

Phenomenology of the Higgs and Flavour Physics In the Standard Model and Beyond

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List of publications

1. **L. Alasfar**, J. de Blas and R. Gröber
“Higgs probes of top quark contact interactions and their interplay with the Higgs self-coupling,”
arXiv:2202.02333 [hep-ph].
2. **L. Alasfar**, G. Degrassi, P. P. Giardino, R. Gröber and M. Vitti
Virtual corrections to $gg \rightarrow ZH$ via a transverse momentum expansion
JHEP **05** (2021), 168
arXiv:2103.06225 [hep-ph].
3. **L. Alasfar**, A. Azatov, J. de Blas, A. Paul and M. Valli
B anomalies under the lens of electroweak precision
JHEP **12** (2020), 016
arXiv:2007.04400 [hep-ph].
4. **L. Alasfar**, R. Corral Lopez and R. Gröber
Probing Higgs couplings to light quarks via Higgs pair production
JHEP **11** (2019), 088
arXiv:1909.05279 [hep-ph].

Part I

Higgs Physics

1 The Standard Model Higgs boson

It's very nice to be right sometimes...
it has certainly been a long wait.

Peter Higgs

Write intro here

1.1 Spontaneous symmetry breaking

Before talking about symmetry breaking, we need to discuss the concept of symmetry in physics. Symmetry has an essential role in studying physical systems. It manifests not only as a geometric feature of physical objects but also in the dynamics of physical systems. For example, one can find symmetries in the equation of motion, Lagrangians/Hamiltonians and actions. The magnetisation of materials is a good example of the role that symmetry plays in describing physical behaviour. For instance, **paramagnetic** materials have a positive magnetic susceptibility χ_B due to the random arrangement of their electrons' spins. The paramagnetic material spins arrangement will therefore possess rotational symmetry. The material has no *preferred direction* in space [1]. On the contrary, **ferromagnetic** materials with the electrons' spins aligned in a certain direction, will not have such symmetry as there will be a preferred direction, see Figure 1.1.

In particle physics and quantum field theory, symmetry plays an essential role in the taxonomy and dynamics of elementary particles and their bound states, i.e. hadrons, cf. [2, 3]. There are two types of symmetries considered when studying elementary particles and their quantum fields: external and internal symmetries. The first is the symmetry of the spacetime background. Typically, this is a four-dimensional Poincaré symmetry. However, in some models, higher spacetime dimensions or non-flat geometries are considered. Though there is no current evidence of higher dimensions or indications of non-flat spacetime from colliders and cosmological observations [4]. The second class of symmetries is internal symmetries stemming from the quantum nature of these particles/fields. Because their state is described by a **ray** in complex Hilbert/Fock spaces, internal symmetries are simply symmetries of rotations in these spaces that keep the action variation unchanged. Internal symmetries are usually described in terms of simple or product of simple **Lie groups**, e.g. $SU(N)$ ¹, and particles/fields will be arranged

¹Gauge theories based on finite groups have been investigated in the literature, but their phenomenological significance is yet to be further investigated [5, 6]

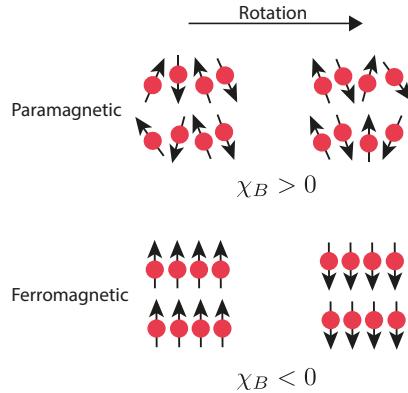


Figure 1.1. In paramagnetic materials, the spins are randomly distributed such that a rotation performed on the system will keep the spin distribution invariant. However, for ferromagnetic materials, where the spins are aligned in a single direction, the symmetry is broken, and the system has a preferred direction.

as multiplets in some representation of the groups. The rotations of the states could be parametrised by constants. In this case, the symmetry is called **global**, or fields of spacetime, where the symmetry is then called **local** or **gauged**.

Gauge symmetries describe rotations in the state space that depend on spacetime, the generator of the gauge transformations could propagate between two spacetime points. This is the way particle/field interactions are described in quantum field theory. The generators of these gauge transformations are called gauge bosons, and they mediate the interactions between the particles/fields and transform under the adjoint representation of the gauge group. Hence, we observe that gauge symmetries are the basis of describing the fundamental interactions of nature, which we call **gauge theories**.

An example of a gauge theory that is realised in nature is the **Standard Model** (SM). Which is a gauge theory based on the group $G_{\text{SM}} := SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$. The first simple group is for the *strong* interaction described by quantum chromodynamics (QCD). The product of the two remaining groups $SU(2)_L \otimes U(1)_Y$ forms the Weinberg-Salam *electroweak* (EW) model [7–9], where $SU(2)_L$ describes the weak interaction which only couples to *left handed* fermions and $U(1)_Y$ is the weak hypercharge Y gauge group, defined by the formula

$$Y = 2(Q - T_3). \quad (1.1)$$

Where Q is the electric charge and T_3 is the third component of the weak isospin. A description of the matter content of the SM and their multiplicities with respect to G_{SM} is shown in Table 1.1

The SM has been very successful at describing particle interactions even when challenged by numerous precision tests at LEP and SLD [11–14] and later at DØ [15] and the LHC [16, 17]. Nevertheless, it fails to describe the ground state if only the fermion and gauge sectors are considered. The reason for this shortcoming is that the W^\pm and Z bosons have a mass, this violates the EW gauge symmetry. This can be easily seen

Particle/Field	G_{SM} multiplicity	mass [GeV]
Quarks		
$Q = \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \begin{pmatrix} c_L \\ s_L \end{pmatrix}, \begin{pmatrix} t_L \\ b_L \end{pmatrix}$	$(\mathbf{3}, \mathbf{2}, 1/6)$	$m_u = 2.16 \cdot 10^{-3}, m_d = 2.67 \cdot 10^{-3}$
$U = u_R, c_R, t_R$	$(\mathbf{3}, \mathbf{1}, 2/3)$	$m_c = 0.93 \cdot 10^{-2}, m_s = 1.27$
$D = d_R, s_R, b_R$	$(\mathbf{3}, \mathbf{1}, -1/3)$	$m_t = 172.4, m_b = 4.18$
Leptons		
$L = \begin{pmatrix} \nu_{e,L} \\ e_L \end{pmatrix}, \begin{pmatrix} \nu_{\mu,L} \\ \mu_L \end{pmatrix}, \begin{pmatrix} \nu_{\tau,L} \\ \tau_L \end{pmatrix}$	$(\mathbf{1}, \mathbf{2}, -1/2)$	$m_e = 0.511 \cdot 10^{-3}, m_\mu = 1.05 \cdot 10^{-2}$
$E = e_R, \mu_R, \tau_R$	$(\mathbf{1}, \mathbf{1}, -1)$	$m_\tau = 1.77, m_\nu = ??$
Gauge bosons		
$g/G_\mu^A, A = 1 \dots 8$	$(\mathbf{8}, \mathbf{1}, 0)$	0.0
γ/A_μ	$(\mathbf{1}, \mathbf{1}, 0)$	0.0
W_μ^\pm	$(\mathbf{1}, \mathbf{3}, 0)$	80.379
Z_μ	$(\mathbf{1}, \mathbf{3}, 0)$	91.1876
The Higgs boson		
h	$(\mathbf{1}, \mathbf{2}, 1/2)$	125.10

Table 1.1. The SM constituents, their multiplicities with respect to the SM gauge group $G_{\text{SM}} := SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ and masses. The mass of the neutrinos ν is zero according to the SM prediction, but observations suggest that they are massive, and only the difference between the three masses is known [10]. The values of the masses are taken from the Particle Data Group (PDG) [4], and used throughout this thesis.

by looking at the mass term of a spin 1 field B_μ^A

$$\mathcal{L} = m_B B^{A,\mu} B_\mu^A, \quad (1.2)$$

and performing an $SU(N)$ gauge transformation

$$B_\mu^A \rightarrow B_\mu^A + \partial_\mu \Lambda^A + g \varepsilon_{BC}^A B_\mu^B \Lambda^C. \quad (1.3)$$

We see that the mass term is invariant under these transformations. Secondly, because the SM is a chiral theory, as only left-handed fermions would be doublets under $SU(2)_L$, the Dirac mass term

$$\mathcal{L}_D = m_D \bar{\psi}_L \psi_R + \text{h.c.}, \quad (1.4)$$

cannot be a singlet under $SU(2)_L$, hence also violating the EW symmetry. Despite quark and lepton masses being forbidden by the EW symmetry, we indeed observe that they do have a mass, and since they also carry charges this mass has to be a Dirac mass.

In order for the EW model to be consistent at the ground state like it is in the interaction states. A mechanism for spontaneous symmetry breaking going from an interaction state to the vacuum ought to be introduced.

1.1.1 Nambu-Goldstone theorem

Coming back to the example of the paramagnetic-ferromagnetic materials, when heated above a certain temperature, known as the **Curie Temperature** T_C will undergo a phase transition and become paramagnetic (losing their permanent magnet property), in the mean-field theory approximation the magnetic susceptibility is related to the temperature of the metal via the relation

$$\chi_B \sim (T - T_C)^{-\gamma}, \quad (1.5)$$

where γ is a critical exponent. We see that if the metal temperature $T > T_C$ the metal is in an *disordered phase* and when $T < T_C$ it is in the *ordered phase*, i.e. χ_B is the **order parameter** of this system. At the Curie temperature, the system will be at the *critical point* where the susceptibility is divergent. The exponent γ is not used to describe the system at the critical point. There is a “pictorial” description of the metal at the critical point which is helpful in picturing the Goldstone theorem. Starting at $T > T_C$, the metal would be in a paramagnetic phase, where the spins are randomly arranged. As the temperature becomes lower and lower, thermal fluctuations start to lessen. One or more regions of the metal, some of the spins will start to get aligned. With continued cooling, nearing T_C , these turned spins will affect their neighbours turning them into their directions. At the critical point $T = T_C$, the system behaves in a peculiar manner, when one would see regions of spins in “up” and others in “down” directions. The system will resemble a fractal of these regions, becoming scale-invariant. Additionally, waves of oscillating local magnetisation will propagate. These waves, or spinless quasiparticles (called **Magnons**) are Goldstone bosons emerging from spontaneous symmetry breaking.

Which will manifest at $T < T_C$ as the spins will be arranged in a certain single direction and the metal becomes ferromagnetic.

Theorem 1 (Nambu-Goldstone). When a continuous symmetry has a conserved currents but broken in the ground state (vacuum) is called to be spontaneously broken. There is a scalar boson associated with each broken generator of this spontaneously broken symmetry. The modes of these bosons are fluctuations of the order parameter.

This theorem first emerged from condensed matter physics, particularly superconductors [18, 19]. However, it soon got applied to relativistic quantum field theories [20].

1.2 The Higgs mechanism

In order to solve the aforementioned shortcomings of the Weinberg-Salam model, Nambu-Goldstone theorem has been first proposed by P. W. Anderson [21]. However, the way that Anderson formulated his theory was unfamiliar to particle physicists and used a non-relativistic picture to illustrate how photons could gain mass in an electron plasma with a plasma frequency ω_p

$$m_\gamma^{\text{plasma}} = \frac{\hbar\omega_p}{c^2} \quad (1.6)$$

Later on, a theory that explains the mass generation of the EW gauge bosons has been published in an almost simultaneous manner by R. Braut and F. Englert [22], P. Higgs [23] and G. Guralnik, C. R. Hagen, and T. Kibble [24, 25]². The Higgs mechanism starts by considering the spontaneous symmetry breaking (SSB) of the EW sector of the SM via the pattern

$$SU(2)_L \otimes U(1)_Y \longrightarrow U(1)_Q \quad (1.7)$$

This is achieved by the vacuum expectation value (vev) of a complex scalar field $\phi \sim (\mathbf{1}, \mathbf{2}, +1/2)$, with the Lagrangian

$$\mathcal{L} = D_\mu \phi^* D^\mu \phi - V, \quad V := \mu^2 \phi^* \phi + \lambda(\phi^* \phi)^2, \quad (1.8)$$

with V denoting the Higgs potential, illustrated in Figure 1.2, which gives non-vanishing vacuum for $\mu^2 < 0$. The field ϕ is given explicitly by

$$\phi = \begin{pmatrix} \phi^1 + i\phi^2 \\ \frac{1}{\sqrt{2}}(h + v) - i\phi^3 \end{pmatrix} \quad (1.9)$$

The covariant derivative

$$D_\mu = \partial_\mu - ig_2 \frac{\sigma_a}{2} W_\mu^a - ig_1 \frac{1}{2} B_\mu, \quad (1.10)$$

²All of these authors have contributed to the theory of SM spontaneous symmetry breaking (SSB). By calling it the “Higgs” mechanism or boson. I, by no means, have intended to ignore the role played by the rest, rather, I wanted to stick the most widely-used terminology in the field.

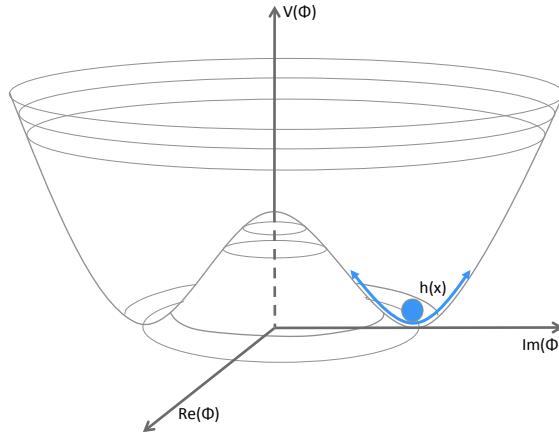


Figure 1.2. The characteristic shape of the Higgs potential showing a non-zero vacuum. While the physical Higgs boson is an oscillation within the energy well illustrated in the diagram with blue arrows., this illustration is taken from [26].

dictates the coupling between the Higgs field and the EW gauge bosons and g_3 , g_2 and g_1 are, respectively, the coupling constants of $SU(3)_C$, $SU(2)_L$ and $U(1)_Y$. The minimum of the scalar potential is then obtained by

$$\frac{\partial V}{\partial \phi} |_{\phi \rightarrow v} = 0, \quad (1.11)$$

which for a tachyonic mass $\mu^2 < 0$ will have a real non-vanishing values v corresponding to the vev of this field $\langle \phi \rangle = (\frac{0}{\sqrt{2}})$.

According to Nambu-Goldstone theorem, the three broken generators of $SU(2)_L \otimes U(1)_Y$ will become massive, and they are the W^\pm and Z bosons, while the photon will remain massless. We will have three massless Goldstone bosons $G^\pm = \frac{1}{2}(\phi^1 \pm i\phi^2)$ and $G^0 = \phi^3$ that are “eaten” by the aforementioned massive photons. Where they become the longitudinal polarisations of W^\pm and Z boson. In order to see this more concretely, we start by looking at the terms of the EW Lagrangian where the field ϕ couples to the gauge bosons, in the unbroken phase

$$D_\mu \phi^* D^\mu \phi = \frac{1}{2} |\partial_\mu \phi|^2 + \frac{1}{8} g_2^2 |\phi|^2 |W_\mu^1 + iW_\mu^2|^2 + \frac{1}{8} |\phi|^2 |g_2 W_\mu^3 - g_1 B_\mu|^2 \quad (1.12)$$

After SSB, we write the gauge bosons in the mass basis

$$\begin{aligned} W_\mu^\pm &= \frac{1}{\sqrt{2}}(W_\mu^1 \pm iW_\mu^2), \\ Z_\mu &= \frac{1}{\sqrt{g_1^2 + g_2^2}} (g_2 W_\mu^3 - g_1 B_\mu), \\ A_\mu &= \frac{1}{\sqrt{g_1^2 + g_2^2}} (g_2 W_\mu^3 + g_1 B_\mu). \end{aligned} \quad (1.13)$$

From this, the electric charge is identified as the coupling constant to the photon A_μ

$$e = \frac{g_1}{\sqrt{g_1^2 + g_2^2}}. \quad (1.14)$$

It is useful to define **Weinberg angle** θ_W , an important EW parameter relating the electric charge to the weak coupling g_2

$$\sin \theta_W = \frac{e}{g_2} \approx 0.231214, \quad (1.15)$$

typically the sin and cos of the Weinberg angle are denoted by s_W and c_W , respectively. We use the unitary gauge, to absorb the Goldstone bosons into the W^\pm and Z longitudinal polarisations. In this gauge the Higgs doublet can be written as

$$\phi \rightarrow \begin{pmatrix} 0 \\ \frac{1}{\sqrt{2}}(h + v) \end{pmatrix}, \quad v = 246 \text{ GeV}. \quad (1.16)$$

With these substitutions, one can read off the masses of the gauge bosons their bilinear terms in (1.12)

$$m_W = \frac{v g_2}{2} \quad m_Z = \frac{v}{2} \sqrt{g_1^2 + g_2^2} \quad m_A = 0. \quad (1.17)$$

Since ϕ is a complex doublet. We have seen that it has four components, and three of them correspond to the Goldstone bosons, thus one remains physical h which is what we now identify with the “Higgs boson” discovered in the Summer of 2012 [27, 28]. The couplings between the Higgs and the electroweak bosons is related to their mass via the vev

$$g_{hVV} = \frac{2m_V^2}{v}, \quad g_{hhVV} = \frac{2m_h^2}{v^2}. \quad (1.18)$$

By substituting (1.16), into the Higgs potential (1.8) one can write the mass of the physical Higgs boson in terms of the vev

$$m_h = \sqrt{2\lambda}v. \quad (1.19)$$

The physical Higgs mass is related to the μ parameter via the relation

$$m_h^2 = -2\mu^2, \quad (1.20)$$

One can see that the mass term after SSB changes its sign, characterising the order-parameter for this system, analogous to the magnetic susceptibility for the magnetisation of materials example. One could also identify the self-couplings of h , the trilinear and quartic couplings

$$g_{hhh} = 3\lambda v = 3\frac{m_h^2}{v}, \quad g_{hhhh} = 3\lambda = 3\frac{m_h^2}{v^2}. \quad (1.21)$$

1.3 Yukawa interaction

It is possible to also use the Higgs vev to give fermions their masses by introducing a Yukawa-interaction terms, first introduced by S. Weinberg [9]

$$\mathcal{L}_{\text{Yuk}} = -y_e \bar{L} \phi E - y_d \bar{Q} \phi D - y_u \bar{Q} \tilde{\phi} U + \text{h.c.}, \quad (1.22)$$

with $\tilde{\phi} = i\sigma_2\phi$ and y_e, y_d, y_u are 3×3 matrices. These matrices are free parameters in the SM. As the Higgs boson acquires a the vev, the fermions will acquire a mass $m_f = vy'_f$ and the Higgs boson coupling to the fermions is given by

$$g_{h\bar{f}f} = \frac{m_f}{v}, \quad (1.23)$$

and the Yukawa matrices will be fixed in the mass basis y'_f by measurements of the fermion masses.

Leptonic Yukawa matrix is diagonal, with a degeneracy between the flavour and masses basis, this manifests as lepton family number conservation (the lepton family operator commutes with the Hamiltonian.). However, for the quarks, the situation is more complicated. One can rotate these matrices to the mass basis via a bi-unitary transformation via the unitary matrices $\mathcal{V}_Q, \mathcal{U}_Q$ for $q = u, d$

$$y_q \longrightarrow y'_f = \mathcal{V}_q^\dagger y_q \mathcal{U}_q = \text{diag}(m_{q_1}, m_{q_2}, m_{q_3}). \quad (1.24)$$

However, there is no degeneracy here as the Hamiltonian does not commute with the quark flavour operator. This is because the transformation matrices for the up and down-type quarks are not the same. The charged EW quark currents contains flavour mixing described by the Cabibbo-Kobayashi-Maskawa (CKM) matrix [29, 30]. More details on the flavour sector of the SM is discussed in ??

Figure 1.3 shows all the SM couplings' strengths, with the thickness of the chord is proportional to the strength of the coupling, one can see the Higgs couplings in orange. In this figure, we cannot easily see Higgs coupling to the fermions, except for its couplings to the third generation. Strictly speaking, if we further examined the Yukawa coupling using a logarithmic scale and focused on the quark sector as Figure 1.4 illustrates. We

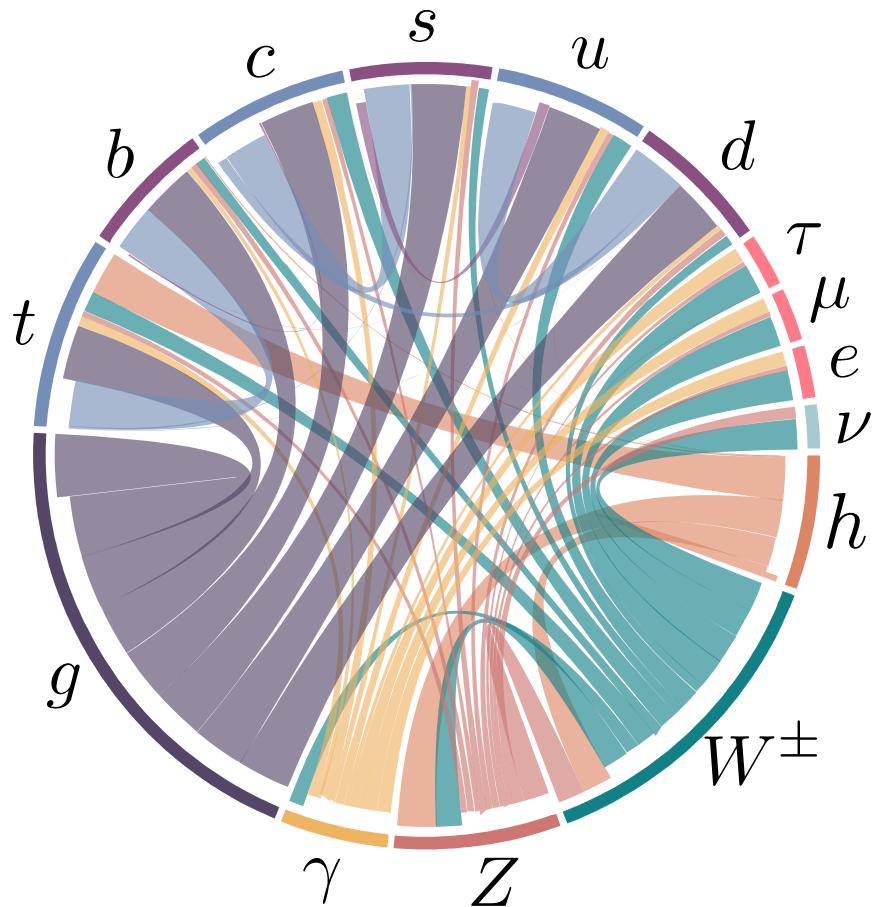


Figure 1.3. The SM Yukawa couplings are proportional to the quark masses, because of the the Higgs Yukawa couplings span about 6 orders of magnitude, as seen in the case of quarks here. This large hierarchy cannot be explained by the SM.

observe that these Yukawa couplings span about 6 orders of magnitudes with marked hierarchy amongst generations. As these couplings are in fact free parameters in the SM, and only determined by the experimental measurements of the quark (or equally applies lepton) masses. This hierarchy of quark masses therefore cannot be explained by the SM Higgs mechanism, and sometimes known as the old flavour puzzle.

In later chapters, we will examine the experimental effort to better measure these couplings and how Higgs pair production can be used to probe them in ???. Even the potential of using techniques from *interpretable machine learning* to further improve Higgs pair sensitivity to probing light Yukawas ???. Then in ?? we'll examine the EFT and UV models to modify them.

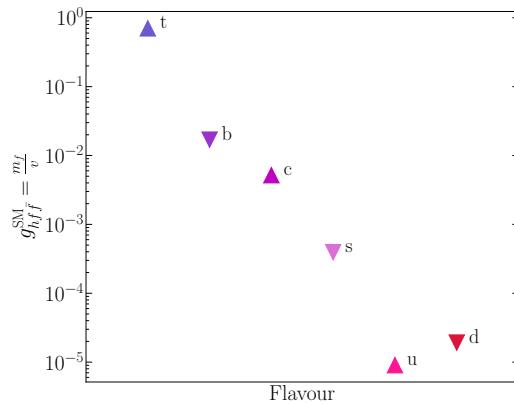


Figure 1.4. A chord diagram showing the SM couplings, with the coupling strength illustrated by the chord thickness. Higgs couplings are coloured in orange.

1.4 The Higgs and EW precision observables

Higgs physics is intertwined with the EW sector for example, the Higgs vev is determined from Fermi's constant $v = (\sqrt{2}G_F)^{-1/2}$, and is fixed by muon lifetime measurements, and comparing it with the theoretical predictions [31–34]

$$\tau_\mu^{-1} = \frac{G_F^2 m_\mu^5}{192\pi^3} \left(1 - \frac{8m_e^2}{m_\mu}\right) \left[1 - 1.810 \frac{\alpha}{\pi} + (6.701 \pm 0.002) \left(\frac{\alpha}{\pi}\right)^2\right], \quad (1.25)$$

which leads to the numerical value of G_F [4]

$$G_F = 1.1663787(6) \cdot 10^{-5} \text{ GeV}^{-2}, \quad (1.26)$$

given the value of the fine structure constant $\alpha^{-1} = 137.03599976(50)$.

Another important EW precision observable (EWPO) is the ratio between the W and

Z masses

$$\rho = \frac{m_W^2}{c_W^2 m_Z^2}. \quad (1.27)$$

At leading order, this parameter is equal to unity in the SM. The ρ parameter depends on the representation of the scalar sector of the EW model having ϕ_i scalars with T_i weak isospin and $T_{3,i}$ being its third component, and a vev v_i , via the relation [35, 36]

$$\rho = \frac{\sum_i [T_i(T_i + 1) - T_{3,i}^2] v_i^2}{2 \sum_i T_{3,i}^2 v_i^2}. \quad (1.28)$$

From (1.28) one can see that a real triplet scalar, for instance, would not fit the experimental EW measurement of ρ . Hence, a complex doublet is the simplest scalar possible for the EW symmetry breaking, and the Higgs boson was expected to be seen almost four decades before its discovery. However, radiative corrections to the EW gauge bosons mass from vacuum polarisation diagrams could potentially cause ρ to deviate significantly from unity. This is not the case, as the experimentally measured value of ρ [4]

$$\rho_{\text{exp}} = 1.00038 \pm 0.00020 \quad (1.29)$$

Additionally, it is possible to think of an extended Higgs sector, where there are multiple scalars with different $SU(2)_L$ multiplicities. Or, a composite Higgs sector, where the Higgs boson is a pseudo Nambu-Goldstone boson, cf. [37, 38]. How can such models be built assuring the ρ parameter is protected from change? The answer to this question lies in a symmetry of the Higgs Lagrangian known as custodial symmetry.

1.4.1 Custodial symmetry

After SSB, a residual global symmetry known as the custodial symmetry protects the ρ parameter from obtaining large radiative corrections at higher orders in perturbation theory. This symmetry must be kept in extended or composite Higgs models. This symmetry can be seen by rewriting the Higgs potential as

$$V = \frac{\lambda}{4} (\phi_1^2 + \phi_2^2 + \phi_3^2 + \phi_4^2 - 2\mu^2)^2. \quad (1.30)$$

This potential is invariant under $SO(4) \simeq SU(2)_L \otimes SU(2)_R$ rotations. However, when the Higgs field squires a non-vanishing vev, $\phi_4 \rightarrow h + v$, the potential becomes

$$V = \frac{\lambda}{4} (\phi_1^2 + \phi_2^2 + \phi_3^2 + h^2 + 2vh + v^2 - 2\mu^2)^2, \quad (1.31)$$

which is only invariant under $SO(3) \simeq SU(2)_V$ transformations, the diagonal part of the original group. This global SSB pattern comes alongside the EW SSB of the gauge group $SU(2)_L \otimes U(1)_Y$ as global $SU(2)_L$ is itself the gauged $SU(2)_L$ group. Additionally the T^3 component of the $SU(2)_R$ global group is the gauged $U(1)_Y$ and the T^3 component of the custodial group $SU(2)_V$ is gauged as well and identified to be the electric charge

operator, i.e. the generator of $U(1)_Q$.

$$\underbrace{SU(2)_R}_{\supset U(1)_Y} \otimes \overbrace{SU(2)_L}^{\text{gauged}} \longrightarrow \underbrace{SU(2)_V}_{\supset U(1)_Q}. \quad (1.32)$$

This pattern indicates that the symmetry is already broken by the gauging of the diagonal part of $SU(2)_R$ (the hypercharge). The custodial symmetry is only *approximate* in the limit of $g_1 \rightarrow 0$, and $\rho = 1$ is a consequence of $g_1 \neq 0$. The symmetry breaking pattern $\mathbf{2} \otimes \mathbf{2} = \mathbf{3} \oplus \mathbf{1}$ also allows us to identify the Goldstone bosons as the custodial triplet and the physical Higgs h as the custodial singlet, explaining the electric charge pattern they have.

We could use the isomorphism between the special orthogonal and special unitary groups to parametrise the Higgs doublet as an $SU(2)_L \otimes SU(2)_R$ bidoublet

$$\mathcal{H} = (\tilde{\phi} \ \phi) = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_4 - i\phi_3 & \phi_1 + i\phi_2 \\ \phi_1 - i\phi_2 & \phi_4 + i\phi_3 \end{pmatrix}, \quad (1.33)$$

with the bi-unitary transformations

$$\mathcal{H} \longrightarrow \mathcal{U}_L \mathcal{H} \mathcal{U}_R^\dagger \quad (1.34)$$

which leaves any traces of the form $\text{Tr}(\mathcal{H}^\dagger \mathcal{H})$, invariant. The Higgs potential could be rewritten in terms of the bidoublet

$$V = -\frac{\mu^2}{2} \text{Tr}(\mathcal{H}^\dagger \mathcal{H} + \frac{\lambda}{4} (\text{Tr}(\mathcal{H}^\dagger \mathcal{H}))^2) \quad (1.35)$$

The vev is hence written in this representation as

$$\langle \mathcal{H} \rangle = \frac{v}{\sqrt{2}} \mathbb{1}_{2 \times 2}. \quad (1.36)$$

We can also look at the Yukawa sector, and observe that in the case where $y_u = y_d = y$, we can also write the left-handed and right-handed quarks as $SU(2)_L \otimes SU(2)_R$ bidoublets and $SU(2)_R$ doublets, respectively. Hence, the quark part of the Yukawa Lagrangian in (1.22) becomes

$$\mathcal{L}_{yuk} \supset \frac{y}{\sqrt{2}} (\bar{u}_L \ \bar{d}_L) \begin{pmatrix} \phi_4 - i\phi_3 & \phi_1 + i\phi_2 \\ \phi_1 - i\phi_2 & \phi_4 + i\phi_3 \end{pmatrix} \begin{pmatrix} u_R \\ d_R \end{pmatrix}, \quad (1.37)$$

which is invariant under custodial transformations, but when $y_u \neq y_d$, this Lagrangian term breaks custodial symmetry. Thus, the differences between the up-type and down-type quark masses $m_u - m_d$ are considered **spurions** of the custodial symmetry and one expects to see radiative corrections to ρ being proportional to these spurions.

