

# Genomes and their variation

Biol 5221

January 18, 2024

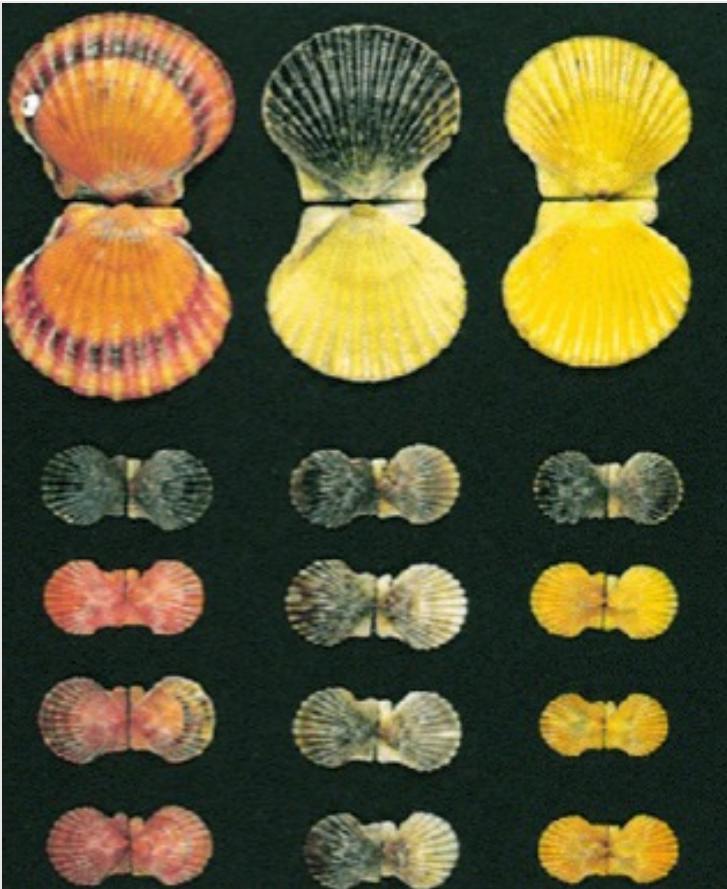
Hancock



# What is population genetics?

- Population genetics is the study of genetic variation within and between populations
- Studying genetic variation in present-day populations allows us to learn about the history of populations, genetic variants and traits and to predict the future
- We will often make simplifying assumptions, but simple models turn out to be powerful to make inferences, and future studies can build on these simple models

# Some questions

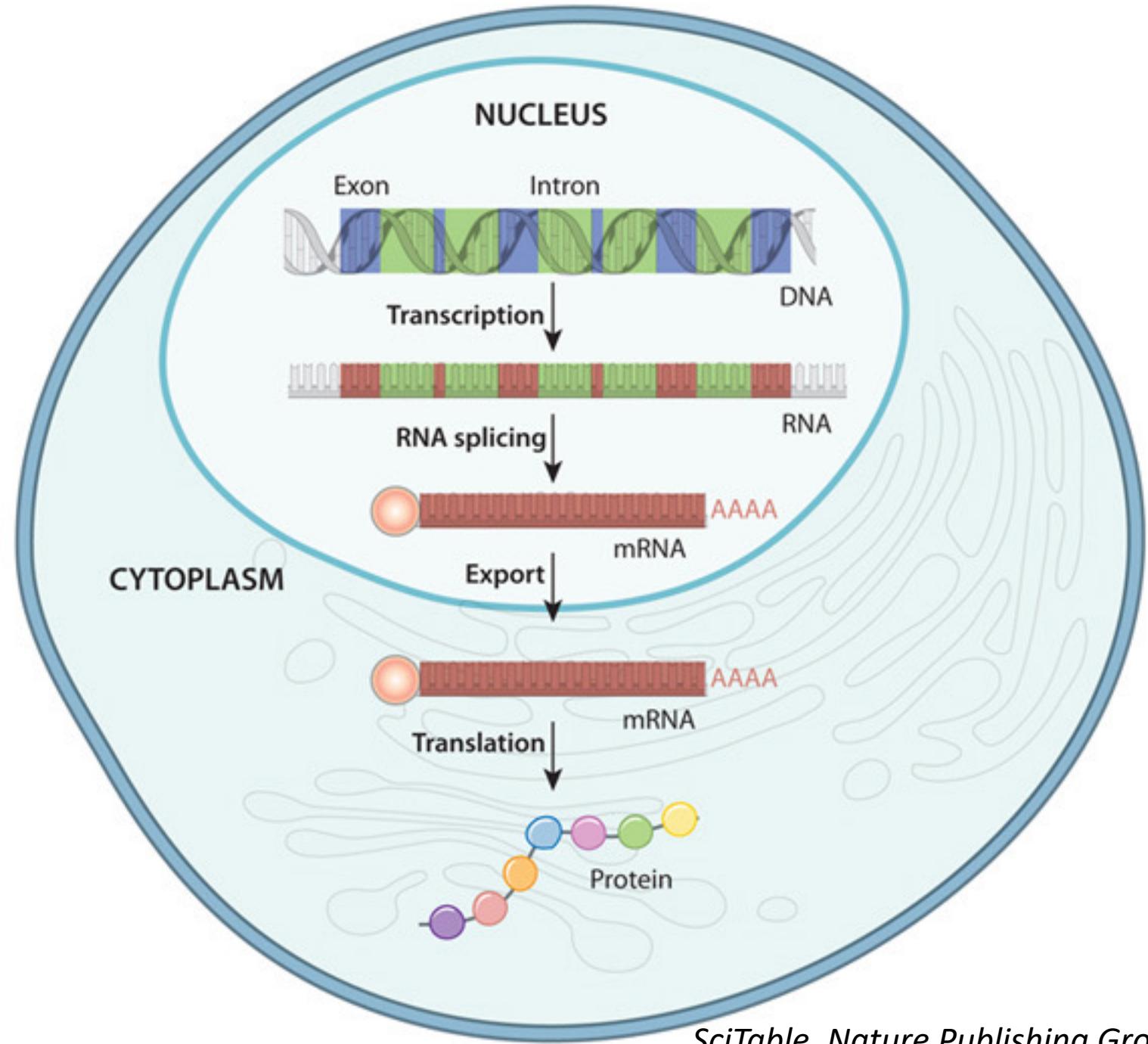


- *How can we assay genetic variation?*
- *What can we learn from genetic variation?*
- *What scientific and practical questions can we address using population genetic variation?*

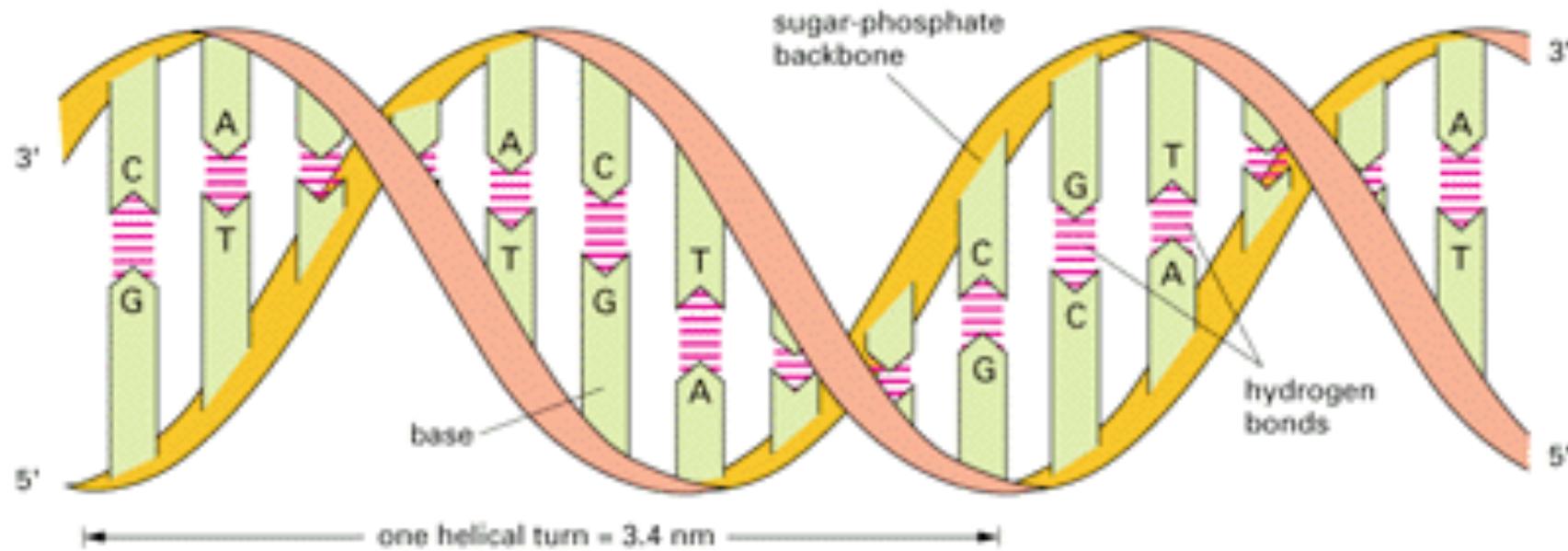
# Levels of regulation from DNA to protein

Not all DNA changes are equivalent!

Context matters!



# We will study variation at the DNA level



This variation may affect coding sequencing, regulatory sequences or it may have no effect on traits

# The standard genetic code

Synonymous mutations are mutations that occur in a protein coding region that do not change the amino acid

Non-synonymous mutations are mutations that occur in a protein coding region that do change the amino acid

		Second letter					
		U	C	A	G		
		UUU UUC UUA UUG	UCU UCC UCA UCG	UAU UAC UAA UAG	UGU UGC UGA UGG		
First letter	U	Phe	Ser	Tyr Stop	Cys Stop	U C	A G
	C	Leu	Pro	His Gln	Arg	U C	A G
	A	Ile Met	Thr	Asn Lys	Ser Arg	U C	A G
	G	Val	Ala	Asp Glu	Gly	U C	A G
Third letter							

# Types of genetic variation we study reflect available technology

- Protein polymorphisms (using gel electrophoresis)
- RFLPs, microsatellites
- Single nucleotide variants (SNPs)
- Structural variants large and small
  - Indels
  - Large deletions
  - Tandem duplications
  - Inversions

Was the only method available before the DNA sequencing revolution

Most studies over the past 20 years have used these

SMRT-cell “long-read” data enables high quality genotyping of these

# Types of variants

Single nucleotide  
Polymorphism (SNP)

ATGGACCTCA**G**CTAGCTTAAG  
ATGGACCTCA**A**CTAGCTTAAG

Simple sequence repeats  
(micro- and minisatellites)

ATGGACCTCA**CACACAC**CTAGCTTAAG  
ATGGACCTCA**CACACACAC**CTAGCTTAAG

Insertion-deletion  
polymorphism (indel)

ATGGACCTCAC**TGAG**CTAGCTTAAG  
ATGGACCTCAC**---**CTAGCTTAAG

Block substitution

ATGGACCT**CACG**CTAGCTTAAG  
ATGGACCT**TGAA**CTAGCTTAAG

Inversion variant

ATGGACCT**CACGCTA**GCTTAAG  
ATGGACCT**TAGCGTG**GCTTAAG

Copy number variant (CNV)

