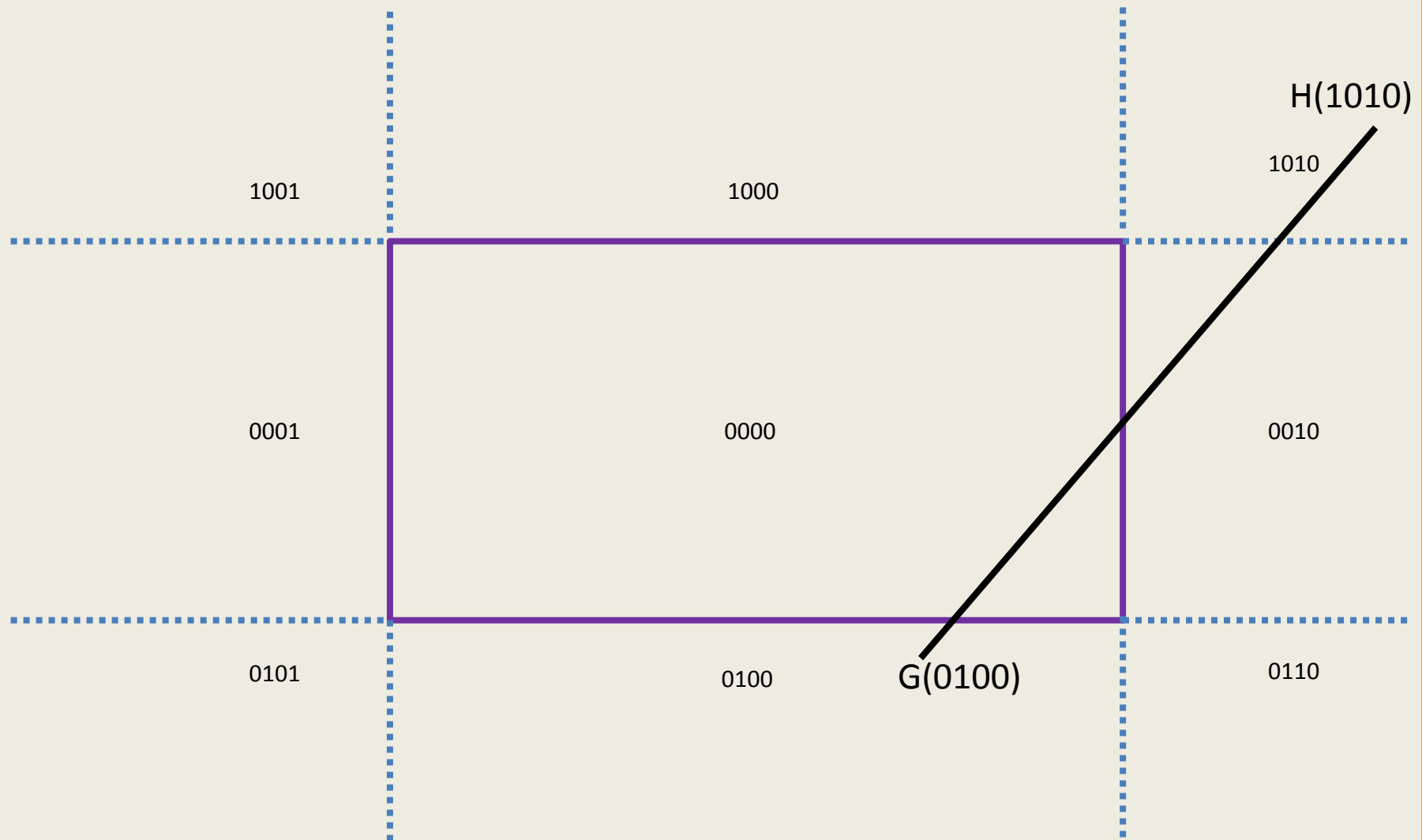
Cohen-Sutherland Algorithm..



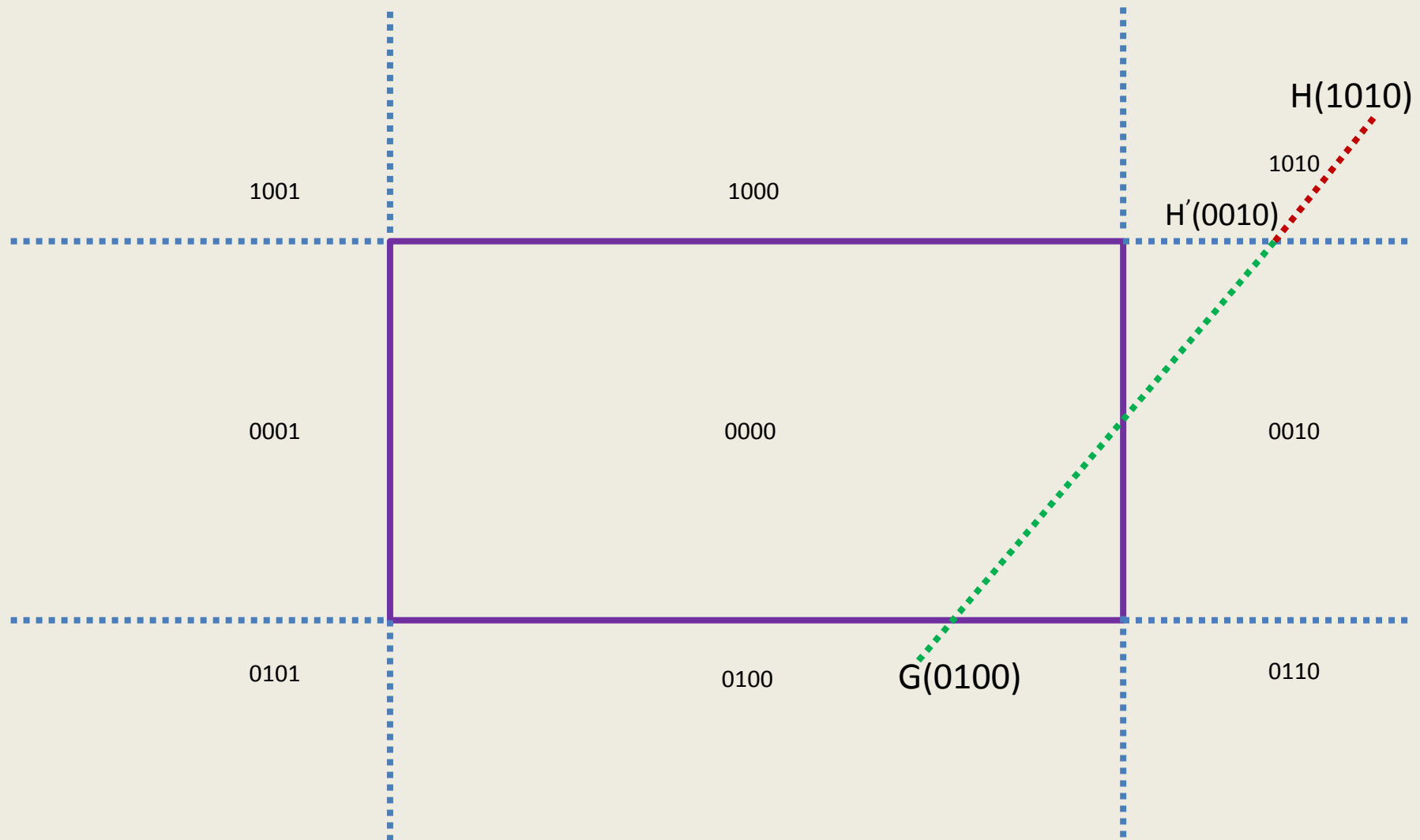
Cohen-Sutherland Algorithm..



