



Trilinos User's Group Meeting 2022

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Outline

- Theory
- Code
- Linear Solvers and Preconditioning



Theory

Ryan Glasby

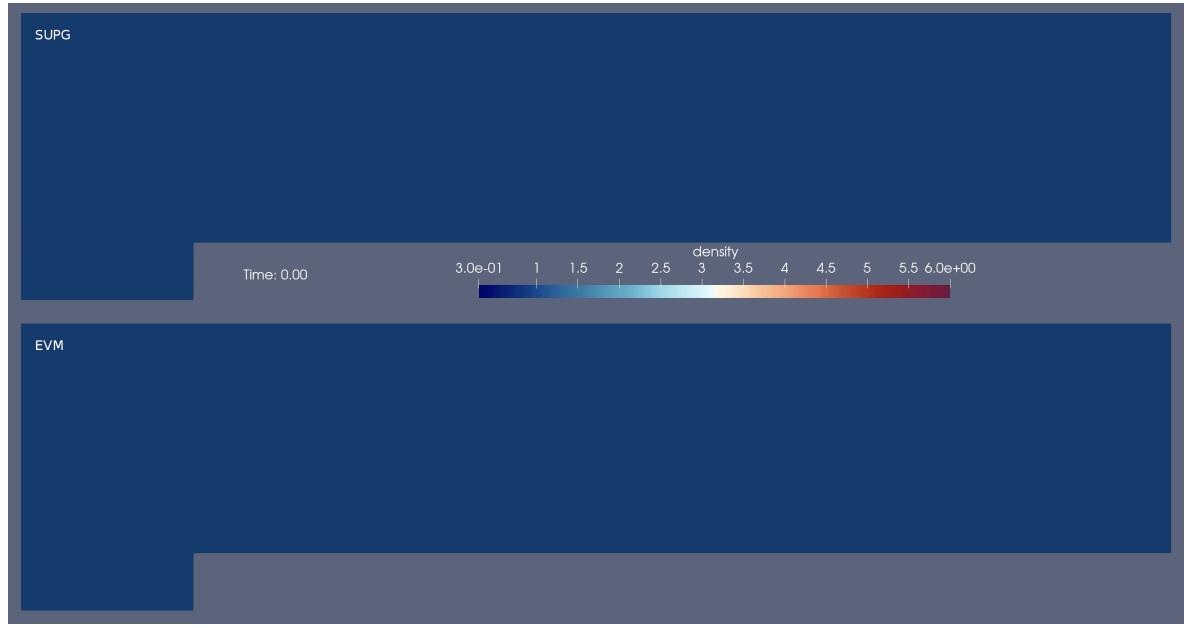


PDE

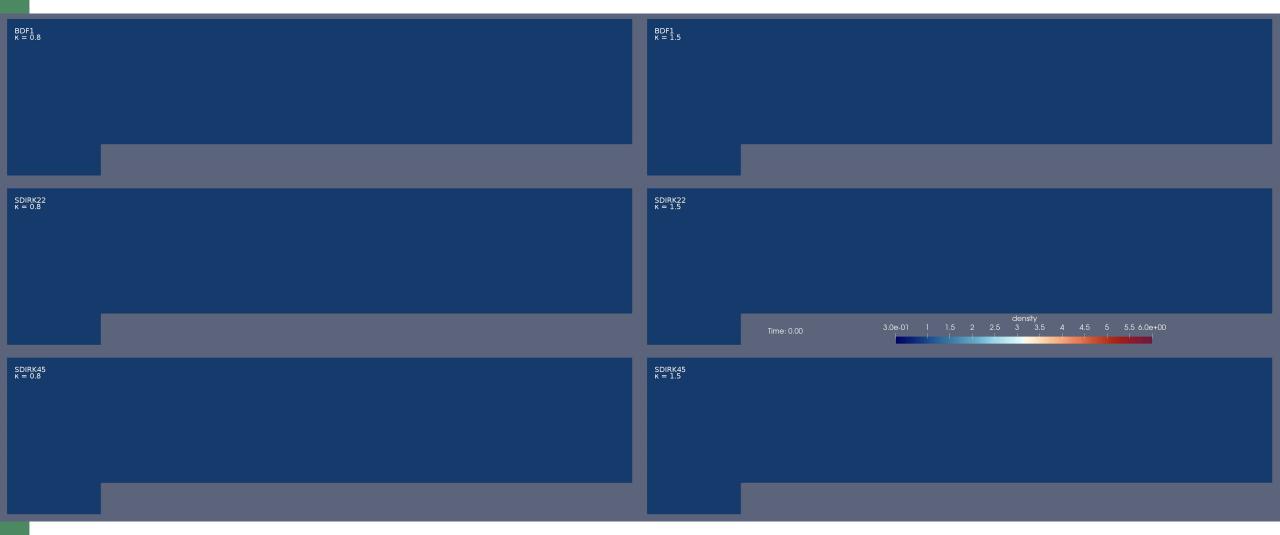
- Navier-Stokes/Euler/(Open ended)
- PDE definition: written in weak conservative form evaluated at quadrature points
 - Time derivative, convective operator, viscous operator, source terms
 - Numerical artificial diffusion for convective operators
 - Boundary flux dot with normal vector operators
 - Boundary state supplied -> convective (flux evaluated), viscous (penalty term)
 - Dirichlet/Neumann



