

# Equity and Efficiency of Childcare Subsidies: A Structural Approach

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## Evaluating childcare policies

- high self-financing rates for targeted programs  
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- ⇒ Fiscal return to expansion: creating subsidised slots in a rationed environment
- ⇒ Fiscal return to increasing subsidy: making slots cheaper in a non-rationed environment
- ⇒ How should subsidies vary with income? Equity-efficiency trade-off of childcare fees vs. taxes

## Key challenge:

→ Which mothers respond to changes in childcare policies and how?

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  - ↳ heterogeneity in wages, family composition, and education
  - ↳ quantification of the model for Germany (current policies)
- rich unobserved heterogeneity:
  - ↳ (i) taste for domestic childcare, (ii) taste for leisure, (iii) access to informal childcare
  - ↳ joint distribution estimated by ML using German panel data

## Expansion of access to public market childcare:

- 103% of the costs are recovered through increased tax revenue
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## Evaluation of childcare fee system versus tax system:

- marginal redistribution through childcare fee schedule implies **lower efficiency cost** than through tax system
- childcare fee schedule should be more progressive if groups are valued equally

Model

## Core setup:

- life cycle model (ages 20-80), three-year model period
- households: two adults with up to 3 children
- **choices**: female labour supply *lm* and domestic childcare *dcc*

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## State variables:

- **observed state space**  $s = (t, w_t^M, w_t^W, K_t, ed) \in S$ 
  - age of both partners  $t$
  - male and female wage  $(w_t^M, w_t^W)$ 
    - Markov processes cond. on not working/part-time/full-time
  - family composition  $K_t$ : age & number of children
    - exog. stochastic process cond. on maternal age & education
- **unobserved heterogeneity**  $h = (g, oth, \alpha) \in H$ 
  - domestic childcare preferences  $g$
  - availability of (informal) other childcare  $oth$
  - leisure preferences  $\alpha$

## Time requirements:

Children's age bracket $i$	0 - 2	3 - 5	6 - 8	$\geq 9$
Hours of childcare needed per week ( $\bar{t}_i$ )	40	40 <sup>†</sup>	15	0

## Provision & cost:

► details on *mcc*

- domestic childcare (*dcc*) → free
- (informal) other childcare (*oth*) → free
- market childcare (*mcc*) → priced dependent on income, family size, and child age



# Instantaneous utility

$$u(c, L, dcc) =$$

$$(1 - \mathcal{G}(g, K)) \left( (1 - \alpha) \frac{c^{1-\gamma_c} - 1}{1 - \gamma_c} + \alpha \frac{(L + \bar{L})^{1-\gamma_L} - 1}{1 - \gamma_L} \right) + \mathcal{G}(g, K) \left( \frac{(dcc + \overline{dcc})^{1-\gamma_{dcc}} - 1}{1 - \gamma_{dcc}} \right)$$

- $\alpha$ : relative preference for leisure vs. consumption
- $g$ : relative preference for domestic childcare vs. consumption-leisure component  
→ households explicitly value  $dcc$ , but not  $mcc$  and  $oth$

$$\mathcal{G}(g, K) = \begin{cases} g & \text{if youngest child's age} \in [0, 3) \\ g \cdot \kappa & \text{if youngest child's age} \in [3, 9) \end{cases}$$

# Dynamic optimization problem

$$V(s_t, h) = \max_{lm_t, dcc_t} u(c_t, L_t, dcc_t | s_t, h) + \beta \mathbb{E}[V(s_{t+1}, h | s_t, h, lm_t)]$$

s.t.

time constraint:  $40 = lm_t + L_t + dcc_t$ , with  $lm_t \in \{0, 20, 40\}$

budget constraint:  $y_t^{net} = c_t + Ecc(K_t, y_t^{gross})$

HH gross income:  $y_t^{gross} = 40 \cdot w_t^M (w_{t-1}^M) + lm_t \cdot w_t^W (w_{t-1}^W, lm_{t-1})$

HH net income:  $y_t^{net} = y_t^{gross} - \mathcal{T}(y_t^{gross}, K_t)$

childcare expenditure:  $Ecc(K_t, y_t^{gross}) = \sum_{i=1}^3 p(i, K_t, y_t^{gross}) \cdot mcc_t(i)$

market childcare takeup:  $mcc_t(i) = \max \{0, \bar{t}_i - dcc_t - oth\}$ , if  $i = 1, 3$   
 $mcc_t(2) = \max \{20, \bar{t}_i - dcc_t - oth\}$

# Quantification

## Auxiliary regressions & government policies

1. Wage process: log-normal estimation [◀ details](#)
2. Fertility process: non-parametric estimation [◀ details](#)
3. Government policies

## Structural estimation

1. Calibration of utility function parameters
2. Maximum likelihood estimation of unobserved heterogeneity

## Government policies:

- *Childcare price schedule* estimated separately by child age  
→ covariates: household income, household income  $\times$  siblings  
▶ Childcare fee schedules
- *Taxes and transfers*: implementation from Bick, Brüggemann, Fuchs-Schündeln, and Paule-Paludkiewicz (2019)
- *Childcare costs*: annual cost per full-time slot from federal statistics  
→ 0-2: 10.900 EUR, 3-5: 7.300 EUR, 6-8: 6.200 EUR (2012 prices)

# Calibrated parameters

## Calibrated model parameters:

parameter	$\beta$	$\gamma_c$	$\gamma_L$	$\bar{L}$	$\gamma_{dcc}$	$\overline{dcc}$	$\kappa$
value	0.94	1	2	1	1.125	4	0.075

## Targets:

- *Labour supply elasticities*
  - participation elasticity and aggregate hours elasticity
- *Labour market outcomes by age of the youngest child*
  - Share of NP, PT, and FT for child age brackets (0 – 2), (3 – 5), (6 – 8), and (9+)
- *Total market childcare shares by age of the youngest child*
  - 3 moments for each child age brackets (0 – 2), (3 – 5), and (6 – 8)

# Estimation of the distribution of unobserved heterogeneity

## Object of interest:

$\ell(h|\mathbf{x})$ , joint distribution of unobserved heterogeneity  $h$

→ conditional on constant characteristics  $\mathbf{x}$

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## Approach: Maximum Likelihood Estimation with panel data

- $lm_1, lm_2, mcc_1, mcc_2$ : observed individual choices
- $mcc$  and wages are observed with *measurement error*



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## Approach: Maximum Likelihood Estimation with panel data

- $lm_1, lm_2, mcc_1, mcc_2$ : observed individual choices
- $mcc$  and wages are observed with *measurement error*
- marginal distributions:  $\ell(h|\mathbf{x}) = l^g(g|\mathbf{x}^g) \cdot l^{oth}(oth|\mathbf{x}^{oth}) \cdot l^\alpha(\alpha|\mathbf{x}^\alpha)$   
→ overlap in  $\mathbf{x}$  creates correlations
- data-generating process of, e.g., domestic childcare preferences:  
 $\mathcal{N}(\gamma^g + \beta^g \mathbf{x}^g, (\sigma^g)^2)$

⇒ jointly estimate parameters  $\gamma$ ,  $\beta$ , and  $\sigma$  for each heterogeneity

