

Question 1

a. $\text{isrc} \rightarrow \text{mln}$

$\text{isrc} \rightarrow \text{artist, genre}$	1. Assumption
$\text{isrc, msin} \rightarrow \text{artist, genre, msin}$	2. Augmentation of (1)
$\text{isrc, msin} \rightarrow \text{msin}$	3. Decomposition of (2)
$\text{msin} \rightarrow \text{mln, inst}$	4. Assumption
$\text{msin} \rightarrow \text{mln}$	5. Decomposition of (4)
$\text{isrc, msin} \rightarrow \text{mln}$	6. Transitivity of (3)(5)

The functional dependency is **not** implied by F because there does not exist a valid axiom to reduce equation 6.

b. $\text{isrc, rep} \rightarrow \text{enddate}$

$\text{artist, label} \rightarrow \text{enddate, rep}$	1. Assumption
$\text{rep} \rightarrow \text{label}$	2. Assumption
$\text{artist, rep} \rightarrow \text{artist label}$	3. Augmentation of (2)
$\text{artist, rep} \rightarrow \text{enddate, rep}$	4. Transitivity of (1)(3)
$\text{isrc} \rightarrow \text{artist, genre}$	5. Assumption
$\text{isrc} \rightarrow \text{artist}$	6. Decomposition of (5)
$\text{isrc, rep} \rightarrow \text{enddate, rep}$	7. Pseudotransitivity of (6)(4)
$\text{isrc, rep} \rightarrow \text{enddate}$	8. Reflexivity of (7)

c. label, msin, artist -> inst, mfn, rep

artist, label -> enddate, rep	1. Assumption
artist, label -> rep	2. Decomposition of (1)
msin -> mln, inst	3. Assumption
artist, label, msin -> msin, enddate, rep	4. Augmentation of (1)
artist, label, msin -> msin	5. Decomposition of (4)
msin -> mln, inst	6. Assumption
msin -> inst	7. Decomposition of (6)
msin, mln -> msin, mfn	8. Assumption
msin, msin -> msin, mfn	9. Pseudotransitivity of (6)(8)
msin -> mfn	10. Reverse augmentation of (9)
artist, label, msin -> rep	11. Decomposition of (4)
artist, label, msin -> mfn	12. Transitivity of (5)(10)
artist, label, msin -> inst	13. Transitivity of (5)(7)
label, msin, artist -> inst, mfn, rep	14. Union of (11)(12)(13)

d. wsin, artist -> genre, royalty

wsin -> wfn, wln	1. Assumption
wsin, artist -> artist, wfn, wln	2. Augmentation of (1)
wsin, artist -> artist	3. Decomposition of (2)
artist -> members, genre	4. Assumption

artist \rightarrow genre

5. Decomposition of (4)

wsin, artist \rightarrow genre

6. Transitivity of (3)(5)

wsin, artist, royalty \rightarrow genre, royalty

7. Augmentation of (6)

wsin, artist \rightarrow genre, royalty

8. Reflexivity of (7)

Question 2

- a. What is the attribute closure of (msin, wsin)?

$(\text{msin}, \text{wsin})^+ = \text{msin}, \text{wsin}, \text{mln}, \text{inst}, \text{mfn}, \text{wfn}, \text{wln}$

- b. What is the attribute closure of (isrc, label)?

$(\text{isrc}, \text{label})^+ = \text{isrc}, \text{label}, \text{lcity}, \text{lcountry}, \text{artist}, \text{genre}, \text{members}, \text{title}, \text{album}, \text{enddate}, \text{rep}, \text{year}$

- c. Identify a minimal superkey for the entire set of attributes, R?

Minimal superkey: isrc, wsin, msin, rep

Question 3

Compute F_c (the canonical cover of F)

Original list of dependencies:

artist \rightarrow members, genre

msin \rightarrow mln, inst

msin, ~~mln~~ \rightarrow msin, mfn

$\{\text{msin}\}^+$ includes all the attributes on the left

isrc, title, album, artist -> syear	{isrc} ⁺ includes year; union with other isrc
isrc, artist -> title, album, artist, genre, syear	{isrc} ⁺ includes title, album; union added
artist, label -> enddate, rep	
rep -> label	
label -> lcity, lcountry	
isrc, wsin, title -> royalty, title, album	{isrc, wsin} ⁺ includes attributes on left
wsin -> wfn, wln	
isrc -> artist, genre	union with other isrc

Canonical Cover:

**Fc = {artist -> members, genre; msin -> mln, inst, mfn; isrc -> syear, artist, title, album, genre;
artist, label -> enddate, rep; rep -> label; label -> lcity, lcountry; isrc, wsin -> royalty; wsin ->
wfn, wln}**

Question 4

- a. lossless join decomposition

Yes

- b. dependency preservation

Yes

- c. BCNF

Yes, because all X's are superkeys for their corresponding relation R.

- d. 3NF

Yes, because it satisfies the conditions for BCNF, therefore will also satisfy conditions for 3NF.

Question 5

- a. lossless join decomposition

Yes

- b. dependency preservation

Yes

- c. BCNF

No, not in BCNF because isrc in isrc \rightarrow artist, genre is not a superkey for the song relation.

- d. 3NF

No, schema is not in 3NF because artist in artist \rightarrow members is not a superkey for the artist relation, nor is $(Y - X)$ contained in a candidate key for the artist relation.

Question 6

- a. lossless join decomposition

No, schema is **not** lossless because the musicians' relation does not intersect with any other relation in the schema.

- b. dependency preservation

Yes

- c. BCNF

Yes, because all X's are superkeys for their corresponding relation R.

- d. 3NF

Yes, because it satisfies the conditions for BCNF, therefore will also satisfy conditions for 3NF.