

Phenomenology of the Higgs and Flavour Physics in the Standard Model and Beyond

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Abstract

This thesis investigates some future aspects of Higgs measurements a decade after its discovery, focusing on the potential for future runs of the Large Hadron Colider (LHC). In particular, it aims to probe challenging couplings of the Higgs like its self-coupling and interaction with light quarks.

The first part provides an overview of Higgs physics within the Standard Model Effective Field theory (SMEFT). The second part is about single-Higgs production, starting with a two-loop calculation of the gluon fusion component of Zh to reduce its theoretical uncertainties. Then, the potential for constraining the Higgs trilinear self-coupling from single Higgs rates is revisited; by including equally weakly-constrained four-heavy-quark operators entering at the next-to-leading order in single Higgs rates. These operators highly correlate with the trilinear self-coupling, thus affecting the fits made on this coupling from single Higgs data.

The third part focuses on the Higgs pair production, an essential process for measuring Higgs-self coupling, employing multivariate analysis to study its potential for probing light Yukawa couplings; thereby exploring the sensitivity of Higgs pair production for the light-quark Yukawa interactions.

Finally, the fourth part showcases some models aiming to explain the recent flavour anomalies in the light of a global SMEFT Bayesian analysis combining flavour and electroweak precision measurements.

Keywords: Higgs Physics, Standard Model Effective Field Theory, Flavour observables, Statistical data analysis.

Zusammenfassung

In dieser Arbeit werden einige zukünftige Aspekte der Higgs-Messungen ein Jahrzehnt nach seiner Entdeckung untersucht, wobei der Schwerpunkt auf dem Potenzial für zukünftige Läufe des Large Hadron Collider (LHC) liegt. Insbesondere sollen anspruchsvolle Kopplungen des Higgs, wie seine Selbstkopplung und die Wechselwirkung mit leichten Quarks, untersucht werden. Der erste Teil gibt einen Überblick über die Higgs-Physik innerhalb der effektiven Feldtheorie des Standardmodells (SMEFT). Der zweite Teil befasst sich mit der Single-Higgs-Produktion, beginnend mit einer Zweischleifenberechnung der Gluonenfusionskomponente von Zh , um deren theoretische Unsicherheiten zu reduzieren. Dann wird das Potenzial für die Einschränkung der trilinearen Higgs-Selbstkopplung aus Einzel-Higgs-Raten erneut untersucht, indem ebenso schwach eingeschränkte Vier-Schwer-Quark-Operatoren einbezogen werden, die bei der nächsthöheren Ordnung in die Einzel-Higgs-Raten eingehen. Diese Operatoren korrelieren in hohem Maße mit der trilinearen Selbstkopplung, was sich auf die Anpassungen auswirkt, die für diese Kopplung anhand von Einzel-Higgs-Daten vorgenommen wurden.

Der dritte Teil konzentriert sich auf die Higgs-Paarproduktion, einen wesentlichen Prozess zur Messung der Higgs-Selbstkopplung, und setzt eine multivariate Analyse ein, um ihr Potenzial zur Untersuchung der leichten Yukawa-Kopplungen zu untersuchen; dadurch wird die Empfindlichkeit der Higgs-Paarproduktion für die leichten Quark-Yukawa-Wechselwirkungen erforscht.

Schließlich werden im vierten Teil einige Modelle vorgestellt, die darauf abzielen, die jüngsten Flavour-Anomalien im Lichte einer globalen SMEFT-Bayesian-Analyse zu erklären, die Flavour- und elektroschwache Präzisionsmessungen kombiniert.

Schlagwörter: Higgs Physik, Standardmodell-Effektivfeld-Theorie, Flavour Anomalies, Statistische Datenanalyse

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List of abbreviations

Colliders and working groups .

CERN	Conseil européen pour la recherche nucléaire.
LHC	Large Hadron Collider
HL-LHC	High-Luminosity LHC
CMS	Compact Muon Solenoid
ATLAS	A Toroidal LHC ApparatuS
LEP	Large Electron-Positron Collider
ALEPH	Apparatus for LEp PHysics
SLC	Stanford Linear Collider
FCC	Future circular collider
PDG	Particle data group

Higgs and Standard Model physics.

SM	Standard Model
QCD	Quantum chromodynamics
QED	Quantum electrodynamics
EFT	Effective field theory
SMEFT	Standard Model effective field theory
HEFT	Higgs effective field theory
EW	Electroweak
VEV/ vev	Vacuum expectation value
EWSB	Electroweak symmetry breaking
EWPO	Electroweak precision observables
EWChL	Electroweak chiral Lagrangian
SSB	Spontaneous symmetry breaking
$SU(N)$	Special unitary (group) of dimension N

ggF	Gluon fusion (processes)
$q\bar{q}A$	Quark anti-quark annihilation (processes)
PDF	Parton distribution functions
BR	Branching ratio
STXS	Simplified template cross-sections

Higher order computations.

RGE	Renormalisation group equation or evolution
LO, NLO ...	Leading order, Next to leading order etc.
HTL	Heavy top limit
HPL	Harmonic polylogarithms
GPL	Generalised polylogarithms
HE	High energy expansion

Flavour.

CKM	Cabibbo-Kobayashi-Maskawa-Matrix
\mathcal{CP}	Charge conjugation and parity
MFV	Minimal flavour violation
AFV	Aligned flavour violation
SFV	Spontaneous flavour violation
PDD	Phenomenological data-driven
PMD	Phenomenological model-driven
FCNC	Flavour-changing neutral currents
LUV	Lepton universality violation

Data analysis/statistics.

MC	Monte Carlo (simulation)
ML	Machine learning
BDT	Boosted decision tree
XGBoost	EXtreme gradient boosted decision tree

DNN	Deep Neural Networks
MCMC	Markov chain Monte Carlo (Bayesian analysis)
PCo	Principle component
FDR	False discovery rate
ANOVA	Analysis of variation
HDPI	Highest density posterior interval
CI	Credible interval (Bayesian statistics)
CL	Confidence interval (Frequentist statistics)

New Physics.

4F	Four-fermion
NP	New physics
BSM	Beyond the Standard Model
VLQ	Vector-like quarks
LQ	Leptoquarks
2HDM	Two-Higgs-doublet model
CHM	Composite Higgs model
MSSM	Minimal supersymmetric Standard Model
SILH	Strongly interacting light Higgs

1 Introduction

The discovery of the Higgs boson in 2012 by the ATLAS [1] and CMS [2] experiments at the Large Hadron Collider (LHC) marks the completion of the Standard Model of particle physics (SM) [3–5]; as it was a direct prediction of the spontaneous symmetry breaking mechanism observed in the SM [6–10]. However, this discovery has brought more questions than answers, and even after a decade of its discovery, there is a lot to know about this particle and its potential connections with physics beyond the SM.

Understanding the properties and couplings of the Higgs boson has become the pre-eminent goal of the LHC. Higgs measurements are getting progressively accurate, and our understanding of this particle is approaching a few per cent-level. The future runs of the LHC will open the doors to the Higgs-precision era. However, increased luminosity, i.e. data acquisition from the LHC, without improving the theoretical prediction of Higgs processes is futile. Therefore, to ensure the success of the experimental efforts in probing Higgs couplings and properties at the required precision, it is imperative to include higher-order calculations for Higgs production cross-sections.

An example of such processes is the associated production of the Higgs boson with a Z boson, which suffers from higher theoretical uncertainties than its sister process, the Wh production, because it contains a gluon fusion sub-process $gg \rightarrow Zh$. Furthermore, the gluon fusion channel generally tends to have large higher-order corrections compared to the quark-initiated one; thereby, prompting the need to compute its higher order corrections, in order to improve the theoretical prediction of Zh production. Such computation can be carried out efficiently using a state-of-the-art analytic technique based on the expansion in small transverse momentum proposed in ref. [11].

After a decade of *Higgs physics*, and over ten-thousand Higgs-related publications, we still have a lot to learn about the Higgs boson. In particular, its potential structure is yet to be probed experimentally, and so are its couplings to the light quarks and leptons. Measurements of Higgs self-coupling will reveal if there are, for instance, new scalars beyond the Higgs boson that we have not yet directly observed. Furthermore, studying Higgs coupling to light fermions is essential in understanding the source of their masses' origin and explaining the significant hierarchy between these across the three generations of matter.

The conclusion of the SM-related discoveries did not leave any specific hints to the nature and scale of new physics (NP). Moreover, many experimental searches have excluded NP at scale close to the electroweak symmetry breaking, for most recent searches cf. [12–23]. Although NP is needed to explain the shortcomings of the SM as for instance: neutrino masses, or give a candidate for dark matter and so on. Experimental searches have excluded for most scenarios that NP is at a scale close to the electroweak symmetry breaking. This motivates parametrising NP effects in a model-independent manner, in

terms of higher-dimensional operators suppressed by some high scale Λ . This formalism is known as the Standard Model Effective Field Theory (SMEFT) framework [24–28]. In SMEFT, all leading NP effects in Higgs physics are summarised in a numerable set of mass dimension six operators, that makes minimal assumptions about the nature of NP, guaranteeing a model-independent approach to collider searches. The use of SMEFT in higher-order calculations of Higgs rates has revealed insights into the Higgs potential by the appearance of the Higgs trilinear self-coupling within electroweak loop corrections of single-Higgs processes. This allows to put constraint on this coupling from measurements of single-Higgs rates at the LHC can be used to constrains this coupling [29–36]. Nevertheless, more SMEFT operators can also enter in single-Higgs loops that alter the constraining power of these measurements. The interconnectivity between the Higgs and top-quark sectors is emphasised within the SMEFT framework, as recent global fits have established strong correlations between observables from both sectors as well as the electroweak precision observables (EWPO) [37]. Strong correlations between the top sector and EWPO are also seen at loop-level [38, 39] thus; one expects to see similar correlations emerging from loop effects of top operators on Higgs processes.

The observation of Higgs pairs is slated for the High-Luminosity (HL) LHC operating phase. This rare process will be –if observed– the *pièce de résistance* of the LHC Higgs physics programme [40], directly measuring the Higgs trilinear self-interaction, also untangling Higgs potential measurements from the top-sector interactions. Furthermore, this process could be of great utility in probing Higgs coupling to light quarks, from the enhancement of the quark-initiated Higgs pair production, cf. [41, 42] and as will be shown in this thesis. The full potential of Higgs pair production can be exploited when it is treated as a multivariate problem by implementing an interpretable machine learning analysis technique [43]. In this manner, it is possible to have simultaneous constraints of the two most elusive Higgs interactions, light-quark Yukawa and the trilinear couplings.

Recent measurements, by Belle and Babar, in addition to the LHCb experiment at CERN, of B -mesons semi-leptonic decays showed some tension with the SM predictions of lepton flavour universality of electroweak couplings [44–48], with up to $\sim 3\sigma$ deviation from the SM [49–52]. These anomalies require models with some flavour violation that makes model-building for explaining these anomalies at tree-level Augean task [53–62]. Additionally, to complicate things further, these anomalies are in tension with EWPO. Hence, this thesis promotes a more careful treatment of these anomalies, by introducing them at the loop level in SMEFT and performing a global fit combining both flavour and EWPO data. The fit result would allow for a SMEFT guided UV-model building for these anomalies, with extended Higgs and top sectors.

This thesis is structured as follows: I start by presenting the basics of Effective Fields Theories relevant to Higgs physics at the LHC in [chapter 2](#).

The second part of the thesis focuses on the production of –single– Higgs at the LHC, starting with an overview in [chapter 3](#), followed by a discussion on the use of the p_T -expansion technique for obtaining an analytic expression for the virtual correction of the gluon fusion Zh production in [chapter 4](#). Next, [chapter 5](#) showcases the poten-

tial of single-Higgs processes to probe four-fermion operators from the top sector, by performing higher-order computations of these processes in SMEFT. The potential for constraining these operators for the considered single-Higgs production processes alongside the trilinear Higgs self-coupling is investigated by means of a Bayesian fit.

The third part of the thesis focuses on the production of Higgs boson in pairs at the HL-LHC ([chapter 6](#)). Afterwards, in [chapter 7](#), I show the potential for employing Higgs pair production to probe light quark couplings to the Higgs boson. In addition, I show a multivariate analysis method, that maximises the efficiency of extracting the Higgs pair signal using interpretable machine learning. The last part of the thesis, [chapter 8](#), describes the potential UV models for the B anomalies, inspired by a global SMEFT fit and minimal flavour violation (MFV).

List of publications

1. **L. Alasfar**, R. Gröber, C. Grojean, A. Paul and Z.Qian,
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5. **L. Alasfar**, R. Corral Lopez and R. Gröber,
Probing Higgs couplings to light quarks via Higgs pair production,
JHEP **11** (2019), 088
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Part I

Preliminaries

2 Higgs and effective field theories

The Standard Model (SM) has been concluded after the Higgs boson discovery [1, 2], followed by its extensive characterisation by the ATLAS and CMS experiments including its general properties [63–70], cross-sections [71–74] and couplings to electroweak and heavier fermions [75, 76]. Nonetheless, there are many open questions regarding the nature of the Higgs boson, which are left unanswered. This includes the shape of Higgs boson potential, its coupling to light quarks and the hierarchy problem. Answering these questions opens space for extending the SM by New Physics (NP) degrees of freedom.

In order to make the search for NP more accessible and model-agnostic, we revert to **effective field theories** (EFT), one of the most perspicacious concepts of quantum field theory. In the EFT framework, the interactions mediated by NP at the small scale of arbitrary complexity can be systematically simplified by approximating these interactions via integrating the UV degrees of freedom, leaving numerable operators consisting of higher dimensional operator consisting of SM fields, which are added to the SM.

These “phenomenological Lagrangians”, as called by Weinberg [77], are not necessarily renormalisable but still allow for robust predictions that can be tested at colliders, including higher-order effects.

This chapter is organised as follows: In section 2.1, the Higgs sector of Standard Model effective field theory (SMEFT) is presented along with the parametrisation of single and di-Higgs rates in terms of the SMEFT Wilson coefficients. In contrast to the SMEFT formalism, section 2.2 will present a non-linear EFT formalism known as the EW Chiral Lagrangian (EWChL) or the Higgs effective field theory (HEFT). Finally, I will conclude this chapter in section 2.3.

2.1 The Higgs boson and Standard Model effective field theory

The idea behind the Standard Model effective field theory is to preserve the SM symmetries and fields. In particular, the Higgs boson $h(x)$ is assumed to originate from the doublet ϕ , like the SM. New operators of higher mass dimension are added to dimension-four SM operators. These new operators consist of the SM fields and obey its symmetries. Although these operators are not renormalisable, they are, nonetheless, predictive.

From simple dimensional analysis, it is known that higher dimensional operators need to contain an inverse mass with some power $p = 4 - d$ in the couplings. Therefore, it is not needed to use the infinite number of the Wilson coefficients C_i when fitting to experimental measurements. Since, the higher dimensional operators are suppressed

by higher powers of the UV scale Λ , hence their effect can be neglected. For example, if the NP scale is set to $\Lambda = 1$, then the effects of dimension-six operators will be at the per cent level. At the same time, dimension-eight operators will have effects of order $\sim 10^{-4}$, allowing to ignore the dimension-eight and higher operators in the majority of the LHC studies. Regarding dimension-five, there is only one operator called the Weinberg operator [78], which does not have a considerable Higgs phenomenology. Hence, I shall be discussing SMEFT with dimension-six operators only as they have the most prominent collider phenomenology [79, 80], for studies on Higher-dimensional SMEFT operators cf. [81–84]. The SMEFT Lagrangian up to dimension-six operators is given by

$$\mathcal{L}_{\text{SMEFT}}^{d=6} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum_i C_i \mathcal{O}_i. \quad (2.1)$$

Phenomenological studies of EFTs with dimension-six operators primarily focus on using a set of complete and non-redundant “basis”. This is since different effective operators will correspond to the same observables, e.g. same scattering amplitudes of SM particles. This is the case if the operators can be related using equations of motion, Fierz transformations, integration by parts or field redefinitions. Thus leading to non-trivial and counter-intuitive relations between operators. Consequently, the construction of basis for the dimension-six SMEFT Lagrangian of eq. (2.1) is a cumbersome task. Such task has been accomplished by [25] recently forming what is known as the **Warsaw Basis**. Another set of basis is the strongly-interacting light Higgs basis (SILH), initially proposed by [24], before the Warsaw basis and completed in refs. [26, 27]. A more recent set of basis has been published in [28] using a subset of couplings characterising the interactions of mass eigenstates in the effective Lagrangian.

The complete $d = 6$ SMEFT is described by 2499 independent parameters [85–87]. However, if one suppresses the flavour indices, assuming SMEFT is flavour universal, their inventory is significantly reduced. In the Warsaw basis, for example, assuming Baryon number conservation and dropping the flavour indices, one has only 59 operators, listed in Table 2.1. It should be noted that all of the SMEFT basis will produce the same phenomenology, though the choice of basis is sometimes helpful in simplifying the analysis. In this thesis, I will focus on Warsaw basis.

2.1.1 Single Higgs processes in SMEFT

Single Higgs production and decay processes are modified at LO by a relatively long list of operators summarised in eqs. (2.2), (2.3) and (2.4). Explicit formulae for the Higgs rates dependence on the Wilson coefficients of these operators can be found in [88]

2.1 The Higgs boson and Standard Model effective field theory

X^3		Pure Higgs		$\psi^2\phi^3 + \text{h.c.}$	
\mathcal{O}_G	$f^{ABC}G_\mu^{A\nu}G_\nu^{B\rho}G_\rho^{C\mu}$	$\mathcal{O}_{\phi\square}$	$(\phi^\dagger\phi)\square(\phi^\dagger\phi)$	$\mathcal{O}_{e\phi}$	$(\phi^\dagger\phi)(\bar{l}_p e_r \phi)$
$\mathcal{O}_{\widetilde{G}}$	$f^{ABC}\widetilde{G}_\mu^{A\nu}G_\nu^{B\rho}G_\rho^{C\mu}$	$\mathcal{O}_{\phi D}$	$(\phi^\dagger D_\mu\phi)^*\left(\phi^\dagger D_\mu\phi\right)$	$\mathcal{O}_{u\phi}$	$(\phi^\dagger\phi)(\bar{q}_p u_r \widetilde{\phi})$
\mathcal{O}_W	$\epsilon^{IJK}W_\mu^{I\nu}W_\nu^{J\rho}W_\rho^{K\mu}$	\mathcal{O}_ϕ	$(\phi^\dagger\phi)^3$	$\mathcal{O}_{d\phi}$	$(\phi^\dagger\phi)(\bar{q}_p d_r \phi)$
$\mathcal{O}_{\widetilde{W}}$	$\epsilon^{IJK}\widetilde{W}_\mu^{I\nu}W_\nu^{J\rho}W_\rho^{K\mu}$				
$X^2\phi^2$		$\psi^2X\phi + \text{h.c.}$		$\psi^2\phi^2D$	
$\mathcal{O}_{\phi G}$	$\phi^\dagger\phi G_{\mu\nu}^A G^{A\mu\nu}$	\mathcal{O}_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \phi W_{\mu\nu}^I$	$\mathcal{O}_{\phi l}^{(1)}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{l}_p \gamma^\mu l_r)$
$\mathcal{O}_{\phi\widetilde{G}}$	$\phi^\dagger\phi \widetilde{G}_{\mu\nu}^A G^{A\mu\nu}$	\mathcal{O}_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \phi B_{\mu\nu}$	$\mathcal{O}_{\phi l}^{(3)}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu^I \phi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$\mathcal{O}_{\phi W}$	$\phi^\dagger\phi W_{\mu\nu}^I W^{I\mu\nu}$	\mathcal{O}_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \widetilde{\phi} G_{\mu\nu}^A$	$\mathcal{O}_{\phi e}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{e}_p \gamma^\mu e_r)$
$\mathcal{O}_{\phi\widetilde{W}}$	$\phi^\dagger\phi \widetilde{W}_{\mu\nu}^I W^{I\mu\nu}$	\mathcal{O}_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \widetilde{\phi} W_{\mu\nu}^I$	$\mathcal{O}_{\phi q}^{(1)}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{q}_p \gamma^\mu q_r)$
$\mathcal{O}_{\phi B}$	$\phi^\dagger\phi B_{\mu\nu} B^{\mu\nu}$	\mathcal{O}_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \widetilde{\phi} B_{\mu\nu}$	$\mathcal{O}_{\phi q}^{(3)}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu^I \phi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$\mathcal{O}_{\phi\widetilde{B}}$	$\phi^\dagger\phi \widetilde{B}_{\mu\nu} B^{\mu\nu}$	\mathcal{O}_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \phi G_{\mu\nu}^A$	$\mathcal{O}_{\phi u}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{u}_p \gamma^\mu u_r)$
$\mathcal{O}_{\phi WB}$	$\phi^\dagger\tau^I\phi W_{\mu\nu}^I B^{\mu\nu}$	\mathcal{O}_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \phi W_{\mu\nu}^I$	$\mathcal{O}_{\phi d}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{d}_p \gamma^\mu d_r)$
$\mathcal{O}_{\phi\widetilde{WB}}$	$\phi^\dagger\tau^I\phi \widetilde{W}_{\mu\nu}^I B^{\mu\nu}$	\mathcal{O}_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \phi B_{\mu\nu}$	$\mathcal{O}_{\phi ud} + \text{h.c.}$	$i(\widetilde{\phi}^\dagger D_\mu \phi)(\bar{u}_p \gamma^\mu d_r)$
$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$			
\mathcal{O}_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	\mathcal{O}_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$		
$\mathcal{O}_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	\mathcal{O}_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$		
$\mathcal{O}_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	\mathcal{O}_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$		
$\mathcal{O}_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	\mathcal{O}_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$		
$\mathcal{O}_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	\mathcal{O}_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$		
		$\mathcal{O}_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$		
		$\mathcal{O}_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$		
$(\bar{L}L)(\bar{R}R)$		$(\bar{L}R)(\bar{L}R) + \text{h.c.}$			
\mathcal{O}_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$	$\mathcal{O}_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \epsilon_{jk} (\bar{q}_s^k d_t)$		
\mathcal{O}_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$	$\mathcal{O}_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \epsilon_{jk} (\bar{q}_s^k T^A d_t)$		
\mathcal{O}_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$	$\mathcal{O}_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \epsilon_{jk} (\bar{q}_s^k u_t)$		
\mathcal{O}_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$	$\mathcal{O}_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$		
$\mathcal{O}_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$	\mathcal{O}_{ledq}	$(\bar{l}_p^j e_r) (\bar{d}_s q_{tj})$		
$\mathcal{O}_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$				
$\mathcal{O}_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$				
$\mathcal{O}_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$				

Table 2.1. Complete list of the dimension-six SMEFT operators in the Warsaw basis [25]. The \mathcal{CP} violating operators contains the dual fields \tilde{X} . The flavour labels of the form p, r, s, t on the \mathcal{O} operators are suppressed on the left hand side of the tables.