# Data and constant characteristics

## Data:

- panel data from SOEP waves 2012 - 2017
  - mapped into two model periods
  - Sample includes women with at least one child and at most three
- ⇒ 2,178 individuals of which 1,073 have a child  $< 9$

## Constant characteristics x:

- domestic childcare preference  $g$ : *east, skilled occupation, catholic*
- availability of other childcare  $oth$  in West: *education, urban*
- leisure preference  $\alpha$ : *education, skilled occupation*

► estimation results

► marginal distributions

► sensitivity plots

## (Set) Identification is based on:

1. use of panel data and assumptions on the structure
  - allows to disentangle wage shocks from the permanent unobserved heterogeneity
  - changes in family composition over time affect which dimension of heterogeneity matters in which observed period
  - panel data also contains households with older children (9+)
2. cross-sectional variation in choices within period
  - conditional on the same observed states & constant characteristics

## Model Fit

## Labour supply shares by age of the youngest child

	Children 0 – 2			Children 3 – 5		
	NP	PT	FT	NP	PT	FT
Model	0.50	0.40	0.10	0.16	0.61	0.23
Data	0.55	0.40	0.05	0.17	0.65	0.18

	Children 6 – 8			Children 9+		
	NP	PT	FT	NP	PT	FT
Model	0.15	0.62	0.23	0.13	0.63	0.24
Data	0.13	0.68	0.19	0.16	0.54	0.30

## Total market childcare take-up shares by age of the youngest child

	Children 0 – 2		
	$Tcc \leq \bar{m}_1$	$\bar{m}_1 < Tcc \leq \bar{m}_2$	$\bar{m}_2 < Tcc$
Model	0.48	0.32	0.20
Data	0.44	0.40	0.16
	Children 3 – 5		
	$Tcc \leq \bar{m}_1$	$\bar{m}_1 < Tcc \leq \bar{m}_2$	$\bar{m}_2 < Tcc$
Model	0.00	0.53	0.47
Data	0.02	0.52	0.46
	Children 6 – 8		
	$Tcc \leq \bar{m}_1$	$\bar{m}_1 < Tcc \leq \bar{m}_2$	$\bar{m}_2 < Tcc$
Model	0.33	0.17	0.50
Data	0.29	0.23	0.48

Notes:  $Tcc$  denotes total market childcare of the household.  $\bar{m}_1$ , respectively  $\bar{m}_2$ , indicates that the household would cover a share of 0.33, respectively 0.75, of its total need for childcare through market childcare.

1. Compensated intensive margin elasticity: 0.17

2. Compensated extensive margin elasticity: 0.15

**Work in Progress:** Relation to other quasi-experimental estimates such as childcare price elasticity

# Policy Evaluations



## What is the fiscal return of a permanent lifting of rationing?

- Expansion of public childcare for 0-2 year olds between 2005 and 2012 in West Germany

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- Expansion of public childcare for 0-2 year olds between 2005 and 2012 in West Germany
- ⇒ comparison of *rationing scenario* with *non-rationing baseline scenario*
- Rationing implementation in a modified framework:
    - 85% rationing probability, matching the pre-expansion take-up share of market childcare for 0-2 year olds
    - fallback option of informal childcare of 17.5h/week to match the employment share of mothers with 0-2 year olds in 2005 (30%)
- ⇒ 45% of mothers who start using public childcare also start working  
[in line with reduced form evidence from Bauernschuster and Schlotter (2015)]

# Policy evaluation I: Expansion of access to public childcare

Self-financing degree of public childcare expansion:  $SFD = \frac{\Delta T}{\Delta S}$

- simulate sample in the rationing and non-rationing scenario
  - $\Delta T$  ( $\Delta S$ ): difference in discounted tax revenue (subsidy expenses)
- time horizons: (i) impact period and (ii) all periods
  - in (ii): evolution of wages (plus age and fertility) are taken into account

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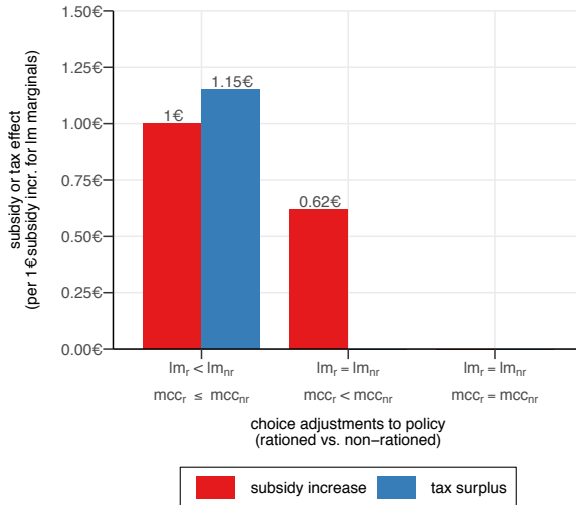
## Resulting self-financing degrees:

- *Impact period:*
  - 71.1% of increase in subsidy expenses recovered through increased tax revenues
- *All periods:*
  - increases to 103.3%
  - of which 35.8pp: positive effect of wage dynamics on future tax revenues

# Policy evaluation I: Expansion of access to public childcare

## Decomposition of subsidy or tax effect in the *Impact period*

- Recall: Self-financing degree in *Impact period*:  $SFD = \frac{\Delta T}{\Delta S} = 71.1\%$



## Self-financing degree of increase in childcare subsidies by 50€/month

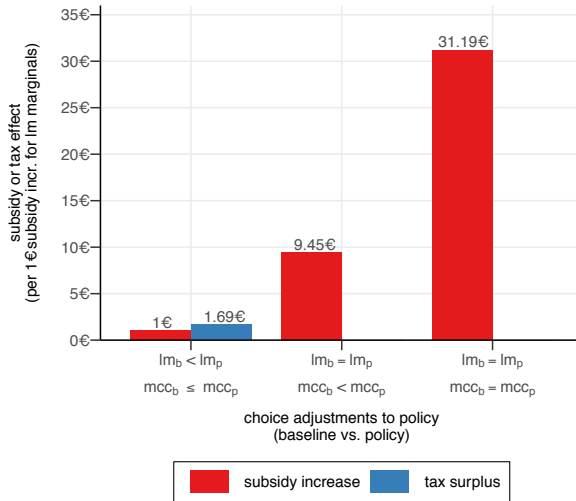
- in the non-rationed environment

	total
<i>(i) untargeted</i>	
Impact period	4.1%
All periods	5.9%
<i>(ii) full-time work contingent</i>	
Impact period	33.5%
All periods	50.1%

# Policy evaluation II: Increasing childcare subsidies

## Decomposition of fiscal effect of an untargeted increase

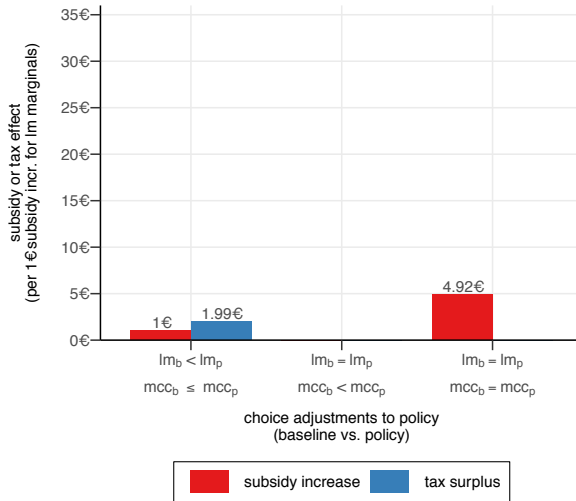
- Recall: Self-financing degree in *Impact period*:  $SFD = \frac{\Delta T}{\Delta S} = 4.1\%$



# Policy evaluation II: Increasing childcare subsidies

## Decomposition of fiscal effect of full-time work contingent increase

- Recall: Self-financing degree in *Impact period*:  $SFD = \frac{\Delta T}{\Delta S} = 33.5\%$





## Policy evaluation III: Redistribution through childcare fees

- current childcare fee schedule entails redistribution
- What are the efficiency costs of redistribution associated with the existing progressive childcare fee schedule?

