

# CS 537 – Interactive Computer Graphics

Lecture 7 – Part 1

Mapping Basics

Texture Mapping in OpenGL

# Topics

- Mapping Basics
- Texture Mapping in OpenGL

# Reading

- Angel
  - Chapter 7
- Red Book
  - Chapter 6
  - Chapter 8

# Limitations of Geometric Modeling

- Although graphics cards can render over 10 million polygons per second, that is still insufficient for a lot of things:
  - Clouds
  - Grass
  - Terrain
  - Skin

# Modeling and Orange

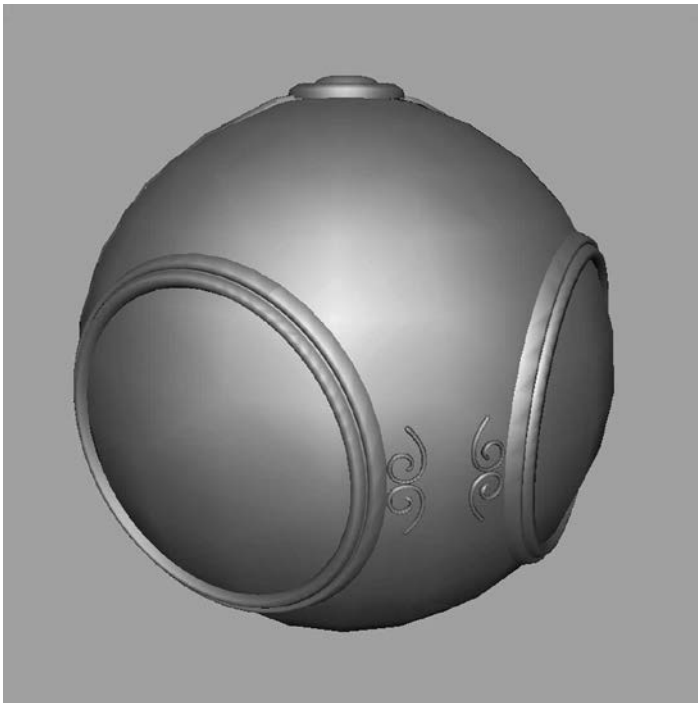
- Considering the problem of modeling an orange (the fruit)
- Start with an orange-colored sphere
  - Too simple
- Replace sphere with a more complex shape
  - Doesn't capture surface characteristics (small dimples)
  - Too many polygons to model all the dimples
- Take a picture of a real orange, scan it, and “paste” onto simple geometric model
  - This is the concept of texture mapping
- May still not be sufficient because the underlying model is smooth
  - Need to change the local shape
  - Bump mapping

# Types of Mapping

- Texture mapping
  - Using images to fill inside of polygons
- Environmental mapping (reflection mapping)
  - Use a picture of the environment for the texture map
- Bump mapping
  - Emulates altering normal vectors during the rendering process to give the illusion of bumps

