Proof of Correctedness for Special Pythagorean Triplets

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Theorem 0.1. Let a,b,c,S be natural numbers such that $a^2 + b^2 = c^2$ and $\begin{aligned} a+b+c &= S.\\ We\ have\ a,b,c &\leq \tfrac{S}{2}. \end{aligned}$

Proof. Consider a right-angled triangle T with side lengths a,b,c. The perimeter of the triangle T is S. By the triangle inequality, $c \le a+b$, hence $2c \le a+b+c=$ S, so $c \leq \frac{S}{2}$. Since $a, b \leq c$, we get the result.