# predicting carseats sales trees

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# 1 Predicting Carseats Sales with Decision Trees and Ensemble Methods

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#### 1.1 Motivation

Retailers often want to understand what drives **product sales** and how to best predict them. In this project, I use the **Carseats dataset** from the ISLP package to predict Sales as a quantitative response. I apply and compare **tree-based regression methods**: - Decision Trees (with pruning) - Bagging - Random Forests

The goal is to evaluate predictive accuracy, interpretability, and feature importance across methods, building on concepts explored in ISLP.

## 1.2 Data Analysis

## 1.2.1 Importing Necessary Dependencies

We begin by importing important libraries and the dataset, which is loaded using the ISLP libraries. We then split the dataset into 70% training and 30% test observations.

```
[1]: import numpy as np
  import pandas as pd
  import matplotlib.pyplot as plt
  import sklearn.model_selection as skm
  from ISLP import load_data
  from ISLP.models import ModelSpec as MS
  from sklearn.tree import DecisionTreeRegressor as DTR
  from sklearn.ensemble import RandomForestRegressor as RF

# Load Carseats dataset
  Carseats = load_data('Carseats')

# Create design matrix with all predictors except Sales
  model = MS(Carseats.columns.drop('Sales'), intercept = False)
  D = model.fit_transform(Carseats)

feature_names = list(D.columns)
```

```
X = np.asarray(D)

# Split dataset train (70%) and test (30%)
(X_train, X_test, y_train, y_test) = skm.train_test_split(X, Carseats['Sales'], u_test_size = 0.3, random_state = 0)

Carseats
```

[1]:	Sales	CompPrice	Income	Advertising	Population	Price	ShelveLoc	Age	\
0	9.50	138	73	11	276	120	Bad	42	
1	11.22	111	48	16	260	83	Good	65	
2	10.06	113	35	10	269	80	Medium	59	
3	7.40	117	100	4	466	97	Medium	55	
4	4.15	141	64	3	340	128	Bad	38	
	•••	•••	•••	•••					
395	12.57	138	108	17	203	128	Good	33	
396	6.14	139	23	3	37	120	Medium	55	
397	7.41	162	26	12	368	159	Medium	40	
398	5.94	100	79	7	284	95	Bad	50	
399	9.71	134	37	0	27	120	Good	49	

	Education	Urban	US
0	17	Yes	Yes
1	10	Yes	Yes
2	12	Yes	Yes
3	14	Yes	Yes
4	13	Yes	No
	•••		
395	14	Yes	Yes
396	11	No	Yes
397	18	Yes	Yes
398	10	V	Yes
	12	res	res
399	16	Yes	

[400 rows x 11 columns]

The response variable is Sales, the unit sales (in thousands) at every location. The predictors are:
- CompPrice: Price charged by competitor at each location - Income: Community income level
(in thousands of dollars) - Advertising: Local advertising budget for company at each location
(in thousands of dollars) - Population: Population size in region (in thousands) - Price: Price
company charges for car seats at each site - ShelveLoc: A factor with levels Bad, Good and Medium
indicating the quality of the shelving location for the car seats at each site - Age: Average age of
the local population - Education: Education level at each location - Urban: A factor with levels
No and Yes to indicate whether the store is in an urban or rural location - US: A factor with levels
No and Yes to indicate whether the store is in the US or not

## 1.2.2 Decision Tree Regressor

We begin with the simplest model, the decision tree. Decision trees provide an interpretable model for regression problems. However, unpruned trees often overfit, so we compare:

- 1. A **full tree** (no pruning)
- 2. A **pruned tree** chosen via cross-validation and cost-complexity pruning

```
[2]: # Create the Decision Tree Regressor model with a fixed random state forusereproducibility
reg = DTR(random_state = 0)

# Fit the model to the training dataset
reg.fit(X_train , y_train)

# Predict values of test dataset
preds = reg.predict(X_test)

# Compute and print test MSE (error metric)
full_mse = np.mean((preds - y_test)**2)
print(f"Test MSE (full tree): {full_mse}")
print(f"Number of terminal nodes (full tree): {reg.get_n_leaves()}")
```

```
Test MSE (full tree): 5.083071666666667
Number of terminal nodes (full tree): 277
```