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### Efficiency cost of redistribution:

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## Implementation:

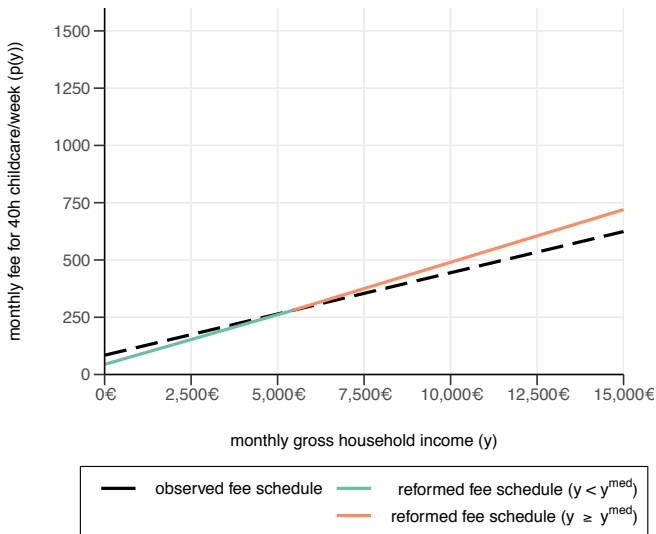
- Parametric reform of (i) tax schedule and (ii) childcare fees:

$$T^*(y) = \begin{cases} T(y) + \tau_1 (y - y^{med}) & \text{for } y \geq y^{med} \\ T(y) - \tau_2 (\tau_1) (y^{med} - y) & \text{for } y < y^{med} \end{cases}$$

- Fix  $\tau_1 = 0.01$  and choose  $\tau_2$  such that reform is budget-neutral taking behavioral changes into account

# Policy evaluation III: Redistribution through childcare fees

## Parametric reform of the childcare fee schedule



## Resulting marginal excess burdens:

- ... for the tax schedule = 0.289
- ... for the childcare fee schedule = 0.182

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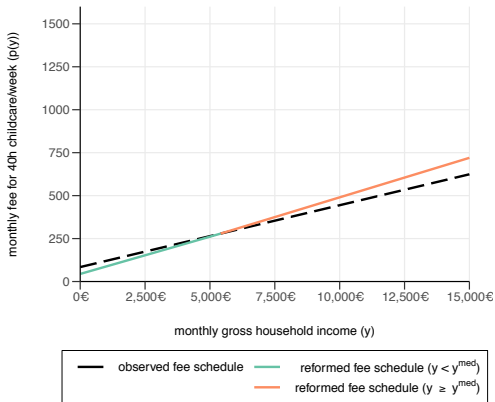
- ... for the tax schedule = 0.289
- ... for the childcare fee schedule = 0.182

⇒ childcare fee schedule: lower efficiency cost of redistribution

⇒ if the government has the same desire to redistribute within the population that uses market childcare, childcare fees should be made *more progressive*

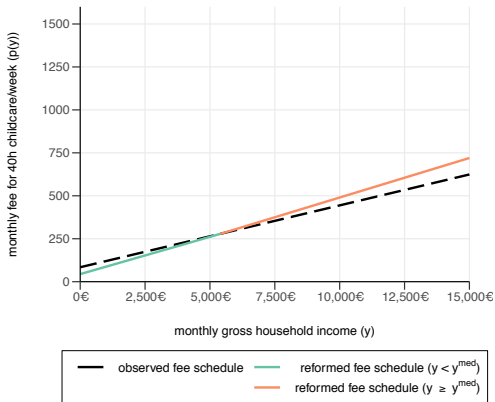
But where does the difference in efficiency costs come from?

# Policy evaluation III: Redistribution through childcare fees



1. Increase in effective marginal tax rates for all income levels  
→ applies to tax schedule and childcare fee schedule  
⇒ labor supply ↓

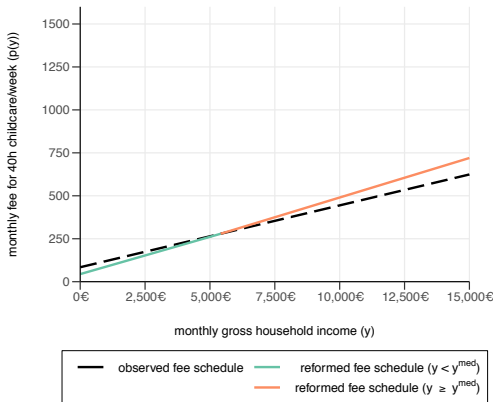
# Policy evaluation III: Redistribution through childcare fees



2. Change in the level of the monthly childcare fee
  - applies only to the childcare fee schedule
  - adjusts the return to working versus not-working
  - ⇒ labor supply  $\uparrow$  if  $y < y^{med}$
  - ⇒ labor supply  $\downarrow$  if  $y \geq y^{med}$



# Policy evaluation III: Redistribution through childcare fees



2. (ctd.)

→ adjusts the relative price of leisure versus domestic childcare (for constant labor supply)

⇒ use of public childcare  $\uparrow$  if  $y < y^{med}$

⇒ use of public childcare  $\downarrow$  if  $y \geq y^{med}$

# Policy evaluation III: Redistribution through childcare fees

Table: Decomposition of the marginal excess burden (MEB)

	tax schedule (MEB = 0.289)		childcare fee schedule (MEB = 0.182)	
	$lm \downarrow$	$lm \uparrow$	$lm \downarrow$	$lm \uparrow$
$y < y^{med}$	0.111 [38.5%]	0.000 [0.0%]	0.016 [8.7%]	-0.003 [-1.7%]
$y \geq y^{med}$	0.178 [61.6%]	0.000 [0.0%]	0.125 [69.1%]	0.000 [0.0%]
	unchanged $lm$ & changed $Tcc$		unchanged $lm$ & changed $Tcc$	
	0.000 [0.1%]		0.044 [24.1%]	