In order to see this more concretely, we start by examining the radiative corrections

that could contribute to the deviation of ρ from unity, i.e. $\Delta\rho$ these corrections are known as the **oblique correction**. These oblique corrections come from electroweak vacuum polarisations $\Pi_{VV}(p^2)$, as shown in Figure 1.5, for more details on these corrections and their calculation see Refs.. [39, 40]

The 1-loop correction to the ρ parameter is given in terms of the Π_{VV} by

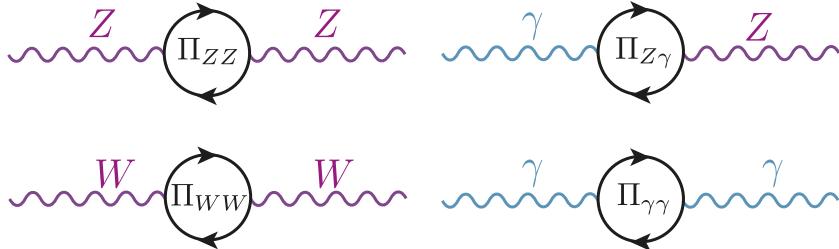


Figure 1.5. The oblique corrections, are radiative correction with electroweak gauge bosons propagators. Namely vacuum polarisations of the Z , W^\pm and γ bosons.

$$\Delta\rho = \frac{\Pi_{WW}(0)}{m_W^2} - \frac{\Pi_{ZZ}(0)}{m_Z^2} \quad (1.38)$$

Where the dominant contributions are given by [41]

$$\Delta\rho = \frac{3G_F}{8\sqrt{2}\pi^2} \left((m_t^2 + m_b^2) - \frac{2m_t^2 m_b^2}{m_t^2 - m_b^2} \ln \frac{m_t^2}{m_b^2} \right) + \dots \quad (1.39)$$

Since $m_b \ll m_t$, the correction is non-vanishing, and (1.39) shows clearly how the radiative corrections are proportional to the spurions of the custodial symmetry. However, this radiative correction is absorbed into the SM definition of ρ , i.e. the $\overline{\text{MS}}$ definition of the ρ -parameter $\rho^{\overline{\text{MS}}}$.

One can study new physics (NP) effects that violates custodial symmetry, by looking at deviations from $\rho = 1$ from it. Given the experimentally measured value of ρ (1.29) many NP models violating custodial symmetry can already be excluded. Nevertheless, ρ alone does not capture the full story of EWPO's. For instance, adding a new quark doublet would not necessarily violate the custodial symmetry though it still can be excluded by EWPO. It is hence useful to introduce new parameters known as **the oblique parameters** [40, 42–45] ³

³The are also called the Peskin–Takeuchi parameters, however, W. Marciano and J. Rosner also D. Kennedy and P. Langacker published the same parametrisation proposals almost simultaneously. Therefore, I preferred not to use this eponym, instead calling them the oblique parameters, as they stem from the oblique corrections .

The oblique parameters

$$\begin{aligned}
 S &:= \frac{4c_W^2 s_W^2}{\alpha} \left[\frac{\Pi_{ZZ}^{\text{NP}}(m_Z^2) - \Pi_{ZZ}^{\text{NP}}(0)}{m_Z^2} - \frac{c_W^2 - s_W^2}{c_W s_W} \frac{\Pi_{Z\gamma}^{\text{NP}}(m_Z^2)}{m_Z^2} - \frac{\Pi_{\gamma\gamma}^{\text{NP}}(m_Z^2)}{m_Z^2} \right], \\
 T &:= \frac{\rho^{\overline{\text{MS}}} - 1}{\alpha} = \frac{1}{\alpha} \left[\frac{\Pi_{WW}^{\text{NP}}(0)}{m_W^2} - \frac{\Pi_{ZZ}^{\text{NP}}(0)}{m_Z^2} \right], \\
 U &:= \frac{4s_W^2}{\alpha} \left[\frac{\Pi_{WW}^{\text{NP}}(m_W^2) - \Pi_{WW}^{\text{NP}}(0)}{m_W^2} - \frac{c_W}{s_W} \frac{\Pi_{Z\gamma}^{\text{NP}}(m_Z^2)}{m_Z^2} - \frac{\Pi_{\gamma\gamma}^{\text{NP}}(m_Z^2)}{m_Z^2} \right] - S.
 \end{aligned} \tag{1.40}$$

The NP contributions to the EW vacuum polarisations $\Pi_{VV}^{\text{NP}}(p^2)$ could either come from loop or tree-level effects. Typically both T and U are related to custodial symmetry violation. However, U has an extra suppression factor of m_{NP}^2/m_Z^2 compared to T and S . The most recent fit result for these parameters is [4]

$$\begin{aligned}
 S &= -0.01 \pm 0.10, \\
 T &= 0.03 \pm 0.13, \\
 U &:= 0.02 \pm 0.11.
 \end{aligned} \tag{1.41}$$

But since T and S tend to give stronger constraint on NP, due to the suppression factor of U . One can perform a two-parameter fit of S and T setting $U = 0$, thus shown in Figure 1.6, with the numerical values [4],

$$\begin{aligned}
 S &= 0.00 \pm 0.07, \\
 T &= 0.05 \pm 0.06.
 \end{aligned} \tag{1.42}$$

The Peskin-Takeuchi parameters are important in constraining effective operators in the Higgs sector , namely

$$\begin{aligned}
 \hat{O}_S &= \phi^\dagger \sigma_i \phi W_{\mu\nu}^i B^{\mu\nu}, \\
 \hat{O}_T &= |\phi^\dagger D_\mu \phi|^2.
 \end{aligned} \tag{1.43}$$

For example, \hat{O}_S appears in Technicolour models causing large deviations of S compared to its measured value [43, 46–48]. Moreover, The constraints on T parameter is important for top mass generation ans well as modifications to $Z b\bar{b}$ coupling in such models [49, 50]. We will revisit the \hat{O}_T when we discuss the Higgs and effective field theories in chapter 3

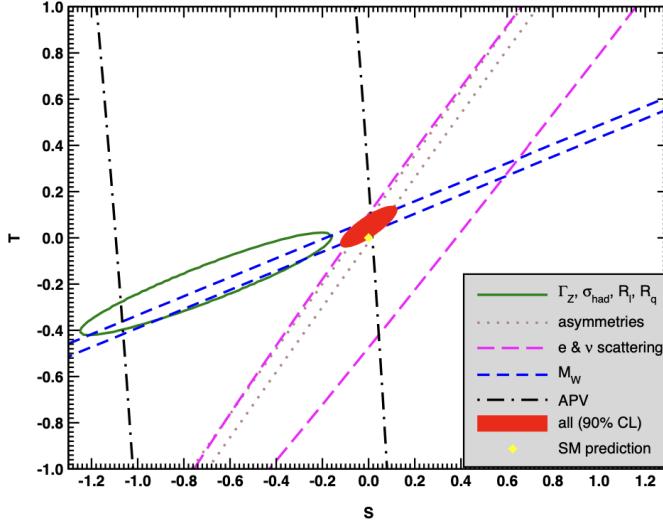


Figure 1.6. Fit results from various EWPO's for T and S setting $U = .$ The contours show 1σ contours (39.35% for closed contours and 68% for the rest). This plot is obtained from the PDG [4]

1.5 Theoretical constraints on the Higgs

1.5.1 Electroweak precision data fits

Even prior to the discovery of the Higgs boson at LHC in 2012, many theoretical aspects of the Higgs sector provided marked bounds on the Higgs properties, particularly its mass. For instance, using the EWPO measurements at LEP provided an input for a fit based of radiative effects coming from the Higgs boson to such observables [11] as in diagram (a) of Figure 1.8, the bounds improved with the improvements of EWPO measurements, these bounds were known as the “blue band” plots seen with their progression in Figure 1.7.

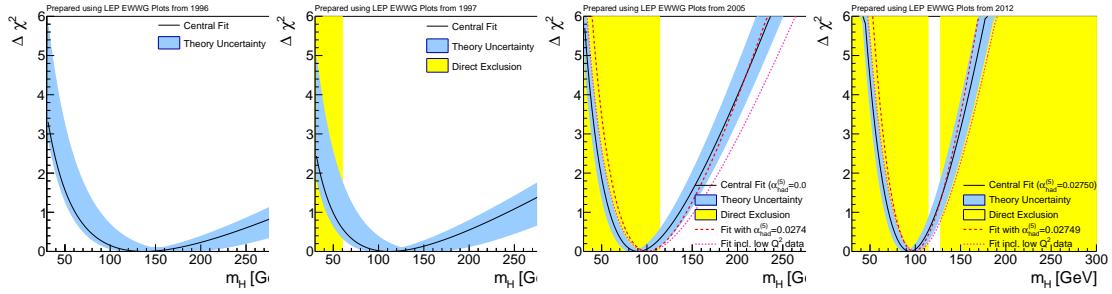


Figure 1.7. Progression of the “blue band” plots with LEP data from 1996 up to 2021 prior to the announcement of the Higgs boson discovery. These plots were taken from [26], based on data from LEP [11]

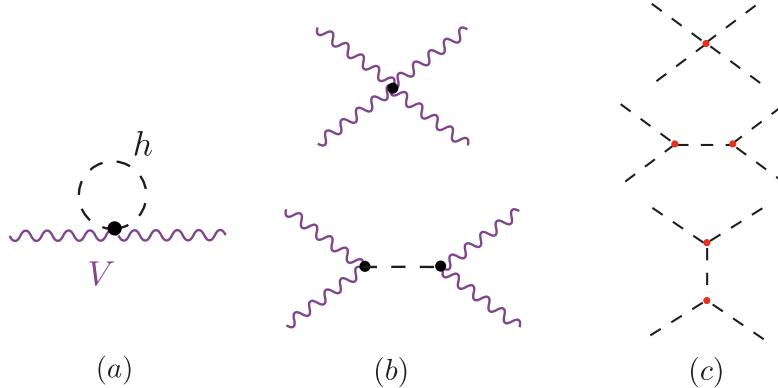


Figure 1.8. Diagrams contributing to theoretical bounds on the Higgs, (a) shows an example of radiative corrections to EWPO from the Higgs bosons. The diagrams in (b) show an elastic scattering of EW vector bosons leading to a bound on the Higgs mass from perturbative unitarity, similarly in (c) diagrams for $hh \rightarrow hh$ scattering leading to constraints on Higgs self-coupling.

1.5.2 Partial-wave unitarity

Another bound on Higgs mass emerged from studying the amplitudes of EW vector bosons elastic scattering having longitudinal polarisations $V_L V_L \rightarrow V_L V_L$ at high energies $E \gg m_W$ (see diagrams (b) in Figure 1.8), where the Goldstone equivalence theorem holds [51]. This bound comes from applying the partial wave perturbative unitarity on the EW boson scattering amplitude. I will derive here this bound starting from the **Optical theorem**, which a direct result from the unitarity of the **S** matrix.

The optical theorem

Let \mathcal{M}_{aa} be a covariant matrix element for an elastic scattering process with for a particle a then the following relation applies

$$\sum_f \int d\Phi_n(p_a, p_i^f) |\mathcal{M}_{af}|^2 = 2\Im(\mathcal{M}_{aa}), \quad (1.44)$$

where the sum is over all intermediate states n -particle states f with momenta p_i^f and $d\Phi_n(p_a, p_i^f)$ is the n -particle phase space.

If we only consider a $2 \rightarrow 2$ process with momentum states. $|p_1, p_2\rangle \rightarrow |k_1, k_2\rangle$, then (1.44), after expanding the 2-particle phase space , simplifies to

$$\begin{aligned} & \int \frac{d^3 k_1}{(2\pi)^3 2E_1} \int \frac{d^3 k_2}{(2\pi)^3 2E_2} (2\pi)^4 \delta^4(p_1 + p_2 - k_1 - k_2) |\mathcal{M}(s, t)|^2, \\ &= \frac{1}{16\pi} \int_{-1}^1 d(\cos \theta) |\mathcal{M}(s, t)|^2, \end{aligned} \quad (1.45)$$

with the Mandelstam variables

$$\begin{aligned} s &= k_1 + k_2, \\ t &= k_1 - p_1, \\ u &= k_1 - p_2, \\ s + t + u &= 4m \end{aligned} \tag{1.46}$$

Recall that the relation between the Mandelstam variable t , and the scattering angle for the elastic scattering is given by

$$t = \frac{1}{2}(s - 4m^2)(\cos \theta - 1) \tag{1.47}$$

We could expand the matrix element $\mathcal{M}(s, t)$ in terms of *partial waves*, isolating s from scattering angle dependence

$$\mathcal{M}(s, t) = 16\pi \sum_j (2j + 1) a_j P_j(\cos \theta). \tag{1.48}$$

Where a_j are called the j th partial wave amplitude, and $P_j(\cos \theta)$ are the Legendre polynomials

$$P_j(z) = \frac{1}{j!} \frac{1}{2^j} \frac{d^j}{dz^j} (z^2 - 1)^j \tag{1.49}$$

Which satisfies the orthonormality condition

$$\int_{-1}^1 dz P_j(z) P_k(z) = \frac{1}{2j + 1} \delta_{jk} \tag{1.50a}$$

$$P_j(1) = 1 \quad \forall j. \tag{1.50b}$$

We hence get for the LHS of (1.44) scattering

$$\begin{aligned} &\int \frac{d^3 k_1}{(2\pi)^3 2E_1} \int \frac{d^3 k_2}{(2\pi)^3 2E_2} (2\pi)^4 \delta^4(p_1 + p_2 - k_1 - k_2) |\mathcal{M}(s, t)|^2, \\ &= \frac{1}{16\pi} \int_{-1}^1 d(\cos \theta) \left[16\pi \sum_j (2j + 1) a_j(s) P_j(\cos \theta) \right] \times \\ &\quad \left[16\pi \sum_k (2k + 1) a_k^*(s) P_k(\cos \theta) \right], \\ &\Rightarrow = 32\pi \sum_j (2j + 1) |a_j(s)|^2. \end{aligned} \tag{1.51}$$

And the RHS of (1.44)

$$2\Im(\mathcal{M}_{aa}) = \underbrace{2\Im(\mathcal{M}(s, 0))}_{t \text{ is integrated out.}} = 32\pi \sum_j (2j+1)\Im(a_j(s)). \quad (1.52)$$

Otherwise large cancellations needed, $a_j(s)$'s are hierachal. Thus, we could compare the partial wave amplitudes term-by-term

$$|a_j(s)|^2 \leq \Im(a_j(s)) \Rightarrow \Re(a_j(s))^2 + \Im(a_j(s))^2 \leq \Im(a_j(s)) \quad (1.53)$$

Rearranging terms, we get

$$\Re(a_j(s)) + \left(\Im(a_j(s)) - \frac{1}{2} \right)^2 \leq \frac{1}{4} \quad (1.54)$$

The partial wave amplitude has to lie within the unitarity circle. We use though perturbation theory if the partial wave amplitude respects the inequality

$$\Re(a_j(s)) \leq \frac{1}{2} \quad (1.55)$$

This is known as the perturbative partial wave unitarity bound.

When (1.55) is applied for $V_L V_L \rightarrow V_L V_L$, in the Goldstone boson equivalence theorem regime in particular for $V = W$ boson, we get for the S -wave partial amplitude

$$a_0 \sim \frac{m_h^2}{16\pi v^2} \left(2 + \mathcal{O}\left(m_h^2/s\right) \right). \quad (1.56)$$

Looking at the asymptotic behaviour as $s \rightarrow \infty$, we obtain the bound

$$\frac{m_h^2}{8\pi v^2} < \frac{1}{2} \Leftrightarrow m_h \leq 870 \text{ GeV}. \quad (1.57)$$

Indeed this bound is obsolete now after th Higgs mass measurement, however it is very important to demonstrate the power of this technique in constraining Higgs parameters. As this method can be applied to any elastic scattering with the Higgs acts as a mediator like $ZZ \rightarrow ZZ$, $WW \rightarrow ff$ and constrain the corresponding couplings g_{ZZh} , g_{ffh} and so on. An important bound can be derived by examining the Higgs elastic scattering $hh \rightarrow hh$ shown in (c) of Figure 1.8 in order to set bounds on Higgs self-interactions g_{hhh} and g_{hhhh} . This is what exactly has been done in ref. [52] where they have found that the S -wave partial amplitude for this process is given by

$$a_0 = -\frac{1}{2} \frac{\sqrt{s(s-4m_h^2)}}{16\pi s} \left[g_{hhh}^2 \left(\frac{1}{s-m_h^2} - 2 \frac{\log \frac{s-3m_h^2}{m_h^2}}{s-4m_h^2} \right) + g_{hhhh} \right], \quad (1.58)$$

which leads to unitarity bounds on the trilinear g_{hhh} and the quartic g_{hhhh} couplings

$$\left| g_{hhh}/g_{hhh}^{\text{SM}} \right| \lesssim 6.5 \quad \text{and} \quad \left| g_{hhhh}/g_{hhhh}^{\text{SM}} \right| \lesssim 65. \quad (1.59)$$

A stronger constrained can be obtained by looking at the one-loop correction to the $hh \rightarrow hh$ scattering amplitude, within the full kinematic range. The unitarity bound here is obtained by looking at the one-loop amplitude at the threshold, and is given by

$$\left| g_{hhhh}/g_{hhhh}^{\text{SM}} \right| \lesssim 6. \quad (1.60)$$

It should be noted that the unitarity bounds on κ_λ depends on the ansatz use estimating the size the New Physics contributions to the scattering amplitudes. These bounds are, hitherto, the strongest on these two couplings even when compared to the ones coming from current experimental searches.

1.5.3 Other bounds

Further theoretical bounds could be obtained by studying quantum effects on the Higgs potential. For example, if we looked at the solution of the renormalisation group equation (RGE) for the Higgs self-coupling λ with the boundary condition $\lambda(v) = \lambda_0$ and ignoring other SM particle-contributions

$$\lambda(Q^2) = \frac{\lambda_0}{1 - \frac{3}{4\pi^2} \log \frac{Q^2}{v^2}} \quad (1.61)$$

We see that the running of λ will hit a pole, known as **Landau pole** when the denominator vanishes. This will happen at the scale

$$Q_c = v e^{4\pi^2/3\lambda_0} = v e^{4\pi^2 v^2 / 3m_h^2} \quad (1.62)$$

This indicates that the theory will break down at scales larger or equal to Q_c . Since the “critical scale” is a function of the Higgs mass, this allows us to set an upper limit on the Higgs mass assuming the SM will be valid up to a certain scale Q_c . This bound is known as **quantum triviality** bound [53]. This is because the low energy behaviour of (1.61) leads to a vanishing interaction, and if we want the Higgs Lagrangian to be perturbative for all scales, then λ has to be vanishing and the theory becomes non-interacting or *trivial*.

Another bound coming from the RGE of λ is the **stability bound**, which considers the stability of the Higgs potential given the running of λ by requiring that the Higgs potential is an operator bounded from below. This bound is obtained by approximating the solution of the RGE at small λ

$$\lambda(Q^2) \sim \lambda_0 + \frac{1}{16\pi^2} \left[-\frac{12m_t^4}{v^4} + \frac{3}{16} (2g_2^4 + (g_2^2 + g_1^2)^2) \right] \log \frac{Q^2}{v^2} \quad (1.63)$$

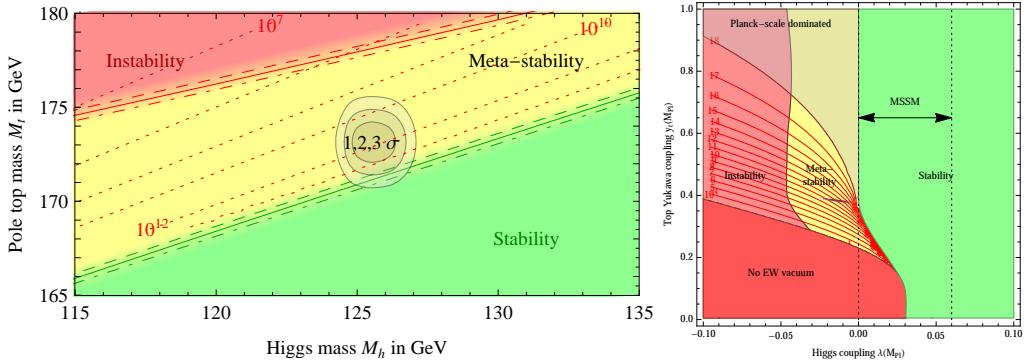


Figure 1.9. Phase diagrams of the Higgs vacuum in the $m_t - m_h$ (left) and $m_t - \lambda(M_{pl})$ (right) planes showing areas of instability, meta stability and absolute stability. In the $m_t - \lambda(M_{pl})$ diagram, the allowed range of the Higgs self-coupling λ in the Minimal Supersymmetric SM (MSSM), this plot is taken from [57]

For the Higgs potential to be bounded from below $\lambda(Q^2)$ ought to be $\lambda(Q^2) > 0$. With this relation for λ_0 in terms of the mass, we get a bound on m_h

$$m_h^2 > \frac{v^2}{8\pi^2} \left[-\frac{12m_t^4}{v^4} + \frac{3}{16} (2g_2^4 + (g_2^2 + g_1^2)^2) \right] \log \frac{Q^2}{v^2} \quad (1.64)$$

Which leads to $m_h \approx 130$ GeV if we assume that the SM is valid up to the Grand Unified Theory (GUT) scale of $\sim 10^{16}$ GeV and $m_h \approx 180$ GeV for Q being at the Planck scale $\sim 10^{19}$ GeV.

More sophisticated calculations and discussion for the Higgs potential and vacuum stability has been a subject of great interest in pre and post-Higgs discovery eras cf. [53–56] and the most state-of-the-art calculation for the vacuum stability at NNLO has been performed in ref. [57] where they also included finite temperature effects to construct a phase diagram in the $m_t - m_h$ and $m_t - \lambda(M_{pl})$ planes as shown in Figure 1.9. Indicating that the measured Higgs mass is likely compatible with a metastable vacuum rather than absolute stability. This indicates that there is a finite probability for the Higgs vacuum (false vacuum) to decay into a lower energy state (true vacuum) via quantum tunnelling.

2 Experimental measurements of the Higgs boson

The observation of the Higgs boson, then the extensive measurement of its properties and couplings has been on the top of the LHC programme priorities [58]. In the time this thesis was in the writing, the particle physics community will be celebrating a decade since the Higgs boson's discovery. Looking back 10 years ago, when I have witnessed the discovery of the Higgs boson via news press-conference in summer of 2012, and decided to be a part of this enormous step that humanity has taken, I feel astonished by the progress made in understanding this newly discovered particle!

In this chapter, I will start by an overview of the extraordinary LHC and its experiments in section 2.1. Then, I will review the state-of-the-art status of experimental measurements of the Higgs properties in section 2.2, cross-sections and couplings in section 2.3, and at the end I will discuss the challenges and outlook for the future runs of the LHC section 2.4, of which the rest of this thesis is going to be aimed to address a small part of them.

2.1 Overview of the Large Hadron Collider

The Large Hadron Collider (LHC) is the largest particle accelerator in the CERN accelerators complex, with a circumference of about 26 km, with over 9590 superconducting magnets cooled to 1.9 K. It was built as an upgrade to the Large electron positron collider (LEP) which ended its operation in the year 2000. The LHC contains four main experiments situated at the four beam collision points and detectors, and these experiments are: ATLAS, CMS, LHCb and ALICE, there also smaller experiments such as LHCf, MilliQan, TOTEM and others. For more details about the LHC cf. [59, 60] or see the LHC technical design report [61] for more technical details.

The LHC started operation in September of 2008, with low energy proton beams, then gradually increased to an energy of 3.5 TeV per proton to reach a centre of mass energy \sqrt{s} of 7 TeV, and data-taking period started from 2011. By 2012, its energy has increased to $\sqrt{s} = 8$ TeV and operated at this energy for about a year and half, then stopping in mid 2013 concluding what is known as **Run-I**. In 2015, the **Run-II** started with almost double the energy $\sqrt{s} = 13$ TeV, and lasted for ca. 3 years. As this thesis being written, preparations are being made to get **Run-III** started until 2024. During these runs, heavier nuclei such as ^{207}Pb and ^{131}Xe have been collided either with protons or with themselves [62].

From, 2025 and beyond, the **High-Luminosity LHC** (HL-LHC) era will commence,

see Figure 2.2. Where the LHC will be shutdown for extensive upgrades [63] to potentially increase its energy to $\sqrt{s} = 14$ TeV and higher collision rates hence the term *high luminosity*. Which leads us to an important notion in particle physics phenomenology *integrated luminosity*.

The performance of colliders depends on many factors, but for phenomenological studies, like this thesis, one mainly considers the centre of mass energy \sqrt{s} and the integrated luminosity \mathcal{L} . This is mainly due to the fact that particle colliders experiments are basically “counting experiments”, and all of the bounds on physical observables or model parameters are obtained from the number of signal versus background events, and the number of expected events N_{explic} for a given resonance R and a subsequent decay final state X at any collider experiments is given by

$$N_{explic} = \sigma(pp \rightarrow R) \mathcal{B}(R \rightarrow X) \mathcal{L} \epsilon_{SEL}. \quad (2.1)$$

Here ϵ_{SEL} is the selection efficiency, which depends on many factors like the detector geometry and particle identification performance etc., as well as the signal one searches for, it can be improved by better detected or selection cuts. The production cross-section increases typically with quadratically with \sqrt{s} , hence comes the need for higher energies but this can only achieved by building new colliders from scratch. The integrated luminosity can be increased much more easily, by longer running time of the same collider as it is the time integral of the collider’s luminosity $L(t)$ over its operation time T

$$\mathcal{L} = \int^T L(t). \quad (2.2)$$

Therefore, we see that the integrated luminosity for the LHC experiments will increase over time, when more collisions taking place, as seen in figure Figure 2.1 showing the integrated luminosity for ATLAS and CMS experiments. As the protons travel in the LHC in **bunches**, and as these bunches cross, protons collide at a certain frequency f , when two bunches with N_1 and N_2 protons per bunch, respectively. Each bunch will have an effective cross-section $4\pi\sigma_i$ corresponding to their physical sizes $\sigma \sim 16 \mu\text{m}$, the luminosity is therefore given -approximately- by

$$L = \frac{f N_1 N_2}{4\pi\sigma_1\sigma_2}, \quad (2.3)$$

which is for the LHC averages to about 10^{34} collisions $\text{cm}^{-2} \text{s}^{-1}$ [64, 65].

The total physics-viable pp -collisions integrated luminosity for Run-I was $4.57/\text{fb}$ for 7TeV and $20.3/\text{fb}$ for 8TeV (ATLAS [66]) and $5.55/\text{fb}$ at 7TeV and $21.8/\text{fb}$ at 8TeV (CMS [67]). As for Run-II the integrated luminosity is $139/\text{fb}$ at 13TeV (ATLAS [68]) and $137/\text{fb}$ at 13TeV (CMS [67]). The expected integrated luminosity by the end of Run-III is $300/\text{fb}$ [69] and $3000/\text{fb}$ by the end of the HL-LHC at energy of 14TeV [63].

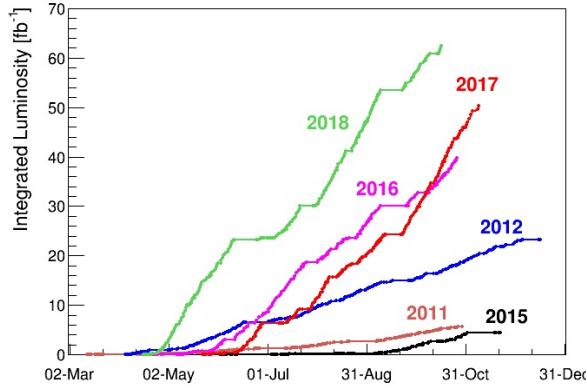


Figure 2.1. The integrated luminosity of the CMS and ATLAS experiments combined over the period from 2011-2018, source [64].



Figure 2.2. A timeline of the LHC operation showing Run-I, Run-II and future planned runs of the LHC, including the HL-LHC, source [62].

2.2 Higgs properties

2.2.1 Higgs boson mass measurements

In order to measure the mass of the Higgs boson with high precision, one needs to consider final states that can be reconstructed with high momentum and mass resolution, this is typically achieved when no hadronic constituents in the decays involved, such as

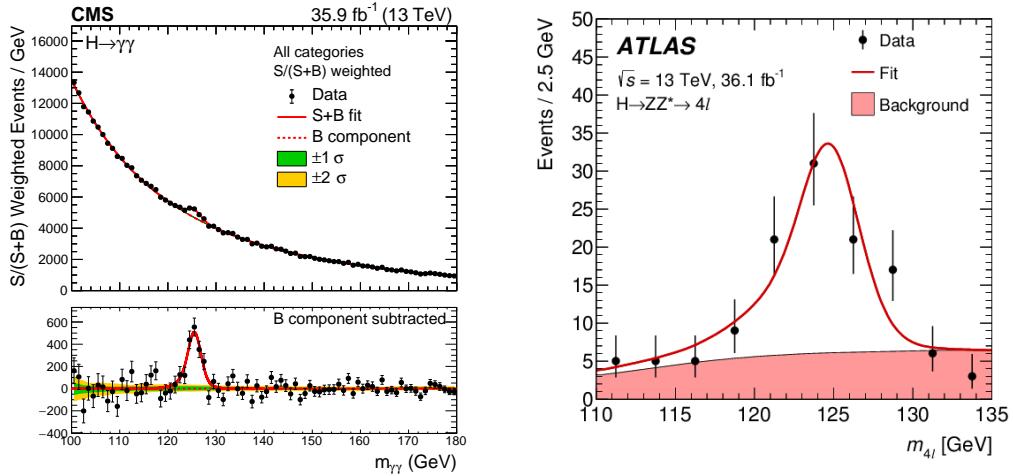


Figure 2.3. The invariant mass distributions of diphoton $m_{\gamma\gamma}$ (CMS [70]) and four lepton $m_{4\ell}$ (ATLAS [71]) final states showing a clear peak at the Higgs mass, with smooth background. These final states are ideal for Higgs mass measurements.

$h \rightarrow \gamma\gamma$ and $h \rightarrow ZZ^* \rightarrow 4\ell$. Reconstructing the invariant mass distributions $m_{\gamma\gamma}$ and $m_{4\ell}$ one observes that the Higgs peak is narrow over a relatively smooth background, see Figure 2.3, which is ideal for the measurement of the Higgs mass. It should be noted that the width of the resonance is due to the detector resolution and does not correspond to the actual Higgs width.

There have been consistent improvements of the Higgs mass measurements since its discovery. In Figure 2.4 I have performed a meta analysis on ATLAS and CMS measurements of the Higgs mass in Run-I and Run-II of the LHC for both diphoton and ZZ^* final states based on the data from the studies [70–73] using a random effects model [74]. The pooling of the studies yielded a mass measurement of $m_h = 125.21 \pm 0.10$, which translates to a 0.11% accuracy, the heterogeneity off the studies was found to be $I^2 = 49\%$ ($p = 0.05$). Different measurements combination techniques were used in [70] and [4] yielded different central values but all of the results agree within the uncertainties.

2.2.2 Higgs full width

The SM values of the Higgs boson full width is $\Gamma_h = 4.1$ GeV and it can be accessed in the LHC by looking at the ratio of on-shell versus off-shell Higgs production and decay to the $ZZ^{(*)}$ state, and $ZZ^{(*)} \rightarrow 4\ell, 2\ell 2\nu$, namely

$$\frac{\sigma(gg \rightarrow h \rightarrow ZZ^*)}{\sigma(gg \rightarrow h^* \rightarrow ZZ)} = \kappa_g^2 \kappa_Z^2 \frac{4m_Z^2}{m_h \Gamma_h}, \quad (2.4)$$

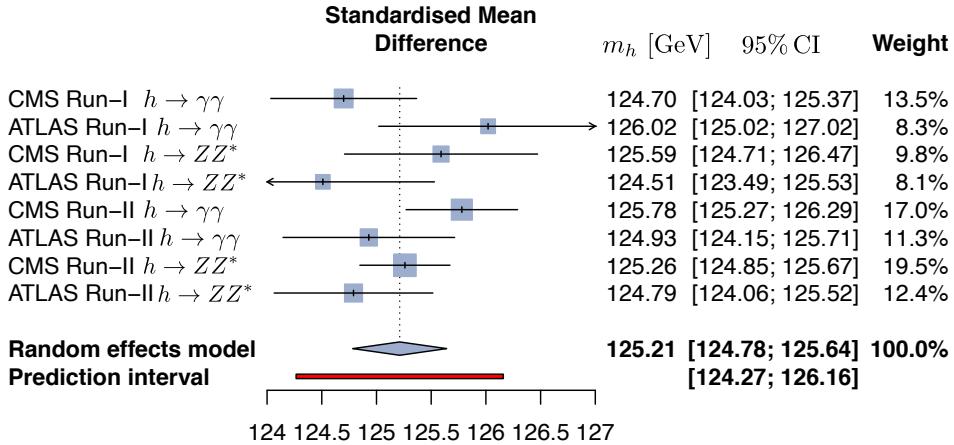


Figure 2.4. A meta analysis preformed to combine all the measurements of the Higgs mass from Run-I and Run-II, the combined result was obtained from pooling all of the studies using the random effects model method.

where the κ here denote the ratio between the measured/ or modified coupling with the Higgs and the SM prediction, i.e.

$$\kappa_X := \frac{g_{XXh}}{g_{X}^{SM}}. \quad (2.5)$$

Which is commonly used in reporting experimental constrains/ measurements of the Higgs couplings, as in the next section [section 2.3](#). We shall discuss the κ formalism more in [chapter 3](#).

