

Problem 1.

$$1 \times 10^9 \times 15 = 1.5 \times 10^{10} \text{ cycles}$$

$$1.5 \times 10^{10} \times 1.2 = 1.8 \times 10^{10} \text{ cycles}$$

$$\frac{1.8 \times 10^{10}}{10^9} = 1.8 \times 10^9 = 1.8 \text{ GHz}$$

Problem 2. CPI

of instruction on one processor

a

Arithmetic : 1

$$3 \times 10^9$$

Load/Store : 10

$$2 \times 10^9$$

Branch : 5

$$2.56 \times 10^8$$

1 processor

$$\text{clock cycle} = 3 \times 10^9 + 2 \times 10^9 + 1.28 \times 10^9 = 2.428 \times 10^{10} \text{ cycles}$$

$$\text{Execution time for 1 processor} \quad t = \frac{2.428 \times 10^{10}}{2 \times 10^9} = 12.14 \text{ s}$$

2 processors

$$\text{clock cycle} = \frac{3 \times 10^9 + 2 \times 10^9}{0.8 \times 2} + 1.28 \times 10^9 = 1.5655 \times 10^{10} \text{ cycles}$$

$$t = \frac{1.5655 \times 10^{10}}{2 \times 10^9} = 7.8275 \text{ s}$$

$$\text{speedup} = \frac{12.14}{7.8275} = 1.55$$

4 processors

$$\text{clock cycle} = \frac{3 \times 10^9 + 2 \times 10^9}{0.8 \times 4} + 1.28 \times 10^9 = 8.47 \times 10^9$$

$$t = \frac{8.47 \times 10^9}{2 \times 10^9} = 4.235 \text{ s}$$

$$\text{speed up} = \frac{12.14}{4.235} = 2.87$$

8 processors

$$\text{clock cycle} = \frac{3 \times 10^9 + 2 \times 10^9}{0.8 \times 8} + 1.28 \times 10^9 = 4.87 \times 10^9$$

$$t = \frac{4.87 \times 10^9}{2 \times 10^9} = 2.435$$

$$\text{speedup} = 4.99$$

b. if CPI of arithmetic instruction was doubled

1 processor

$$\text{clock cycle} : 2 \times 3 \times 10^9 + 2 \times 10^{10} + 1.28 \times 10^9 = 2.728 \times 10^{10} \text{ cycles}$$

$$t = \frac{2.728 \times 10^{10}}{2 \times 10^9} = 13.64 \text{ s}$$

2 processors

$$t = \frac{\frac{6 \times 10^9 + 2 \times 10^{10}}{0.8 \times 2} + 1.28 \times 10^9}{2 \times 10^9} = 8.765 \text{ s}$$

4 processors

$$t = \frac{\frac{6 \times 10^9 + 2 \times 10^{10}}{0.8 \times 4} + 1.28 \times 10^9}{2 \times 10^9} = 4.7025 \text{ s}$$

8 processors

$$t = \frac{\frac{6 \times 10^9 + 2 \times 10^{10}}{0.8 \times 8} + 1.28 \times 10^9}{2 \times 10^9} = 2.67 \text{ s}$$

1.5 s, 0.94 s, 0.46 s, 0.235 s increase in execution time

$$C. \quad 3 \times 10^9 + 0.2 \times 10^{10} + \cancel{1.28 \times 10^9} = \frac{3 \times 10^9 + 2 \times 10^{10} + \cancel{1.28 \times 10^9}}{0.8 \times 4}$$

$a = 0.21$ reduced to 21%.

3 a. $P_1 : t = \frac{0.9 \times 5 \times 10^9}{4 \times 10^9} = 1.125 \text{ s}$

$$P_2: t = \frac{0.75 \times 1 \times 10^9}{3 \times 10^9} = 0.25s$$

not true

$$b. \frac{1 \times 10^9 \times 0.9}{4 \times 10^9} = \frac{0.225}{1}$$

$$a = 9 \times 10^8$$

C. $P_1: \frac{4 \times 10^9}{0.9} = 4.44 \times 10^9$ Instructions

$P_2: \frac{3 \times 10^9}{0.75} = 4 \times 10^9$ Instruction

but p_2 has better performance so not true

$$d. P_1 \text{ MFLOPS} = \frac{0.4 \times 5 \times 10^9}{1.125 \times 10^6} = 1.78 \times 10^3$$

$$P_2 \text{ MFLOPS} = \frac{0.4 \times 10^9}{0.25 \times 10^6} = 1.6 \times 10^3$$

4. $||00101000 \ 0010| \ 000000 \ 0100 \ 0000|$

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$|0\rangle|0\rangle|00\rangle \quad ||||| \quad |||||/0\rangle \quad |00\rangle$

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5. B.LT 4

ADDI X2, X2, #1

B 0

ADDI X31, X31, 0

CBZ X0, 5