SMEFT operators modifying Higgs rates at LO

Higgs operators

$$\begin{aligned} & C_{\phi D}, \mathcal{O}_{\phi\square}, \mathcal{O}_{\phi G}, \mathcal{O}_{\phi W}, \mathcal{O}_{\phi B}, \mathcal{O}_{\phi WB}, \mathcal{O}_{\phi l}^{(1)}, \\ & \mathcal{O}_{\phi l}^{(3)}, \mathcal{O}_{\phi e}, \mathcal{O}_{\phi q}^{(1)}, \mathcal{O}_{\phi q}^{(3)}, \mathcal{O}_{\phi u}, \mathcal{O}_{\phi d}, \mathcal{O}_{\tau\phi}, \mathcal{O}_{t\phi}, \mathcal{O}_{b\phi}, \mathcal{O}_{tb\phi}. \end{aligned} \quad (2.2)$$

Top-quark operators

$$\mathcal{O}_{tG}, \mathcal{O}_{tW}, \mathcal{O}_{tB}, \quad (2.3)$$

other

$$\mathcal{O}_G, \mathcal{O}_{ll}^{(1)}, \mathcal{O}_{Qq}^{(1),(3)}, \mathcal{O}_{tu}, \mathcal{O}_{td}^{(1),(8)}, \mathcal{O}_{Qu}^{(1),(8)}, \mathcal{O}_{Qd}^{(1),(8)}. \quad (2.4)$$

The third-generation quarks are denoted by Q while the first and second-generation quarks are assumed to have the same coupling and are denoted by q, u, d .

Some of these operators are strongly constrained from EWPO data such as $\mathcal{O}_{\phi D}$ and $\mathcal{O}_{\phi WB}$, while others still have weak bounds from current measurements and do not affect EWPOs. A most recent fit on SMEFT Wilson coefficients can be found in ref. [38], where Higgs and EW data were used to fit a subset of the SMEFT Wilson coefficients of the operators listed above. The fit also includes the effects of RGE and NLO (even NNLO corrections to m_W). Instead, in [89], a global fit for a larger set of operators, but only including LO effects, including EW, Higgs and top-quark data. A study that was published in ref. [39], has utilised EWPO data to constrain the four-fermion operators appearing in Higgs rates at LO and operators with four heavy quarks, using their NLO effects on EW bosons pole masses. We shall see in chapter 5 that the latter operators also contribute to Higgs rates at NLO. A wider scope analysis including a wide range of Higgs, top-quark, di-boson and EWPO data has been performed in [37].

The dependence of single Higgs rates on the SMEFT Wilson coefficients gets more complicated once higher-order effects are taken into account. In the fit results reported from [38], the RGE of these Wilson coefficients introduces mixing with operators that do not appear at LO, and also the non-log piece of the loop corrections to the rates and masses of the EW and Higgs bosons, see for example refs.[31, 90, 91].

A prominent example of an operator appearing only at NLO in single Higgs processes is \mathcal{O}_ϕ , which modifies the Higgs self-interactions, namely the trilinear coupling. Typically, one needs to observe Higgs pair production to directly probe the Higgs trilinear self-coupling. However, due to the appearance of Higgs self-interaction and its modifiers, i.e. C_ϕ in SMEFT context, in higher-order EW corrections to Higgs observables and EWPO data [29–31, 33–36, 91?]. Figure 2.1 illustrates example Feynman diagrams of single Higgs processes to which the trilinear Higgs self-coupling enters via NLO corrections. Using the results from the aforementioned references, a global fit with all operators that enter at tree-level in addition to the loop effects from the Higgs self-coupling has been performed in refs. [38, 92]. Additionally, experimental searches for

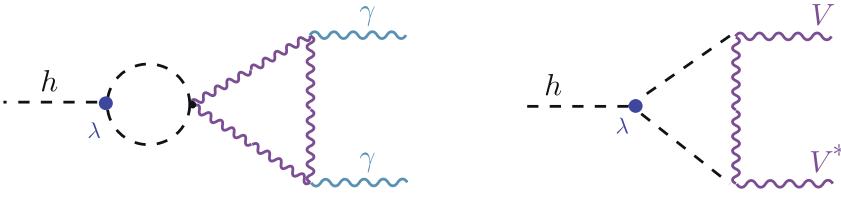


Figure 2.1. NLO EW corrections of single Higgs processes, were the Higgs trilinear self-coupling (the red circle) enters. Here the Higgs decay to two photons is shown as an example.

the Higgs trilinear self-coupling in single-Higgs rates have been presented by ATLAS [93] and CMS [76].¹

2.1.2 Higgs pair production and SMEFT

Higgs pair production in hadron colliders is sensitive to six \mathcal{CP} even SMEFT operators², under the assumption of Minimal Flavour violation (MFV).³ These operators are

$$\mathcal{O}_{\phi D}, \mathcal{O}_{\phi \square}, \mathcal{O}_\phi, \mathcal{O}_{t\phi}, \mathcal{O}_{\phi G}, \mathcal{O}_{tG}, \quad (2.5)$$

and their effects, with the corresponding colours are demonstrated in Figure 2.2, except for $\mathcal{O}_{\phi D}$ and $\mathcal{O}_{\phi \square}$, as they modify all SM Higgs vertices. However, MFV is not the only way to approach SMEFT, there exist more complex flavour structures that allow for significant enhancements of the first and second generation Yukawa couplings without being excluded by flavour observables. Such formalisms will be discussed in chapter 7.

The primary operator to constrain from Higgs pair as mentioned before is \mathcal{O}_ϕ , for two reasons; a) the rest of the operators appearing in di-Higgs can be strongly constrained from single Higgs and top quark processes. b) The effect of \mathcal{O}_ϕ on Higgs pair production is significantly higher than in single Higgs or EW observables. This is illustrated in Figure 2.3 by comparing the relative change of the gluon fusion cross-sections at NLO QCD for single and di-Higgs production. This is not surprising since C_ϕ appears at LO in Higgs pair production.

Another advantage for Higgs pair production searches is the sensitivity of this process to non-linear couplings, for example, diagrams (b) and (d) of Figure 2.2. Although in SMEFT, these diagrams correspond to the same operators in (a) and (c), respectively, in HEFT, this is not necessarily the case.

¹I present references here to the most recent results.

²For or Higgs pair production with \mathcal{CP} violating operators, see ref. [94].

³MFV assumes that new physics operators will follow the same flavour hierarchies as the SM.

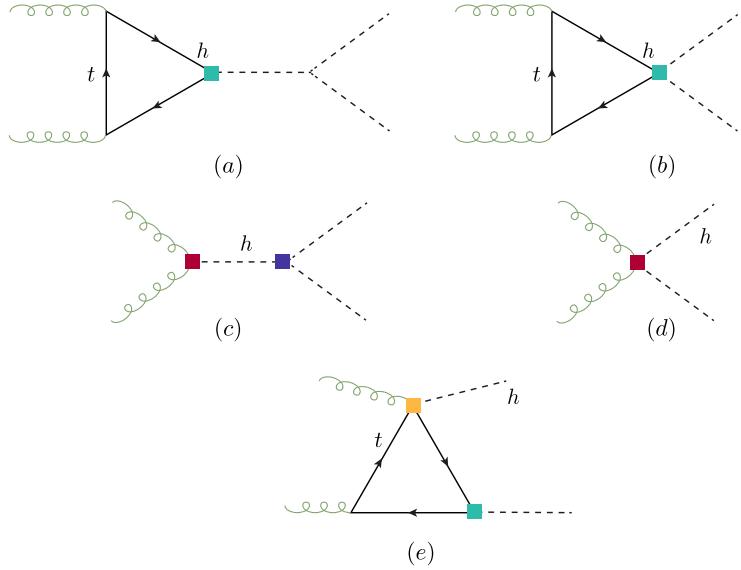


Figure 2.2. Example of diagrams illustrating how the dimension-six SMEFT operators enter in Higgs pair production at hadron colliders.

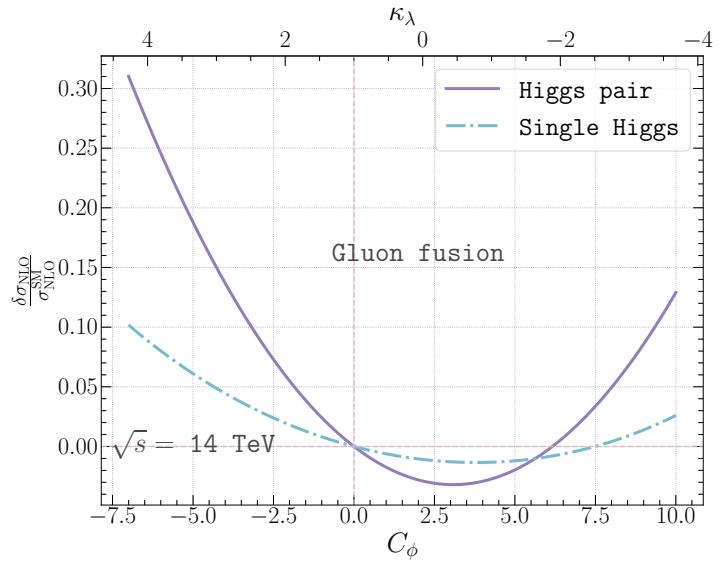


Figure 2.3. The relative change of the NLO QCD cross-section of gluon fusion production of single Higgs (dashed line) and Higgs pair (solid line) at a pp collider with $\sqrt{s} = 14$ TeV as a function of C_ϕ or the corresponding κ_λ .

2.2 The Higgs effective field theory

Given the strong bonds on the ρ parameter, it would be plausible to assume that the NP maintains the custodial symmetry $SU(2)_V$ and treats the chiral symmetry breaking pattern $SU(2)_L \otimes SU(2)_R \rightarrow SU(2)_V$ the same way the QCD chiral symmetry breaking is treated. This formalism considers the pions as pseudo-Nambu Goldstone bosons to describe their properties and couplings. In the pion case, this is known as **chiral perturbation theory** [95, 96]. The same mathematical description could be applied to the case of EW symmetry breaking by constructing the EW chiral Lagrangian (EWChL). In this formalism, the Goldstone bosons $\pi^a(x)$ of the SM are considered the generators of $SU(2)_L$ unitary transformation.

$$\mathcal{U}(x) = e^{i\pi^a(x)\sigma_a/v}, \quad (2.6)$$

which implies that the Goldstone fields transform non-linearly under $SU(2)_L \otimes SU(2)_R$. The Higgs boson $h(x)$ is added as an $SU(2)_L \otimes U(1)_Y$ singlet, and can appear in the EWChL at any power. Contrary to the SMEFT power counting in the NP scale Λ , in the EWChL, terms are ordered according to their *chiral dimension* χ , defined for spacetime derivatives ∂_μ , bosonic ϕ, X_μ and ψ fermionic generic fields as [97, 98]

$$[\phi]_\chi = 0, [X]_\chi = 0, [\partial_\mu]_\chi = 1, [\psi]_\chi = 2. \quad (2.7)$$

The zeroth-order term of the EWChL possesses a chiral dimension of $\chi = 2$, while higher-order terms could be considered terms generated perturbatively from L loop interactions, an having a chiral dimension $\chi = 2L + 2$. This power-counting causes some SMEFT dimension-six operators, in the Warsaw basis, to be considered of a higher order in EWChL. A prominent example of this is the chromomagnetic operator \mathcal{O}_{tG} being of chiral dimension five. The relevant terms for single- and di-Higgs production of the EWChL are given in the unitary gauge by [92, 99]

$$\begin{aligned} \mathcal{L}_{\text{HEFT}} = & \frac{h}{v} \left[\left(\delta c_W m_W^2 W_\mu^+ W^{-\mu} + \delta c_Z \frac{m_Z^2}{2} Z_\mu Z^\mu \right) \right. \\ & + c_{ww} \frac{g_2^2}{2} W_{\mu\nu}^+ W^{-\mu\nu} + c_{w\square} g_2^2 \left(W_\mu^- \partial_\nu W^{+\mu\nu} + \text{h.c.} \right) + c_{\gamma\gamma} \frac{\alpha}{8\pi} A_{\mu\nu} A^{\mu\nu} \\ & + c_{zz} \frac{g_2^2 + g_1^2}{4} Z_{\mu\nu} Z^{\mu\nu} + c_{z\gamma} \frac{eg_1}{16\pi^2} Z_{\mu\nu} A^{\mu\nu} + c_{z\square} g_2^2 Z_\mu \partial_\nu Z^{\mu\nu} + c_{\gamma\square} g_2 g_1 Z_\mu \partial_\nu A^{\mu\nu} \Big] \\ & + \frac{\alpha_s}{8\pi} \left(c_{gg} \frac{h}{v} + c_{gg}^{(2)} \frac{h^2}{2v^2} \right) \text{Tr}[G_{\mu\nu} G^{\mu\nu}] - \sum_f \left[m_f \left(c_f \frac{h}{v} + c_{ff} \frac{h^2}{2v^2} \right) \bar{f}_R f_L + \text{h.c.} \right] \\ & - c_{hh} \frac{m_h^2}{2v} h^3 + \dots \end{aligned} \quad (2.8)$$

I have omitted here the kinetic and mass terms of the Higgs, \mathcal{CP} violating terms, as well as couplings not relevant to LHC phenomenology.

In addition to NP effects, this Lagrangian also includes the LO and NLO SM vertices, for example the parameter $\delta_{CV} = 1$ corresponds to the tree-level coupling between the Higgs field and the EW bosons $V = W, Z$. While the coupling $c_{gg} = 2/3$ corresponds to the SM effective coupling at NLO if the heavy top limit (HTL) $m_t \rightarrow \infty$ is applied. In contrast to the SMEFT, the couplings of one and two Higgs bosons to fermions or gluons become de-correlated. This feature gives this Lagrangian a richer phenomenology for Higgs pair production.

The HEFT coefficients modifying the Higgs pair production via gluon fusion are

$$c_{hh}, c_t \text{ (a)}, c_{tt} \text{ (b)}, c_{gg} \text{ (c)}, c_{gg}^{(2)} \text{ (d)}, \quad (2.9)$$

with the same colours highlighted in the operator insertions of Figure 2.2 and where the letter next to the coefficient indicates the diagram, in which the coefficient appears. A full parametrisation of the Higgs pair cross-section at NLO (inclusive and differential) and NNLO (inclusive) can be found in refs. [100–102] and is implemented at NLO in the POWHEG-BOX software [103].

2.2.1 Translation between SMEFT and HEFT

In order to have a canonical Higgs boson propagator and facilitate the translation between SMEFT and HEFT or to the κ -formalism, one needs to put the SMEFT Lagrangian into the canonical form, that is to convert the operators with covariant derivatives acting on the Higgs to canonically normalised Higgs kinetic term. This is done by the field redefinition.

$$\phi = \begin{pmatrix} 0 \\ h(1 + c_{h,kin}) + v \end{pmatrix}, \quad (2.10)$$

with

$$c_{h,kin} = \left(C_{\phi,\square} - \frac{1}{4} C_{\phi D} \right) \frac{v^2}{\Lambda^2}. \quad (2.11)$$

This field redefinition will generate derivative interactions of the form $h(\partial_\mu h)^2$ and $h^2(\partial_\mu h)^2$. In order to remove these terms, and for sake of simplicity, I use a gauge-dependent field redefinition⁴

$$h \rightarrow h + c_{h,kin} \left(h + \frac{h^2}{v} + \frac{h^3}{3v^2} \right). \quad (2.12)$$

This field redefinition leads to $c_{h,kin}$ modifying all Higgs couplings.

Before discussing the translation between SMEFT and HEFT, some words of caution are in order: First, HEFT is less restrictive than SMEFT. Therefore, it contains more degrees of freedom. This makes some points of the HEFT parameter space unmappable

⁴For gauge-independent formalism cf. [104].

to SMEFT. In addition, the operator ordering is different in both formalisms, as mentioned before. Some operators present in SMEFT will be absent in HEFT and vice-versa. In Table 2.2, the translation between the HEFT and SMEFT Wilson coefficients of the operators relevant to Higgs pair production at LO is shown. More general translation

HEFT	SMEFT (Warsaw)
c_{hh}	$1 - 2 \frac{v^4}{m_h^2} C_\phi + 3c_{h,kin}$
c_f	$1 + c_{h,kin} - C_{f\phi} \frac{v^3}{\sqrt{2}m_f}$
c_{ff}	$-C_{f\phi} \frac{3v^3}{2\sqrt{2}m_f} + c_{h,kin}$
c_{gg}	$8\pi/\alpha_s v^2 C_{\phi G}$
$c_{gg}^{(2)}$	$4\pi/\alpha_s v^2 C_{\phi G}$

Table 2.2. Translation between the Wilson coefficients of HEFT and SMEFT for the operators relevant to Higgs pair production.

between SMEFT in Warsaw and SILH basis and HEFT can be done automatically using [Rosetta](#) package [105]

2.2.2 EFT and κ -formalism

The κ -formalism provides an experimentally accessible approach to study the Higgs boson properties. The κ parameters are part of a more generalised formalism called the Higgs **Pseudo-observables** [106]. If the new physics contributions do not generate new Lorentz structures, there is a possible translation between the Wilson coefficients in the SMEFT Warsaw basis and the κ formalism. In particular, taking the rescaling of the trilinear coupling, κ_λ , the translation is given by

$$\kappa_\lambda = 1 - \frac{2v^4}{m_h^2} \frac{C_\phi}{\Lambda^2} + 3c_{h,kin}. \quad (2.13)$$

A similar relation exists for the rescaling of the quark Yukawa couplings κ_q

$$\kappa_q = 1 + c_{h,kin} - \frac{v^3}{\sqrt{2}m_q} \frac{C_{q\phi}}{\Lambda^2}. \quad (2.14)$$

In these two examples, one can see the similarities between κ -formalism and HEFT, but this is not always the case. Other translations could be obtained by comparing how SMEFT operators modify the Higgs couplings with the SM and matching it with the corresponding κ or other Higgs pseudo-observable.

However, one should be careful while interpreting results quoted in terms of Wilson coefficients in the SMEFT framework extracted from multi-Higgs or multi-vector bosons searches. These results include couplings that are not present in the SM. For example,

the $hhq\bar{q}$ coupling, though being linearly related to the quark Yukawa coupling $hq\bar{q}$, is not a rescaling of any SM Higgs coupling. With this in mind, one can strictly remain within a linear EFT and link the rescaling of the quark Yukawa, κ_q , to the $hhq\bar{q}$ coupling through

$$g_{hhq\bar{q}}^{\text{linear-EFT}} = -\frac{3}{2} \frac{1-\kappa_q}{v} g_{hq\bar{q}}^{\text{SM}}. \quad (2.15)$$

This relation will no longer hold once a non-linear EFT, like HEFT, is used. Hence, the κ -formalism must be applied carefully when multi-Higgs signals are considered.

2.3 Conclusions

Effective field theories provide a systematic yet simplified approach for NP searches by simplifying its complex interaction structures. This can be viewed as a dimensionality reduction approach and collapsing all the NP interactions into effective ones. They would be observed at colliders with energy reaches below the NP scale Λ . The linear approach to EFT is called the SMEFT that preserves the SM fields and symmetries, and the Higgs boson is a part of an $SU(2)_L$ doublet ϕ like the SM. In contrast, non-linear approaches such as HEFT/EWChL treat the Higgs boson as a singlet. The latter approach is more general and introduces independent parameters involving multiple Higgs bosons. For example, the couplings $f\bar{f}h$ and $f\bar{f}hh$ will be generated in SMEFT and HEFT. Still, in SMEFT, both are related by the Wilson coefficient $C_{\phi f}$ ⁵, while in HEFT, they have independent Wilson coefficients c_f and c_{ff} , respectively.

Most of the Wilson coefficients involving Higgs interactions are strongly constrained by EWPOs and Higgs and top-quark data. However, the bounds on the Wilson coefficient modifying Higgs self-couplings C_ϕ remain dominated by theoretical constraints from perturbative unitarity [107, 108]. This can be improved by the searches for Higgs pair production at the HL-LHC, as this process is more sensitive to the trilinear Higgs self-coupling than EWPO and single-Higgs data.

⁵They are also related by the coefficient $c_{h,kin}$ that modifies all couplings of the Higgs boson

Part II

Single Higgs Processes at the LHC

3 Overview of Higgs production at colliders

The four most important Higgs production processes at the LHC: gluon fusion (ggF), vector-boson fusion (VBF), vector bosons Higgsstrahlung (Vh), and the production with top (and anti-top) pair ($t\bar{t}h$). It should be noted that sometimes the ggF category will include the quark anti-quark annihilation, but this is negligible in the SM but becomes important for significant modifications of light Yukawa couplings. These processes are illustrated in Figure 3.1, and their details were summarised in Table 3.1. These four channels have been observed at the LHC with $> 5\sigma$ significance. This chapter aims to provide an overview of the current theoretical status of these channels.

Process	Cross-section 13 TeV (pb)	Theo. accuracy	Exp. uncertainty (%)	Contribution (%)
ggF	48.51	N3LO QCD & NLO EW	6.5	88
$t\bar{t}h$	0.58	NLO QCD & NLO EW	20.0	1
VBF	3.78	NNLO QCD* & NLO EW	10.0	7
Vh	2.25	NNLO QCD & NLO EW	15.0	4

Table 3.1. Summary of the Higgs production processes at the LHC.

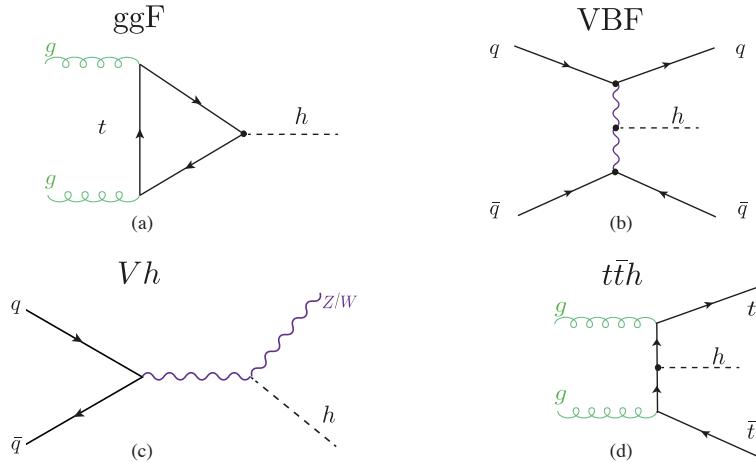


Figure 3.1. Feynman-diagram examples of the leading Higgs production processes at the LHC.

3.1 Current status of the Higgs production channels

3.1.1 Gluon fusion process

The gluon fusion (ggf) has the largest cross-section amongst all the Higgs production channels, and consequently has the lowest experimental uncertainty. This motivates continuous improvements of its theoretical prediction. The current state-of-the-art theoretical computation for the Higgs inclusive cross-section is N³LO in QCD ¹ and NLO in EW [109]. A full differential cross-section for the final state $gg \rightarrow h \rightarrow \gamma\gamma$ has been computed recently to N³LO in QCD, also for the kinematic variables y_h , y_{γ_1} , y_{γ_2} , $\Delta y_{1,2}$ using the projection-to-born method [110]. In addition, the fiducial differential cross-section in p_T with experimental cuts has been computed up to third resummed logarithms ² and fixed order, i.e. N³LL' N³LO dependence [111]. The state-of-the-art total theoretical uncertainty is 5.4%; this includes uncertainties comes from the branching fraction calculation, PDF+ α_s , missing higher-order EW corrections and quark mass uncertainties.