# Texture Mapping

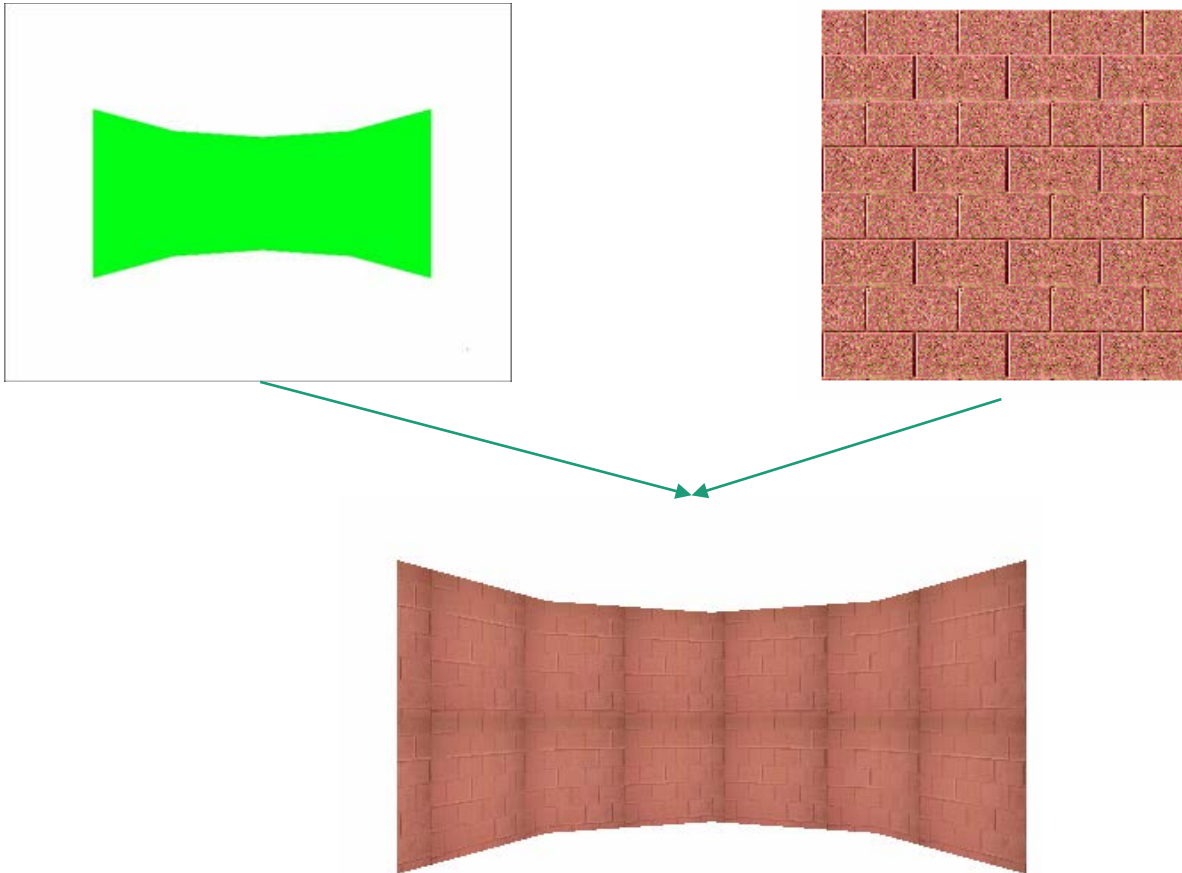
**Geometric Model**



**Texture mapped**

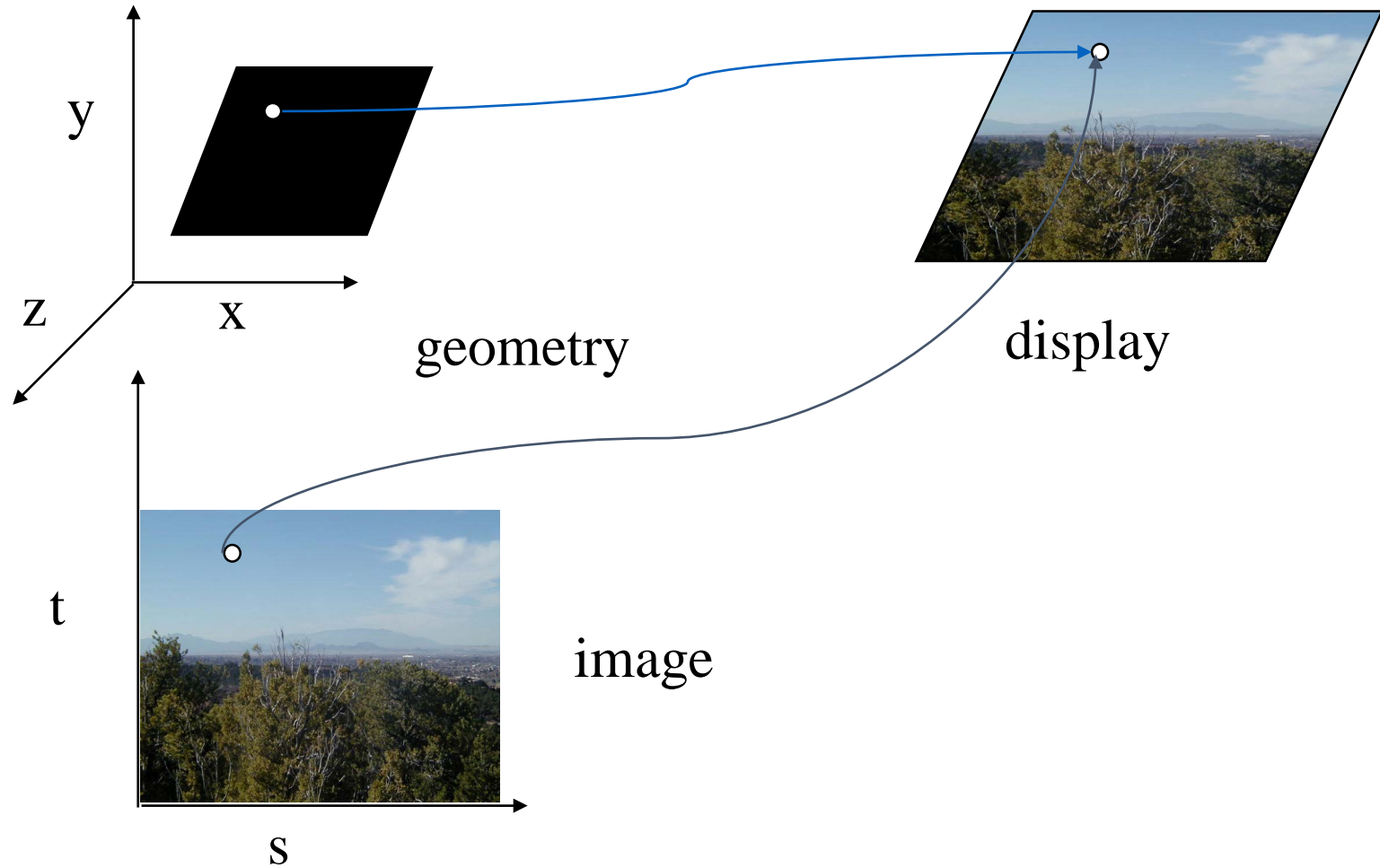


# Texture Mapping





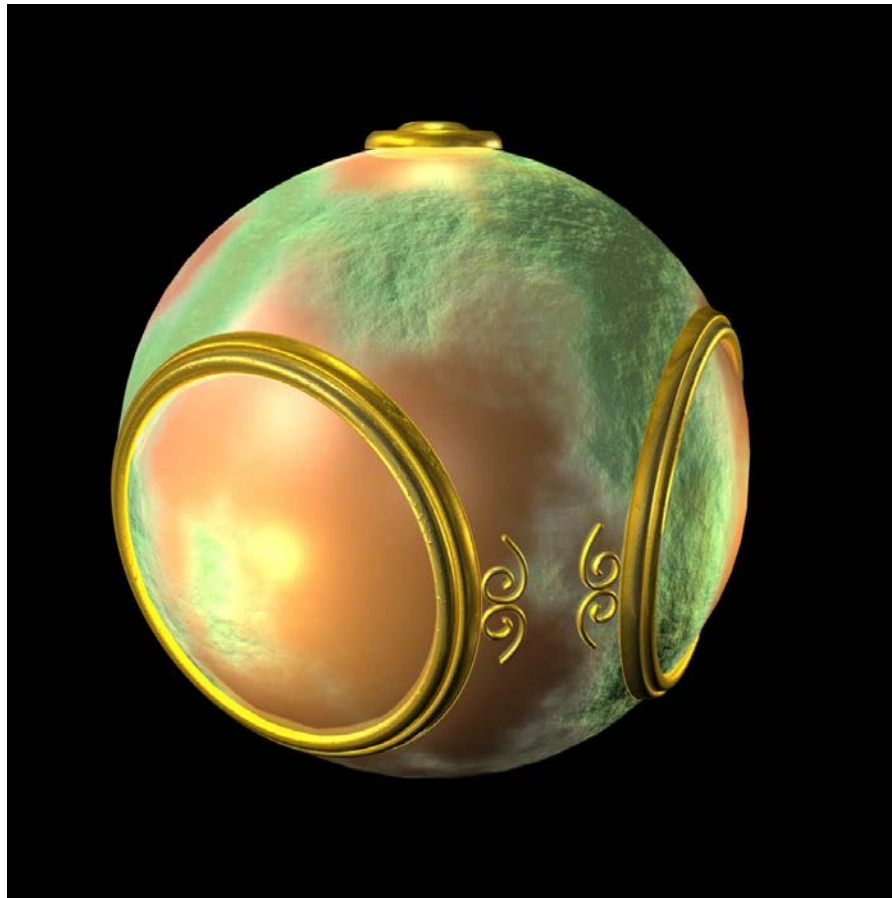
# Texture Mapping



# Environment Mapping

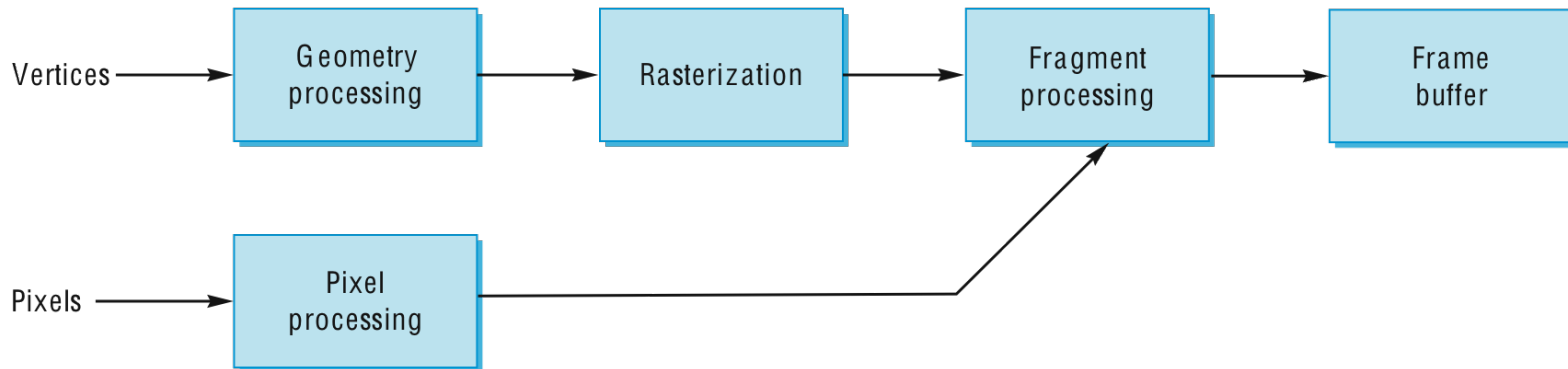


# Bump Mapping



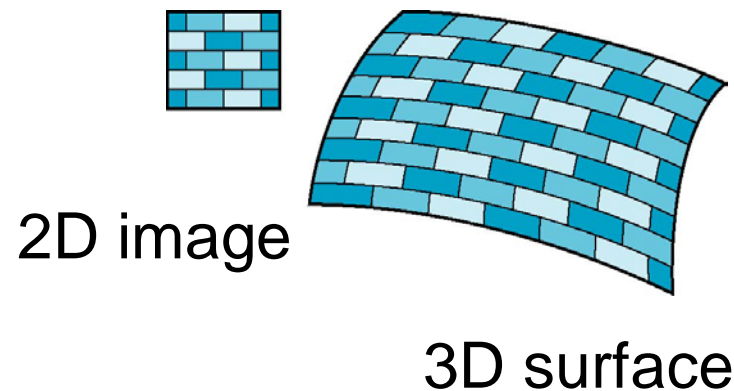
