Table 1
 Microeconomic Model Calibration

Calibrated Parameters					
Description	Parameter	Value	Source		
Permanent Income Growth Factor	Φ	1.03	PSID: Carroll (1992)		
Interest Factor	R	1.04	Conventional		
Time Preference Factor	β	0.96	Conventional		
Coefficient of Relative Risk Aversion	ρ	2	Conventional		
Probability of Zero Income	\wp	0.005	PSID: Carroll (1992)		
Std Dev of Log Permanent Shock	$\sigma_{f \Psi}$	0.1	PSID: Carroll (1992)		
Std Dev of Log Transitory Shock	$\sigma_{ heta}$	0.1	PSID: Carroll (1992)		

 Table 2
 Model Characteristics Calculated from Parameters

				Approximate
				Calculated
Description	Syr	nbol	and Formula	Value
Finite Human Wealth Factor	\mathcal{R}^{-1}	=	Φ/R	0.990
PF Value of Autarky Factor	コ	=	$eta oldsymbol{\Phi}^{1- ho}$	0.932
Growth Compensated Permanent Shock	Ψ	=	$(\mathbb{E}[\mathbf{\Psi}^{-1}])^{-1}$	0.990
Uncertainty-Adjusted Growth	$\underline{\Phi}$	=	$\Phi \underline{\Psi}$	1.020
Utility Compensated Permanent Shock	$\underline{\underline{\Psi}}$	=	$(\mathbb{E}[\mathbf{\Psi}^{1- ho}])^{1/(1- ho)}$	0.990
Utility Compensated Growth	Φ	=	$\Phi \underline{\Psi}$	1.020
Absolute Patience Factor	Þ	=	$(Reta)^{1/ ho}$	0.999
Return Patience Factor	\mathbf{p}_{R}	\equiv	\mathbf{p}/R	0.961
Growth Patience Factor	${\bf b}_\Phi$	=	\mathbf{P}/Φ	0.970
Modified Growth Patience Factor	${\tt P}_{\underline{\Phi}}$	=	$\mathbf{P}/\underline{\Phi}$	0.980
Value of Autarky Factor	⊒	=	$eta oldsymbol{\Phi}^{1- ho} \underline{\underline{\Psi}}^{1- ho}$	0.941
Weak Return Impatience Factor	$\wp^{1/ ho}\mathbf{p}$	=	$(\wp eta R)^{1/ ho}$	0.071

 ${\bf Table~3}~~{\bf Definitions~and~Comparisons~of~Conditions}$

Uncertainty Versions				
h Condition (FHWC)				
$\Phi/R < 1$				
The model's risks are mean-preserving spreads, so the PDV of future income is unchanged by their introduction.				
ce Condition (AIC)				
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If wealth is large enough, the expectation of consumption next period will be smaller than this period's consumption: $\lim_{m_t \to \infty} \mathbb{E}_t[\mathbf{c}_{t+1}] < \mathbf{c}_t$				
$m_t \rightarrow \infty$				
ence Conditions				
Weak RIC (WRIC)				
$\wp^{1/\rho}\mathbf{p}/R < 1$				
If the probability of the zero-income event is $\wp=1$ then income is always zero and the condition becomes identical to the RIC. Otherwise, weaker.				
$c'(m) < 1 - \wp^{1/\rho} \mathbf{P}/R < 1$				
ence Conditions				
GIC-Mod				
$\mathbf{p}\mathbb{E}[\mathbf{\Psi}^{-1}]/\mathbf{\Phi} < 1$				
By Jensen's inequality stronger than GIC. Ensures consumers will not expect to accumulate m unboundedly. $\lim_{m_t \to \infty} \mathbb{E}_t[m_{t+1}/m_t] = \mathbf{P}_{\underline{\Phi}}$				
Finite Value of Autarky Conditions				
FVAC				
$\beta \mathbf{\Phi}^{1-\rho} \mathbb{E}[\mathbf{\Psi}^{1-\rho}] < 1$				
By Jensen's inequality, stronger than the PF-FVAC because for $\rho > 1$ and nondegenerate Ψ , $\mathbb{E}[\Psi^{1-\rho}] > 1$.				