ATGGACCT**CACTGGACCTCAC**CTAGCTTAAG  
ATGGACCT**CAC-----**CTAGCTTAAG

Segmental duplications



Translocations

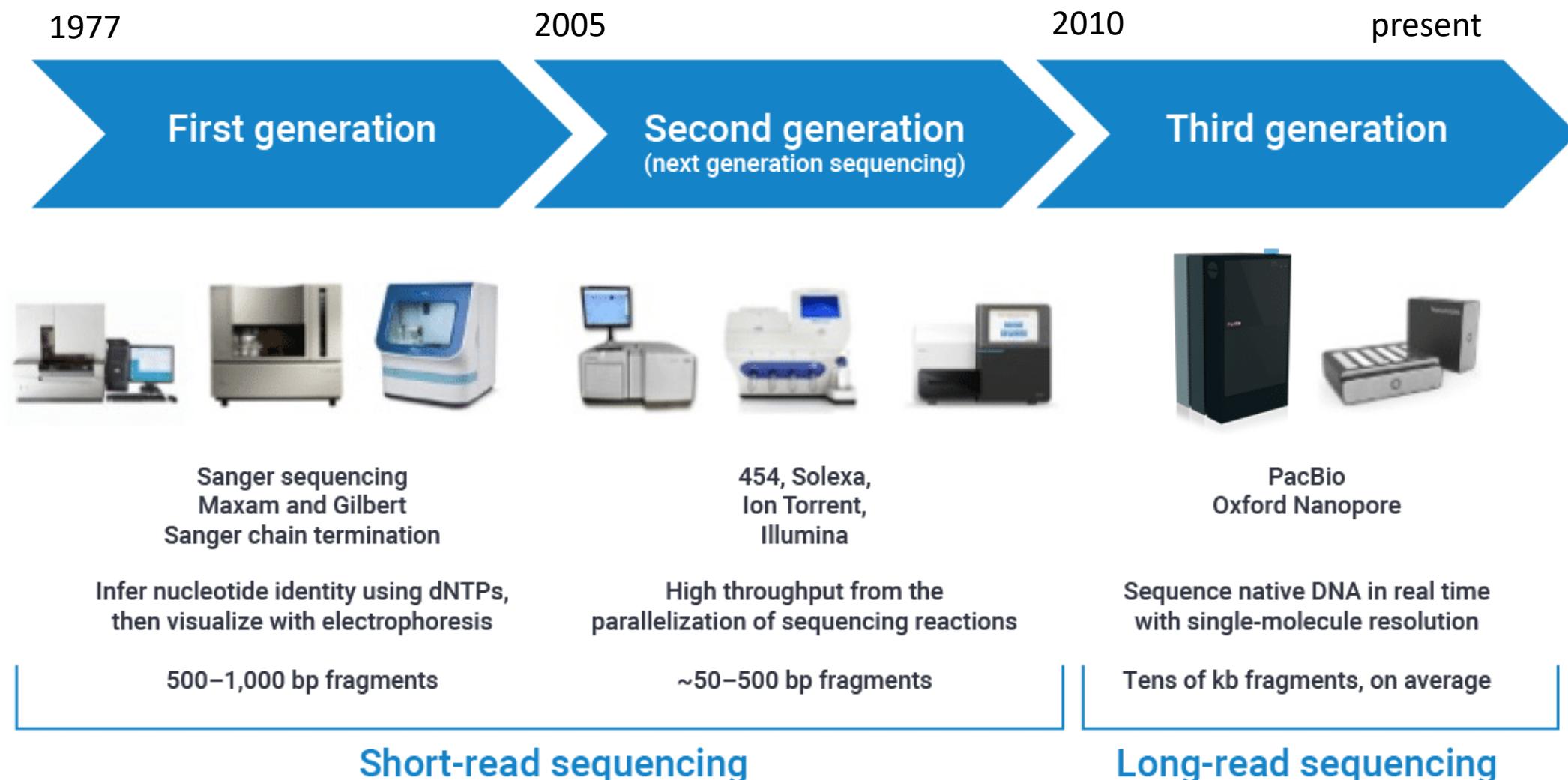


Structural variants

# Major landmarks in population genetics and genomics

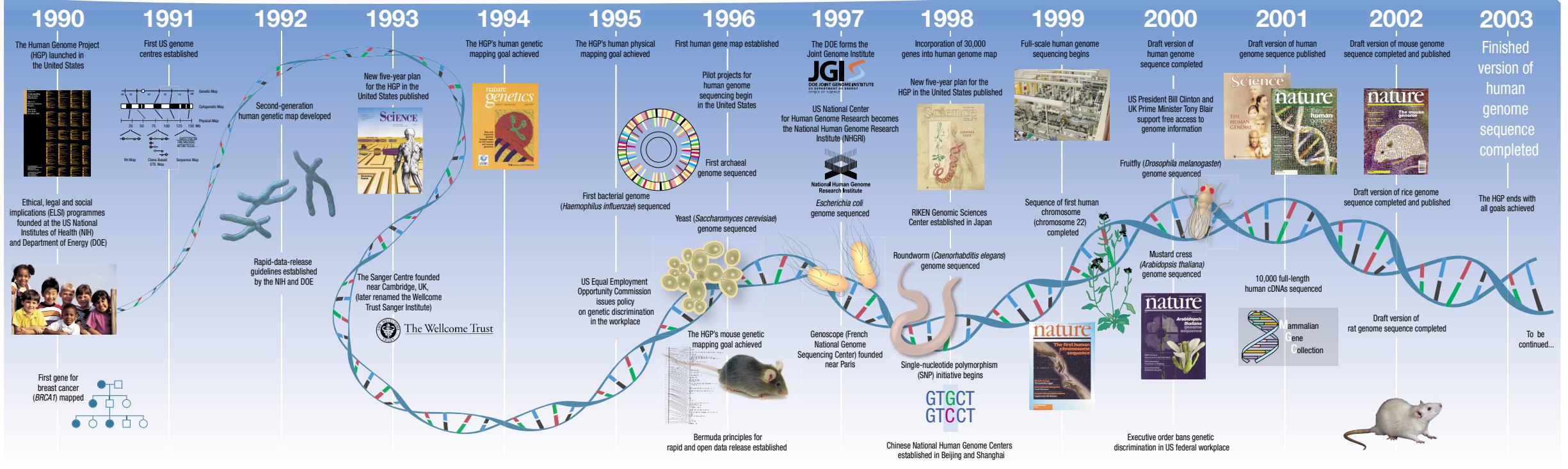
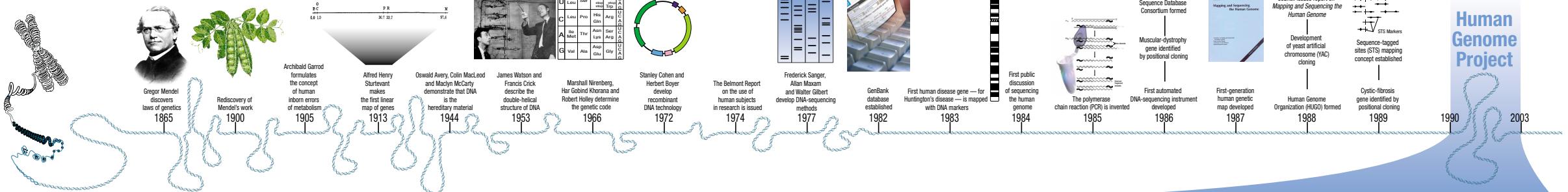
- Mendel's work showing how inheritance at the trait level could work through individual units, later termed "genes"
- Discovery of the structure of DNA
- Central Dogma: DNA-> RNA, RNA -> protein
- Assaying variation within a species using protein electrophoretic markers (Lewontin and Hubby, 1966)
- Assaying DNA sequence variation within a species (Kreitman 1983)
- Studies of variation using microsatellites
- Studies of DNA sequence of candidate genes and 'neutral' controls across genomes
- SNP-chips (genome-wide or partial genome-wide)
- Whole genome short-read sequencing
- Whole genome-long read sequencing (single-molecule real-time (SMRT) sequencing)

# Timeline of sequencing technology



# The Human Genome Project

## Landmarks in genetics and genomics



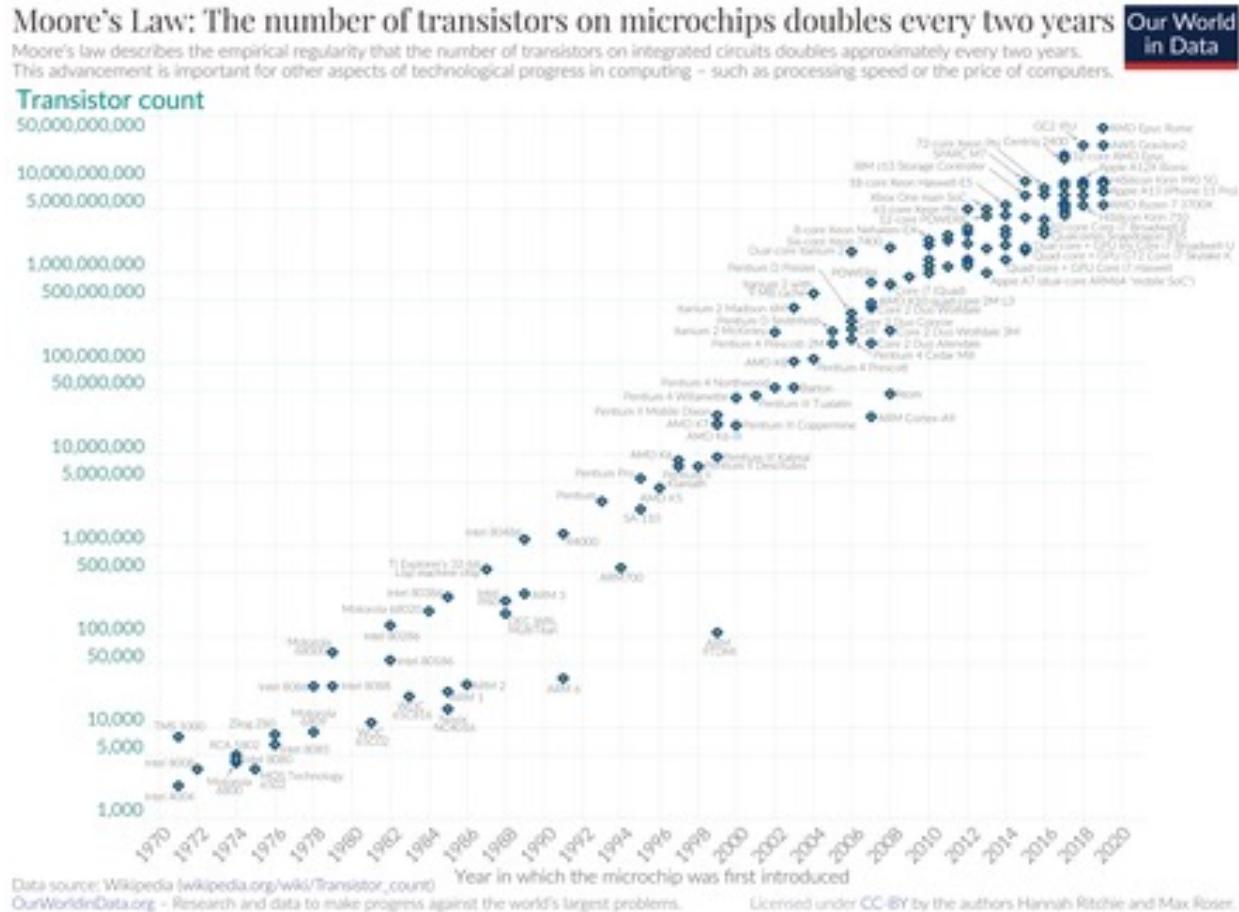
Source and more info: <https://www.genome.gov/human-genome-project>

<https://geneticsunzipped.com/blog/2020/10/22/s322-the-past-present-and-future-of-the-human-genome-project>

# A summary of the structure of the human genome

- *Genome size: 3.1 Gb (haploid size).*
- *Number of chromosomes: 23 pairs*
- *Number of coding genes: ~20, 000*
- *Exons per gene: 8 (median)*
- *Number of genes per megabase: 6.5 (mean)*
- *Total in protein-coding exons: 1% of genome*
- *Total in genes (introns+exons): 40% of genome*
- *Active chromatin (per cell type): 1% of genome*
- *Active chromatin (all cell types): 13% of genome*