We see from (2.4) that if one fixes the coupling between the gluons and the Z boson and the Higgs it is possible to access the full width directly. Unfortunately, it is not possible to directly measure the Higgs full width at the LHC, as this requires full reconstruction of the collision event and study the recoil mass which is only possible at lepton colliders [75, 76]. Alas, it is still possible to extract bounds on Γ_h using (2.4). ATLAS used this method to constrain the full width of the Higgs using Run-II data [77], while CMS has preformed the same analysis using Run-I and Run-II data combined [78], the results are

95% CL bounds of Γ_h

$$\Gamma_h < 14.4 \text{ GeV} \quad (\text{ATLAS}) \qquad 0.08 \text{ GeV} < \Gamma_h < 9.16 \text{ GeV} \quad (\text{CMS}), \quad (2.6)$$

with the combined bound being $\sim 3\Gamma_h^{\text{SM}}$.

2.2.3 Higgs spin and parity

As we have seen in section 1.2, the Higgs boson is a scalar and \mathcal{CP} even ($J^p = 0^+$) in the SM. However, the discovery of a peak in the $m_{\gamma\gamma}$ distribution, would not automatically imply that the particle discovered is scalar, it could be a spin-2 boson, or a pseudoscalar ($J^p = 0^-$). In order to study the J^p properties of the Higgs, one needs to examine the differential distributions of angular variables such as rapidity y or transverse momentum p_T . Both ATLAS and CMS collaborations studied using Run-I data the angular distributions of the Higgs decays $h \rightarrow ZZ^*$, $h \rightarrow WW^*$ and $h \rightarrow \gamma$, to study an anomalous VVh coupling. Then test the alternative hypothesis for J^p against the SM [79, 80]. The analysis results show that the SM 0^+ hypothesis is favoured at $> 99.9\%$ CL.

2.3 Measurements of Higgs rates and couplings

2.3.1 Higgs cross-sections

The total inclusive Higgs cross-section has been measured using the final states $h \rightarrow \gamma\gamma$ and $h \rightarrow ZZ^* \rightarrow 4\ell$, and their combinations. The measurements have been done at the three energies the LHC was operating at: 7 TeV, 8 TeV [81] and 13 TeV [82–84] and combined with more data and compared to the SM prediction as shown in [85]. As shown in Figure 2.5, the measured inclusive cross-section is in agreement with the SM prediction across all of the LHC operation energies.

In addition to the inclusive cross-section measurements, differential cross-sections of the Higgs have been measured for p_T and y as we have seen in subsection 2.2.3 for Higgs's J^p determination. Additionally, the differential cross-sections for other variables have been measured, and they include $N_{\text{jets}}, p_T^{\text{jet}}, m_{jj}, \delta\phi_{jj}$ and others using the channels $h \rightarrow ZZ^*$, $h \rightarrow WW^*$ and $h \rightarrow \gamma$. The most recent results using the full Run-II data can be found in Refs. [83, 85–87].

In addition to the total inclusive cross-section, a collection of measurements of Higgs production and decay rates has been carried out by both ATLAS and CMS. These measurements also carried out in what is known as Standard Template Cross-Sections (STXS) framework. The STXS's are fiducial cross-sections in exclusive phase-space regions or bins separately per Higgs boson production channel. They have the advantage of standardisation of cuts and final results such that measurements could be easily combined across analyses. More details about the STXS framework can be found in the reports of LHC Higgs cross-sections working group (LHCHXSWG) cf. [88]. In Table 2.1 I summarise the state-of-art measurements of the Higgs rates separated into production and decay channels using the total LHC Run-II data from ATLAS and CMS experiments. Additionally,

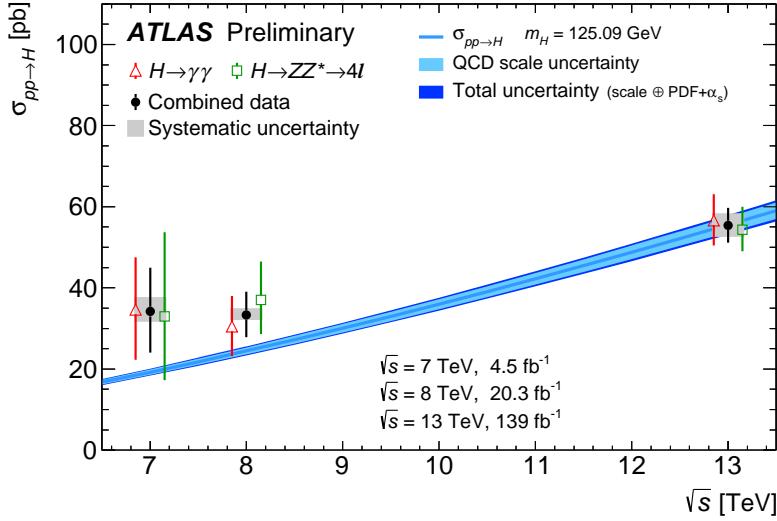


Figure 2.5. The total inclusive cross-section measurements by ATLAS collaboration [85] for 7, 8 and 13 TeV using $h \rightarrow \gamma\gamma$ and $h \rightarrow ZZ^* \rightarrow 4\ell$. channels and their combination (black points) compared to the SM prediction with the uncertainties shown as blue line with light and dark blue bands for QCD scale uncertainties and total uncertainties, respectively.

I give the HL-LHC projections from CMS experiment as a comparison. The results in this table are written in terms of the signal strength, which is directly extracted from measuring the number of events dividing them by the standard model,

$$\mu_{\text{Exp}} := \frac{\sigma \cdot \mathcal{B}}{\sigma^{\text{SM}} \cdot \mathcal{B}^{\text{SM}}} \quad (2.7)$$

Production	Decay	$\mu_{\text{Exp}} \pm \delta\mu_{\text{Exp}}$ (symmetrised)		Ref.	
		LHC Run-II			
		CMS 137 fb^{-1}	ATLAS 139 fb^{-1}		
ggF	$h \rightarrow \gamma\gamma$	0.99 ± 0.12 1.030 ± 0.110		1.000 ± 0.042 [89–91]	
	$h \rightarrow ZZ^*$	0.985 ± 0.115 0.945 ± 0.105		1.000 ± 0.040	
	$h \rightarrow WW^*$	1.285 ± 0.195 1.085 ± 0.185		1.000 ± 0.037 [89, 91, 92]	
	$h \rightarrow \tau^+\tau^-$	0.385 ± 0.385 1.045 ± 0.575		1.000 ± 0.055	
	$h \rightarrow b\bar{b}$	2.54 ± 2.44 —		1.000 ± 0.247 [91, 92]	
	$h \rightarrow \mu^+\mu^-$	0.315 ± 1.815 —		1.000 ± 0.138 [91, 92]	
VBF	$h \rightarrow \gamma\gamma$	1.175 ± 0.335 1.325 ± 0.245		1.000 ± 0.128 [89–91]	
	$h \rightarrow ZZ^*$	0.62 ± 0.41 1.295 ± 0.455		1.000 ± 0.134	
	$h \rightarrow WW^*$	0.65 ± 0.63 0.61 ± 0.35		1.000 ± 0.073 [89, 91, 92]	
	$h \rightarrow \tau^+\tau^-$	1.055 ± 0.295 1.17 ± 0.55		1.000 ± 0.044	
	$h \rightarrow b\bar{b}$	— 3.055 ± 1.645		— [89]	
	$h \rightarrow \mu^+\mu^-$	3.325 ± 8.075 —		1.000 ± 0.540 [91]	
$t\bar{t}h$	$h \rightarrow \gamma\gamma$	1.43 ± 0.30 0.915 ± 0.255		1.000 ± 0.094 [89–91]	
	$h \rightarrow VV^*$	$0.64 \pm 0.64 (ZZ^*)$ $0.945 \pm 0.465 (WW^*)$ 1.735 ± 0.545		$1.000 \pm 0.246 (ZZ^*)$ $1.000 \pm 0.097 (WW^*)$ —	
	$h \rightarrow \tau^+\tau^-$	0.845 ± 0.705 1.27 ± 1.0		1.000 ± 0.149 [89, 91, 92]	
	$h \rightarrow b\bar{b}$	1.145 ± 0.315 0.795 ± 0.595		1.000 ± 0.116	
Vh	$h \rightarrow \gamma\gamma$	0.725 ± 0.295 1.335 ± 0.315		$1.000 \pm 0.233 (Zh)$ $1.000 \pm 0.139 (W^\pm h)$ [89–91]	
	$h \rightarrow ZZ^*$	1.21 ± 0.85 1.635 ± 1.025		$1.000 \pm 0.786 (Zh)$ $1.000 \pm 0.478 (W^\pm h)$ [89, 91, 92]	
	$h \rightarrow WW^*$	1.850 ± 0.438 —		$1.000 \pm 0.184 (Zh)$ $1.000 \pm 0.138 (W^\pm h)$ [91, 93]	
	$h \rightarrow b\bar{b}$	— 1.025 ± 0.175		$1.000 \pm 0.065 (Zh)$ $1.000 \pm 0.094 (W^\pm h)$ [89, 91]	
Zh CMS	$h \rightarrow \tau^+\tau^-$	1.645 ± 1.485		[92]	
	$h \rightarrow b\bar{b}$	0.94 ± 0.32	—		
$W^\pm h$ CMS	$h \rightarrow \tau^+\tau^-$	3.08 ± 1.58		[92]	
	$h \rightarrow b\bar{b}$	1.28 ± 0.41			

Table 2.1. The experimental single Higgs production and decay rates measurements from the complete data of LHC Run II and projections for the HL-LHC. The uncertainties were symmetrised here.

2.3.2 Constraints on Higgs couplings

The measurements of the Higgs rates and their combination (also including STXS) have been used to set bounds on the Higgs couplings, the most recent bounds - as this thesis being written - have been reported by ATLAS using the Higgs inclusive rates and STXS for the full Run-II data [94], and by CMS using Higgs rates shown in Table 2.1 [92]. In Figure 2.6, I present the aggregation the ATLAS and CMS bounds on the Higgs coupling modifiers in the κ formalism defined in eq. (2.5). The aggregation of these bounds was preformed using the method described in [95] assuming there is no correlation between ATLAS and CMS measurements.

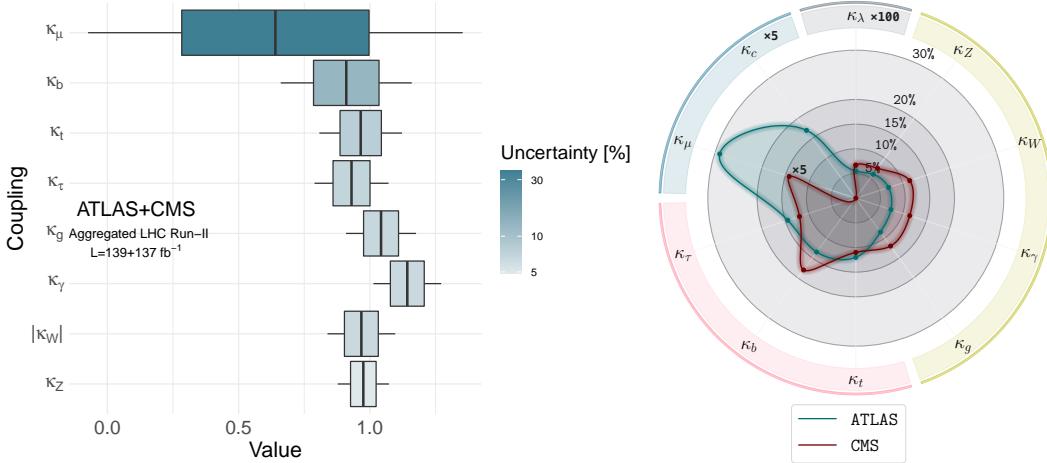


Figure 2.6. Meta analysis aggravating the most recent bounds from ATLAS [94] and CMS [92] on the Higgs coupling modifiers κ . [update the fig](#)

Examining Figure 2.6, we observe that the bounds on the Higgs boson's coupling to the gauge boson, including the effective couplings to γ and g , as well as the couplings to the third-generation fermions are in few percent within the SM prediction. The bounds on the coupling to the W boson seems to favour a negative value in CMS fits, due to the channel used to constraint it $h \rightarrow WW$ which depends on κ_W^2 , thus making the best fit value of ~ -1 within the SM prediction. An independent analysis on the relative signs of κ_W and κ_t was preformed using $th/t\bar{h}$ processes in Ref. [96], hence only the absolute value of κ_W is reported in my combination of the analysis results. Additionally, the observation of the decays $h \rightarrow b\bar{b}$ [97–99] and $h \rightarrow \tau\tau$ [100, 101] leading to direct measurements of the beauty and τ Yukawa couplings has made their bounds comparable to the gauge bosons and top couplings with the Higgs, having less than 10% uncertainty. Au contraire, bounds on the Yukawa couplings of second and first generation fermions remain very weak.

Recently, searches for the decay $h \rightarrow \mu\mu$ [102, 103] using the whole Run-II data by both collaborations, yielded an evidence for its observation of about 3σ . Improving the constraints on κ_μ , though as seen in Figure 2.6, the uncertainty remains high

$\sim 36\%$. Searches for the Higgs decaying to charm pairs is significantly more challenging than the dimuon decays and only yielded an upper 95% CL bounds on $|\kappa_c|$ of 8.5 for ATLAS [104, 105] and 70 for CMS [106]. There is no planned direct searches for the first generation Yukawa couplings (*direct*) measurements planned for the LHC as it is not possible to directly access decays of the Higgs to up or down quarks. Other methods for probing these couplings will be extensively discussed in ??.

By the end of the HL-LHC, it is projected that the couplings of the Higgs, including the couplings with gauge bosons, third generation fermions as well as the muon Yukawa will be measured at few percent level, particularly the couplings with the gauge bosons will be reaching $\sim 1\%$ level uncertainty [107]. This is highlighted by Figure 2.7, this figure shows the improvement in the κ measurement uncertainty expected by the HL-LHC over Run-II.

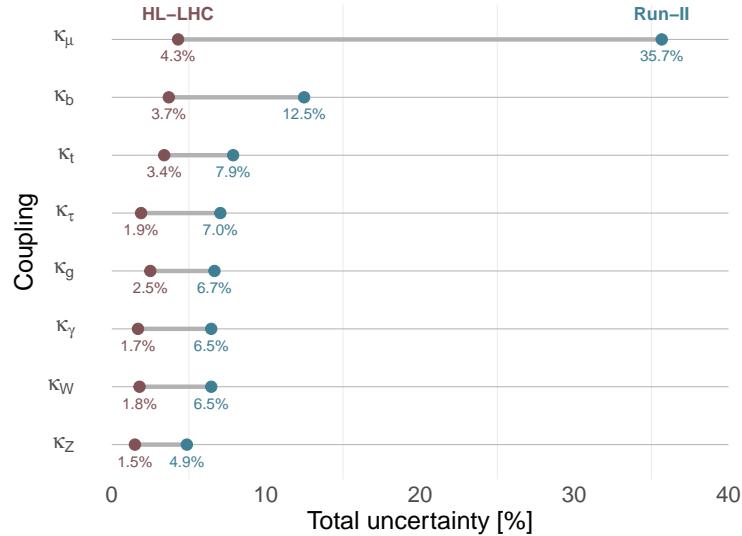


Figure 2.7. Dumbbell plot illustrating the improvement of the uncertainties on the Higgs coupling's measurement project for the HL-LHC compared to the current combined CMS and ATLAS measurements of Run-II.

2.4 Challenges and outlook

The future runs of the LHC hold a lot of potential for further understanding of the 10-year old Higgs boson ! Although, for some processes and couplings there will still be a lot of challenges. For instance, the observation of $h \rightarrow c\bar{c}$ will require highly efficient charm-tagging, which is expected to improve at the HL-LHC by a factor of 2.5 [108]. The signal strength with rare decay $h \rightarrow Z\gamma$ currently is constrained to 3.6 times the SM values at 95% CL [109] and it is projected to be measured at the HL-LHC with $\sim 10\%$ uncertainty.

One of the couplings of the Higgs which we did not discuss above is the Higgs self-interaction (trilinear and quartic), as I have shown in subsection 1.5.2 that the perturbative unitarity bound derived in Ref. [52] is the strongest bound on these couplings so far. This is due to the fact that to experimentally measure the Higgs self-coupling, one needs to search for double Higgs production to access the trilinear self-coupling, and triple Higgs production for the quartic. These processes are very challenging, due to their low inclusive cross-section ~ 30 fb for hh [110] and < 0.1 fb for hhh at LHC maximum expected operational energy of 14 TeV and the latter is challenging even for future colliders of inclusive cross section at 100 TeV of only ~ 5 fb [111]; as opposed to single Higgs production with inclusive cross-section of ~ 70 pb. Certainly the difficulty is aggravated when one considers that the second Higgs would also decay, further lowering the signal strength. The triple Higgs production thus, will not be accessible at the LHC and consequently the quartic self-coupling. However, there is a lot of potential for the trilinear self-coupling, particularly at the HL-LHC.

In chapter 5 I will discuss the potential for using single Higgs processes as proposed by several studies, cf. [112–119] and the challenges accompanying it. Later in ?? the Higgs pair production at the LHC will be overviewed along the current and future searches for this process and the bounds from them on the trilinear Higgs self-coupling.

Another elusive couplings that we have came across are the light Yukawas. In particular light quark Yukawa couplings of the first generation. After overviewing the proposed methods for constraining them, in ?? I will discuss a novel method for directly measuring light quark Yukawa coupling using Higgs pair production. And in ?? a sophisticated method based on interpretable machine learning will be showcased, by which, it is possible to simultaneously constrain the two elusive Higgs interactions: light Yukawas and the trilinear self-coupling using Higgs pair production.

3 Higgs and effective field theories

The study of the Higgs properties, couplings and rates aims to shed light on the structure of its potential, how and why it is responsible for the EW symmetry breaking. Explaining the vacuum expectation value and the mass of the Higgs has been the aim of many theoreticians and phenomenologists. This is because the SM provides no insights on the nature of the Higgs potential and its parameters, as in the SM these are input parameters that is needed to be provided from experimental observations. The Higgs potential shown in eq. (1.8) is the minimal one that could cause the EW symmetry breaking, but nature may not have taken this minimalist approach. In particular, that this potential suffers from severe fine-tuning as we have discussed in the hierarchy problem [add a discussion about this](#).

In order to test whether the Higgs potential and the way it generates SSB is the minimalist SM way or there are other more complex structures involved one needs to measure Higgs rates and compare them with the SM, as overviewed in the previous chapter, using the κ formalism. Alas, this approach does not help in understanding what would the new physics (NP) structures be more likely to case a certain deviation, if any observed. Conversely, we would be interested in knowing what the allowed NP structures given the current (or future) measurements of the Higgs rates are. Of course, by looking at concrete models, one-by-one, confronting them with Higgs data one would get an insight on the aforementioned questions but withal very tedious as there are numerous ways NP might manifest itself.

In order to make our search for NP more accessible and model-agnostic, we could revert to **effective field theories** (EFT), one of the most perspicacious concepts of quantum field theory. In the EFT framework, the interactions mediated by the NP at small scale of an arbitrary complexity can be systematically simplified by approximating these interactions via integrating the UV degrees of freedom thus leaving only numerable operators added to the SM. The premise of EFT's can be simply illustrated in [Figure 3.1](#), the LHC-for example- would not be able to resolve the UV degrees of freedom at their scale Λ , rather one can only observe the effective interactions they mediates. These new effective interactions are parametrised using a set of free parameters known as **Wilson coefficients**, that would be constrained from experiments. These “phenomenological Lagrangians” as called by Weinberg [120], are not necessarily renormalisable but would still allow for robust predictions that can be tested at colliders, including higher order effects . These predictions usually manifest as modifications to rates.

In this chapter I will be discussing the EFT's that modify Higgs rates, including single Higgs and Higgs pair production at leading order. In later chapters like ?? EFT operators from the top quark sector that modify Higgs rates at NLO will be shown. Lastly, in ?? more EFT operators that are responsible for lepton flavour universality

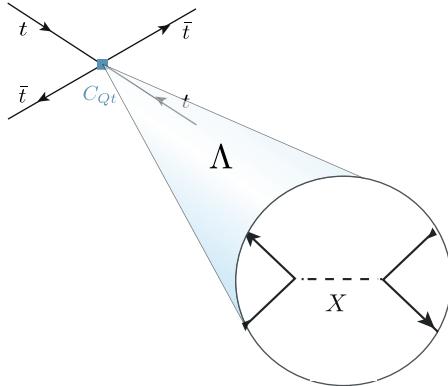


Figure 3.1. eft

violation also at NLO will be showcased. This chapter is organised as follows: In ?? the Higgs sector of Standard Model effective field theory (SMEFT) will be presented along with the parametrisation of single and di-Higgs rates in terms of the SMEFT Wilson coefficients. Au contraire to the SMEFT formalism, section 3.2 will present a non-linear EFT formalism known as the Chiral Lagrangian or (Higgs)EFT . Finally I will conclude this chapter with section 3.3.

3.1 Standard Model EFT

There is no unique way of defining an EFT for the Higgs boson $h(x)$. One could consider the field h as an EW singlet or as a part of the doublet ϕ like the SM. The first ansatz way is more compatible with a heavier Higgs and the effective coupling based on it could be derived from the EW chiral Lagrangian (EWChL) as we shall see in section 3.2. However, after the discovery of the Higgs, having a mass close to m_Z , the second option for an EFT seemed more fitting, though more restrictive. Assuming that the NP resonances would occur at masses $\Lambda \gg m_Z$, one could integrate them out yielding a set of effective operators of mass dimension > 4 . Hence, one can think of the SM Lagrangian of mass dim 2 and 4 as a part of a more general EFT that contain the same fields and symmetries known as the Standard Model Effective field theory (SMEFT).

From simple dimensional analysis, we know that the Higher dimensional operators need to contain an inverse mass with some power $p = 4 - d$ in the couplings, we will have a clear power counting in the SMEFT Lagrangian, such that we could collect all operators of the same mass dimension d into a d -mass-dimensional Lagrangians taking the form

$$\mathcal{L}^{(d)} = \frac{1}{\Lambda^{d-4}} \sum_i C_i \mathcal{O}_i. \quad (3.1)$$

For any $d > 4$ the Lagrangian in eq. (3.1) is not be renormalisable in the strict sense, yet it is still predictive via fitting the Wilson coefficients C_i order-by-order. This power-

counting property allows for predictability even when we, in principle, have infinite number of free Wilson coefficients, as all of these operators are suppressed by the NP scale (irrelevant operators w.r.t. the renormalisation group) [1]. In order to illustrate this, we let $\Lambda = 1$, then the effects of dimension-six operators will be in percent level, while dimension-eight operators will have effects of order $\sim 10^{-4}$, allowing us to ignore the dimension-eight and higher operators. Regarding dimension-five, we have only one operator called the Weinberg operator [121]

$$\mathcal{O}_{\nu\nu} = (\tilde{\phi} L_p)^T \hat{C} (\tilde{\phi}^\dagger L_q), \quad (3.2)$$

where \hat{C} is the charge conjugation operator. The Weinberg operator violates leptonic number and generates neutrino masses after EW symmetry breaking, similar effects are generated from dimension-seven operators [122]. These effects do not yield considerable collider phenomenology. Hence, I shall be discussing SMEFT with dimension-six operators only, for studies on Higher dimensional SMEFT operators cf. [122–125]. The SMEFT Lagrangian up to dimension-six operators is given by

$$\mathcal{L}_{\text{SMEFT}}^{d=6} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum_i C_i \mathcal{O}_i. \quad (3.3)$$

The study of dimension-six effective operators in characterising NP effects at energies beyond colliders reach has been first proposed in [127, 128]. Nowadays, phenomenological studies of EFT's with dimension-six operators primarily focus on using a set of complete and non-redundant “basis”. This is due to the fact that different effective operators will correspond to same observables e.g. same scattering amplitudes of SM particles. This is the case if the operators can be related by using equations of motion, Fierz transformations, integration by parts or field redefinitions. This leads to non-trivial and counter-intuitive relations between operators. Thus making the construction of basis for the dimension-six SMEFT Lagrangian of eq. (3.3) a cumbersome task. Such task has been accomplished recently by [126, 129] forming what is known as **Warsaw Basis**. Another set of basis is the strongly-interacting light Higgs basis (SILH), originally proposed by [130], before the Warsaw basis, and completed in [131, 132]. A more recent set of basis has been published in [133] using a subset of couplings characterising the interactions of mass eigenstates in the effective Lagrangian.

The complete $d = 6$ SMEFT is described by 2499 independent parameters [129]. However, if one suppresses the flavour indices, then the dimension-six operators themselves are much less, in the Warsaw basis for example, assuming Baryon number conservation and dropping the flavour indices one has only 59 operators, listed in Table 3.1. It should be noted that all of the basis of SMEFT will produce the same phenomenology, the choice of basis is sometimes helpful in simplifying the analysis. In this thesis, I will mainly focus on Warsaw basis.

The SMEFT operators can either modify SM parameters (couplings, masses) or introduce new vertices that do not exist in the SM, like four-fermion operators, or both like $\mathcal{O}_{\phi e}$. An example of operators modifying SM parameters is $\mathcal{O}_{\phi D}$, which leads to

X^3		Pure Higgs		$\psi^2\phi^3 + \text{h.c.}$	
\mathcal{O}_G	$f^{ABC}G_\mu^{A\nu}G_\nu^{B\rho}G_\rho^{C\mu}$	$\mathcal{O}_{\phi\square}$	$(\phi^\dagger\phi)\square(\phi^\dagger\phi)$	$\mathcal{O}_{e\phi}$	$(\phi^\dagger\phi)(\bar{l}_p e_r \phi)$
$\mathcal{O}_{\widetilde{G}}$	$f^{ABC}\widetilde{G}_\mu^{A\nu}G_\nu^{B\rho}G_\rho^{C\mu}$	$\mathcal{O}_{\phi D}$	$(\phi^\dagger D_\mu\phi)^*(\phi^\dagger D_\mu\phi)$	$\mathcal{O}_{u\phi}$	$(\phi^\dagger\phi)(\bar{q}_p u_r \widetilde{\phi})$
\mathcal{O}_W	$\epsilon^{IJK}W_\mu^{I\nu}W_\nu^{J\rho}W_\rho^{K\mu}$	\mathcal{O}_ϕ	$(\phi^\dagger\phi)^3$	$\mathcal{O}_{d\phi}$	$(\phi^\dagger\phi)(\bar{q}_p d_r \phi)$
$\mathcal{O}_{\widetilde{W}}$	$\epsilon^{IJK}\widetilde{W}_\mu^{I\nu}W_\nu^{J\rho}W_\rho^{K\mu}$				
$X^2\phi^2$		$\psi^2 X\phi + \text{h.c.}$		$\psi^2\phi^2 D$	
$\mathcal{O}_{\phi G}$	$\phi^\dagger\phi G_{\mu\nu}^A G^{A\mu\nu}$	\mathcal{O}_{eW}	$(\bar{l}_p\sigma^{\mu\nu}e_r)\tau^I\phi W_{\mu\nu}^I$	$\mathcal{O}_{\phi l}^{(1)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{l}_p\gamma^\mu l_r)$
$\mathcal{O}_{\phi\widetilde{G}}$	$\phi^\dagger\phi\widetilde{G}_{\mu\nu}^A G^{A\mu\nu}$	\mathcal{O}_{eB}	$(\bar{l}_p\sigma^{\mu\nu}e_r)\phi B_{\mu\nu}$	$\mathcal{O}_{\phi l}^{(3)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu^I\phi)(\bar{l}_p\tau^I\gamma^\mu l_r)$
$\mathcal{O}_{\phi W}$	$\phi^\dagger\phi W_{\mu\nu}^I W^{I\mu\nu}$	\mathcal{O}_{uG}	$(\bar{q}_p\sigma^{\mu\nu}T^A u_r)\widetilde{\phi} G_{\mu\nu}^A$	$\mathcal{O}_{\phi e}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{e}_p\gamma^\mu e_r)$
$\mathcal{O}_{\phi\widetilde{W}}$	$\phi^\dagger\phi\widetilde{W}_{\mu\nu}^I W^{I\mu\nu}$	\mathcal{O}_{uW}	$(\bar{q}_p\sigma^{\mu\nu}u_r)\tau^I\widetilde{\phi} W_{\mu\nu}^I$	$\mathcal{O}_{\phi q}^{(1)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{q}_p\gamma^\mu q_r)$
$\mathcal{O}_{\phi B}$	$\phi^\dagger\phi B_{\mu\nu}B^{\mu\nu}$	\mathcal{O}_{uB}	$(\bar{q}_p\sigma^{\mu\nu}u_r)\widetilde{\phi} B_{\mu\nu}$	$\mathcal{O}_{\phi q}^{(3)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu^I\phi)(\bar{q}_p\tau^I\gamma^\mu q_r)$
$\mathcal{O}_{\phi\widetilde{B}}$	$\phi^\dagger\phi\widetilde{B}_{\mu\nu}B^{\mu\nu}$	\mathcal{O}_{dG}	$(\bar{q}_p\sigma^{\mu\nu}T^A d_r)\phi G_{\mu\nu}^A$	$\mathcal{O}_{\phi u}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{u}_p\gamma^\mu u_r)$
$\mathcal{O}_{\phi WB}$	$\phi^\dagger\tau^I\phi W_{\mu\nu}^I B^{\mu\nu}$	\mathcal{O}_{dW}	$(\bar{q}_p\sigma^{\mu\nu}d_r)\tau^I\phi W_{\mu\nu}^I$	$\mathcal{O}_{\phi d}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{d}_p\gamma^\mu d_r)$
$\mathcal{O}_{\phi\widetilde{WB}}$	$\phi^\dagger\tau^I\phi\widetilde{W}_{\mu\nu}^I B^{\mu\nu}$	\mathcal{O}_{dB}	$(\bar{q}_p\sigma^{\mu\nu}d_r)\phi B_{\mu\nu}$	$\mathcal{O}_{\phi ud} + \text{h.c.}$	$i(\widetilde{\phi}^\dagger D_\mu\phi)(\bar{u}_p\gamma^\mu d_r)$
$(\bar{L}L)(\bar{L}L)$			$(\bar{R}R)(\bar{R}R)$		
\mathcal{O}_{ll}	$(\bar{l}_p\gamma_\mu l_r)(\bar{l}_s\gamma^\mu l_t)$		\mathcal{O}_{ee}	$(\bar{e}_p\gamma_\mu e_r)(\bar{e}_s\gamma^\mu e_t)$	
$\mathcal{O}_{qq}^{(1)}$	$(\bar{q}_p\gamma_\mu q_r)(\bar{q}_s\gamma^\mu q_t)$		\mathcal{O}_{uu}	$(\bar{u}_p\gamma_\mu u_r)(\bar{u}_s\gamma^\mu u_t)$	
$\mathcal{O}_{qq}^{(3)}$	$(\bar{q}_p\gamma_\mu\tau^I q_r)(\bar{q}_s\gamma^\mu\tau^I q_t)$		\mathcal{O}_{dd}	$(\bar{d}_p\gamma_\mu d_r)(\bar{d}_s\gamma^\mu d_t)$	
$\mathcal{O}_{lq}^{(1)}$	$(\bar{l}_p\gamma_\mu l_r)(\bar{q}_s\gamma^\mu q_t)$		\mathcal{O}_{eu}	$(\bar{e}_p\gamma_\mu e_r)(\bar{u}_s\gamma^\mu u_t)$	
$\mathcal{O}_{lq}^{(3)}$	$(\bar{l}_p\gamma_\mu\tau^I l_r)(\bar{q}_s\gamma^\mu\tau^I q_t)$		\mathcal{O}_{ed}	$(\bar{e}_p\gamma_\mu e_r)(\bar{d}_s\gamma^\mu d_t)$	
			$\mathcal{O}_{ud}^{(1)}$	$(\bar{u}_p\gamma_\mu u_r)(\bar{d}_s\gamma^\mu d_t)$	
			$\mathcal{O}_{ud}^{(8)}$	$(\bar{u}_p\gamma_\mu T^A u_r)(\bar{d}_s\gamma^\mu T^A d_t)$	
$(\bar{L}L)(\bar{R}R)$			$(\bar{L}R)(\bar{L}R) + \text{h.c.}$		
\mathcal{O}_{le}	$(\bar{l}_p\gamma_\mu l_r)(\bar{e}_s\gamma^\mu e_t)$		$\mathcal{O}_{quqd}^{(1)}$	$(\bar{q}_p^j u_r)\epsilon_{jk}(\bar{d}_s^k d_t)$	
\mathcal{O}_{lu}	$(\bar{l}_p\gamma_\mu l_r)(\bar{u}_s\gamma^\mu u_t)$		$\mathcal{O}_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r)\epsilon_{jk}(\bar{q}_s^k T^A d_t)$	
\mathcal{O}_{ld}	$(\bar{l}_p\gamma_\mu l_r)(\bar{d}_s\gamma^\mu d_t)$		$\mathcal{O}_{lequ}^{(1)}$	$(\bar{l}_p^j e_r)\epsilon_{jk}(\bar{q}_s^k u_t)$	
\mathcal{O}_{qe}	$(\bar{q}_p\gamma_\mu q_r)(\bar{e}_s\gamma^\mu e_t)$		$\mathcal{O}_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r)\epsilon_{jk}(\bar{q}_s^k \sigma^{\mu\nu} u_t)$	
$\mathcal{O}_{qu}^{(1)}$	$(\bar{q}_p\gamma_\mu q_r)(\bar{u}_s\gamma^\mu u_t)$		\mathcal{O}_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_{tj})$	
$\mathcal{O}_{qu}^{(8)}$	$(\bar{q}_p\gamma_\mu T^A q_r)(\bar{u}_s\gamma^\mu T^A u_t)$				
$\mathcal{O}_{qd}^{(1)}$	$(\bar{q}_p\gamma_\mu q_r)(\bar{d}_s\gamma^\mu d_t)$				
$\mathcal{O}_{qd}^{(8)}$	$(\bar{q}_p\gamma_\mu T^A q_r)(\bar{d}_s\gamma^\mu T^A d_t)$				

Table 3.1. Complete list of the dimension-six SMEFT operators in the Warsaw basis [126]. The \mathcal{CP} violating operators contains the dual fields \tilde{X} . The flavour labels of the form p, r, s, t on the \mathcal{O} operators are suppressed on the left hand side of the tables.

modification of the Z boson mass after EW symmetry breaking

$$\frac{C_{\phi D}}{\Lambda^2} |\phi^\dagger D_\mu \phi|^2 \rightarrow \frac{C_{\phi D} v^4}{16\Lambda^2} (g_2^2 + g_1^2) Z^\mu Z_\mu. \quad (3.4)$$

Additionally, from field redefinitions, we get indirect contributions to the W mass from $C_{\phi D}$, combining both effects as a deviation in the ρ parameter, we get

$$\delta\rho = \frac{v^2}{2\Lambda^2} C_{\phi D}. \quad (3.5)$$

Which allows us to constrain $C_{\phi D}$ from the T parameter

$$T = \frac{-2\pi v^2}{\Lambda^2} \frac{(g_1^2 + g_2^2)}{g_1^2 g_2^2} C_{\phi D} \quad (3.6)$$

Another operator that affects the oblique parameters directly is $\mathcal{O}_{\phi WB}$, as it modifies the S parameter in the following way

$$S = \frac{16\pi v^2}{g_1 g_2 \Lambda^2} C_{\phi WB} \quad (3.7)$$

Other SM coupling modifications by SMEFT operators related to EWPO's are investigated in [134], and [?]. Additionally, the contributions of the SMEFT Wilson coefficients to SM parameters are not only from tree-level effects like in eq. (3.4) but could also come at (N)NLO, either from finite or RGE contributions.