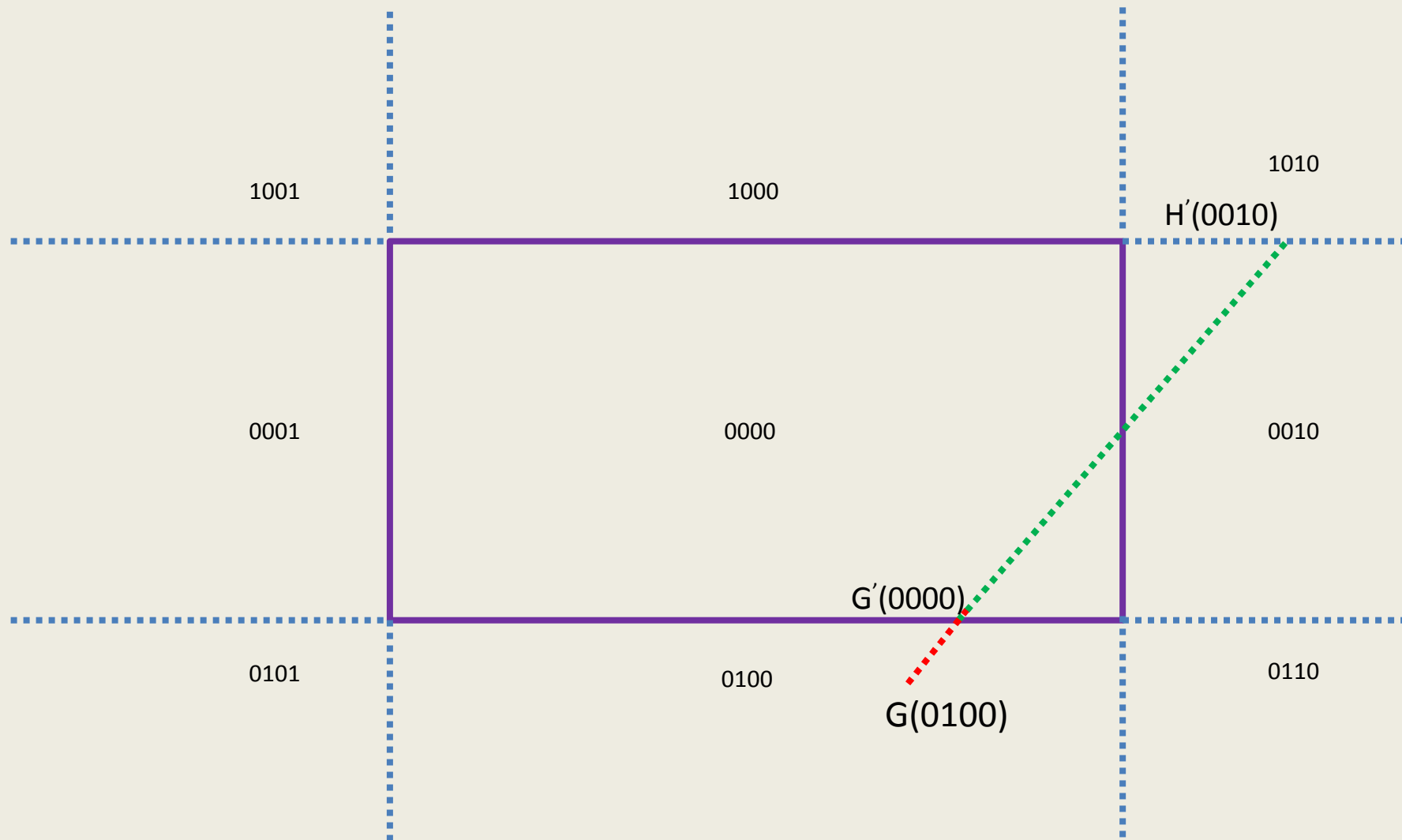
Cohen-Sutherland Algorithm..