The predictions can be further improved by the computation of mixed QCD-EW effects. The virtual corrections of these effects were computed in [112], while the two-loop effects with two particle final states appearing in the real corrections of $gg \rightarrow hg$ were computed in [113]. The computation was completed by inclusion of light quark initial states for the real corrections in [114] with exact quark mass dependence, reducing the EW uncertainty from 2% to $\sim 0.6\%$. The computation of the three-loop form-factors with full top-mass dependence was carried out by [115, 116]. However, there remains an intricate interplay between the mass effects of gg , qg and qq initial states for the real matrix elements that cannot be fully controlled due to the light quark mass effects. NLO corrections to the $h + j$ and $h + 2j$ processes were computed by [117] in the FT-approximation that uses exact born and real correction amplitudes, then approximates the two-loop virtuals by

$$|\mathcal{A}^{2\text{-loop}}(m_t, \mu_R^2)|^2 \approx |\mathcal{A}^{1\text{-loop}}(m_t \rightarrow \infty, \mu_R^2)|^2 \frac{|\mathcal{A}^{1\text{-loop}}(m_t)|^2}{|A^{(0)}(m_t) \rightarrow \infty|^2}. \quad (3.1)$$

This approximation works superbly even for $p_T \gg m_t$. Later, the full top mass effects computations have been carried out in [118, 119] using the high energy (HE) expansion technique.

3.1.2 Vector boson fusion

The VBF channel has a distinctive signature, making it a *bona fide* channel for Higgs signal extraction. The suppressed colour exchange between the quarks results in a little jet activity in the central rapidity region. The quarks will be scattered into two forward jets such that the decay products of the Higgs are found in the region between them.

¹in the heavy top limit

²Resummation implies accounting for a logarithmically enhanced subset of terms at each and every order of the perturbative series.

These features allow for excellent measurement of Higgs couplings, observation of challenging decays, and \mathcal{CP} properties determination. Some of these features are also shared with the Vh production channel. Both of these channels contain the VVh vertex that could be written generally as [99]

$$T^{\mu\nu}(p_1, p_2) = a_1 g^{\mu\nu} + a_2 \left(g^{\mu\nu} - 2 \frac{p_2^\mu p_2^\nu}{p_1 \cdot p_2} \right) + a_3 \frac{p_1^\alpha p_2^\beta}{p_1 \cdot p_2} \epsilon^{\mu\nu\alpha\beta}. \quad (3.2)$$

In the SM, only $a_1 \neq 0$, while the rest of the coefficients represent the anomalous coupling. For example, if $a_3 \neq 0$, then the Higgs is \mathcal{CP} odd. The study of the azimuthal angle distribution $d\sigma_{VBF}/d\Delta\phi_{jj}$ allows for the determination of these coefficients, with very little dependence on the higher-order perturbative corrections [120].

The NLO QCD inclusive cross-section is known since the 90's [121]. Later, these corrections were made for the differential distributions cf. [122, 123]. Unlike the ggF channel, which has an NLO K-factor of 1.6 at 13 TeV [124], the VBF NLO corrections are small $\sim 10\%$. The two-loop NNLO QCD cross-section has been computed, and the most recent results of the two-loop computation were calculated via the structure-function approach [125], in addition to STXS level 1.2 bins with EW corrections [126]. These calculation are implemented in the MC event generator **HAWK** [126–129]. Although these are small corrections, they are non-negligible, and their inclusion is important for uncertainty reduction.

3.1.3 Associated production with EW bosons

The vector boson Higgsstrahlung channels $pp \rightarrow Wh/Zh$ are at tree-level processes quark-initiated **Drell-Yan processes** [130, 131]. They have been computed up to NNLO in QCD ($\sim \alpha_s^2$), and NLO EW ($\sim \alpha^2$) [132]. Despite arising for the first time at NLO, the gluon fusion channel $gg \rightarrow Zh$ has a non-negligible contribution to the total hadronic cross-section $pp \rightarrow Zh$ that reaches up to 16% of the total cross-section contribution at 14 TeV [133], see Figure 3.2. The contribution becomes more significant when one considers the large invariant mass bins of the differential cross-section. Because at large x gluons are relatively more abundant at the LHC and the extra enhancement coming from the top quark initiated contribution near the $t\bar{t}$ threshold [134], also it has a higher scale uncertainty than the quark anti-quark annihilation $q\bar{q}A$ channel. Leading to a higher theoretical uncertainty of the Zh channel with respect to Wh , where no gluon fusion channel is present. This highlights the need to calculate the $gg \rightarrow Zh$ channel to higher orders in perturbation theory to reduce these uncertainties. The inclusion of the two-loop calculations for the ggF part is a necessary input for the a precision measurement of the Zh channel at the future LHC runs, which in terms provides better constraints on several observables, such as sign and magnitude of the top Yukawa and ZZh couplings amongst others [135].

The leading order (LO) contribution to the $gg \rightarrow Zh$ amplitude, given by one-loop diagrams, were computed in refs.[136, 137], with full quark mass dependence. For the NLO computations, the virtual corrections contain multi-scale two-loop integrals, some

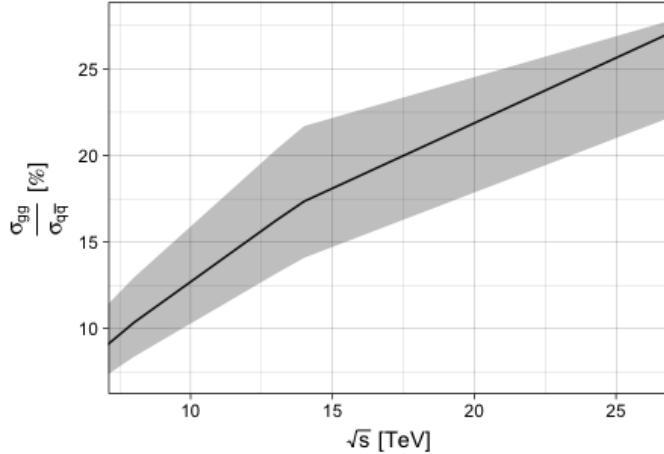


Figure 3.2. The ratio of the LO gluon fusion production cross-section $gg \rightarrow Zh$ (σ_{gg}) with respect to the NLO Drell-Yan process $q\bar{q} \rightarrow Zh$ cross-section ($\sigma_{q\bar{q}}$) at a pp collider with centre-of-mass energy \sqrt{s} . The error band captures the total theoretical uncertainties on both cross-sections dominated by σ_{gg} .

of which are still not known analytically. The first computation of the NLO terms has been accomplished by [138], using the HTL asymptotic expansion and setting $m_b = 0$. The HTL NLO computations pointed to a significant K -factor of about ~ 2 . Later, the computation was improved via soft gluon resummation, including NLL terms found in ref. [139]. Top quark mass effects were first implemented using a combination of HTL and Padé approximants [140]. A data-driven approach to extract the gluon fusion-dominated non-Drell-Yan part of Zh production using the known relation between Wh and Zh associated production has been investigated in ref. [141]. The differential distributions of $gg \rightarrow Zh$ at NLO were studied in ref. [142] via LO matrix element matching.

More recent studies of the NLO virtual corrections to this process were based on the high-energy (HE) expansion improved by Padé approximants with the LME, which extended the validity range of the HE expansion [143]. However, this expansion is only valid for in the invariant mass region $\sqrt{\hat{s}} \gtrsim 750 \text{ GeV}$ and $\sqrt{\hat{s}} \lesssim 350 \text{ GeV}$ that only covers $\sim 32\%$ of the hadronic cross-section. Furthermore, numerical computation of the two-loop virtual corrections, though implemented exactly in [144], are rather slow for practical use in MC simulations. This highlights the importance of an analytical method that can cover the remaining region of the cross-section. Fortunately, the two-loop corrections to the triangle diagrams can be computed exactly.

In this thesis, I will discuss an approach which allows for an analytic computation of the $gg \rightarrow Zh$ process, which covers 95% of the phase space. This approach is based on expansion in small Z (or Higgs) transverse momentum p_T , and was first used for Higgs pair production in [11] to compute the NLO virtual corrections to the box diagrams in the forward kinematics. While the triangle diagrams are computed exactly. This work,

by myself and my collaborators has been published in [145]. More recently, the full NLO corrections to this channel has been computed in ref. [146], including the real corrections as well.

3.1.4 Associated production with top quarks

The higher-order corrections to the $t\bar{t}h/th$ channel itself, the NLO QCD+EW effects on the off-shell multileptons final state were studied in [147]. In contrast, the NLO corrections, including SMEFT operators, were calculated in [148]. The NLO QCD+EW with Parton showering is available in all event generators. As of writing this thesis, there is no NNLO calculation of $t\bar{t}h/th$ available. However, it should be noted that the largest part of the $t\bar{t}h/th$ expected uncertainty budget comes from the theoretical modelling of this process's backgrounds, mainly $t\bar{t}b\bar{b}$, $t\bar{t}W$ as backgrounds for $t\bar{t}(h \rightarrow b\bar{b})$ and $t\bar{t}(h \rightarrow \text{multileptons})$, respectively. There have been several theoretical developments regarding these backgrounds, see for example refs. [149–157]. However, further discussion of the theoretical developments of these channels is beyond the scope of this thesis.

3.2 Concluding remarks

The precision-era of Higgs measurements requires developments on both experimental and theoretical levels. The experimental precision can be improved with higher luminosities and energies, better detectors and improved analysis techniques. Theoretical uncertainties require higher-order calculations in perturbation theory, the inclusion of mixed EW and QCD terms, the inclusion of mass effects and suitable Parton distribution functions at higher order in QCD. Much effort was and is being put into improving the theoretical predictions of Higgs production channels. Moreover, a plethora of computer tools have been made available to facilitate the computation of these cross-sections, for example `iHixs2` [158] or to generate full events, like `POWHEG` [159–165] and `MadGraph5_aMC@NLO` [166]. The LHC-Higgs working group is working group that joins the community efforts in making the best predictions available to the theory and experiment community, see their Twiki page for further details [167].

4 Virtual two-loop calculation of Zh production via gluon fusion

Higgs couplings to the weak vector bosons are approaching the precision level. For their measurements, both VBF and Vh channels are needed. The associated Higgs production with the vector bosons is crucial for measuring the VVh coupling amongst others, as discussed in subsection 3.1.3. The most notable example emphasising the importance of this channel is the measurement of the Higgs decaying to beauty quarks $h \rightarrow b\bar{b}$ by both ATLAS and CMS [168, 169]. The statistical and systematic uncertainties coming from the experimental setup of the LHC will be eventually reduced in future runs due to higher integrated luminosity, upgraded detectors and improved analysis techniques. There is an exigency to reduce theoretical uncertainties emerging from the perturbative calculations of cross-sections; to achieve that, one should include higher-order terms. As mentioned before, the Wh channel has a much smaller theoretical uncertainties than Zh due to the lack of gluon-fusion component in the former. This is due to the fact that the main source of uncertainties stems from the gluon fusion sub-process present in Zh . Higher-order corrections to the $gg \rightarrow Zh$ are essential for improving the theoretical modelling of this process.

It should be noted that the Zh channel can receive contributions from new particles [170], also as we shall see in chapter 8; particularly at the large invariant-mass region where the gluon fusion contribution becomes more important, and the HTL approximation would typically fail. Therefore, a better understanding of the SM prediction of the Zh gluon fusion channel is crucial for the SM precision measurements of Higgs production and testing NP in this channel.

This chapter aims to demonstrate the use of the p_T -expansion technique, developed in [11] as an approach for computing the two-loop virtual corrections to $gg \rightarrow Zh$ analytically, including top quark mass effects. As has been demonstrated in ref. [171], this method can be further upgraded with Padé approximants and combined with the HE expansion of [143]. This allows to describe the whole phase space analytically.

This chapter is structured as follows: section 4.1 contains the general notation that is used for the gluon fusion production Zh production calculation. Then in subsection 4.1.1, the transverse momentum expansion method is discussed. Calculation of the LO form-factors in the transverse momentum expansion is illustrated in section 4.2 as a proof of concept for this technique. The outline of the two-loop calculation is discussed in section 4.3. Finally, in section 4.4, the results of this calculation are shown with concluding remarks at the end. This chapter is based on the work that my collaborators and I have published in [145].

4.1 General notation

The amplitude $g_a^\mu(p_1)g_b^\nu(p_2) \rightarrow Z^\rho(p_3)h(p_4)$ can be written as

$$\mathcal{A} = i\sqrt{2} \frac{m_Z G_F \frac{\alpha_s^0}{4\pi}(\mu_R)}{\pi} \delta_{ab} \epsilon_\mu^a(p_1) \epsilon_\nu^b(p_2) \epsilon_\rho(p_3) \hat{\mathcal{A}}^{\mu\nu\rho}(p_1, p_2, p_3), \quad (4.1)$$

$$\hat{\mathcal{A}}^{\mu\nu\rho}(p_1, p_2, p_3) = \sum_{i=1}^6 \mathcal{P}_i^{\mu\nu\rho}(p_1, p_2, p_3) \mathcal{A}_i(\hat{s}, \hat{t}, \hat{u}, m_t, m_h, m_Z), \quad (4.2)$$

where μ_R is the renormalisation scale and $\epsilon_\mu^a(p_1) \epsilon_\nu^b(p_2) \epsilon_\rho(p_3)$ are the polarization vectors of the gluons and the Z boson, respectively. It is possible to decompose the amplitude into a maximum of six Lorentz structures encapsulated by the tensors $\mathcal{P}_i^{\mu\nu\rho}$. Due to the presence of the γ_5 , these projectors are proportional to the Levi-Civita total anti-symmetric tensor $\epsilon^{\alpha\beta\gamma\delta}$. One can choose to project the amplitude using a set of orthogonal basis, which is explicitly shown in section A.1. By this choice one obtains unique form-factors corresponding to each projector

$$\mathcal{A}_i(\hat{s}, \hat{t}, \hat{u}, m_t, m_h, m_Z), \quad (4.3)$$

that are multivariate complex functions of the top quark (m_t), Higgs (m_h) and Z (m_Z) bosons masses, and of the partonic Mandelstam variables

$$\hat{s} = (p_1 + p_2)^2, \quad \hat{t} = (p_1 + p_3)^2, \quad \hat{u} = (p_2 + p_3)^2, \quad (4.4)$$

where $\hat{s} + \hat{t} + \hat{u} = m_Z^2 + m_h^2$ and all the momenta are considered to be incoming. The form-factors \mathcal{A}_i can be perturbatively expanded in orders of α_s ,

$$\mathcal{A}_i = \sum_{k=0} \left(\frac{\alpha_s}{\pi} \right)^k \mathcal{A}_i^{(k)}. \quad (4.5)$$

Where $\mathcal{A}_i^{(0)}$ and $\mathcal{A}_i^{(1)}$ are the LO and NLO terms, respectively. Using Fermi's Golden Rule, we can write the Born Partonic cross-section as

$$\hat{\sigma}^{(0)}(\hat{s}) = \frac{m_Z^2 G_F^2 \alpha_s(\mu_R)^2}{64 \hat{s}^2 (2\pi)^3} \int_{\hat{t}^-}^{\hat{t}^+} d\hat{t} \sum_i \left| \mathcal{A}_i^{(0)} \right|^2, \quad (4.6)$$

where $\hat{t}^\pm = [-\hat{s} + m_h^2 + m_Z^2 \pm \sqrt{(\hat{s} - m_h^2 - m_Z^2)^2 - 4m_h^2 m_Z^2}] / 2$.

The LO ggF process has two sets of diagrams, the triangle, and the box, depicted in Figure 4.1. In (a), the triangle diagram contains a neutral Goldstone boson G^0 . Instead in (b), the Z boson is mediated. The interplay between these two diagram types depends on the ξ gauge. Moreover, the Z boson is strictly off-shell, due to Furry's theorem [172]. In the Landau gauge, the Z -mediated diagrams will also vanish; this can be seen by considering the sub-amplitude ggZ^* that, in the Landau gauge, can be related to the decay of a massive vector boson with mass $\sqrt{\hat{s}}$ into two massless ones.

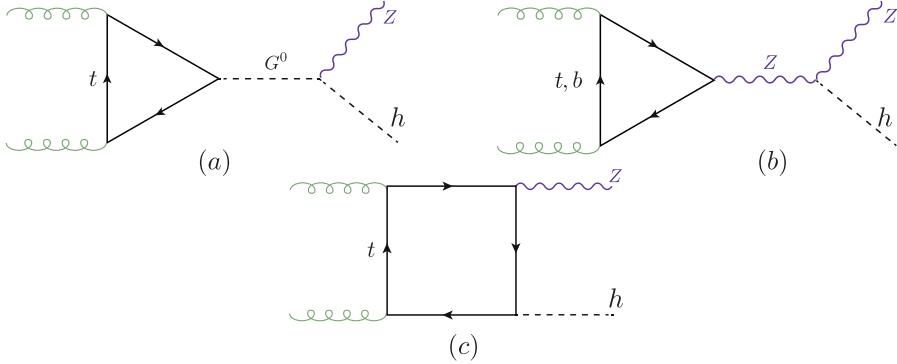


Figure 4.1. Example Feynman diagrams for the LO $gg \rightarrow Z h$ process. The triangle diagrams in a general ξ gauge involve Z and the neutral Goldstone G^0 propagators.

Such process is forbidden by the Landau-Yang theorem [173, 174]. As a consequence, the triangle diagram can be obtained from the Goldstone-mediated one, which can be adopted from the results of pseudoscalar Higgs production [175, 176]. The triangle diagrams are also proportional to the mass difference between the up- and down-type quarks. In this calculation, only the top quark is considered massive. Therefore, light quarks loops do not contribute to this process.

4.1.1 The transverse momentum expansion

Choosing to expand in small p_T of the Z boson, the first step is expressing the transverse momentum in terms of the Mandelstam variables and masses

$$p_T^2 = \frac{\hat{t}\hat{u} - m_Z^2 m_h^2}{\hat{s}}. \quad (4.7)$$

From eq.(4.7), together with the relation between the Mandelstam variables, one finds

$$p_T^2 + \frac{m_h^2 + m_Z^2}{2} \leq \frac{\hat{s}}{4} + \frac{\Delta_m^2}{\hat{s}}, \quad (4.8)$$

where $\Delta_m = (m_h^2 - m_Z^2)/2$. Eq.(4.8) implies $p_T^2/\hat{s} < 1$ that, together with the kinematical constraints $m_h^2/\hat{s} < 1$ and $m_Z^2/\hat{s} < 1$. With these relations in mind, one can expand the amplitudes in terms of small p_T^2/\hat{s} , m_h^2/\hat{s} and m_Z^2/\hat{s} , which is technically valid throughout the whole phase space, contrary to the HTL and HE limits. The caveat for this expansion is that the amplitude does not depend on p_T explicitly. Instead, one would expand in the reduced Mandelstam variables $t'/s' \ll 1$ or $u'/s' \ll 1$, defined as

$$s' = p_1 \cdot p_2 = \frac{\hat{s}}{2}, \quad t' = p_1 \cdot p_3 = \frac{\hat{t} - m_Z^2}{2}, \quad u' = p_2 \cdot p_3 = \frac{\hat{u} - m_Z^2}{2}, \quad (4.9)$$

that satisfy

$$s' + t' + u' = \Delta_m. \quad (4.10)$$

The choice of the expansion parameter t' or u' depends on whether one expands in the forward or backwards kinematics. Because the process $gg \rightarrow Zh$ has two particles in the final states with different masses, the amplitude is not symmetric under their exchange. Therefore, it is not possible to simply compute the cross-section via integrating the forward-expanded amplitude, contrary to what has been done for the Higgs pair production [11]. To overcome this issue, the amplitude can be split into symmetric and anti-symmetric parts with respect to the exchange $t' \leftrightarrow u'$, constructing directly symmetric and anti-symmetric projectors. Then, one can expand the symmetric part in the forward kinematics, like the Higgs pair case. Regarding the anti-symmetric part, the antisymmetric factor is simply extracted by multiplying the form-factors by $1/(\hat{t} - \hat{u})$. Afterwards, the expansion in the forward kinematics can be performed then the result should be multiplied back by $(\hat{t} - \hat{u})$.

In order to implement the p_T -expansion at the Feynman-diagram level, we start by splitting the momenta into longitudinal and transverse components with respect to the beam direction. This can be done by introducing the auxiliary vector [11],

$$r^\mu = p_1^\mu + p_3^\mu, \quad (4.11)$$

that satisfies

$$r^2 = \hat{t}, \quad r \cdot p_1 = \frac{\hat{t} - m_Z^2}{2}, \quad r \cdot p_2 = -\frac{\hat{t} - m_h^2}{2}, \quad (4.12)$$

and hence can be also written as

$$r^\mu = -\frac{\hat{t} - m_h^2}{\hat{s}} p_1^\mu + \frac{\hat{t} - m_Z^2}{\hat{s}} p_2^\mu + r_\perp^\mu = \frac{t'}{s'} (p_2^\mu - p_1^\mu) - \frac{\Delta_m}{s'} p_1^\mu + r_\perp^\mu, \quad (4.13)$$

where

$$r_\perp^2 = -p_T^2. \quad (4.14)$$

substituting the definition of p_T from eq.(4.7) one obtains

$$t' = -\frac{s'}{2} \left\{ 1 - \frac{\Delta_m}{s'} \pm \sqrt{\left(1 - \frac{\Delta_m}{s'}\right)^2 - 2\frac{p_T^2 + m_Z^2}{s'}} \right\}. \quad (4.15)$$

This implies that the expansion in small p_T (the minus sign case in eq.(4.15)) can be realised at the level of Feynman diagrams, by expanding the propagators in terms of the vector r^μ around $r^\mu \sim 0$ or, equivalently, $p_3^\mu \sim -p_1^\mu$, see eq.(4.13).

4.2 Born cross-section in the p_T -expansion

As a baseline test for the validity and convergence behaviour of the p_T -expansion, this method is first applied to the LO amplitude, and consequently used to compute the

Born Partonic cross-section. The results are then compared to the exact cross-section calculation found in [136, 137]. We start by defining the one-loop functions appearing in the similar calculation of the Born cross-section for $gg \rightarrow hh$ in the same expansion carried out in ref. [11]

$$B_0[\hat{s}, m_t^2, m_t^2] \equiv B_0^+, \quad B_0[-\hat{s}, m_t^2, m_t^2] \equiv B_0^-, \quad (4.16)$$

$$C_0[0, 0, \hat{s}, m_t^2, m_t^2, m_t^2] \equiv C_0^+, \quad C_0[0, 0, -\hat{s}, m_t^2, m_t^2, m_t^2] \equiv C_0^- \quad (4.17)$$

$$B_0[q^2, m_1^2, m_2^2] = \frac{1}{i\pi^2} \int \frac{d^n k}{\mu^{n-4}} \frac{1}{(k^2 - m_1^2)((k+q)^2 - m_2^2)}, \quad (4.18)$$

$$C_0[q_a^2, q_b^2, (q_a + q_b)^2, m_1^2, m_2^2, m_3^2] = \frac{1}{i\pi^2} \int \frac{d^d k}{\mu^{d-4}} \frac{1}{[k^2 - m_1^2][(k+q_a)^2 - m_2^2][(k-q_b)^2 - m_3^2]} \quad (4.19)$$

are the Passarino-Veltman functions [177], d is the spacetime dimension and μ the 't Hooft mass. The A_2 and A_6 form-factors are given in section A.2, as an example of symmetric and anti-symmetric form-factors. These form-factors are divided into triangle (\triangle) and box (\square) contributions, and B_0 functions are understood as the finite part of the integrals on the right hand side of eq.(4.18).

