Table 1
 Microeconomic Model Calibration

Calibrated Parameters				
Description	Parameter	Value	Source	
Permanent Income Growth Factor	Γ	1.03	PSID: Carroll (1992)	
Interest Factor	R	1.04	Conventional	
Time Preference Factor	β	0.96	Conventional	
Coefficient of Relative Risk Aversion	$\rho$	2	Conventional	
Probability of Zero Income	$\wp$	0.005	PSID: Carroll (1992)	
Std Dev of Log Permanent Shock	$\sigma_{\psi}$	0.1	PSID: Carroll (1992)	
Std Dev of Log Transitory Shock	$\sigma_{ heta}$	0.1	PSID: Carroll (1992)	

 Table 2
 Model Characteristics Calculated from Parameters

				Approximate
				Calculated
Description	Syr	nbol	and Formula	Value
Finite Human Wealth Factor	$\mathcal{R}^{-1}$	=	$\Gamma/R$	0.990
PF Finite Value of Autarky Factor	⊐	$\equiv$	$eta\Gamma^{1- ho}$	0.932
Growth Compensated Permanent Shock	$\underline{\psi}$	$\equiv$	$(\mathbb{E}[\psi^{-1}])^{-1}$	0.990
Uncertainty-Adjusted Growth	$\Gamma$	=	$\Gamma \underline{\psi}$	1.020
Utility Compensated Permanent Shock	$\underline{\underline{\psi}}$	≡	$(\mathbb{E}[\psi^{1-\rho}])^{1/(1-\rho)}$	0.990
Utility Compensated Growth	$\overline{\underline{\Gamma}}$	=	$\Gamma \underline{\psi}$	1.020
Absolute Patience Factor	Þ	$\equiv$	$(R\beta)^{1/ ho}$	0.999
Return Patience Factor	$\mathbf{p}_{R}$	$\equiv$	$\mathbf{P}/R$	0.961
Growth Patience Factor	$\mathbf{b}_{\Gamma}$	$\equiv$	$\mathbf{p}/\Gamma$	0.970
Normalized Growth Patience Factor	$\mathbf{b}_{\underline{\Gamma}}$	$\equiv$	$\mathbf{P}/\underline{\Gamma}$	0.980
Finite Value of Autarky Factor	I⊒	$\equiv$	$\beta\Gamma^{1-\rho}\underline{\psi}^{1-\rho}$	0.941
Weak Impatience Factor	$\wp^{1/ ho}\mathbf{p}$	=	$(\wp \beta R)^{\overline{1/\rho}}$	0.071

 ${\bf Table~3}~~{\bf Definitions~and~Comparisons~of~Conditions}$ 

Perfect Foresight Versions	Uncertainty Versions			
<u> </u>	v			
Finite Human Wealth Condition (FHWC) $\Gamma/R < 1 \qquad \qquad \Gamma/R < 1$				
The growth factor for permanent income $\Gamma$ must be smaller than the discounting factor R for human wealth to be finite.	The model's risks are mean-preserving spreads, so the PDV of future income is unchanged by their introduction.			
Absolute Impatien	ce Condition (AIC)			
<b>Þ</b> < 1	<b>p</b> < 1			
The unconstrained consumer is sufficiently impatient that the level of consumption will be declining over time: $\mathbf{c}_{t+1} < \mathbf{c}_t$	If wealth is large enough, the expectation of consumption next period will be smaller than this period's consumption: $\lim_{m_t \to \infty} \mathbb{E}_t[\mathbf{c}_{t+1}] < \mathbf{c}_t$			
D -4 I 1:				
Return Impatience Condition (RIC)	ence Conditions Weak RIC (WRIC)			
$\mathbf{p}/R < 1$	$\wp^{1/\rho}\mathbf{p}/R<1$			
,	,			
The growth factor for consumption <b>P</b> must be smaller than the discounting factor R, so that the PDV of current and future consumption will be finite:	If the probability of the zero-income event is $\wp = 1$ then income is always zero and the condition becomes identical to the RIC. Otherwise, weaker.			
$c'(m) = 1 - \mathbf{P}/R < 1$	$c'(m) < 1 - \wp^{1/\rho} \mathbf{P}/R < 1$			
Growth Impati	ence Conditions			
GIC	GIC-Nrm			
$\mathbf{p}/\Gamma < 1$	$\mathbf{p}\mathbb{E}[\psi^{-1}]/\Gamma<1$			
For an unconstrained PF consumer, the ratio of $\mathbf{c}$ to $\mathbf{p}$ will fall over time. For constrained, guarantees the constraint eventually binds. Guarantees $\lim_{m_t \uparrow \infty} \mathbb{E}_t[\psi_{t+1} m_{t+1}/m_t] = \mathbf{p}_{\Gamma}$	By Jensen's inequality stronger than GIC. Ensures consumers will not expect to accumulate $m$ unboundedly. $\lim_{m_t \to \infty} \mathbb{E}_t[m_{t+1}/m_t] = \mathbf{p}_{\underline{\Gamma}}$			
Finite Value of A	Finite Value of Autarky Conditions			
PF-FVAC	FVAC			
$eta \Gamma^{1- ho} < 1$ equivalently $\mathbf{P} < R^{1/ ho} \Gamma^{1-1/ ho}$	$\beta \Gamma^{1-\rho}  \mathbb{E}[\psi^{1-\rho}] < 1$			
The discounted utility of constrained consumers who spend their permanent income each period should be finite.	By Jensen's inequality, stronger than the PF-FVAC because for $\rho > 1$ and nondegenerate $\psi$ , $\mathbb{E}[\psi^{1-\rho}] > 1$ .			