SMEFT is suitable as a low energy limit for supersymmetric models [135] or some classes of composite Higgs models [136, 137]

3.1.1 Single Higgs processes in SMEFT

Single Higgs production and decay processes are modified at LO by a relatively long list of operators summarised in eqs. (3.8), (3.9) and (3.10). Explicit formulae for the Higgs rates dependence on the Wilson coefficients of these operators can be found in [138]

SMEFT operators modifying Higgs rates at LO

Higgs operators

$$\begin{aligned} C_{\phi D}, \mathcal{O}_{\phi \square}, \mathcal{O}_{\phi G}, \mathcal{O}_{\phi W}, \mathcal{O}_{\phi B}, \mathcal{O}_{\phi WB}, \mathcal{O}_{\phi l}^{(1)}, \\ \mathcal{O}_{\phi l}^{(3)}, \mathcal{O}_{\phi e}, \mathcal{O}_{\phi q}^{(1)}, \mathcal{O}_{\phi q}^{(3)}, \mathcal{O}_{\phi u}, \mathcal{O}_{\phi d}, \mathcal{O}_{\tau \phi}, \mathcal{O}_{t \phi}, \mathcal{O}_{b \phi}, \mathcal{O}_{tb \phi}. \end{aligned} \quad (3.8)$$

Top-quark operators

$$\mathcal{O}_{tG}, \mathcal{O}_{tW}, \mathcal{O}_{tB}, \quad (3.9)$$

other

$$\mathcal{O}_G, \mathcal{O}_{ll}^{(1)}, \mathcal{O}_{Qq}^{(1),(3)}, \mathcal{O}_{tu}, \mathcal{O}_{td}^{(1),(8)}, \mathcal{O}_{Qu}^{(1),(8)}, \mathcal{O}_{Qd}^{(1),(8)}. \quad (3.10)$$

The third generation quarks are denoted by Q while the first and second generation quarks are assumed to have the same coupling and denoted by q, u, d .

Some of these operators are strongly constrained from EWPO data such as $\mathcal{O}_{\phi D}$ and $\mathcal{O}_{\phi WB}$. Others are weakly constrained from Higgs data alone like the four-fermion or top sector operators, and require additional experimental data to constrain them. Global fits on SMEFT Wilson coefficients can be found in [139]. Where they have used Higgs and EW data on a subset of the SMEFT Wilson coefficients of the operators listed above. The fit also includes RGE and NLO (even NNLO for m_W) effects. While in [140], a global fit for a larger set of operators, but only with LO effects, including EW, Higgs and top data for C_G the fits are found in [141]. More recent study [142] has utilised EWPO data to constrain the four-fermion operators appearing in Higgs rates at LO and others involving four heavy quarks, using their NLO effects to EW bosons pole masses. We shall see in chapter 5 that the four-fermions operators with all heavy quarks will contribute also to Higgs rates at NLO. A wider scope analysis including a wide range of Higgs, top, di-boson and EWPO data has been preformed in [143].

The dependence of single Higgs rates on the SMEFT Wilson coefficients gets more complicated once NLO and higher effects are taken into an account. As shown in the fit results reported from [139], the RGE of these Wilson coefficients introduces new operators that do not appear at LO, also loop corrections to masses of the EW and Higgs bosons as well as their process will depend on some SMEFT coefficients. A prominent example of an operator appearing only at NLO in single Higgs processes is \mathcal{O}_ϕ , which modifies the Higgs self interactions, namely the trilinear coupling.

Typically, in order to probe the Higgs trilinear self-coupling directly, one ought to observe Higgs pair production, see ???. However, due to the appearance of Higgs self-interaction and its modifiers- C_ϕ in SMEFT context- in (N)NLO EW [144, 145] and Higgs observables [112–119], one can extract bounds on the Higgs trilinear coupling from single Higgs and EWPO data. Figure 3.2 illustrates example Feynman diagrams of single Higgs processes of which the trilinear Higgs self-coupling enters via NLO corrections. Using the results from the aforementioned references, a global fit with all operators that enter at tree-level in addition to the loop effects from the Higgs self-coupling has been preformed

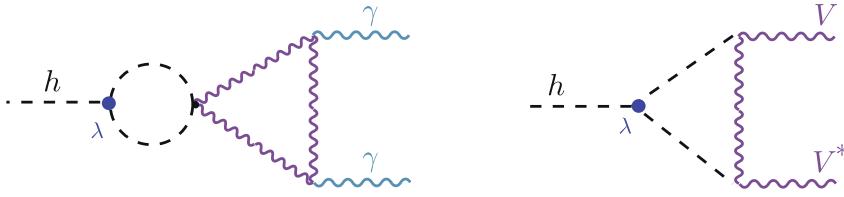


Figure 3.2. NLO EW corrections of single Higgs processes, were the Higgs trilinear self-coupling (the red circle) enters. Here the Higgs decay to two photons is shown as an example.

in ref. [146] and later as we have seen in ref. [139]. Additionally, experimental searches for Higgs trilinear self-coupling have been presented by ATLAS [147] and CMS [92].

3.1.2 Higgs pair production and SMEFT

Higgs pair production in Hadron colliders is sensitive to six \mathcal{CP} even SMEFT operators, under the assumption of Minimal Flavour violation (MFV)¹. These operators are

$$\mathcal{O}_{\phi D}, \mathcal{O}_{\phi \square}, \mathcal{O}_\phi, \mathcal{O}_{t\phi}, \mathcal{O}_{\phi G}, \mathcal{O}_{tG}, \quad (3.11)$$

and their effects, with the corresponding colours are illustrated in Figure 3.3, except for $\mathcal{O}_{\phi D}$ and $\mathcal{O}_{\phi \square}$, as they modify all SM Higgs vertices. However, MFV is not the only way to approach SMEFT, there exist more complex flavour structures that allow for significant enhancements of the first and second generation Yukawas with being excluded by flavour observables. Such formalisms will be discussed in ?? and ??, where I discuss the potential for Higgs pair production in probing operators modifying Light Yukawa couplings. Moreover, for Higgs pair production with \mathcal{CP} operators, see ref. [148]. The main operator to constrain from Higgs pair as mentioned before is \mathcal{O}_ϕ , for two reasons; a) the other operators are already strongly constraint from single Higgs and top processes b) the effect of \mathcal{O}_ϕ on Higgs pair production is significantly higher than in single Higgs or EW observables. This is illustrated in Figure 3.4, by comparing the relative change of the gluon fusion cross-sections at NLO QCD for single and di-Higgs production. This is not surprising, since C_ϕ appears at LO in Higgs pair production. Another advantage for Higgs pair production searches is the sensitivity of this process to non-linear couplings, for example diagrams (b) and (d) of Figure 3.3. Although in SMEFT these diagrams correspond to the same operators in (a) and (c), respectively, in an another EFT this is not necessary the case.

¹MFV assumes that new physics operators will follow the same flavour hierarchies as the SM.

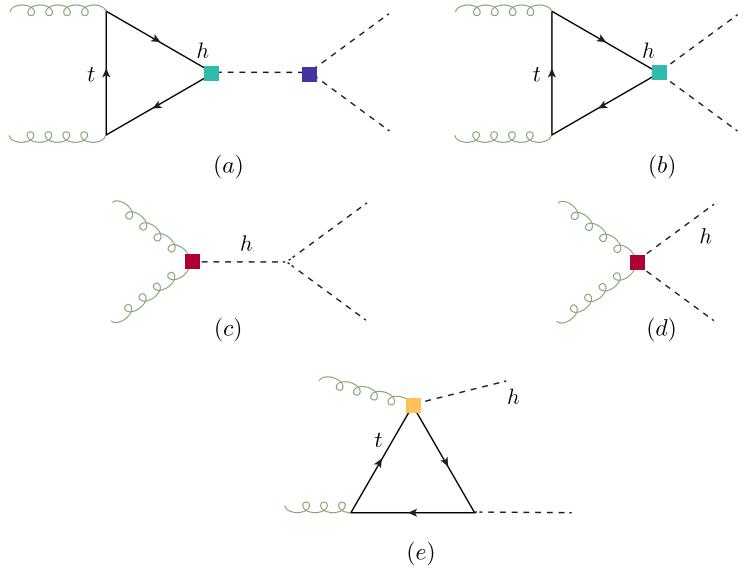


Figure 3.3. Example of diagrams illustrating how the dimension-six SMEFT operators enter in Higgs pair production at Hadron colliders.

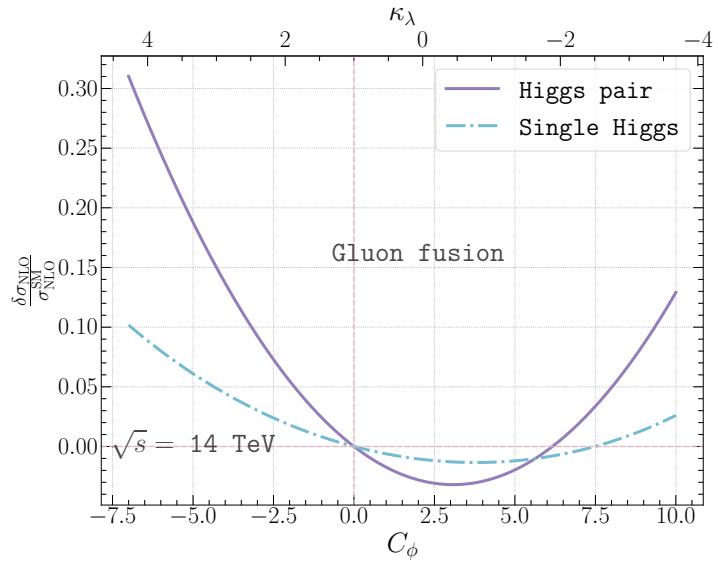


Figure 3.4. The relative change of the NLO QCD cross-section of gluon fusion production of single Higgs (dashed line) and Higgs pair (solid line) at a pp collider with $\sqrt{s} = 14 \text{ TeV}$ as a function of C_ϕ or the corresponding κ_λ .

3.2 The chiral Lagrangian

Given the strong bounds on the ρ parameter, it would plausible to assume that NP would maintain the custodial symmetry $SU(2)_V$, and treat the chiral symmetry breaking pattern $SU(2)_L \otimes SU(2)_R \rightarrow SU(2)_V$ in the same way the QCD chiral symmetry breaking is treated in terms of considering the pions as pNG bosons in order to describe their interaction. For pions this is known as **chiral perturbation theory** [149, 150]. The same mathematical description could be applied for the case of EW symmetry breaking by constructing the EW chiral Lagrangian (EWChL). In the EWChL the Goldstone fields $\pi^a(x)$ of the SM are part of $SU(2)$ unitary transformation

$$\mathcal{U}(x) = e^{i\pi^a(x)\sigma_a/v}, \quad (3.12)$$

which implies that the Goldstone fields transform non-linearly under $SU(2)_L \otimes SU(2)_R$. As for the Higgs field $h(x)$, it is added as an $SU(2)_L \otimes U(1)_Y$ singlet, and appears in the EWChL at any power in principle. As contrary to the power counting in the NP scale Λ like in SMEFT, in the EWChL, one counts the *chiral dimension* χ , defined for the fields as [151, 152]

$$[\phi]_\chi = 0, \quad [X]_\chi = 0, \quad [\partial_\mu]_\chi = 1, \quad [\psi]_\chi = 2. \quad (3.13)$$

The zeroth order term of the EWChL will have $\chi = 2$, higher order terms could be considered as terms generated perturbatively from L loop interactions, with chiral dimensions $\chi = 2L + 2$, hence the first order EWChL or HEFT would have operators of $\chi = 4$. Hence the expansion of the EWChL is in chiral order as well as in powers of $h(x)/v$. This power-counting results in some SMEFT dimension-six operators being considered of higher order in HEFT a prominent example of this is C_{tG} being of chiral dimension 5 in HEFT.

The relevant terms for single and di-Higgs production of the EWChL /HEFT is typically parametrised in the Unitary gauge by [146, 153]

$$\begin{aligned} \mathcal{L}_{\text{HEFT}} = & \frac{h}{v} \left[\left(\delta c_W m_W^2 W_\mu^+ W^{-\mu} + \delta c_Z \frac{m_Z^2}{2} Z_\mu Z^\mu \right) \right. \\ & + c_{ww} \frac{g_2^2}{2} W_{\mu\nu}^+ W^{-\mu\nu} + c_{w\square} g_2^2 \left(W_\mu^- \partial_\nu W^{+\mu\nu} + \text{h.c.} \right) + c_{\gamma\gamma} \frac{\alpha}{8\pi} A_{\mu\nu} A^{\mu\nu} \\ & + c_{zz} \frac{g_2^2 + g_1^2}{4} Z_{\mu\nu} Z^{\mu\nu} + c_{z\gamma} \frac{eg_1}{16\pi^2} Z_{\mu\nu} A^{\mu\nu} + c_{z\square} g_2^2 Z_\mu \partial_\nu Z^{\mu\nu} + c_{\gamma\square} g_2 g_1 Z_\mu \partial_\nu A^{\mu\nu} \Big] \\ & + \frac{\alpha_s}{8\pi} \left(c_{gg} \frac{h}{v} + c_{gg}^{(2)} \frac{h^2}{2v^2} \right) \text{Tr} [G_{\mu\nu} G^{\mu\nu}] - \sum_f \left[m_f \left(c_f \frac{h}{v} + c_{ff} \frac{h^2}{2v^2} \right) \bar{f}_R f_L + \text{h.c.} \right] \\ & - c_{hh} \frac{m_h^2}{2v} h^3 + \dots, \end{aligned} \quad (3.14)$$

I have omitted here the kinetic and mass terms of the Higgs, \mathcal{CP} violating terms, as well as couplings not contributing to the LHC phenomenology and Higher chiral order operators. In addition to NP effects, this Lagrangian also includes the LO and NLO SM vertices, for example the parameter $\delta c_V = 1$ corresponds to the tree-level coupling between the Higgs field and the EW bosons $V = W, Z$. While the coupling $c_{gg} = 4/3$ corresponds to the SM effective coupling at NLO if the heavy top limit (HTL) $m_t \rightarrow \infty$. In contrast to eqs. (??) and (??) the couplings of one and two Higgs bosons to fermions or gluons become de-correlated. Giving this Lagrangian a richer phenomenology for Higgs pair production.

The HEFT coefficients modifying the Higgs pair production via gluon fusion are

$$c_{hh}, \textcolor{blue}{c_t} \text{ (a)}, \textcolor{teal}{c_{tt}} \text{ (b)}, \textcolor{red}{c_{gg}} \text{ (c)}, \textcolor{red}{c_{gg}^{(2)}} \text{ (d)}, \quad (3.15)$$

with the same colours highlighted in the operator insertions of Figure 3.3 and the letter next to the coefficient indicates the diagram its operator contributes to. Full parametrisation of the Higgs pair cross-section at NLO (inclusive and differential) and NNLO (inclusive) can be found in refs. [154–156] and implemented at NLO in **POWHEG-BOX** [157]. UV-complete models that yield in the EWChL are composite Higgs models [136, 137, 158], dilaton theories [159], techni-dilaton models [160], technicolour models [161] and other models with induced EW symmetry breaking [162, 163].

3.2.1 Translation between SMEFT and HEFT

In order to facilitate the translation between SMEFT and HEFT or to the κ -formalism, one needs to put the SMEFT Lagrangian into the canonical form, that is to convert the operators with covariant derivatives acting on the Higgs to canonically normalised Higgs kinetic term. This is done done by the field redefinition.

$$\phi = \begin{pmatrix} 0 \\ h(1 + c_{h,kin}) + v \end{pmatrix} \quad (3.16)$$

with

$$c_{h,kin} = \left(C_{\phi,\square} - \frac{1}{4} C_{\phi D} \right) \frac{v^2}{\Lambda^2}. \quad (3.17)$$

This field redefinition will generate derivative interactions of the form $h(\partial_\mu h)^2$ and $h^2(\partial_\mu h)^2$. In order to remove these terms, and for sake of simplicity one needs to use a gauge-dependent field redefinition²

$$h \rightarrow h + c_{h,kin} \left(h + \frac{h^2}{v} + \frac{h^3}{3v^2} \right). \quad (3.18)$$

This field redefinition hence leads to a dependence on $c_{h,kin}$ of all Higgs boson couplings. There are however some caveats to the translation between HEFT and SMEFT, for

²For gauge-independent formalism cf. [164].

example, HEFT is less restrictive than SMEFT and it covers loop effects. This makes some points of the HEFT parameter space unmappable to SMEFT. In addition, the power counting is different in both formalisms, as mentioned before there will be some operators present in SMEFT that are absent in HEFT and vice-versa. In [Table 3.2](#), the translation between the HEFT and SMEFT Wilson coefficients of the operators relevant to Higgs pair production at LO is shown. More general translation between

HEFT	SMEFT (Warsaw)
c_{hh}	$1 - 2 \frac{v^4}{m_h^2} C_\phi + 3c_{h,kin}$
c_f	$1 + c_{h,kin} - C_{f\phi} \frac{v^3}{\sqrt{2}m_f}$
c_{ff}	$-C_{f\phi} \frac{3v^3}{2\sqrt{2}m_f} + c_{h,kin}$
c_{gg}	$8\pi/\alpha_s v^2 C_{\phi G}$
$c_{gg}^{(2)}$	$4\pi/\alpha_s v^2 C_{\phi G}$

Table 3.2. Translation between the Wilson coefficients of HEFT and SMEFT for the operators relevant to Higgs pair production

SMEFT in Warsaw and SILH basis and HEFT can be done automatically using [Rosetta](#) package [\[165\]](#)

3.2.2 EFT and κ -formalism

The κ formalism provides an experimentally accessible and well-defined in terms of QFT way to study the Higgs properties [\[166\]](#). The κ parameters are part of more generalised formalism called the **Higgs Pseudo-observables** (PO's), which is discussed in [chapter 4](#). If the new physics contributions do not generate new Lorentz structures there is a possible translation between the Wilson coefficients in the SMEFT Warsaw basis, and the κ formalism. In particular, taking the rescaling of the trilinear coupling, κ_λ , the translation is given by

$$\kappa_\lambda = 1 - \frac{v^4}{m_h^2} \frac{C_\phi}{\Lambda^2} + 3c_{h,kin}, \quad (3.19)$$

A similar relation exists for the rescaling of the quark Yukawa couplings κ_q

$$\kappa_q = 1 + c_{h,kin} - \frac{v^3}{\sqrt{2}m_q} \frac{C_{q\phi}}{\Lambda^2}. \quad (3.20)$$

One can see the similarities between κ -formalism and HEFT in these two examples, but this is not always the case. Other translations could be obtained by comparing how SMEFT operators modify the Higgs couplings with the SM, and matching it with the corresponding κ or other Higgs PO's.

However, one should be careful while interpreting results quoted in terms of Wilson

coefficients in the SMEFT framework extracted from di-Higgs, multi-Higgs or multi-vector bosons searches, as these results include couplings that are not present in the SM. For example, the $hhq\bar{q}$ coupling, though being linearly related to the quark Yukawa coupling $hq\bar{q}$, is not a rescaling of any SM Higgs coupling as has been discussed in ???. With this in mind, one can strictly remain within a linear EFT and link the rescaling of the quark Yukawa, κ_q , to the $hhq\bar{q}$ coupling through

$$g_{hhq\bar{q}}^{\text{linear-EFT}} = -\frac{3}{2} \frac{1-\kappa_q}{v} g_{hq\bar{q}}^{\text{SM}}. \quad (3.21)$$

This relation will no longer hold once a non-linear EFT, like HEFT, is used. Hence, the κ -formalism, in a strict sense, is not applicable to multi-Higgs studies.

3.3 Conclusions

Effective field theories provide a systematic yet simplified approach for NP searches by simplifying its complex interaction structures. This can be thought of as a dimensionality reduction approach by collapsing all the NP interaction into their effective ones as observed at colliders with energy reaches below the NP scale Λ . The linear approach to EFT is called the SMEFT, which preserves the SM fields and symmetries and the Higgs boson is a part of an $SU(2)_L$ doublet ϕ like the SM case. While non-linear approaches such as the chiral EW Lagrangian (or HEFT) treats the Higgs boson as an added singlet. The latter approach is more general and introduces independent parameters involving multiple Higgs bosons. For example, the couplings $f\bar{f}h$ and $f\bar{f}hh$ will be both generated in SMEFT and HEFT, but in SMEFT they are related by the Wilson coefficient $C_{\phi f}$, while in HEFT they have independent Wilson coefficients c_f and c_{ff} respectively.

Most of the Wilson coefficients involving Higgs interactions are strongly bounds by EWPO's, Higgs and top data. In addition to theoretical bounds found in [167]. However, the Wilson coefficients modifying the Higgs self-couplings, though bounds from the first two aforementioned data and perturbative unitarity [52, 168] exist, these bounds remain weak. This can be improved by the searches for Higgs pair production at the HL-LHC, as this process is far more sensitive to these Wilson coefficients than EWPO and single-Higgs data, as they only appear at NLO in the theoretical predictions of the later two experimental observables. In ??, I show the best bounds on the Wilson coefficients relevant to Higgs production as well as heavy quark four-fermion operators, with a heatmap indicating the contribution of each operator in prominent Higgs, top and EW precision observables. Although this is a subset of the total SMEFT operators and observables used in the fits, one can see the interconnectivity of the measurements. The main objective of this thesis is to extend these connections by exploiting the potential of single-Higgs data and Higgs pair production to constrain the Higgs trilinear coupling modifiers (mainly in SMEFT) and the interplay between C_ϕ and heavy quark four-fermion operators in single Higgs data. Moreover, the SMEFT picture can be further extended by unravelling interplay between Light quark couplings modifiers in

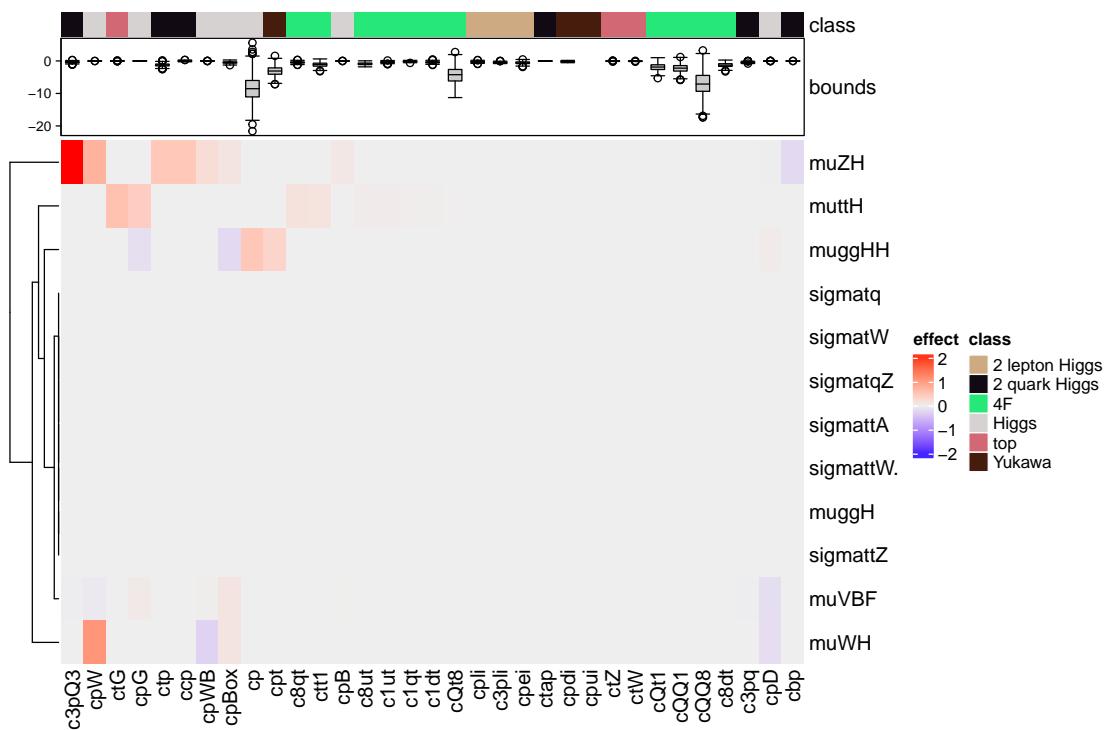


Figure 3.5

Higgs pair production. Lastly, I will show another connection between Higgs operators in SMEFT and flavour anomalies. Emphasising the complex interconnectivity between experimental observables and SMEFT operators.

Part II

Single Higgs Processes at the LHC

4 Overview of Higgs production at colliders

The production of the Higgs boson at the LHC occurs via four distinct processes: gluon fusion (ggF), vector boson fusion (VBF), associated production with electroweak boson (Vh) and the production with top (and anti-top) pair ($t\bar{t}h/\bar{t}th$). It should be noted that sometimes the ggF category will include the quark anti-quark annihilation, but this is negligible in the SM, but becomes important for significant modifications of light Yukawa couplings. These process are illustrated in [Figure 4.1](#), and their details were summarised in [Table 4.1](#). All of these four channels have been observed at the LHC with $> 5\sigma$ precision.

Since the experimental measurements of this Higgs were discussed previously in [section 2.3](#), the aim of this chapter is to provide an overview of the current theoretical status of these channels in [section 4.1](#). I will then conclude this overview in [section 4.2](#).

Process	Cross-section 13 TeV (pb)	Theo. accuracy	Exp. uncertainty (%)	Contribution (%)
ggF	48.51	N3LO QCD & NLO EW	6.5	88
$t\bar{t}h$ & $\bar{t}th$	0.58	NLO QCD & NLO EW	20.0	1
VBF	3.78	NNLO QCD* & NLO EW	10.0	7
Vh	2.25	NNLO QCD & NLO EW	15.0	4

Table 4.1. Summary of the Higgs production processes at the LHC.

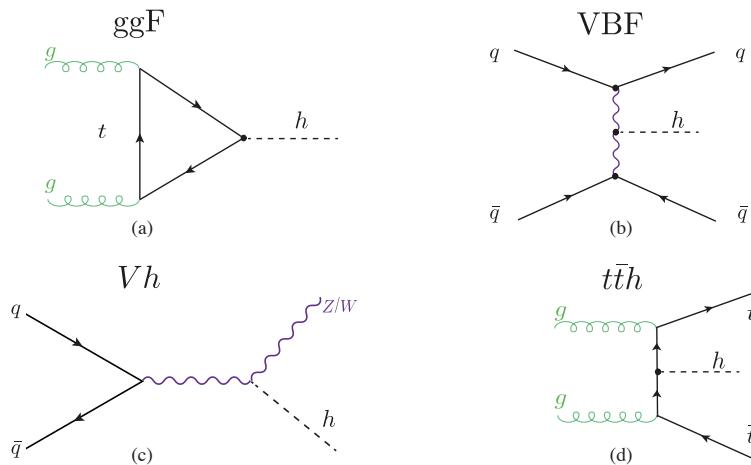


Figure 4.1. Feynman diagram examples of the leading processes for Higgs production at the LHC.