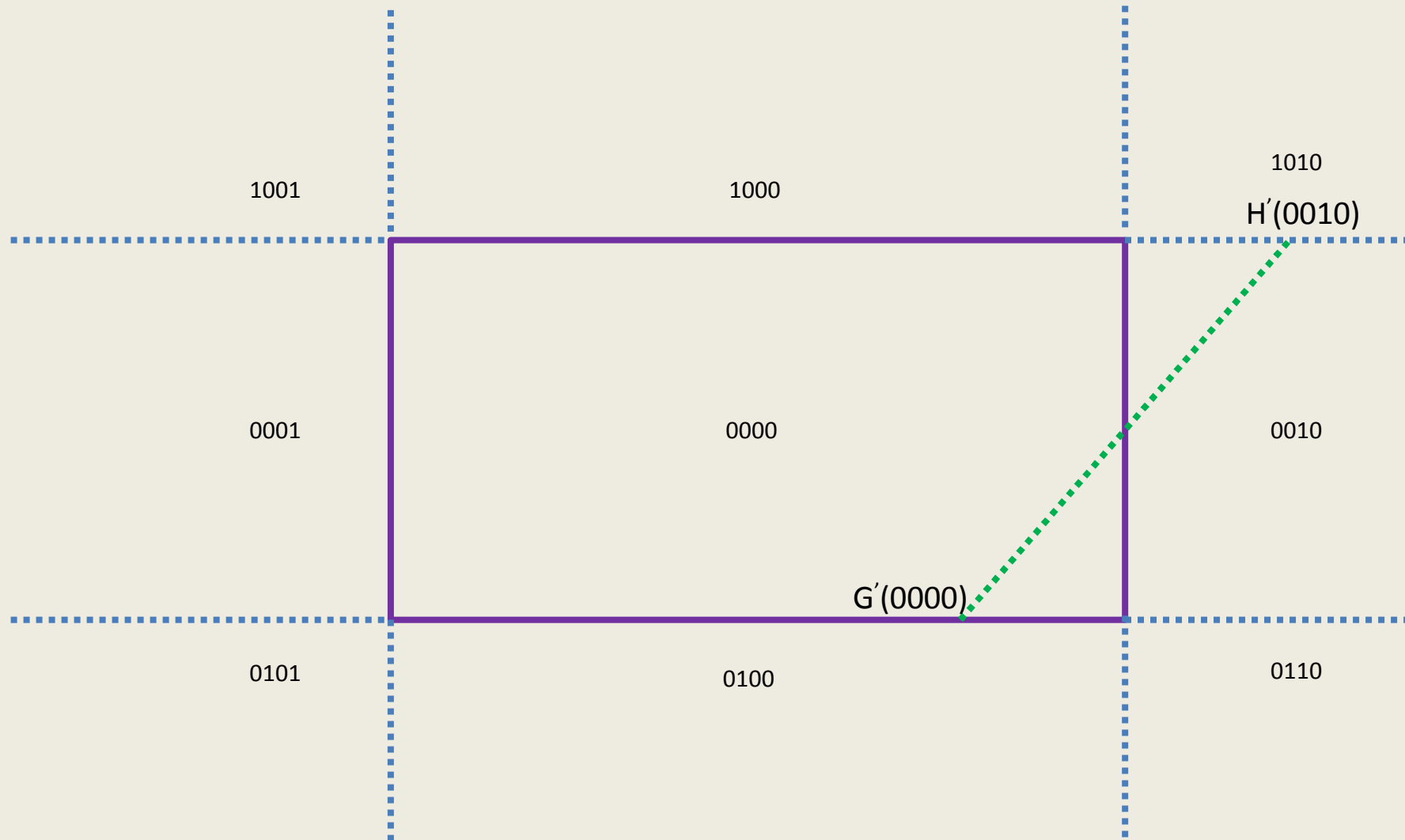
Cohen-Sutherland Algorithm..



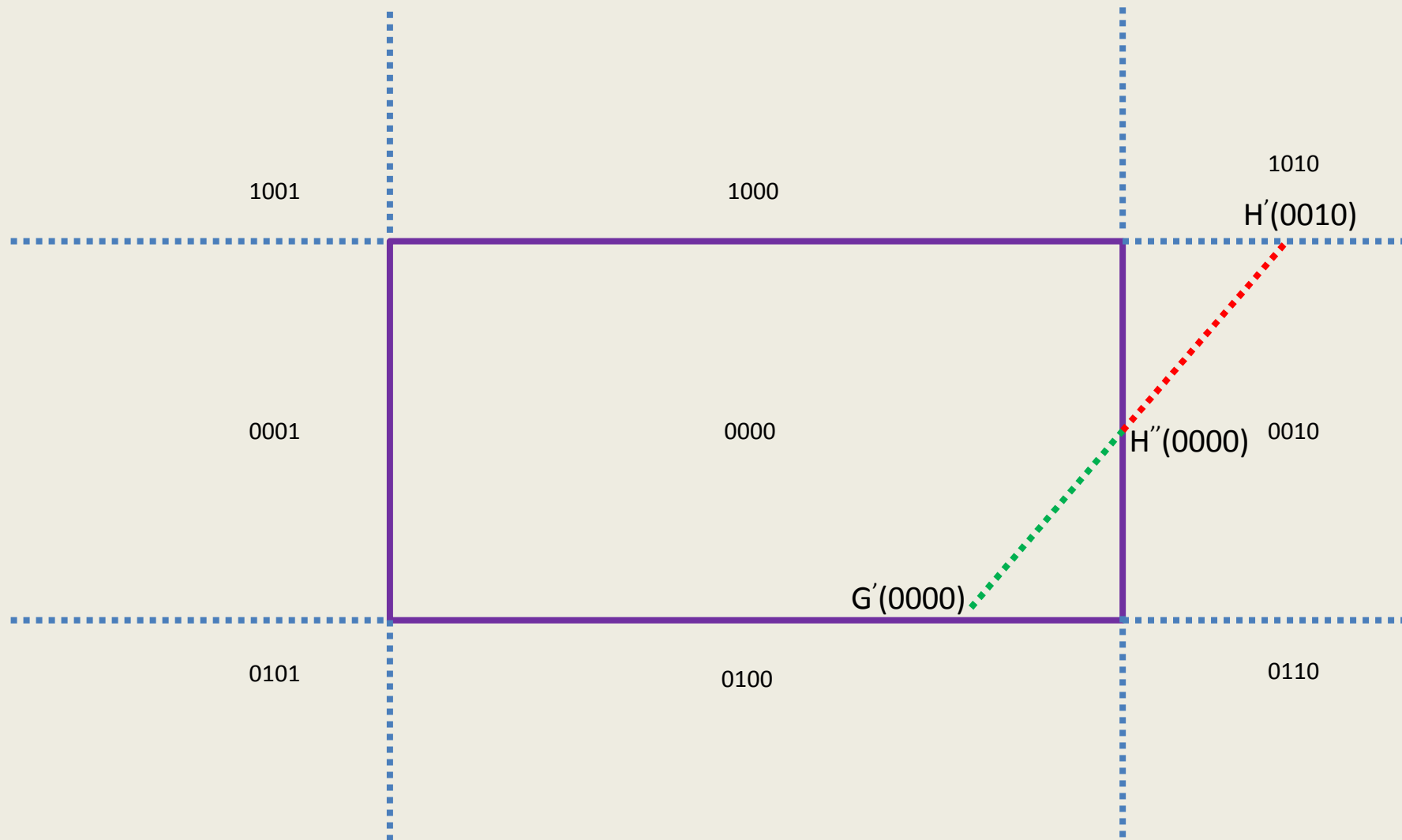
Cohen-Sutherland Algorithm..