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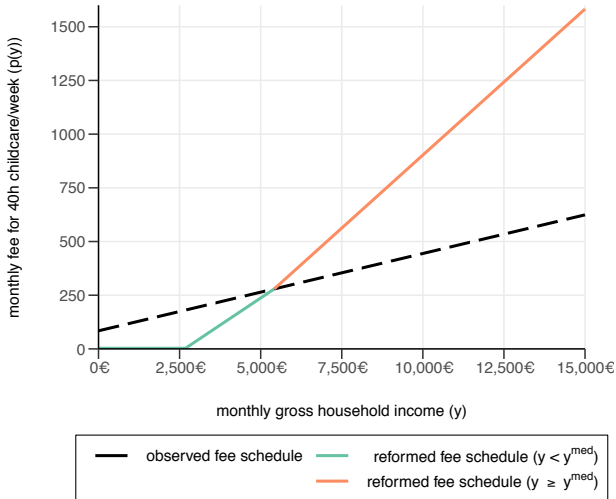
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# Policy evaluation III: Childcare fee reform

**Reform:** adjusting childcare fee schedule to imply same efficiency costs as the tax system



# Conclusion

**This paper:** rich structural model to investigate the dynamic fiscal implications of childcare policies

1. *What are the effective fiscal costs of expanding access to public childcare?*
  - ↳ A large public childcare expansion fully paid for itself through the dynamic effects on maternal earnings.
2. *Given the current level of subsidization, to what extent are additional childcare subsidies self-financing?*
  - ↳ Further (untargeted) increases from the current generous level would only be 6% self-financing.
3. *How does the efficiency of redistribution via childcare fees compare to taxes?*
  - ↳ The current childcare fee schedule implies substantially lower efficiency cost of redistribution.

Thank you for your attention!

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Backup



# Rationing in Germany?

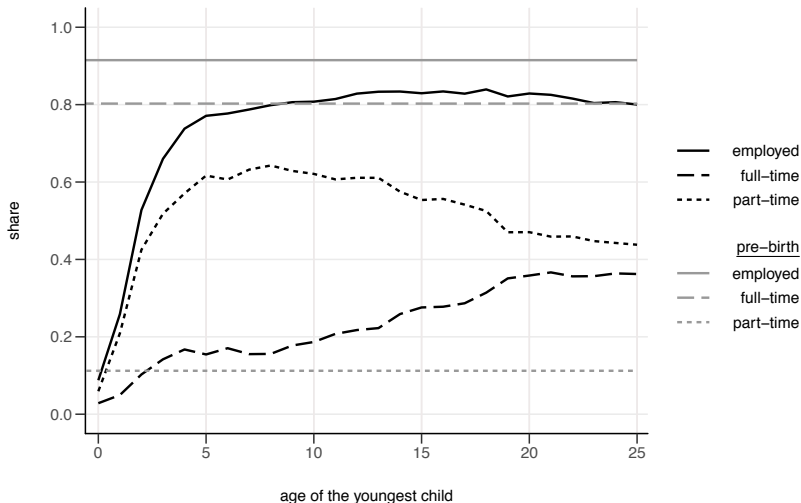
- it seems that the “hard rationing” is smaller than what it is usually thought of (see table below)
- we identify the distribution of  $g$  conditional on current policy
- “rationing” is partly expressing preferences as visible from the table below: the distribution of  $g$  will capture this in a reduced form way, e.g., rationing related to location-dependency (distance, neighbourhood), quality ...

## Excess demand for public childcare - children aged below 3:

desired hours per week $\leq 20$		desired hours per week $> 20$	
slot offered, but not used	no slot offered	slot offered, but not used	no slot offered
3.14%	1.09%	3.07%	2.09%

Notes: Source: DJI-Kinderbetreuungsstudie (waves 3 & 4, 2014 & 2015). Sample: children below 3, weighted to achieve representativeness at the national level.

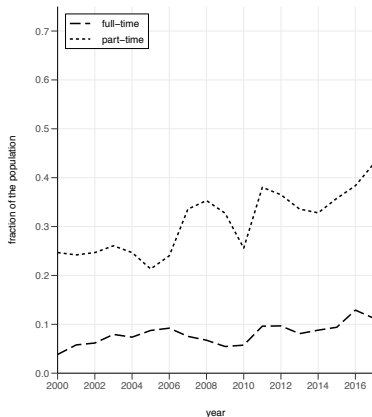
# Mothers on the labour market in Germany

[< back](#)

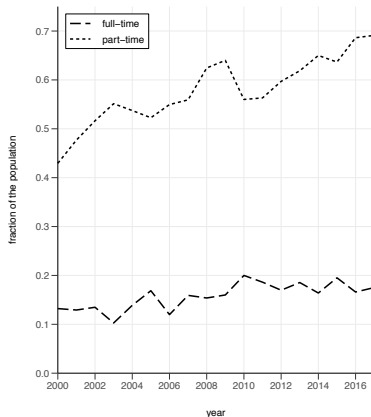
Sample: females aged 20 to 65 who are not in education and live with a full-time working partner, conditional on having at least one child. Source: 2000 to 2017 GSOEP.

[▶ labour supply over time](#)[▶ childcare takeup over time](#)

# Employment of mothers across time

[◀ back](#)

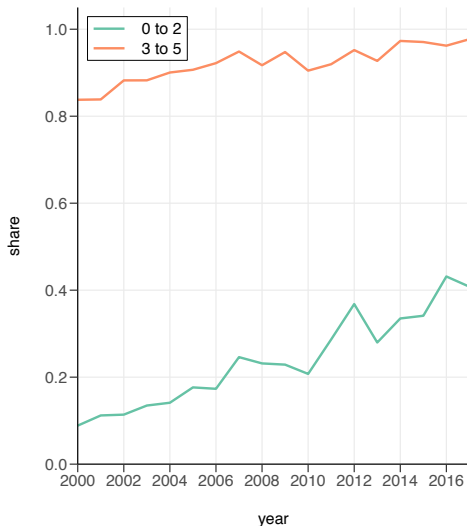
(a) Children aged 0-2



(b) Children aged 3-5

Sample: mothers aged 20 to 65 that are not in education and live with a full-time working partner, conditional on having a child aged 0 to 2 for panel (a) or 3 to 5 for panel (b). Source: 2000 to 2017 GSOEP.

# Public market childcare enrolment across time

[◀ back](#)

Notes: Enrolment is binary in the sense that it is not conditional on a minimum number of hours. Sample: mothers aged 20 to 65 that are not in education and live with a full-time working partner. Source: 2000 to 2017 GSOEP.

## Market childcare:

- largely provided by government or non-profit organizations (approx. > 95%)
- quality is highly regulated

## Taxes and transfers:

- child-dependent taxes and transfers

## Parental leave:

- one-year paid parental leave
- job guarantee for three years

⇒ Market childcare and taxes and transfers realistically modelled

⇒ Parental leave policies are not modelled because:

- i. dynamic effects of child birth related career breaks are well captured by the estimated wage process
- ii. only small effect of a one-year paid parental leave on the three year budget
- iii. state-dependent policy on previous labour market choice (complication of model)

- 1996: Legal right to a slot in Kindergarten for all children aged  $\geq 3$
- Before 2005: Only 5 public childcare slots per 100 children under age of 3
- 2005: A federal law (Tagesbetreuungsbaugesetz):  
Commitment to 230,000 additional childcare slots → 17 slots per 100 children
- 2007: summit of federal, state and regional German governments agreed on an increase up to 35 slots per 100 children
- 2008: Kinderförderungsgesetz:
  - From October 2010: Legal right to subsidized child-care slot for all children below the age of 3 if both parents are working
  - From August 2013: Legal right to a subsidized childcare slot for all children aged 1 and above

### **Structural work on female labour supply & child-related policies:**

Bick (2016); Adda, Dustmann, and Stevens (2017); Turon (2019); Guner, Kaygusuz, and Ventura (2020); Hannusch (2020)

- clear-cut public economics research question
- modelling rich heterogeneity in family structures
- estimating a joint distribution of three-dim. unobserved heterogeneity

### **Public Finance:**

Domeij and Klein (2013); Ho and Pavoni (2019); Colas, Findeisen, and Sachs (2021)

- introduction of universal childcare & marginal change in childcare subsidy, both including dynamic fiscal effects
- evaluating the value of the implied redistribution

### **Reduced Form Empirical Evidence on Labour Supply Effects:**

Bauernschuster and Schlotter (2015); Gathmann and Sass (2018)

- long-run (fiscal) effects and counter-factual policy changes
- effects of (targeted) subsidies

Exogenous price of one hour of market childcare:

$$p(i, K, y^{gross})$$

where  $i = 1, 2, 3$  indicates the child age and  $K$  the number & age structure of children.