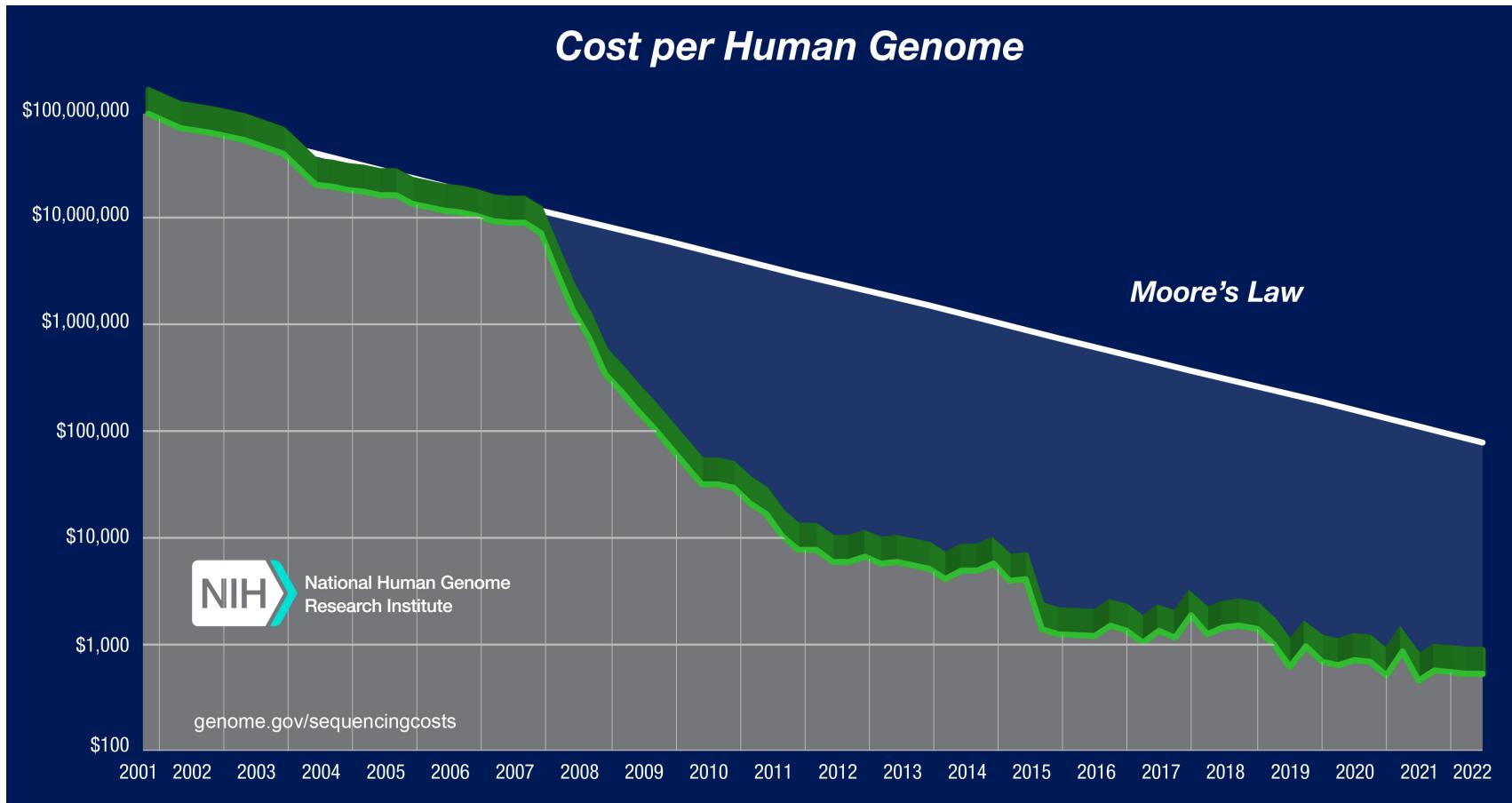
# Moore's law posits that manufacturing costs for semi-conductors should fall exponentially over time



Gordon Moore, projected that the ideal number of transistors per square inch on a microchip would double each year while the manufacturing cost per component would halve.

Moore's law has since been widely applied to diverse technologies

Since 2007, with “next generation sequencing” the cost reduction per human genome has outpaced Moore’s law



# Scale of sequencing in human populations

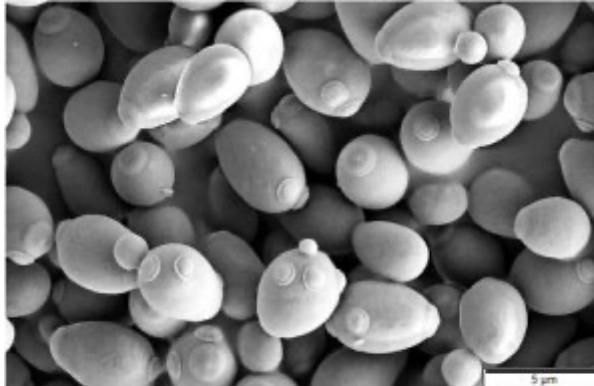
- Human Genome Project (1 reference sequence built from 4 individuals)
- Population genomics aimed at assaying diversity across worldwide populations
  - HapMap Project (90 CEPH, 90 CHN, 90 YRI)
  - Human Genome Diversity Panel
  - 1000 Genomes Project assays diversity across worldwide populations
- Population genomics aimed at trait mapping
  - Wellcome Trust (WTCCC) 14K cases, 3K shared controls
  - UK Biobank 500K individuals
  - AllofUs Research Program -> goal: health + genomic data for 1M+ US citizens

# Comparative genomics and comparative population genomics

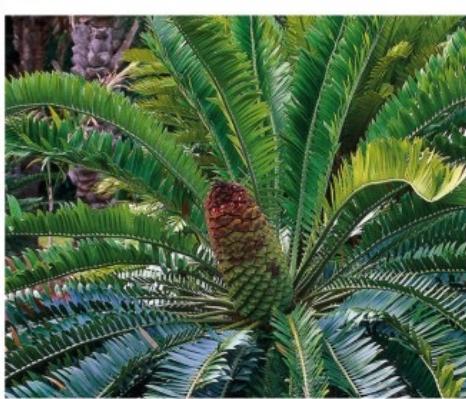
The Human Genome Project also provided funding for sequencing other species. **Why?**

- Comparative genomics not only helps us to understand other genomes, but also our own
- Identifying non-coding loci that are deeply conserved is useful to annotate likely functional regions
- Regions that evolve relatively rapidly over phylogenetic time scales may be involved in adaptation
- Experiments in model organisms, which would not be possible in humans, can connect genetic variation to functional variation

# Genomes projects in model organisms examine variation across the species distribution



# 10,000 plant genomes aims to assay diversity across species



- Plants make up the majority of biomass on Earth
- Plants are directly exposed to their environments, making adaptation especially important (***plants can't hide from the elements!***)
- Plants have high variation in genome size, chromosome number and diversity



# The Zoonomia Project

**Aims to identify the genetic basis for shared and distinct traits across animals**

## Publications:

Christmas et al. Evolutionary constraint and innovation across hundreds of placental mammals

<https://www.science.org/doi/10.1126/science.abn3943>

Sullivan et al. Leveraging base pair mammalian constraint to understand genetic variation and human disease

<https://www.science.org/doi/10.1126/science.abn2937>

Andrews et al. Mammalian evolution of human cis-regulatory elements and transcription factor binding sites

<https://www.science.org/doi/10.1126/science.abn7930>

Foley et al. A genomic timescale for placental mammal evolution

<https://www.science.org/doi/10.1126/science.abl8189> Kaplow et al. Relating enhancer genetic variation across mammals to complex phenotypes using machine learning

<https://www.science.org/doi/10.1126/science.abm7993>

Keough et al. Three-dimensional genome re-wiring in loci with human accelerated regions

<https://www.science.org/doi/10.1126/science.abm1696>

Kirilenko et al. Integrating gene annotation with orthology inference at scale

<https://www.science.org/doi/10.1126/science.abn5887>

Osmanski et al. Insights into mammalian TE diversity via the curation of 248 mammalian genome assemblies

<https://www.science.org/doi/10.1126/science.abn1430>

Wilder et al. The contribution of historical processes to contemporary extinction risk in placental mammals

<https://www.science.org/doi/10.1126/science.abn5856>

Xue et al. The functional and evolutionary impacts of human-specific deletions in conserved elements

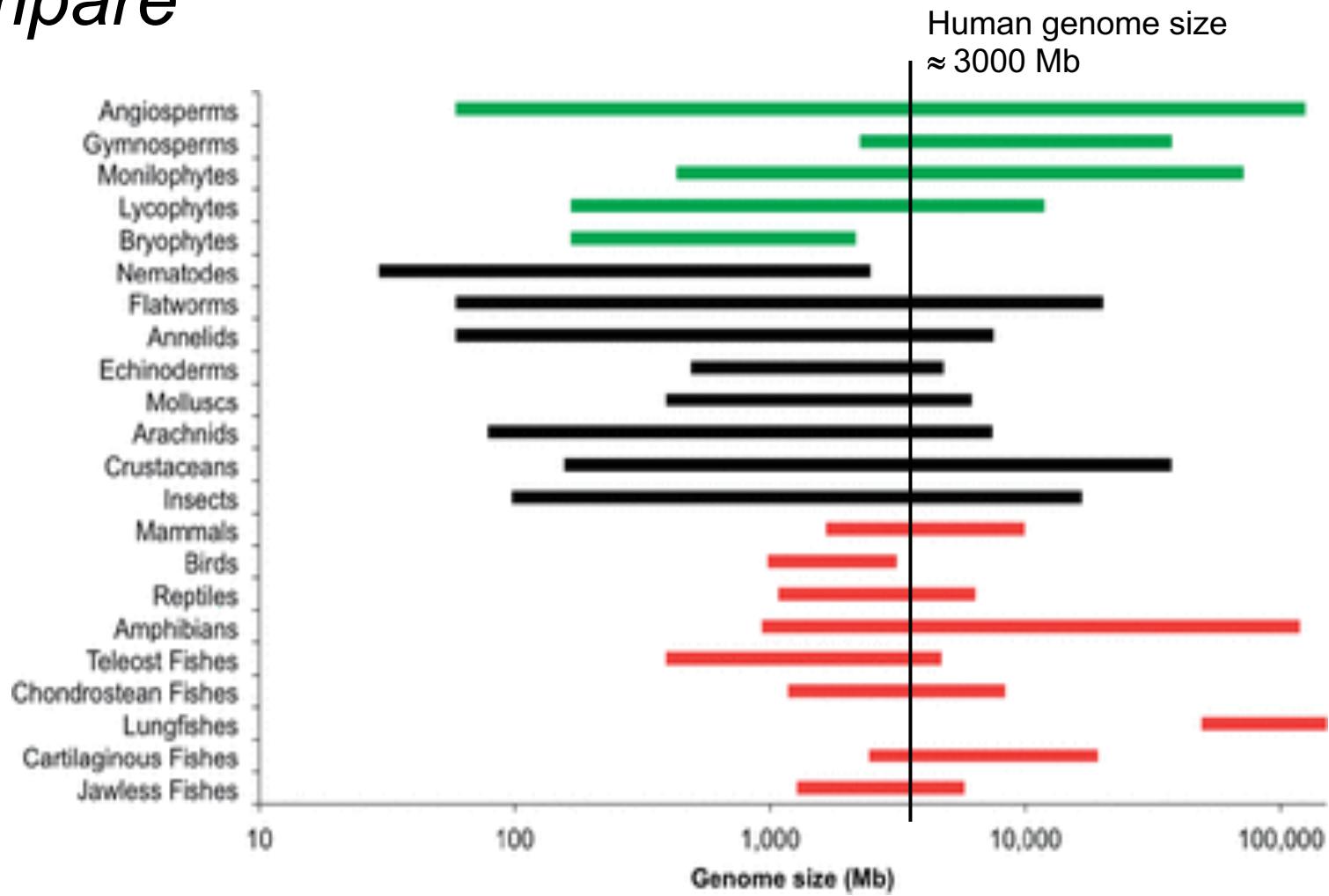
<https://www.science.org/doi/10.1126/science.abn2253>

How does the human genome  
compare to others?