# Where does mapping take place?

- Mapping techniques are implemented at the end of the rendering pipeline
  - Very efficient because few polygons make it past the clipper



# Mapping

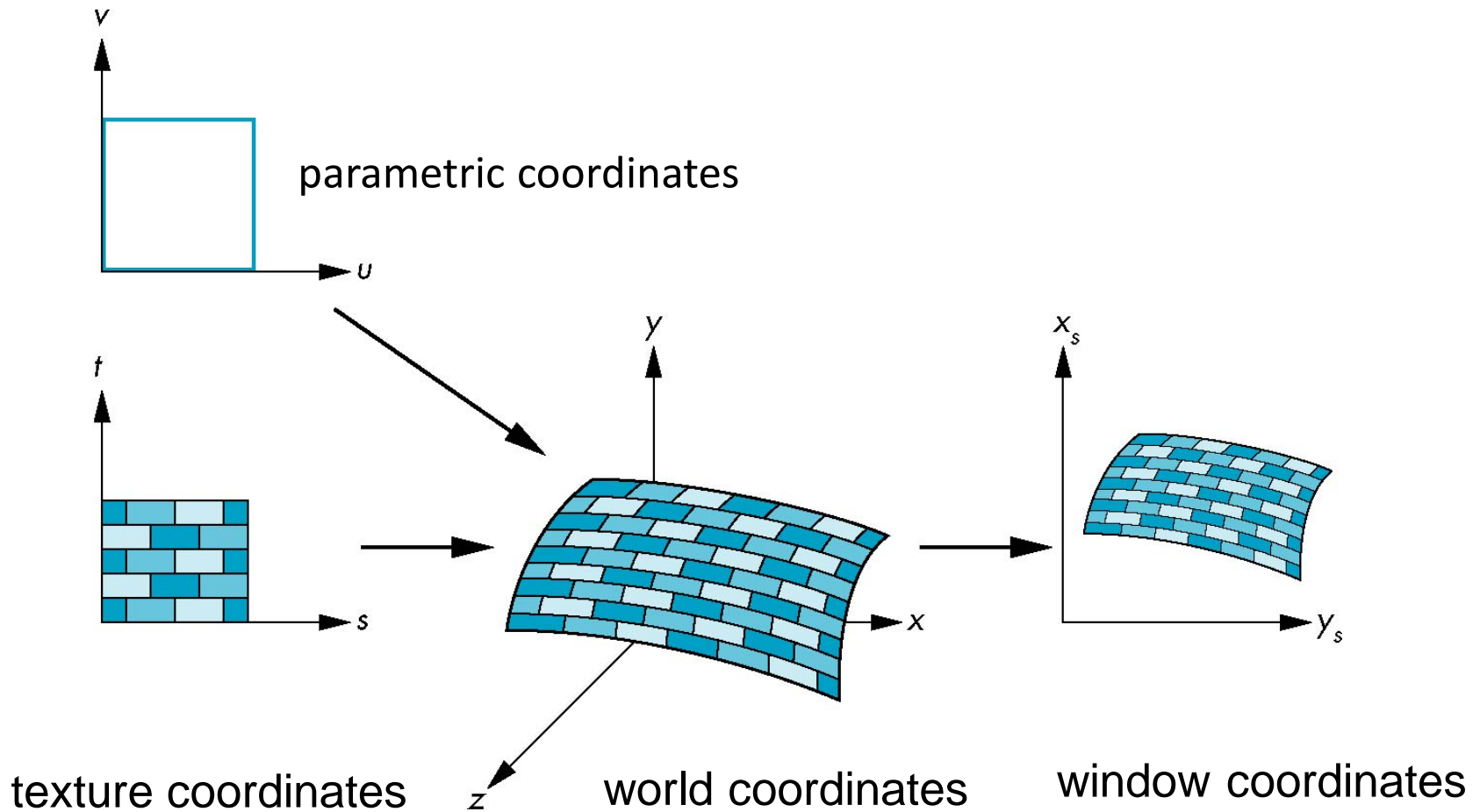
- To do mapping we're essentially assigning locations in one coordinate to another
- In particular, since images are usually 2D we're mapping a 2D surface to a 3D surface
- The whole processes involves quite a few coordinate systems