Using several truncations of the p_T -expansion, and comparing it to the exact LO result, one can see in Figure 4.2 the exact Born partonic LO cross-section (red line) as a function of the invariant mass of the Zh system M_{Zh} , in comparison to the p_T -expansions. For the numerical evaluation of the cross-section here and in the following section, the SM input parameters are used

$$\begin{aligned} m_Z &= 91.1876 \text{ GeV}, & m_h &= 125.1 \text{ GeV}, & m_t &= 173.21 \text{ GeV}, \\ m_b &= 0 \text{ GeV}, & G_F &= 1.16637 \text{ GeV}^{-2}, & \alpha_s(m_Z) &= 0.118. \end{aligned}$$

From the ratio plotted in the lower panel of Figure 4.2, we observe that the $\mathcal{O}(p_T^0)$ expansion is in good agreement with the exact result when $M_{Zh} \lesssim 2m_t$. Inclusion of higher-order terms up to $\mathcal{O}(p_T^6)$ extended the validity of the expansion to reach $M_{Zh} \lesssim 750$ GeV. This is the similar to what has been seen in [11] for the Higgs pair production. Therefore, one would expect the p_T -expanded two-loop virtual correction to be an accurate approximation with the exact (numerical) result for the region of the invariant mass of $M_{Zh} \sim 700 - 750$ GeV. Similar conclusions can be derived from Table 4.1, where it is shown that the partonic cross-section expanded to order $\mathcal{O}(p_T^4)$ agrees with the full result for $M_{ZH} \lesssim 600$ GeV on the per-mille level. The agreement further improves when $\mathcal{O}(p_T^6)$ terms are included.

M_{Zh} [GeV]	$\mathcal{O}(p_T^0)$	$\mathcal{O}(p_T^2)$	$\mathcal{O}(p_T^4)$	$\mathcal{O}(p_T^6)$	full
300	0.3547	0.3393	0.3373	0.3371	0.3371
350	1.9385	1.8413	1.8292	1.8279	1.8278
400	1.6990	1.5347	1.5161	1.5143	1.5142
600	0.8328	0.5653	0.5804	0.5792	0.5794
750	0.5129	0.2482	0.3129	0.2841	0.2919

Table 4.1. The partonic cross-section $\hat{\sigma}^{(0)}$ at various orders in p_T and the full computation for several values of M_{Zh} . This table has been published in [145].

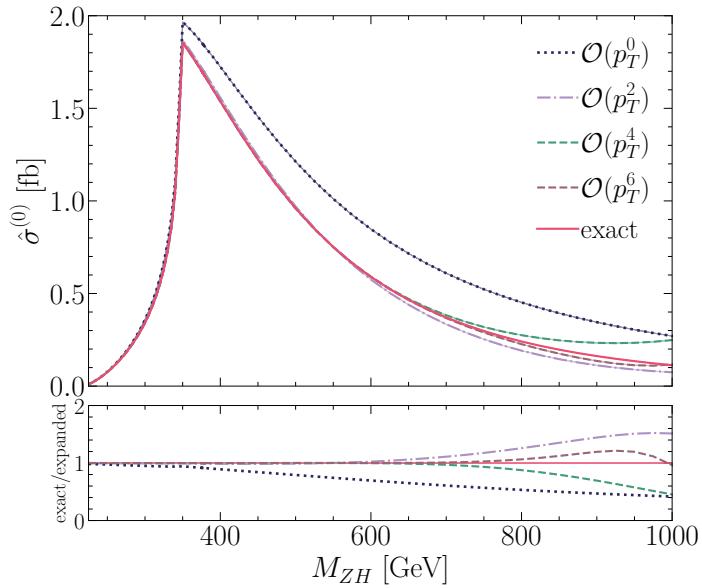


Figure 4.2. The Born partonic cross-section as a function of the invariant mass M_{Zh} . The exact result (red line) is plotted together with expansions at different orders in p_T (dashed lines). In the bottom part, the ratios of the full result over the p_T -expanded ones at various orders are shown. This plot has been published in [145].

4.3 NLO calculation

Figure 4.3 shows example Feynman diagrams for the virtual two-loop corrections to $gg \rightarrow Zh$, which involve corrections to the triangle topology in (a) and (b), corrections to the box topology in (c); also (d) shows a new topology a double triangle. Both two-loop corrections to the triangles and the double triangle diagrams can be computed analytically. The loop-integrals of the triangle contributions effectively depend on one scale only, while the double-triangles' are products of two one-loop integrals. The boxes are much more difficult as they depend on several mass scales. This makes the reduction to MI's extremely challenging. Moreover, even if that were possible, not all of the MI's will have been analytically solved thus far.

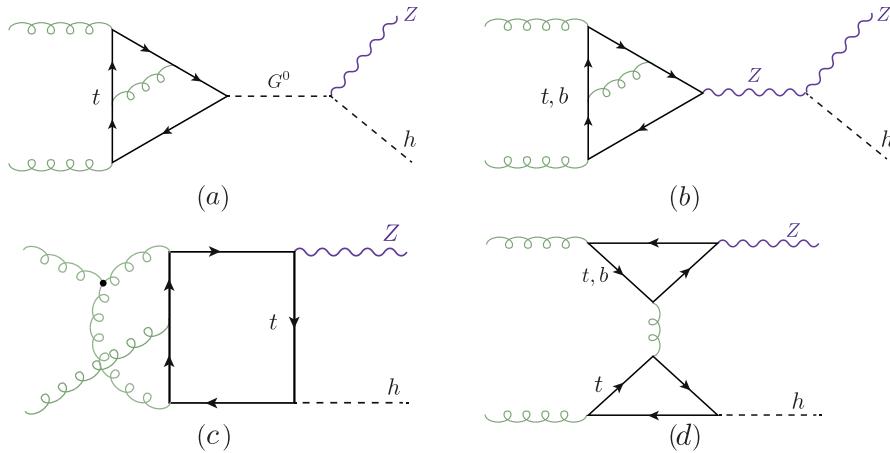


Figure 4.3. Feynman diagrams examples for the virtual NLO corrections to the $gg \rightarrow Zh$ process.

4.3.1 Renormalisation

The two-loop corrections to the triangle and box diagrams contain both UV and IR divergences. The first emerges from UV divergent sub-diagrams, such as top-quark mass renormalisation and QCD vertex correction, while the IR divergences come from massless loops. In order to remove these divergences, are needed. Instead, the double triangle topology is both UV and IR finite. The on-shell scheme for the top-quark mass renormalisation has been used, in which the bare mass is replaced by the renormalised one $m_0 = Z_m m$ in the propagators. This gives the $\overline{\text{MS}}$ renormalised mass.

$$Z_m = 1 + C_F \frac{3}{\epsilon} \quad (4.20)$$

In order to convert the mass definition to the on-shell scheme, it is possible to add the finite renormalisation term

$$Z_m^{OS} = 1 - 2C_F, \quad (4.21)$$

here $C_F = (N_c^2 - 1)/2N_c$ is one of the two Casimir invariants of QCD along with $C_A = N_c$. The $q\bar{q}g$ vertex correction involves a renormalisation of the strong couplings constant α_s , which is achieved via replacing the bare constant α_s^0 with the renormalised one, hence it becomes $\alpha_s^0 = \frac{\mu_R^{2\epsilon}}{S_\epsilon} Z_{\alpha_s} \alpha_s$, where

$$Z_{\alpha_s} = 1 - \frac{\alpha_s}{4\pi} \frac{1}{\epsilon} \left(\beta_0 - \frac{2}{3} \right) \left(\frac{\mu_R^2}{m_t^2} \right)^\epsilon, \quad (4.22)$$

and the constant $\beta_0 = \frac{11}{3}C_A - \frac{2}{3}N_f$, where N_f is the number of “active” flavours. The 5-flavour scheme $N_f = 5$ is adopted here. This is only done for the triangle diagrams, as for the boxes the background field gauge was used, which renders the renormalisation of α_s unnecessary.

The loop integrals were evaluated using dimensional regularisation in $d = 4 - 2\epsilon$ dimensions. This scheme requires some caution when γ_5 is present in the amplitude. The approach followed in this calculation is letting γ_5 naively anti-commute with all d -dimensional γ_μ ’s, and then correct that with the finite renormalisation constant known as **Larin counter-term** [178]

$$Z_5 = 1 - 2C_F. \quad (4.23)$$

The renormalised amplitude is written as

$$\mathcal{M}(\alpha_s, m, \mu_R) = Z_A \mathcal{M}(\alpha_s^0, m^0). \quad (4.24)$$

Putting all the above substitutions together, we get the renormalised two-loop form-factor:

$$(\mathcal{A}^{(1)})^R = \mathcal{A}^{(1)} - \mathcal{A}_{UV}^{(0)} - \mathcal{A}_{UV,m}^{(0)} + \mathcal{A}_{\text{Larin}}^{(0)} \quad (4.25)$$

$$\begin{aligned} \mathcal{A}_{UV}^{(0)} &= \frac{\alpha_s}{4\pi} \frac{\beta_0}{\epsilon} \left(\frac{\mu_R^2}{\hat{s}} \right)^{-\epsilon} \mathcal{A}^{(0)}. \\ \mathcal{A}_{UV,m}^{(0)} &= \frac{\alpha_s}{4\pi} \left(\frac{3}{\epsilon} - 2 \right) C_F \left(\frac{\mu_R^2}{\hat{s}} \right)^{-\epsilon} m^0 \partial_m \mathcal{A}^{(0)}. \end{aligned} \quad (4.26)$$

$$\mathcal{A}_{\text{Larin}}^{(0)} = -\frac{\alpha_s}{4\pi} C_F \mathcal{A}^{(0)}.$$

The following IR-counter-term is used in order to cancel the IR divergences

$$\mathcal{A}_{IR}^{(0)} = \frac{e^{\gamma_E \epsilon}}{\Gamma(1-\epsilon)} \frac{\alpha_s}{4\pi} \left(\frac{\beta_0}{\epsilon} + \frac{C_A}{\epsilon^2} \right) \left(\frac{\mu_R^2}{\hat{s}} \right)^{2\epsilon} \mathcal{A}^{(0)}. \quad (4.27)$$

The one-loop form-factors, need to be expanded up to order $\mathcal{O}(\epsilon^2)$, for the UV and IR counter-terms.

4.3.2 Calculation of the exact virtual corrections

The two-loop calculations of the triangle diagrams involves the diagrams with Z^* and G^0 propagators, depending on the gauge of choice. Observations found in ref. [138] shows that due to Landau-Yang theorem in the Landau gauge, all diagrams with the Z^* exchange vanish. Therefore, the part of the top triangle diagrams can be obtained from the decay amplitude of a pseudoscalar boson into two gluons that is known in the literature in the full mass dependence up to NLO terms [175, 176]. On the contrary, using the unitary gauge, the NLO calculation needs to be done with the Z^* exchange diagrams only. The calculations in these two gauges result in apparently different Lorentz structures that are linked via the Schouten identity

$$q^\alpha \epsilon^{\beta\gamma\delta\phi} + q^\beta \epsilon^{\gamma\delta\phi\alpha} + q^\gamma \epsilon^{\delta\phi\alpha\beta} + q^\gamma \epsilon^{\delta\phi\alpha\beta} + q^\delta \epsilon^{\phi\alpha\beta\gamma} + q^\phi \epsilon^{\alpha\beta\gamma\delta} = 0. \quad (4.28)$$

A cross-check has been preformed in order to ensure that the NLO calculation introduces no new Lorentz structures, and gives the same result in a general R_ξ gauge as the results in [175, 176]. The two-loop calculation has been carried out in the R_ξ gauge. The amplitudes have been automatically generated by **FeynArts** [179] and contracted with the projectors as defined in section A.1 using **FeynCalc** [180, 181] and **Package x** [182] and in-house Mathematica routines. The two-loop integrals were reduced to a set of master integrals MI, illustrated graphically in Figure 4.4 using **Kira** [183]. These MI's are either products of one-loop functions (a)-(c), (e),(f),(h) and (l) or can be found in the literature [176, 184]. Their implementation in this calculation has been validated numerically using **SecDec** [185, 186].

The virtual correction for the triangle diagrams can be separated according to their colour factors into

$$\mathcal{A}^{(1)} = C_F \mathcal{A}_{CF}^{(1)} + C_A \mathcal{A}_{CA}^{(1)}, \quad (4.29)$$

The C_A part contains a double pole $\mathcal{O}(1/\epsilon^2)$ and a single pole $\mathcal{O}(1/\epsilon)$. Whilst the C_F part only contains a UV divergent single pole, which needs to be cancelled via mass and vertex renormalisation. The poles do not have a dependence on the renormalisation scale μ_R . However, there is a dependence on that scale in the finite part, as well. No new Lorentz structures appears, and the final result in R_ξ matched the one found in [175, 176] for the Landau gauge. The explicit results are shown in Appendix B

The calculation of the double triangle diagrams (d) of Figure 4.3 is fairly straightforward, all of the integrals can be rewritten in terms of products of one-loop functions. All of the Lorentz structures appear in the double triangle except for \mathcal{P}_6 , analogous to the triangle case. The explicit forms of form-factors corresponding to these structures is presented in Appendix B. Although in this calculation, the amplitude has been written using a different tensorial structure compared to ref. [143]. It was checked, using the relations between the two tensorial structures reported in section A.1 that the result obtained here is in agreement with the one presented in ref. [140].

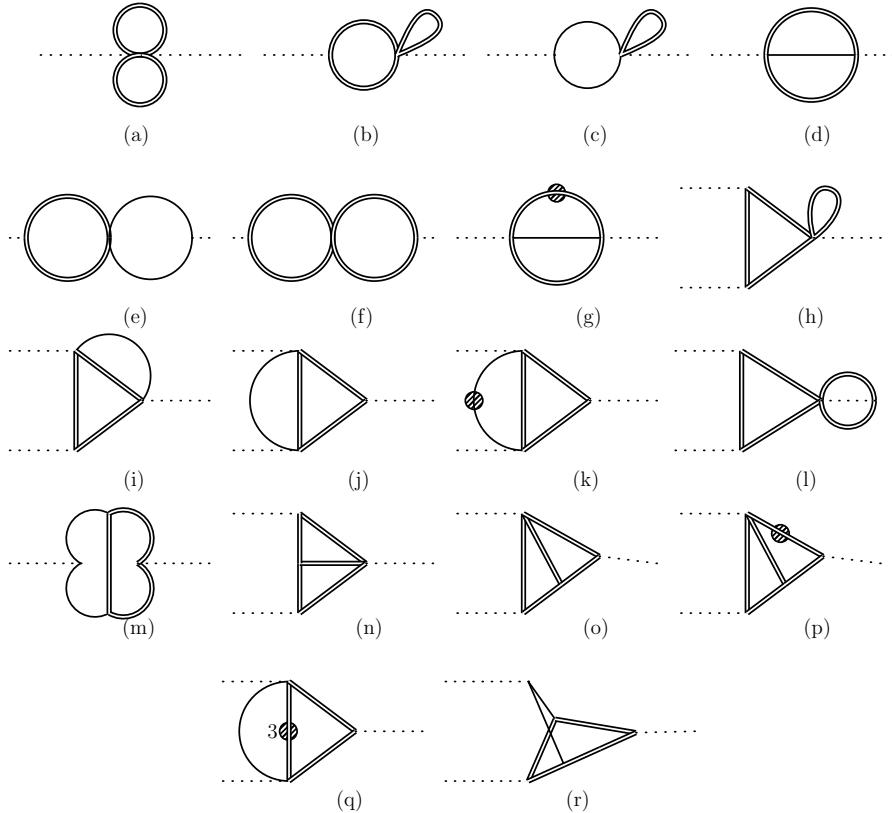


Figure 4.4. The list of two-loop master integrals (MI's) resulting from the reduction of the two-loop triangle corrections. The product of one-loop MI's appearing in this list also appear in the calculation of the double-triangle diagrams. A single line denotes a massless propagator, while a double line denotes a massive one. The dot denotes a squared propagator unless the number of the exponent is indicated.

4.3.3 Calculation of the p_T -expanded virtual corrections

The two-loop triangle diagrams can also be interpreted as an expansion in p_T , but this expansion terminates at $\mathcal{O}(p_T^2)$, rather than being an infinite series. Hence, in this section, we concentrate on the two-loop box diagrams p_T -expansion¹.

Like the two-loop triangle diagrams, the box diagrams amplitudes were generated and projected through the same pipeline. After the contraction of the epsilon tensors, the diagrams were expanded as described in subsection 4.1.1, keeping only $\mathcal{O}(p_T^4)$ terms. They were reduced to MI's using FIRE [187] and LiteRed [188]. The resulting MI's were identical to those for Higgs pair production [11]. Nearly all of them are expressed in terms of generalised harmonic polylogarithms, except for two elliptic integrals [189, 190]. The renormalisation and IR pole subtraction procedure was carried out as prescribed subsection 4.3.1. Furthermore, the treatment of γ_5 was cross-checked with a Pauli-Villar regulator in the HTL.

The two-loop box diagrams were also computed in the HTL up to $\mathcal{O}(1/m_t^6)$. These results were confronted with the p_T -expanded are after expanding them in small \hat{s}/m_t^2 , providing a cross-check of the expansion.

4.4 Results and conclusions

The virtual corrections to the ggF $Z h$ production have been implemented in a FORTRAN code using `handyG` [191], for the evaluation of generalised harmonic polylogarithms and `Chaplin` [192] for the harmonic polylogarithms appearing in the triangle two-loop functions. On the other hand, the elliptic integrals are evaluated using the routines developed in ref. [190]. Since the result is analytic, the code is significantly faster than the numerical evaluation of the two-loop amplitude [144], with evaluation time of ca. 0.1 sec per one phase space point on a personal laptop.

In order to facilitate the comparison of these results with the ones presented in the literature, we define the finite part of the virtual corrections as in ref. [143]²

$$\begin{aligned} \mathcal{V}_{fin} = & \frac{G_F^2 m_Z^2}{16} \left(\frac{\alpha_s}{\pi} \right)^2 \left[\sum_i |\mathcal{A}_i^{(0)}|^2 \frac{C_A}{2} \left(\pi^2 - \log^2 \left(\frac{\mu_R^2}{\hat{s}} \right) \right) \right. \\ & \left. + 2 \sum_i \operatorname{Re} \left[\mathcal{A}_i^{(0)} \left(\mathcal{A}_i^{(1)} \right)^* \right] \right], \end{aligned} \quad (4.30)$$

and in the numerical evaluation of eq.(4.30) is fixed $\mu_R = \sqrt{\hat{s}}$. The triangle and HTL box topologies were validated against the results of refs. [140, 143] finding perfect agreement at the form-factor level, i.e. $\mathcal{A}_i^{(1)}$. The finite virtual part of the partonic cross-section

¹The calculation of the box diagrams has been done by my collaborators, the co-authors of [145].

²The definition of the matrix elements here differs by a factor of $\frac{1}{\hat{s}}$ from ref. [143], cf. also section A.1.

\hat{s}/m_t^2	\hat{t}/m_t^2	ref.[144]	$\mathcal{O}(p_T^6)$
1.707133657190554	-0.441203767016323	35.429092(6)	35.430479
3.876056604162662	-1.616287256345735	4339.045(1)	4340.754
4.130574250302561	-1.750372271104745	6912.361(3)	6915.797
4.130574250302561	-2.595461551488002	6981.09(2)	6984.20

Table 4.2. Comparison of $\mathcal{V}_{fin}4/(\alpha_s^2 \alpha^2)$ with the numerical results of ref. [144]. This table has been published in [145].

in eq. (4.30) is defined by

$$\Delta\hat{\sigma}_{virt} = \int_{\hat{t}^-}^{\hat{t}^+} d\hat{t} \frac{\alpha_s}{16\pi^2} \frac{1}{\hat{s}^2} \mathcal{V}_{fin}. \quad (4.31)$$

This function is used to compare the p_T -expanded results with the other expansion methods. Starting with low M_{Zh} , the p_T -expanded is compared with the HTL \mathcal{V}_{fin} , finding an excellent numerical agreement. It is important to note that, at the same order in the expansion, the p_T -expanded terms are more accurate than the HTL ones, albeit computationally more demanding. Additional checks have been done using the numerical evaluation of the NLO amplitude by [144], where the authors have evaluated the exact two-loop MI's using `pySecDec` [193, 194]. Table 4.2 shows a comparison between the p_T -expanded $\mathcal{V}_{fin}4/(\frac{\alpha_s^0}{4\pi} \alpha^2)$ vs the exact numerical result of [144] for several phase space points. As can be seen from the table the relative difference between the two results is less than half a per-mille.

In Figure 4.5, the dashed lines show the different orders of the expansion in p_T . For all parts of the matrix elements, the best results available were used. The triangle and double-triangle topologies were evaluated exactly, while the boxes various orders in the p_T -expansion were used. For comparison, the results are shown where $\mathcal{A}^{(1)}$ is replaced by the one computed in HTL up to $\mathcal{O}(1/m_t^6)$ (full black line), which, is valid up to $M_{Zh} < 2m_t$. Within the validity of the HTL, the p_T -expanded results agree well with it. Furthermore, the results in the infinite top mass limit reweighted by the full amplitudes squared can be seen as the full red line in the plot, corresponding to the approach of ref.[138], keeping though the double triangle contribution in full top mass dependence. Differently from the HTL line, the $m_t \rightarrow \infty$ reweighted one shows a behaviour, for $M_{Zh} \gtrsim 400$ GeV, similar to the behaviour of the p_T lines. Still, the difference between the reweighted result and the p_T -expanded ones is significant. The p_T -expanded results show very good convergence. The zero-order in term of the p_T -expansion agrees exceptionally well with the higher orders, and all the three results are very close up to $M_{Zh} \sim 500$ GeV.

In conclusion, we have shown that the p_T -expansion can be applied to a very good accuracy to $gg \rightarrow Zh$. The same MI's that were found for Higgs pair production [11] also appear in the Zh virtual corrections. Predominantly, these MI's are expressed in

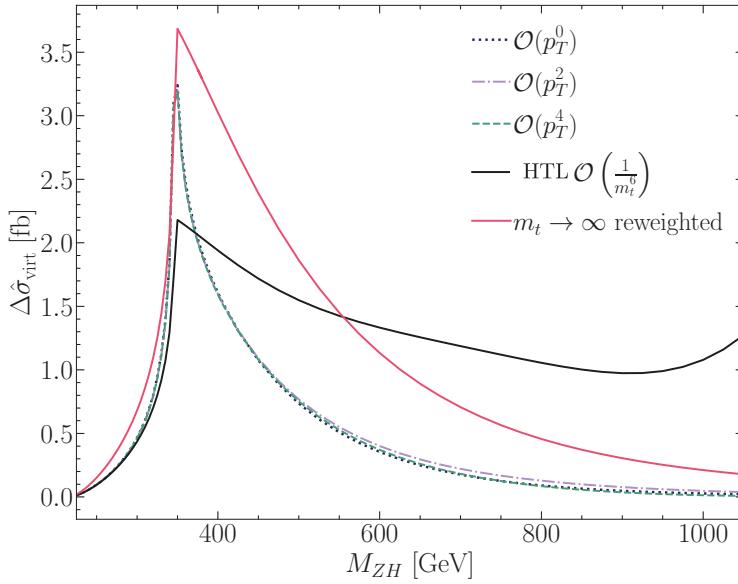


Figure 4.5. $\Delta\hat{\sigma}_{\text{virt}}$ defined by eq. (4.31), shown as a function of M_{Zh} . The various orders of the p_T -expansion are plotted as dashed lines, while the black and red continuous lines stand for the HTL and reweighted $m_t \rightarrow \infty$ results, respectively. This plot has been published in [145].

terms of generalised harmonic polylogarithms except two elliptic integrals. Using the LO calculation, we have shown the validity of the p_T -expansion covering the invariant mass interval $M_{Zh} \lesssim 750$ GeV, which covers $\sim 98\%$ of the total phase space for 13 – 14 TeV energies.