SUPG vs. EVM

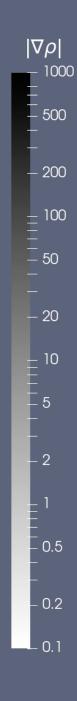


Time Integration



Mach 17 Gnoffo Cylinder





Code Stuart Slattery



Use of Trilinos

- Amesos
- Amesos2
- Belos
- Epetra
- Exodus
- Ifpack
- Ifpack2
- Intrepid2

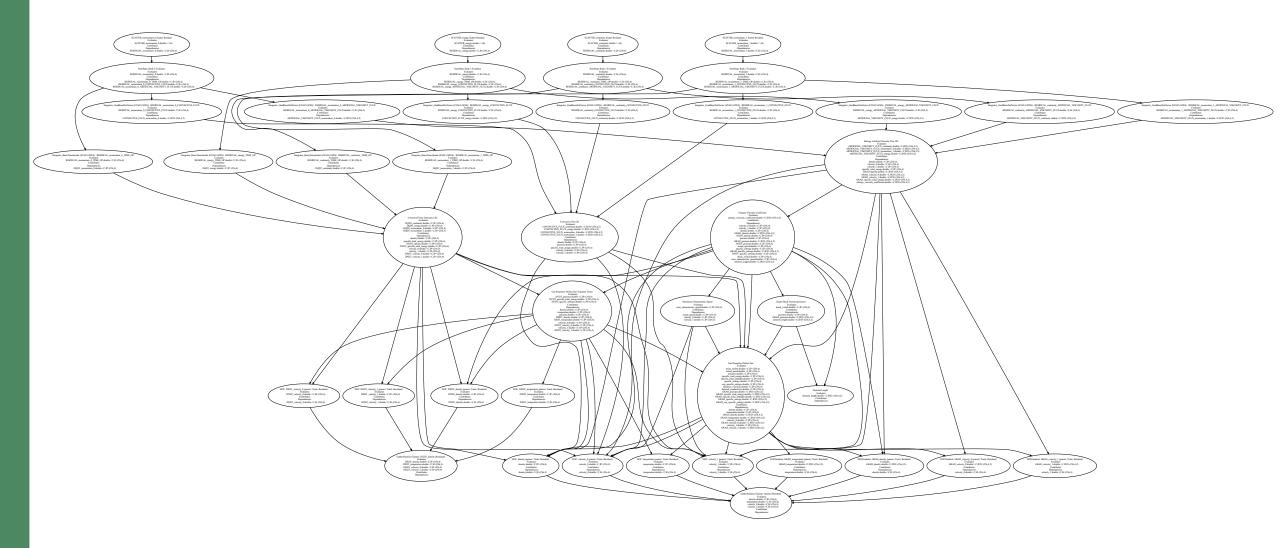
- Kokkos
- Muelu
- NOX
- Panzer
- Phalanx
- Seacas
- Sacado
- Shards