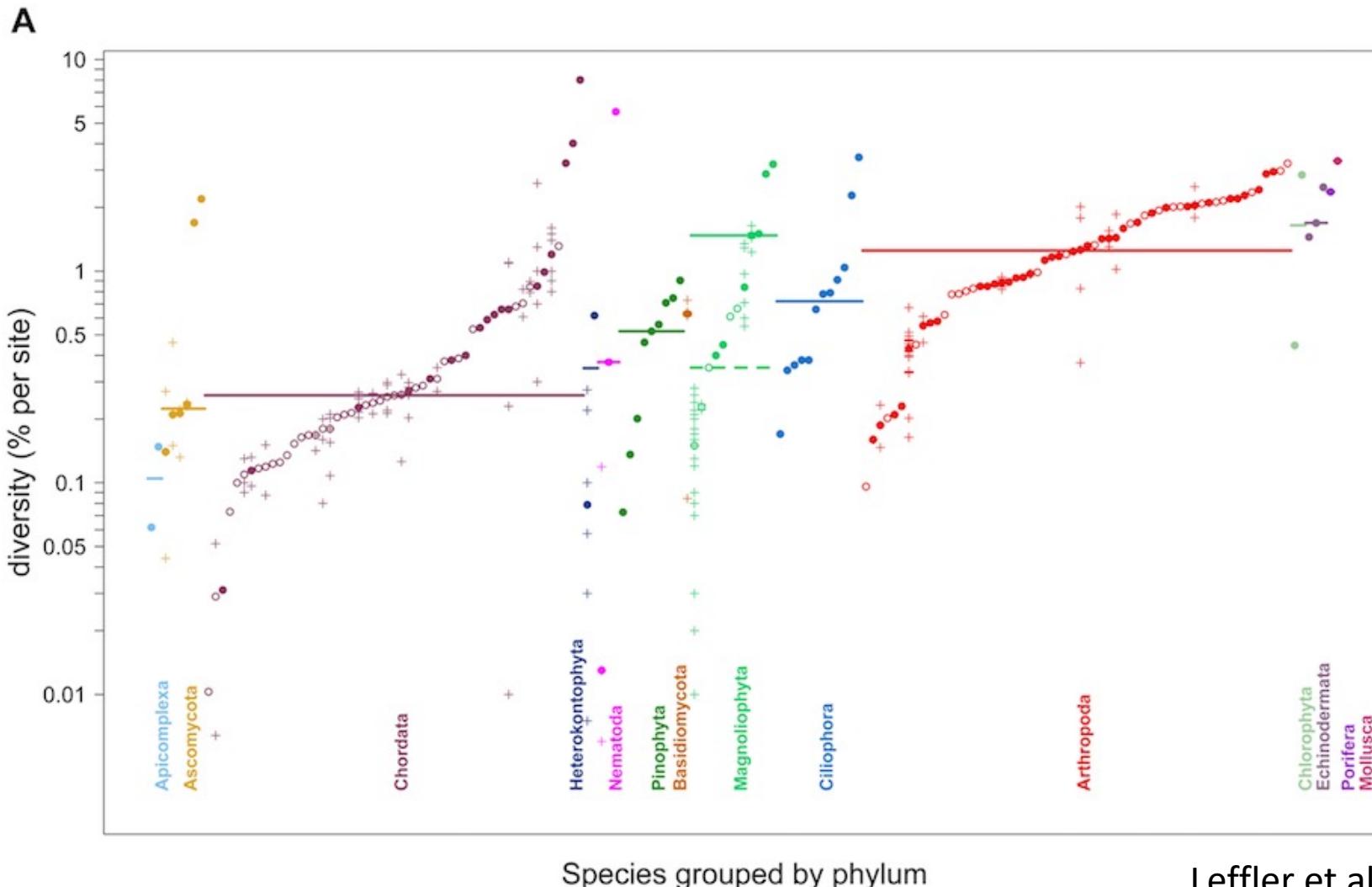
# *How does the size of the human genome compare with other species?*

Four orders of magnitude of variation in genome size

Humans are not outliers for genome size!



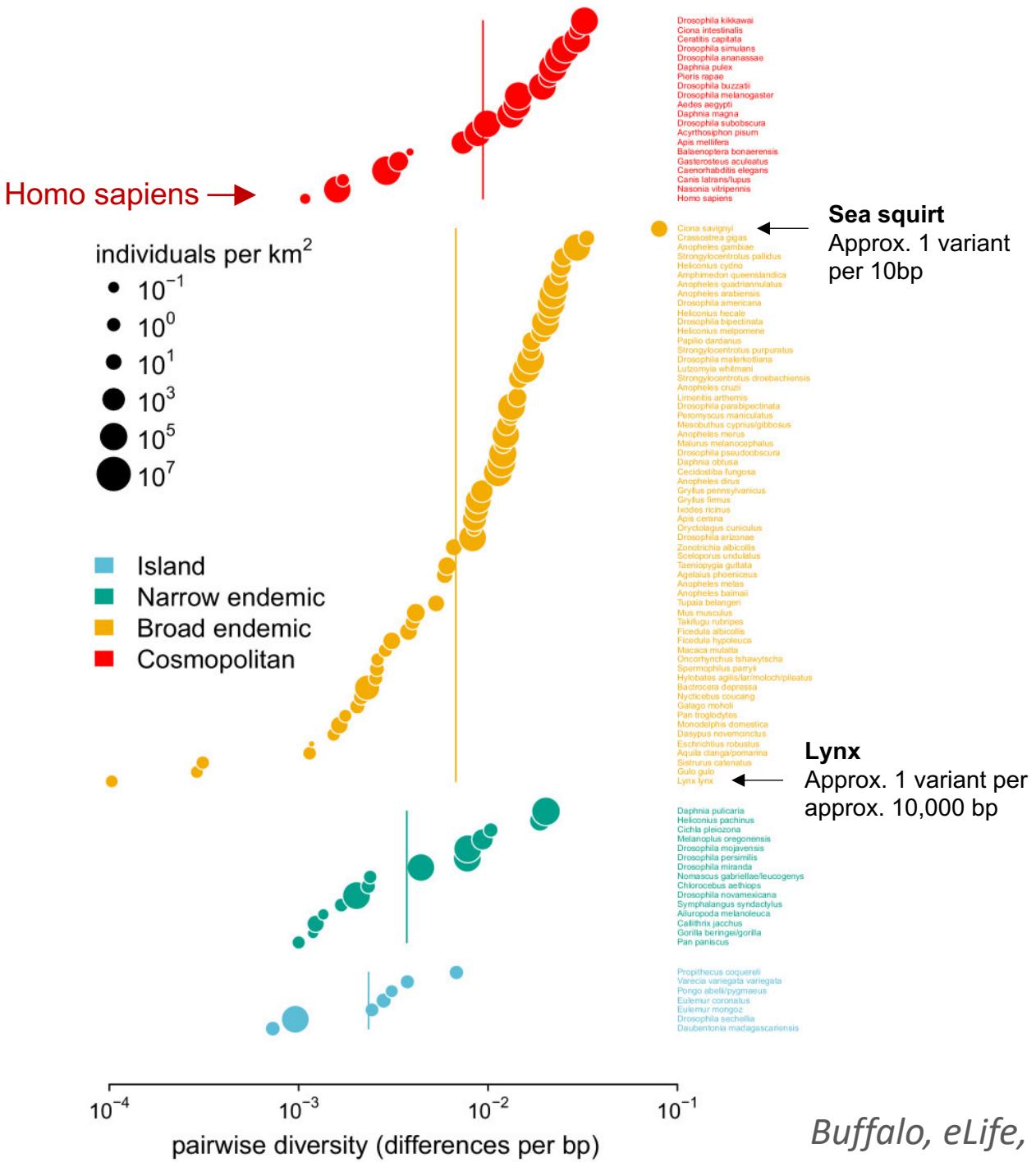
# Diversity varies widely across species



# Can census size explain variation in diversity?



# Differences in census population size explain some of the variation in diversity

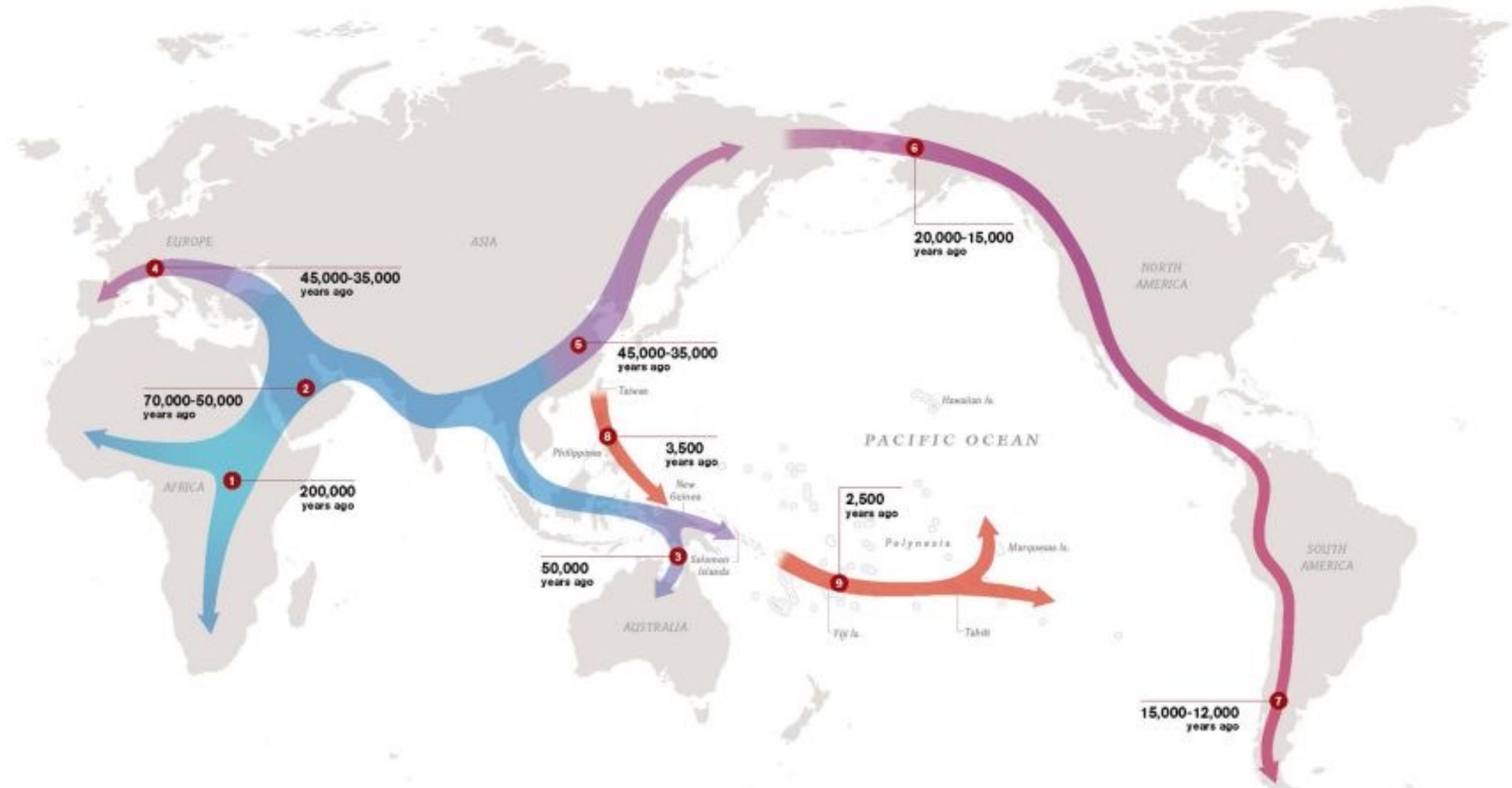


Some applications of  
population and quantitative  
genetics/genomics

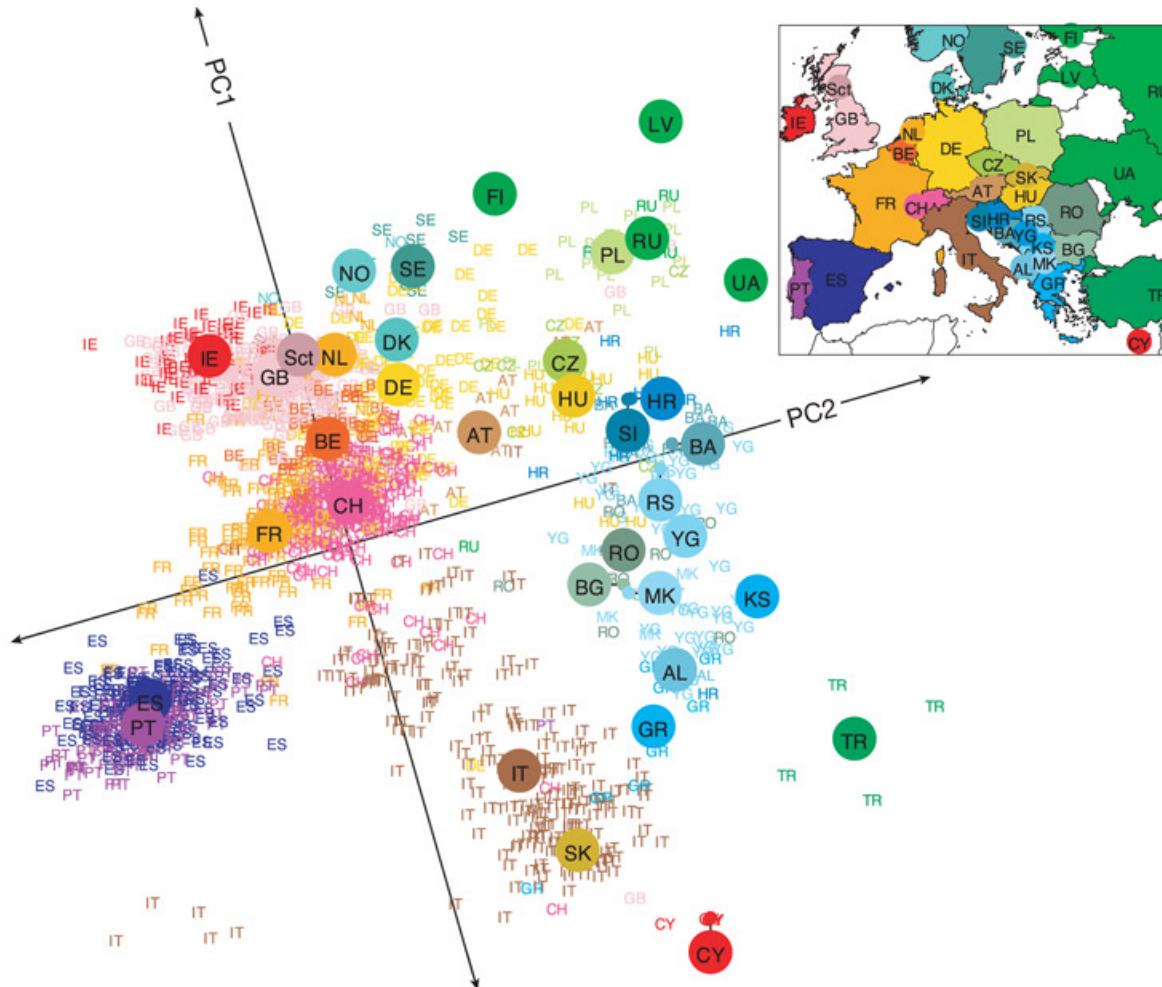
# Applications of population genetics

- Estimate diversity in populations
- Reconstruct evolutionary history and predict future evolvability
- Understand the evolutionary mechanisms that act on variation
- Understand the processes of local adaptation and speciation
- Trait mapping and personal genomics
- DNA fingerprinting – tracking individuals/forensics
- Conservation

