

## Problem 1.

$A \oplus B$

A	B	C
0	0	0
0	1	0
1	0	1
1	1	0

$$C = A\bar{B}$$

$A \oplus B$

A	B	C
0	0	1
0	1	1
1	0	0
1	1	1

$$C = \bar{A} + B$$

$A \oplus B$

A	B	C
0	0	1
0	1	0
1	0	0
1	1	1

$$C = AB + \bar{A}\bar{B}$$

$A \oplus B$

A	B	C
0	0	0
0	1	1
1	0	1
1	1	0

$$C = A\bar{B} + \bar{A}B$$

$A \oplus B$

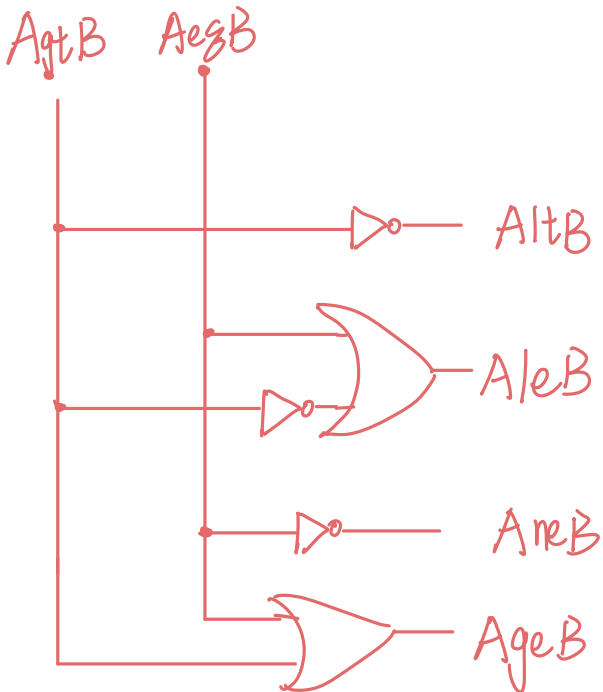
A	B	C
0	0	0
0	1	0
1	0	0
1	1	0

$$C = \bar{A}B$$

$A \oplus B$

A	B	C
0	0	1
0	1	0
1	0	1
1	1	1

$$C = A + \bar{B}$$



## Problem 2

MOV  $X_{15}, \#1$

MOV  $X_1, X_0$

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LDR X2 [X1]
ADD X1, X1, #4
LDR X3 [X1]
ADD X1, X1, #4
LDR X4 [X1]
CMP X2, X3
BLE L1
MOV X15, #0
B L2

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L1:

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CMP X3, X4
BLE L2
MOV X15, #0

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L2:

Problem 3 =

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LSR X1, X0, #2
ADD X1, X1, X0

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Problem 4

$$\begin{aligned}
 \text{a) CPU Time}_A &= \frac{1}{3.5 \text{ GHz}} \cdot 1.5 = 4.29 \times 10^{-10} \text{ s} & \text{IPS} &= 2.3 \times 10^9 \\
 \text{CPU Time}_B &= \frac{1}{2.8 \text{ GHz}} = 3.57 \times 10^{-10} \text{ s} & \text{IPS} &= 2.8 \times 10^9
 \end{aligned}$$

$$\text{CPU Time}_c = \frac{1}{4 \text{ GHz}} \cdot 2.2 = 5.5 \times 10^{-10} \text{ s} \quad \text{IPS} = 1.82 \times 10^9$$

$P_2$  has highest performance

b)

$P_1: 7 \times 10^{10}$ cycles	$4.7 \times 10^{10}$ instructions
$P_2: 5.6 \times 10^{10}$ cycles	$5.6 \times 10^{10}$ instructions
$P_3: 8 \times 10^{10}$ cycles	$3.64 \times 10^{10}$ instructions

c)

$$t = \text{CPI} \cdot \frac{1}{\text{CR}}$$

$$0.7 = 1.15 \text{ CPI} \cdot \frac{1}{x \cdot \text{CR}}$$

$$0.7 = \frac{1.15 \text{ CPI}}{x \cdot \text{CR}} \cdot \frac{\text{CR}}{\text{CPI}}$$

$$x = 1.64$$

New clock rate:

$$P_1 = 5.7 \text{ GHz}$$

$$P_2 = 4.6 \text{ GHz}$$

$$P_3 = 6.6 \text{ GHz}$$

Problem 5:

a. Class A:  $1 \times 10^5$  instructions

B:  $2 \times 10^5$  instructions

C:  $4 \times 10^5$  instructions

D:  $3 \times 10^5$  instructions

$$P_1: T = \frac{1 \times 10^5 + 4 \times 10^5 + 12 \times 10^5 + 12 \times 10^5}{2.8 \times 10^9} = 1.04 \times 10^{-3} \text{ s}$$

$$P_2: T = \frac{2 \times 10^5 + 6 \times 10^5 + 8 \times 10^5 + 9 \times 10^5}{3.5 \times 10^9} = 7.14 \times 10^{-4} \text{ s}$$

second implementation is faster.

b.

$$P_1: 1.04 \times 10^{-3} \cdot 2.8 \times 10^9 = 2.9 \times 10^6 \text{ cycles}$$

$$P_2: 7.14 \times 10^{-4} \cdot 3.5 \times 10^9 = 2.5 \times 10^6 \text{ cycles}$$

Global CPI for  $P_1$ : 2.9

$$P_2 = 2.5$$

c) Clock cycles:  $P_1 = 2.9 \times 10^6$   
 $P_2 = 2.5 \times 10^6$

Problem 6:

a)  $CPI_A = \frac{1.15}{1 \times 10^9 \text{ ns} \cdot 1 \times 10^9} = 1.1$

$$CPI_B = \frac{1.4}{1 \times 10^9 - 1.3 \times 10^9} = 1.08$$

b)  $CR = \frac{\text{Instruction count} \cdot CPI}{\text{execution time}}$

$$\frac{CRA}{CRB} = \frac{10^9 \cdot 1.1}{t} \cdot \frac{t}{1.3 \times 10^9 \cdot 1.08} = 0.78$$

CR of processor running A is 22% slower than the processor running B

c) A:  $\frac{1 \times 10^9 \times 1.1}{6 \times 10^8 \times 1.1} = 1.67$

B:  $\frac{1.3 \times 10^9 \times 1.08}{6 \times 10^8 \times 1.1} = 1.96$