Amount of market childcare for a child of age  $i$ :

$$\begin{aligned}mcc(i) &= \max \{0, \bar{t}_i - dcc - oth\}, & \text{if } i = 1, 3 \\mcc(2) &= \max \{20, \bar{t}_i - dcc - oth\}\end{aligned}$$

Household expenditure for market childcare:

$$Ecc(K, y^{gross}) = \sum_{i=1}^3 p(i, K, y^{gross}) \cdot mcc(i)$$

where  $K$  indicates the number & age structure of children.



Estimation of wage process based on GSOEP 2000 - 2017:

- imputing unobserved wages accounting for selection
  - female wages are determined by  $\log(w_{it}^W) = \mathbf{X}_{it}\boldsymbol{\beta} + u_{it}$ 
    - Mincer-type covariates, number of children (+ below 5), urban, former East Germany, year dummies
  - female wages are observed if:  $\mathbf{Z}_{it}\boldsymbol{\zeta} + \nu_{it} > 0$ 
    - exclusion restrictions: dummies for presence of (0-2,3-5,6-8,9-17,18+) year old children, husband's wage quintile, net household income in case of not working

- fit log-normal wage models

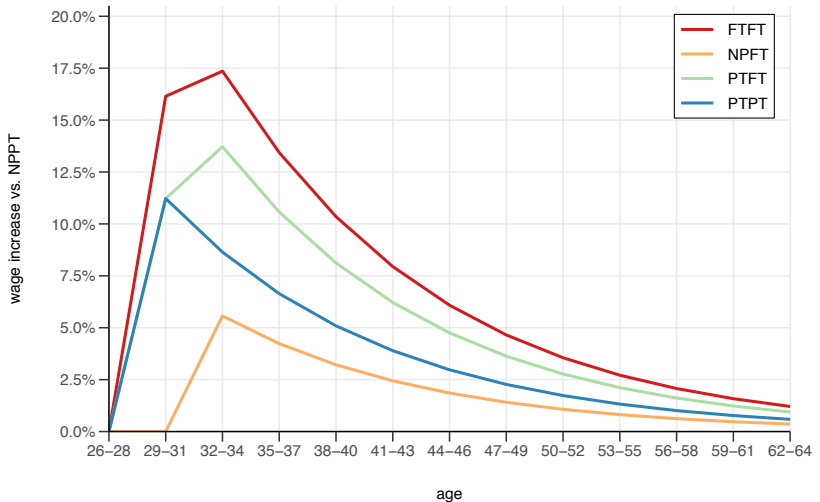
[▶ estimation results](#)

$$\log(w_{i,t}^W) = \alpha + \beta_1 \log(w_{i,t-1}^W) + \beta_2 \mathbb{1}\{lm_{i,t-1} = NP\} + \beta_3 \mathbb{1}\{lm_{i,t-1} = PT\} \\ + \beta_4 educ_i + f(t) + \varepsilon_{i,t}^W$$

- compute gender- and age-specific transition probabilities between wage gridpoints conditional on labour supply choice

[▶ Wage dynamics across the life cycle](#)

# Illustration of Wage Process Dynamics



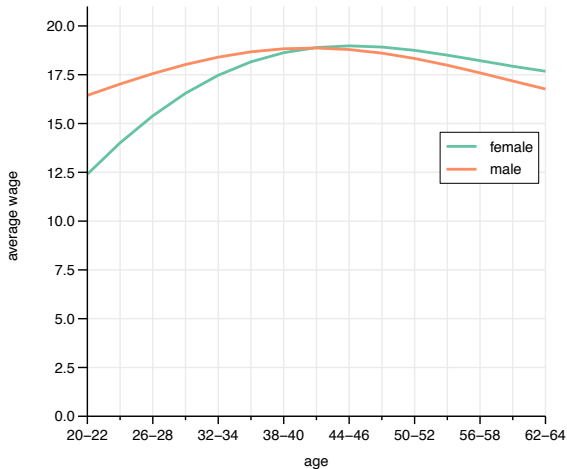
Notes: Relative increase in wages of different labour supply patterns, always compared to not working at age 26-28 and working part-time at age 29-31. NP, PT, and FT denote not working, part-time work, and full-time work respectively.

# Estimation of female and male wage dynamics

[◀ back](#)

	$\log(w_t^{\text{female}})$	$\log(w_t^{\text{male}})$
$\text{age}_t$	0.020 (0.013)	0.010 (0.0093)
$\text{age}_t^2$	-0.0026 (0.0017)	-0.0018 (0.0012)
$\text{age}_t^3$	0.000082 (0.000067)	0.000059 (0.000048)
$\text{educ}$	0.076 (0.0052)	0.027 (0.0036)
$\text{NP}_{t-1}$	-0.18 (0.0065)	
$\text{PT}_{t-1}$	-0.057 (0.0057)	
$\log(w_{t-1}^{\text{female}})$	0.75 (0.0057)	
$\log(w_t^{\text{male}})$		0.91 (0.0040)
constant	0.70 (0.032)	0.30 (0.023)
$\sigma^2$	0.28 (0.0017)	0.20 (0.0012)

# Wage dynamics across the lifecycle

[◀ back](#)

Notes: Simulated average wages starting with the observed wage distributions for individuals without A-Levels aged 20-22 and assuming continuous full-time work for the remaining lifecycle.