- Stratimikos
- STK
- Tempus
- Teuchos
- Thyra
- Tpetra
- Zoltan

~40% of Trilinos packages



Phalanx Execution Graph



Parameterization: Objectives

- Allow developers to declare scalars in objects that may be parameterized
- Allow users to declare global scalar parameters in the input file and map those global parameters to local object parameters
- Orchestrate the updating of parameters automatically from the Thyra ModelEvaluator parameter interface
- Examples:
 - Scalar values in material properties
 - Scalar values in boundary conditions
 - Scalar values in initial conditions



Parameterization: User Input

```
<ParameterList name="Scalar Parameters">
   <ParameterList>
     <Parameter name="Name" type="string" value="Thermal Conductivity" />
     <Parameter name="Nominal Value" type="double" value="1.23e-4" />
  </ParameterList>
  <ParameterList>
     <Parameter name="Name" type="string" value="Inflow Velocity" />
     <Parameter name="Nominal Value" type="double" value="0.53" />
   </ParameterList>
</ParameterList>
```

Parameterization: Using parameters in objects

```
<ParameterList>
  <Parameter name="Sideset ID"</pre>
                                      type="string" value="left"
  <Parameter name="Element Block ID" type="string" value="eblock-0 0" />
  <Parameter name="Strategy"</pre>
                                      type="string" value="BoundaryFlux"/>
  <ParameterList name="Data">
    <Parameter name="Type" type="string" value="Farfield"/>
    <Parameter name="Farfield Density" type="double" value="1.0"/>
   <Parameter name="Farfield Velocity 0" type="ScalarParameter" value="Inflow Velocity"/>
   <Parameter name="Farfield Velocity 1" type="double" value="0.0"/>
    <Parameter name="Farfield Temperature" type="double" value="1.0"/>
  </ParameterList>
```

- GlobalScalarParameter will be a special type for which we write ParameterList serialization
- A user can toggle between a standard double value and a ScalarParameter value to link an object parameter to a global parameter.



</ParameterList>

Parameterization: Design Considerations

- Updated parameters get assigned before every evalModel() call in Panzer::ModelEvaluator and reset back to nominal values after
 - This means an automated process during graph execution must be created to automatically update parameters we can't interject our own code otherwise
- An observer pattern is used to automatically update the parameters in an object based on the content of the Thyra parameter vectors provided to evalModel()
 - Parameter observers must be registered upon construction. This will occur in all factories as well as any hand-built observers. An object must manage the state of the observers and trigger their update
 - Parameters hold reference to object data and update automatically in update()
- New evaluator that is always at bottom of graph and triggers parameter update.
 This will allow for exodus graph evaluation with parameters.
 - Will still need to get parameters into parameter library before Exodus output
 - Make a dummy field upon which all evaluators depend. Write our own base class upon which all of our evaluators depend. This base class depends on the dummy field. The dummy field is evaluated in the ParameterEvaluator and hence triggers parameter evaluation prior to all graph evaluations



Parameterization: Parameter Distribution

```
template<class EvalType, class Traits>
ScalarParameterEvaluator<EvalType, Traits>::ScalarParameterEvaluator(
    const Teuchos::RCP<ScalarParameterManager<EvalType>>& param_manager,
    const Teuchos::RCP<panzer::GlobalData>& global data)
    : _param_manager(param_manager)
    , _global_data(global_data)
    auto dummy layout = Teuchos::rcp(new PHX::MDALayout<panzer::Dummy>(0));
    _param_update_trigger = Teuchos::rcp(
        new PHX::Tag<scalar_type>("scalar_parameter_eval", dummy_layout));
    this->addEvaluatedField(*_param_update_trigger);
    this->setName("Scalar Parameter Evaluation");
template<class EvalType, class Traits>
void ScalarParameterEvaluator<EvalType, Traits>::preEvaluate(
    typename Traits::PreEvalData)
    param_manager->update(*_global_data);
template<class EvalType, class Traits>
void ScalarParameterEvaluator<EvalType, Traits>::evaluateFields(
    typename Traits::EvalData)
```