The p_T -expansion agrees within per mill level accuracy with the numerical results found in [144]. However, it allows for fast amplitude computation with less than 0.1 second per phase space point using a modern laptop with mid-range specifications. Furthermore, the integration over the \hat{t} variable in eq.(4.31) converges superbly. With the flexibility of these analytic results, an application to the beyond-the SM is certainly possible.

Finally, it should be noted that this calculation complements nicely the results obtained in ref. [143] using a HE expansion, which according to the authors, provides precise results for $p_T \gtrsim 200$ GeV. The merging of the two analyses provided a result that covers the whole phase space, and can be easily implemented into a Monte Carlo code. A combination of the two expansions for the virtual corrections has been published in [171].

5 Four top operators in Higgs production and decay

In chapter 2, the SMEFT has been portrayed as a pragmatic yet robust parametrisation of potential NP degrees of freedom for LHC searches assuming that these degrees of freedom have masses that are higher than the LHC reach. From the discussion and overview of Higgs-related SMEFT operators in that chapter, the operator \mathcal{O}_ϕ stood out as one of the weakly constrained among them. This is due to the current low experimental sensitivity on the Higgs self-couplings.

Though many of the top quark operators are strongly constrained from top quark production observables, some remain as weakly constrained as the trilinear Higgs self-coupling, particularly four-fermion operators involving the third generation quarks. They would be constrained directly from the production of four top quarks or $t\bar{t}b\bar{b}$ observation. However, the four top quark production process has a small cross-section at the LHC $\sim 12 \text{ fb}$ [195], which is more or less comparable to Higgs pair production. Experimental searches for the production of four top quarks have been first done by CMS [196] combining different LHC runs, followed by ATLAS [197], the latter reporting a 4.3σ observation of this processes with a cross-section of 24^{+7}_{-6} fb . The same story can be told for the observation of $t\bar{t}b\bar{b}$ production, see [198, 199] for experimental searches and [200, 201] for SMEFT fits. It should be noted that for the production of four top quarks, or two top, two beauty quarks in SMEFT, that the contact terms do not interfere with the SM process and only appear proportional to $\mathcal{O}(1/\Lambda^4)$. This makes the SMEFT global analysis of these operators highly dependent on the EFT truncation scheme used, i.e. whether to keep quadratic terms or not.

Intriguingly, these four-fermion operators enter in single Higgs processes at NLO similarly to the Higgs self-coupling. Since the four-fermions operators are weakly constrained, they should be included in fits that include Higgs data. In this chapter, I shall demonstrate a significant correlation between the Higgs self-coupling and the four-fermion operators.

The chapter is based on the paper [202] and structured as follows: in section 5.1 the complete NLO calculation of Higgs rates due to the four-fermion operators is shown. Afterwards, in section 5.2, a fit from single-Higgs data combining the Higgs trilinear coupling and the four-fermion operators is presented for both Run-II and HL-LHC,. More elaborate results for the HL-LHC are found in Appendix B. The results are further discussed in section 5.3.

5.1 Contribution of four-fermion operators to Higgs rates at NLO

We will consider the following dimension-six SMEFT operators:

Four-heavy-quark SMEFT operators modifying Higgs rates at NLO

Operators with homogenous chiral structure, i.e. (RR)(RR) or (LL)(LL)

$$\mathcal{O}_{tt}, \mathcal{O}_{bb}, \mathcal{O}_{tb}^{(1)}, \mathcal{O}_{tb}^{(8)}, \mathcal{O}_{QQ}^{(1)}, \mathcal{O}_{QQ}^{(3)}. \quad (5.1)$$

Operators with heterogeneous chiral structure, i.e. (LR)(LR) or (LL)(RR)

$$\mathcal{O}_{Qt}^{(1)}, \mathcal{O}_{Qt}^{(8)}, \mathcal{O}_{Qb}^{(1)}, \mathcal{O}_{Qb}^{(8)}, \mathcal{O}_{QtQb}^{(1)}, \mathcal{O}_{QtQb}^{(8)}. \quad (5.2)$$

The explicit definition of these operators can be found in [Table 2.1](#). Here, the notation is slightly modified from the standard Warsaw basis. The flavour indices were suppressed since only the third generation is considered throughout this chapter. Adopting the same notation from previous chapters, Q denotes the (heavy) left-handed $SU(2)_L$ doublet quarks while t and b refer to the right-handed singlets. In studies involving SMEFT fits, such as [89] the $SU(3)_C$ singlet and octet left-handed operators $\mathcal{O}_{QQ}^{(1),SU(3)}$, $\mathcal{O}_{QQ}^{(8)}$ are often used instead of the singlet and triplet of $SU(2)_L$ appearing in the standard Warsaw basis. The two conventions are related via the relations

$$\begin{aligned} C_{QQ}^{(1),SU(3)} &= 2C_{QQ}^{(1)} - \frac{2}{3}C_{QQ}^{(3)}, \\ C_{QQ}^{(8)} &= 8C_{QQ}^{(3)}. \end{aligned} \quad (5.3)$$

Additionally, all of these Wilson coefficients are assumed to be real.

The operators considered here are the ones that induce sizeable NLO corrections to Higgs processes. These operators turn out to be the ones that introduce loop corrections to the top- or beauty-quark Yukawa, their masses and finite corrections from top-quark loops; therefore these corrections are proportional to the top mass. On the contrary, corrections from only beauty-quark loops are highly suppressed by m_b . Also, operators with a chiral structure that do not enable them to enter the Yukawa RGE's will not give strong constraints from Higgs data as they would only contribute through small finite terms, as we shall see later. Hence, only four-top-quark and the $\mathcal{O}_{QtQb}^{(1),(8)}$ operators will be considered. The argument on the chiral structures is general and also excludes \mathcal{O}_{tt} and \mathcal{O}_{QQ} in principle.

In this section, I will present the calculation of NLO Higgs production and decay rates induced by the four heavy-quarks operators as discussed above. The results were computed fully analytically of Higgs production via gluon fusion and Higgs decay to gluon, photons and beauty quarks, while for the associated production of the Higgs with top pair $t\bar{t}h$, the corrections were computed numerically due to the length of the expressions of the result.

5.1.1 Analytic calculations

The NLO corrections to gluon fusion, $h \rightarrow gg$, $h \rightarrow \gamma\gamma$ and $h \rightarrow b\bar{b}$ all come from the sub-diagrams listed in [Table 5.1](#), with top loops entering in the mass renormalisation or top- or beauty-quark Yukawa vertex correction. In this table, $N_c = 3$ is the number of colours, and $c_F = (N_c^2 - 1)/(2N_c) = 4/3$ are the eigenvalues of the Casimir operator of $SU(3)_c$ in the fundamental representation. The effect of the beauty-quark loops

Diagram	colour factor		mass/coupling
	singlet	octet	
	$2N_c + 1$	c_F	$y_t m_b m_t^2$
	1	c_F	$y_t m_t^3$
	$2N_c + 1$	c_F	m_t^3
	1	c_F	m_t^3

Table 5.1. Sub-diagrams contributing to the NLO corrections of gluon fusion Higgs production and its decay to gluons, photons and beauty quarks.

coming from $C_{QtQb}^{(1/8)}$ can be easily read from this table by exchanging $t \leftrightarrow b$, although such corrections are significantly smaller than their counterparts coming from top-quark loops.

We see that these corrections correspond to the Wilson coefficients appearing in the RGE, and operators with (LL)(LL) or (RR)(RR) chiral structures do not contribute to these processes. Confronting the Feynman diagram of [Figure 5.1](#) with the subgraphs of [Table 5.1](#), we see that all of the Feynman diagrams contain the subgraphs of the table. The only exception is diagram (e), which though vanishes if the gluons are on-shell. Following the Feynman rules derived in ref. [203] for the four-fermion operators of interest here, the $gg \rightarrow h$ two-loop amplitude was calculated, then Dirac algebra and further algebraic manipulations were performed in Mathematica using `PackageX` [204]. Reduction of the resulting two-loop loop integrals to Master integrals has been preformed using `KIRA` [205]. The computation has been cross-checked independently by my collab-

orators, using a different pipeline: **FeynRules** [206] for constructing the model, followed by **FeynArts** [179] for amplitude generation then **PackageX** and **Fire** [207] for algebraic manipulation and loop-integral reduction, respectively.

The sub-diagrams appearing in the two-loop calculation correspond to mass and vertex renormalisation, which require counter-terms for pole cancellation. A mixture of on-shell (OS) and $\overline{\text{MS}}$ – schemes have been used for the mass and $hq\bar{q}$ coupling renormalisation, respectively. The renormalisation of SM quantities is done in the OS scheme, while the NP parameters are renormalised according to the $\overline{\text{MS}}$ scheme. This method of mixed-scheme renormalisation was proposed by [208].

The top/beauty mass renormalisation can be expressed as

$$m_{t/b}^{\text{OS}} = m_{t/b}^{(0)} - \delta m_{t/b}, \quad (5.4)$$

with the corresponding counter-terms

$$\delta m_t = \frac{1}{8\pi^2} \frac{C_{Qt}^{(1)} + c_F C_{Qt}^{(8)}}{\Lambda^2} m_t^3 \left[\frac{2}{\bar{\epsilon}} + 2 \log \left(\frac{\mu_R^2}{m_t^2} \right) + 1 \right] \quad (5.5)$$

$$- \frac{1}{16\pi^2} \frac{(2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \left[\frac{1}{\bar{\epsilon}} + \log \left(\frac{\mu_R^2}{m_b^2} \right) + 1 \right] m_b^3,$$

$$\delta m_b = - \frac{1}{16\pi^2} \frac{(2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \left[\frac{1}{\bar{\epsilon}} + \log \left(\frac{\mu_R^2}{m_t^2} \right) + 1 \right] m_t^3. \quad (5.6)$$

Here, we have $\bar{\epsilon}^{-1} = \epsilon^{-1} - \gamma_E + \log(4\pi)$, in dimensional regularisation in $d = 4 - 2\epsilon$ dimensions. It is possible to convert from OS to the $\overline{\text{MS}}$ – scheme for mass counter-terms via the following relations

$$\delta m_t^{\overline{\text{MS}}} = \frac{1}{8\pi^2} \frac{C_{Qt}^{(1)} + c_F C_{Qt}^{(8)}}{\Lambda^2} m_t^3 \frac{1}{\bar{\epsilon}} + \frac{1}{16\pi^2} \frac{(2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \frac{1}{\bar{\epsilon}} m_b^3, \quad (5.7)$$

$$\delta m_b^{\overline{\text{MS}}} = \frac{1}{16\pi^2} \frac{(2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \frac{1}{\bar{\epsilon}} m_t^3. \quad (5.8)$$

Changing from OS to the $\overline{\text{MS}}$ scheme results in a small effect for the top quark but in a significant one, up to 100% effect, for the beauty. The top/beauty Higgs coupling in SMEFT, is written as

$$g_{ht\bar{t}/hb\bar{b}} = \frac{m_{t/b}}{v} - \frac{v^2}{\Lambda^2} \frac{C_{t\phi/b\phi}}{\sqrt{2}}. \quad (5.9)$$

A modification of the Higgs couplings to beauty and top quarks is generated by operator mixing even if $C_{t\phi/b\phi}$ is set to zero, as the considered four-fermion operators enter in the

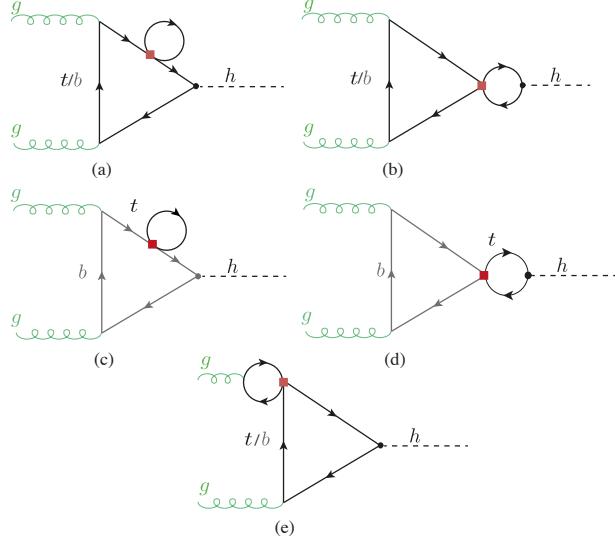


Figure 5.1. Example Feynman diagrams for the four-fermion-operator contributions to the Higgs production via gluon fusion. The red box indicates the four-fermion operator.

RGE's of $C_{t\phi/b\phi}$.

$$\delta g_{h\bar{t}t/h\bar{b}b} = \frac{m_{t/b}}{v} \delta m_{t/b} - \frac{v^2 \delta C_{t\phi/b\phi}}{\sqrt{2}}, \quad (5.10)$$

where $\delta C_{t\phi/b\phi}$ is directly read from the anomalous dimension [87]

$$\begin{aligned} \mu \frac{dC_{t\phi}}{d\mu} = & \frac{m_t^2}{16\pi^2 v^2} \left(2N_c C_{t\phi} - 2 \left(C_{\phi Q}^{(1)} + (3 - 4N_c) C_{\phi Q}^{(3)} \right) y_t + 2C_{\phi t} y_t + C_{\phi t} y_t \right. \\ & \left. + 8 \left(C_{Qt}^{(1)} + \langle C_F \rangle C_{Qt}^{(8)} \right) y_t \right), \end{aligned} \quad (5.11)$$

and for the beauty quark

$$\mu \frac{dC_{b\phi}}{d\mu} = \frac{m_t^2}{16\pi^2 v^2} \left(-2 \left((2N_c + 1) C_{QtQb}^{(1)*} + \langle C_F \rangle C_{QtQb}^{(8)*} \right) y_t \right), \quad (5.12)$$

Correction to gluon fusion and $h \rightarrow gg$

The modification of the Higgs production via gluon fusion can be written as

$$\frac{\sigma_{ggF}}{\sigma_{ggF}^{\text{SM}}} = 1 + \frac{\sum_{i=t,b} 2\text{Re}(F_{\text{LO}}^i F_{\text{NLO}}^*)}{|F_{\text{LO}}^t + F_{\text{LO}}^b|^2}, \quad (5.13)$$

with

$$F_{\text{LO}}^i = -\frac{8m_i^2}{m_h^2} \left[1 - \frac{1}{4} \log^2(x_i) \left(1 - \frac{4m_i^2}{m_h^2} \right) \right], \quad (5.14)$$

and the NLO form-factors are given by

$$\begin{aligned} F_{\text{NLO}} = & \frac{1}{4\pi^2\Lambda^2} (C_{Qt}^{(1)} + c_F C_{Qt}^{(8)}) F_{\text{LO}}^t \left[2m_t^2 + \frac{1}{4}(m_h^2 - 4m_t^2) \left(3 + 2\sqrt{1 - \frac{4m_t^2}{m_h^2}} \log(x_t) \right) \right. \\ & \left. + \frac{1}{2}(m_h^2 - 4m_t^2) \log \left(\frac{\mu_R^2}{m_t^2} \right) \right] \\ & + \frac{1}{32\pi^2\Lambda^2} ((2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}) \left[F_{\text{LO}}^b \frac{m_t}{m_b} (4m_t^2 - 2m_h^2) \right. \\ & \left. - (m_h^2 - 4m_t^2) \sqrt{1 - \frac{4m_t^2}{m_h^2}} \log(x_t) - (m_h^2 - 4m_t^2) \log \left(\frac{\mu_R^2}{m_t^2} \right) \right] + (t \leftrightarrow b) \end{aligned} . \quad (5.15)$$

Only top-quark loops contribute to the parts proportional to $C_{Qt}^{(1),(8)}$. The variable x_i for a loop particle with mass m_i is given by

$$x_i = \frac{-1 + \sqrt{1 - \frac{4m_i^2}{m_h^2}}}{1 + \sqrt{1 - \frac{4m_i^2}{m_h^2}}}. \quad (5.16)$$

Using the same amplitudes, the $h \rightarrow gg$ partial width modification can be written as

$$\frac{\Gamma_{h \rightarrow gg}}{\Gamma_{h \rightarrow gg}^{\text{SM}}} = 1 + \frac{\sum_{i=t,b} 2\text{Re}(F_{\text{LO}}^i F_{\text{NLO}}^*)}{|F_{\text{LO}}^t + F_{\text{LO}}^b|^2}. \quad (5.17)$$

Correction to Higgs decay to photons

Since the decay $h \rightarrow \gamma\gamma$ contains the same topologies as gluon fusion, it is possible to use the results from the above calculation in obtaining the NLO correction to the partial width for this decay

$$\frac{\Gamma_{h \rightarrow \gamma\gamma}}{\Gamma_{h \rightarrow \gamma\gamma}^{\text{SM}}} = 1 + \frac{2\text{Re}(F_{\text{LO},\gamma} F_{\text{NLO},\gamma}^*)}{|F_{\text{LO},\gamma}|^2}. \quad (5.18)$$

However, one should pay attention to the change in the prefactors, and the extra EW contributions for $h \rightarrow \gamma\gamma$

$$F_{\text{LO},\gamma} = N_C Q_t^2 F_{\text{LO}}^t + N_C Q_b^2 F_{\text{LO}}^b + F_{\text{LO}}^W + F_{\text{LO}}^G, \quad (5.19)$$

and $F_{\text{NLO},\gamma}$ is obtained from F_{NLO} by replacing the LO form-factor that appears inside of it by $F_{\text{LO}}^i \rightarrow N_C Q_i^2 F_{\text{LO}}^i$. The charges of the top and beauty quarks are $Q_t = 2/3$ and $Q_b = -1/3$, respectively.

The W -boson loops contribution is given by

$$F_{\text{LO}}^W = 2 \left(1 + 6 \frac{m_W^2}{m_h^2} \right) - 6 \frac{m_W^2}{m_h^2} \left(1 - 2 \frac{m_W^2}{m_h^2} \right) \log^2(x_W), \quad (5.20)$$

and the Goldstone contribution by

$$F_{\text{LO}}^G = 4 \frac{m_W^2}{m_h^2} \left(1 + \frac{m_W^2}{m_h^2} \log^2(x_W) \right). \quad (5.21)$$

These operators also affect the $h \rightarrow Z\gamma$ partial width. However, as in the diphoton case, the effect is rather small due to the dominance of the W -boson contributions. Furthermore, given the smallness of the $h \rightarrow Z\gamma$ branching ratio and the relatively low precision expected in probing this channel at the LHC, the effects of four-fermion interactions in the $h \rightarrow Z\gamma$ decay are neglected in this study.

Correction to Higgs decays to $b\bar{b}$

The dominant four-fermion contributions to decay channel $h \rightarrow b\bar{b}$ come from the operators $\mathcal{O}_{QtQb}^{(1),(8)}$; the corresponding diagram at NLO is shown in fig 5.2. Adopting the same renormalisation procedure as described earlier, we have the following expression for the correction to the $h \rightarrow b\bar{b}$ decay rate in the presence of $\mathcal{O}_{QtQb}^{(1),(8)}$

$$\begin{aligned} \frac{\Gamma_{h \rightarrow b\bar{b}}}{\Gamma_{h \rightarrow b\bar{b}}^{\text{SM}}} &= 1 + \frac{1}{16\pi^2} \frac{m_t}{m_b} (m_h^2 - 4m_t^2) \frac{(2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}}{\Lambda^2} \\ &\times \left[2 + \sqrt{1 - \frac{4m_t^2}{m_h^2} \log(x_t)} - \log\left(\frac{m_t^2}{\mu_R^2}\right) \right]. \end{aligned} \quad (5.22)$$

This NLO correction carries an enhancement factor of m_t/m_b and is hence expected to be rather large. The expression in (5.22) agrees with results obtained from the full

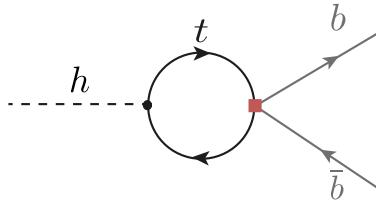


Figure 5.2. Feynman diagram contributing to the NLO $h \rightarrow b\bar{b}$ process.

calculation of the NLO effects in the dimension-six SMEFT, computed in ref. [209].

The results of the NLO effects from the four-fermion operators reported for the three channels above do not take into account the running of the Wilson coefficients. This

would be based on assuming that these coefficients are defined at the process scale. Nevertheless, when we want to compare different processes or assume that the four-fermion operators are defined at the UV scale Λ , one has to consider the running of these Wilson coefficients from Λ down to the process scale.

These running effects can be included via the RGE for the operators with Wilson coefficient $C_{t\phi}$ and $C_{b\phi}$ [85, 86], that leads approximatively to

$$C_{t\phi}(\mu_R) - C_{t\phi}(\Lambda) = \frac{1}{16\pi^2 v^2} \left[-2y_t(m_h^2 - 4m_t^2)(C_{Qt}^{(1)} + c_F C_{Qt}^{(8)}) \log\left(\frac{\mu_R^2}{\Lambda^2}\right) + \frac{y_b}{2}(m_h^2 - 4m_b^2) ((2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}) \log\left(\frac{\mu_R^2}{\Lambda^2}\right) \right], \quad (5.23)$$

and

$$C_{b\phi}(\mu_R) - C_{b\phi}(\Lambda) = \frac{y_t}{32\pi^2 v^2} \left[(m_h^2 - 4m_t^2) ((2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}) \log\left(\frac{\mu_R^2}{\Lambda^2}\right) \right], \quad (5.24)$$

where $y_{t/b} = \sqrt{2}m_{t/b}/v$. Note that the combinations of the Wilson coefficients appearing in (5.23) and (5.24) are the same as in F_{NLO} in (5.15). Effectively, it is possible to obtain the result under the assumption that the four-fermion operators are the only non-zero ones at the large scale by replacing in (5.15) $\mu_R \rightarrow \Lambda$. In the leading logarithmic running approximation.

