

NO: 27/02/23

Date:

Assignment 1. Vector Algebra

$$E=(1,-1) \quad F=(1,1) \quad G=(2,3) \\ V=(1,-1,0) \quad W=(1,1,1) \quad Z=(0,1,2) \\ a=0.5, b=2, c=1.62$$

$$X_1 = a \cdot E + b \cdot F + c \cdot G \\ (0.5 \cdot 1, 0.5 \cdot (-1)) + (2 \cdot 1, 2 \cdot 1) + (1.62 \cdot 2, 1.62 \cdot 3) \\ (0.5, -0.5) + (2, 2) + (3.24, 4.86) \\ (2.5, 1.5) + (3.24, 4.86) \\ X_1 = (5.74, 6.36)$$

$$X_2 = E/|E| + F/|F| \\ \frac{(1,-1)}{\sqrt{1^2+(-1)^2}} + \frac{(1,1)}{\sqrt{1^2+1^2}} \\ = \frac{(1,-1)}{\sqrt{2}} + \frac{(1,1)}{\sqrt{2}} \\ = \left(\frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}\right) + \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \\ = \left(\frac{2}{\sqrt{2}}, 0\right) = \frac{\sqrt{2} \cdot \sqrt{2}}{\sqrt{2}} \\ X_2 = (\sqrt{2}, 0)$$

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$$X_3 = W/|W| - Z/|Z| \\ \frac{(1,1,1)}{\sqrt{1^2+1^2+1^2}} - \frac{(0,1,2)}{\sqrt{0^2+1^2+2^2}} \\ = \frac{(1,1,1)}{\sqrt{3}} - \frac{(0,1,2)}{\sqrt{5}} \\ = \left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}\right) - \left(0, \frac{1}{\sqrt{5}}, \frac{2}{\sqrt{5}}\right) \\ = \left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}} - \frac{1}{\sqrt{5}}, \frac{1}{\sqrt{3}} - \frac{2}{\sqrt{5}}\right) \\ X_3 = \left(\frac{1}{\sqrt{3}}, \frac{\sqrt{5}-\sqrt{3}}{\sqrt{15}}, \frac{\sqrt{5}-2\sqrt{3}}{\sqrt{15}}\right)$$

$$X_4 = a \cdot V - b \cdot W + c \cdot Z \\ = (0.5 \cdot 1, 0.5 \cdot (-1), 0.5 \cdot 0) - (2 \cdot 1, 2 \cdot 1, 2 \cdot 1) \\ + (1.62 \cdot 0, 1.62 \cdot 1, 1.62 \cdot 2) \\ = (0.5, -0.5, 0) - (2, 2, 2) + (0, 1.62, 3.24) \\ = (-1.5, -2.5, -2) + (0, 1.62, 3.24) \\ X_4 = (-1.5, -0.88, 1.24)$$

$$X_5 = ? \\ D = E + X_5 \quad \theta = 45^\circ \\ D = (2, 3) + X_5$$

$$\tan(45^\circ) = \frac{v}{h} \\ 1 = \frac{v}{h} \\ (h, v) = (2, 3) + X_5$$

$$X_5 = (h-2, v-3) \quad h=v=x \\ X_5 = (x-2, x-3)$$

$$D = (1, 1) \\ x=1$$

$$X_5 = (-1, -2) \quad D = (2, 2) \\ x=2$$

donde D es un vector de componentes iguales positivas