Parameterization: New Evaluators

```
template<class EvalType, class Traits>
class EvaluatorWithParameter
    : public EvaluatorBase<EvalType, Traits>,
      public Response::ScalarParameterObserver<EvalType>
  public:
    using scalar_type = typename EvalType::ScalarT;
    EvaluatorWithParameter(const panzer::IntegrationRule& ir,
                           const Teuchos::ParameterList& params)
        : _pre_f1("pre_f1", ir.dl_scalar)
        , _pre_f2("pre_f2", ir.dl_scalar)
        , _pre_f3("pre_f3", ir.dl_scalar)
        , _f1("f1", ir.dl_scalar)
        , _f2("f2", ir.dl_scalar)
        , _f3("f3", ir.dl_scalar)
        this->addEvaluatedField(_pre_f1);
        this->addEvaluatedField(_pre_f2);
        this->addEvaluatedField(_pre_f3);
        this->addEvaluatedField( f1);
        this->addEvaluatedField( f2);
        this->addEvaluatedField(_f3);
        this->registerParameter("p1", 2.0, params, _p1);
        this->registerParameter("p2", 3.0, params, _p2);
        this->registerParameter("p3", 4.0, params, _p3);
        this->setName("EvaluatorWithParameter");
```

```
protected:
   void updateStateWithNewParameters() override
       // Get the parameters here to make sure these are available in
       // evaluators to do pre-evaluate calculations.
       _{pre_p1} = _{p1};
       _{pre_p2} = _{p2};
       _pre_p3 = _p3;
   void preEvaluateImpl(typename Traits::PreEvalData) override
       _pre_f1.deep_copy(_pre_p1);
       _pre_f2.deep_copy(_pre_p2);
       _pre_f3.deep_copy(_pre_p3);
   void evaluateFieldsImpl(typename Traits::EvalData) override
       _f1.deep_copy(_p1);
       _f2.deep_copy(_p2);
       _f3.deep_copy(_p3);
};
// <ParameterList>
        <Parameter name="p2"
                               type="ScalarParameter" value="Parameter2"/>
        <Parameter name="p3"
                               type="double" value="9.2"/>
// </ParameterList>
11
// Note that pl is not included to trigger the default evaluation.
```

Development Ideas

Short Term:

- High-order element topology support (quadratic and cubic) in both Exodus and Panzer assembly
- General Panzer/Trilinos support for CUDA (non-UVM) and HIP

Long Term:

- Tangent support in Tpetra
- Hessian support in Panzer
- Delayed Jacobian evaluation in Panzer



Linear Solvers and Preconditioning

Steven Hamilton



Solver considerations

- Primarily targeting multithreaded CPUs for near-term
 - Support for both Nvidia and AMD GPUs is important for future
- Currently focused on algebraic preconditioning (with AD-generated Jacobian matrices)
- Main solver strategy is GMRES (w/o restart if possible) and overlapping additive Schwarz preconditioner
 - Incomplete factorizations or sparse direct solvers for local solves
- Algebraic multigrid performs poorly on all but trivial problems
 - Similar behavior in ML, MueLu, and BoomerAMG
 - Ongoing work to understand challenges
- Overlap and threading (larger local domains) improve robustness and strong scaling