# Reconstructing historical relationships



# Genetics recapitulates geography in population samples from Europe

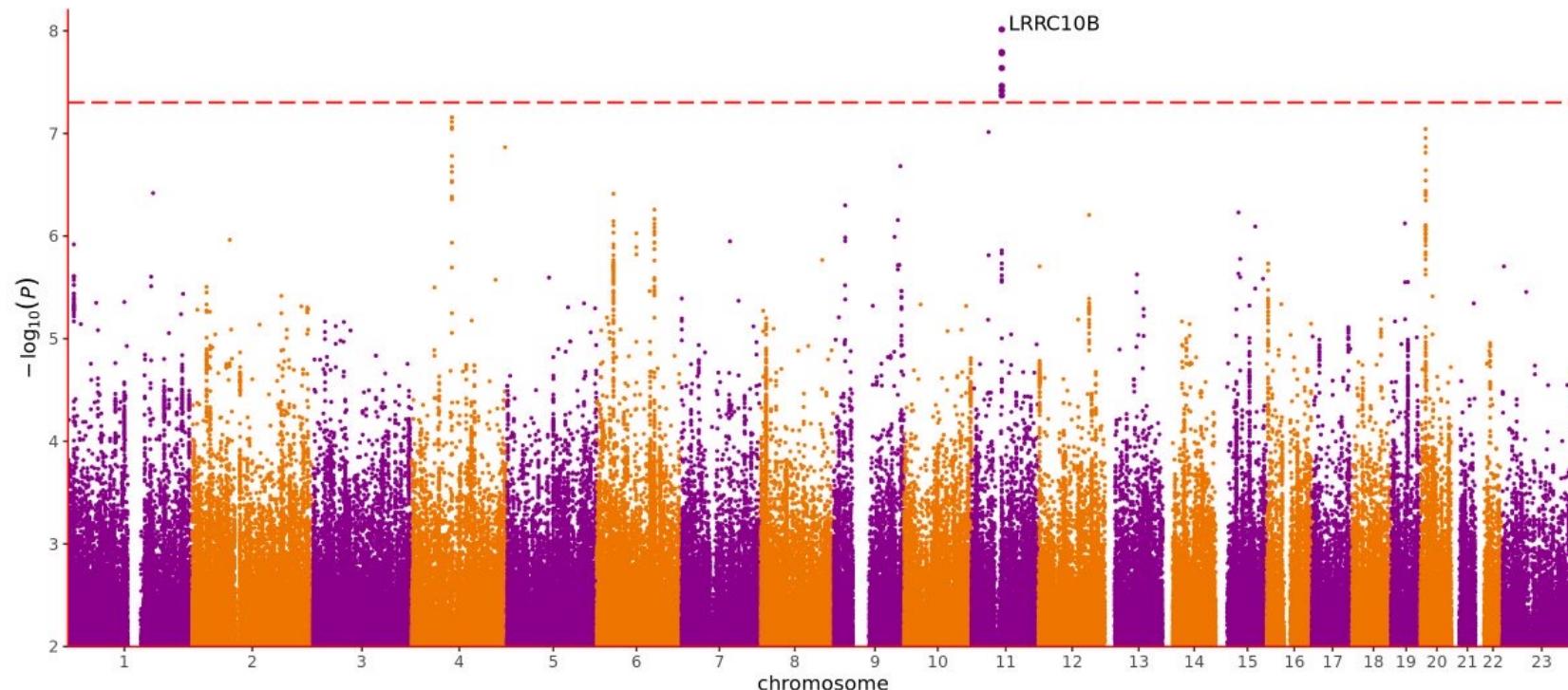


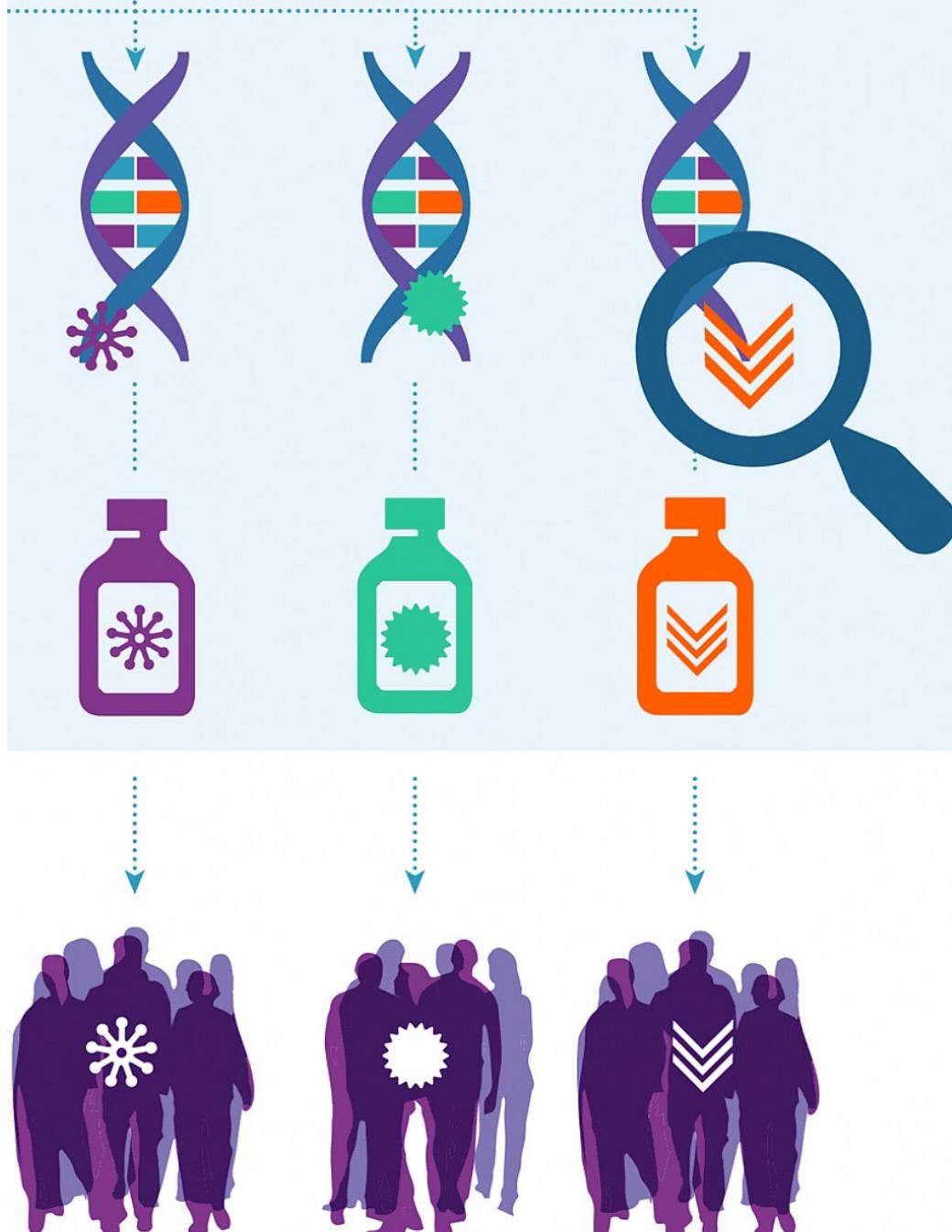
First two principal components derived from a matrix of SNP genotypes across a sample of Europeans

The resulting pattern is similar to the map of locations of origin

# Trait mapping

**Loci associated with diastolic blood pressure variation in the UK Biobank population sample**





# Precision medicine

## Goals:

- To understand genetic and environmental risk factors for human disease
- To learn which treatments work best for people of different backgrounds
- To precision medicine aims to improve treatment to take into account a person's specific genetic and environmental differences

# Precision agriculture and resilience

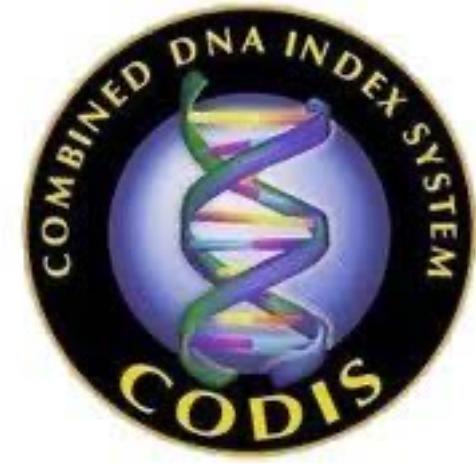


Understanding how plant populations have adapted to extreme climates can provide insights into how to improve resilience in crops

# Forensics



Source: HudsonAlpha.org



Genomics is establishing more robust methods for DNA-based forensic analyses

# Conservation



Understanding the amount and spatial distribution of variation within threatened species can inform conservation strategies

# Timeline of population genetic/genomics

- Mendel's work showing how inheritance at the trait level could work; connected to "genes", which were abstract constructs
- Discovery of the structure of DNA: Watson, Crick and Wilkens received the Nobel prize from work that was inspired by a photo by Rosalind Franklin
- DNA-> RNA -> protein
- Assaying variation using protein electrophoretic markers
- **First study of DNA sequence variation within a species (Kreitman 1983)**
- Studies of variation using microsatellites
- Studies of DNA sequence of candidate genes and 'neutral' controls across genomes
- SNP-chips (genome-wide or partial genome-wide)
- Whole genome short-read sequencing
- Whole genome-long read sequencing (single-molecule real-time (SMRT) sequencing)

*Time flies like an arrow, a fruit fly likes a banana\**



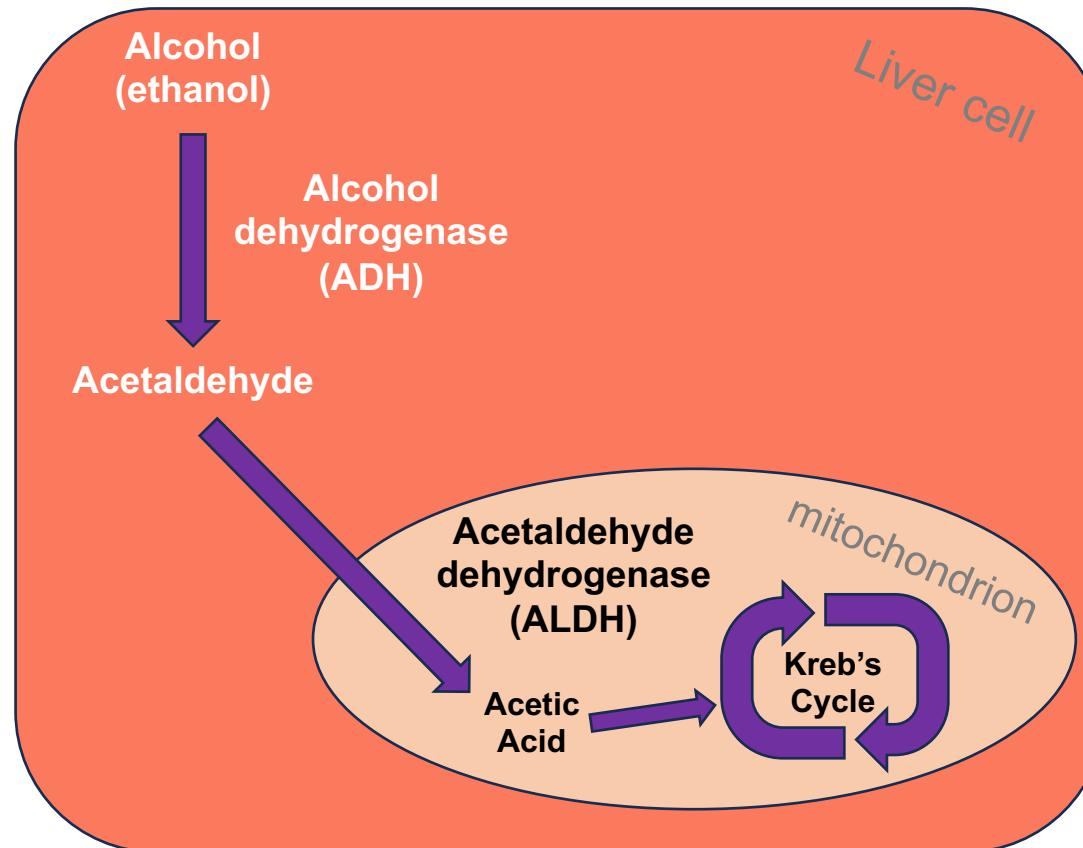
But aging bananas contain high levels of ethanol!