# Coordinate Systems

- Parametric Coordinates
  - May be used to model curves and surfaces
- Texture coordinates
  - Used to identify points in the image to be mapped
- Object or Model Coordinates
  - This is where the mapping can happen

# Texture Mapping

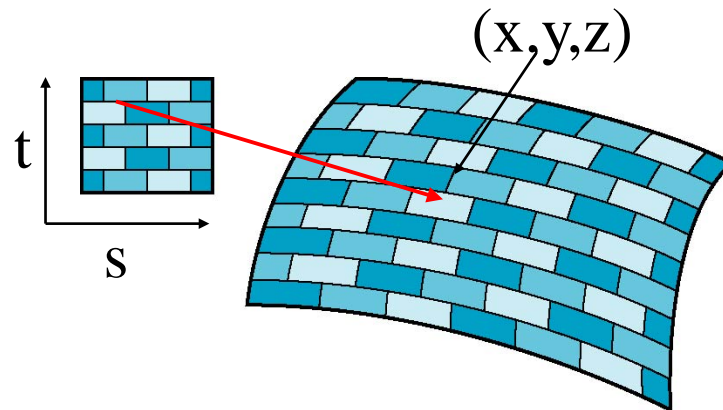


# Mapping Functions

- The most difficult problem is finding the mapping functions from one coordinate system to another
- Consider mapping from texture coordinates to a point on a surface

- We need 3 functions

- $x = f_x(s, t);$
- $y = f_y(s, t)$
- $z = f_z(s, t)$



- Or we can go the other way, from object/model coordinates to texture coordinates



# Backwards Mapping

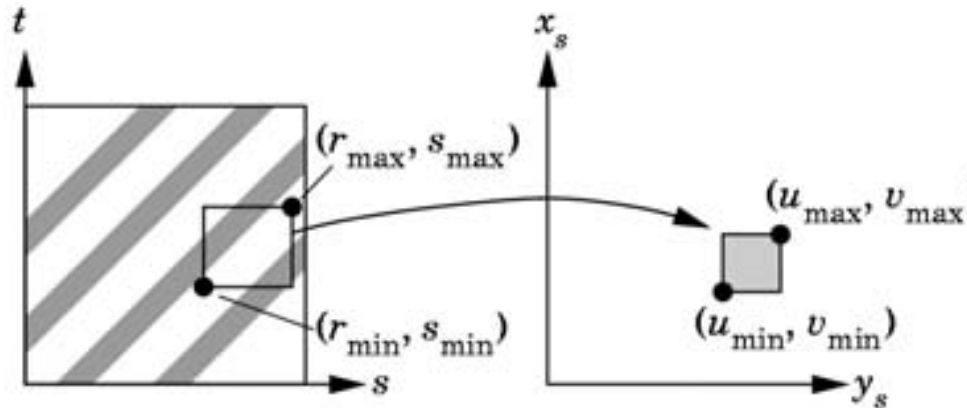
- To map from object/world coordinates back to texel:
  - Given a point on an object, we want to know to which point in the texture it corresponds
- Need mapping of the form
  - $s = f_s(x, y, z)$
  - $t = f_t(x, y, z)$
- But these are generally difficult to come up with ☹️

# Common Mappings

- Most mappings can fit into one of three categories
  1. Map to plane
  2. Map to parametric surface
  3. Map to polyhedron (closed surface)
- Each have their own common approaches

# Mapping a Plane

- For each vertex we just need to specify the location on the texture  $0 \leq (s, t) \leq 1$
- We can also call this “direct mapping”



# Mapping a Parametric Surface

- If we can specify a surface parametrically  $f(u, v)$  then we can find functions that go from
  - Object space  $(x, y, z)$  to
  - Parametric space  $(u, v)$  to
  - Texture space  $(s, t)$  the last of which is a planar/linear mapping

# Cylindrical Mapping

- We can map a rectangle in parametric  $0 \leq u, v \leq 1$  space to cylinder of radius  $r$  and height  $h$  in world coordinates as :
  - $x = r \cos(2\pi u)$
  - $y = r \sin(2\pi u)$
  - $z = v/h$
- So given a point on the cylinder in 3D space  $(x, y, z)$ , the radius  $r$ , and the height  $h$ , we can find its location in parametric space as:
  - $u = \frac{\cos^{-1}\left(\frac{x}{r}\right)}{2\pi}$
  - $v = z * h$
- Then to map from parameter space to texture space we can assign
  - $s = u$
  - $t = v$