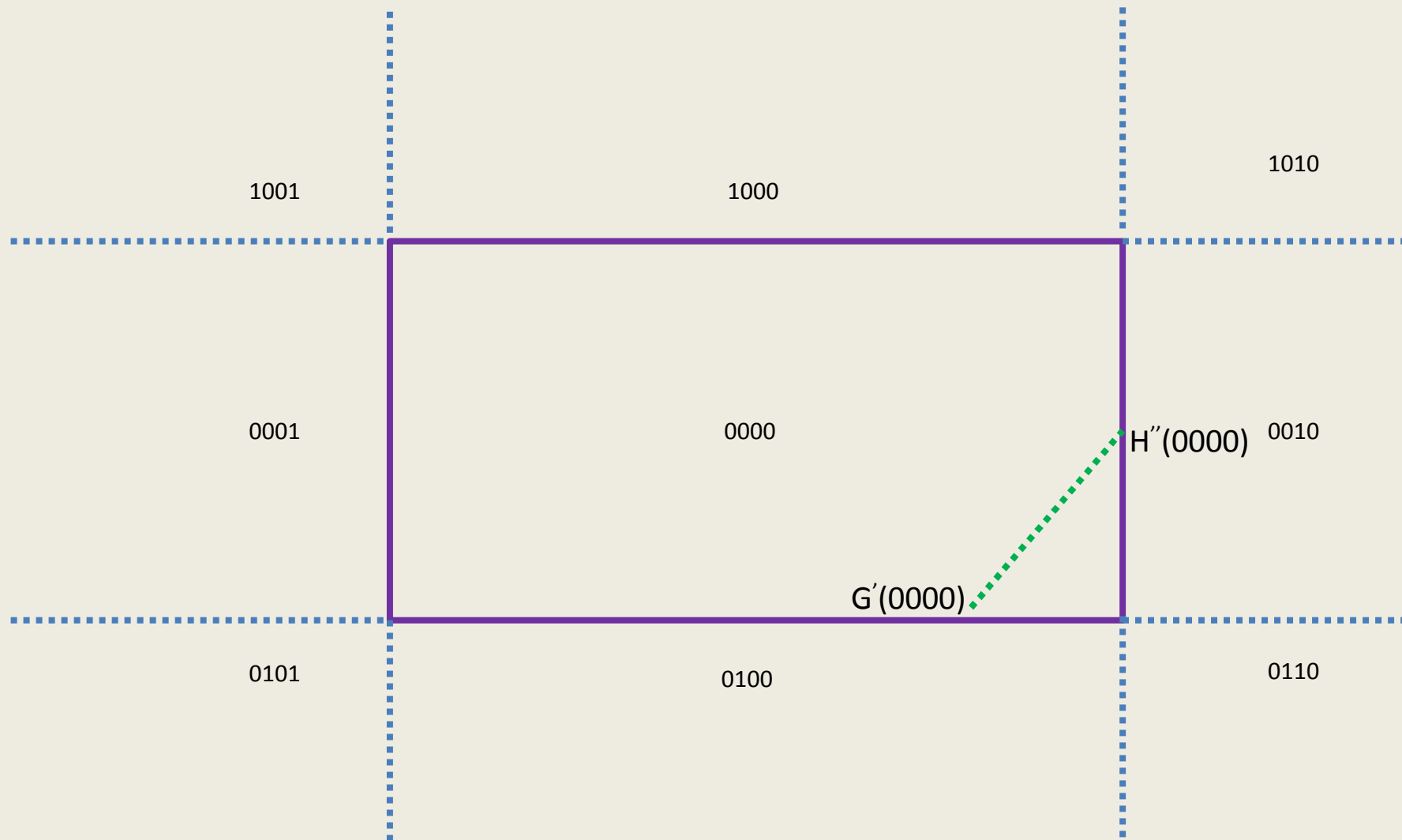
Cohen-Sutherland Algorithm..



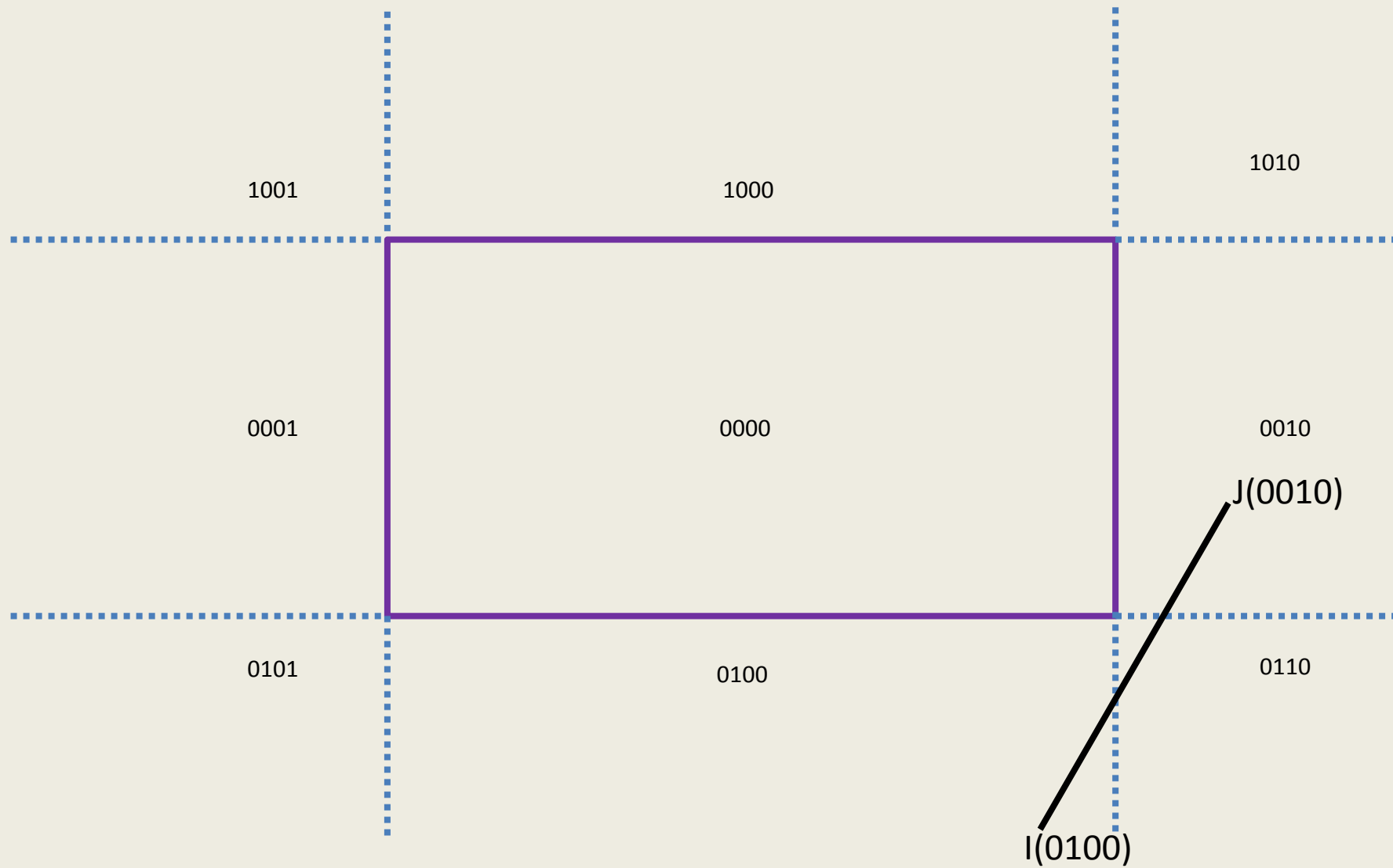
Cohen-Sutherland Algorithm..