4.1 Current status of the Higgs production channels

4.1.1 Gluon fusion

The ggF channel has the highest cross-section amongst the Higgs production channels, and consequently has the lowest experimental uncertainties. In order to increase the precision of the channel, Higher order corrections need to be included. The current state-of-the-art theoretical computation for the Higgs inclusive cross-section is N³LO in QCD and NLO in EW [169]. A full differential cross-section for the final state $gg \rightarrow h \rightarrow \gamma\gamma$ has been computed recently to N³LO in QCD for the kinematic variables y_h , y_{γ_1} , y_{γ_2} , $\Delta y_{1,2}$ using the projection-to-born method [170]. The same final state fiducial differential cross-section in p_T with experimental cuts has been computed up to third re-summed and fixed order, i.e. N³LL' N³LO dependence [171], the theoretical computation of this fiducial cross-section with difference orders compared to the experimental measurement by ATLAS [86] is shown in Figure 4.2. We can see that the resummed result has significantly smaller theoretical uncertainties. The current total theoretical uncertainty with this order calculation is 5.4%, with only 2.7% of it coming from the perturbation order cut-off of the calculation, while the rest comes from the branching fraction, PDF+ α_s , EW corrections and mass uncertainties. When compared to Table 2.1, the projected experimental uncertainty of this final states at the HL-LHC is 4.2%, we see that the uncertainties will becomes comparable, and if the PDF uncertainties are reduced the uncertainties will remain experimentally-dominated for this channel. The predictions can be further improved by the computation of mixed QCD-EW effects.

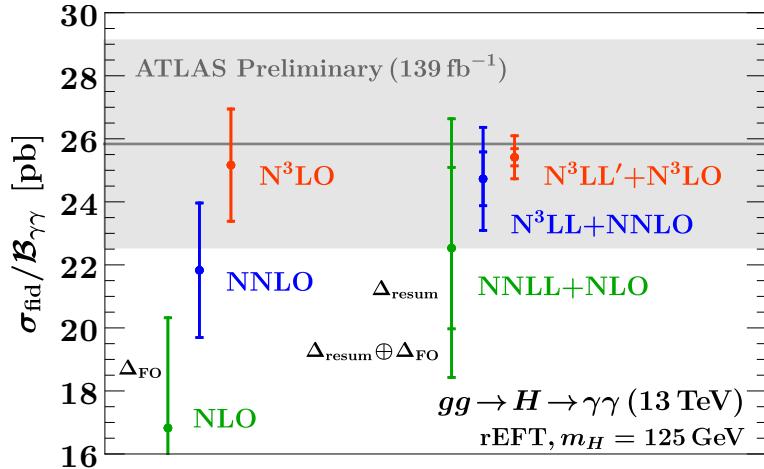


Figure 4.2. The total fiducial cross-section for the final state $gg \rightarrow h \rightarrow \gamma\gamma$ at both fixed and resumed third order compared to the experimental ATLAS measurement [86] this figure is taken from [171]

Alas, these computations invokes three-loop integrals with both gluons and EW bosons, computed in [172] or two-loop ones with two particle final states appearing in the real

corrections with the process $gg \rightarrow hg$ computed in [173] using differential equations. The computation was completed by inclusion of light quark initial states for the real corrections in [174] with exact quark mass dependence, reducing the EW uncertainty from 2% to $\sim 0.6\%$.

The computation of the three-loop form-factors with full top-mass dependence has been achieved in [175, 176] correction the cross-section by -0.26% . However, there remains an intricate interplay between the mass effects of gg , qg and qq initial states for the real matrix elements that cannot be fully controlled due to the light quark mass effects.

NLO corrections to the $h + j$ and $h + 2j$ processes were computed by [177] in the FT approximation, which used exact born and real correction amplitudes, and approximates the two-loop virtuals by

$$|\mathcal{A}^{2\text{-loop}}(m_t, \mu_R^2)|^2 \approx |\mathcal{A}^{1\text{-loop}}(m_t \rightarrow \infty, \mu_R^2)|^2 \frac{|\mathcal{A}^{1\text{-loop}}(m_t)|^2}{|A^{(0)}(m_t) \rightarrow \infty|^2}. \quad (4.1)$$

Although this approximation works very well even for $p_T \gg m_t$, the full top mass effects computations have been carried out in [178–180] using the high energy expansion technique.

4.1.2 Vector boson fusion

The VBF channel has a very distinctive signature, making it very suitable channel for Higgs signal extraction. The suppressed colour exchange between the quarks result in a little jet activity in the central rapidity region, and the quarks will be scattered resulting in two forward jets. The decay products of the Higgs are found in the region between these two forward jets. These features allows for excellent measurement of Higgs couplings and more difficult decays, and \mathcal{CP} properties determination. Some of these features are also shared with the Vh production channel via Higgs-strahlung. Both of these channels contain the VVh vertex which could be written generally as [153]

$$T^{\mu\nu}(p_1, p_2) = a_1 g^{\mu\nu} + a_2 \left(g^{\mu\nu} - 2 \frac{p_2^\mu p_2^\nu}{p_1 \cdot p_2} \right) + a_3 \frac{p_1^\alpha p_2^\beta}{p_1 \cdot p_2} \epsilon^{\mu\nu\alpha\beta}. \quad (4.2)$$

In the SM only $a_1 \neq 0$, and the other coefficients represent the anomalous coupling, for example if $a_3 \neq 0$ then the Higgs is \mathcal{CP} odd. The study of the azimuthal angle distribution $d\sigma_{VBF}/d\Delta\phi_{jj}$ allows for the determination of these coefficients, with very little dependence on the Higher order corrections on VBF [181].

The NLO QCD inclusive cross-section is known since the 90's [182], and later these corrections were made for the differential distributions cf. [183, 184]. Unlike the ggF channel, that has an NLO K-factor of 1.6 at 13 TeV [185], the VBF NLO corrections are small $\sim 10\%$. The two-loop NNLO QCD cross-section has been computed, the most recent is via the structure function approach [186] and later in STXS level 1.2 bins with EW corrections [187] implemented in an MC generator **HAWK**. Despite these corrections being small, they are non-negligible and their inclusion is important for uncertainties

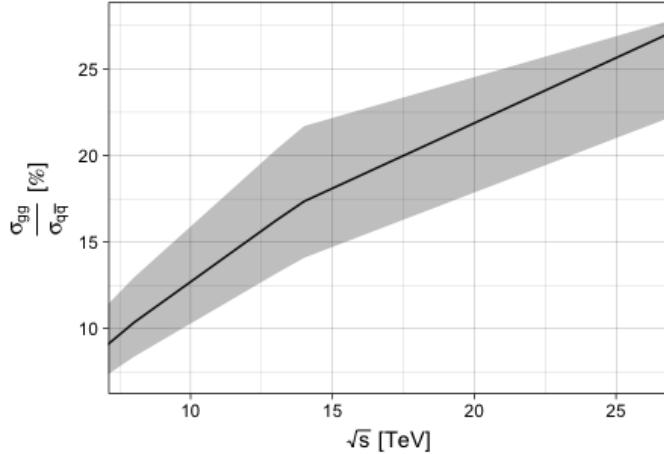


Figure 4.3. The ratio of the *LO* gluon fusion production cross-section $gg \rightarrow Zh$ (σ_{gg}) with respect to the *NLO* Drell-Yan process $q\bar{q} \rightarrow Zh$ cross-section ($\sigma_{q\bar{q}}$) at a pp collider with centre-of-mass energy \sqrt{s} . The error band captures the total theoretical uncertainties on both cross-sections dominated by σ_{gg} .

reduction.

4.1.3 Associated production with EW bosons

The channels $pp \rightarrow Wh/Zh$ are quark-initiated tree-level processes at *LO* interpreted as **Drell-Yan process** [188, 189]. These process has been computed up to *NNLO* in QCD ($\sim \alpha_s^2$), and *NLO* EW ($\sim \alpha^2$) [190].

Despite arising for the first time at *NNLO* in perturbation theory to the partonic cross-section, the gluon fusion channel $gg \rightarrow Zh$ has a non-negligible contribution to the hadronic cross-section $pp \rightarrow Zh$, which could reach $> 16\%$ of the total cross-section contribution at 14 TeV [191], see Figure 4.3. The contribution becomes more significant when looking at large invariant mass bins in the differential cross-section. This is due to the significant abundance of gluons at the LHC for large energy fraction Q as well as the extra enhancement coming from the top quark initiated contribution near the $t\bar{t}$ threshold [192]. The gluon fusion channel has a higher scale uncertainties than the quark induced one, as one can see from the uncertainty band of Figure 4.3 predominantly coming from the gluon fusion part σ_{gg} . With that in mind, and the absence of gluon fusion channel for Wh channel, the Zh channel has higher theoretical uncertainties. This further motivates *NLO* calculation of the $gg \rightarrow Zh$ channel to higher orders in perturbation theory, in order to reduce these uncertainties. Facilitating the precision measurement of the Zh channel at the future LHC runs, which in term provides better constraints on several observables, such as sign and magnitude of the top Yukawa coupling, dipole operators [193].

The leading order (*LO*) contribution to the $gg \rightarrow Zh$ amplitude, given by one-loop

diagrams, was computed exactly in refs.[194, 195]. However, for the NLO, the virtual corrections contain multi-scale two-loop integrals some of which are still not known analytically (for the box diagram). The first computation of the NLO terms has been done by [196] using an asymptotic expansion in the limit $m_t \rightarrow \infty$ and $m_b = 0$, and pointed to a K -factor of about ~ 2 . Later, the computation has been improved via soft gluon resummation, and including NLL terms found in ref.[197], the NLL terms has been matched to the fixed NLO computation of [196]. Top quark mass effects to the $gg \rightarrow Zh$ process were first implemented using a combination of large- m_t expansion (LME) and Padé approximants [198]. A data-driven approach to extract the gluon fusion dominated non-Drell-Yan part of Zh production using the known relation between Wh and Zh associated production when only the Drell-Yan component of the two processes is considered has been investigated in ref.[199]. The differential distributions of $gg \rightarrow Zh$ at NLO was studied in ref.[200] via LO matrix element matching.

More recent studies of the NLO virtual corrections to this process were based on the high-energy (HE) expansion improved by Padé approximants with the LME, which extended the validity range of the HE expansion [201]. However, this expansion is only valid for in the invariant mass region $\sqrt{\hat{s}} \gtrsim 750 \text{ GeV}$ and $\sqrt{\hat{s}} \lesssim 350 \text{ GeV}$, which only covers $\sim 32\%$ of the hadronic cross section. Additionally, numerical computation of the two-loop virtual corrections, though implemented exactly in [202], are rather slow for practical use in MC simulations. This highlights the importance of an analytical method that can cover the remaining region of the cross-section and can be merged with the HE expansion via Padé approximants. Fortunately, the two-loop corrections to the triangle diagrams can be computed exactly. And the loop integrals appearing in the box correction having no analytic expression can be expanded in small Z (or Higgs) transverse momentum, p_T . This method was first used for Higgs pair production in [203], to compute the NLO virtual corrections to the box diagrams in the forward kinematics. In chapter 6, I will discuss the calculation preformed by my collaborators and myself and published in [204], which includes the full top mass dependence of the virtual two-loop correction to $gg \rightarrow Zh$ in an analytic form using the same p_T expansion technique.

4.1.4 Associated production with top quarks

The largest part of the $t\bar{t}h/th$ uncertainty budget comes from the theoretical modelling of this process's backgrounds, mainly $t\bar{t}b\bar{b}$, $t\bar{t}W$ as backgrounds for $t\bar{t}(h \rightarrow b\bar{b})$ and $t\bar{t}(h \rightarrow \text{multileptons})$, respectively. There have been several theoretical developments regarding these backgrounds. Starting with $t\bar{t}W$, the differential cross-section at NNLO+ NLO QCD calculation of this channel has been done in [205, 206] including EW corrections. The fully decayed final state at NLO QCD [207–209] and at NLO-EW [210] have been computed. Additionally, these calculations were implemented in **POWHEG-BOX** [211]. The comparison between the NLO-QCD with parton showering vs on-shell can be found in [212]. As for $t\bar{t}b\bar{b}$, the progress in obtaining higher order corrections is faced with challenges posed by the complexity of this channel. However, progress has been made, for instance the off-shell effects in the fully decayed $pp \rightarrow 2\ell 2\nu 4b$ with NLO corrections was studied in [213, 214]. Further discussion of the theoretical developments of these

channels is beyond the scope of this thesis.

Regarding the higher order corrections to the $t\bar{t}h/th$ channel itself, the NLO QCD+EW effects on the off-shell multileptons final state were studied in [215], while the NLO corrections including SMEFT operators were calculated in [216]. The NLO QCD+EW with parton showering is available in all event generators, and the SMEFT operators at NLO are available in `MadGraph5_aMC@NLO`. As of the time of writing this thesis, there is no NNLO calculation of $t\bar{t}h/th$ available.

4.2 Concluding remarks

The precise determination of the Higgs boson properties is one of the main focus of the Large Hadron Collider (LHC) physics programme. In order to achieve precision-level Higgs measurements both experimental and theoretical uncertainties need to be improved. Though the first can be improved with Higher luminosities and energies, better detectors and improved analysis techniques. Theoretical uncertainties require higher-order calculations, inclusion of mixed EW and QCD terms , inclusion of mass effects and suitable parton distribution functions with Higher order in QCD. As we have seen, a lot of effort is being put into improving the theoretical predictions of Higgs production channels. Moreover, many computer tools have been made available to compute these cross-sections, for example `iHixs2` [217] or to generate full events, like `POWHEG` [218–224] and `MadGraph5_aMC@NLO` [225], and many others can be found with greater detail in the Higgs cross-sections working group [226].

Sometimes, to improve the measurement of the process, it is not sufficient to only improve the theoretical prediction of the channel itself, but also its backgrounds, which is particularly important for $t\bar{t}h$. Hence, higher order calculations of processes like $t\bar{t}W$ with parton-shower effects as well as improved analysis to distinguish $t\bar{t}(h \rightarrow b\bar{b})$ have a significant impact on $t\bar{t}h$ measurements. Event generator tools with SMEFT implementation in Higgs processes with patron showing interface capabilities have been implemented in a `MadGraph5_aMC@NLO` model `SMEFTatNLO` [227] which enabled loop computations with SMEFT operators and consequently fits of the SMEFT Wilson coefficients with Higgs data at NLO as we have seen in chapter 3.

There is plenty of room for future improvements in the reduction of theory uncertainty budget, and providing better theoretical prediction of the Higgs processes in the SM and beyond. From inclusion of patron shower matching , merging and validation to inclusion of two-loop calculations of gluon fusion Zh and EW NLO effects of $t\bar{t}h$, all in preparation to the HL-LHC Higgs precision era !

5 Four top operator in Higgs production and decay

In chapter 3, the SM effective field theory has been portrayed as a pragmatic yet robust parametrisation of potential NP degrees of freedom for LHC searches, with the ansatz that these degrees of freedom have masses that are higher than the LHC reach. From the discussion and overview of Higgs-related SMEFT operator in that chapter, the operator \mathcal{O}_ϕ stood out as one of the weakly constrained amongst them. This is due to the current low experimental sensitivity on the Higgs self-coupling as shown in ??.

The physics of the top quark is deeply intertwined with Higgs physics, and when one starts looking at the operators entering at NLO of Higgs processes, and by restricting oneself to pure Higgs or EW operators, one would miss the full picture in a global fit. Namely, the top quark operators. Though many of these operators are strongly constraint from top observables, a subset of them remain as weakly constraint as the trilinear Higgs self-coupling. These operators are four-fermion operators involving the third generation quarks. They would be constrained directly from the production of four tops observation. However, this process has small cross-section at the LHC of $\sim 12 \text{ fb}$ [228], which is more or less comparable to the Higgs pair production signal strength. In addition, we have seen in the previous chapter that the theoretical predictions of $t\bar{t}b\bar{b}$ remain limited. Experimental searches for the production of four top quarks has been first made by CMS [229] combining different LHC runs, followed by ATLAS [230], the latter reporting a 4.3σ observation of this processes with cross-section of 24^{+7}_{-6} fb . When the whole third generation quarks is included, one sees the same story with $t\bar{t}b\bar{b}$ contact interaction which require the observation of $t\bar{t}b\bar{b}$ production for a direct constraint, see [231, 232] for experimental searches and [233, 234] for SMEFT fits. It should be noted that for the production of four tops, or two tops two beauty quarks in SMEFT, the contact terms do not interfere with the SM process, and only appear proportional to $\mathcal{O}(1/\Lambda^4)$. This makes the SMEFT global analysis of these operators depend highly on the EFT truncation scheme used, i.e. whether to keep quadratic terms or not.

These four-fermion operators enter in single Higgs processes at NLO, in a similar manner as the Higgs self-coupling. In this chapter, the exact NLO corrections to the Higgs rates, i.e. production and decay, due to these four-fermion operators have been computed, and it was found to be significantly larger or at the same scale as the corrections from C_ϕ . Since the four-fermions operators are weakly constrained they should be included in fits involving Higgs data. We shall demonstrate that, there is a significant correlation amongst the Higgs self-coupling and the four-fermion operators.

As the direct bounds for $t\bar{t}t\bar{t}$ and $t\bar{t}b\bar{b}$ contact interactions are weak, single Higgs data provides competitive bounds of these operators alongside other alternative constraints

like top quark pair production [227] and electroweak precision data [235].

The chapter is based on a the paper [236] and structured as follows: in ?? the full NLO calculation of Higgs rates due to the four-fermion operators is illustrated. Afterwards, in section 5.2, a fit from Higgs data combining the Higgs trilinear coupling and the four-fermion operators is presented, for both Run-II and HL-LHC, with more elaborate results for the latter is found in ?? . The results are further discussed in section 5.3.

5.1 Contribution of four-fermion operators to Higgs rates at NLO

We will consider the following dimension-six SMEFT operators in the NLO calculations

Four-Heavy-quarks SMEFT operators modifying Higgs rates at NLO

Operators with homogenous chiral structure, i.e. (RR)(RR) or (LL)(LL)

$$\mathcal{O}_{tt}, \mathcal{O}_{bb}, \mathcal{O}_{tb}^{(1)}, \mathcal{O}_{tb}^{(8)}, \mathcal{O}_{QQ}^{(1)}, \mathcal{O}_{QQ}^{(3)}. \quad (5.1)$$

Operators with heterogeneous chiral structure, i.e. (LR)(LR) or (LL)(RR)

$$\mathcal{O}_{Qt}^{(1)}, \mathcal{O}_{Qt}^{(8)}, \mathcal{O}_{Qb}^{(1)}, \mathcal{O}_{Qb}^{(8)}, \mathcal{O}_{QtQb}^{(1)}, \mathcal{O}_{QtQb}^{(8)} \quad (5.2)$$

The explicit definition of these operators can be found in Table 3.1. However, the notation is slightly modified from the standard Warsaw basis one. The flavour indices were suppressed since only the the third generation is considered throughout this chapter. Adopting the same notation from previous chapters, Q denotes the (heavy) left-handed $SU(2)_L$ doublet quarks while t and b refer to the right-handed singlets. In studies involving SMEFT fits, such as [140] the $SU(3)_C$ singlet and octet left-handed operators $\mathcal{O}_{QQ}^{(1),SU(3)}, \mathcal{O}_{QQ}^{(8)}$ are used instead of the singlet and triplet of $SU(2)_L$ appearing in the stabdard Warsaw basis. These two conventions' Wilson coefficients are related via the relations

$$\begin{aligned} C_{QQ}^{(1),SU(3)} &= 2C_{QQ}^{(1)} - \frac{2}{3}C_{QQ}^{(3)}, \\ C_{QQ}^{(8)} &= 8C_{QQ}^{(3)}. \end{aligned} \quad (5.3)$$

Additionally, all of these Wilson coefficients are assumed to be real.

From here on, only operators that induce sizeable NLO correction to Higgs processes are taken into account. These operators turns out to be the ones that introduce loop corrections to the top or beauty Yukawa, top or beauty masses and finite corrections from top loops. Such corrections will be proportional to the top mass. On the contrary, corrections from beauty loops are highly suppressed by m_b . Also, operators that have chiral structure that does not enable them to enter in the Yukawa renormalisation group

equation (RGE)'s will not be constrained from Higgs data as they would only contribute through small finite terms, as we shall see later. Hence, only four top and the $\mathcal{O}_{QtQb}^{(1),(8)}$ operators will be considered, as they will possess corrections with top quark loops.

This section will demonstrate the calculation of NLO Higgs production and decay rates from the four-heavy-quarks operators discussed above. For the production of Higgs via gluon fusion or Higgs decay to gluon, photons and beauty quarks, the results were computed fully analytically and presented in this section. However, for the associated production of the Higgs with top pair $t\bar{t}h$, the corrections were computed numerically, due to the length of the the analytic expressions if the result.

5.1.1 Analytic calculations

The NLO corrections to gluon fusion, $h \rightarrow gg$, $h \rightarrow \gamma\gamma$ and $h \rightarrow b\bar{b}$ all come from the sub-diagrams listed in Table 5.1, with top loops entering in the mass renormalisation or to/beauty Yukawa vertex correction. Where $N_c = 3$ the number of colours, and $c_F = (N_c^2 - 1)/(2N_c) = 4/3$ the $SU(3)$ quadratic Casimir in the fundamental representation. The effect of beauty loops coming from for $C_{QtQb}^{(1/8)}$, can be easily read from this table by

Diagram	colour factor		mass/coupling
	singlet	octet	
	$2N_c + 1$	c_F	$y_t m_b m_t^2$
	1	c_F	$y_t m_t^3$
	$2N_c + 1$	c_F	m_t^3
	1	c_F	m_t^3

Table 5.1. The sub diagrams contributing to the NLO corrections of gluon fusion Higgs production higgsdecay to gluon, photon and beauty quarks.

exchanging $t \leftrightarrow b$, which is significantly smaller than the corrections coming from top loops.

We see that these corrections correspond to the Wilson coefficients appearing in the RGE's **include them in the appendix**, and operators with (LL)(LL) or (RR(RR)) chiral structures do not contribute to these processes.

By considering the two-loop corrections to the gluon fusion illustrated in Figure 5.1 we find that such correction contain the sub-diagrams shown in Table 5.1, except for diagram (e), which is found to be vanishing for on-shell gluons. Additionally, these diagrams indicated that the two-loop corrections will be reduced to a product of two one-loop functions after the integral reduction.

Following the Feynman rules derived in ref. [237] for the four-fermion operators of interest here, the *ggtoh* two-loop amplitude was calculated, then Dirac algebra and further algebraic manipulations were preformed in Mathematica using **PackageX** [238]. Reduction of the resulting two-loop to Master integrals has been preformed using **KIRA** [239], all of the resulting master integrals were indeed products on one-loop functions as expected. The computation has been cross-checked independently by my collaborators, using a different pipeline : **FeynArts** [240], for amplitude generation then **FeynRules** [241] and **Fire** [242] for algebraic manipulation and loop-integral reduction.

The sub-diagrams appearing in the two-loop calculation, correspond to mass and vertex renormalisation, hence they contain poles that require counter-terms. A mixture of on-shell (OS) and $\overline{\text{MS}}$ – schemes has been used for the mass and $hq\bar{q}$ coupling renormalisation, respectively. The renormalisation of SM quantities in the OS and NP ones in the $\overline{\text{MS}}$ scheme was proposed by [243], which provides consistency since the NP is assumed to be of a Higher scale than the SM.

The top/beauty mass renormalisation can be expressed as

$$m_{t/b}^{\text{OS}} = m_{t/b}^{(0)} - \delta m_{t/b}, \quad (5.4)$$

with the corresponding counter-terms

$$\begin{aligned} \delta m_t &= \frac{1}{16\pi^2} \frac{C_{Qt}^{(1)} + c_F C_{Qt}^{(8)}}{\Lambda^2} m_t^3 \left[\frac{2}{\epsilon} + 2 \log \left(\frac{\mu_R^2}{m_t^2} \right) + 1 \right] \\ &\quad + \frac{1}{16\pi^2} \frac{(2N_c + 1) C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \left[\frac{1}{\epsilon} + \log \left(\frac{\mu_R^2}{m_b^2} \right) + 1 \right] m_b^3, \end{aligned} \quad (5.5)$$

$$\delta m_b = \frac{1}{16\pi^2} \frac{(2N_c + 1) C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \left[\frac{1}{\epsilon} + \log \left(\frac{\mu_R^2}{m_t^2} \right) + 1 \right] m_t^3, \quad (5.6)$$

with $\bar{\epsilon}^{-1} = \epsilon^{-1} - \gamma_E + \log(4\pi)$, in dimensional regularization with $d = 4 - 2\epsilon$. It is possible

to convert from OS to the $\overline{\text{MS}}$ – scheme for mass counter-terms via the following relations

$$\delta m_t^{\overline{\text{MS}}} = \frac{1}{8\pi^2} \frac{C_{Qt}^{(1)} + c_F C_{Qt}^{(8)}}{\Lambda^2} m_t^3 \frac{1}{\bar{\epsilon}} + \frac{1}{16\pi^2} \frac{(2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \frac{1}{\bar{\epsilon}} m_b^3, \quad (5.7)$$

$$\delta m_b^{\overline{\text{MS}}} = \frac{1}{16\pi^2} \frac{(2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \frac{1}{\bar{\epsilon}} m_t^3. \quad (5.8)$$

The effect of changing to the mass renormalisation scheme is small for the top mass but rather significant, up to 100% for the beauty mass.

The top/beauty Higgs coupling in SMEFT, is written as

$$g_{ht\bar{t}/hb\bar{b}} = \frac{m_{t/b}}{v} - \frac{v^2}{\Lambda^2} \frac{C_{t\phi/b\phi}}{\sqrt{2}}. \quad (5.9)$$

Hence, a modification of the Higgs couplings to bottom and top quarks is generated by operator mixing, even if $C_{t\phi/b\phi}$ are zero at Λ . From this, the $\overline{\text{MS}}$ counter-term should take the form

$$\delta g_{ht\bar{t}/hb\bar{b}} = \frac{m_{t/b}}{v} \delta m_{t/b} - \frac{v^2 \delta C_{t\phi/b\phi}}{\sqrt{2}}, \quad (5.10)$$

where $\delta C_{t\phi/b\phi}$ is directly read from the anomalous dimension, see App for the explicit expression of the RGE's.

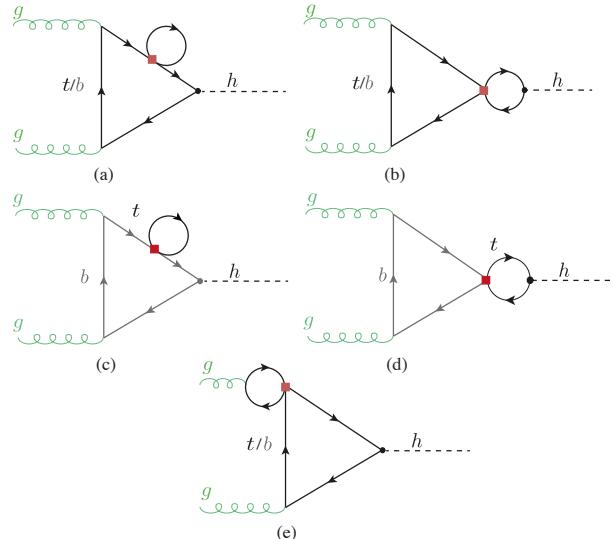


Figure 5.1. Example Feynman diagrams for four-fermion-operator contributions to the Higgs production via gluon fusion. The red box indicates the four-fermion operator.

Correction to gluon fusion and $h \rightarrow gg$

The modification of the Higgs production via gluon fusion can be written as

$$\frac{\sigma_{ggF}}{\sigma_{ggF}^{\text{SM}}} = 1 + \frac{\sum_{i=t,b} 2\text{Re}(F_{\text{LO}}^i F_{\text{NLO}}^*)}{|F_{\text{LO}}^t + F_{\text{LO}}^b|^2} \quad (5.11)$$

with

$$F_{\text{LO}}^i = -\frac{8m_i^2}{m_h^2} \left[1 - \frac{1}{4} \log^2(x_i) \left(1 - \frac{4m_i^2}{m_h^2} \right) \right] \quad (5.12)$$

and

$$\begin{aligned} F_{\text{NLO}} = & \frac{1}{4\pi^2 \Lambda^2} (C_{Qt}^{(1)} + c_F C_{Qt}^{(8)}) F_{\text{LO}}^t \left[2m_t^2 + \frac{1}{4} (m_h^2 - 4m_t^2) \left(3 + 2\sqrt{1 - \frac{4m_t^2}{m_h^2}} \log(x_t) \right) \right. \\ & \left. + \frac{1}{2} (m_h^2 - 4m_t^2) \log \left(\frac{\mu_R^2}{m_t^2} \right) \right] \\ & + \frac{1}{32\pi^2 \Lambda^2} ((2N_c + 1) C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}) \left[F_{\text{LO}}^b \frac{m_t}{m_b} (4m_t^2 - 2m_h^2 \right. \\ & \left. - (m_h^2 - 4m_t^2) \sqrt{1 - \frac{4m_t^2}{m_h^2}} \log(x_t) - (m_h^2 - 4m_t^2) \log \left(\frac{\mu_R^2}{m_t^2} \right)) + (t \leftrightarrow b) \right]. \end{aligned} \quad (5.13)$$

Only top quark loops contribute to the parts proportional to $C_{Qt}^{(1),(8)}$. The variable x_i for a loop particle with mass m_i is given by

$$x_i = \frac{-1 + \sqrt{1 - \frac{4m_i^2}{m_h^2}}}{1 + \sqrt{1 - \frac{4m_i^2}{m_h^2}}}. \quad (5.14)$$

Using the same amplitudes, the $h \rightarrow gg$ partial width modification can be written as

$$\frac{\Gamma_{h \rightarrow gg}}{\Gamma_{h \rightarrow gg}^{\text{SM}}} = 1 + \frac{\sum_{i=t,b} 2\text{Re}(F_{\text{LO},i}^i F_{\text{NLO},i}^*)}{|F_{\text{LO},t}^i + F_{\text{LO},b}^i|^2} \quad (5.15)$$

Correction to Higgs decays to photons

Analogously, since the decay $h \rightarrow \gamma\gamma$ contains the same topologies as gluon fusion, we could use the result from the above calculation to calculate the correction to the partial width for this decay

$$\frac{\Gamma_{h \rightarrow \gamma\gamma}}{\Gamma_{h \rightarrow \gamma\gamma}^{\text{SM}}} = 1 + \frac{2\text{Re}(F_{\text{LO},\gamma} F_{\text{NLO},\gamma}^*)}{|F_{\text{LO},\gamma}|^2}. \quad (5.16)$$

However, one should pay attention to the change in the prefactors, and the extra

EW contributions for $h \rightarrow \gamma\gamma$

$$F_{\text{LO},\gamma} = N_C Q_t^2 F_{\text{LO}}^t + N_C Q_b^2 F_{\text{LO}}^b + F_{\text{LO}}^W + F_{\text{LO}}^G, \quad (5.17)$$

and $F_{\text{NLO},\gamma}$ is obtained from F_{NLO} by replacing the LO form factor that appears inside of it by $F_{\text{LO}}^i \rightarrow N_c Q_i^2 F_{\text{LO}}^i$, with the charges $Q_t = 2/3$ and $Q_b = -1/3$. The W boson contribution

$$F_{\text{LO}}^W = 2 \left(1 + 6 \frac{m_W^2}{m_h^2} \right) - 6 \frac{m_W^2}{m_h^2} \left(1 - 2 \frac{m_W^2}{m_h^2} \right) \log^2(x_W), \quad (5.18)$$

with m_W the W mass, and the Goldstone contribution

$$F_{\text{LO}}^G = 4 \frac{m_W^2}{m_h^2} \left(1 + \frac{m_W^2}{m_h^2} \log^2(x_W) \right). \quad (5.19)$$

Four-fermion operators also affect the $h \rightarrow Z\gamma$ partial width. However, as in the diphoton case, the effect is expected to be small due to the dominance of the W boson loop. Because of this, and given the smallness of the $h \rightarrow Z\gamma$ branching ratio and the relatively low precision expected in this channel at the LHC, the effects of four-fermion interactions in this decay are neglected.

Correction to Higgs decays to $b\bar{b}$

The dominant four-fermion contributions to decay channel $h \rightarrow b\bar{b}$ come from the operators with Wilson coefficients $C_{QtQb}^{(1),(8)}$. The corresponding diagram at NLO is shown in fig 5.2. Adopting the same renormalisation procedure as outlined in the previous subsection, we obtain the following expression for the correction to the $h \rightarrow b\bar{b}$ decay rate in the presence of $\mathcal{O}_{QtQb}^{(1),(8)}$,

$$\begin{aligned} \frac{\Gamma_{h \rightarrow b\bar{b}}}{\Gamma_{h \rightarrow b\bar{b}}^{\text{SM}}} &= 1 + \frac{1}{16\pi^2} \frac{m_t}{m_b} (m_h^2 - 4m_t^2) \frac{(2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \\ &\times \left[2 + \sqrt{1 - \frac{4m_t^2}{m_h^2}} \log(x_t) - \log\left(\frac{m_t^2}{\mu_R^2}\right) \right], \end{aligned} \quad (5.20)$$

which carries an enhancement factor of m_t/m_b and is hence expected to be rather large.

