

Friedman (1957) Concretely, a consumer born  $n$  periods before date  $T$  solves the problem

$$v_{T-n} = \max \mathbb{E}_t \left[ \sum_{i=0}^n \beta^i u(c_{t+i}) \right]$$

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