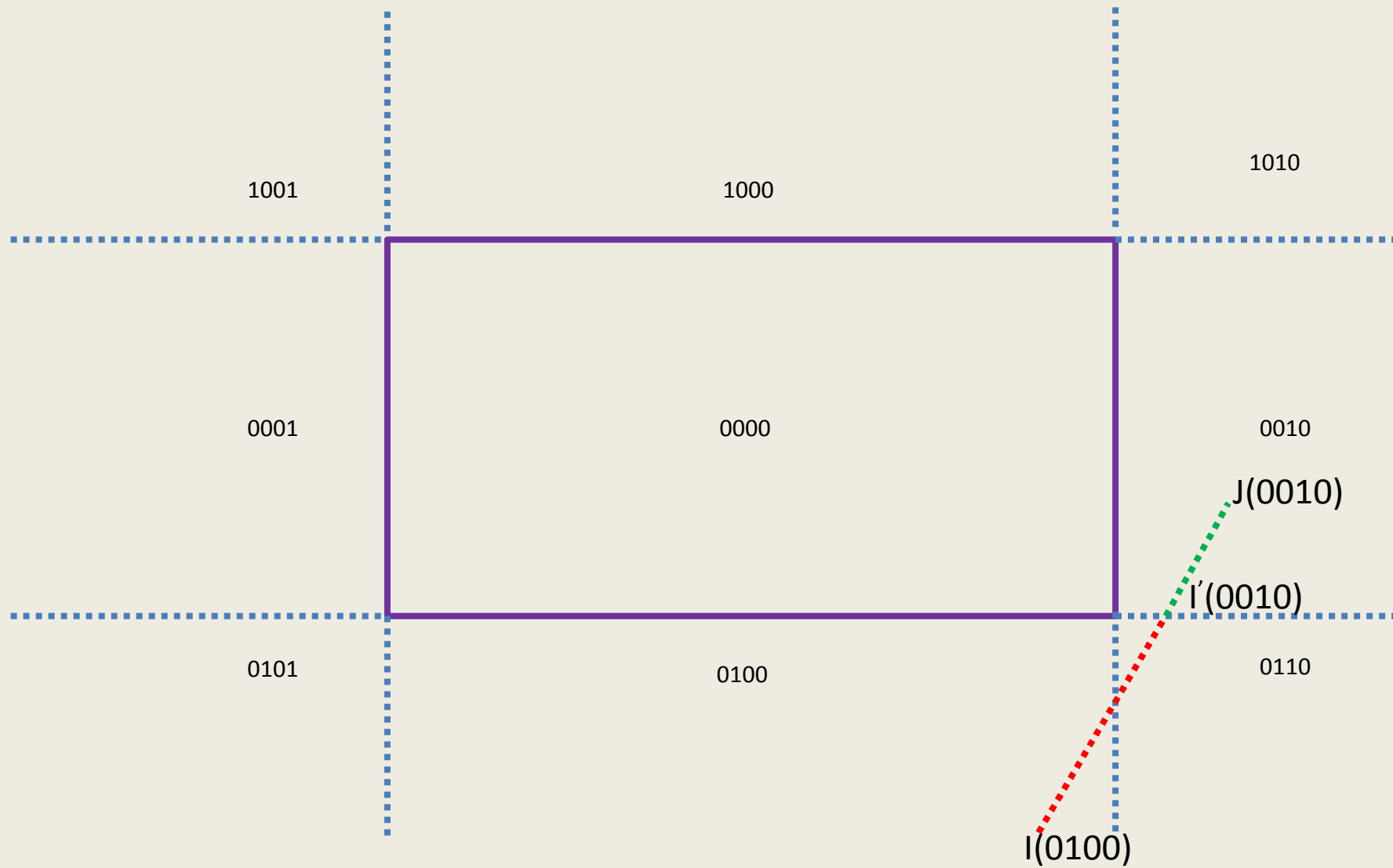
Cohen-Sutherland Algorithm..