The results of the NLO effects from the four-fermion operators reported above, do not take into account the running of the Wilson coefficients. This would be based on the assumption that these coefficients are defined at the process scale. Nevertheless, when we want to compare different process or assume that the four-fermion operators are defined at the UV scale, i.e. Λ , for example after matching with some UV model. One has to take into account the running of these Wilson coefficients from Λ down to the process scale. Those running effects can be included via the renormalisation group

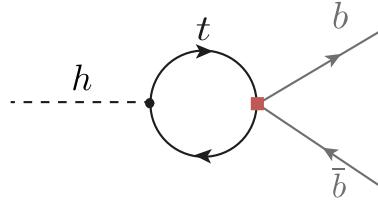


Figure 5.2. Feynman diagram contributing to the NLO $h \rightarrow b\bar{b}$ process.

equation (RGE) for the operators with Wilson coefficient $C_{t\phi}$ and $C_{b\phi}$ [244, 245], that lead approximatively to

$$C_{t\phi}(\mu_R) - C_{t\phi}(\Lambda) = \frac{1}{16\pi^2 v^2} \left[-2y_t(m_h^2 - 4m_t^2)(C_{Qt}^{(1)} + c_F C_{Qt}^{(8)}) \log\left(\frac{\mu_R^2}{\Lambda^2}\right) + \frac{y_b}{2}(m_h^2 - 4m_b^2) ((2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}) \log\left(\frac{\mu_R^2}{\Lambda^2}\right) \right] \quad (5.21)$$

and

$$C_{b\phi}(\mu_R) - C_{b\phi}(\Lambda) = \frac{y_t}{32\pi^2 v^2} \left[(m_h^2 - 4m_t^2) ((2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}) \log\left(\frac{\mu_R^2}{\Lambda^2}\right) \right], \quad (5.22)$$

where $y_{t/b} = \sqrt{2}m_{t/b}/v$. Note that the combinations of Wilson coefficients appearing in (5.21)-(5.22) are the same as in F_{NLO} in (5.13). Effectively, we can then obtain the result under the assumption that the four-fermion operators are the only non-zero ones at the high scale by replacing in (5.13) $\mu_R \rightarrow \Lambda$, noting that we have renormalised the top and beauty quark masses in the OS scheme. Including the leading logarithmic running of $C_{b\phi}$ of (5.22) from the high scale Λ to the electroweak scale is achieved by setting in (5.20) $\mu_R \rightarrow \Lambda$. The expression in (5.20) agrees with results obtained from the full calculation of the NLO effects in the dimension-six SMEFT, first computed in [246].

5.1.2 SMEFT-NLO calculation of $t\bar{t}h$

Unlike the previous processes, the associated production of the Higgs with top quark pair involves new topologies not limited to Yukawa vertex or mass renormalisation. At the LHC, there are two sub-processes responsible for the $t\bar{t}h$ production: gluon-initiated process illustrated in Figure 5.3 and quark-initiated one, see in Figure 5.4. We see the new *finite* topologies induced by the four-fermion operator corrections in (d) triangle and (e) box topologies in Figure 5.3 and (b) triangle topology in Figure 5.4. Additionally, the $t\bar{t}g$ vertex correction in the quark-initiated process (diagram (c)) of Figure 5.4 is non-vanishing as the gluon is off-shell. This vertex correction has a UV pole that requires a

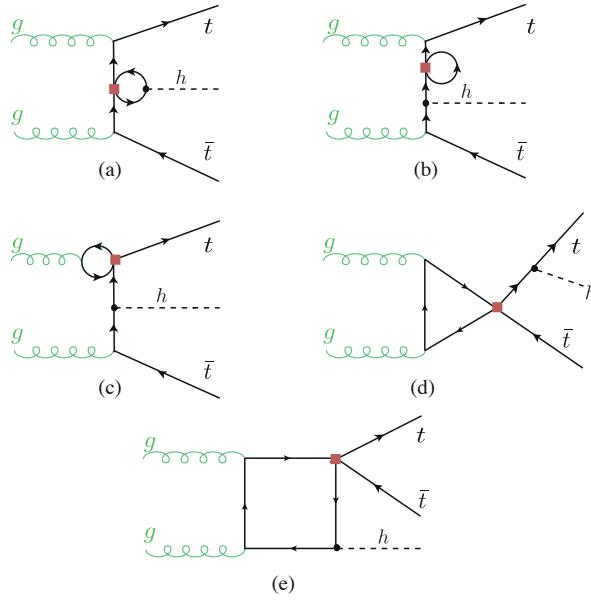


Figure 5.3. Feynman diagrams including the four-fermion loop contributions to the $gg \rightarrow t\bar{t}h$ subprocess.

counter-term for its cancellation

$$\text{---} \overset{\text{---}}{\star} \text{---} = \frac{ig_s}{12\pi^2\Lambda^2} T_{ij}^A p_g^2 \gamma^\mu \left(C_{tt} P_R + \left(C_{QQ}^{(1)} + C_{QQ}^{(3)} \right) P_L + \frac{C_{Qt}^{(8)}}{4} \right) \left(\frac{1}{\epsilon} - 1 \right). \quad (5.23)$$

Another difference between $t\bar{t}h$ and the rest of the processes considered, is that this process has multiple colour projectors, as the quark anti quark triplets or the gluon pairs do not have to recombine to only a singlet state rather to both a singlet and an octet, according to the expansion of product $\mathbf{3} \otimes \overline{\mathbf{3}} \rightarrow \mathbf{1} + \mathbf{8}$. This breaks the degeneracy between the singlet and octet Wilson coefficients. Lastly, due to the new topologies and $t\bar{t}g$ vertex correction, operators with single chirality will contribute to NLO corrections, namely C_{tt} and $C_{QQ}^{(1,3)}$.

All of the four-fermion operators are implemented in the loop-capable UFO model SMEFTatNLO [227] and their contribution to NLO corrections of $t\bar{t}h$ can hence be computed via Madgraph_aMCNLO [225] (version 3.1.0) with some tweaking to remove the NLO QCD corrections. This is done via a user-defined loop filter function in Madgraph. The results were reproduced by an analytic computation based on the reduction of one-loop amplitudes via the method developed by G. Ossola, C.G. Papadopoulos and R. Pittau (OPP reduction) [247]. The OPP reduction was done using the CutTools programme [248]. This programme takes the full one-loop amplitude and then reduces it to terms with 1,2,3 and 4-point loop functions in four dimensions, keeping spurious terms from the ϵ part of the amplitude. To correct for such terms, one needs to compute the

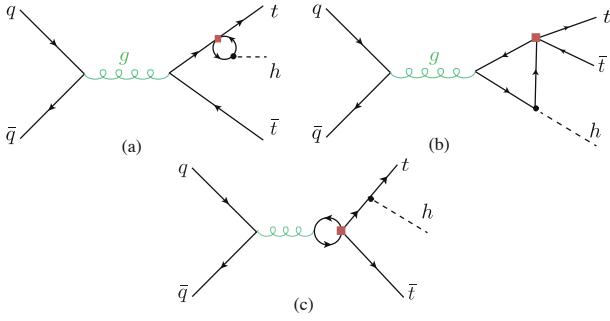


Figure 5.4. Feynman diagrams including the four-fermion loop contributions to the $q\bar{q} \rightarrow t\bar{t}h$ subprocess.

divergent UV counter-term as well as a finite rational terms, denoted R_2 as in Ref. [249].¹ The amplitudes were generated in the same way as for gluon fusion. The UV and R_2 counter-terms, that need to be supplemented to `CutTools`, were computed manually following the method detailed in [249]. For both codes, the NNPDF23 parton distribution functions set at NLO [250] was used.

The singlet and octet operators $\mathcal{O}_{Q_t Q_b}^{(1),(8)}$ contribute to $t\bar{t}h$ only via beauty loops and in principle, could be directly dismissed like the other beauty quark operators mentioned above. However, it is instructive to investigate their effect albeit it is expected to be small. Since the `SMEFTatNLO` model does not have these operators, it was needed to implement them manually in that model. This is simply done by include the vertices generated by these operators as well as their UV and R_2 counter-terms, only relevant for $t\bar{t}h$ calculation. The calculation of the NLO correction by these operators was done both in Madgraph using a modified UFO model and with the code based on `CutTools`. The effects where comparable to the leading log effects computed using `SMEFTsim` package [251] of $\sim 10^{-6}$. Hence confirming the expectation that beauty quark loops have a negligible effect.

In order to take the effect of Wilson coefficients' running, the relevant contribution for the gluon-initiated process as the same as the stated for the gluon fusion in (5.21). While for the quark-initiated process, one needs to consider the operator mixing in the running, particularly between operators that contain second and third generation quarks mixed together. These corrections can be obtained from the RGEs in refs. [129, 244, 245].

5.1.3 Results

The NLO correction from the four-fermion operators of the third generation quarks on the Higgs rates i.e., partial width Γ or cross-section σ , is extracted from the above

¹Another rational term R_1 appears due to the mismatch between the four and d dimensional amplitudes, but this is computed automatically in `CutTools`.

computation using the formula

$$\delta R(C_i) = R/R^{\text{SM}} - 1, \quad (5.24)$$

here effect from the operator with Wilson coefficient C_i on the Higgs rate R is denoted by $\delta R(C_i)$. Only contributions linear in the Wilson coefficients are considered. In order to isolate the finite terms from the ones coming from the RGE leading log approximation, the correction is further expanded to finite $\delta R_{C_i}^{fin}$ and leading log terms $\delta R_{C_i}^{log}$ as follows

$$\delta R(C_i) = \frac{C_i}{\Lambda^2} \left(\delta R_{C_i}^{fin} + \delta R_{C_i}^{log} \log \left(\frac{\mu_R^2}{\Lambda^2} \right) \right). \quad (5.25)$$

Using this formula, one can obtain the correction at any NP scale Λ , though in the remainder of this chapter this scale is set to 1 TeV. In [Table 5.2](#), the finite and logarithmic corrections for the operators considered in this study is reported. Using this table in filling the formula (5.25) will give the correction to Higgs rates. However, since some of the rates are Higgs partial widths, the Higgs total width Γ_h will be affected and therefore all of Higgs rates are changed. An important observation from [Table 5.2](#) is that the finite terms, are either larger or at the same order than the leading log ones, except for $h \rightarrow b\bar{b}$ corrections from $\mathcal{O}_{QtQb}^{(1),(8)}$. This highlights the importance of thee full NLO calculation for these corrections in constraining these four-fermion operators, in particular $\mathcal{O}_{Qt}^{(1),(8)}$.

As mentioned earlier, there is a degeneracy amongst the singlet and octet operators, seen clearly in the analytic result for gluon fusion and Higgs decays considered. This degeneracy is though broken for $\mathcal{O}_{Qt}^{(1),(8)}$ due to $t\bar{t}h$. Since, the effect of $\mathcal{O}_{QtQb}^{(1),(8)}$ is negligible for this process, thee true degree of freedom for these operators' Wilson coefficients is the linear combination

$$C_{QtQb}^+ = (2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}. \quad (5.26)$$

5.2 Fit to Higgs observables

Using the results from the previous NLO calculations, and combining them with the calculations of NLO Higgs rates from the trilinear Higgs self-coupling λ_3 , preformed in refs. [113–116, 118] we could expand on the previous fits for λ_3 from Higgs data, to include four-fermion SMEFT Wilson coefficients as well. In order to examine the true sensitivity of single Higgs observables to λ_3 . Although combined fits from Higgs data including λ_3 and SMEFT operators modifying Higgs rates at LO has been preformed [146]. Such fits would not be sufficient in determine the actual sensitivity for λ_3 , in particular when the SMEFT operators are weakly constraint and possess significant modifications to Higgs rates as we have seen in [Table 5.2](#). This chapter does not include a global SMEFT fit, but merely motivates it by illustrating how thee sensitivity for probing the Higgs-self coupling from single Higgs data gets diluted when the four-fermion operators are included, and how these two are correlated.

Operator	Process	μ_R	$\delta R_{C_i}^{fin}$ [TeV 2]	$\delta R_{C_i}^{log}$ [TeV 2]
$\mathcal{O}_{Qt}^{(1)}$	ggF	$\frac{m_h}{2}$	$9.91 \cdot 10^{-3}$	$2.76 \cdot 10^{-3}$
	$h \rightarrow gg$	m_h	$6.08 \cdot 10^{-3}$	$2.76 \cdot 10^{-3}$
	$h \rightarrow \gamma\gamma$		$-1.76 \cdot 10^{-3}$	$-0.80 \cdot 10^{-3}$
	$t\bar{t}h$ 13 TeV	$m_t + \frac{m_h}{2}$	$-4.20 \cdot 10^{-1}$	$-2.78 \cdot 10^{-3}$
$\mathcal{O}_{Qt}^{(8)}$	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$-4.30 \cdot 10^{-1}$	$-2.78 \cdot 10^{-3}$
	ggF	$\frac{m_h}{2}$	$1.32 \cdot 10^{-2}$	$3.68 \cdot 10^{-3}$
	$h \rightarrow gg$	m_h	$8.11 \cdot 10^{-3}$	$3.68 \cdot 10^{-3}$
	$h \rightarrow \gamma\gamma$		$-2.09 \cdot 10^{-3}$	$-1.07 \cdot 10^{-3}$
$\mathcal{O}_{QtQb}^{(1)}$	$t\bar{t}h$ 13 TeV	$m_t + \frac{m_h}{2}$	$6.81 \cdot 10^{-2}$	$-2.40 \cdot 10^{-3}$
	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$7.29 \cdot 10^{-2}$	$-2.48 \cdot 10^{-3}$
	ggF	$\frac{m_h}{2}$	$2.84 \cdot 10^{-2}$	$9.21 \cdot 10^{-3}$
	$h \rightarrow gg$	m_h	$1.57 \cdot 10^{-2}$	$9.21 \cdot 10^{-3}$
$\mathcal{O}_{QtQb}^{(8)}$	$h \rightarrow \gamma\gamma$		$-1.30 \cdot 10^{-3}$	$-0.78 \cdot 10^{-3}$
	$h \rightarrow b\bar{b}$		$9.25 \cdot 10^{-2}$	$1.68 \cdot 10^{-1}$
	ggF	$\frac{m_h}{2}$	$5.41 \cdot 10^{-3}$	$1.76 \cdot 10^{-3}$
	$h \rightarrow gg$	m_h	$2.98 \cdot 10^{-3}$	$1.76 \cdot 10^{-3}$
$\mathcal{O}_{QQ}^{(1)}$	$h \rightarrow \gamma\gamma$		$-0.25 \cdot 10^{-3}$	$-0.15 \cdot 10^{-3}$
	$h \rightarrow b\bar{b}$		$1.76 \cdot 10^{-2}$	$3.20 \cdot 10^{-2}$
$\mathcal{O}_{QQ}^{(3)}$	$t\bar{t}h$ 13 TeV	$m_t + \frac{m_h}{2}$	$1.75 \cdot 10^{-3}$	$1.84 \cdot 10^{-3}$
	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$1.65 \cdot 10^{-3}$	$1.76 \cdot 10^{-3}$
\mathcal{O}_{tt}	$t\bar{t}h$ 13 TeV	$m_t + \frac{m_h}{2}$	$4.60 \cdot 10^{-3}$	$1.82 \cdot 10^{-3}$
	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$4.57 \cdot 10^{-3}$	$1.74 \cdot 10^{-3}$

Table 5.2. The NLO effects of the four heavy-quarks operators on the Higgs rates. The effects are separated into finite $\delta R_{C_i}^{fin}$ and leading log parts, in correspondence with (??). Effects of $\mathcal{O}(10^{-5} - 10^{-6})$ TeV $^{-2}$ have been omitted from this table. This table has been published in [236]

In the previous references, the modification to Higgs self coupling was reported in terms of the κ -formalism, for the consistency of this analysis, the NLO corrections from the trilinear self-coupling will be converted from this formalism to the SMEFT notation, in terms of the Wilson coefficient C_ϕ . For more details on the conversion between SMEFT and κ -formalism see subsection 3.2.2. In order to keep track of power counting (in terms of Λ) in SMEFT, we expand the results of [114] after converting it to SMEFT, to get

$$\delta R_{\lambda_3} \equiv \frac{R_{\text{NLO}}(\lambda_3) - R_{\text{NLO}}(\lambda_3^{\text{SM}})}{R_{\text{LO}}} = -2 \frac{C_\phi v^4}{\Lambda^2 m_h^2} C_1 + \left(-4 \frac{C_\phi v^4}{\Lambda^2 m_h^2} + 4 \frac{C_\phi^2 v^8}{m_h^4 \Lambda^4} \right) C_2. \quad (5.27)$$

In (5.27), the coefficient C_1 corresponds to the contribution of the trilinear coupling to the single Higgs processes at one loop, adopting the same notation as [114]. The values of C_1 for the different processes of interest for this paper are given in ???. The coefficient

C_2 describes universal corrections and is given by

$$C_2 = \frac{\delta Z_h}{1 - \left(1 - \frac{2C_\phi v^4}{\Lambda^2 m_h^2}\right)^2 \delta Z_h}, \quad (5.28)$$

where the constant δZ_h is the SM contribution from the Higgs loops to the wave function renormalisation of the Higgs boson,

$$\delta Z_h = -\frac{9}{16} \frac{G_F m_h^2}{\sqrt{2\pi^2}} \left(\frac{2\pi}{3\sqrt{3}} - 1 \right). \quad (5.29)$$

The coefficient C_2 thus introduces additional $\mathcal{O}(1/\Lambda^4)$ (and higher order) terms in δR_{λ_3} . In ref. [114] considering the κ formalism the full expression of (5.28) is kept, while we define two different descriptions: one in which we expand δR_{λ_3} up to linear order and an alternative scheme in which we keep also terms up to $\mathcal{O}(1/\Lambda^4)$ in the EFT expansion. Keeping the full expression in (5.28) and including terms up to $\mathcal{O}(1/\Lambda^4)$ in C_2 lead to nearly the same results as the simple $\mathcal{O}(1/\Lambda^4)$ fit.

Process	C_1	$\delta R_{C_\phi}^{fin}$
ggF/ $gg \rightarrow h$	$6.60 \cdot 10^{-3}$	$-3.10 \cdot 10^{-3}$
$t\bar{t}h$ 13 TeV	$3.51 \cdot 10^{-2}$	$-1.64 \cdot 10^{-2}$
$t\bar{t}h$ 14 TeV	$3.47 \cdot 10^{-2}$	$-1.62 \cdot 10^{-2}$
$h \rightarrow \gamma\gamma$	$4.90 \cdot 10^{-3}$	$-2.30 \cdot 10^{-3}$
$h \rightarrow b\bar{b}$	0.00	0.00
$h \rightarrow W^+W^-$	$7.30 \cdot 10^{-3}$	$-3.40 \cdot 10^{-3}$
$h \rightarrow ZZ$	$8.30 \cdot 10^{-3}$	$-3.90 \cdot 10^{-3}$
$pp \rightarrow Zh$ 13 TeV	$1.19 \cdot 10^{-2}$	$-5.60 \cdot 10^{-3}$
$pp \rightarrow Zh$ 14 TeV	$1.18 \cdot 10^{-2}$	$-5.50 \cdot 10^{-3}$
$pp \rightarrow W^\pm h$	$1.03 \cdot 10^{-2}$	$-4.80 \cdot 10^{-3}$
VBF	$6.50 \cdot 10^{-3}$	$-3.00 \cdot 10^{-3}$
$h \rightarrow 4\ell$	$8.20 \cdot 10^{-3}$	$-3.80 \cdot 10^{-3}$

Table 5.3. The NLO dependence of single Higgs rate on C_ϕ , these results were computed in [118]. The C_1 coefficients are to be used in eq. (5.27), while for a direct comparison with the effect of the four-fermion operators, we quote the translated effect $\delta R_{C_\phi}^{fin}$, which can be used directly in eq. (5.25). If the value of \sqrt{s} is not indicated the effect is the same for both 13 and 14 TeV. This table has been published in [236]

A Bayesian fit was preformed using Markov-chain Monte Carlo (MCMC) method. Using a flat prior s $\pi(C_i) = const.$ and a log likelihood of a Gaussian distribution

$$\log(L) = -\frac{1}{2} \left[(\vec{\mu}_{\text{Exp}} - \vec{\mu})^T \cdot \mathbf{V}^{-1} \cdot (\vec{\mu}_{\text{Exp}} - \vec{\mu}) \right]. \quad (5.30)$$

Constructed as follows:

Experimental input $\vec{\mu}_{\text{Exp}}$ The signal strength from experimental measurements of single Higgs rates defined as

$$\mu_{\text{Exp}} \equiv \sigma_{\text{Obs}}/\sigma_{\text{SM}}. \quad (5.31)$$

These measurements are taken from LHC Run II for centre-of-mass energy of $\sqrt{s} = 13$ TeV and integrated luminosity of 139 fb^{-1} for ATLAS and 137 fb^{-1} for CMS. In addition to HL-LHC projections by CMS for $\sqrt{s} = 14$ TeV and integrated luminosity of 3000 fb^{-1} . Both of these input types have been already discussed in chapter 2 and summarised in Table 2.1.

Theoretical prediction $\vec{\mu}$ The corresponding theoretical predictions for each of the experimental measurement /projection have been built using the modification to the cross-sections and branching ratios coming from the SMEFT four-fermion operators and C_ϕ . To keep with the power-counting, the signal strength is also expanded in powers of Λ , keeping only Λ^{-2} terms.

$$\mu(C_\phi, C_i) = \frac{\sigma_{\text{Prod}}(C_\phi, C_i) \times \text{BR}(C_\phi, C_i)}{\sigma_{\text{Prod,SM}} \times \text{BR}_{\text{SM}}} \approx 1 + \delta\sigma(C_\phi, C_i) + \delta\Gamma(C_\phi, C_i) - \delta\Gamma_h(C_\phi, C_i). \quad (5.32)$$

Uncertainties and correlations \mathbf{V} The correlation matrix \mathbf{V} is build from the experimental uncertainties found in Table 2.1. For Run-II data, only ATLAS collaboration reported the correlation amongst different channels, and only correlations $> 10\%$ are considered. While for the HL-LHC, the whole correlation matrix found on the webpage [252]. The HL-LHC projections for the S2 scenario explained in [191] were used. These assume the improvement on the systematics that is expected to be attained by the end of the HL-LHC physics programme, and that theory uncertainties are improved by a factor of two with respect to current values. Theoretical uncertainties were not considered in this fit

The python package `pymc3` [253] was used to construct the posterior distribution. We use the `Arviz` Bayesian analysis package [254] to extract the credible intervals (CIs) from the highest density posterior intervals (HDPI) of the posterior distributions, where the intervals covering 95% (68%) of the posterior distribution are considered the 95% (68%) CIs. In the Gaussian limit, these 95% (68%) CIs should be interpreted as equivalent to the 95% (68%) Frequentist Confidence Level (CL) two-sided bounds. `HEPfit` [255] code was used to validate the fits. Given that current bounds on these operators are rather weak, one may wonder about the uncertainty in our fits associated to the truncation of the EFT. Note that, since the four-quark operators only enter into the virtual corrections at NLO, Higgs production and decay contain only linear terms in $1/\Lambda^2$ in the corresponding Wilson coefficients, i.e. the quadratic terms coming from squaring the amplitudes are technically of next-to-NLO. Hence, the quadratic effects in the signal strengths come from not linearising the corrections to the product $\sigma_{\text{Prod}} \times \text{BR}$. These

effects have been investigated, and found to have a negligible effect on the fit. The operators of single chirality \mathcal{O}_{tt} and $\mathcal{O}_{QQ}^{(1)/(3)}$ were not included in the fit, as their effect on Higgs rates is limited to small δR for $t\bar{t}h$. Thus, they cannot be contained simultaneously with C_ϕ using single Higgs data.

5.2.1 Fit results

In Figure 5.5 and Figure 5.6 the 68% and 95% highest posterior density contours of the two-parameter posterior distributions and their marginalisation for the two-parameter fits involving C_ϕ and one of the four-heavy quark Wilson coefficients, evaluated at the scale $\Lambda = 1$ TeV for Run-II LHC measurements . Both linearised and quadratically truncated δR_{λ_3} fits are shown, and we observe that the 95% CI bounds (shown on top of the panels) and correlations depends on the truncation.

We observe that the four-fermion operators are strongly correlated with Higgs self-coupling modifier \mathcal{O}_ϕ , in the linear fit. With Pearson's correlation of $\gtrsim 0.7$ with p -value $< 10^{-4}$. In the case of quadratic δR_{λ_3} fit, we observe diminished Pearson correlation, but in this scenario Pearson's correlation test is not particularly applicable, as we have non-linear relation between the variables.

The two-parameter fit results for the four-fermion Wilson coefficients are mesmerised in the forest plots in Figure 5.7 marginalising the posteriors distributions over C_ϕ . The finite effects were isolated by performing fits with δR^{fin} only. The finite effects are small for $\mathcal{O}_{QtQb}^{(1)/(8)}$ but dominant for the four-top operators $\mathcal{O}_{Qt}^{(1)/(8)}$ mainly coming from $t\bar{t}h$. The effect of EFT truncations of δR_{λ_3} can also be observed as shifts in the mean value for the Wilson coefficients, but the 95% CI's themselves are not significantly affected. In these plots, the fits results from this study are also confronted with the limits obtained from fits to top data [140, 143, 233, 234, 256, 257] and EWPO fits from [142]. Showing that when the Wilson coefficient running is taken into an account, the 95% CI bounds obtained from Higgs data are consistently stronger than the ones from top data.

In Figure 5.8 the fit results for C_ϕ after marginalising over the four-fermion Wilson coefficients in both EFT truncations schemes of δR_{λ_3} . In addition to a single parameter fit for C_ϕ . Additionally the current 95 % CL bound on C_ϕ extracted from Higgs pair production search using th final state $b\bar{b}\gamma\gamma$ performed by ATLAS using Run-II data [258], translated from κ formalism.

The mean values and the 95%CI's change depending on the four-fermion Wilson coefficient that was paired with C_ϕ in the two.-parameter fit. As expected, the single parameter fits for C_ϕ yield stronger bound on C_ϕ than the two-parameter fits, thus the inclusion of the four-fermion operators in single Higgs data dilutes C_ϕ bounds . Additionally, the truncation order of δR_{λ_3} appears to have a significant effect on the length of the CI's, with quadratic fits giving more stringent constraint on C_ϕ . Instead, for Higgs pair production makes only a negligible effect if linear or up to quadratic terms in the EFT expansion are kept for the $C_\phi > 0$ bound, while the bound weakens at linear order in $1/\Lambda^2$ for $C_\phi < 0$ [259]. For instance, the quadratic single parameter fit for C_ϕ is comparable to the direct bound from Higgs pair production. However, this changes

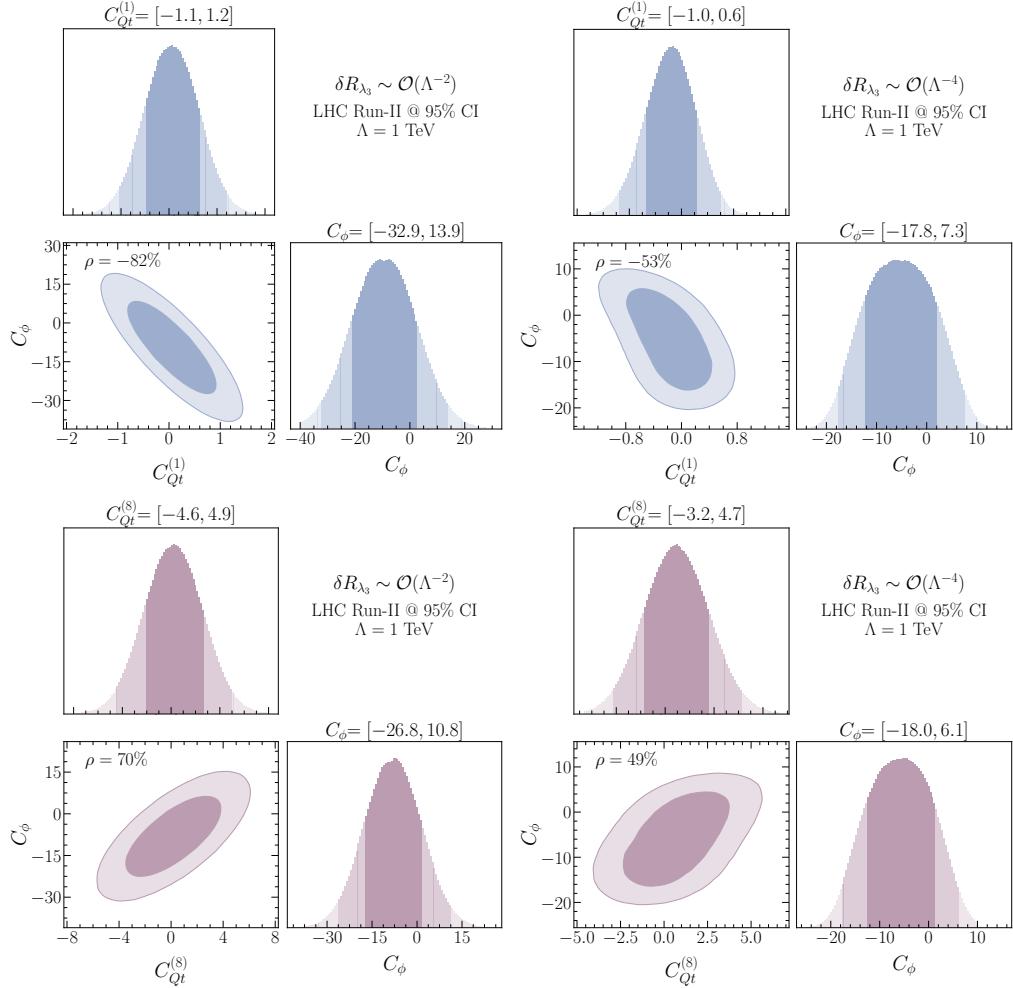


Figure 5.5. The posterior distributions of the Run-II data fits for C_ϕ with $C_{Qt}^{(1)}$ (up) and C_ϕ with $C_{Qt}^{(8)}$ (down). With 68% and 95% highest density posterior contours indicated. The limits shown on top of the plots indicate the 95% CI's. Plots on the left are made for the fully linearised δR_{λ_3} , while the ones on the right include the quadratic effects. This figure has been published in [236].

dramatically, when one includes the four-fermion operators in a combined fit, and the single Higgs data constraints on C_ϕ become less significant compared to the direct hh bounds.

It should be noted that the strongest bound on the Higgs self-coupling currently comes from the perturbative unitarity bound of ref. [52], as discussed in chapter.