Table 4 Sufficient Conditions for Nondegenerate[‡] Solution

Consumption Model(s)	Conditions	Comments
$\bar{\mathbf{c}}(m)$: PF Unconstrained	RIC, FHWC°	$\text{RIC} \Rightarrow \mathbf{v}(m) < \infty; \text{ FHWC} \Rightarrow 0 < \mathbf{v}(m) $
$\underline{c}(m) = \underline{\kappa}m$		PF model with no human wealth $(h = 0)$
Section 2.5.3:		RIC prevents $\bar{\mathbf{c}}(m) = \underline{\mathbf{c}}(m) = 0$
Section 2.5.3:		FHWC prevents $\bar{\mathbf{c}}(m) = \infty$
Eq (21) :		$PF-FVAC+FHWC \Rightarrow RIC$
Eq (22):		$GIC+FHWC \Rightarrow PF-FVAC$
$\grave{\mathrm{c}}(m)$: PF Constrained	GIC, RIC	FHWC holds ($\Phi < \mathbf{P} < R \Rightarrow \Phi < R$)
Section 2.5.6:		$\grave{\mathbf{c}}(m) = \bar{\mathbf{c}}(m) \text{ for } m > m_{\#} < 1$
		(RHC would yield $m_{\#} = 0$ so $\grave{c}(m) = 0$)
Appendix E:	GIC,RIC	$\lim_{m\to\infty} \dot{c}(m) = \bar{c}(m), \lim_{m\to\infty} \dot{\boldsymbol{k}}(m) = \underline{\kappa}$
		kinks where horizon to $b = 0$ changes*
Appendix E:	GIC,RIC	$\lim_{m\to\infty} \grave{\boldsymbol{\kappa}}(m) = 0$
		kinks where horizon to $b = 0$ changes*
c(m): Friedman/Muth	Section 3.1,	$\underline{\mathbf{c}}(m) < \mathbf{c}(m) < \bar{\mathbf{c}}(m)$
	Section 3.2	$\underline{\mathbf{v}}(m) < \mathbf{v}(m) < \overline{\mathbf{v}}(m)$
Section 2.10:	FVAC, WRIC	Sufficient for Contraction
Section 2.12:		WRIC is weaker than RIC
Figure 3:		FVAC is stronger than PF-FVAC
Section 2.12.2:		EHWC+RIC \Rightarrow GIC, $\lim_{m\to\infty} \kappa(m) = \underline{\kappa}$
Section 2.12.1:		RHC \Rightarrow EHWC, $\lim_{m\to\infty} \kappa(m) = 0$
Section 3.3:		"Buffer Stock Saving" Conditions
Section 3.3.2:		GIC $\Rightarrow \exists \ \check{m} \text{ s.t. } 0 < \check{m} < \infty$
Section 3.3.1:		GIC-Mod $\Rightarrow \exists \hat{m} \text{ s.t. } 0 < \hat{m} < \infty$

[‡]For feasible m satisfying $0 < m < \infty$, a nondegenerate limiting consumption function defines a unique optimal value of c satisfying $0 < c(m) < \infty$; a nondegenerate limiting value function defines a corresponding unique value of $-\infty < \mathrm{v}(m) < 0$.

[°]RIC, FHWC are necessary as well as sufficient for the perfect foresight case. *That is, the first kink point in c(m) is $m_{\#}$ s.t. for $m < m_{\#}$ the constraint will bind now, while for $m > m_{\#}$ the constraint will bind one period in the future. The second kink point corresponds to the m where the constraint will bind two periods in the future, etc.

^{**}In the Friedman/Muth model, the RIC+FHWC are sufficient, but not necessary for nondegeneracy

Table 5 Appendix: Perfect Foresight Liquidity Constrained Taxonomy For constrained \hat{c} and unconstrained \bar{c} consumption functions

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Main Condition				
Subcondition		Math		Outcome, Comments or Results
SIC		1 <	Φ/Φ	Constraint never binds for $m \geq 1$
and RIC	⊅ /R	< 1		FHWC holds $(R > \Phi)$;
				$\grave{\mathbf{c}}(m) = \bar{\mathbf{c}}(m) \text{ for } m \geq 1$
and RIC		1 <	\mathbf{P}/R	$\grave{\mathbf{c}}(m)$ is degenerate: $\grave{\mathbf{c}}(m) = 0$
GIC	$\mathbf{p}/\mathbf{\Phi}$	< 1		Constraint binds in finite time $\forall m$
and RIC	Þ /R	< 1		FHWC may or may not hold
				$\lim_{m\uparrow\infty} \bar{\mathbf{c}}(m) - \grave{\mathbf{c}}(m) = 0$
				$\lim_{m\uparrow\infty} \hat{\boldsymbol{\kappa}}(m) = \underline{\kappa}$
and RHC		1 <	\mathbf{P}/R	EHWC
				$\lim_{m\uparrow\infty} \grave{\boldsymbol{\kappa}}(m) = 0$

Conditions are applied from left to right; for example, the second row indicates conclusions in the case where GIC and RIC both hold, while the third row indicates that when the GIC and the RIC both fail, the consumption function is degenerate; the next row indicates that whenever the GICholds, the constraint will bind in finite time.