\*attributed to Groucho Marx, but this is questionable

# Alcohol is metabolized using two enzymes: ADH and ALDH

ADH breaks alcohol down into acetaldehyde, representing the first step of alcohol metabolism

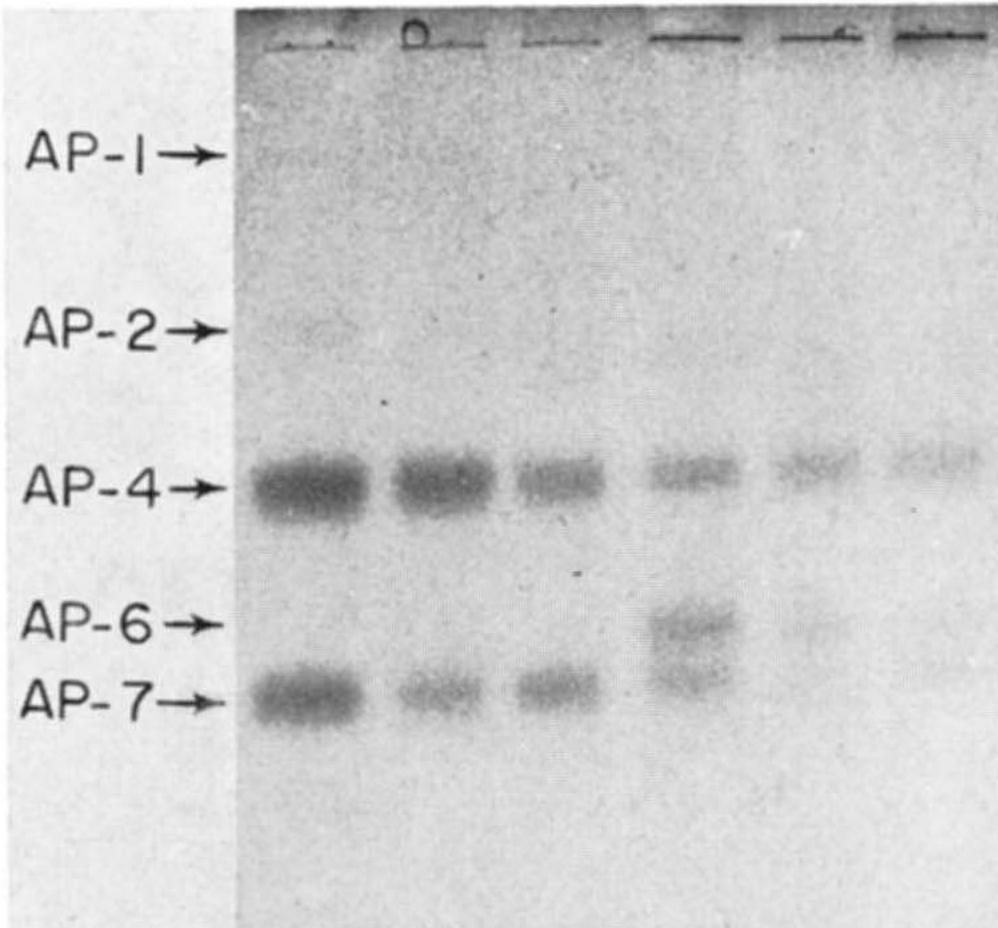
In a second step, ALDH breaks acetaldehyde into acetic acid



Two alleles segregate in *Drosophila melanogaster*: a **fast** (*Adh-f*) and a **slow** (*Adh-s*) metabolizing allele

The fast allele is encoded by a Thr → Lys amino acid replacement

# The standard way to assay variation was using protein electrophoresis gels



The rate at which a protein moves through the gel depends on its electrostatic charge.

Protein variation could be assayed across a set of individuals, as in this gel showing different alkaline phosphatase proteins in *Drosophila pseudoobscura* samples.

Lewontin and Hubby, Genetics, 1966

# In the 1980's Church and Gilbert were working out an approach to sequence DNA

*Proc. Natl. Acad. Sci. USA*  
Vol. 81, pp. 1991–1995, April 1984  
Biochemistry

## Genomic sequencing

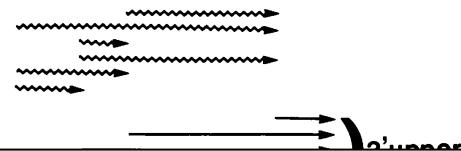
(DNA methylation/UV crosslinking/filter hybridization/immunoglobulin genes)

GEORGE M. CHURCH\* AND WALTER GILBERT\*†

\*Biological Laboratories, Harvard University, Cambridge, MA 02138; and †Biogen, Inc., 14 Cambridge Center, Cambridge, MA 02142

*Contributed by Walter Gilbert, December 19, 1983*

**ABSTRACT** Unique DNA sequences can be determined directly from mouse genomic DNA. A denaturing gel separates by size mixtures of unlabeled DNA fragments from complete restriction and partial chemical cleavages of the entire genome.



Marty Kreitman, a student in Dick Lewontin's lab thought it would be interesting to look at variation within a species at the DNA sequence level

# *Adh* gene variation in *D. melanogaster*

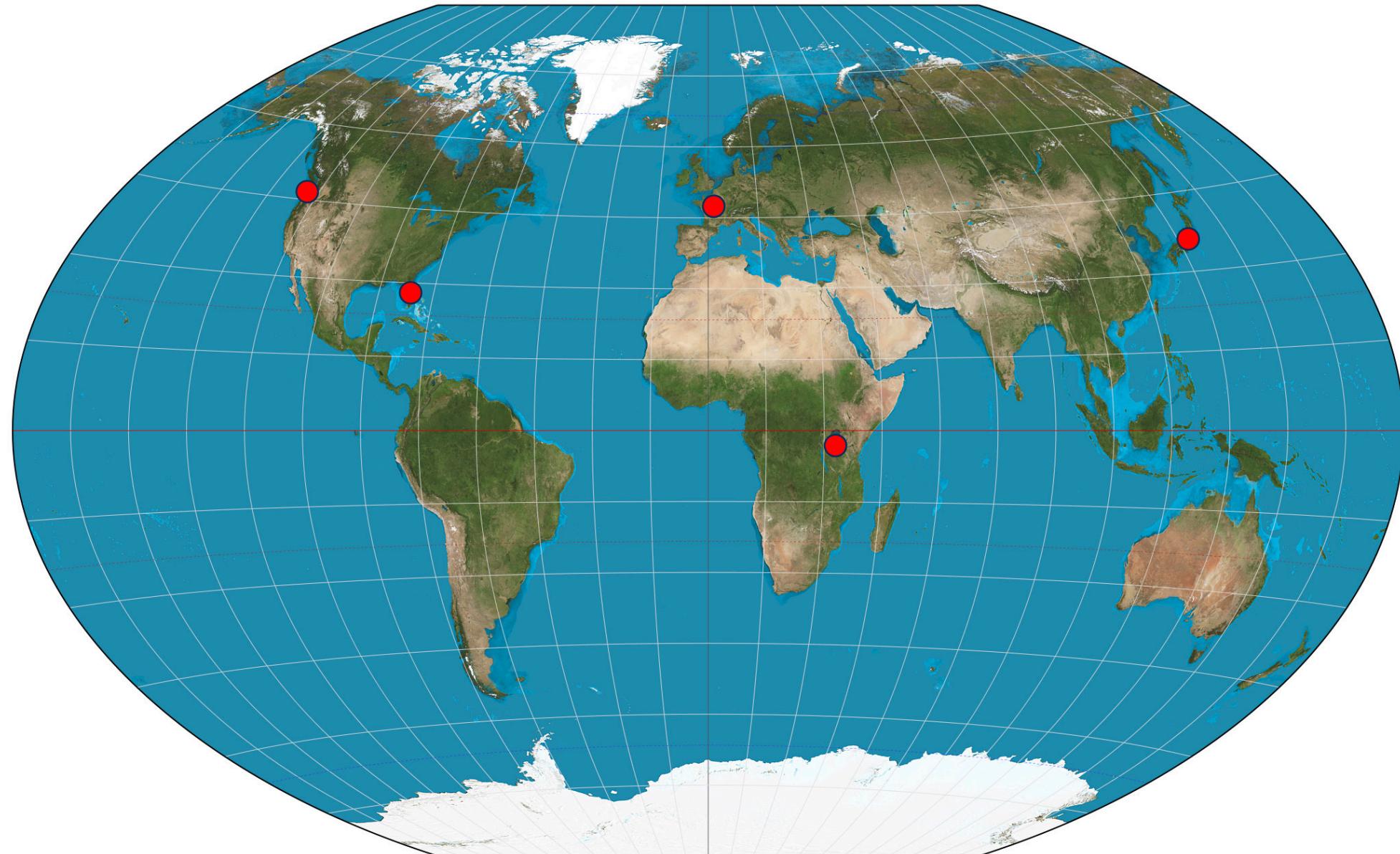
## *Abstract*

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The sequencing of eleven cloned *Drosophila melanogaster* alcohol dehydrogenase (*Adh*) genes from five natural populations has revealed a large number of previously hidden polymorphisms. Only one of the 43 polymorphisms results in an amino acid change, the one responsible for the two electrophoretic variants (fast, *Adh-f*, and slow, *Adh-s*) found in nearly all natural populations. The implication is that most amino acid changes in *Adh* would be selectively deleterious.