 Table 4 Conditions for Nondegenerate<sup>‡</sup> Solution

Consumption Model(s)	Conditions	Comments
$\bar{\mathbf{c}}(m)$ : PF Unconstrained	RIC, FHWC°	$RIC \Rightarrow  v(m)  < \infty; FHWC \Rightarrow 0 <  v(m) $
$\underline{c}(m) = \underline{\kappa}m$		PF model with no human wealth $(h = 0)$
Section 2.5.3:		RICprevents $\bar{\mathbf{c}}(m) = \underline{\mathbf{c}}(m) = 0$
Section 2.5.3:		FHWCprevents $\bar{\mathbf{c}}(m) = \infty$
Eq $(26)$ :		$PF-FVAC+FHWC \Rightarrow RIC$
Eq (27):		$GIC+FHWC \Rightarrow PF-FVAC$
$\grave{\mathrm{c}}(m)$ : PF Constrained	GIC, RIC	FHWC holds $(\Gamma < \mathbf{b} < R \Rightarrow \Gamma < R)$
Section 2.5.6:		$ \dot{c}(m) = \bar{c}(m) \text{ for } m > m_{\#} < 1 $
		(RHC would yield $m_{\#} = 0$ so $\grave{c}(m) = 0$ )
Appendix A:	GIC,RIC	$\lim_{m\to\infty} \dot{c}(m) = \bar{c}(m), \lim_{m\to\infty} \dot{\boldsymbol{k}}(m) = \underline{\kappa}$
		kinks where horizon to $b = 0$ changes*
Appendix A:	GIC,RIC	$\lim_{m\to\infty} \grave{\boldsymbol{\kappa}}(m) = 0$
		kinks where horizon to $b = 0$ changes*
c(m): Friedman/Muth	Section 3.1,	$\underline{\mathbf{c}}(m) < \mathbf{c}(m) < \overline{\mathbf{c}}(m)$
	Section 3.2	$\underline{\mathbf{v}}(m) < \mathbf{v}(m) < \bar{\mathbf{v}}(m)$
Section 2.10:	FVAC, WRIC	Sufficient for Contraction
Section 2.12.1:		WRICis weaker than RIC
Figure 3:		FVACis stronger than PF-FVAC
Section 2.12.3:		EHWC+RIC $\Rightarrow$ GIC, $\lim_{m \to \infty} \kappa(m) = \underline{\kappa}$
Section 2.12.2:		RHC $\Rightarrow$ EHWC, $\lim_{m\to\infty} \kappa(m) = 0$
Section 3.3:		"Buffer Stock Saving" Conditions
Section 3.3.2:		$GIC \Rightarrow \exists 0 < \check{m} < \infty$
Section 3.3.1:		GIC-Nrm $\Rightarrow \exists 0 < \hat{m} < \infty$

<sup>‡</sup>For feasible m satisfying  $0 < m < \infty$ , a nondegenerate limiting consumption function defines a unique optimal value of c satisfying  $0 < c(m) < \infty$ ; a nondegenerate limiting value function defines a corresponding unique value of  $-\infty < \mathrm{v}(m) < 0$ . °RIC, FHWCare necessary as well as sufficient for the perfect foresight case. \*That is, the first kink point in c(m) is  $m_{\#}$  s.t. for  $m < m_{\#}$  the constraint will bind now, while for  $m > m_{\#}$  the constraint will bind one period in the future. The second kink point corresponds to the m where the constraint will bind two periods in the future, etc.\*\*In the Friedman/Muth model, the RIC+FHWC are sufficient, but not necessary for nondegeneracy

 Table 5
 Taxonomy of Perfect Foresight Liquidity Constrained Model Outcomes

 For constrained  $\grave{c}$  and unconstrained  $\bar{c}$  consumption functions

				1
Main Condition				
Subcondition		Math		Outcome, Comments or Results
SIC		1 <	$\mathbf{P}/\Gamma$	Constraint never binds for $m \geq 1$
and RIC	<b>Þ</b> /R	< 1		FHWC holds $(R > \Gamma)$ ; $\dot{c}(m) = \bar{c}(m)$ for $m \ge 1$
and RIC		1 <	$\mathbf{P}/R$	$\grave{\mathbf{c}}(m)$ is degenerate: $\grave{\mathbf{c}}(m) = 0$
GIC	$\mathbf{p}/\Gamma$	< 1		Constraint binds in finite time for any $m$
and RIC	<b>Þ</b> /R	< 1		FHWC may or may not hold
				$\lim_{m\uparrow\infty} \bar{\mathbf{c}}(m) - \grave{\mathbf{c}}(m) = 0$
				$\lim_{m\uparrow\infty} \grave{\boldsymbol{\kappa}}(m) = \underline{\kappa}$
and RIC		1 <	$\mathbf{P}/R$	EHWC
			•	$\lim_{m\uparrow\infty} \hat{\boldsymbol{\kappa}}(m) = 0$

Conditions are applied from left to right; for example, the second row indicates conclusions in the case where CHC and RIC both hold, while the third row indicates that when the GIC and the RIC both fail, the consumption function is degenerate; the next row indicates that whenever the GICholds, the constraint will bind in finite time.