One of the important aspects of multivariate studies is the correlation among variables. Apart from the two-parameter fits discussed above, here we also consider a four-parameter fit to C_ϕ plus the three directions in the four heavy-quark operator parameter

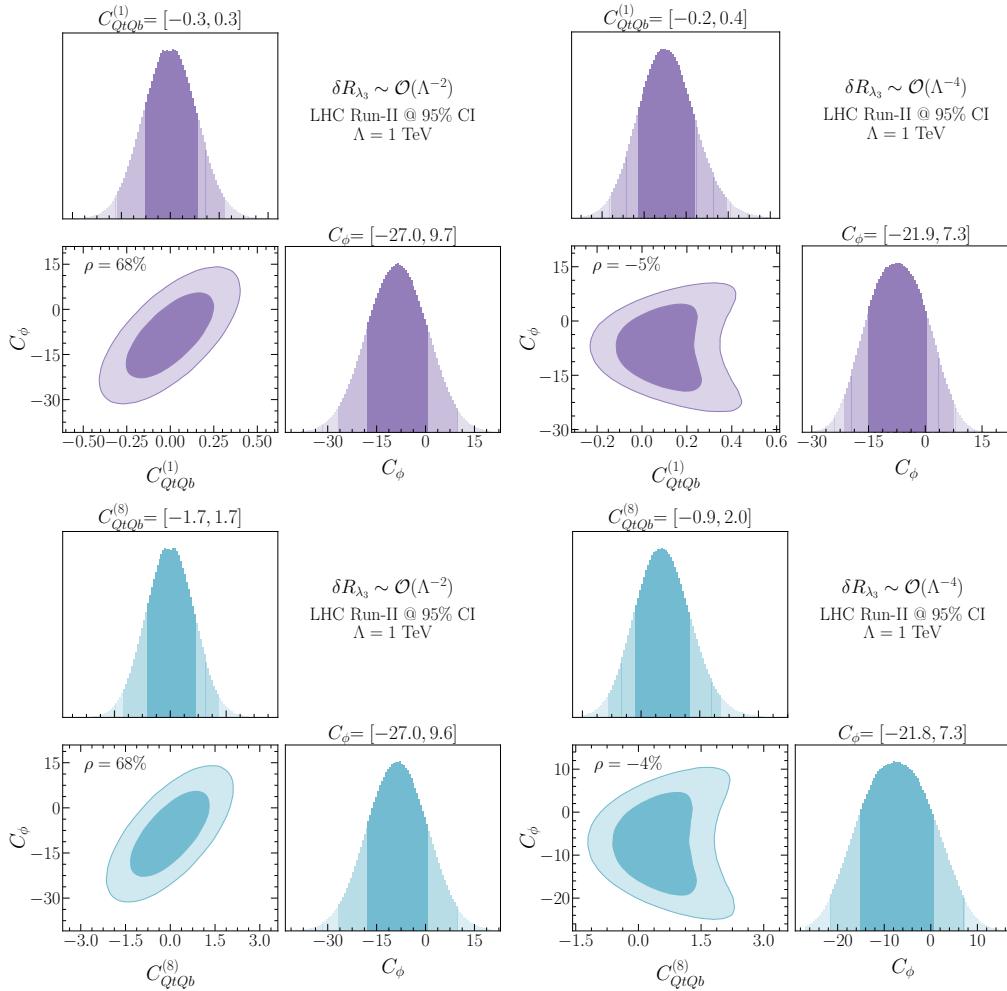


Figure 5.6. The posterior distributions of the Run-II data fits for C_ϕ with $C_{QtQb}^{(1)}$ (up) and C_ϕ with $C_{QtQb}^{(8)}$ (down). With the same annotations as in Figure 5.5. This figure has been published in [236].

space that the Higgs rates are mostly sensitive too, i.e. neglecting $C_{QQ}^{(1),(3)}$ and C_{tt} , and trading $C_{QtQb}^{(1)}$ and $C_{QtQb}^{(8)}$ by C_{QtQb}^+ . When considering two- or four-parameter fits of C_ϕ and the four-heavy-quark Wilson coefficients, we observe a non-trivial correlation patterns amongst these coefficients. Figure 5.9 illustrates these correlation patterns clearly for the four-parameter fit. We observe that the Wilson coefficients $C_{Qt}^{(1),(8)}$ are strongly correlated because, in analogy to $C_{QtQb}^{(1),(8)}$, they only appear in certain linear combination whenever correcting the Yukawa coupling. However, unlike $C_{QtQb}^{(1),(8)}$ they are not completely degenerate because the main part of the NLO correction to $t\bar{t}h$ does not

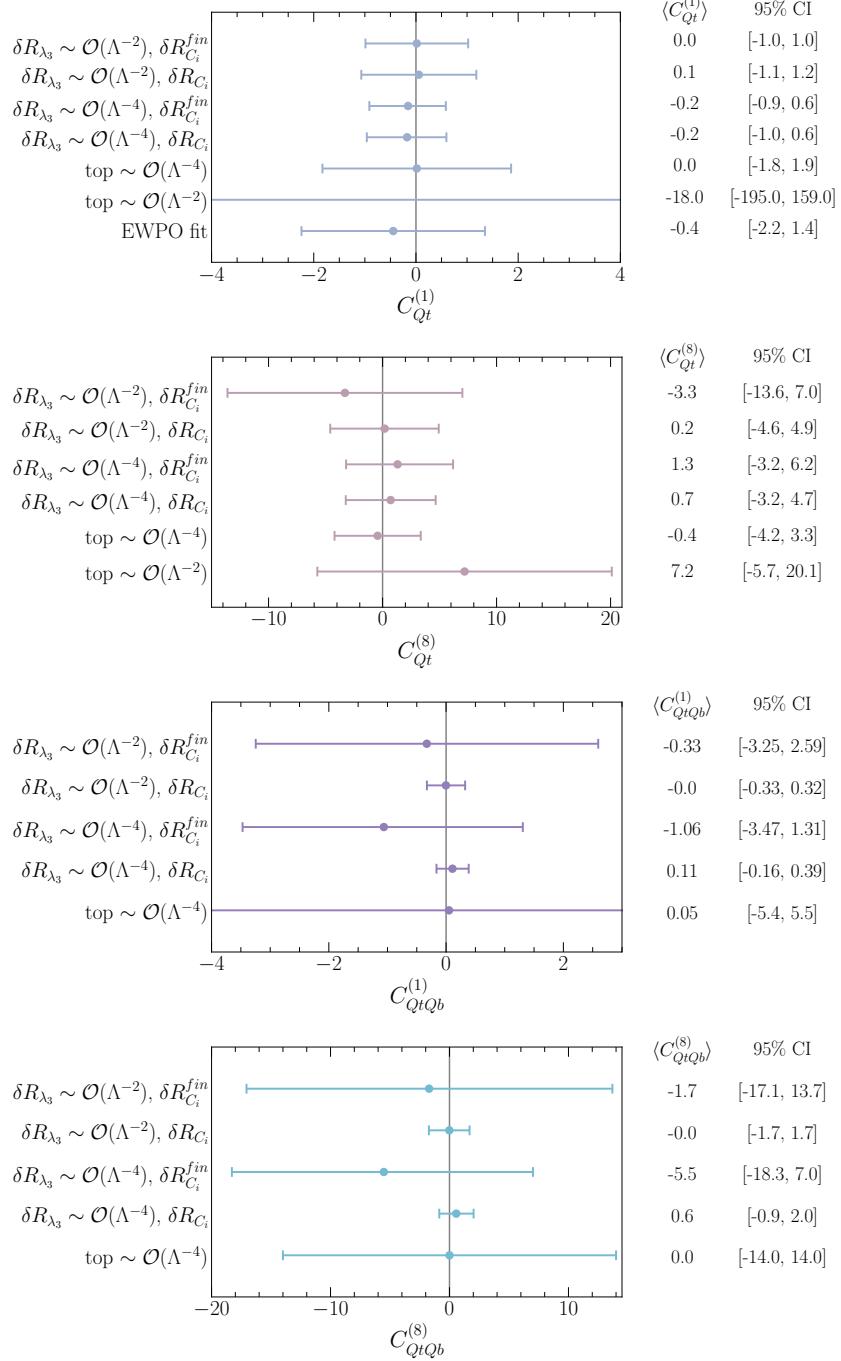


Figure 5.7. Forest plots illustrating the means and 95% CI's constraints on the four-heavy-quark Wilson coefficients C_i from Run-II data. These bounds are obtained from two-parameter fits including the aforementioned coefficients along with C_ϕ , then marginalising over the latter. The different fits with only the finite part of the NLO correction included VS the full results, as well as the EFT truncation scheme for the trilinear coupling, linear vs quadratic. Fits from top data [140] for $C_{Qt}^{(1),(8)}$ and [234] for $C_{QtQb}^{(1),(8)}$ as well as EWPO fits from [142] were included for comparison. This figure has been published in [236].

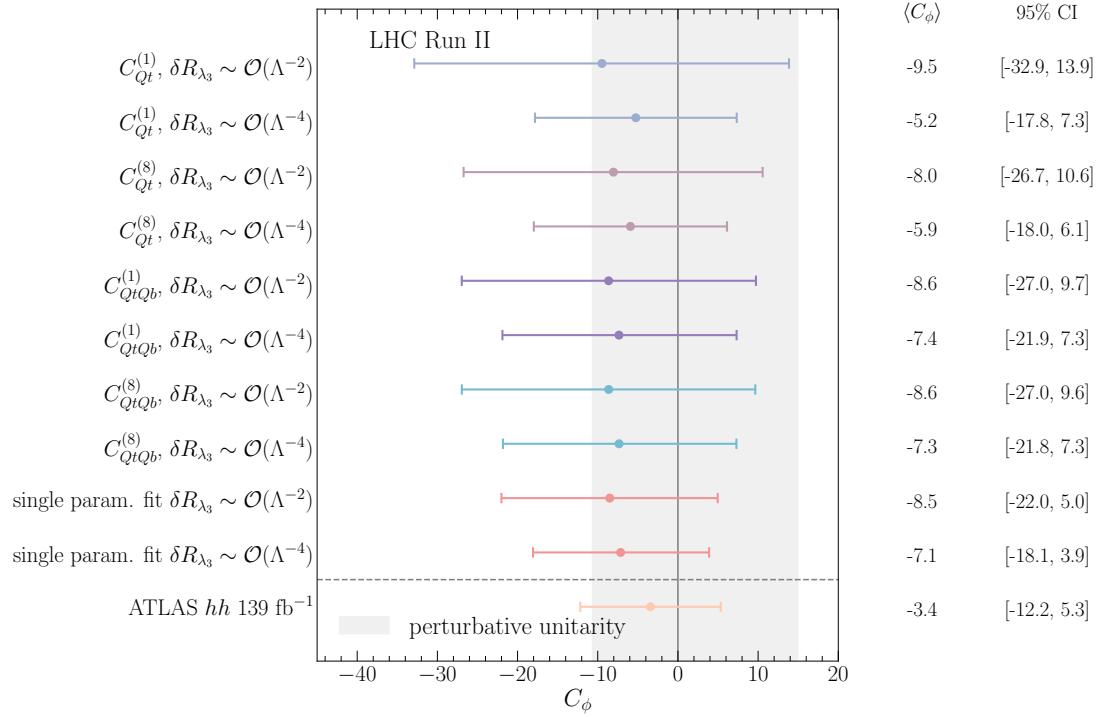


Figure 5.8. A forest plot illustrating the means and 95% CI's bounds for C_ϕ from the two-parameter fit with the four-fermion operators marginalised. The fits results for C_ϕ from full run-II Higgs data keeping terms up to $\mathcal{O}(1/\Lambda^2)$ or $\mathcal{O}(1/\Lambda^4)$ in δR_{λ_3} are shown. For comparison, also the 95% CI and means for the single parameter fit for C_ϕ with the same single Higgs data is shown as well as the bounds on C_ϕ from the 139 fb^{-1} search for Higgs pair production [258]. The horizontal grey band illustrates the perturbative unitarity bound [52]. This figure has been published in [236].

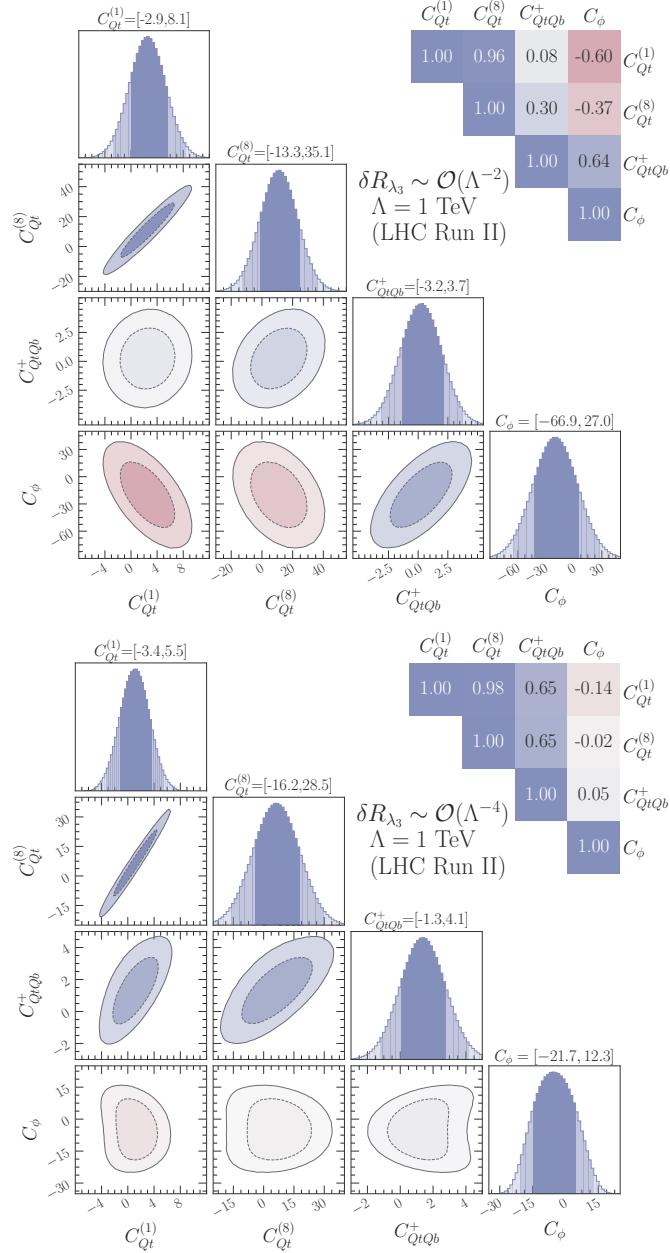


Figure 5.9. The marginalised 68% and 95% Highest density posterior contours for the four-parameter fits including the different four-quark Wilson coefficients and C_ϕ . The numbers above the plots show the 95% CI bounds while the correlations are given on the top-right side. The correlation between each pair of the Wilson coefficients is highlighted as a heatmap. The upper panel shows the fit including up to $\mathcal{O}(1/\Lambda^2)$ in δR_{λ_3} while the lower one shows the fit with including also $\mathcal{O}(1/\Lambda^4)$. This figure has been published in [236].

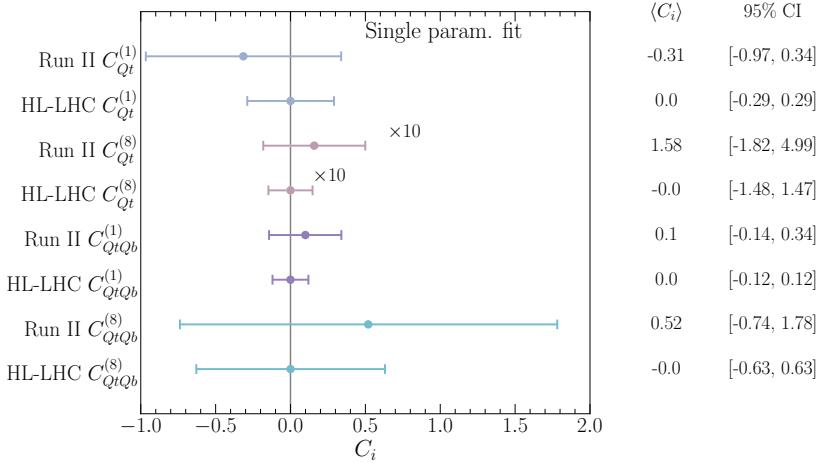


Figure 5.10. Results of a single parameter fit showing the improvement in constraining power of the HL-LHC over the current bounds from Run-2 data. This figure has been published in [236].

contain the aforementioned linear combination. The four-parameter fit also reveals that the Wilson coefficients $C_{Qt}^{(1),(8)}$ have a large correlation with C_{QtQb}^+ because all of the four Wilson coefficients appear in a linear combination in the NLO corrections except for $h \rightarrow b\bar{b}$ and $t\bar{t}h$. However, this correlation is not as strong due to the large NLO correction of the Higgs decay $h \rightarrow b\bar{b}$ from $C_{QtQb}^{(1),(8)}$. Moreover, the correlation between the four-heavy-quark Wilson coefficients and C_ϕ depends on the δR_{λ_3} truncation.

5.2.2 Prospects for HL-LHC

Using the CMS Higgs signal strength measurement projections for the HL-LHC in refs. [91, 252] for a centre-of-mass energy of $\sqrt{s} = 14$ TeV and integrated luminosity of 3 ab^{-1} , it is possible to repeat the fits done for Run-II. The projections for the S2 scenario explained in [191] were used. These assume the improvement on the systematics that is expected to be attained by the end of the HL-LHC physics programme, and that theory uncertainties are improved by a factor of two with respect to current values. These projections are assumed to have their central values in the SM prediction with the total uncertainties summarised in table 2.1 in Appendix ??.

In Figure 5.10 I show the comparison between the fit results of Run-II data and the projections for the HL-LHC for single parameter fits. For the operators $\mathcal{O}_{Qt}^{(1),(8)}$ the constraining power of the HL-LHC is roughly a factor two better as the current bounds we could set from single Higgs data, while for the operators $\mathcal{O}_{QtQb}^{(1),(8)}$ the improvement is a little less. While in Figure 5.11 the limits on C_ϕ in a single parameter fit for Run-2 and the projections for the HL-LHC are shown. including in δR_{λ_3} up to order $\mathcal{O}(1/\Lambda^2)$ or $\mathcal{O}(1/\Lambda^4)$. While for Run-II data the inclusion of $\mathcal{O}(1/\Lambda^4)$ made a significant difference, this is less pronounced for the HL-LHC projections. These results are very similar to

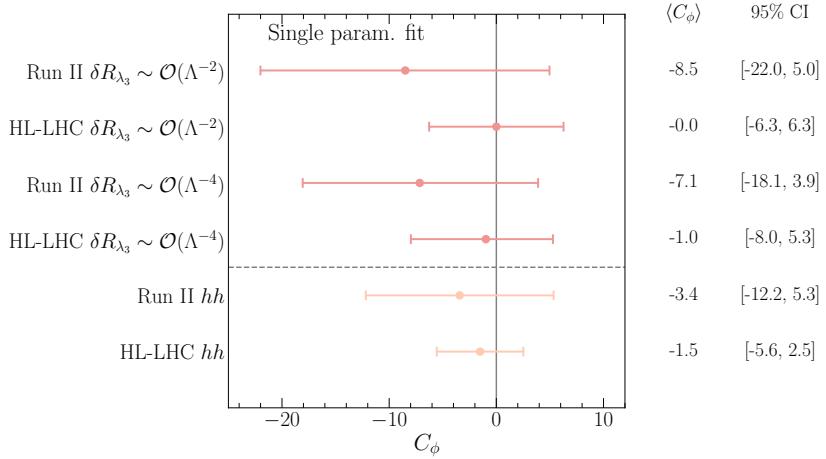


Figure 5.11. A forest plot illustrating the means and 95% CI's of the posteriors built from the C_ϕ in a single-parameter fit, showing also the differences in including terms of $\mathcal{O}(1/\Lambda^2)$ or up to $\mathcal{O}(1/\Lambda^4)$ in the definition of δR_{λ_3} . For comparison, also the limits and projections from searches for Higgs pair production are shown. This figure has been published in [236].

the projections presented in a κ_λ fit in [260]. The results were also confronted with data from searches for Higgs pair production 139 fb^{-1} [258] and HL-LHC projections [261] on Higgs pair production, showing that Higgs pair production will still allow to set stronger limits on C_ϕ .

5.3 Conclusion

In this chapter, the calculations of the NLO corrections depending on four-heavy-quark operators to single Higgs rates have been calculated. We have seen that operators both homogenous and heterogeneous chirality structures contribute to Higgs rates at NLO. Though, the operators with heterogeneous chirality structure have more sizeable effects as they would contribute to $hf\bar{f}$ vertex renormalisation in SMEFT and therefore appear in more channels compared to the operators baring homogenous chirality structure. Using the calculation results, fits using Higgs data have been performed. The operators with the same chirality structure will not be constrained strongly by the Higgs data, and hence their results were not included. This applies to the operators that contribute only via beauty quarks loops, like $\mathcal{O}_{Qb}^{(1),(8)}$.

Two processes stood out in this calculation in terms of their sensitivity to these operators. The decay of the Higgs to beauty quarks, which had strong sensitivity to $\mathcal{O}_{QtQb}^{(1),(8)}$, Moreover, the associated production of the Higgs with top pair $t\bar{t}h$, which had large finite corrections coming from $\mathcal{O}_{Qt}^{(1),(8)}$. These corrections were depending on the colour factor and thus broke the degeneracy between the singlet and octet operators.

Using these calculations combined Higgs measurements using complete Run-II data as

well as HL-LHC projections, fits for constraining these operators have been preformed. These fits also included the SMEFT operator modifying the Higgs self-coupling C_ϕ which is weakly constrained, and only appears at NLO in single Higgs rates; like the group of four-heavy-quark operators considered. One can observe from the fits, that the constraints on C_ϕ from single Higgs data will become significantly diluted compared to the fits preformed with this operator alone, or even with ones that enter at LO [113–116, 118]. This is due to the strong correlation patters amongst C_ϕ and the four-fermion operators in question. On the contrary, The fits yielded overall stronger bounds on the four-heavy-quark operators than the ones obtained from top data [140, 234]. Comparable bounds can be also seen when EWPO data is considered [142], which these operators also enter at NLO in these observables. Additionally, the authors of ref. [262] have shown that these operators could also be constrained from flavour observables involving $\Delta F = 2$, in particular $B_s - \bar{B}_s$ mixing. Although these bounds depend on the flavour ansatz of the New Physics, and not completely model independent.

The results of these calculations and consequent fits further emphasize the interconnectivity of SMEFT operators and experimental observables, which was discussed in chapter 3. Then remains the question: *How this interconnectivity would manifest in a NP model?* Particularly, one might wonder if the strong correlation between these four-fermion operators and \mathcal{O}_ϕ could appear in a UV complete model. In fact, large effective couplings involving four top quarks are expected in many NP models, for example partial compositeness [271]. These models would also generate sizeable modifications to the Higgs self-interaction. Similar effects could be obtained from models containing new scalars such as an additional Higgs doublet $\varphi \sim (1, 2)_{\frac{1}{2}}$, or other scalars with non-singlet representation under $SU(3)_c$ like $(6, 1)_{\frac{1}{3}}$ and $(8, 2)_{\frac{1}{2}}$. For further details on these models and their matching see [272]. In addition, for NLO matching to SMEFT see [273].

6 Virtual two-loop calculation of Zh production via gluon fusion

As we have seen in section 2.3, Higgs couplings to the weak vector bosons, i.e. Z and W is approaching the precision level. For their measurements both VBF and Vh channels are used, the associated Higgs production with the vector bosons are not only important for measuring the VVh coupling but also other couplings and properties as discussed in subsection 4.1.3. The most notable example emphasising the importance of this channel is the measurement of the Higgs decaying to beauty quarks $h \rightarrow b\bar{b}$ by both ATLAS and CMS [274, 275]. Hence, the Vh Higgs production is an important channel to look for in the future runs of the LHC. As the statistical and systematic uncertainties coming from the experimental setup of the LHC will be eventually reduced in the future runs, due to higher integrated luminosity, upgraded detectors and improved analysis techniques. There is an exigency to reduce theoretical uncertainties emerging from the perturbative calculations of cross-sections. In order to accomplish that, one should include higher order terms to the theoretical prediction. Since Wh production has no gluon fusion channel, and the main source of Zh uncertainties actually come from its gluon fusion part. Higher order correction to the $gg \rightarrow Zh$ is the key to improve the theoretical modelling for Vh .

It should be noted that the Zh channel can receive contributions from new particles [276], particularly at the large invariant-mass region where the gluon fusion contribution becomes more important, and HTL approximation would typically fail. Therefore, better understanding of the SM prediction of the Zh gluon fusion channel is crucial for both the SM precision measurements of Higgs production within the SM and for testing NP in this channel, e.g. new vector-like leptons.

This chapter aims to demonstrate the use of p_T -expansion technique, developed in [203] as an approach to compute the two-loop virtual corrections to $gg \rightarrow Zh$ analytically, including top mass effects. This method also allows for the use of Padé approximants, in order to extend the range of validity of this calculation.cite the paper once it is out

This chapter is structured as follows : In section 6.1 contains the general notation we have used for the gluon fusion Zh process calculation. Then, in subsection 6.1.1 the transverse momentum expansion method is discussed. Calculation of the LO form-factors in the transverse momentum expansion is illustrated in section 6.2 as a proof of concept for the p_T -expansion technique. Outline of the two-loop calculation is discussed in section 6.3. Finally, in section 6.4, the results of our calculation are shown with concluding remarks at the end. This chapter is based on the work my collaborators and I have published in [204].

6.1 General notation

The amplitude $g_a^\mu(p_1)g_b^\nu(p_2) \rightarrow Z^\rho(p_3)h(p_4)$ can be written as

$$\mathcal{A} = i\sqrt{2}\frac{m_Z G_F \frac{\alpha_s^0}{4\pi}(\mu_R)}{\pi} \delta_{ab} \epsilon_\mu^a(p_1) \epsilon_\nu^b(p_2) \epsilon_\rho(p_3) \hat{\mathcal{A}}^{\mu\nu\rho}(p_1, p_2, p_3), \quad (6.1)$$

$$\hat{\mathcal{A}}^{\mu\nu\rho}(p_1, p_2, p_3) = \sum_{i=1}^6 \mathcal{P}_i^{\mu\nu\rho}(p_1, p_2, p_3) \mathcal{A}_i(\hat{s}, \hat{t}, \hat{u}, m_t, m_h, m_Z), \quad (6.2)$$

where μ_R is the renormalisation scale and $\epsilon_\mu^a(p_1) \epsilon_\nu^b(p_2) \epsilon_\rho(p_3)$ are the polarization vectors of the gluons and the Z boson, respectively. It is possible to decompose the amplitude into a maximum of 6 Lorentz structures encapsulated by the tensors $\mathcal{P}_i^{\mu\nu\rho}$. Due to the presence of the γ_5 these projectors are proportional to the Levi-Civita total anti-symmetric tensor $\epsilon^{\alpha\beta\gamma\delta}$. One can choose to an orthogonal basis explicitly shown in ??, such that

$$\mathcal{P}_i^{\mu\nu\rho} \mathcal{P}_{j\mu\nu\rho} = 0, \quad \text{for } i \neq j \quad (6.3)$$

By this choice one obtains unique form factors corresponding to each projector

$$\mathcal{A}_i(\hat{s}, \hat{t}, \hat{u}, m_t, m_h, m_Z), \quad (6.4)$$

that are multivariate complex functions of the top (m_t), Higgs (m_h) and Z (m_Z) bosons masses, and of the partonic Mandelstam variables

$$\hat{s} = (p_1 + p_2)^2, \quad \hat{t} = (p_1 + p_3)^2, \quad \hat{u} = (p_2 + p_3)^2, \quad (6.5)$$

where $\hat{s} + \hat{t} + \hat{u} = m_Z^2 + m_h^2$ and all the momenta are considered to be incoming. The form-factors \mathcal{A}_i can be perturbatively expanded in orders of α_s ,

$$\mathcal{A}_i = \sum_{k=0} \left(\frac{\alpha_s}{\pi} \right)^k \mathcal{A}_i^{(k)} \quad (6.6)$$

Where $\mathcal{A}_i^{(0)}$ and $\mathcal{A}_i^{(1)}$ are the LO and NLO terms, respectively. Using Fermi's Golden Rule, we can write the Born partonic cross-section as

$$\hat{\sigma}^{(0)}(\hat{s}) = \frac{m_Z^2 G_F^2 \alpha_s(\mu_R)^2}{64\hat{s}^2(2\pi)^3} \int_{\hat{t}-}^{\hat{t}+} d\hat{t} \sum_i |\mathcal{A}_i^{(0)}|^2, \quad (6.7)$$

where $\hat{t}^\pm = [-\hat{s} + m_h^2 + m_Z^2 \pm \sqrt{(\hat{s} - m_h^2 - m_Z^2)^2 - 4m_h^2 m_Z^2}] / 2$.

The LO has two sets of diagrams, the triangle, and box diagrams shown in Figure 6.1. In (a), the triangle diagrams contain a neutral Goldstone boson G^0 , instead in (b) the Z boson is mediated. The interplay between these two diagram types depends on the ξ gauge. Moreover, the Z boson is strictly off-shell, due to Furry's theorem. In the Landau gauge the Z -mediated diagrams will also vanish, this can be seen by considering the

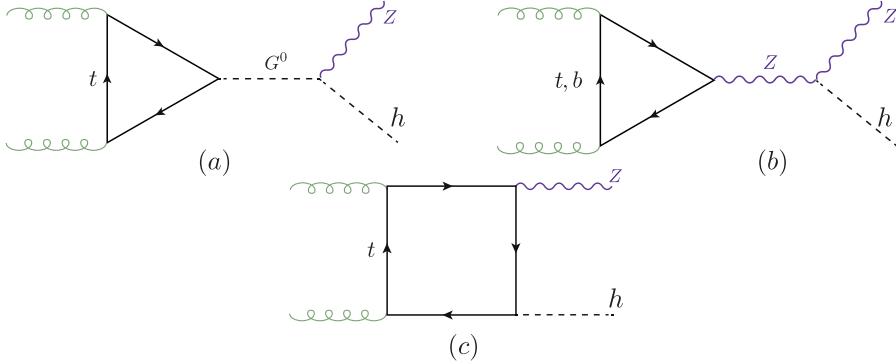


Figure 6.1. Feynman diagrams type for the LO $gg \rightarrow Z h$ process. The triangle diagrams in a general ξ gauge involve Z and the neutral Goldstone G^0 propagators.

subamplitude ggZ^* which in the Landau gauge can be related to the decay of a massive vector boson with mass $\sqrt{\hat{s}}$ into two massless ones, a process that is forbidden by the Landau-Yang theorem [277, 278]. The triangle diagrams are also proportional to the mass difference between the up and down type quarks. In this calculation, the first and second generation quarks are assumed to be massless, as well as the b quark, hence light quarks loops do not contribute to this process. The same would apply to the box diagrams (c), as they are proportional to the quark Yukawa coupling, and vanish in the massless quarks case. Moreover, triangle diagrams with $b-$ quark loops contribute to $\sim 1\%$ of the total amplitude, computed in the limit $m_b \rightarrow 0$.

6.1.1 The transverse momentum expansion

Choosing to expand in small p_T of the Z boson, the first step is expressing p_T in terms of the Mandelstam variables and masses

$$p_T^2 = \frac{\hat{t}\hat{u} - m_Z^2 m_h^2}{\hat{s}}. \quad (6.8)$$

From eq.(6.8), together with the relation between the Mandelstam variables, one finds

$$p_T^2 + \frac{m_h^2 + m_Z^2}{2} \leq \frac{\hat{s}}{4} + \frac{\Delta_m^2}{\hat{s}}, \quad (6.9)$$

where $\Delta_m = (m_h^2 - m_Z^2)/2$. Eq.(6.9) implies $p_T^2/\hat{s} < 1$ that, together with the kinematical constraints $m_h^2/\hat{s} < 1$ and $m_Z^2/\hat{s} < 1$. With these relations in mind, one can expand the amplitudes in terms of small p_T^2/\hat{s} , m_h^2/\hat{s} and m_Z^2/\hat{s} , which is technically valid throughout the whole phase space, contrary to the LME and HE limits. The caveat for this expansion is that, the amplitude does not depend on p_T explicitly. Instead, one would expand in

the reduced Mandelstam variables $t'/s' \ll 1$ or $u'/s' \ll 1$, defined as

$$s' = p_1 \cdot p_2 = \frac{\hat{s}}{2}, \quad t' = p_1 \cdot p_3 = \frac{\hat{t} - m_Z^2}{2}, \quad u' = p_2 \cdot p_3 = \frac{\hat{u} - m_Z^2}{2} \quad (6.10)$$

and satisfy

$$s' + t' + u' = \Delta_m. \quad (6.11)$$

The choice of the expansion parameter t' or u' depends whether one expands in the forward or backwards kinematics. Because the process $gg \rightarrow Zh$, has two particles in the final states with different masses, the amplitude is not symmetric under the their exchange. One therefore cannot compute the cross-section by integrating only the forward-expanded amplitude [204], contrary what has been done for the Higgs pair [203]. In order to overcome this issue, one could further examine the projectors in ?? and observe that they can be split into symmetric and anti-symmetric parts with respect to the exchange $t' \leftrightarrow u'$. Then, expand the symmetric part in the forward kinematics, like the Higgs pair case. As for the anti-symmetric part, the antisymmetric factor is simply extracted by multiplying the form-factors by $1/(\hat{t} - \hat{u})$, written as $1/(2s' - 4t' - 2\Delta_m)$, then perform the expansion in the forward kinematics and finally multiply back by $(\hat{t} - \hat{u})$.