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**The study used 11 *D. melanogaster* strains derived from 5 locations**



# Structure of the *Adh* gene in *Drosophila melanogaster*

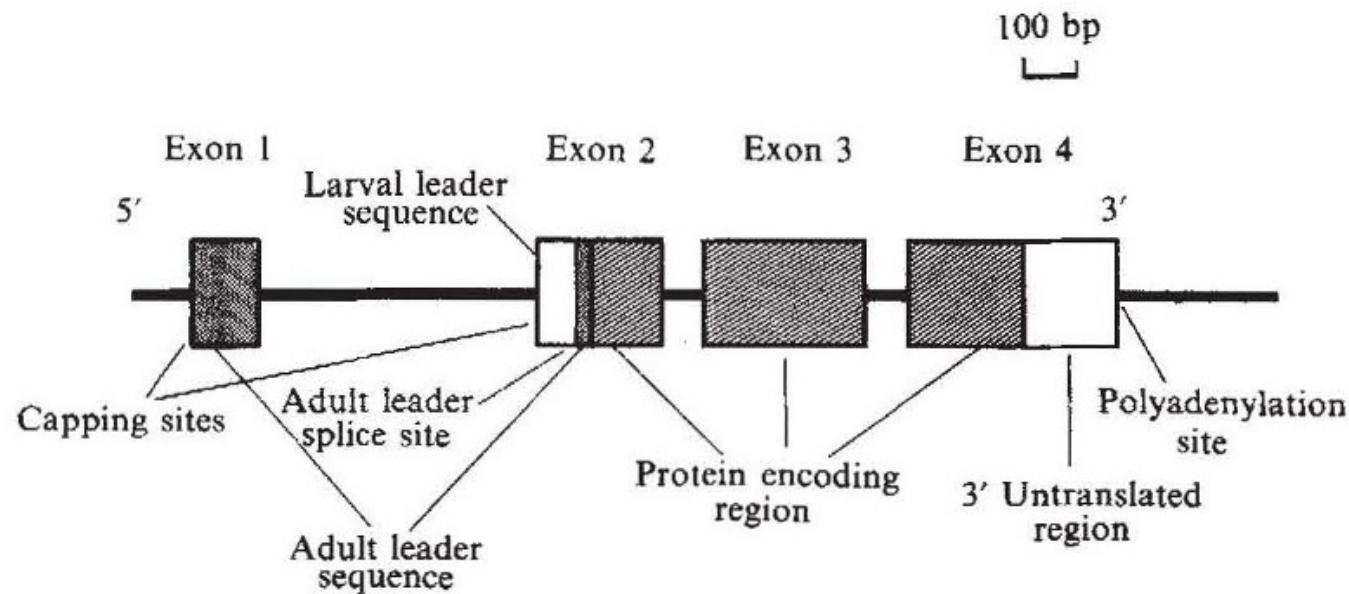


Figure 1 from Kreitman 1983

# DNA sequence variation at *Adh*

*Polymorphic sites* are sites that vary across individuals in the population

## Consensus sequence showing polymorphic sites

721 GCCCTTCCAATTGAAACAGATCGAAAGAGCCTGCTAAAGCAAAAAGAAGTCACCATGTCGTTACTTGACCAACAA  
Met Ser Phe Thr Leu Thr Asn Lys

801 GAACTGTATTTCGTTCCCGTCTGGGAGGCATTGGCTGGACACCAGCAAGGAGCTGCTCAAGCGCGATCTGAAGGTAA  
s Asn Val Ile Phe Val Ala Gly Leu Gly Gly Ile Gly Leu Asp Thr Ser Lys Glu Leu Leu Lys Arg Asp Leu Lys

881 CTATGCGATGCCAACAGGCTCCATGCACCGATGGAGGTTAACATCGTGTATTCAATCCTAGAACCTGGTATCCTCGACC  
Asn Leu Val Ile Leu Asp A

961 GCATTGAGAACCCGGCTGCCATTGCCAGCTGAAGGCAATCAATCAAAGGTGACCGTCACCTTACCCCTATGATGTC  
rg Ile Glu Asn Pro Ala Ala Ile Ala Glu Leu Lys Ala Ile Asn Pro Lys Val Thr Val Thr Phe Tyr Pro Tyr Asp Val

1041 ACCGTGCCATTGCCAGACCACCAACCTGTAAGAACCATCTCGCCACCTGAAAGACCGTCATGTCCTGATCAACCGG  
Thr Val Pro Ile Ala Glu Thr Thr Lys Leu Leu Lys Thr Ile Phe Ala Gln Leu Lys Thr Val Asp Val Leu Ile Asn Gl

1121 AGCTGGTATCCTGGACGATCACAGATCGAGCGCACCATGCCGTCAACTACACTGCCGTGGTCAACACCACGACGGCCA  
y Ala Gly Ile Leu Asp Asp His Gln Ile Glu Arg Thr Ile Ala Val Asn Tyr Thr Gly Leu Val Asn Thr Thr Ala I

1201 TTCTGGACTTCTGGACAAGCGCAAGGCCGTGCCGTGGTATCATCTGCAACATTGGATCCGTCACTGGATTCAATGCC  
Ile Leu Asp Phe Trp Asp Lys Gly Pro Gly Ile Ile Cys Asn Ile Gly Ser Val Thr Gly Phe Asn Ala

1281 ATCTACCAAGGTCCCCGTCTACTCCGGCACCAAGGCCGTGGTCAACTTCACCAGCTCCCTGGCGTAAGTTGATCAAA  
Ile Tyr Gln Val Pro Val Tyr Ser Gly Thr Lys Ala Ala Val Val Asn Phe Thr Ser Ser Leu Ala

1361 GAAACGCAAAGTTTCAAGAAAAAAACAACAACTAATTGATTATAACACCTTAGAAACTGGCCCGATTCACCGTG  
Lys Leu Ala Pro Ile Thr Gly Val

1441 ACCGCTTACACCGTGAACCCGGCATCACCGCACCCCTGTGCACAAATTCAACTCTGGTTGGATGTTGAGGCC  
Thr Ala Tyr Thr Val Asn Pro Gly Ile Thr Arg Thr Leu Val His Lys Phe Asn Ser Trp Leu Asp Val Glu Pro Gl

1521 GGTTGCTAGAAGCTCCTGGCTCATCCCACCCAGCGATCGTTGGCTGCGCCGAGAACTTCGTCAAGGCTATCGAGCTGA  
n Val Ala Glu Lys Leu Leu Ala His Pro Thr Gln Pro Ser Leu Ala Cys Ala Glu Asn Phe Val Lys Ala Ile Glu Leu A

1601 ACCAGAACGGAGCCATCTGGAAACTGGACTTGGGACCCCTGGAGGCCATCCAGTGGACCAAGCAGTGGACTCCGGCATC  
sn Gln Asn Gly Ala Ile Trp Lys Leu Asp Leu Gly Thr Leu Glu Ala Ile Gln Trp Thr Lys His Trp Asp Ser Gly Ile

# DNA sequence variation at *Adh*

A polymorphism at site 1490 encodes a Lys -> Thr amino acid **nonsynonymous substitution**, which results in a change from the 'slow' metabolising to 'fast' metabolizing allele

## Consensus sequence showing polymorphic sites

721 GCCCTTTCAATTGAAACAGATCGAAAGAGCCTGCTAAAGCAAAAAGAAGTCACCATGTCGTTACTTGACCAACAA  
Met Ser Phe Thr Leu Thr Asn Lys

801 GAACGTGATTTCTGTTGCCGTCTGGGAGGCATTGGCTGGACACCAGCAAGGAGCTGCTCAAGCGCGATCTGAAGGTAA  
s Asn Val Ile Phe Val Ala Gly Leu Gly Gly Ile Gly Leu Asp Thr Ser Lys Glu Leu Leu Lys Arg Asp Leu Lys

881 CTATGCGATGCCAACAGGCTCCATGCACCGATGGAGGTTAACATCGTGTATTCAATCCTAGAACCTGGTATCCTCGACC  
Asn Leu Val Ile Leu Asp A

961 GCATTGAGAACCCGGCTGCCATTGCCAGCTGAAGGCAATCAATCAAAGGTGACCGTCACCTTACCCCTATGATGTC  
rg Ile Glu Asn Pro Ala Ala Ile Ala Glu Leu Lys Ala Ile Asn Pro Lys Val Thr Val Thr Phe Tyr Pro Tyr Asp Val

1041 ACCGTGCCATTGCCAGACCACCAAGCTGCTGAAGACCATCTCGCCACCTGAAGACCGTCATGTCCTGATCAACCG  
Thr Val Pro Ile Ala Glu Thr Thr Lys Leu Leu Lys Thr Ile Phe Ala Gln Leu Lys Thr Val Asp Val Leu Ile Asn Gl

1121 AGCTGGTATCCTGGACGATCACAGATCGAGCGCACCATGCCGTCAACTACACTGCCGTGGTCAACACCACGACGGCCA  
y Ala Gly Ile Leu Asp Asp His Gln Ile Glu Arg Thr Ile Ala Val Asn Tyr Thr Gly Leu Val Asn Thr Thr Ala I

1201 TTCTGGACTTCTGGACAAGCGCAAGGGCGGTCCCCGGTGGTATCATCTGCAACATTGGATCCGTCACTGGATTCAATGCC  
Ile Leu Asp Phe Trp Asp Lys Gly Gly Pro Gly Gly Ile Ile Cys Asn Ile Gly Ser Val Thr Gly Phe Asn Ala

1281 ATCTACCAAGGTCCCCGTCTACTCCGGCACCAAGGCCGCCGTGGTCAACTTCACCAGCTCCCTGGCGTAAGTTGATCAAA  
Ile Tyr Gln Val Pro Val Tyr Ser Gly Thr Lys Ala Ala Val Val Asn Phe Thr Ser Ser Leu Ala

1361 GGAAACGCAAAGTTCAAGAAAAACAAAACAAACTATTGATTATAACACCTTAGAAACTGGCCCCATTACCGCGTG  
Lys Leu Ala Pro Ile Thr Gly Val

1441 ACCGCTTACACCGTGAACCCGGCATCACCGCACCCCTGTCAGAAAGTTCAACTCCTGGTGGATGTTGAGCCCCA  
Thr Ala Tyr Thr Val Asn Pro Gly Ile Thr Arg Thr Thr Leu Val His Lys Phe Asn Ser Trp Leu Asp Val Glu Pro Gl

1521 GGTTGCTGAGAACGCTCCTGGCTCATCCCACCCAGCCATCGTGGCCTGCCGGAGAACCTCGTCAAGGCTATCGAGCTGA  
n Val Ala Glu Lys Leu Leu Ala His Pro Thr Gln Pro Ser Leu Ala Cys Ala Glu Asn Phe Val Lys Ala Ile Glu Leu A

1601 ACCAGAACGGAGCCATCTGGAAACTGGACTTGGGACCCCTGGAGGCCATCCAGTGGACCAAGCAGCTGGACTCCGGCATC  
sn Gln Asn Gly Ala Ile Trp Lys Leu Asp Leu Gly Thr Leu Glu Ala Ile Gln Trp Thr Lys His Trp Asp Ser Gly Ile

# Key results from Kreitman 1983

- Variation was higher than expected: 43 out of 2721 sites varied within the sample
- Most variation involved ***single nucleotide polymorphisms*** (**SNPs**)
- Only one polymorphism was ***non-synonymous\****, i.e., affected the amino acid sequence, while 14 polymorphisms were ***synonymous*** (i.e., affected the coding sequence but did not change the amino acid sequence). The others affected ***non-coding DNA***.

# What was novel about this study?

- Previous studies focused on protein variation assayed using rate of movement through an electrophoretic gel. ***This was the first study to examine sequence variation within a species.***
- This study showed that contrary to the limited variation that could be assayed using gel electrophoresis, ***variation at the DNA sequence level was relatively common.***
- However, ***no new variation was detected that affected the amino acid sequence*** of the Adh protein.
- These results imply ***that strong purifying selection likely acted to limit changes in the Adh protein sequence.***

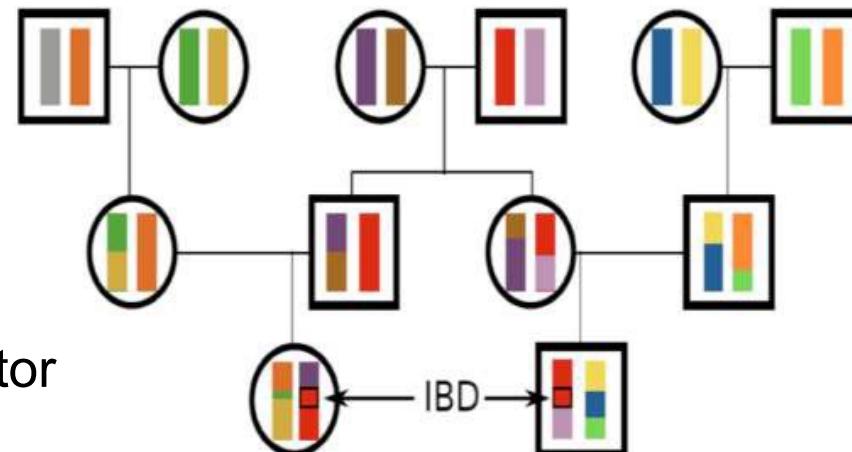
# Describing population genetic variation (part 0)

# Some terminology

- A *locus* is a genomic location
- Sites that vary with a population are called *segregating sites* or *polymorphic sites*
- In the protein-coding or gene regions
  - Coding variants that change the amino acid sequence are called *nonsynonymous* or *replacement* polymorphisms
  - Coding variants that do not change the amino acid sequence are called *synonymous* or *silent* polymorphisms
- An *allele* is the physical copy of DNA at a locus on a chromosome; usually used in the context of a polymorphic locus
- A *heterozygote* at a given locus carries two different alleles on its two chromosomes
- A *homozygote* at a given locus carries the same allele on both chromosomes

# Evolution involves descent with modification

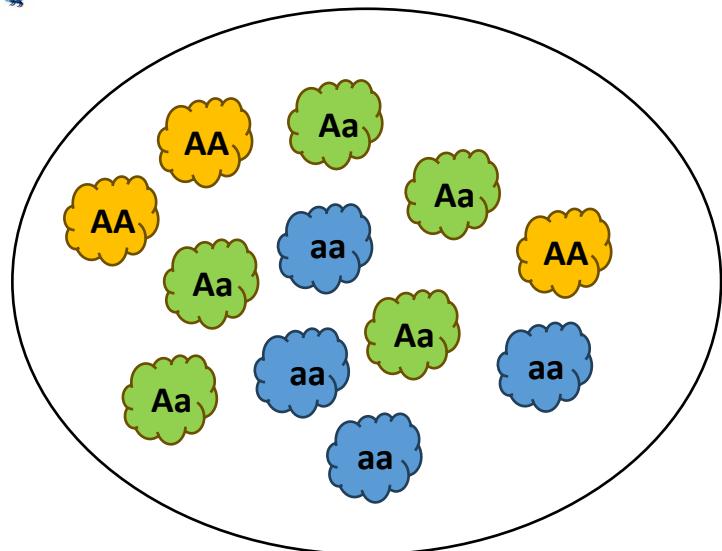
Identity by state (IBS) occurs when two alleles at a given locus are the same



Two alleles derived from the same ancestor  
are shared identical by descent (IBD)

\*\* Note that two alleles could be identical by state but differ by descent due to mutation

# Genotype and allele frequencies



Since we normally cannot sample an entire population, we are generally working with a **sample** from the populations we are studying.

