

NO:

Date:

Assignment 2. Linear Algebra

Given vectors A, B, C, D, E, F, G perform and sketch the following inner products.

$$A = [2 \ 3] \quad B = [-2, 3] \quad C = [2] \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad D = [2][1] \quad E = [1 \ 2 \ 3]$$

$$F = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} \quad G = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$$

$$\begin{aligned} x_1 &= (A)(C) \\ &= (2 \ 3) \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} \\ &= 2 \cdot 2 + 3 \cdot 3 \\ &= 4 + 9 = 13 \end{aligned}$$

$$\begin{aligned} x_2 &= (A)(D) \\ &= (2 \ 3) (2 \ 1) \\ &= 2(2) + (3)1 \\ &= 4 + 3 \\ &= 7 \end{aligned}$$

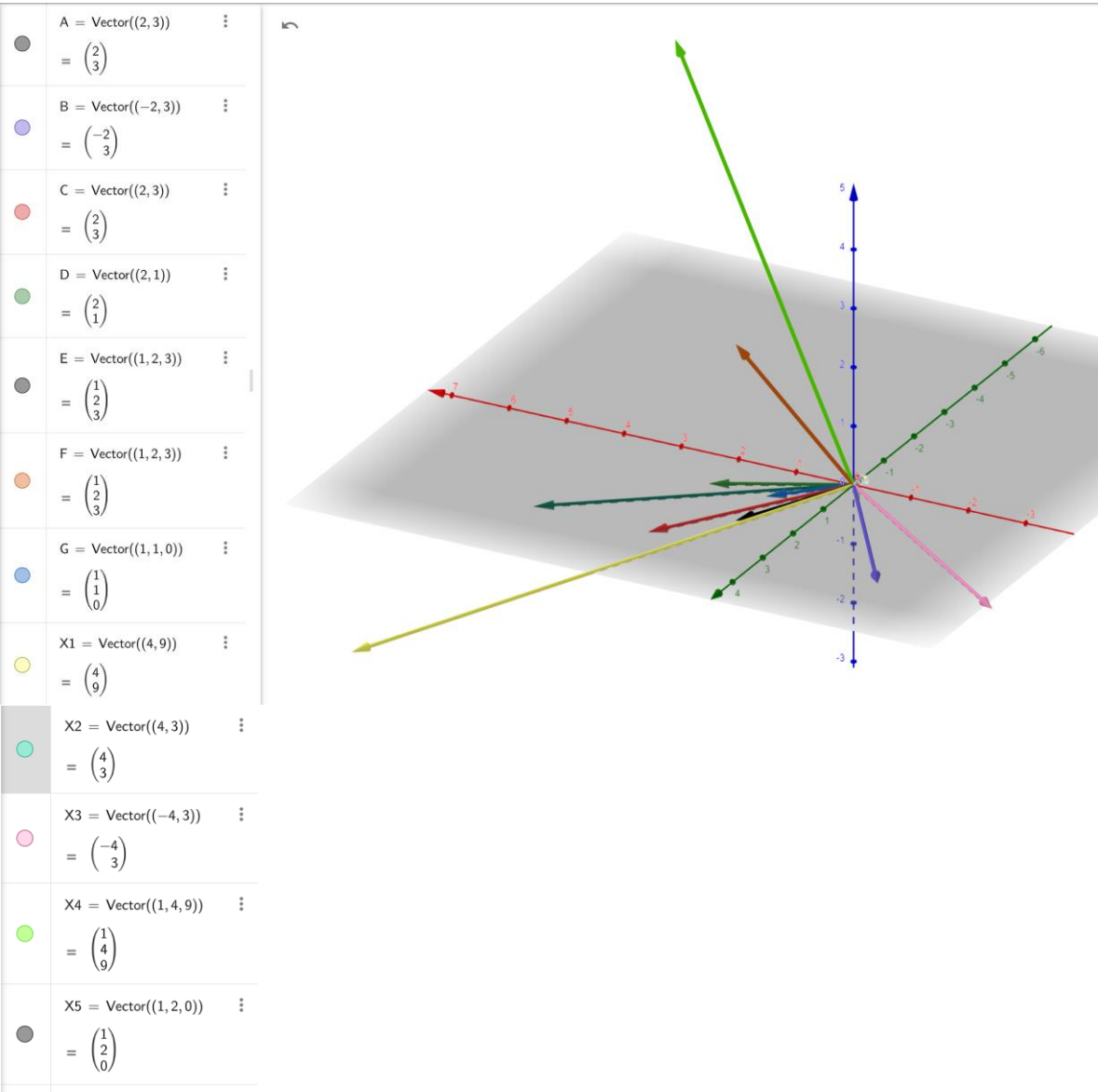
$$\begin{aligned} x_3 &= (B)(C) \\ &= (-2, 3) \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} \\ &= (-2)2 + 3(1) \\ &= -4 + 3 \\ &= -1 \end{aligned}$$

$$\begin{aligned} x_4 &= (E)(F) \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} \\ &= (1 \ 2 \ 3) \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} \\ &= 1(1) + 2(2) + 3(3) \\ &= 1 + 4 + 9 \\ &= 14 \end{aligned}$$

$$\begin{aligned} x_5 &= (E)(G) \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} \\ &= (1 \ 2 \ 3) \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} \\ &= 1(1) + 2(1) + 3(0) \\ &= 1 + 2 + 0 \\ &= 3 \end{aligned}$$

What is x_6 , if $(x_6)(G) = 0$?