## Definition family composition type $K$ :

- number of children aged  $(0 - 2)$ ,  $(3 - 5)$ ,  $(6 - 8)$ ,  $(9+)$
- 4-element vector  $K$  indicating the presence of a child in each bracket

## Assumptions:

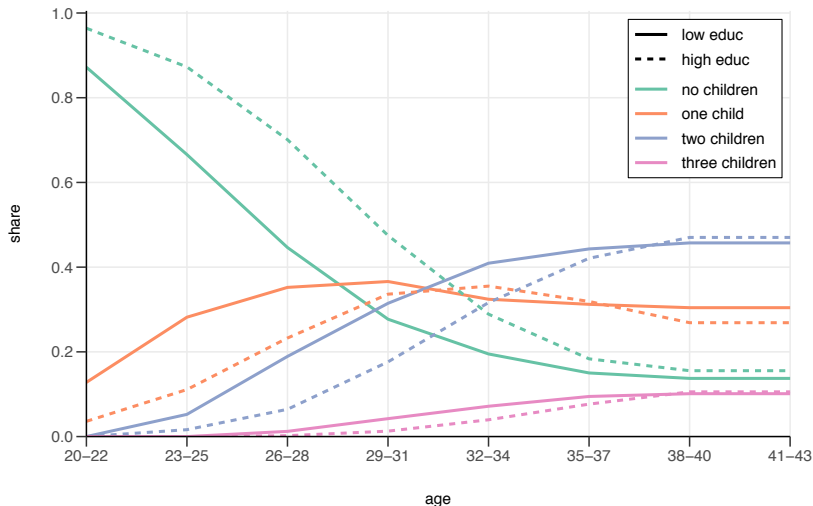
- one child per 3 year period
- subsequent siblings can only be born in one or two three-year intervals
- children's age difference is equal to the period length

## Non-parametric estimation:

- observed age and education specific transition probabilities between consecutive types

# Illustration of the fertility process

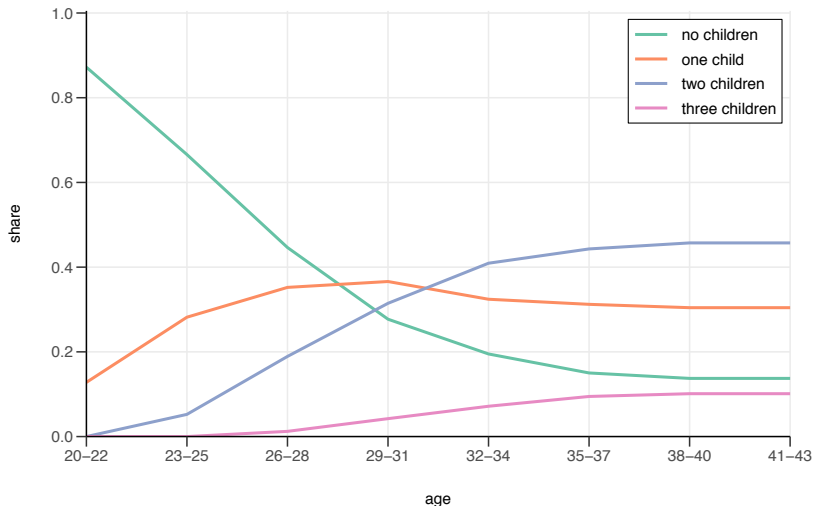
[▶ back to illustration for low educated](#)



Notes: Population shares of family size, high educ: A-levels or college, childbirths between age 20 and 40. Sample: Females aged 20 and 65, not in education, and living with a full-time working husband, Microcensus 2014 & 2018.

# Illustration of the fertility process [low educated]

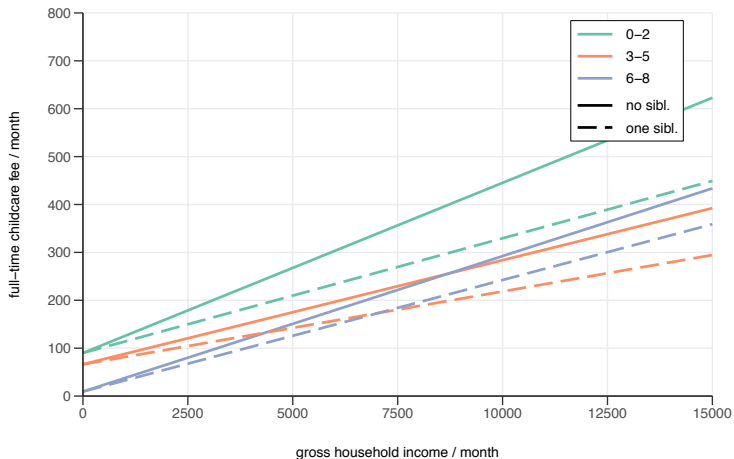
► Figure: high & low educated



Notes: Population shares of family size, high educ: A-levels or college, childbirths between age 20 and 40. Sample: Females aged 20 and 65, not in education, and living with a full-time working husband, Microcensus 2014 & 2018.

# Childcare fee schedule

[◀ back to Government policies](#)



Full-time equivalent monthly childcare fees, based on estimates from Tobit models.



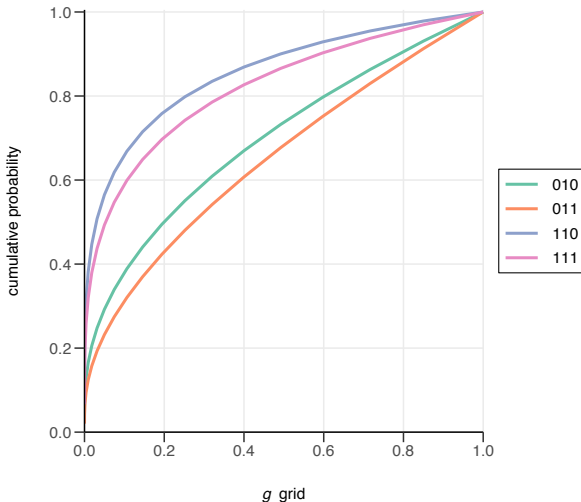
## Calibrated model parameters:

parameter	$\beta$	$\gamma_c$	$\gamma_L$	$\bar{L}$	$\gamma_{dcc}$	$\overline{dcc}$	$\kappa$
value	0.94	1	2	1	1.125	4	0.075

## Targets:

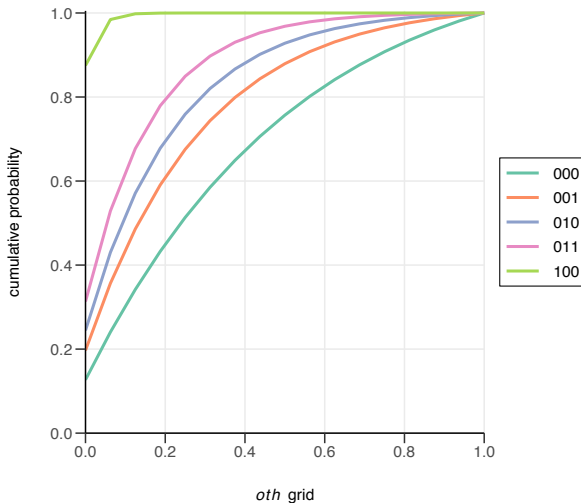
- *Labour supply elasticities*
  - participation elasticity and aggregate hours elasticity
- *Labour market outcomes by age of the youngest child*
  - Share of NP, PT, and FT for child age brackets (0 – 2), (3 – 5), (6 – 8), and (9+)
- *Total market childcare shares by age of the youngest child*
  - 3 moments each for child age brackets (0 – 2), (3 – 5), and (6 – 8)

# Estimated CDFs of home produced childcare preference $g$

[◀ back](#)

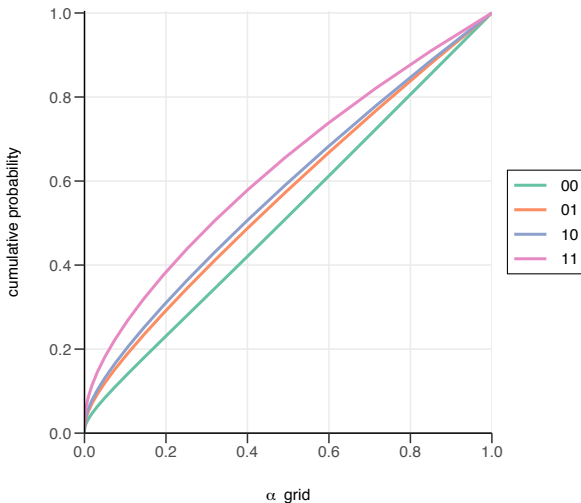
Notes: The legend indicates if the respective dummy of – in this order – **east**, **skilled occupation**, **catholic** is 0 or 1. We omit the plots for *no* skilled occupation because the implied difference by skilled occupation is small and would render the graph unreadable.