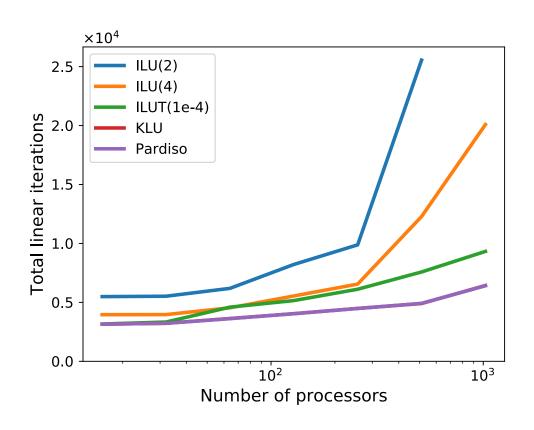
Solver selection

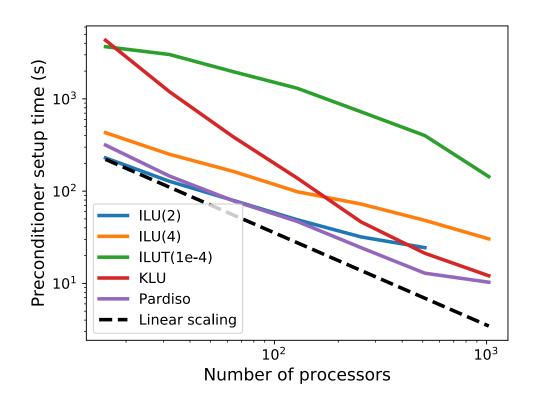
- Stratimikos allows extensive solver and preconditioner selection from input file
 - Belos, Ifpack(2), Amesos(2), ML, MueLu...
- Both Epetra and Tpetra stacks are supported for complete flexibility
 - Ifpack2 doesn't recognize overlap for additive Schwarz
 - Epetra implementations of some TPLs (e.g., PardisoMKL?) seem to be more robust
- For Nvidia GPUs, cuSOLVER GLU sparse direct solver is used
 - One-time host factorization, refactor on device
 - Not in public documentation



Solver performance

- MPI only (1 thread per rank), 2x 64-core AMD CPUs
- Global matrix size: 120k spatial elements, 600k DOFs





Preconditioner comparison

- 2x 64-core AMD CPUs, 2x Nvidia V100 GPUs per node
- Global Matrix size: 120k spatial elements, 600k DOFs

Device	CPU	CPU	CPU	GPU
MPI ranks	128	16	2	2
OpenMP threads per rank	1	8	64	1
Local solver	KLU2	Pardiso	Pardiso	GLU
Total linear solve (s)	500.8	471.5	929.9	964.5
Total preconditioner setup (s)	43.9	106.3	825.4	330.8
One-time CPU prec. setup (s)				64.3
Total preconditioner apply (s)	224.6	232.3	81.6	550.6
Total linear iterations	$32,\!513$	$22,\!172$	3,737	3,757
Avg. linear iterations per Newton	86.7	59.1	10.0	10.0

Native preconditioner implementation

- Panzer provides method to construct Thyra linear solver factory from parameters
 - Internally uses Stratimikos
 - Registers mesh coordinates with AMG solvers
- Stratimikos factory registration is instance based
 - No way to inject user preconditioner

```
// Replicate behavior of panzer_stk::buildLOWSFactory
RCP < Thyra::LinearOpWithSolveFactoryBase <>>
LOWSFactoryBuilder::buildLOWS(RCP<ParameterList> params)
    Stratimikos::DefaultLinearSolverBuilder builder;
    using Base = Thyra::PreconditionerFactoryBase<>;
    // Register Trilinos factories that aren't automatic
    using Ifpack2Factory = Thyra::Ifpack2PreconditionerFactory <...>>;
    builder.setPreconditioningStrategyFactory(
        abstractFactoryStd <Base, Ifpack2Factory>(), "Ifpack2");
    Stratimikos::enableMueLu<...>(builder, "MueLu");
    // Register our own preconditioner factory with Stratimikos
    builder.setPreconditioningStrategyFactory(
        abstractFactoryStd < Base , NativeFactory > () , "Native");
    builder.setParameterList(params);
    RCP < Thyra::LinearOpWithSolveFactoryBase <>> lowsFactory
        = createLinearSolveStrategy(builder);
    return lowsFactory;
```