Therefore, the genotype and allele frequencies we calculate from our sample are only **estimates** of the actual value in the population.

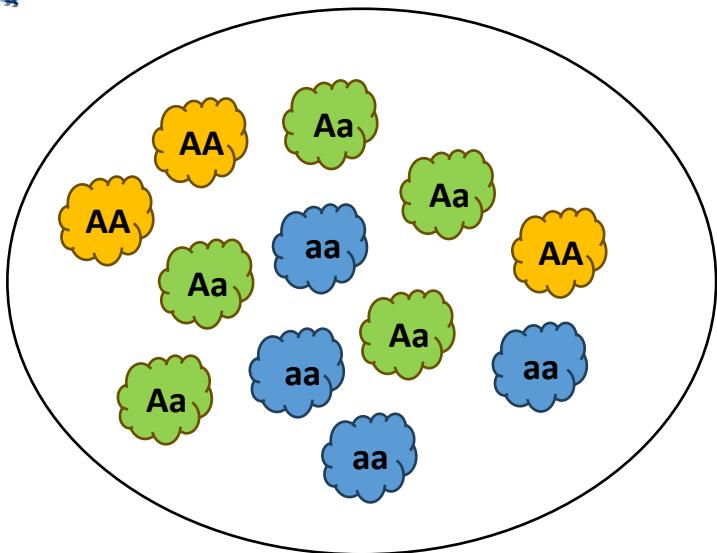
The **confidence** we have in our allele frequency estimates depends on the allele frequency and on how deeply we sampled from the population

95% confidence interval on estimate of the allele frequency

$$\hat{p} \pm 1.96 \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$$

*As sample size increases, the confidence interval becomes tighter*

# Genotype frequencies

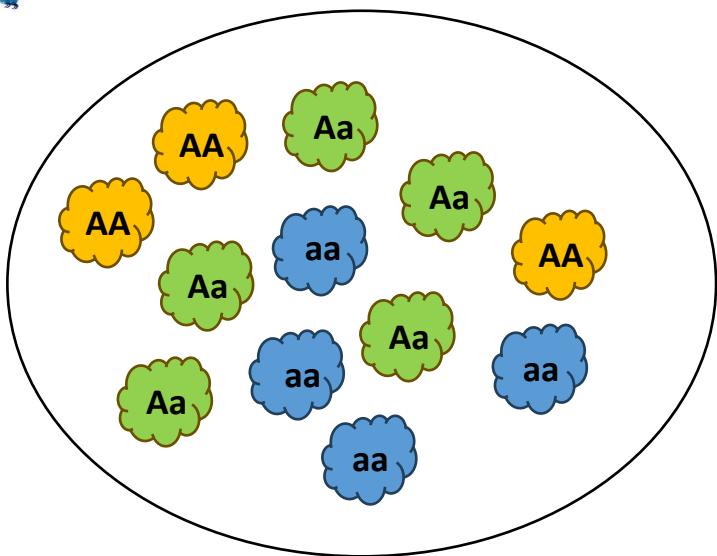


Genotype frequencies sum up to 1:

$$x_{11} + x_{12} + x_{22} = 1$$

Or, alternatively:  $x_{AA} + x_{Aa} + x_{aa} = 1$

# Genotype frequencies



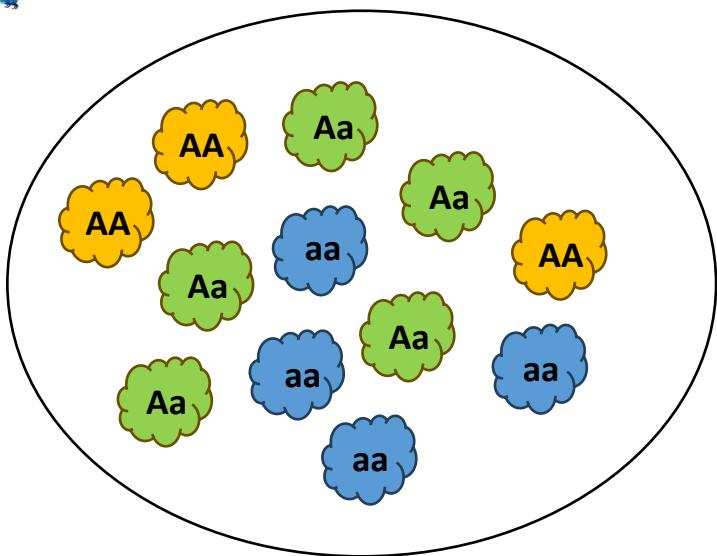
Genotype frequencies sum up to 1:

$$x_{11} + x_{12} + x_{22} = 1$$
$$x_{AA} + x_{Aa} + x_{aa} = 1$$

The frequency of each genotype is the number of that genotype divided by the total number of individuals:

$$x_{AA} = N_{AA}/N$$
$$x_{Aa} = N_{Aa}/N$$
$$x_{aa} = N_{aa}/N$$

# Genotype frequencies



Genotype frequencies sum up to 1:

$$x_{11} + x_{12} + x_{22} = 1$$

$$x_{AA} + x_{Aa} + x_{aa} = 1$$

The frequency of each genotype is the number of that genotype divided by the total number of individuals:

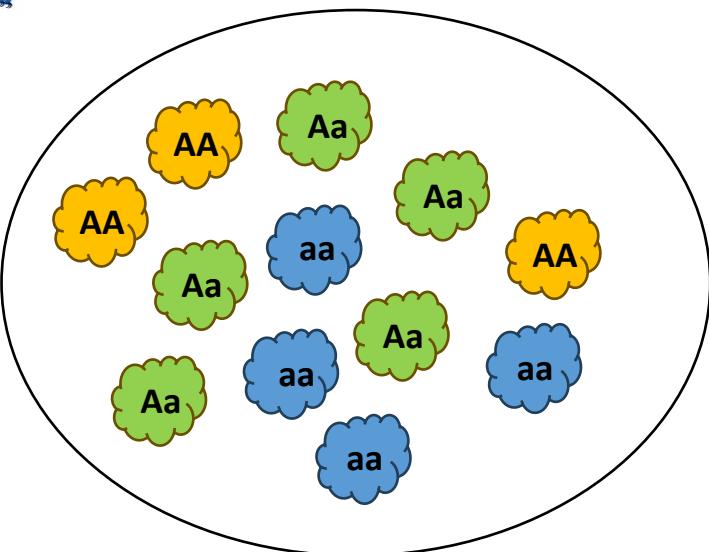
$$x_{AA} = \frac{N_{AA}}{N} = \frac{3}{12} = 0.25$$

$$x_{Aa} = \frac{N_{Aa}}{N} = \frac{5}{12} = 0.42$$

$$x_{aa} = \frac{N_{aa}}{N} = \frac{4}{12} = 0.33$$

# Genotype and allele frequencies

## Genotype frequencies



$$x_{AA} = 0.25$$

$$x_{Aa} = 0.42$$

$$x_{aa} = 0.33$$

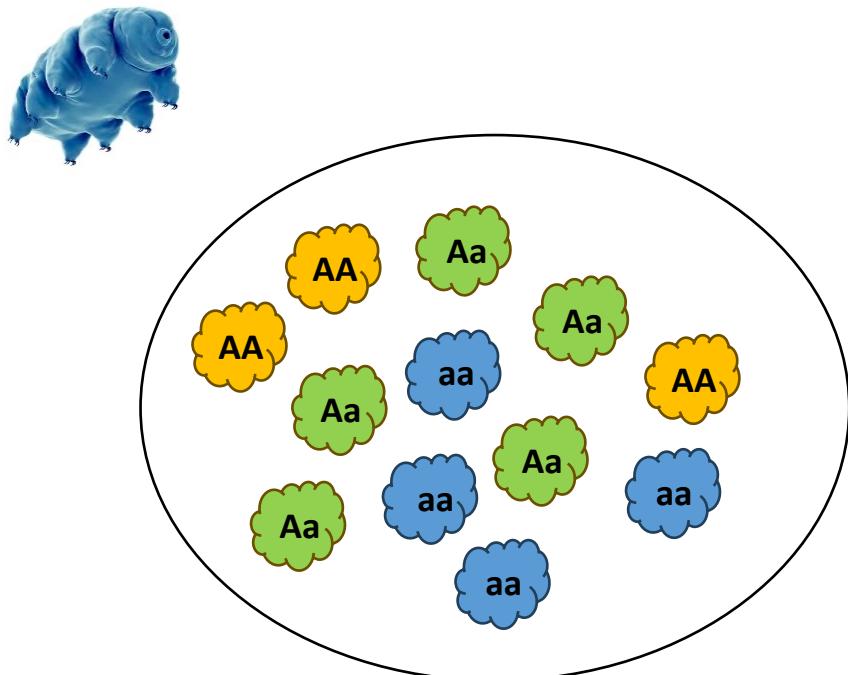
## Allele frequencies

$$p = x_{AA} + \frac{1}{2} x_{Aa}$$

$$q = 1 - p = x_{aa} + \frac{1}{2} x_{Aa}$$

# Genotype and allele frequencies

## Genotype frequencies



$$x_{AA} = 0.25$$

$$x_{Aa} = 0.42$$

$$x_{aa} = 0.33$$

## Allele frequencies

$$p = x_{AA} + \frac{1}{2} x_{Aa} = 0.25 + 0.21 = 0.46$$

$$q = 1 - p = x_{aa} + \frac{1}{2} x_{Aa} = 0.33 + 0.21 = 0.54$$

# Generalization to K-allelic loci

*What about the case(s) where a locus is not bi-allelic?*

For example, microsatellite loci tend to have more than two alleles.

Genotype frequencies still sum up to 1:

$$\begin{aligned} 1 &= x_{11} + x_{22} + \dots + x_{nn} + x_{12} + x_{13} + \dots + x_{(n-1)n} \\ &= \sum_{i=1}^n \sum_{j \geq 1} x_{ij} \end{aligned}$$

And the frequency of the  $i$ th allele is:

$$p_i = x_{ii} + \frac{1}{2} \sum_{j=1}^{i-1} x_{ji} + \frac{1}{2} \sum_{j=i+1}^n x_{ij}$$

# Evolution is the change in allele frequencies over time.

***What causes allele frequencies to change?***

- Mutation
- Genetic drift
- Migration
- Selection

*We will explore each of these forces of evolution in more detail in future lectures*

# Summary

- Population genetics can help to address a wide variety of basic and applied questions
- The genomic revolution is opening up new opportunities to study variation within and between populations
- Not all mutations are created equal; some affect non-coding DNA and some affect coding regions. Those that impact coding DNA may be synonymous or non-synonymous
- Evolution involves a process of descent with modification
- We can estimate population allele frequencies from a sample. The size of the sample and frequency of the allele in the population determines the precision of our estimate

# More resources

- <https://www.genome.gov/leadership-initiatives/History-of-Genomics-Program>
- <https://www.genome.gov/about-genomics/policy-issues>
- [Genetics unzipped podcasts from The Genetics Society](#)
- <https://geneticsunzipped.com/blog/2019/4/11/011-darwin-vs-mendel>
- <https://geneticsunzipped.com/blog/2024/1/11/the-battle-for-biology-mendel>
- <https://geneticsunzipped.com/blog/2020/10/22/s322-the-past-present-and-future-of-the-human-genome-project>
- <https://www.nature.com/immersive/d42859-020-00099-0/index.html>