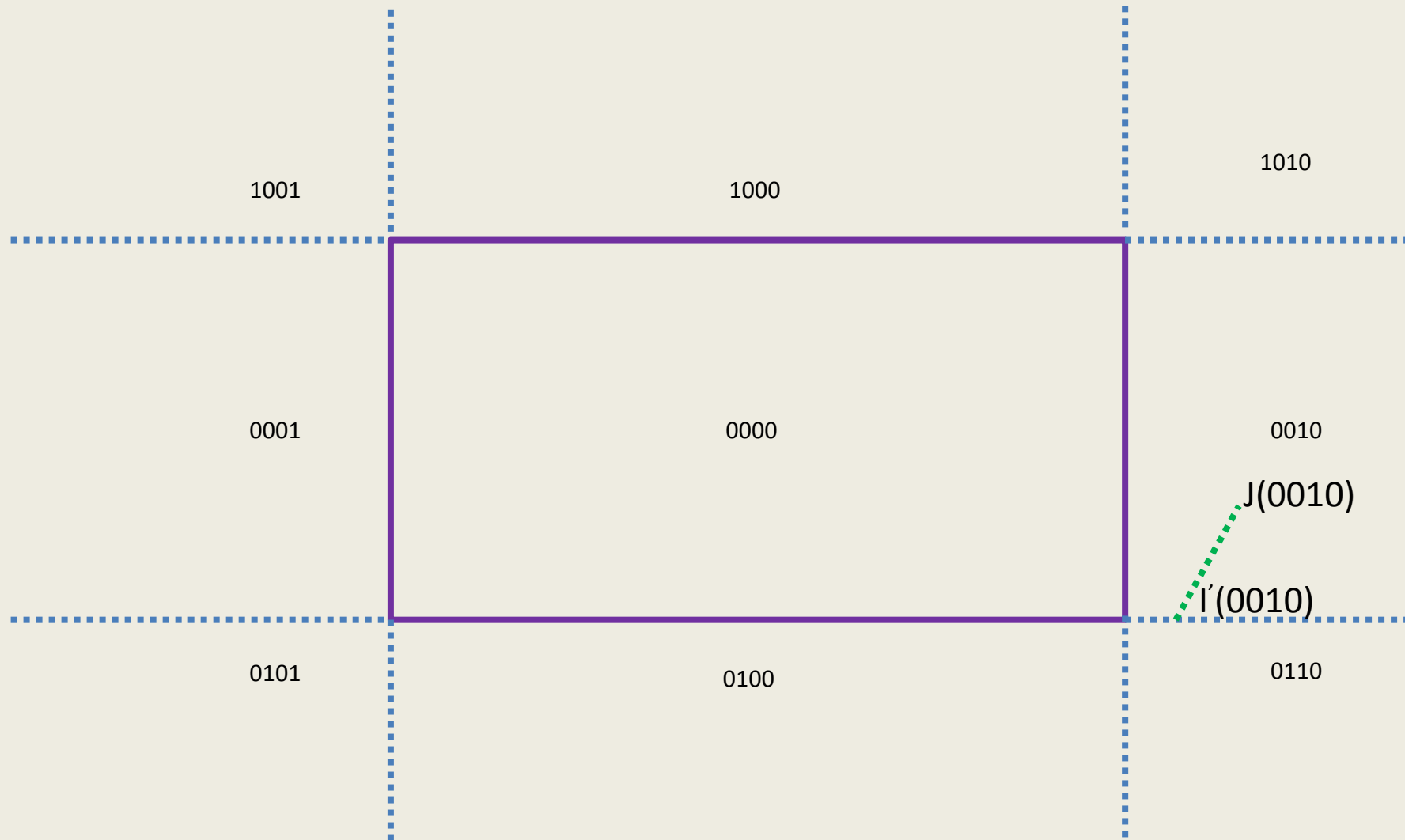
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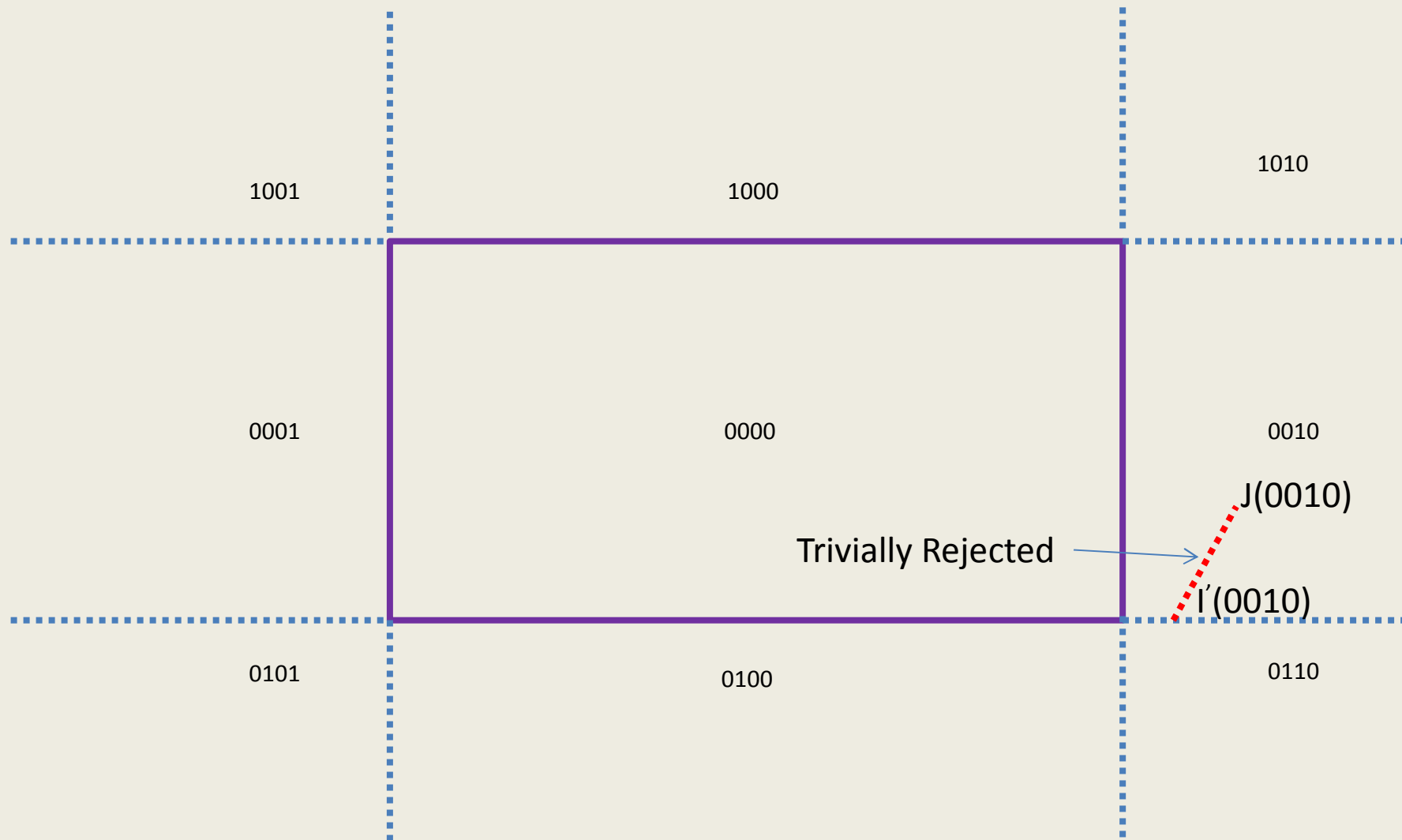
Cohen-Sutherland Algorithm..



Cohen-Sutherland Algorithm..



Cohen-Sutherland Algorithm..