5.1.2 SMEFT-NLO calculation of $t\bar{t}h$

Unlike the previous processes, the associated production of the Higgs with top quark pair involves new topologies that are not limited to Yukawa vertex correction or mass renormalisation. At the LHC, there are two sub-processes responsible for the $t\bar{t}h$ production: the gluon-initiated process that is depicted in Figure 5.3 and the quark-initiated one that is shown in Figure 5.4. The new *finite* topologies induced by the four-fermion operator correction are: triangle and box topologies, shown in diagrams (d) and (e) in Figure 5.3, as well as in the triangle topology shown in diagram (b) of Figure 5.4. Additionally, the $t\bar{t}g$ vertex correction in the quark-initiated process (diagram (c)) of Figure 5.4 is non-vanishing as the gluon is off-shell. This vertex correction has a UV pole that requires a counter-term for its cancellation

$$= \frac{ig_s}{12\pi^2 \Lambda^2} T_{ij}^A p_g^2 \gamma^\mu \left(C_{tt} P_R + (C_{QQ}^{(1)} + C_{QQ}^{(3)}) P_L + \frac{C_{Qt}^{(8)}}{4} \right) \left(\frac{1}{\epsilon} - 1 \right). \quad (5.25)$$

Another difference between $t\bar{t}h$ and the other Higgs processes studied in this chapter is that this channel has a non-trivial colour structure. This manifests in the presence of multiple colour projectors, because the quark anti-quark triplets or the gluon pairs

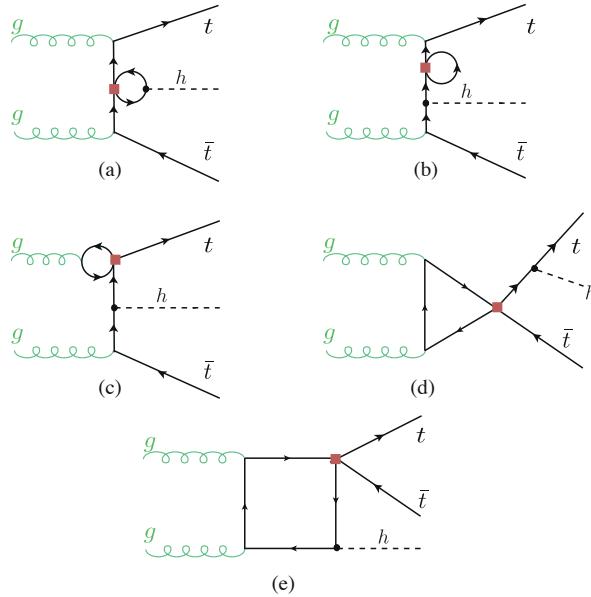


Figure 5.3. Feynman diagrams including the four-fermion loop contributions to the $gg \rightarrow t\bar{t}h$ subprocess.

do not have to recombine to only a singlet state rather to both a singlet and an octet states, according to the expansion of product $\mathbf{3} \otimes \overline{\mathbf{3}} \rightarrow \mathbf{1} + \mathbf{8}$. This breaks the degeneracy between the singlet and octet Wilson coefficients. Lastly, due to the new topologies and $t\bar{t}g$ vertex correction, operators with single chirality will contribute to NLO corrections, namely the operators \mathcal{O}_{tt} and $\mathcal{O}_{QQ}^{(1,3)}$.

All of the four-fermion operators are implemented in the loop-capable UFO model `lSMEFTatNLO` [210], which allows to compute the process with the help of `Madgraph_aMCNLO` [166] with some tweaking to remove the NLO QCD corrections. This is done via a user-defined loop filter function in `Madgraph_aMCNLO`. The results were reproduced by an analytic computation based on the reduction of one-loop amplitudes via the method developed by G. Ossola, C.G. Papadopoulos and R. Pittau (OPP reduction) [211], implemented in the FORTRAN code `CutTools` [212]. This programme takes the full one-loop amplitude and then reduces it to terms with 1,2,3, and 4-point loop functions in four dimensions, keeping spurious terms from the ϵ part of the amplitude. To correct for such terms, one needs to compute the divergent UV counter-terms as well as finite rational terms, denoted by R_2 as in ref. [213].¹ The amplitudes were generated in the same way as for ggF . The UV and R_2 counter-terms, which need to be supplemented to `CutTools`, were computed manually following the method detailed in [213]. For both codes, the NNPDF23 PDF set at NLO [214] was used.

The singlet and octet operators $\mathcal{O}_{QtQb}^{(1),(8)}$ contribute to $t\bar{t}h$ only via beauty-quark loops

¹Another rational term R_1 appears due to a mismatch between the four and d dimensional amplitudes, but this is computed automatically in `CutTools`.

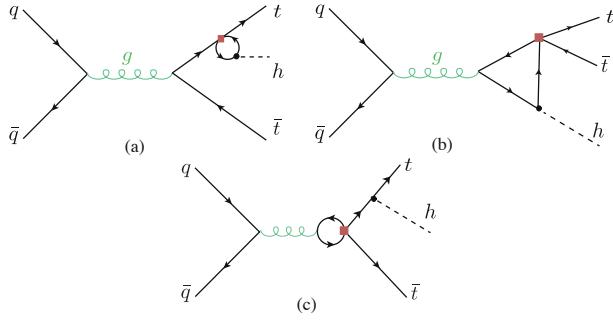


Figure 5.4. Feynman diagrams including the four-fermion loop contributions to the $q\bar{q} \rightarrow t\bar{t}h$ subprocess.

and, in principle, could be directly dismissed like the other beauty quark operators mentioned above. However, it is instructive to investigate their effect, albeit it is very small. Since the **SMEFTatNLO** model does not have these operators, they were implemented manually in this model. This is simply done by including the vertices generated by these operators and their UV and R_2 counter-terms. The calculation of the NLO correction by these operators was done both in **Madgraph_aMCNLO** using a modified UFO model and with the code based on **CutTools**. The effects were comparable to the leading log effects computed using **SMEFTsim** package [215] of $\sim 10^{-6}$, hence confirming the expectation that beauty quark loops have a negligible effect. The effects of the running of the Wilson coefficients from the high scale Λ to μ_R can be accounted for as described in (5.23) for the gluon-initiated process, while for the quark-initiated one, one needs to consider the operator mixing of the four-fermion operators that contain the first/second generation and the third generation. These corrections can be obtained from the RGEs in refs. [85–87].

5.1.3 Results

The NLO effects generated by the SMEFT four-fermion operators of the third generation quarks on the Higgs rate have been extracted from the above computation using the formula

$$\delta R(C_i) = R/R^{\text{SM}} - 1. \quad (5.26)$$

Here, R stands for either a cross-section σ or a partial width γ . The dependence of a given Higgs rate R on the Wilson coefficient C_i is denoted by $\delta R(C_i)$. Only contributions linear in the Wilson coefficients are considered. In order to isolate the finite terms from the ones coming from the RGE leading log approximation, the correction is further expanded to finite $\delta R_{C_i}^{fin}$ and leading log terms $\delta R_{C_i}^{log}$ as follows

$$\delta R(C_i) = \frac{C_i}{\Lambda^2} \left(\delta R_{C_i}^{fin} + \delta R_{C_i}^{log} \log \left(\frac{\mu_R^2}{\Lambda^2} \right) \right). \quad (5.27)$$

Operator	Process	μ_R	$\delta R_{C_i}^{fin}$ [TeV 2]	$\delta R_{C_i}^{log}$ [TeV 2]
$\mathcal{O}_{Qt}^{(1)}$	ggF	$\frac{m_h}{2}$	$9.91 \cdot 10^{-3}$	$2.76 \cdot 10^{-3}$
	$h \rightarrow gg$	m_h	$6.08 \cdot 10^{-3}$	$2.76 \cdot 10^{-3}$
	$h \rightarrow \gamma\gamma$		$-1.76 \cdot 10^{-3}$	$-0.80 \cdot 10^{-3}$
	$t\bar{t}h$ 13 TeV		$-4.20 \cdot 10^{-1}$	$-2.78 \cdot 10^{-3}$
	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$-4.30 \cdot 10^{-1}$	$-2.78 \cdot 10^{-3}$
$\mathcal{O}_{Qt}^{(8)}$	ggF	$\frac{m_h}{2}$	$1.32 \cdot 10^{-2}$	$3.68 \cdot 10^{-3}$
	$h \rightarrow gg$	m_h	$8.11 \cdot 10^{-3}$	$3.68 \cdot 10^{-3}$
	$h \rightarrow \gamma\gamma$		$-2.09 \cdot 10^{-3}$	$-1.07 \cdot 10^{-3}$
	$t\bar{t}h$ 13 TeV		$6.81 \cdot 10^{-2}$	$-2.40 \cdot 10^{-3}$
	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$7.29 \cdot 10^{-2}$	$-2.48 \cdot 10^{-3}$
$\mathcal{O}_{QtQb}^{(1)}$	ggF	$\frac{m_h}{2}$	$2.84 \cdot 10^{-2}$	$9.21 \cdot 10^{-3}$
	$h \rightarrow gg$		$1.57 \cdot 10^{-2}$	$9.21 \cdot 10^{-3}$
	$h \rightarrow \gamma\gamma$	m_h	$-1.30 \cdot 10^{-3}$	$-0.78 \cdot 10^{-3}$
	$h \rightarrow b\bar{b}$		$9.25 \cdot 10^{-2}$	$1.68 \cdot 10^{-1}$
$\mathcal{O}_{QtQb}^{(8)}$	ggF	$\frac{m_h}{2}$	$5.41 \cdot 10^{-3}$	$1.76 \cdot 10^{-3}$
	$h \rightarrow gg$		$2.98 \cdot 10^{-3}$	$1.76 \cdot 10^{-3}$
	$h \rightarrow \gamma\gamma$	m_h	$-0.25 \cdot 10^{-3}$	$-0.15 \cdot 10^{-3}$
	$h \rightarrow b\bar{b}$		$1.76 \cdot 10^{-2}$	$3.20 \cdot 10^{-2}$
$\mathcal{O}_{QQ}^{(1)}$	$t\bar{t}h$ 13 TeV		$1.75 \cdot 10^{-3}$	$1.84 \cdot 10^{-3}$
	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$1.65 \cdot 10^{-3}$	$1.76 \cdot 10^{-3}$
$\mathcal{O}_{QQ}^{(3)}$	$t\bar{t}h$ 13 TeV		$1.32 \cdot 10^{-2}$	$5.48 \cdot 10^{-3}$
	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$1.24 \cdot 10^{-2}$	$5.30 \cdot 10^{-3}$
\mathcal{O}_{tt}	$t\bar{t}h$ 13 TeV		$4.60 \cdot 10^{-3}$	$1.82 \cdot 10^{-3}$
	$t\bar{t}h$ 14 TeV	$m_t + \frac{m_h}{2}$	$4.57 \cdot 10^{-3}$	$1.74 \cdot 10^{-3}$

Table 5.2. The NLO effects of the four heavy-quarks operators on the Higgs rates. The effects are separated into finite $\delta R_{C_i}^{fin}$ and leading log parts, in correspondence with (5.27). This table has been published in [202].

Using this formula, one can obtain the correction at any NP scale Λ . Though, in the remainder of this chapter, this scale is set to 1 TeV. In Table 5.2, the finite and logarithmic corrections for the operators considered in this study are reported. Using this table in filling the formula (5.27) gives the correction to the Higgs rate in question. However, since some of the rates are Higgs partial widths, the Higgs total width Γ_h will be affected, and therefore, all Higgs rates are changed, as the branching fractions will carry the full width dependence on the Wilson coefficients.

An important observation from Table 5.2 is that the finite terms, are either larger or of the same order than the leading-log ones, except for $h \rightarrow b\bar{b}$ corrections from $\mathcal{O}_{QtQb}^{(1),(8)}$. This highlights the importance of the full NLO calculation for these corrections in constraining these four-fermion operators, in particular for $\mathcal{O}_{Qt}^{(1),(8)}$.

As mentioned earlier, there is a degeneracy between the singlet and octet operators,

seen clearly in the analytic result for gluon fusion and the Higgs decays considered. This degeneracy is though broken for $\mathcal{O}_{Qt}^{(1),(8)}$ due to $t\bar{t}h$. Since, the effect of $\mathcal{O}_{QtQb}^{(1),(8)}$ is negligible for this process, effectively one can only constrain the linear combination

$$C_{QtQb}^+ = (2N_c + 1)C_{QtQb}^{(1)} + c_F C_{QtQb}^{(8)}. \quad (5.28)$$

5.2 Fit to Higgs observables

The results from the NLO calculations discussed above allows for a combined fit between these four-fermion Wilson coefficients and the trilinear Higgs self-coupling λ_3 , thus extending the previous fits on λ_3 from single Higgs data refs. [30–33, 35]. A combined fit on λ_3 and the SMEFT operators modifying Higgs rates at LO have been performed in ref. [92]. The goal of this analysis is to show that this is not sufficient to determine the actual sensitivity on λ_3 . At the example of the four-fermion operators that are weakly constrained, As seen in Table 5.2, such operators despite entering at NLO induce significant modifications to Higgs rates. This chapter does not include a global SMEFT fit; instead merely motivates it by illustrating how the sensitivity for probing the Higgs-self coupling from single Higgs data gets mitigated when the four-fermion operators are included in the fit.

In the antecedent studies, the modification to Higgs self coupling was reported in terms of the κ -formalism. For the consistency of this analysis, the NLO corrections from the trilinear self-coupling will be converted to the SMEFT notation, in terms of the Wilson coefficient C_ϕ . For more details on the conversion between SMEFT and κ -formalism see subsection 2.2.2. In order to keep track of the SMEFT power-counting, the results of [31] are rewritten in terms of the SMEFT Wilson coefficient C_ϕ

$$\delta R_{\lambda_3} \equiv \frac{R_{\text{NLO}}(\lambda_3) - R_{\text{NLO}}(\lambda_3^{\text{SM}})}{R_{\text{LO}}} = -2 \frac{C_\phi v^4}{\Lambda^2 m_h^2} C_1 + \left(-4 \frac{C_\phi v^4}{\Lambda^2 m_h^2} + 4 \frac{C_\phi^2 v^8}{m_h^4 \Lambda^4} \right) C_2. \quad (5.29)$$

In (5.29), the coefficient C_1 corresponds to the contribution of the trilinear coupling to the single Higgs processes at one loop, adopting the same notation as [31]. The values of C_1 for the different processes of interest for this study are given in Table 5.3. The coefficient C_2 describes universal corrections and is given by

$$C_2 = \frac{\delta Z_h}{1 - \left(1 - \frac{2C_\phi v^4}{\Lambda^2 m_h^2} \right)^2 \delta Z_h}, \quad (5.30)$$

where the constant δZ_h is the SM contribution from the Higgs loops to the wave function renormalisation of the Higgs boson,

$$\delta Z_h = -\frac{9}{16} \frac{G_F m_h^2}{\sqrt{2}\pi^2} \left(\frac{2\pi}{3\sqrt{3}} - 1 \right). \quad (5.31)$$

The coefficient C_2 thus introduces additional $\mathcal{O}(1/\Lambda^4)$ (and higher order) terms in δR_{λ_3} . In ref. [31] considering the κ -formalism, the full expression of (5.30) is kept, while here two different descriptions will be discussed: one in which δR_{λ_3} is expanded up to linear order in C_ϕ and an alternative scheme in which terms up to $\mathcal{O}(1/\Lambda^4)$ are also kept in the EFT expansion. Keeping the full expression in (5.30) and including terms up to $\mathcal{O}(1/\Lambda^4)$ in C_2 lead to nearly the same results as the simple $\mathcal{O}(1/\Lambda^4)$ fit.

Process	C_1	$\delta R_{C_\phi}^{fin}$
ggF/ $gg \rightarrow h$	$6.60 \cdot 10^{-3}$	$-3.10 \cdot 10^{-3}$
$t\bar{t}h$ 13 TeV	$3.51 \cdot 10^{-2}$	$-1.64 \cdot 10^{-2}$
$t\bar{t}h$ 14 TeV	$3.47 \cdot 10^{-2}$	$-1.62 \cdot 10^{-2}$
$h \rightarrow \gamma\gamma$	$4.90 \cdot 10^{-3}$	$-2.30 \cdot 10^{-3}$
$h \rightarrow b\bar{b}$	0.00	0.00
$h \rightarrow W^+W^-$	$7.30 \cdot 10^{-3}$	$-3.40 \cdot 10^{-3}$
$h \rightarrow ZZ$	$8.30 \cdot 10^{-3}$	$-3.90 \cdot 10^{-3}$
$pp \rightarrow Zh$ 13 TeV	$1.19 \cdot 10^{-2}$	$-5.60 \cdot 10^{-3}$
$pp \rightarrow Zh$ 14 TeV	$1.18 \cdot 10^{-2}$	$-5.50 \cdot 10^{-3}$
$pp \rightarrow W^\pm h$	$1.03 \cdot 10^{-2}$	$-4.80 \cdot 10^{-3}$
VBF	$6.50 \cdot 10^{-3}$	$-3.00 \cdot 10^{-3}$
$h \rightarrow 4\ell$	$8.20 \cdot 10^{-3}$	$-3.80 \cdot 10^{-3}$

Table 5.3. The NLO dependence of single Higgs rates on C_ϕ , see [31]. The C_1 coefficients are to be used in eq. (5.29), while for a direct comparison with the effect of the four-fermion operators, we quote the translated effect $\delta R_{C_\phi}^{fin}$, which can be used directly in eq. (5.27). If the value of \sqrt{s} is not indicated the effect is the same for both 13 and 14 TeV. This table has been published in [202].

A Bayesian fit was performed using Markov-chain Monte Carlo (MCMC) method, using a flat prior $s \pi(C_i) = const.$ and a log likelihood of a Gaussian distribution

$$\log(L) = -\frac{1}{2} \left[(\vec{\mu}_{\text{Exp}} - \vec{\mu})^T \cdot \mathbf{V}^{-1} \cdot (\vec{\mu}_{\text{Exp}} - \vec{\mu}) \right]. \quad (5.32)$$

The log-likelihood is constructed as follows:

Experimental inputs $\vec{\mu}_{\text{Exp}}$ The signal strengths from experimental measurements of single Higgs rates defined as

$$\mu_{\text{Exp}} \equiv \sigma_{\text{obs}} / \sigma_{\text{SM}}. \quad (5.33)$$

The values of μ_{Exp} are taken from LHC Run II for centre-of-mass energy of $\sqrt{s} = 13$ TeV and integrated luminosity of 139 fb^{-1} for ATLAS and 137 fb^{-1} for CMS. In addition to HL-LHC projections by CMS for $\sqrt{s} = 14$ TeV and integrated luminosity of 3000 fb^{-1} were used to estimate the prospects of the HL-LHC for this fit, cf. Table 5.4.

Theoretical predictions $\vec{\mu}$ The corresponding theoretical predictions for each of the experimental measurement /projections have been built using the modification to

the cross-sections and branching ratios coming from the SMEFT four-fermion operators and C_ϕ . The signal strength is expanded in powers of Λ , keeping only Λ^{-2} terms,

$$\mu(C_\phi, C_i) = \frac{\sigma_{\text{Prod}}(C_\phi, C_i) \times \text{BR}(C_\phi, C_i)}{\sigma_{\text{Prod,SM}} \times \text{BR}_{\text{SM}}} \approx 1 + \delta\sigma(C_\phi, C_i) + \delta\Gamma(C_\phi, C_i) - \delta\Gamma_h(C_\phi, C_i). \quad (5.34)$$

I have explicitly checked that including terms up to Λ^{-4} in the expansion order only slightly alters the fit.

Uncertainties and correlations V The variance matrix \mathbf{V} is build from thee experimental uncertainties can be found in [Table 5.4](#). For Run-II data, only the ATLAS collaboration reported the correlation amongst different channels (here, only correlations $> 10\%$ are considered), while for the HL-LHC, the whole correlation matrix found on the webpage [\[216\]](#). The HL-LHC projections for the S2 scenario explained in [\[133\]](#) were used. These assume the improvement on the systematics that is expected to be attained by the end of the HL-LHC physics programme, and that theory uncertainties are improved by a factor of two with respect to current values. Theoretical uncertainties were not considered in this fit.

The python package `pymc3` [\[217\]](#) was used to construct the posterior distribution. I have used the `Arviz` Bayesian analysis package [\[218\]](#) to extract the credible intervals (CIs) from the highest density posterior intervals (HDPI) of the posterior distributions, where the intervals covering 95% (68%) of the posterior distribution are considered the 95% (68%) CIs. In the Gaussian limit, these 95% (68%) CIs should be interpreted as equivalent to the 95% (68%) Frequentist confidence level (CL) two-sided bounds. The `HEPfit` [\[219\]](#) code was used to validate the fits. Given that current bounds on these operators are rather weak, one may wonder about the uncertainty in these fits associated with the truncation of the EFT. Note that, since the four-quark operators only enter into the virtual corrections at NLO, Higgs production and decay contain only linear terms in $1/\Lambda^2$ in the corresponding Wilson coefficients, i.e. the quadratic terms coming from squaring the amplitudes are technically NNLO. Hence, quadratic effects in the signal strengths stem from only linearising the corrections to the product $\sigma_{\text{Prod}} \times \text{BR}$. These effects have been investigated and found to have a negligible impact on the fit. The operators of single chirality \mathcal{O}_{tt} and $\mathcal{O}_{QQ}^{(1)/(3)}$ were not included in the fit, as their effect on Higgs rates is limited to small δR for $t\bar{t}h$, and hence no meaningful bounds from single Higgs inclusive data can be obtained.

Production	Decay	$\mu_{\text{Exp}} \pm \delta\mu_{\text{Exp}}$ (symmetrised)		Ref.	
		LHC Run-II			
		CMS 137 fb^{-1}	ATLAS 139 fb^{-1}		
ggF	$h \rightarrow \gamma\gamma$	0.99 ± 0.12 1.030 ± 0.110		1.000 ± 0.042 [220–222]	
	$h \rightarrow ZZ^*$	0.985 ± 0.115 0.945 ± 0.105		1.000 ± 0.040	
	$h \rightarrow WW^*$	1.285 ± 0.195 1.085 ± 0.185		1.000 ± 0.037 [76, 220, 222]	
	$h \rightarrow \tau^+\tau^-$	0.385 ± 0.385 1.045 ± 0.575		1.000 ± 0.055	
	$h \rightarrow b\bar{b}$	2.54 ± 2.44 —		1.000 ± 0.247 [76, 222]	
	$h \rightarrow \mu^+\mu^-$	0.315 ± 1.815 —		1.000 ± 0.138 [76, 222]	
VBF	$h \rightarrow \gamma\gamma$	1.175 ± 0.335 1.325 ± 0.245		1.000 ± 0.128 [220–222]	
	$h \rightarrow ZZ^*$	0.62 ± 0.41 1.295 ± 0.455		1.000 ± 0.134	
	$h \rightarrow WW^*$	0.65 ± 0.63 0.61 ± 0.35		1.000 ± 0.073 [76, 220, 222]	
	$h \rightarrow \tau^+\tau^-$	1.055 ± 0.295 1.17 ± 0.55		1.000 ± 0.044	
	$h \rightarrow b\bar{b}$	— 3.055 ± 1.645		— [220]	
	$h \rightarrow \mu^+\mu^-$	3.325 ± 8.075 —		1.000 ± 0.540 [222]	
$t\bar{t}h$	$h \rightarrow \gamma\gamma$	1.43 ± 0.30 0.915 ± 0.255		1.000 ± 0.094 [220–222]	
	$h \rightarrow VV^*$	$0.64 \pm 0.64 (ZZ^*)$ $0.945 \pm 0.465 (WW^*)$ 1.735 ± 0.545		$1.000 \pm 0.246 (ZZ^*)$ $1.000 \pm 0.097 (WW^*)$ —	
	$h \rightarrow \tau^+\tau^-$	0.845 ± 0.705 1.27 ± 1.0		1.000 ± 0.149 [76, 220, 222]	
	$h \rightarrow b\bar{b}$	1.145 ± 0.315 0.795 ± 0.595		1.000 ± 0.116	
	$h \rightarrow \gamma\gamma$	0.725 ± 0.295 1.335 ± 0.315	$1.000 \pm 0.233 (Zh)$ $1.000 \pm 0.139 (W^\pm h)$	[220–222]	
Vh	$h \rightarrow ZZ^*$	1.21 ± 0.85 1.635 ± 1.025	$1.000 \pm 0.786 (Zh)$ $1.000 \pm 0.478 (W^\pm h)$	[76, 220, 222]	
	$h \rightarrow WW^*$	1.850 ± 0.438 —	$1.000 \pm 0.184 (Zh)$ $1.000 \pm 0.138 (W^\pm h)$	[222, 223]	
	$h \rightarrow b\bar{b}$	— 1.025 ± 0.175	$1.000 \pm 0.065 (Zh)$ $1.000 \pm 0.094 (W^\pm h)$	[220, 222]	
	Zh CMS	$h \rightarrow \tau^+\tau^-$ $h \rightarrow b\bar{b}$	1.645 ± 1.485 0.94 ± 0.32	— [76]	
$W^\pm h$ CMS	$h \rightarrow \tau^+\tau^-$ $h \rightarrow b\bar{b}$	3.08 ± 1.58 1.28 ± 0.41			

Table 5.4. The experimental single Higgs production and decay rates measurements from the complete data of LHC Run II and projections for the HL-LHC. The uncertainties were symmetrised here. The table is published in [202].

