

Coordinate Direction Angles

Angles between vector and positive x, y, z .

$\alpha, \beta, \gamma \in [0 \text{ deg}, 180 \text{ deg}]$

$$\cos \alpha = \frac{A_x}{A} \quad \cos \beta = \frac{A_y}{A} \quad \cos \gamma = \frac{A_z}{A}$$

$$\vec{A} = A \cos \alpha \hat{i} + A \cos \beta \hat{j} + A \cos \gamma \hat{k}$$

$$\hat{u}_A = \frac{\vec{A}}{A} = \cos \alpha \hat{i} + \cos \beta \hat{j} + \cos \gamma \hat{k}$$

$$\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$

Dot Product

$$\vec{A} \cdot \vec{B} = AB \cos \theta$$

$$\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z$$

Projection of a Vector

$$\text{proj}_{\vec{A}}(\vec{B}) = \frac{\vec{B} \cdot \vec{A}}{\vec{A} \cdot \vec{A}} \vec{A}$$

Transverse & Azimuthal Angles

Cross Product

$$\vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix}$$

Triple Scalar Product

$$\vec{C} \cdot (\vec{A} \times \vec{B})$$