In order to implement the p_T -expansion at the Feynman diagrams level we start by splitting the momenta into longitudinal and transverse with respect to the beam direction, by introducing the vector [203],

$$r^\mu = p_1^\mu + p_3^\mu, \quad (6.12)$$

which satisfies

$$r^2 = \hat{t}, \quad r \cdot p_1 = \frac{\hat{t} - m_Z^2}{2}, \quad r \cdot p_2 = -\frac{\hat{t} - m_h^2}{2}, \quad (6.13)$$

and hence can be also written as

$$r^\mu = -\frac{\hat{t} - m_h^2}{\hat{s}} p_1^\mu + \frac{\hat{t} - m_Z^2}{\hat{s}} p_2^\mu + r_\perp^\mu = \frac{t'}{s'} (p_2^\mu - p_1^\mu) - \frac{\Delta_m}{s'} p_1^\mu + r_\perp^\mu, \quad (6.14)$$

where

$$r_\perp^2 = -p_T^2. \quad (6.15)$$

substituting the definition of p_T from eq.(6.8) one obtains

$$t' = -\frac{s'}{2} \left\{ 1 - \frac{\Delta_m}{s'} \pm \sqrt{\left(1 - \frac{\Delta_m}{s'}\right)^2 - 2\frac{p_T^2 + m_Z^2}{s'}} \right\} \quad (6.16)$$

implying that the expansion in small p_T (the minus sign case in eq.(6.16)) can be realized at the level of Feynman diagrams, by expanding the propagators in terms of the vector r^μ around $r^\mu \sim 0$ or, equivalently, $p_3^\mu \sim -p_1^\mu$, see eq.(6.14).

6.2 Born cross-section in the p_T -expansion

As a baseline test for the validity and convergence behaviour of the p_T expansion we start by computing the LO amplitude, and consequently the Born partonic cross-section in the p_T expansion then compare it with the exact results found in [194, 195].

Starting by defining the one-loop functions appearing in the similar calculation of the Born cross-section for $gg \rightarrow hh$ in the same expansion carried out in ref. [203]

$$B_0[\hat{s}, m_t^2, m_t^2] \equiv B_0^+, \quad B_0[-\hat{s}, m_t^2, m_t^2] \equiv B_0^-, \quad (6.17)$$

$$C_0[0, 0, \hat{s}, m_t^2, m_t^2, m_t^2] \equiv C_0^+, \quad C_0[0, 0, -\hat{s}, m_t^2, m_t^2, m_t^2] \equiv C_0^- \quad (6.18)$$

$$B_0[q^2, m_1^2, m_2^2] = \frac{1}{i\pi^2} \int \frac{d^n k}{\mu^{n-4}} \frac{1}{(k^2 - m_1^2)((k+q)^2 - m_2^2)}, \quad (6.19)$$

$$C_0[q_a^2, q_b^2, (q_a + q_b)^2, m_1^2, m_2^2, m_3^2] = \frac{1}{i\pi^2} \int \frac{d^d k}{\mu^{d-4}} \frac{1}{[k^2 - m_1^2][(k+q_a)^2 - m_2^2][(k-q_b)^2 - m_3^2]} \quad (6.20)$$

are the Passarino-Veltman functions [279], with d the dimension of spacetime and μ the 't Hooft mass. There are only two non-vanishing form-factors at LO, one is symmetric \mathcal{A}_2 , and the other is antisymmetric \mathcal{A}_6 , in the p_T -expansion, these form-factors are give by,

up to order $\mathcal{O}(p_T^2)$

$$\begin{aligned}
\mathcal{A}_2^{(0,\Delta)} &= -\frac{p_T}{\sqrt{2}(m_Z^2 + p_T^2)}(\hat{s} - \Delta_m)m_t^2 C_0^+, \\
\mathcal{A}_2^{(0,\square)} &= \frac{p_T}{\sqrt{2}(m_Z^2 + p_T^2)} \left\{ \right. \\
&\quad \left(m_t^2 - m_Z^2 \frac{\hat{s} - 6m_t^2}{4\hat{s}} - p_T^2 \frac{12m_t^4 - 16m_t^2\hat{s} + \hat{s}^2}{12\hat{s}^2} \right) B_0^+ \\
&- \left(m_t^2 - \Delta_m \frac{m_t^2}{(4m_t^2 + \hat{s})} + m_Z^2 \frac{24m_t^4 - 6m_t^2\hat{s} - \hat{s}^2}{4\hat{s}(4m_t^2 + \hat{s})} - \right. \\
&\quad \left. p_T^2 \frac{48m_t^6 - 68m_t^4\hat{s} - 4m_t^2\hat{s}^2 + \hat{s}^3}{12\hat{s}^2(4m_t^2 + \hat{s})} \right) B_0^- \\
&+ \left(2m_t^2 - \Delta_m + m_Z^2 \frac{3m_t^2 - \hat{s}}{\hat{s}} + p_T^2 \frac{3m_t^2\hat{s} - 2m_t^4}{\hat{s}^2} \right) m_t^2 C_0^- \\
&+ \left(\hat{s} - 2m_t^2 + m_Z^2 \frac{\hat{s} - 3m_t^2}{\hat{s}} + p_T^2 \frac{2m_t^4 - 3m_t^2\hat{s} + \hat{s}^2}{\hat{s}^2} \right) m_t^2 C_0^+ \\
&+ \log \left(\frac{m_t^2}{\mu^2} \right) \frac{m_t^2}{(4m_t^2 + \hat{s})} \left(\Delta_m + 2m_Z^2 + p_T^2 \frac{2\hat{s} - 2m_t^2}{3\hat{s}} \right) \\
&- \left. \Delta_m \frac{2m_t^2}{(4m_t^2 + \hat{s})} + m_Z^2 \frac{\hat{s} - 12m_t^2}{4(4m_t^2 + \hat{s})} + p_T^2 \frac{8m_t^4 - 2m_t^2\hat{s} + \hat{s}^2}{4\hat{s}(4m_t^2 + \hat{s})} \right\},
\end{aligned} \tag{6.22}$$

and

$$\mathcal{A}_6^{(0,\Delta)} = 0, \tag{6.23}$$

$$\begin{aligned}
\mathcal{A}_6^{(0,\square)} &= \frac{\hat{t} - \hat{u}}{\hat{s}^2} p_T \left[\frac{m_t^2}{2} \left(B_0^- - B_0^+ \right) - \frac{\hat{s}}{4} \right. \\
&- \left. \frac{2m_t^2 + \hat{s}}{2} m_t^2 C_0^- + \frac{2m_t^2 - \hat{s}}{2} m_t^2 C_0^+ \right],
\end{aligned} \tag{6.24}$$

where these form-factors were divided into triangle (Δ) and box (\square) contributions, and B_0 functions are understood as the finite part of the integrals on the right hand side of eq.(6.19).

Using several truncations of the p_T -expansion, and comparing it to the exact LO result, one can see in Figure 6.2 the exact Born partonic LO cross section (red line) as a function of the invariant mass of the Zj system, M_{Zh} , in comparison to the p_T -expansions. For the numerical evaluation of the cross section here and in the following, we used as SM

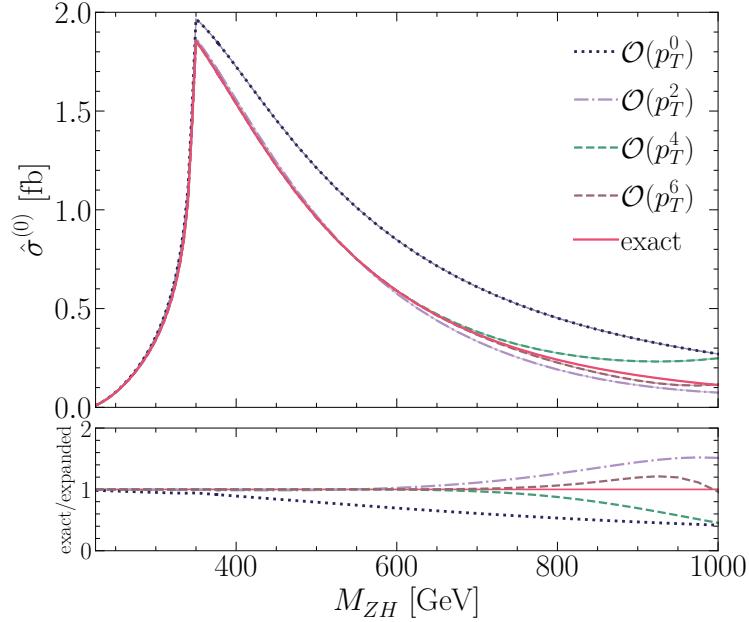


Figure 6.2. The Born partonic cross-section as a function of the invariant mass M_{Zh} . The exact (red line) is plotted together with results at different orders in the p_T -expansion (dashed lines). In the bottom part, the ratio of the full result over the p_T -expanded one at various orders is shown. This plot has been already published in [204]

input parameters

$$\begin{aligned} m_Z &= 91.1876 \text{ GeV}, & m_h &= 125.1 \text{ GeV}, & m_t &= 173.21 \text{ GeV}, \\ m_b &= 0 \text{ GeV}, & G_F &= 1.16637 \text{ GeV}^{-2}, & \alpha_s(m_Z) &= 0.118. \end{aligned}$$

From the ratio plotted in the lower panel of Figure 6.2, we observe that the $\mathcal{O}(p_T^0)$ expansion is in good agreement with the exact result when $M_{Zh} \lesssim 2m_t$. Inclusion of higher order terms up to $\mathcal{O}(p_T^6)$ extended the validity of the expansion to reach $M_{Zh} \lesssim 750$ GeV. This is the similar behaviour seen in [203] for Higgs pair. Therefore, one would expect the p_T -expanded two-loop virtual correction to be an accurate approximation with the exact (numerical) result for the region of the invariant mass of $M_{Zh} \sim 700 - 750$ GeV. Similar conclusions can be seen more explicitly in Table 6.1, where it is shown that the partonic cross-section at $\mathcal{O}(p_T^4)$ agrees with the full result for $M_{ZH} \lesssim 600$ GeV on the permille level and the agreement further improves when $\mathcal{O}(p_T^6)$ terms are included.

M_{Zh} [GeV]	$\mathcal{O}(p_T^0)$	$\mathcal{O}(p_T^2)$	$\mathcal{O}(p_T^4)$	$\mathcal{O}(p_T^6)$	full
300	0.3547	0.3393	0.3373	0.3371	0.3371
350	1.9385	1.8413	1.8292	1.8279	1.8278
400	1.6990	1.5347	1.5161	1.5143	1.5142
600	0.8328	0.5653	0.5804	0.5792	0.5794
750	0.5129	0.2482	0.3129	0.2841	0.2919

Table 6.1. The partonic cross section $\hat{\sigma}^{(0)}$ at various orders in p_T and the full computation for several values of M_{Zh} . This table has been already published in [204].

6.3 NLO calculation

The virtual two-loop corrections to $gg \rightarrow Zh$ are shown in Figure 6.3, which involve corrections to the triangle topology in (a) and (b). The corrections to the box topology in (c) and a new topology , dented by double triangle in (d). Both two-loop corrections to the triangles, and the double triangle diagrams can be computed exactly analytically. However, the two-loop box diagrams contain master-integrals (MI's) that have no analytic solutions, so far. The two-loop box diagrams will be computed in the p_T -expansion.

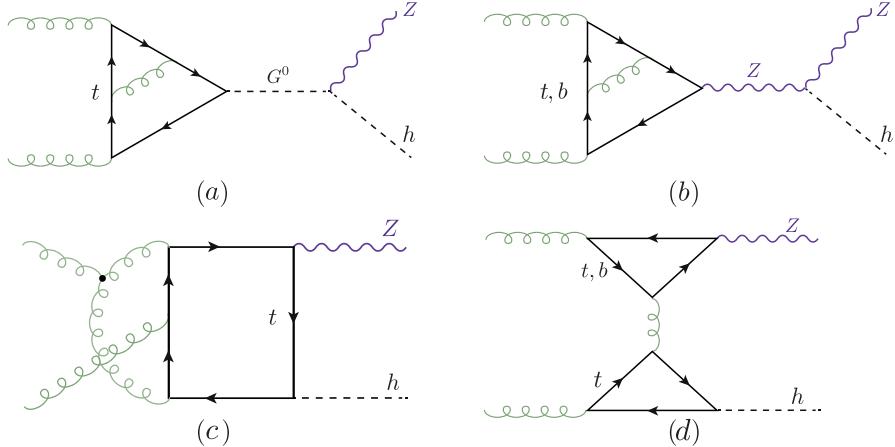


Figure 6.3. Feynman diagrams types for the virtual NLO corrections to the $gg \rightarrow Zh$ process.

6.3.1 Renormalisation

The two-loop corrections to the triangle and box diagrams contain both UV and IR divergences. The first emerges from UV divergent sub-diagrams, such as top mass renormalisation and QCD vertex correction. While the IR divergences come from massless

loops. In order to remove these divergences, one introduces adequate counter-terms. On the other hand, the double triangle is both UV and IR finite.

We start by the gluon wavefunction renormalisation of the incoming gluons (external legs) such that the amplitude is renormalised by $Z_A^{1/2}$ for each gluon.

$$Z_A = 1 + \frac{\alpha_s^0}{4\pi} \frac{2}{3\epsilon} \left(\frac{\mu_R^2}{m_t^2} \right)^\epsilon. \quad (6.25)$$

The on-shell scheme for the top mass renormalisation has been used, in which the bare mass is replaced by the renormalised one $m_0 = Z_m m$ in the propagators this gives the $\overline{\text{MS}}$ renormalised mass.

$$Z_m = 1 + C_F \frac{3}{\epsilon}. \quad (6.26)$$

In order to convert the mass definition to the on-shell scheme we add the finite renormalisation term

$$Z_m^{OS} = 1 - 2C_F, \quad (6.27)$$

here $C_F = (N_c^2 - 1)/2N_c$ is one of the two Casimir invariants of QCD along with $C_A = N_c$. The $q\bar{q}g$ vertex correction involves a renormalisation of the strong couplings constant α_s which is done via replacing the bare constant α_s^0 with the renormalised one, hence it becomes $\alpha_s^0 = \frac{\mu_R^{2\epsilon}}{S_\epsilon} Z_{\alpha_s} \alpha_s$, where

$$Z_{\alpha_s} = 1 - \frac{\alpha_s}{4\pi} \frac{1}{\epsilon} \left(\beta_0 - \frac{2}{3} \right) \left(\frac{\mu_R^2}{m_t^2} \right)^\epsilon, \quad (6.28)$$

and the constant $\beta_0 = \frac{11}{3}C_A - \frac{2}{3}N_f$, where N_f is the number of “active” flavours. The 5-flavour scheme $N_f = 5$ is adopted here.

The loop integrals were evaluated via dimensional regularisation in $d = 4 - 2\epsilon$ dimensions. Which requires some caution when γ_5 is present in the amplitude. We let γ_5 naively anti-commute with all d -dimensional γ_μ 's and then correct that with the finite renormalisation constant known as **Larin counter-term** [280]

$$Z_5 = 1 - 2C_F. \quad (6.29)$$

The renormalised amplitude is written as

$$\mathcal{M}(\alpha_s, m, \mu_R) = Z_A Z_m^{OS} Z_{\alpha_s} \mathcal{M}(\alpha_s^0, m^0). \quad (6.30)$$

Putting all the above substitutions together, we get the renormalised two-loop form-

factor:

$$(\mathcal{A}^{(1)})^R = \mathcal{A}^{(1)} - \mathcal{A}_{UV}^{(0)} - \mathcal{A}_{UV,m}^{(0)} + \mathcal{A}_{\text{Larin}}^{(0)} \quad (6.31)$$

$$\mathcal{A}_{UV}^{(0)} = \frac{\alpha_s}{4\pi} \frac{\beta_0}{\epsilon} \left(\frac{\mu_R^2}{\hat{s}} \right)^{-\epsilon} \mathcal{A}^{(0)}.$$

$$\mathcal{A}_{UV,m}^{(0)} = \frac{\alpha_s}{4\pi} \left(\frac{3}{\epsilon} - 2 \right) C_F \left(\frac{\mu_R^2}{\hat{s}} \right)^{-\epsilon} m^0 \partial_m \mathcal{A}^{(0)}. \quad (6.32)$$

$$\mathcal{A}_{\text{Larin}}^{(0)} = -\frac{\alpha_s}{4\pi} C_F \mathcal{A}^{(0)}.$$

The following IR-counter-term is used in order to cancel the IR divergences.

$$\mathcal{A}_{IR}^{(0)} = \frac{e^{\gamma_E \epsilon}}{\Gamma(1-\epsilon)} \frac{\alpha_s}{4\pi} \left(\frac{\beta_0}{\epsilon} + \frac{C_A}{\epsilon^2} \right) \left(\frac{\mu_R^2}{\hat{s}} \right)^{2\epsilon} \mathcal{A}^{(0)} \quad (6.33)$$

The one-loop form-factors, need to be expanded up to order $\mathcal{O}(\epsilon^2)$, for the UV and IR counter-terms.

6.3.2 Calculation of the exact virtual corrections

The two-loop calculations of the triangle diagrams involves the diagrams of with virtual Z^* and G^0 , depending on the gauge of choice. Observations found in ref.[196] shows that due to Landau-Yang theorem in the Landau gauge the diagrams with the Z^* exchange vanishes. Therefore, the part of the top triangle diagrams can be obtained from the decay amplitude of a pseudoscalar boson into two gluons which is known in the literature in the full mass dependence up to NLO terms [281, 282]. On the contrary, in the unitary gauge, the NLO calculation needs to be done with the Z^* exchange diagrams only. The calculations result in apparently different Lorentz structures, that are linked via the Schouten identity

$$q^\alpha \epsilon^{\beta\gamma\delta\phi} + q^\beta \epsilon^{\gamma\delta\phi\alpha} + q^\gamma \epsilon^{\delta\phi\alpha\beta} + q^\gamma \epsilon^{\delta\phi\alpha\beta} + q^\delta \epsilon^{\phi\alpha\beta\gamma} + q^\phi \epsilon^{\alpha\beta\gamma\delta} = 0 \quad (6.34)$$

A cross-check has been preformed in order to ensure that the NLO calculation introduces no new Lorentz structures, and gives the same result in a general R_ξ gauge as the results in [281, 282]. The two-loop calculation has been carried out in R_ξ gauge. The amplitudes have been automatically generated by **FeynArts** [240] and contracted with the projectors as defined in ?? using **FeynCalc** [283, 284] and **Package X** [285] and in-house Mathematica routines. The two-loop integrals were reduced to a set of master integrals MI, illustrated graphically in Figure 6.4 using **Kira** [286]. These MI's are either products of one-loop functions (a)-(c), (e),(f),(h) and (l) or can be found in the literature [282, 287]. Their implementation in our calculation has been validated numerically using **SecDec** [288, 289]. The virtual correction for the triangle diagrams

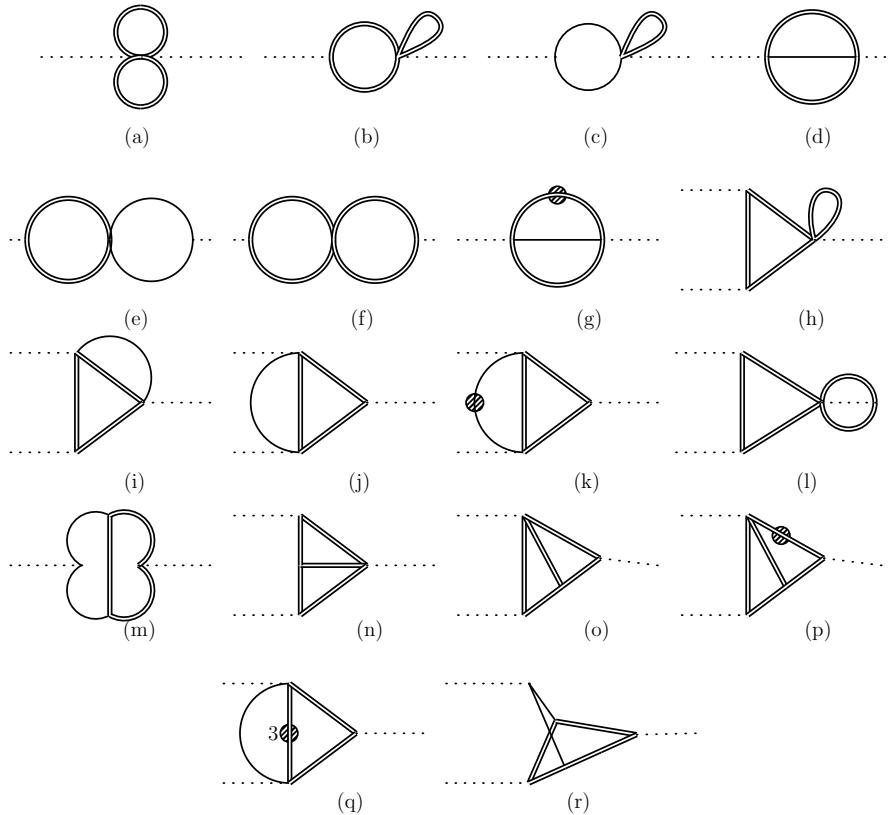


Figure 6.4. The list of two-loop master integrals (MI's) resulting from the reduction of the two-loop triangle corrections, and the product of one-loop MI's appearing in this list also appear in the calculation of the double-triangle diagrams. A single line denotes a massless propagator, while a double line denotes a massive one. The dot denotes a squared propagator, unless the number of the exponent is indicated, here only 3 appears in diagram (q).

can be separated according to their colour factors into

$$\mathcal{A}^{(1)} = C_F \mathcal{A}_{CF}^{(1)} + C_A \mathcal{A}_{CA}^{(1)}, \quad (6.35)$$

The C_A part contains a double pole $\mathcal{O}(1/\epsilon^2)$ and a single pole $\mathcal{O}(1/\epsilon)$, both coming from the IR divergence. Whilst the C_F part contains a UV divergent pole that needs to be cured via mass renormalisation. The poles do not have a dependence on the renormalisation scale μ_R . However, there is a dependence on that scale in the finite part, as well. No new Lorentz structures appeared, and the final result in R_ξ matched the one found in [281, 282] for the Landau gauge. The explicit results are shown in ??

The calculation of the double triangle diagrams (d) of Figure 6.3 is fairly straightforward, all of the integrals can be rewritten in terms of products of one-loop functions. All of the Lorentz structures appear in the double triangle except for \mathcal{P}_6 , analogous to the triangle case. The explicit forms of form-factors corresponding to these structures are presented in ???. Although we write the amplitude using a different tensorial structure with respect to ref.[201] we have checked, using the relations between the two tensorial structures reported in ???, that our result is in agreement with the one presented in ref.[198].

6.3.3 Calculation of the p_T -expanded virtual corrections

The two-loop triangle diagrams can also be interpreted as an expansion in p_T , but this expansion terminates at $\mathcal{O}(p_T^2)$, rather being an infinite series. Hence, in this section we concentrate on the two-loop box diagrams p_T -expansion ¹.

Similar to the two-loop triangle diagrams, the box diagrams amplitudes were generated projected through the same pipeline. After the contraction of the epsilon tensors the diagrams were expanded as described in subsection 6.1.1, keeping only $\mathcal{O}(p_T^4)$ terms. They were reduced to MI's using FIRE [290] and LiteRed [291]. The resulting MI's were identical to the one for Higgs pair production [203]. Nearly all of them are expressed in terms of generalised harmonic polylogarithms with the exception of two elliptic integrals [292, 293]. The renormalisation and IR pole subtraction procedure was carried out like prescribed subsection 6.3.1.

As a control, the two-loop box diagrams were also computed in the LME up to $\mathcal{O}(1/m_t^6)$. Since this expansion should be included within the p_T -expansion. We have retained the LME analytic expression by further expanding the p_T -expanded amplitude in small \hat{s}/m_t^2 . Providing an additional cross-check for the validity of the p_T -expansion.

6.4 Results and conclusions

The virtual corrections to the gluon fusion Zh production have been implemented in a FORTRAN code using `handyG` [294], for the evaluation of generalised harmonic polylogarithms, `Chaplin` [295] for the harmonic polylogarithms appearing in the triangle two-loop

¹The calculation of the box diagrams has been done mainly by my collaborators, the co-authors of [204]

\hat{s}/m_t^2	\hat{t}/m_t^2	ref.[202]	$\mathcal{O}(p_T^6)$
1.707133657190554	-0.441203767016323	35.429092(6)	35.430479
3.876056604162662	-1.616287256345735	4339.045(1)	4340.754
4.130574250302561	-1.750372271104745	6912.361(3)	6915.797
4.130574250302561	-2.595461551488002	6981.09(2)	6984.20

Table 6.2. Comparison of $\mathcal{V}_{fin}4/(\alpha_s^2 \alpha^2)$ with the numerical results of ref.[202]. This plot has been already published in [204].

functions while the elliptic integrals are evaluated using the routines of ref.[293]. Since the result is analytic, the code is significantly faster than the numerical evaluation of the two-loop amplitude [202], with evalution time of ca. 0.5 min per one phase space point on a personal laptop.

In order to facilitate the comparison of our results with the ones presented in the literature, we define the finite part of the virtual corrections as in ref.[201]²

$$\begin{aligned} \mathcal{V}_{fin} = & \frac{G_F^2 m_Z^2}{16} \left(\frac{\alpha_s}{\pi} \right)^2 \left[\sum_i |\mathcal{A}_i^{(0)}|^2 \frac{C_A}{2} \left(\pi^2 - \log^2 \left(\frac{\mu_R^2}{\hat{s}} \right) \right) \right. \\ & \left. + 2 \sum_i \text{Re} \left[\mathcal{A}_i^{(0)} \left(\mathcal{A}_i^{(1)} \right)^* \right] \right] \end{aligned} \quad (6.36)$$

and in the numerical evaluation of eq.(6.36) we fixed $\mu_R = \sqrt{\hat{s}}$. Triangle and LME box topologies were validated against the results of refs.[198, 201] finding perfect agreement at the form-factor level, i.e. $\mathcal{A}_i^{(1)}$.

The virtual part of the partonic cross-section from the finite part of the virtual corrections in eq.(6.36) is defined by

$$\Delta \hat{\sigma}_{virt} = \int_{\hat{t}^-}^{\hat{t}^+} d\hat{t} \frac{\alpha_s}{16\pi^2} \frac{1}{\hat{s}^2} \mathcal{V}_{fin} \quad (6.37)$$

This function is used to confront p_T -expanded results. Starting with low M_{Zh} we have compared the p_T -expanded with the LME \mathcal{V}_{fin} , finding a good numerical agreement. It is important to note that, at the same order in the expansion, the p_T -expanded terms are more accurate than the LME ones, although computationally more demanding. Additional checks have been done using the numerical evaluation of the NLO amplitude by [202], where they have evaluated the exact two-loop MI's using `pySecDec` [296, 297]. Table 6.2 shows a comparison between our p_T -expanded $\mathcal{V}_{fin}4/(\frac{\alpha_s^0}{4\pi} \alpha^2)$ versus the exact numerical result of [202] for several phase space points. As can be seen from the table the relative difference between the two results is less than half a permille.

In Figure 6.5, the dashed lines show the different orders of the expansion. For all

²The definition of the matrix elements here differs by a factor of $\frac{1}{\hat{s}}$ from ref.[201], cf. also ??.

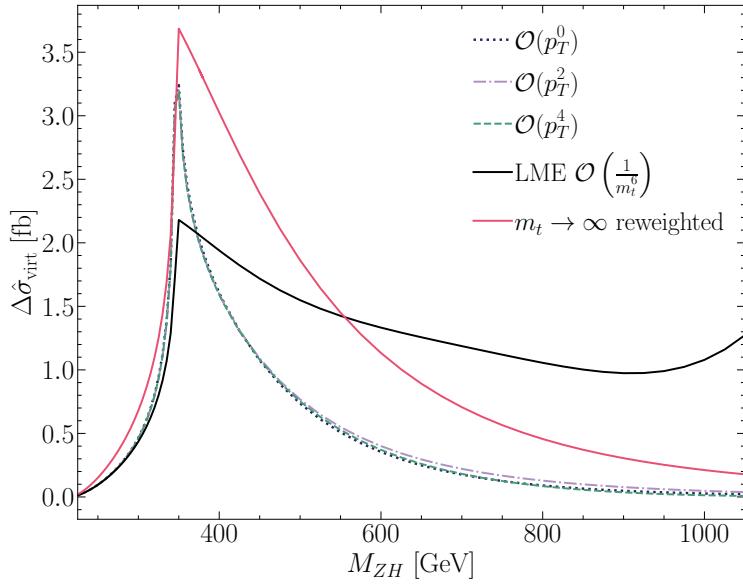


Figure 6.5. $\Delta\hat{\sigma}_{\text{virt}}$ defined by eq.(6.37), shown as a function of M_{ZH} . The various orders of the p_T -expansion are plotted as dashed lines, while the black and red continuous lines stand for the LME and reweighted $m_t \rightarrow \infty$ results, respectively. This plot has been already published in [204].

parts of the matrix elements the best results available, i.e. both $\mathcal{A}^{(0)}$ were used and the double-triangle contribution are evaluated exactly, while for $\mathcal{A}^{(1)}$ we use the various orders in the p_T -expansion. For comparison, the results are shown were $\mathcal{A}^{(1)}$ is replaced by the one computed in LME up to $\mathcal{O}(1/m_t^6)$ (full black line), which as mentioned before is valid up to $M_{ZhH} < 2m_t$. We observe that within the validity of the LME our results agree well with it. Furthermore, the results in the infinite top mass limit reweighted by the full amplitudes squared can be seen as the full red line in the plot, corresponding to the approach of ref.[196], keeping though the double triangle contribution in full top mass dependence. Differently from the LME line, the $m_t \rightarrow \infty$ reweighted one shows a behaviour, for $M_{Zh} \gtrsim 400$ GeV, similar to the behaviour of the p_T lines. Still, the difference between the reweighted result and the p_T -expanded ones is significant. The p_T -expanded results show very good convergence. The zero order in our expansion agrees extremely well with the higher orders in the expansion, and all the three results are very close up to $M_{Zh} \sim 500$ GeV.

The calculation of the virtual two-loop corrections to the $gg \rightarrow Zh$ is done using exact results for the triangle and double-triangle topologies, and in the p_T -expansion for the box one. The result of the calculation showed that we get the exact same MI's that was found for Higgs pair production [203], mostly these MI's are expressed in terms of generalised harmonic polylogarithms with the exception of two elliptic integrals. Using the LO calculation, we have shown the validity of the p_T -expansion covering the invariant mass interval $M_{Zh} \lesssim 750$ GeV which covers $\sim 98\%$ of the total phase space for 13 – 14

TeV energies.

The p_T -expansion agrees with per mill level with the numerical results found in [202]. However, it allows for fast computation of the amplitude with circa one second per phase space point using a modern laptop with mid-range specifications. Additionally, the integration over the \hat{t} variable in eq.(6.37) converges very well. The flexibility of our analytic results, an application to beyond-the-Standard Model is certainly possible.

Finally, it should be noted that this calculation complements nicely the results obtained in ref.[201] using a high-energy expansion, that according to the authors provides precise results for $p_T \gtrsim 200$ GeV. The merging of the two analyses is going to provide a result that covers the whole phase space, can be easily implemented into a Monte Carlo code using v which is currently a work in progress in [Cite the new paper here-later](#)

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