Native preconditioner implementation (2)

```
// Replicate behavior of panzer_stk::buildLOWSFactory
RCP < Thyra::LinearOpWithSolveFactoryBase <>>
LOWSFactoryBuilder::buildLOWS(RCP<ParameterList> params)
    Stratimikos::DefaultLinearSolverBuilder builder;
    using Base = Thyra::PreconditionerFactoryBase<>;
    // Register Trilinos factories that aren't automatic
    using Ifpack2Factory = Thyra::Ifpack2PreconditionerFactory <...>>;
    builder.setPreconditioningStrategyFactory(
        abstractFactoryStd < Base, Ifpack2Factory > (), "Ifpack2");
    Stratimikos::enableMueLu<...>(builder, "MueLu");
    // Register our own preconditioner factory with Stratimikos
    builder.setPreconditioningStrategyFactory(
        abstractFactoryStd < Base (NativeFactory > ), "Native");
    builder.setParameterList(params);
    RCP < Thyra::LinearOpWithSolveFactoryBase <>> lowsFactory
        = createLinearSolveStrategy(builder);
    return lowsFactory;
```

```
// Replicate behavior of panzer_stk::buildLOWSFactory
RCP < Thyra::LinearOpWithSolveFactoryBase <>>
LOWSFactoryBuilder::buildLOWS(RCP<ParameterList> params)
    Stratimikos::DefaultLinearSolverBuilder builder;
    using Base = Thyra::PreconditionerFactoryBase<>;
    // Register Trilinos factories that aren't automatic
    using Ifpack2Factory = Thyra::Ifpack2PreconditionerFactory <...>>;
    builder.setPreconditioningStrategyFactory(
        abstractFactoryStd < Base, Ifpack2Factory > (), "Ifpack2");
    Stratimikos::enableMueLu <...>(builder, "MueLu");
    // Register our own preconditioner factory with Stratimikos
    builder.setPreconditioningStrategyFactory(
        abstractFactoryStd < Base , NativeFactory > () , "Native");
    builder.setParameterList(params);
    RCP < Thyra::LinearOpWithSolveFactoryBase <>> lowsFactory
        = createLinearSolveStrategy(builder);
    return lowsFactory:
class NativeFactory : public Thyra::PreconditionerFactoryBase<>
    void initializePrec(
        const Teuchos::RCP<const Thyra::LinearOpSourceBase<>>& fwdOpSrc,
        Thyra::PreconditionerBase<>* precOp,
        const Thyra::ESupportSolveUse supportSolveUse
        = Thyra::SUPPORT_SOLVE_UNSPECIFIED) const
        // Lots of Thyra stuff here...
        // Build AdditiveSchwarz and register our local solver
        auto schwarz = rcp(
            new Ifpack2::AdditiveSchwarz <> (tpetra_matrix));
        auto inner_prec = Teuchos::rcp(new LocalGLUSolver());
        schwarz->setInnerPreconditioner(inner_prec);
        // More Thyra stuff...
```

Native preconditioner implementation (3)

```
class NativeFactory : public Thyra::PreconditionerFactoryBase<>
{
    void initializePrec(
        const Teuchos::RCP<const Thyra::LinearOpSourceBase<>>& fwdOpSrc,
        Thyra::PreconditionerBase<>* precOp,
        const Thyra::ESupportSolveUse supportSolveUse
        = Thyra::SUPPORT_SOLVE_UNSPECIFIED) const
{
        // Lots of Thyra stuff here...
        ...

        // Build AdditiveSchwarz and register our local solver
        auto schwarz = rcp(
            new Ifpack2::AdditiveSchwarz<>>(tpotra_matrix));
        auto inner_prec = Teuchos::rcp(new LocalGLUSolver());
        schwarz->setInnerPreconditioner(inner_prec);

        // More Thyra stuff...
        ...
}
};
```

Wishlist

- More preconditioners "automatically" supported by Stratimikos
 - Including documentation on valid parameters
- Simpler approach to registering user-implemented preconditioners
- More GPU-capable preconditioners
 - When AMG doesn't work, there aren't many alternatives...
 - cuSOLVER for Nvidia GPUs, AMD path is unclear (SuperLU?)
 - Refactor-based sparse direct solvers?

