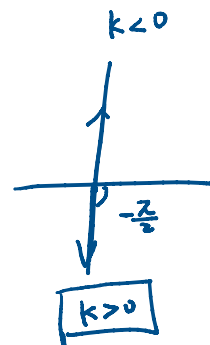


1. $a_0 = 0.5$ $a_k = \frac{1}{jk\omega} = \frac{-j}{k\omega}$

$|a_k| = \sqrt{\left(\frac{1}{k\omega}\right)^2} = \frac{1}{k\omega}$

$\angle a_k = \tan^{-1}\left(\frac{-\frac{1}{k\omega}}{0}\right)$
 $= -\frac{\pi}{2}$



$x(t) = 0.5 + \sum_{k=1}^{\infty} \frac{2}{k\omega} \cos\left(k\frac{2\pi}{0.005}t - \frac{\pi}{2}\right)$

2. length T $0 \sim N$, f_0 F_s

$\frac{T}{F_s}$

\downarrow
 $2\pi f_0 = \omega_0$

$\text{np.angle}()$
 $\text{np.abs}()$

```
def x(Fourier_Coef, f, T, Fs):
    t = np.arange(0, T, 1/Fs)
    xt = ones(len(t)) * Fourier_Coef[0]
    w = 2*np.pi*f
    N = len(Fourier_Coef)

    for k in range(1, N):
        xt = xt + 2*np.abs(Fourier_Coef[k]) * np.cos(k*w*t + np.angle(Fourier_Coef[k]))

    return xt
```

3. $F_s = 11025 \text{ Hz}$ $T_s = \frac{1}{11025}$

$200 \text{ ms} \rightarrow 0.25$

$\frac{0.2}{T_s} = 0.2 \times 11025 = 2205 \text{ (index)}$

4

$0.1 \times 11025 = 1102.5$ $2^n = 1102.5$

$n \ln 2 = \ln 1102.5$

$n \approx 10$

Freq resolution = $\frac{f_s}{N} = \frac{11025}{10} = 1102.5$

$$\text{Freq resolution} = \frac{f_s}{N} = \frac{11025}{10} = 1102.5$$