G is a matrix of the same length as x_6 full of 0's



NO:

Date:

Given a triangle with vertices A, B, C and the matrices S, M, R , sketch the transformation that results from multiplying each matrix by the three vertices. For instance: $A' = (S)(A), B' = (S)(B), C' = (S)(C)$

$$A = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad B = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad C = \begin{pmatrix} 3 \\ 1 \end{pmatrix} \quad S = \begin{pmatrix} 2 & 0 \\ 0 & 0.5 \end{pmatrix} \quad M = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \quad R = \begin{pmatrix} \cos(a) & -\sin(a) \\ \sin(a) & \cos(a) \end{pmatrix}$$

$$a = 60^\circ$$

$$T = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

$$S \quad A \quad B \quad C = \begin{pmatrix} 2 \cdot 0 + 0 \cdot 0 & 2 \cdot 1 + 0 \cdot 1 & 2 \cdot 3 + 0 \cdot 1 \\ 0 \cdot 0 + 0.5 \cdot 0 & 0 \cdot 1 + 0.5 \cdot 1 & 0 \cdot 3 + 0.5 \cdot 1 \end{pmatrix}$$

$$\begin{pmatrix} 2 & 0 \\ 0 & 0.5 \end{pmatrix} \begin{pmatrix} 0 & 1 & 3 \\ 0 & 1 & 1 \end{pmatrix} = \begin{pmatrix} 0 & 2 & 6 \\ 0 & 0.5 & 0.5 \end{pmatrix}$$

M

$$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} 0 & 1 & 3 \\ 0 & 1 & 1 \end{pmatrix} = \begin{pmatrix} 1 \cdot 0 + 0 \cdot 0 & 1 \cdot 1 + 0 \cdot 1 & 1 \cdot 3 + 0 \cdot 1 \\ 0 \cdot 0 + (-1) \cdot 0 & 0 \cdot 1 + (-1) \cdot 1 & 0 \cdot 3 + (-1) \cdot 1 \end{pmatrix}$$

$$= \begin{pmatrix} 0 & 1 & 3 \\ 0 & -1 & -1 \end{pmatrix}$$

R

$$\begin{pmatrix} \cos 60 & -\sin 60 \\ \sin 60 & \cos 60 \end{pmatrix} \begin{pmatrix} 0 & 1 & 3 \\ 0 & 1 & 1 \end{pmatrix} = \begin{pmatrix} \cos 60 \cdot 0 + (-\sin 60) \cdot 0 & \cos 60 \cdot 1 + (-\sin 60) \cdot 1 & \cos 60 \cdot 3 + (-\sin 60) \cdot 1 \\ \sin 60 \cdot 0 + \cos 60 \cdot 0 & \sin 60 \cdot 1 + \cos 60 \cdot 1 & \sin 60 \cdot 3 + \cos 60 \cdot 1 \end{pmatrix}$$

$$= \begin{pmatrix} 0 & \cos 60 - \sin 60 & 3\cos 60 - \sin 60 \\ 0 & \sin 60 + \cos 60 & 3\sin 60 + \cos 60 \end{pmatrix}$$

$$= \begin{pmatrix} 0 & \frac{1}{2} - \frac{\sqrt{3}}{2} & 3 \cdot \frac{1}{2} - \frac{\sqrt{3}}{2} \\ 0 & \frac{\sqrt{3}}{2} + \frac{1}{2} & 3 \cdot \frac{\sqrt{3}}{2} + \frac{1}{2} \end{pmatrix}$$

$$= \begin{pmatrix} 0 & \frac{1-\sqrt{3}}{2} & \frac{3-\sqrt{3}}{2} \\ 0 & \frac{\sqrt{3}+1}{2} & \frac{3\sqrt{3}+1}{2} \end{pmatrix}$$

T

$$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 0 & 1 & 3 \\ 0 & 1 & 1 \end{pmatrix} = \begin{pmatrix} 0 \cdot 0 + 1 \cdot 0 & 0 \cdot 1 + 1 \cdot 1 & 0 \cdot 3 + 1 \cdot 1 \\ 1 \cdot 0 + 0 \cdot 0 & 1 \cdot 1 + 0 \cdot 1 & 1 \cdot 3 + 0 \cdot 1 \end{pmatrix}$$

$$= \begin{pmatrix} 0 & 1 & 1 \\ 0 & 1 & 3 \end{pmatrix}$$

Black: Original Triangle

Green: S

Red: M

Purple: T