# Sphere Map

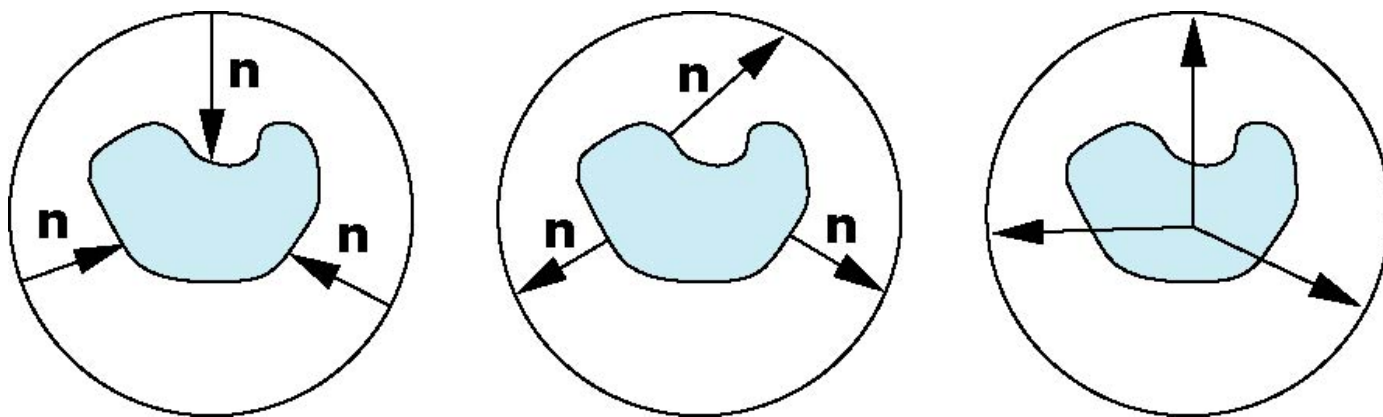
- Recall the parametric form of a sphere
  - $x(\theta, \Phi) = r \cos \theta \sin \Phi$
  - $y(\theta, \Phi) = r \sin \theta \sin \Phi$
  - $z(\theta, \Phi) = r \cos \Phi$
- Using some basic algebra and trig functions:
  - $\frac{y}{x} = \frac{r \sin \theta \sin \phi}{r \cos \theta \sin \phi} = \tan \theta$
- Therefore:
  - $\theta = \tan^{-1} \left( \frac{y}{x} \right)$  //NOTE: Use the  $\tan 2(y, x)$  function to handle cases when  $x = 0$
  - $\phi = \cos^{-1} \left( \frac{z}{r} \right)$
- Since  $\theta$  and  $\Phi$  range from  $-\pi$  to  $\pi$  we must shift them by  $\pi$  and then divide by  $2\pi$  to get our range in  $[0 \ 1]$ 
  - $s = (\theta + \pi)/(2\pi)$
  - $t = (\phi + \pi)/(2\pi)$

# Mapping an Enclosed Polyhedron

- An approach to mapping an enclosed polyhedron is a two-step process
  1. Map the texture to an intermediate surface
    - Commonly a sphere or box
  2. Project points on one surface to the other
    - Generally using the surface normals
    - For the 2<sup>nd</sup> stage, there are a few approaches

# Second Mapping

- Map from intermediate object to actual object
  - Normals from intermediate to actual (find where intersect actual object)
  - Normals from actual to intermediate (find where intersect intermediate object). Probably the best
  - Vectors from center of intermediate (find where intersects both objects)





# Texture Mapping in OpenGL

- Basic Strategy:
  1. Get the texture data
    - Read or generate image
  2. Make a texture active (bind it) and move data to that texture (put on GPU)
  3. Specify texture parameters
    - Wrapping, filtering
  4. Assign texture coordinates to vertices
    - Proper mapping function is left to application
  5. Draw the scene, making texture units active and associating textures with texture units as necessary.

# Design Ideas

- You may want to include with the object (static or not?)
  - Texture coordinates
  - Texture

# Create Texture Object

- Texel values can be up to 4D (RGBA)
- Loading textures is **expensive**
- Faster to bind (`glBindTexture`) then to load (`glTexImage*D`)
  - So load once, and reuse/bin when needed
- Textures are similar to VBOs and VAOs
  - Create texture names:
    - `GLuint texName[4];`  
`glGenTextures(4, texName);`
  - Enable/activate a texture object
    - `glBindTexture(GL_TEXTURE_2D, texName[0]);`

# Multi-Texturing

- We can use *multi-texturing* to allow for several textures per object.
- This is done by assigning textures to *texture units*
- Think of texture locations a matrix:

GL_TEXTURE0	GL_TEXTURE1	...	GL_TEXTUREN
GL_TEXTURE_2D	GL_TEXTURE_2D	...	GL_TEXTURE_2D
GL_TEXTURE_CUBE_MAP	GL_TEXTURE_CUBE_MAP	...	GL_TEXTURE_CUBE_MAP

# Multi-Texturing

- When drawing, we do the following:
  - We must first select/activate a texture unit:
    - `glActiveTexture(GL_TEXTURE0);`
  - Next we must make sure that the texture type we want within that unit is active
    - `glEnable(GL_TEXTURE_2D)`
  - Finally we just associate a texture with the texture type in that texture unit
    - `glBindTexture(GL_TEXTURE_2D, textures[0]);`

# Step 1: Get Texture Data

- We define a texture image from an array of *texels* (texture elements) in CPU memory
  - `GLubyte my_texels[512][512][3]`
- We may populate this texture image by
  - Manually/systematically providing values
  - Loading from image

# Step 1: Create Data

```
GLubyte image[64][64][3];

//Create a 64x64 checkerboard pattern
for(int i=0; i<64; i++){
    for(int j=0; j<64; j++){
        GLubyte c = (((i&(0x8))==0)^(j&0x8)==0))*255;
        image[i][j][0] = c;
        image[i][j][1] = c;
        image[i][j][2] = c;
    }
}
```

# Step 1: Load Data

- For simplicity in this class to load texture from images let's
  1. Convert an image to a portable pix map (PPM) using an online utility:
    - <http://ziin.pl/en/utilities/convert/>
  2. Load the PPM into an unsigned byte array. Code provided for you in the Drawable class in the sample code:

```
static unsigned char* ppmRead(char* filename,  
                               int* width, int* height);
```