5.2.1 Fit results

In Figure 5.5 and Figure 5.6, I show the 68% and 95% CIs of the two-parameter posterior distributions and their marginalisation for the two-parameter fits involving C_ϕ and one of the four-heavy quark Wilson coefficients, evaluated at the scale $\Lambda = 1$ TeV for Run-II LHC measurements. Both linearised and quadratically truncated δR_{λ_3} fits are shown, and one can observe that the 95% CI bounds (shown on top of the panels) and correlations depend on the truncation.

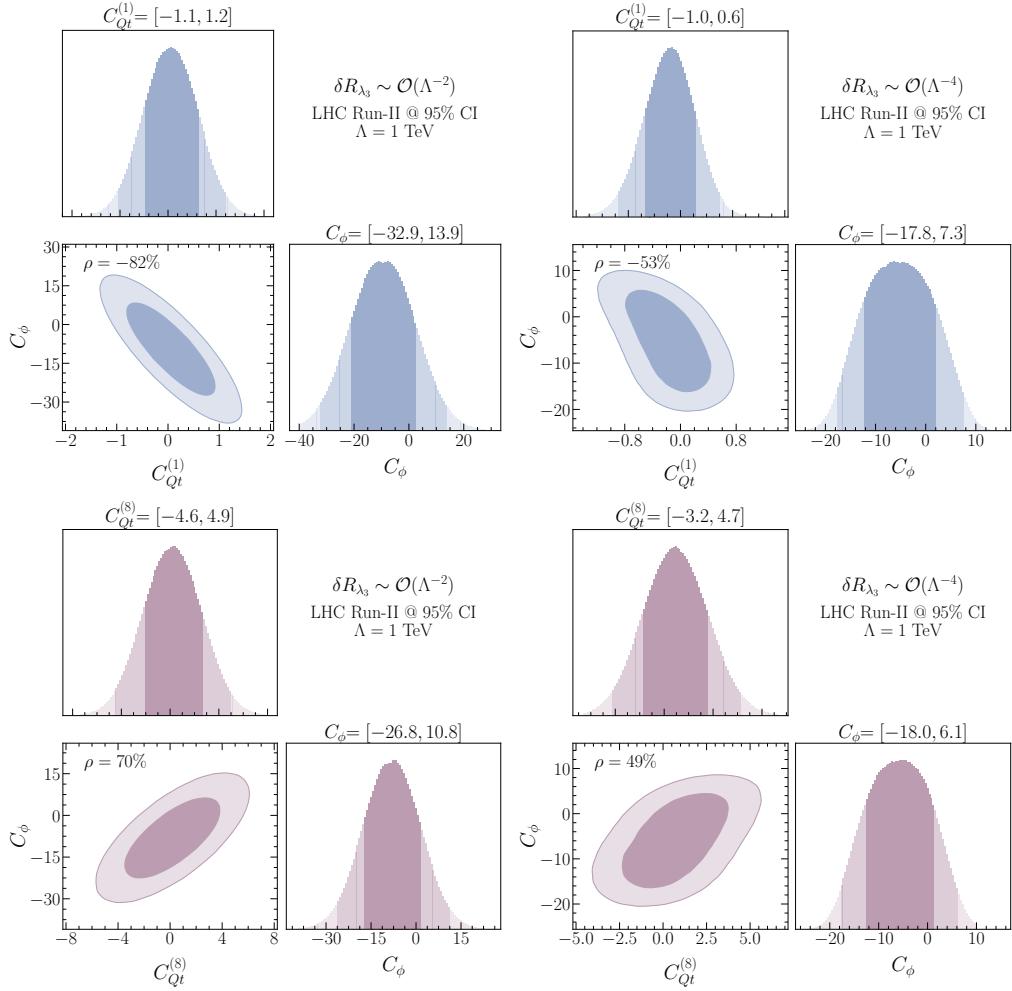


Figure 5.5. The posterior distributions of the Run-II data fits for C_ϕ with $C_{Qt}^{(1)}$ (up) and C_ϕ with $C_{Qt}^{(8)}$ (down). The 68% and 95% highest density posterior contours indicated. The limits shown on top of the plots indicate the 95% CIs. Plots on the left are made for the fully linearised δR_{λ_3} , while the ones on the right include the quadratic effects. This figure has been published in [202].

We observe that the four-fermion operators are strongly correlated with the Higgs

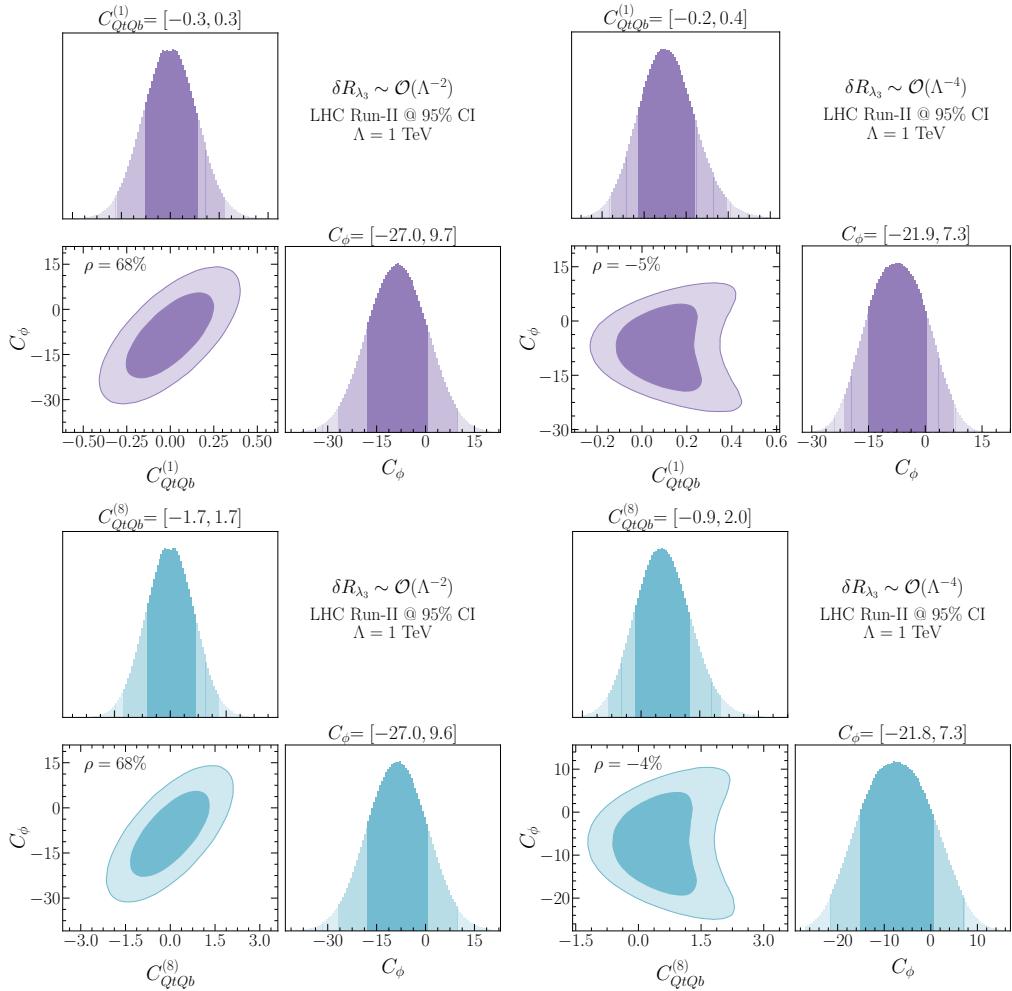


Figure 5.6. The posterior distributions of the Run-II data fits for C_ϕ with $C_{QtQb}^{(1)}$ (up) and C_ϕ with $C_{QtQb}^{(8)}$ (down). With the same annotations as in Figure 5.5. This figure has been published in [202].

self-coupling modifier \mathcal{O}_ϕ , in the linear fit, with Pearson's correlation of $\gtrsim 0.7$ and a p -value $< 10^{-4}$. In the case of the quadratic δR_{λ_3} fit, we observe diminished Pearson correlation, but in this scenario Pearson's correlation test is not particularly applicable, as we have non-linear relation between the variables.

The two-parameter fit results for the four-fermion Wilson coefficients are summarised in the forest plots in Figure 5.7, which is obtained by marginalising the posteriors distributions over C_ϕ . The finite effects were isolated by performing fits with δR^{fin} only. The finite effects are small for $O_{QtQb}^{(1)/(8)}$ but dominant for the four-top operators $O_{Qt}^{(1)/(8)}$; they are mainly coming from $t\bar{t}h$. The effect of EFT truncations of δR_{λ_3} can also be observed

as shifts in the mean values of the Wilson coefficients, but the 95% CIs themselves are not significantly affected. In these plots, the fit results from this study are also confronted with the limits obtained from fits to top-quark data [37, 89, 200, 201, 224, 225] and EWPO fits from [39]. When the Wilson coefficient running is taken into account, the 95% CI bounds obtained from Higgs data are consistently stronger than the ones from top data.

In Figure 5.8, the fit results for C_ϕ are shown after marginalising over the four-fermion Wilson coefficients in both EFT truncations schemes of δR_{λ_3} , as well as a single parameter fit for C_ϕ . These fits are compared also to the current 95 % CL bound on C_ϕ extracted from Higgs pair production search using the final state $b\bar{b}\gamma\gamma$ performed by ATLAS using Run-II data [226], which is translated from κ formalism.

The mean values and the 95%CIs change depending on the four-fermion Wilson coefficient that was paired with C_ϕ in the two-parameter fits. As expected, the single parameter fits for C_ϕ yield stronger bound on C_ϕ than the two-parameter fits, thus the inclusion of the four-fermion operators in single Higgs data dilutes C_ϕ bounds. Additionally, the truncation order of δR_{λ_3} appears to have a marked effect on the length of the CIs, with quadratic fits giving more stringent constraints on C_ϕ . Instead, for Higgs pair production it makes only a negligible effect if linear or up to quadratic terms in the EFT expansion are kept for the $C_\phi > 0$ bound, while the bound weakens at linear order in $1/\Lambda^2$ for $C_\phi < 0$ [227]. For instance, the quadratic single parameter fit for C_ϕ is comparable to the direct bound from Higgs pair production. However, this changes dramatically, when one includes the four-fermion operators in a combined fit, and the single-Higgs data constraints on C_ϕ become less significant compared to the direct hh bounds. It should be noted that the strongest bond on the Higgs self-coupling currently comes from the perturbative unitarity bound of ref. [107].

One of the important aspects of multivariate studies is the correlation between the variables. Apart from the two-parameter fits discussed above, four-parameter fits are also considered. These fits include C_ϕ plus the three directions in the four heavy-quark operator parameter spaces that the Higgs rates are mostly sensitive too, i.e. neglecting $C_{QQ}^{(1),(3)}$ and C_{tt} , and trading $C_{QtQb}^{(1)}$ and $C_{QtQb}^{(8)}$ by C_{QtQb}^+ .

When considering two- or four-parameter fits of C_ϕ and the four-heavy-quark Wilson coefficients, we observe non-trivial correlation patterns emerging amongst these coefficients. Figure 5.9 illustrates these correlation patterns for the four-parameter fit. We observe that the Wilson coefficients $C_{Qt}^{(1),(8)}$ are strongly correlated because, in analogy to $C_{QtQb}^{(1),(8)}$, they only appear in particular linear combination whenever correcting the Yukawa coupling. However, unlike $C_{QtQb}^{(1),(8)}$, they are not entirely degenerate because the main part of the NLO correction to $t\bar{t}h$ does not contain the aforementioned linear combination. The four-parameter fit also reveals that the Wilson coefficients $C_{Qt}^{(1),(8)}$ have a large correlation with C_{QtQb}^+ because all of the four Wilson coefficients appear in a linear combination in the NLO corrections except for $h \rightarrow b\bar{b}$ and $t\bar{t}h$. However, this correlation is not as strong due to the large NLO correction of the Higgs decay $h \rightarrow b\bar{b}$ from $C_{QtQb}^{(1),(8)}$. Moreover, the correlation between the four-heavy-quark Wilson

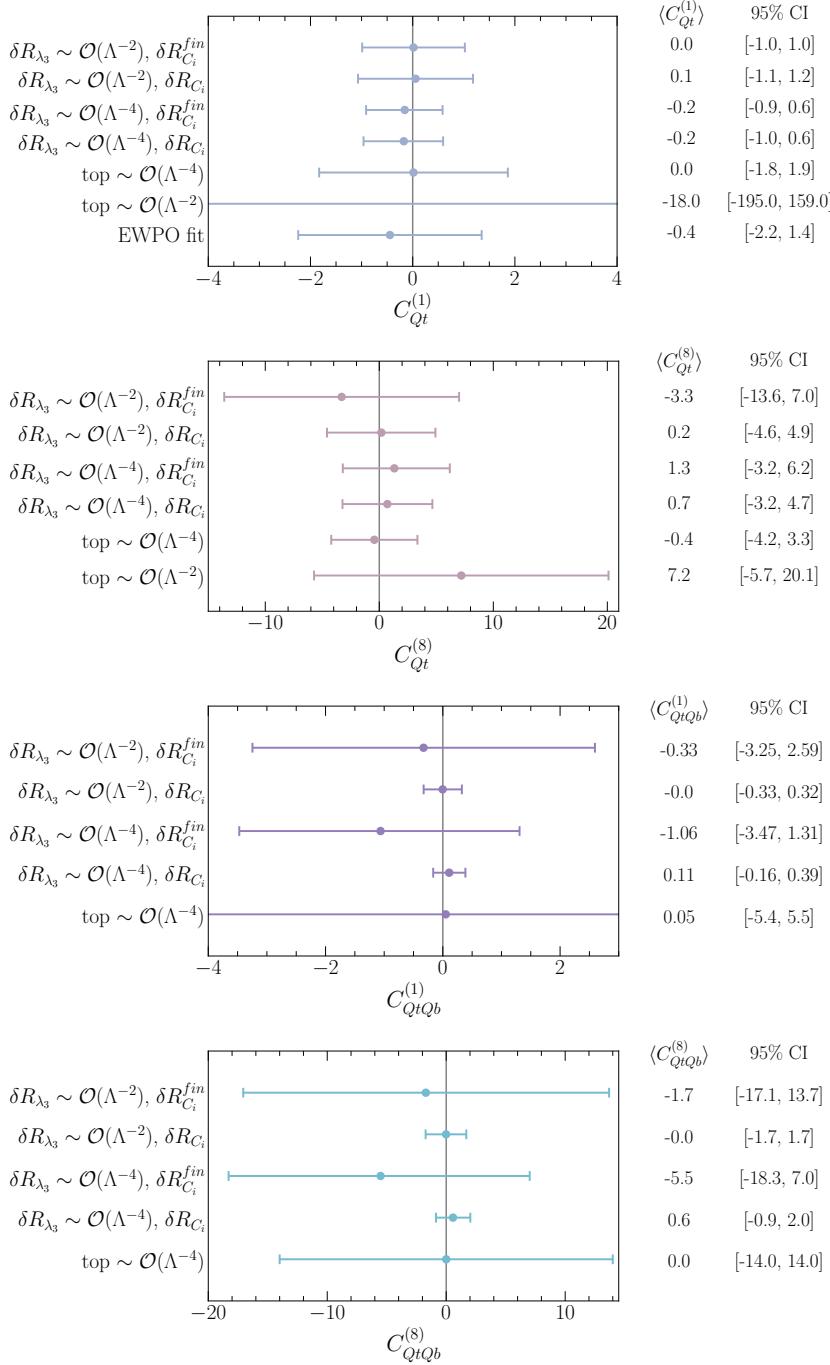


Figure 5.7. Forest plots illustrating the means and 95% CIs constraints on the four-heavy-quark Wilson coefficients C_i from Run-II data. These bounds are obtained from two-parameter fits including the aforementioned coefficients along with C_ϕ , then marginalising over the latter. In these plots, I show different fit scenarios: only the finite part of the NLO correction included vs the full results, as well as the EFT truncation scheme for the trilinear coupling, linear vs quadratic. Fits from top data [89] for $C_{Qt}^{(1),(8)}$ and [201] for $C_{QtQb}^{(1),(8)}$ as well as EWPO fits from [39] were included for comparison. This figure has been published in [202].

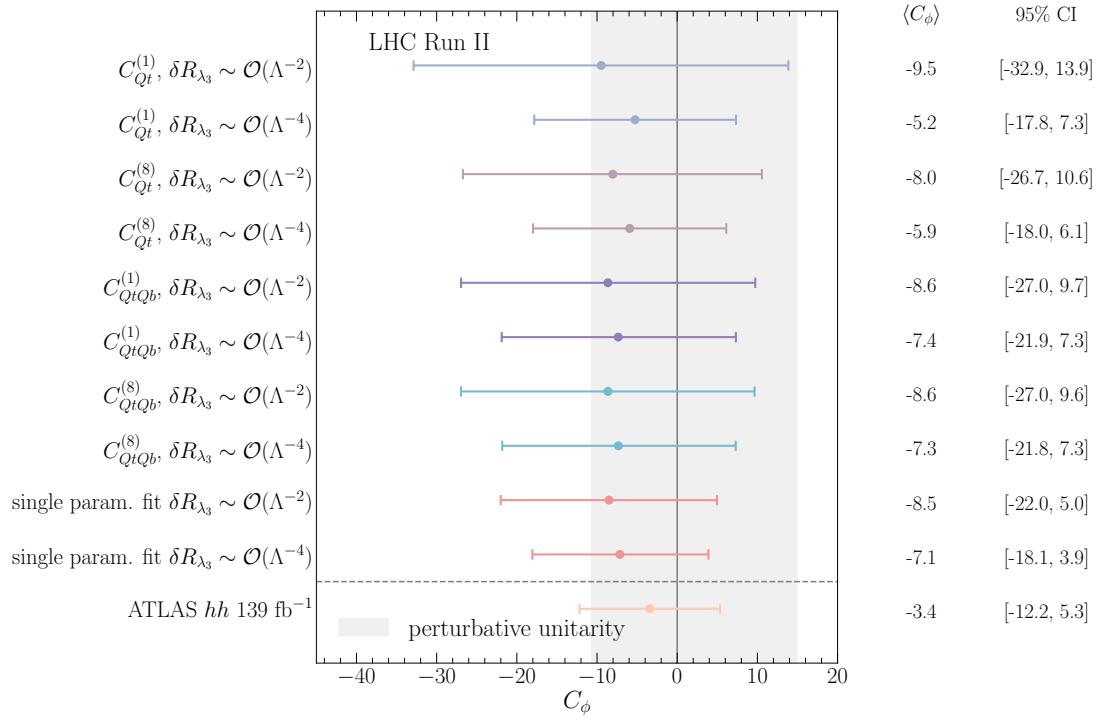


Figure 5.8. A forest plot illustrating the means and 95% CIs bounds for C_ϕ from the two-parameter fit, with the four-fermion operators marginalised. The fits results for C_ϕ from full Run-II Higgs data keeping terms up to $\mathcal{O}(1/\Lambda^2)$ or $\mathcal{O}(1/\Lambda^4)$ in δR_{λ_3} are shown. For comparison, also the 95% CI and means for the single parameter fit for C_ϕ with the same single Higgs data is shown as well as the bounds on C_ϕ from the 139 fb^{-1} search for Higgs pair production [226]. The horizontal grey band highlights the perturbative unitarity bound [107]. This figure has been published in [202].

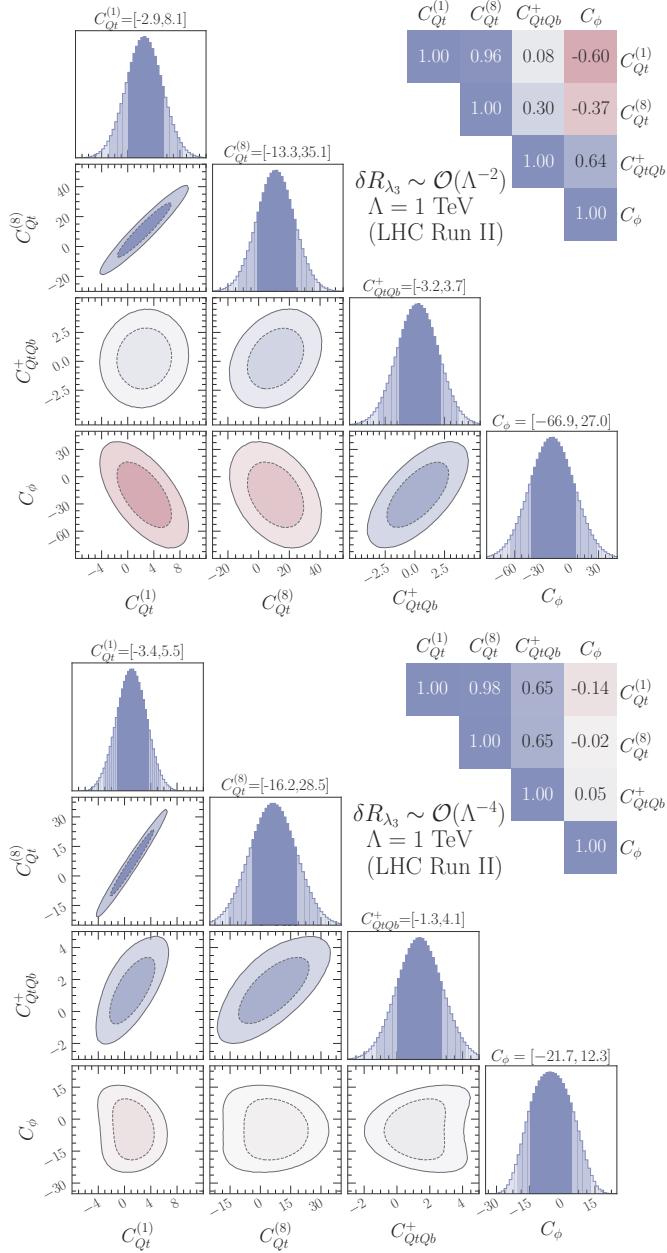


Figure 5.9. The marginalised 68% and 95% Highest density posterior contours for the four-parameter fits including the different four-quark Wilson coefficients and C_ϕ . The numbers above the plots show the 95% CI bounds while the correlations are given on the top-right side. The correlation between each pair of the Wilson coefficients is highlighted as a heatmap. The upper panel shows the fit including up to $\mathcal{O}(1/\Lambda^2)$ in δR_{λ_3} while the lower one shows the fit including also $\mathcal{O}(1/\Lambda^4)$. This figure has been published in [202].