# Estimated CDFs of informal childcare *oth*

[◀ back](#)

Notes: The legend indicates if the respective dummy of – in this order – **east**, **education**, **urban** is 0 or 1.

# Estimated CDFs of leisure preferences $\alpha$

[◀ back](#)

Notes: The legend indicates if the respective dummy of – in this order – **high experience**, **education** is 0 or 1.

# Maximum likelihood estimates

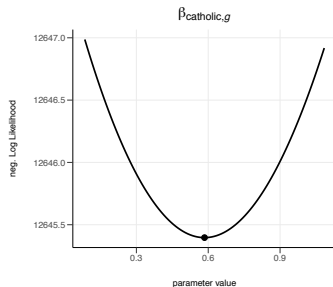
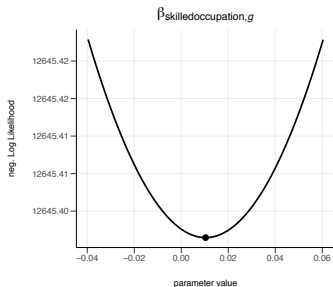
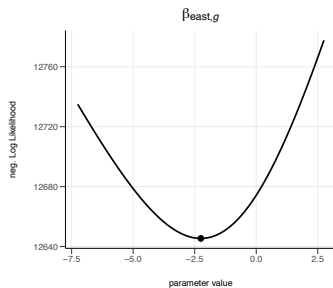
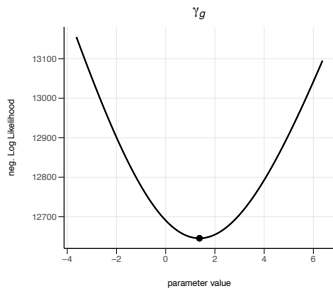
[◀ back](#)

	home produced childcare ( $g$ )	avail. of other childcare ( $oth^{west}$ )	avail. of other childcare ( $oth^{east}$ )	leisure ( $\alpha$ )
$\gamma$	1.37	-7.12	-33.25	1.63
$\beta_{east}$	-2.25			
$\beta_{skilled\ occupation}$	0.01			-0.22
$\beta_{catholic}$	0.58			
$\beta_{education}$		-10.44		-0.28
$\beta_{urban}$		-6.27		
$\sigma$	1.00	2.00	1.00	0.55

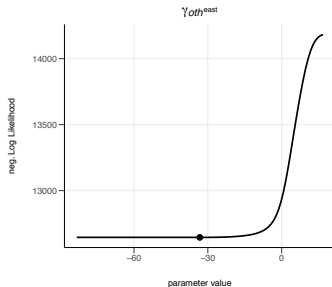
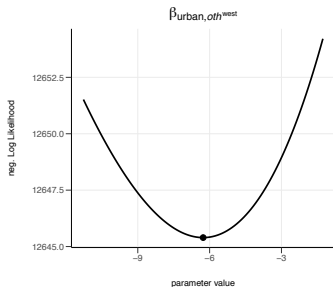
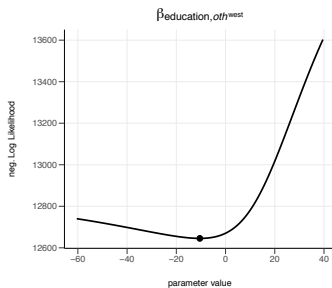
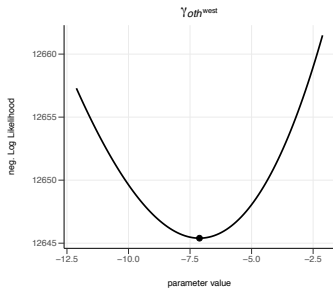
Notes: Estimation results for the distributional parameters of the unobserved heterogeneity.

$\sigma$  of  $oth^{east}$  is fixed to 1 for computational reasons.

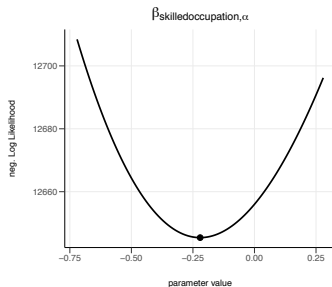
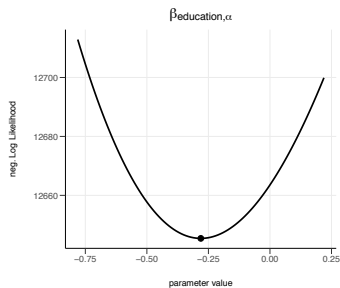
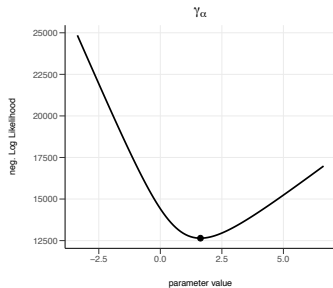
# Sensitivity plots of the ML estimates of the means of $g$

[◀ back](#)

# Sensitivity plots of the ML estimates of the means of $oth$

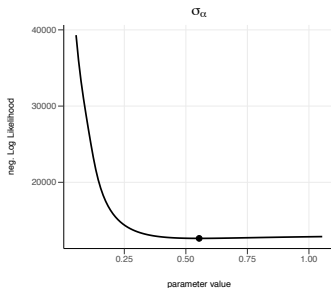
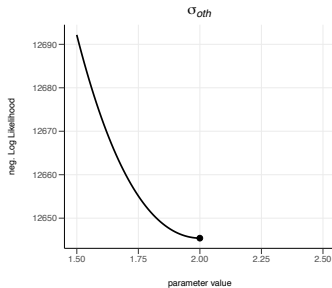
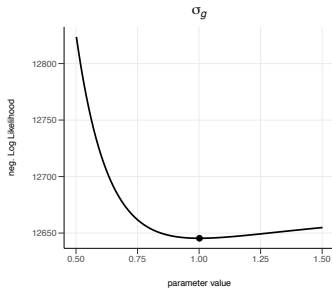
[◀ back](#)

# Sensitivity plots of the ML estimates of the means of $\alpha$

[◀ back](#)



# Sensitivity plots of the ML estimates of the variances

[◀ back](#)

## 1. Simulation of a permanent increase in gross female wages by 1%:

⇒ (Marshallian) Participation elasticity in the model: 0.09

⇒ (Marshallian) Aggregate hours elasticity in the model: 0.18

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## 2. Simulation of a permanent lump-sum net transfer of 1000 EUR:

⇒ Income effect (net of taxes): -0.135

## 1. Simulation of a permanent increase in gross female wages by 1%:

⇒ (Marshallian) Participation elasticity in the model: 0.09

⇒ (Marshallian) Aggregate hours elasticity in the model: 0.18

## 2. Simulation of a permanent lump-sum net transfer of 1000 EUR:

⇒ Income effect (net of taxes): -0.135

This yields by the Slutsky equation ...