We now train a pruned tree by utilizing k-fold cross validation with k = 5 to see if the testing MSE will decrease.

```
[3]: # Cost-complexity pruning path
    ccp_path = reg.cost_complexity_pruning_path(X_train, y_train)

# Cross-validation to select optimal alpha
    kfold = skm.KFold(5, shuffle = True, random_state = 10)
    grid = skm.GridSearchCV(
        reg, {'ccp_alpha': ccp_path.ccp_alphas},
        refit = True, cv = kfold, scoring='neg_mean_squared_error'
)

# Fit the model to the training dataset
    G = grid.fit(X_train, y_train)
    best_ = grid.best_estimator_

# Compute and print test MSE for pruned tree
    cv_mse = np.mean((y_test - best_.predict(X_test))**2)
    print(f"Test MSE (pruned tree): {cv_mse}")
    print(f"Number of terminal nodes (pruned tree): {best_.get_n_leaves()}")
```

Test MSE (pruned tree): 4.431070971603666 Number of terminal nodes (pruned tree): 55 Despite dropping to 55 terminal nodes in the pruned tree as opposed to the 277 terminal nodes in the full tree, we improve the test MSE by over 10%, showcasing the power of pruned trees in capturing data patterns and delivering accurate predictions while reducing complexity by preventing overfitting.

## 1.2.3 Bagging

Bagging (Bootstrap Aggregating) reduces variance by training many trees on bootstrap samples and averaging their predictions. This typically improves predictive accuracy compared to a single tree by preventing overfitting and introducing randomization (through bootstrapping). We also examine **feature importance** to see which predictors matter most for Sales.

```
[4]: # Create the bagging model (random forest with all predictors considered)
     bag_carseats = RF(max_features = X_train.shape[1], random_state = 0)
     # Fit the model to the training dataset
     bag_carseats.fit(X_train, y_train)
     # Predict values of the test dataset
     bag_preds = bag_carseats.predict(X_test)
     # Compute and print test MSE
     bag_mse = np.mean((bag_preds - y_test)**2)
     print(f"Test MSE (bagging): {bag_mse}")
     # Compute feature importance
     importances = bag_carseats.feature_importances_
     feature_importance_df = pd.DataFrame({
         'Feature': feature_names,
         'Importance': importances
     })
     # Sort feature importances in descending order and print
     feature_importance_df = feature_importance_df.sort_values(by='Importance',__
      →ascending=False)
     print("Feature importance for bagging model:")
     print(feature_importance_df)
```

Test MSE (bagging): 2.0077445197500015 Feature importance for bagging model:

```
Feature Importance
4
                Price
                          0.278666
5
      ShelveLoc[Good]
                          0.222431
7
                          0.108637
                   Age
0
            CompPrice
                          0.097085
6
    ShelveLoc[Medium]
                          0.082965
2
          Advertising
                          0.074627
1
               Income
                          0.051799
```

3	Population	0.040945
8	Education	0.030836
10	US[Yes]	0.006815
9	Urban[Yes]	0.005195

We see that bagging places the most emphasis on price and good shelf location. These are both logical indicators of sales performances, as the value of a good carseat and its selling position in a marketplace would heavily influence buyer traffic and encourage potential customers to consider and purchase the carseat.

#### 1.2.4 Random Forests

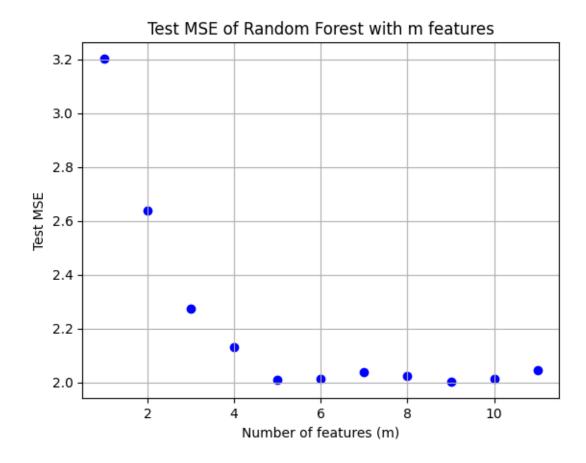
Random forests improve upon bagging by decorrelating trees. At each split, only a random subset of features is considered, which reduces the dominance of strong features and leads to more diverse trees.