Cyrus Beck Line Clipping Algorithm

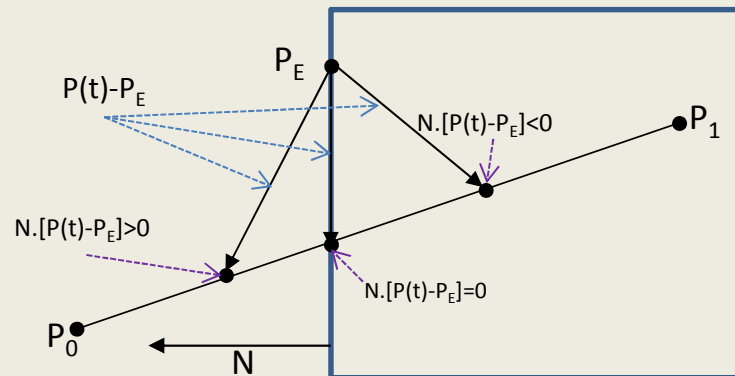
Parametric Line Equation:

$$P(t) = P_0 + (P_1 - P_0)t$$

$$P(0) = P_0$$

$$P(1) = P_1$$

P_E is any arbitrary value on the edge

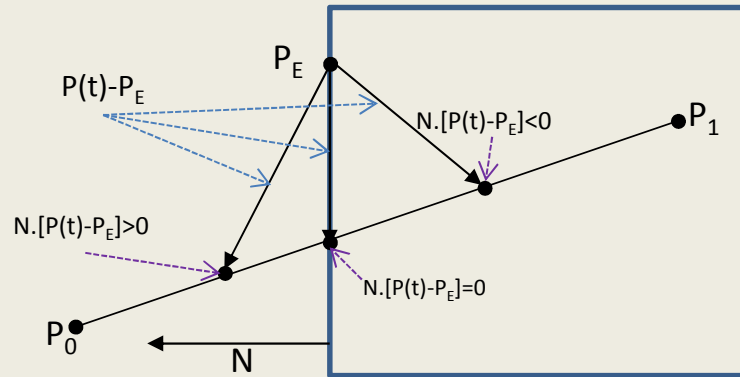


$$\begin{aligned} N.[P(t)-P_E] &= 0 \\ \Rightarrow N.[P_0 + (P_1 - P_0)t - P_E] &= 0 \\ \Rightarrow N.[P_0 - P_E] + N.[P_1 - P_0]t &= 0 \end{aligned}$$

$$\text{Let, } D = (P_1 - P_0)$$

$$t = \frac{N_i \cdot [P_0 - P_E]}{-N \cdot D}$$

Cyrus Beck Line Clipping Algorithm



$$t = \frac{N_i \cdot [P_0 - P_E]}{-N \cdot D}$$

For this to be true, the algorithm checks that

$N \neq 0$, normal should not be zero

$D \neq 0$, ($P_1 \neq P_0$)

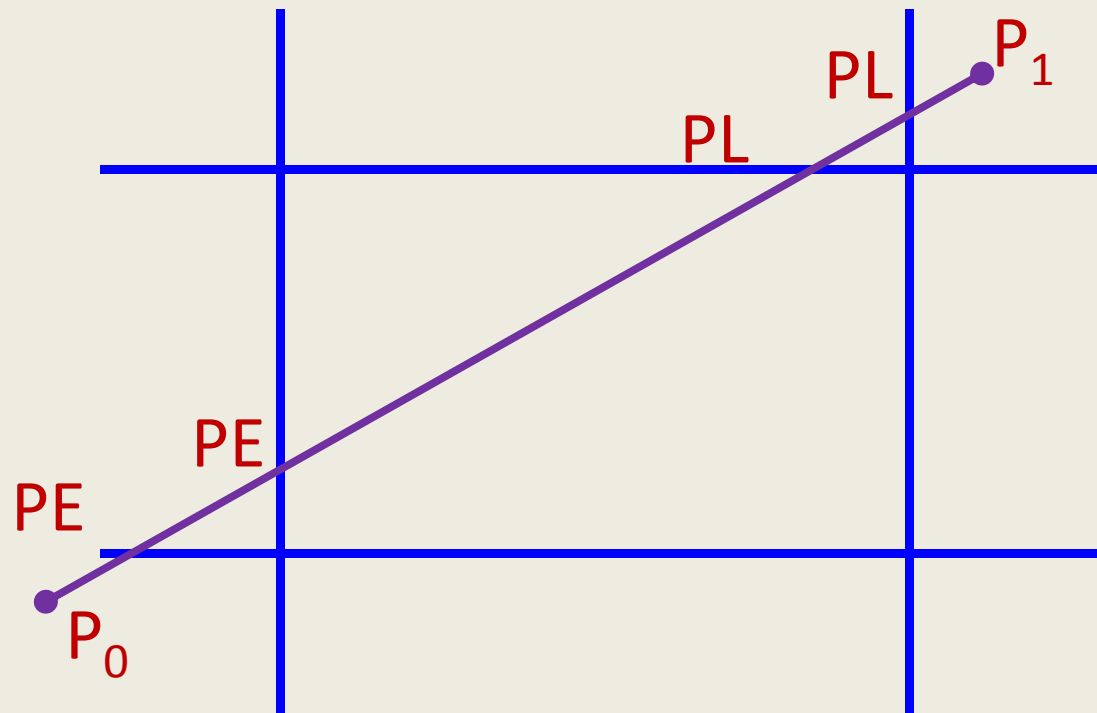
$N \cdot D \neq 0$ (Edge and line should not be parallel)