# Step 2: Bind Data to Texture Unit

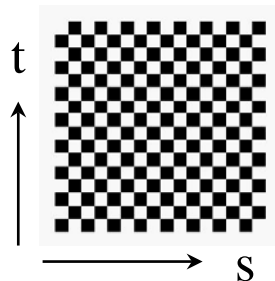
- We must first request from GPU a list of available textures
  - `getGenTextures(3, textures)`
- Then we must make active the texture we want
  - `glBindTexture(GL_TEXTURE_2D, textures[2]);`
- Next we must move the data into the texture
  - `glTexImage2D(target, level, components, w, h, border, format, type, texels)`
    - `target`: Type of texture, e.g. `GL_TEXTURE_2D`
    - `level`: Used for mipmapping (discussed later)
    - `components`: # of elements per texel (RGB, etc..)
    - `w, h`: Width and Height of texture in pixels
    - `border`: Use for smoothing (typically 0 or 1)
    - `format` and `type`: Describe texels
    - `texels`: Pointer to texel array
  - EX:  
`glTexImage2D(GL_TEXTURE_2D, 0, GL_RGB, 512, 512, 0,  
GL_RGB, GL_UNSIGNED_BYTE, my_texels)`

# Step 3: Texture Parameters

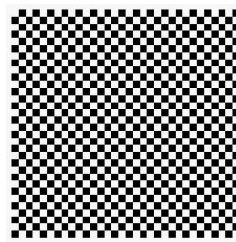
- OpenGL has a variety of parameters that determine how texture is applied
  - Wrapping parameters determine what happens if  $s$  and  $t$  are outside the  $(0,1)$  range
  - Filter mode allows us to use area averaging instead of point samples
  - Mipmapping allows us to use textures at multiple resolutions
  - Environment parameters determine how texture mapping interacts with shading

# Wrapping Mode

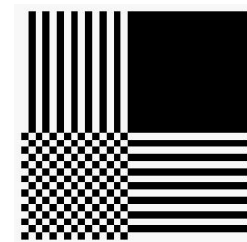
- Clamping: If  $s, t > 1$  use 1, if  $s, t < 0$  use 0
  - `glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_S, GL_CLAMP);`
- Repeating: Use  $s, t \text{ modulo } 1$ 
  - `glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_T, GL_REPEAT);`



texture



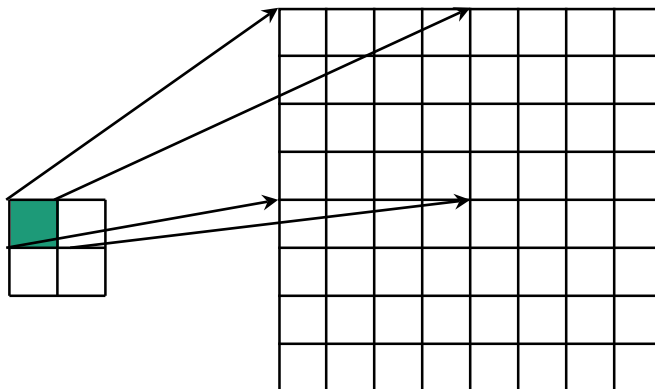
GL\_REPEAT  
wrapping



GL\_CLAMP  
wrapping

# Magnification and Minification

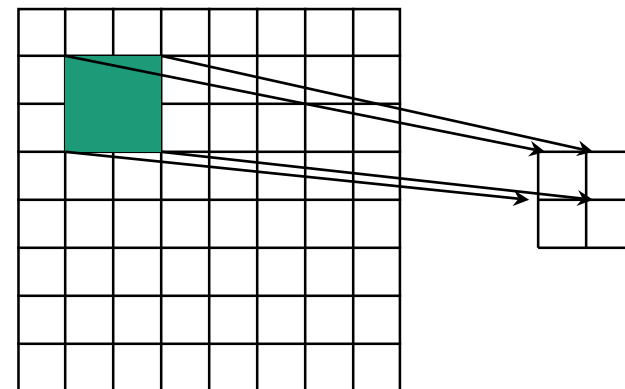
- One texel can cover more than one pixel (magnification) or one pixel can be covered by more than one texel (minification).
- To specify how to deal with this, for each situation (OpenGL detects if either situation occurs) we can specify:
  - Use point sampling (nearest texel)
  - Use linear filtering (2x2 filter) to obtain texture values



Texture

Polygon

Magnification



Texture

Polygon

Minification

# Filter Modes

- Modes determined by
  - `glTexParameteri(target, type, mode)`
- Examples:
  - `glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, GL_NEAREST);`
  - `glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, GL_LINEAR);`
- Note: Linear filtering requires a border of an extra texel for filtering at edges (`border = 1`)

# Mipmapped Textures

- Mipmapping allows for prefiltered texture maps of decreasing resolutions
- Lessens interpolation errors for smaller textured objects
  - Probably want higher resolution images for closer objects, lower resolution for further objects
- Declare mipmap level during texture definition
  - `glTexImage2D(GL_TEXTURE_2D, level, ...)`
- Alternatively allow OpenGL to make the mipmaps
  - `glGenerateMipmaps(GL_TEXTURE_2D);`
  - `glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, GL_NEAREST_MIPMAP_NEAREST);`

# Step 4: Assign Texture Coordinates

- We talked about different ways in Part 1
- Let's look at the simple plane->plane mapping:

```
void Cube::quad2Triangles(vec4 v1, vec4 v2, vec4 v3, vec4 v4){  
    //triangle 1  
    vec3 N = normalize(cross(v2-v1,v3-v1));  
    vertices[index]=v1;  normals[index] = N;    textures[index] = vec2(0.0,0.0);    index++;  
    vertices[index]=v2;  normals[index] = N;    textures[index] = vec2(1.0,0.0);    index++;  
    vertices[index]=v3;  normals[index] = N;    textures[index] = vec2(1.0,1.0);    index++;  
  
    N = normalize(cross(v3-v1,v4-v1));  
    vertices[index]=v1;  normals[index] = N;    textures[index] = vec2(0.0,0.0);    index++;  
    vertices[index]=v3;  normals[index] = N;    textures[index] = vec2(1.0,1.0);    index++;  
    vertices[index]=v4;  normals[index] = N;    textures[index] = vec2(0.0,1.0);    index++;  
}
```