⇒ (Hicksian) Participation elasticity: 0.1575

⇒ (Hicksian) Aggregate hours elasticity: 0.315

# Fiscal calculations from main part

Permanent decrease in hourly childcare price schedule  $p' < p$

⇒ We consider two time horizons

- Impact period
- All periods  
→ here, we need to take the evolution of wages (plus age and fertility) into account

# Fiscal calculations from main part

Permanent decrease in hourly childcare price schedule  $p' < p$

⇒ Self-financing degree over all periods

$$SFD_{rem} = \frac{T_{rem}}{S_{rem}}$$

- we calculate for every combination of observed and unobserved heterogeneity  $(s_t, h)$  and price change  $p' < p$ 
  - ... the change in the government tax revenue  $\Delta T(s_t, h; p, p')$
- weighted by the distributions of observed and unobserved heterogeneity,  $l_{3,t}(s_{t,n}, x_n)$  and  $l_2(h|x_n)$
- discounted sum over all periods

$$T_{rem} = \sum_{n=1}^N \sum_{h \in H} \sum_{t=imp}^{T(n)} \left( \frac{1}{1+r} \right)^{t-imp} \Delta T(s_{t,n}, h; p, p') l_2(h|x_n) l_{3,t}(s_{t,n}, x_n)$$

⇒ Permanent decrease in the childcare price schedule  $p' < p$   
[given hourly cost of market childcare for the government:  $C$ ]

- for every state  $(s, h)$  and the price change  $p' < p$ , we calculate
  - ... the government subsidy  $\Delta S(s, h; p, p')$ 
    - mechanical: price decrease for constant  $mcc$
    - behavioral: adjustments in  $mcc$
  - ... the government revenue  $\Delta T(s, h; p, p')$
- weighting by  $l_2(h|x_n) \cdot l_3(s_n, x_n)$  [households from the data]
- we consider two time horizons:
  - Impact period
  - All periods
    - here, we need to take the evolution of wages into account

## Fiscal calculations I

⇒ Permanent decrease in the childcare price schedule  $p' < p$   
given hourly cost of market childcare for the government:  $C$



# Fiscal calculations I

⇒ Permanent decrease in the childcare price schedule  $p' < p$   
given hourly cost of market childcare for the government:  $C$

**Government expenses for subsidies for given  $(s, h)$ :**

$$\Delta S(s, h; p, p') = (C - p') \cdot mcc^*(s, h; p') - (C - p) \cdot mcc^*(s, h; p)$$

→ mechanical:  $\Delta S_m(s, h) = [(C - p') - (C - p)] \cdot mcc^*(s, h; p)$

→ behavioural:  $\Delta S_b(s, h) = (C - p') \cdot [mcc^*(s, h; p') - mcc^*(s, h; p)]$

# Fiscal calculations I

⇒ Permanent decrease in the childcare price schedule  $p' < p$   
given hourly cost of market childcare for the government:  $C$

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$$\rightarrow \text{mechanical: } \Delta S_m(s, h) = [(C - p') - (C - p)] \cdot mcc^*(s, h; p)$$

$$\rightarrow \text{behavioural: } \Delta S_b(s, h) = (C - p') \cdot [mcc^*(s, h; p') - mcc^*(s, h; p)]$$

**Government revenues for given  $(s, h)$ :**

$$\begin{aligned} \Delta T(s, h; p, p') &= T(y^{gross}(s, h; p')) - T(y^{gross}(s, h; p)) \\ &= T(40 \cdot (w^M + lm^*(s, h; p') \cdot w^W)) - T(40 \cdot (w^M + lm^*(s, h; p) \cdot w^W)) \end{aligned}$$

## Population-wide self-financing degree in the *impact period*:

- Government revenues through taxes:

$$T_{imp} = \sum_{n=1}^N \sum_{h \in H} \Delta T(s_n, h; p, p') l_2(h|x_n) l_3(s_n, x_n)$$

- Government expenses through subsidies:

$$S_{imp} = \sum_{n=1}^N \sum_{h \in H} \Delta S(s_n, h; p, p') l_2(h|x_n) l_3(s_n, x_n)$$

⇒ Self-financing degree in the impact period

$$SFD_{imp} = \frac{T_{imp}}{S_{imp}}$$

## Population-wide self-financing degree over all periods:

- Government revenues through taxes:

$$T_{rem} = \sum_{n=1}^N \sum_{h \in H} \sum_{t=imp}^{T(n)} \left( \frac{1}{1+r} \right)^{t-imp} \Delta T(s_{t,n}, h; p, p') l_2(h|x_n) l_{t,3}(s_{t,n}, x_n)$$

- Government expenses through subsidies:

$$S_{rem} = \sum_{n=1}^N \sum_{h \in H} \sum_{t=imp}^{T(n)} \left( \frac{1}{1+r} \right)^{t-imp} \Delta S(s_{t,n}, h; p, p') l_2(h|x_n) l_{t,3}(s_{t,n}, x_n)$$

where  $r$  corresponds to 1% per year.

⇒ Self-financing degree over all periods

$$SFD_{rem} = \frac{T_{rem}}{S_{rem}}$$

# Policy evaluation II: Increasing childcare subsidies

## Self-financing degree of increase in childcare subsidy by 50€/month

		female hourly wage		
	total	≤ 15€	20€	≥ 25€
<i>(i) untargeted +50 EUR</i>				
Impact period	4.1%	3.4%	5.4%	4.3%
All periods	5.9%	5.3%	7.1%	6.2%

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All periods	5.9%	5.3%	7.1%	6.2%
(ii) <i>work contingent +50 EUR</i>				
Impact period	8.7%	7.4%	11.9%	8.0%
All periods	12.4%	11.0%	15.4%	11.6%

# Policy evaluation II: Increasing childcare subsidies

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(ii) <i>work contingent +50 EUR</i>				
Impact period	8.7%	7.4%	11.9%	8.0%
All periods	12.4%	11.0%	15.4%	11.6%
(ii) <i>full-time contingent +50 EUR</i>				
Impact period	33.5%	29.6%	40.4%	33.6%
All periods	50.1%	48.3%	54.0%	47.2%

→ targeting creates work incentives ⇒ higher tax returns

→ targeting reduces share of inframarginal mothers ⇒ lower costs of subsidy

1. increase taxes for above-median income households by 1% and reduce them for below-median households by  $\tau$ , choosing  $\tau$  to keep the budget balanced after behavioral adjustments
  2.  $\text{excess burden} = 1 - \frac{\text{net income increase for below-median HH}}{\text{net income decrease for above-median HH}}$ , holding labour supply and domestic childcare choices fixed (as the indirect effects from the behavioral changes are second order [*envelope theorem*])
- ⇒ measure for the governments preference to redistribute from above- to below-median income households