Cyrus Beck Line Clipping Algorithm

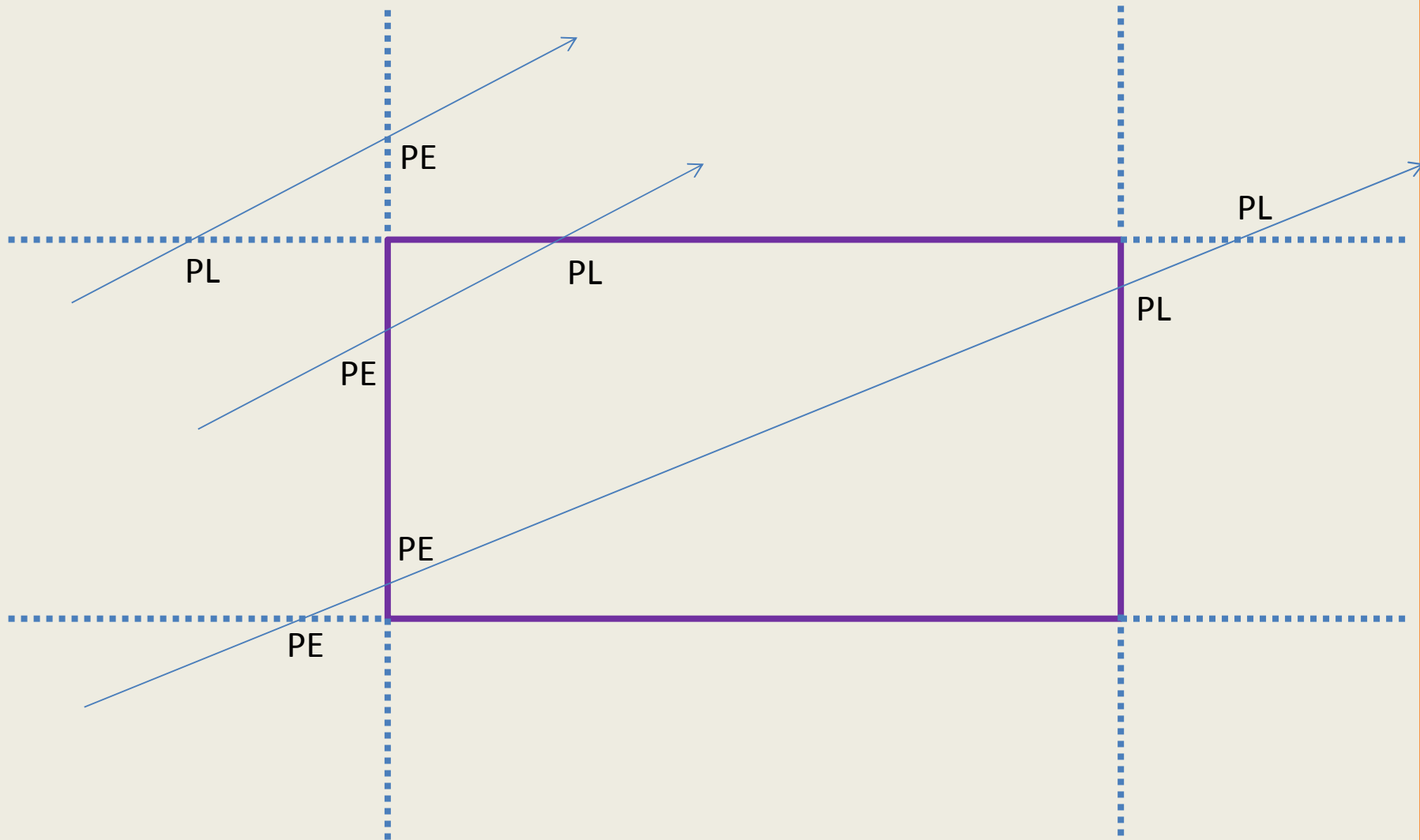
- Compute t for line intersection with all four edges by selecting in each of the four edges of clip rectangle
- Obtain the values for t
- Discard all ($t < 0$) and ($t > 1$)
- Classify each remaining intersection as
 - Potentially Entering (PE)
 - Potentially Leaving (PL)
- $N_L [P_1 - P_0] > 0$ implies PL
- $N_L [P_1 - P_0] < 0$ implies PE
 - Note that we computed this term when computing t

Cyrus Beck Line Clipping Algorithm..

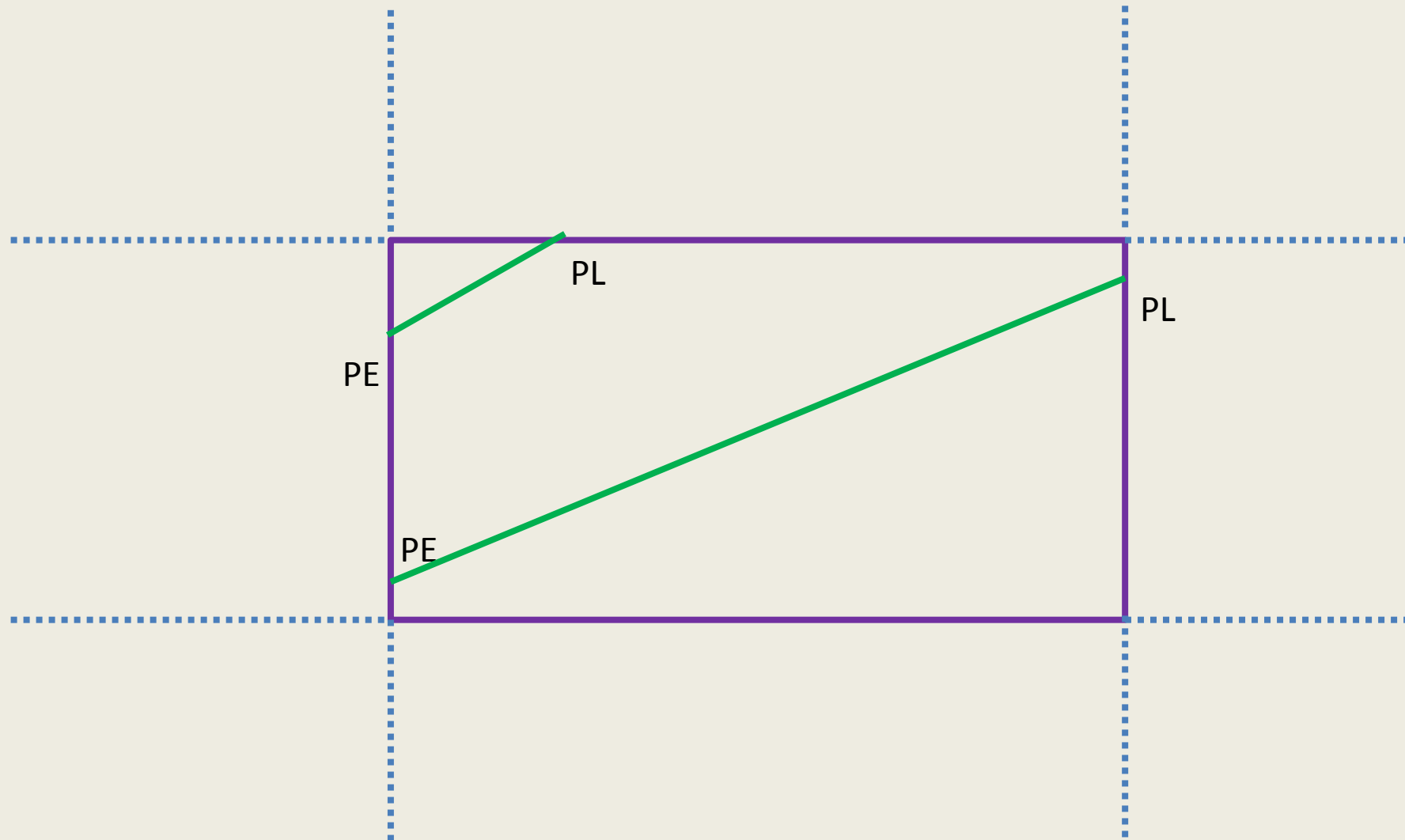
- Compute PE with largest t
- Compute PL with smallest t
- Clip to these two points



Cyrus Beck Line Clipping Algorithm..



Cyrus Beck Line Clipping Algorithm..



Thank you