# Step 5: Rendering with Textures

- Just need to
  - Make sure texture location attributes are linked and enabled
    - `vTexture = glGetAttribLocation(program, "vTexCoord");`
    - `glEnableVertexAttribArray(vTexture);`
    - `glVertexAttribPointer(vTexture, 2, GL_FLOAT, GL_FALSE, 0, BUFFER_OFFSET(sizeof(vertices) + sizeof(normals)));`
  - Make sure desired texture unit is active (for drawing)
    - `glActiveTexture(GL_TEXTURE0);`
    - `glEnable(GL_TEXTURE_2D)`
    - `glBindTexture(GL_TEXTURE_2D, texture);`
    - `glUniform1i(glGetUniformLocation(program, "texture"), 0);`



# Shaders

- Vertex Shader
  - Often just pass the texture attribute through to fragment shader
- Fragment Shader
  - Use a texture “sampler” to get the color from the current texture at the specified texture location

# Vertex Shader

```
in vec4 vPosition; //vertex position in object cords
in vec4 vColor; //vertex color from application
in vec2 vTexCoord; //texture coord from app

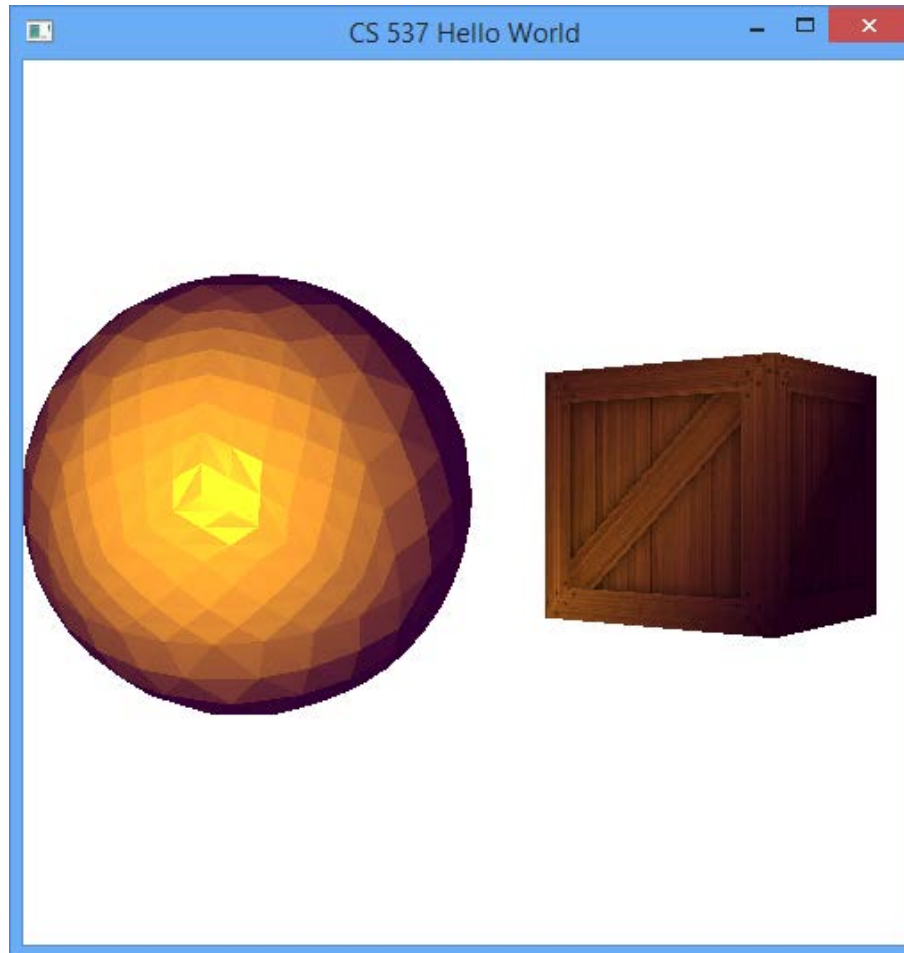
out vec4 color; //output color to be interpolated
out vec2 texCoord; //output tex coordinate to be interpolated
```

# Fragment Shader

```
in vec4 color; //color from rasterizer
in vec2 texCoord; //texture coordinate from rasterizer
uniform sampler2D textureID; //texture object from application;
out vec4 fColor;

void main(){
    fColor = color*texture(textureID,texCoord);
}
```

# Example: $\text{Crate} = \text{Lights} + \text{Texture}$



# Crate Example: Building Object

```
CubeTextured::CubeTextured() {
    glGenBuffers(1, &VBO);
    glGenVertexArrays(1, &VAO);
    program = InitShader("../vshader09_texture_v150.glsl", "../fshader09_texture_v150.glsl");

    index = 0;
    TextureSize = 512;

    build();

    glBindVertexArray(VAO);
    glBindBuffer(GL_ARRAY_BUFFER, VBO);
    glBufferData(GL_ARRAY_BUFFER, sizeof(vertexLocations) + sizeof(vertexNormals) + sizeof(vertexTextureCoords),
        NULL, GL_STATIC_DRAW);
    glBufferSubData(GL_ARRAY_BUFFER, 0, sizeof(vertexLocations), vertexLocations);
    glBufferSubData(GL_ARRAY_BUFFER, sizeof(vertexLocations), sizeof(vertexNormals), vertexNormals);
    glBufferSubData(GL_ARRAY_BUFFER, sizeof(vertexLocations) + sizeof(vertexNormals), sizeof(vertexTextureCoords),
        vertexTextureCoords);

    GLuint vPosition = glGetAttribLocation(program, "vPosition");
    glEnableVertexAttribArray(vPosition);
    glVertexAttribPointer(vPosition, 4, GL_FLOAT, GL_FALSE, 0, BUFFER_OFFSET(0));

    GLuint vNormal = glGetAttribLocation(program, "vNormal");
    glEnableVertexAttribArray(vNormal);
    glVertexAttribPointer(vNormal, 3, GL_FLOAT, GL_FALSE, 0, BUFFER_OFFSET(sizeof(vertexLocations)));

    GLuint vTex = glGetAttribLocation(program, "vTexCoord");
    glEnableVertexAttribArray(vTex);
    glVertexAttribPointer(vTex, 2, GL_FLOAT, GL_FALSE, 0, BUFFER_OFFSET(sizeof(vertexLocations) + sizeof(vertexNormals)));
}
```