We evaluate random forests in two ways:

- 1. Varying m (the number of features considered at each split) and plotting test MSE.
- 2. Using the default recommendation of  $m = \sqrt{p}$  (rounded) and examining feature importance.

Our random forests will use 1,000 trees and vary in number of features considered.

```
[5]: # Set up number of features
     p = len(feature_names)
     # Create lists for MSE values and number of features
     rf_mse_vals = []
     m_vals = np.arange(1, p+1)
     # Fit a random forest for varying number of features
     for i in m_vals:
         RF_carseats = RF(max_features = i, n_estimators = 1000, random_state = 0) #__
      ⇔set random state for reproducibility
         RF_carseats.fit(X_train, y_train)
         rf_preds = RF_carseats.predict(X_test)
         rf_mse_vals.append(np.mean((rf_preds - y_test)**2))
     # Plot MSE vs. m (number of features)
     plt.scatter(m_vals, rf_mse_vals, color = "b")
     plt.title("Test MSE of Random Forest with m features")
     plt.xlabel("Number of features (m)")
     plt.ylabel("Test MSE")
     plt.grid()
```



The test MSE decreases sharply when m increases from very small values, but then stabilizes. This is expected: once the strongest predictors are available to the trees, adding more predictors only increases correlation between trees without reducing bias much further. As a result, the predictive accuracy levels off, with small fluctuations due to randomness.

We now move on to the default procedure of setting  $m = \sqrt{p}$  to see the MSE metric and feature importances.

```
# Predict values of the test dataset
rf_preds_opt = RF_carseats_opt.predict(X_test)
# Compute and print test MSE
rf_opt_mse = np.mean((rf_preds_opt - y_test)**2)
print(f"Test MSE (random forest with sqrt(p) features): {rf_opt_mse}")
# Compute feature importance
importances = RF_carseats_opt.feature_importances_
feature_importance_df = pd.DataFrame({
      'Feature': feature_names,
      'Importance': importances
})
# Sort feature importances in descending order and print
feature_importance_df = feature_importance_df.sort_values(by='Importance',_
  ⇒ascending=False)
print("Feature importance for model with m = sqrt(p) features:")
print(feature_importance_df)
Number of features (p): 11
m = sqrt(p): 3
Test MSE (random forest with sqrt(p) features): 2.2756299329358276
```

```
Feature importance for model with m = sqrt(p) features:
              Feature Importance
4
                Price
                         0.243342
5
      ShelveLoc[Good]
                         0.160471
7
                  Age
                         0.122006
0
            CompPrice
                         0.097027
2
          Advertising
                         0.087855
1
               Income
                         0.085006
           Population
3
                        0.076153
            Education
                         0.050686
8
    ShelveLoc[Medium]
6
                         0.048134
10
              US[Yes]
                         0.016977
9
           Urban[Yes]
                         0.012344
```

The rule-of-thumb  $m = \sqrt{p}$  is a reasonable default, but it does not always minimize test error. In this dataset, the optimal m could be slightly higher or lower depending on which features are most predictive and how correlated they are, reflecting the practical challenges of balancing bias and variance in real-world machine learning.

## 1.2.5 Overall Takeaways

**Decision Trees:** - Easy to interpret and visualize. - Full trees tend to overfit, leading to higher test MSE. - Pruning improves generalization by reducing the number of terminal nodes, balancing bias and variance.

Bagging: - Aggregating multiple trees reduces variance and stabilizes predictions. - Test MSE is

lower than a single decision tree, showing the benefit of ensemble averaging. - Feature importance analysis highlights the predictors most strongly influencing Sales, providing actionable insights.

**Random Forests:** - Further reduces variance by decorrelating trees through random feature selection at splits. - Provides the best predictive performance in this dataset. - The choice of m (number of features per split) affects performance, and the default heuristic  $m = \sqrt{p}$  is reasonable but not guaranteed optimal.

**Practical insights:** - Certain predictors (e.g., Price, ShelveLoc, Age) consistently emerge as important, reflecting key drivers of product sales. - Ensemble methods balance interpretability and accuracy, making them useful for both predictive modeling and business decision-making.

**Overall learning:** - Tree-based methods offer flexible modeling for tabular data. - Combining multiple trees via bagging or random forests improves predictive reliability. - Understanding hyperparameters, like pruning complexity or m in random forests, is critical to achieving strong generalization.