# Crate Example : Building (cont)

- Continued...

```
glGenTextures(1, &texture);
GLubyte *image0 = ppmRead("../crate_texture.ppm", &TextureSize, &TextureSize);
glBindTexture(GL_TEXTURE_2D, texture);
glTexImage2D(GL_TEXTURE_2D, 0, GL_RGB, TextureSize, TextureSize, 0, GL_RGB, GL_UNSIGNED_BYTE, image0);
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, GL_NEAREST);
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, GL_NEAREST);
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_S, GL_REPEAT);
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_T, GL_REPEAT);
}
```

# Crate Example: Coords

```
void CubeTextured::build(){
    makeQuad(1,0,3,2); //front
    makeQuad(2,3,7,6); //right
    makeQuad(3,0,4,7); //bottom
    makeQuad(6,5,1,2); //top
    makeQuad(4,5,6,7); //back
    makeQuad(5,4,0,1); //left
}
```

```
void CubeTextured::makeQuad(GLuint ind1, GLuint ind2, GLuint ind3, GLuint ind4){ //assume vertices in counter-clockwise order from top-left
    vec4 data[] = {vec4(-0.5,-0.5,0.5,1.0),vec4(-0.5,0.5,0.5,1.0),vec4(0.5,0.5,0.5,1.0),vec4(0.5,-0.5,0.5,1.0),
        vec4(-0.5,-0.5,-0.5,1.0),vec4(-0.5,0.5,-0.5,1.0),vec4(0.5,0.5,-0.5,1.0),vec4(0.5,-0.5,-0.5,1.0)};

    //first triangle
    vec3 N = normalize(cross(data[ind2]-data[ind1],data[ind3]-data[ind1]));
    vertexLocations[index] = data[ind1]; vertexNormals[index] = N; vertexTextureCoords[index] = vec2(0,0); index++;
    vertexLocations[index] = data[ind2]; vertexNormals[index] = N; vertexTextureCoords[index] = vec2(1,0); index++;
    vertexLocations[index] = data[ind3]; vertexNormals[index] = N; vertexTextureCoords[index] = vec2(1,1); index++;

    //second triangle
    N = normalize(cross(data[ind3] - data[ind1],data[ind4]-data[ind1]));
    vertexLocations[index] = data[ind3]; vertexNormals[index] = N; vertexTextureCoords[index] = vec2(0,0); index++;
    vertexLocations[index] = data[ind4]; vertexNormals[index] = N; vertexTextureCoords[index] = vec2(1,1); index++;
    vertexLocations[index] = data[ind1]; vertexNormals[index] = N; vertexTextureCoords[index] = vec2(0,1); index++;
}
```

# Crate Example: Draw Cube

```
void CubeTextured::draw(Camera cam, vector<Light> lights){
    glBindVertexArray(VAO);
    glUseProgram(program);

    GLuint light_loc = glGetUniformLocation(program, "lightPos");
    glUniform4fv(light_loc, 1, cam.getEye());

    GLuint diffuse_loc = glGetUniformLocation(program, "diffuseProduct");
    glUniform4fv(diffuse_loc, 1, diffuse*lights[0].getDiffuse());

    GLuint spec_loc = glGetUniformLocation(program, "specularProduct");
    glUniform4fv(spec_loc, 1, specular*lights[0].getSpecular());

    GLuint ambient_loc = glGetUniformLocation(program, "ambientProduct");
    glUniform4fv(ambient_loc, 1, ambient*lights[0].getAmbient());

    GLuint alpha_loc = glGetUniformLocation(program, "alpha");
    glUniform1f(alpha_loc, shininess);

    GLuint model_loc = glGetUniformLocation(program, "model_matrix");
    glUniformMatrix4fv(model_loc, 1, GL_TRUE, modelmatrix);

    GLuint view_loc = glGetUniformLocation(program, "camera_matrix");
    glUniformMatrix4fv(view_loc, 1, GL_TRUE, cam.getViewMatrix());

    GLuint proj_loc = glGetUniformLocation(program, "proj_matrix");
    glUniformMatrix4fv(proj_loc, 1, GL_TRUE, cam.getProjectionMatrix());

    glEnable(GL_TEXTURE_2D);
    glActiveTexture(GL_TEXTURE0);
    glBindTexture(GL_TEXTURE_2D, texture);
    glUniform1i(glGetUniformLocation(program, "textureID"), 0);

    glDrawArrays(GL_TRIANGLES, 0, numVertices);
}
```



# Crate Example: Shaders

```
#version 150

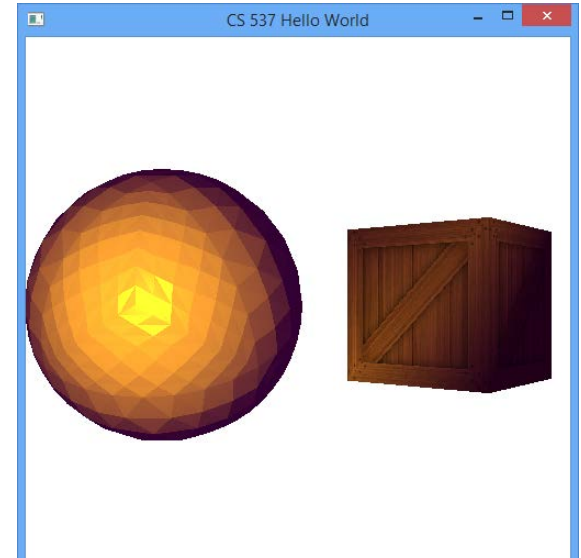
in vec4 vPosition;
in vec3 vNormal;
in vec2 vTexCoord;

out vec4 color;
out vec2 texCoord;

uniform mat4 model_matrix;
uniform mat4 camera_matrix;
uniform mat4 proj_matrix;

uniform vec4 lightPos;
uniform vec4 ambientProduct,
           diffuseProduct, specularProduct;
uniform float alpha;

void main()
{
    texCoord = vTexCoord;
    //Then all the lighting effects
    // to compute output color....
    //...
}
```



```
#version 150

in vec4 color;
in vec2 texCoord;

uniform sampler2D textureID;

out vec4 fColor;

void main()
{
    fColor = texture(textureID, texCoord) * color;
}
```