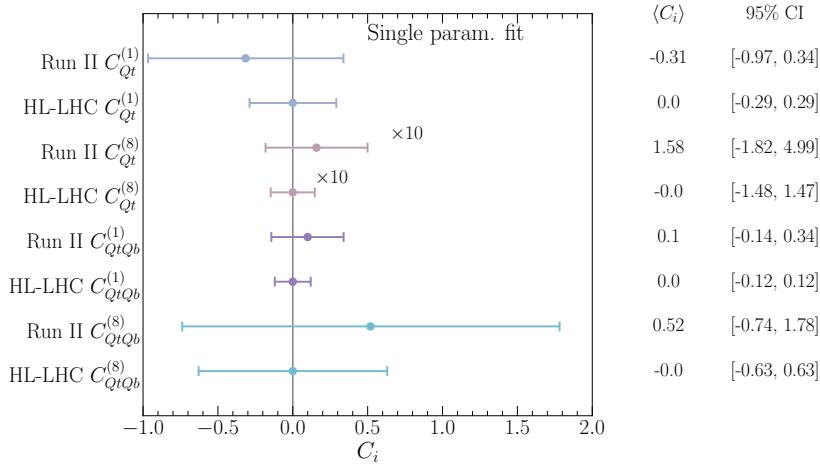


Figure 5.10. Results of single parameter fit showing the improvement in the constraining power of the HL-LHC over the current bounds from Run-II data. This figure has been published in [202].

coefficients and C_ϕ depends on the δR_{λ_3} truncation.

5.2.2 Prospects for HL-LHC

Using the CMS Higgs signal strength projections for the HL-LHC in refs. [216, 222] for a centre-of-mass energy of $\sqrt{s} = 14$ TeV and integrated luminosity of 3 ab^{-1} , it is possible to repeat the fits done for Run-II. The projections for the S2 scenario explained in [133] were used. In Figure 5.10, I show the comparison between the fit results of Run-II data and the projections for the HL-LHC for single parameter fits. For the operators $\mathcal{O}_{Qt}^{(1),(8)}$ the constraining power of the HL-LHC is roughly a factor two better as the current bounds from single Higgs data, while for the operators $\mathcal{O}_{QtQb}^{(1),(8)}$ the improvement is a little less prominent. In Figure 5.11, the limits on C_ϕ in a single parameter fit for Run-II and the projections for the HL-LHC are shown, including δR_{λ_3} up to order $\mathcal{O}(1/\Lambda^2)$ or $\mathcal{O}(1/\Lambda^4)$. While for Run-II data, the inclusion of $\mathcal{O}(1/\Lambda^4)$ made a significant difference; this is less pronounced for the HL-LHC projections. These results are similar to the projections presented in a κ_λ fit in [228]. The results were also confronted with data from searches for Higgs pair production 139 fb^{-1} [226] and HL-LHC projections [229] on Higgs pair production, showing that Higgs pair production would still allow setting firmer limits on C_ϕ .

5.3 Conclusion

This chapter calculates the NLO corrections emanating from the SMEFT four-heavy-quark operators to single-Higgs rates. We have seen that both four-fermion operators involving homogenous and heterogeneous chirality structures contribute to Higgs rates

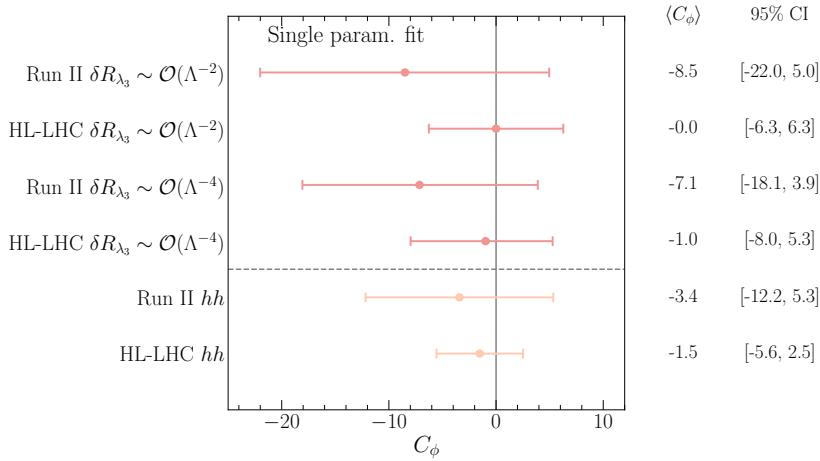


Figure 5.11. A forest plot illustrating the means and 95% CI's of the posteriors built from the C_ϕ in a single-parameter fit, showing also the differences in including terms of $\mathcal{O}(1/\Lambda^2)$ or up to $\mathcal{O}(1/\Lambda^4)$ in the definition of δR_{λ_3} . For comparison, also the limits and projections from searches for Higgs pair production are shown. This figure has been published in [202].

at NLO. It turns out that, the operators with heterogeneous chirality structures have more sizeable effects as they would contribute to $h f \bar{f}$ vertex correction and quark mass renormalisation in SMEFT. Therefore, the appear in more channels compared to the operators baring homogenous chirality structures. The results of these calculations were utilised in fits on the Wilson coefficients associated with these operators using single-Higgs data. The operators with the same chirality structure are not constrained strongly by these fits, and hence their results were not included. This applies also to the operators that contribute only via beauty-quark loops, like $\mathcal{O}_{Qb}^{(1),(8)}$. Two processes stood out in this calculation in terms of their sensitivity to these operators. The first process is the decay of the Higgs to beauty quarks, which had a strong sensitivity to $\mathcal{O}_{QtQb}^{(1),(8)}$ operators, the second process is the associated production of the Higgs with top pair $t\bar{t}h$ having large finite corrections coming from $\mathcal{O}_{Qt}^{(1),(8)}$. Furthermore, these corrections depend on the colour factor and thus break the degeneracy between the singlet and octet operators.

Bayesian analysis combining the four-fermion operators with the SMEFT operator modifying the Higgs self-coupling C_ϕ has been performed and motivated by the fact that both four-fermion operators and \mathcal{O}_ϕ are weakly constrained and only appear at NLO in single-Higgs rates. The fit results showed that the constraints on C_ϕ from single Higgs data would become significantly diluted compared to the fits performed with this operator alone, or even with respect to the fits including the operators that enter at LO [30–33, 35]. This is due to the strong correlation between C_ϕ and the four-fermion operators considered in this study. On the other hand, the fits yielded stronger bounds on the four-heavy-quark operators than those obtained from top-quark data [89, 201]. Comparable bounds can instead be obtained in a fit to EWPO data [39].

Similarly to single-Higgs processes, EWPO are modified by these operators at NLO, as well. Additionally, the authors of ref. [230] have shown that these operators could also be constrained from flavour observables involving $\Delta F = 2$, in particular $B_s - \overline{B}_s$ mixing. However, these bounds depend on the flavour ansatz of the NP and hence are not entirely model-independent. The results of these calculations and fits further emphasise the interconnectivity of SMEFT operators and experimental observables.

Finally, the question remains: *How this interconnectivity would manifest in an NP model?*. In fact, large effective couplings involving four top quarks are expected in many NP models, for example, partial compositeness [231]. These models would also generate sizeable modifications to the Higgs self-interaction. Similar effects could be obtained from models containing new scalars, such as an additional Higgs doublet $\varphi \sim (1, 2)_{\frac{1}{2}}$, or other scalars with non-singlet representation under $SU(3)_c$ like $(6, 1)_{\frac{1}{3}}$ and $(8, 2)_{\frac{1}{2}}$, these are models that would generate both four-fermion operators and \mathcal{O}_ϕ . For further details on these models and their matching, see [232]; for the NLO matching to SMEFT, see [233].

Part III

Higgs Pair Production

6 Overview of Higgs pair production at colliders

The determination of the shape of the Higgs potential is an essential part of the LHC physics programme. Unlike other Higgs measurements reviewed in this thesis, the light Yukawa and Higgs-self couplings are exceptionally hard to probe. This is evident from the conclusion of chapter 5 for the case of trilinear Higgs coupling. We have seen that the effectiveness of using single-Higgs signals to probe the Higgs trilinear coupling is challenged by other weakly constrained operators also affecting these signals. Thus, Higgs pair production remains the only direct way to access this elusive interaction.

The production of Higgs in pairs has roughly 10^{-3} of the signal producing single Higgs at the LHC. Higgs pair production, with Higgs decays considered, has a cross-section of $\sim 1\text{fb}$, in the SM. Sensitivity to the SM Higgs pair production will hence only be reached in the high luminosity phase of the LHC [133]. The quartic coupling, that requires NLO corrections to Higgs pair or can be directly accessed in triple Higgs production, both of which remain elusive at the LHC [234]. The main advantages for Higgs pair production in determining the Higgs trilinear self-coupling come from the dependence of the cross-section on λ_3 at the LO level, as well as the fact that the rest of SMEFT operators entering this process (see eq (2.5)) can also be constrained from other processes. This will improve the constraints on these operators when both Higgs pair and other Higgs measurements are combined cf. [92]¹. However, the inclusion of light quark Yukawa couplings modifiers, e.g. $C_{u\phi}$ and $C_{d\phi}$ can influence potential bounds on C_ϕ .

This chapter starts by reviewing the theoretical status of the dominant process for Higgs pair production, beginning with the gluon fusion in section 6.1. Then, the other subdominant channels will be briefly reviewed in section 6.2. Afterwards, I overview the experimental efforts in probing these rare yet fascinating processes in section 6.3. Finally, I present in section 6.4 a summary of the potential for Higgs pair production in probing Higgs elusive interactions.

6.1 Higgs pair production by gluon fusion

The dominant process for Higgs pair production at the LHC (and hadron colliders in general) is the gluon fusion channel via top quarks in the loops, while the beauty-quark loops contribute less than 1%. This process is well-studied at leading order (LO) ana-

¹The same could not be said for non-linear HEFT operators; such operators require Higgs pair production to be directly probed.

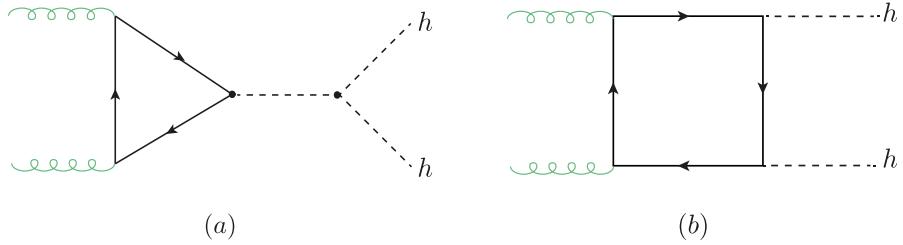


Figure 6.1. Feynman diagrams for the ggF process of Higgs pair production in the SM.

lytically [235–238]. The higher-order computations are significantly more complicated to perform compared to the gluon fusion production of single-Higgs. As has been outlined in chapter 4 for $gg \rightarrow Zh$, the computation of multi-scale amplitudes at two-loop order is extremely challenging and requires numerical approaches or approximations. The first attempt to compute the NLO corrections to di-Higgs were via the HTL approximation [138, 239, 240], improved by reweighing with the full LO matrix element squared. These corrections are implemented in HPAIR [238]. These corrections are large, with a K-factor of ~ 2 . This prompted more calculations with inclusion of top quark mass effects [117, 241–243], which improved the stability of the HTL expansion as well as corrected the cross-section by $\sim 10\%$.

Later, the threshold resummation effects of the HTL have been included in [244]. This approach, however, is not sufficient to produce corrections to the differential cross-section, as the HTL fails for $M_{hh}^2/4m_t^2 \lesssim 1$. The cross-section though peaks at $M_{hh} \approx 400$ GeV, hence this approximation only describes well a small part of the phase space. Using the numerical evaluation of the two-loop integrals, it is possible to obtain exact results with full top quark mass dependence, see refs. [245–247]. Nonetheless, this comes at the cost of computational power required to evaluate the cross-section. Fast and flexible implementations at NLO QCD can be obtained from analytical computations, i.e. small p_T [11], high energy (HE) expansion [248] and expansions in small Higgs mass [249, 250]. The latter covers of the whole M_{hh} spectrum. The NNLO cross-section has been computed numerically in [251], and also at differential level [252]. analytical NNLO computations are only available in the HTL [253]. Also, NLO+NNL analytical results have been obtained by [254]. Parton shower matching for NLO Higgs pair production has been computed in [255], which was essential for the POWHEG implementation for di-Higgs, with NLO corrections computed from a grid that has been made available by [103, 256, 257].

The small p_T and HE expansions can be bridged using Padé approximants [171]. The matching between the results across low and high energy intervals of m_{hh} shows the strength of the Padé approximants technique. The LO Higgs pair production with SMEFT operators is available in SMEFTatNLO model [210] for Madgraph_aMCNLO. Calculation of higher-order corrections to Higgs pair production in EFT have been performed in refs. [100, 258–260].

In the analysis shown in the next chapter, the Higgs pair production cross-section at NNLO QCD order was used in accordance with according to the LHC Higgs working

	σ [fb]	Scale [fb]	PDF+ α_s [fb]	Total [fb]
SM (LO)	21.45	+4.29 -3.43	± 1.46	+4.53 -3.73
SM (NLO) [268]	33.89	+6.17 -4.98	+2.37 -2.01	+6.61 -5.37
SM (NNLO) [251]	36.69	+0.77 -1.83	± 1.10	+1.66 -6.43 (incl. m_t uncertainty [266])

Table 6.1. Gluon fusion Higgs pair production cross-section at 14 TeV with theoretical uncertainties, the HTL is computed using HEFT, top running mass, LO, NLO and NNLO QCD corrections. The NLO and NNLO results are taken from the references cited in the table. The LO results are computed via a FORTRAN code. Using the NNPDF30 PDFs [269], a central scale of M_{hh}/\sqrt{s} and $\alpha_s(m_z) = 0.118$.

group recommendations [261, 262]:

$$K = \frac{\sigma_{NNLO}}{\sigma_{LO}}, \quad K_{14\text{TeV}} \approx 1.71. \quad (6.1)$$

The ^3LO corrections in the HTL have been performed in ref. [263].

6.1.1 Theoretical uncertainties

There are four dominant sources of the theoretical uncertainties for Higgs pair production:

1. Scale uncertainty: coming from the arbitrariness of scale choice. This is used as a measure of missing higher-order corrections.
2. PDF uncertainties: as a result of the uncertainty in the PDF fitting and modelling.
3. α_s running uncertainty: originating from the initial value (i.e. $\alpha_s(M_Z)$).
4. The choice of the quark mass renormalisation scheme that involves m_t appearing in the loop propagators and in the top Yukawa.

The computation of the PDF and α_s uncertainties is described in [264, 265]. In order to calculate the scale uncertainties, the cross-section was computed with different μ_R and μ_F values ranging between:

$$\frac{M_{hh}}{4} \leq \mu_R/\mu_F \leq M_{hh} \quad (6.2)$$

The combination of the m_t renormalisation and scale uncertainties can be found in [266]. The total 14 TeV ggF hh , cross-section at different orders in computation with its uncertainties is shown in Table 6.1, which indicates that the uncertainties are dominated by the m_t renormalisation scheme of $\sim -18\%$ uncertainty in the lower envelope. This is a significant part of the uncertainty budget and needs to be resolved by including $N^3\text{LO}$ corrections to ggF hh . Such corrections are available hitherto only in the HTL [263, 267]; however, in this approximation, the m_t uncertainty cannot be computed.

6.2 Other processes

Like single-Higgs production at hadron colliders, the production of Higgs pairs has the same subdominant channels VBF, di-Higgsstrahlung Vhh and associates production of Higgs pair with top quarks $t\bar{h}/tjh$. Their cross-sections and uncertainties at 14 TeV are shown in [Table 6.2](#), while in [Figure 6.2](#) their cross-sections as a function of the centre-of-mass energy \sqrt{s} is shown [228].

Process	Cross-section 14 TeV (fb)	Theo. accuracy	Theo. uncertainty (%)	Contribution (%)
1. ggF hh	36.690	NNLO QCD	12.3	90.1
2. VBF hh	2.050	N ³ LO QCD	2.1	5.0
3. Zhh	0.415	NNLO QCD	3.6	1.0
4. W ⁺ hh	0.369	NNLO QCD	2.1	0.9
5. W ⁻ hh	0.198	NNLO QCD	3.0	0.5
6. tth & tjhh	0.986	NLO QCD	5.1	2.4

Table 6.2. Summary of the Higgs pair production processes at 14 TeV LHC. Event generation software implementation of the gluon fusion channel is only available at NNLO theoretical accuracy, despite that N³LO corrections have been performed in [263]

6.2.1 VBF hh

Vector boson fusion hh production has the second largest cross-section after ggF hh , which is calculated up to N³LO [268, 270, 271] inclusively and differentially at NNLO [272]. The dominant diagrams are analogous to the single Higgs VBF involving the W/Z bosons exchanged in the t -channel. The process has the same topology as the off shell single Higgs VBF, with the off-shell Higgs giving two final states ones via the trilinear self-coupling.

6.2.2 Di-Higgsstrahlung

The associated production of the Higgs pair with W and Z bosons has a small cross-section compared to ggF and VBF. This process is known up to NNLO QCD accuracy, including the gluon-fusion component in the full computation [268, 273, 274].

6.2.3 Associated Higgs pair production with t -quarks

Sometimes called the di-Higgs bremsstrahlung off top quarks [228], this channel has a steeper dependence on \sqrt{s} than the single Higgs bremsstrahlung $t\bar{h}$. One can see, for example, from [Figure 6.2](#) that its cross-section becomes at roughly the same values as the VBF's at large \sqrt{s} . Only NLO computations for these channels have been carried out [275]. All three channels have a relatively small NLO correction compared to ggF, which ranges from 10-30%.

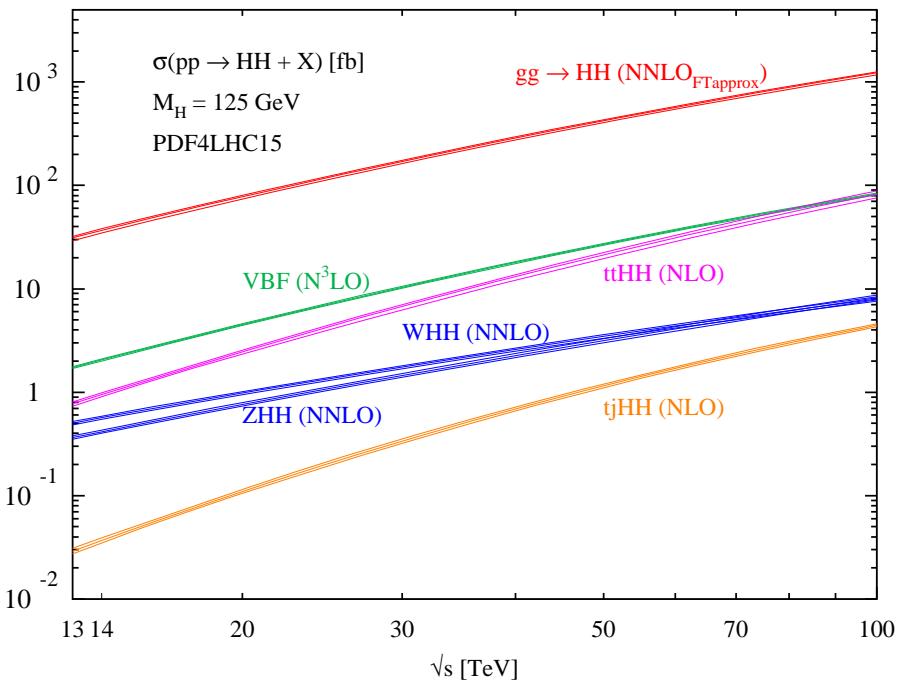


Figure 6.2. The cross-section of all Higgs pair production processes at the highest available perturbation order as a function of centre-of-mass energy \sqrt{s} . The bands show the uncertainties without the top quark mass renormalisation scheme. This plot is taken from [228].

6.3 Experimental overview for Higgs pair production

The search for Higgs pair production can be divided into two categories, resonant and non-resonant production. The first searches for heavy resonances that decay into a Higgs pair, while the latter is concerned about the SM scenario or if the NP has a scale beyond the reach of the LHC, i.e. when the EFT limit is valid. In this review, I shall focus on the non-resonant searches, as these are the ones relevant to the focus of this thesis; for a detailed overview of the resonant searches, cf. [228].

$$hh \rightarrow b\bar{b}b\bar{b}$$

The final state $hh \rightarrow b\bar{b}b\bar{b}$ has the highest SM cross-section possible for the Higgs pair but is difficult to probe due to the large QCD background of four b-tagged jets in the final state. CMS [276] has used boosted decision trees (BDT) for studying this final state for ggF and VBF channels. This allowed for sensitivity on the trilinear and $hhVV$ couplings. Their analysis led to 95% CL bounds on $\kappa_\lambda \in [-2.3; 9.4]$ and $\kappa_{2V} \in [-0.1; 2.2]$. They have also performed a boosted analysis for the VBF channel by defining two large jets with a jet radius of $\Delta R = 0.8$. Despite their analysis not being sensitive to the trilinear self-coupling, it could probe both κ_V and κ_{2V} , which leads to the most stringent bound on the latter coupling modifier so far $\kappa_{2V} \in [0.6; 1.4]$. The $\kappa_{2V} = 0$ hypothesis is excluded with $p < 0.001$ [277]. On the other hand, ATLAS has performed only a resolved analysis for this final state and the VBF production channel [278]. Hence they were able to report bounds on $hhVV$ coupling $\kappa_{2V} \in [-0.43; 2.56]$.

$$hh \rightarrow b\bar{b}VV$$

ATLAS has considered the gluon fusion final state $hh \rightarrow b\bar{b}\ell\ell$, with the leptons coming from WW/ZZ decays [279]. This state covers around 90% of the total $hh \rightarrow b\bar{b}VV$ signal. Their analysis was divided into two categories: same-flavour and different-flavour leptons. The observed signal strength was lower than the expected one. Hence, no bounds on the self-coupling could be extracted from this search. CMS has carried out a similar analysis but with a requirement to observe four leptons instead of two. That is, they have searched for the final state $hh \rightarrow b\bar{b}(ZZ^* \rightarrow 4\ell)$. The 95% CL upper limit on the signal strength was 30 times the SM one, with bounds on Higgs self-coupling of $\kappa_\lambda \in [-9; 14]$ [280].

$$hh \rightarrow b\bar{b}\tau\tau$$

This channel has backgrounds coming from real τ 's, such as $t\bar{t}$ and Zj with heavy jets. In addition to fake τ 's coming from QCD multijet process. A neural network (NN) has been used by ATLAS [281] investigating this channel, using resolved b jets. The extracted bounds on the trilinear self-coupling are $\kappa_\lambda \in [-2.4; 9.2]$.

$$hh \rightarrow b\bar{b}\gamma\gamma$$

This final state is the most promising for Higgs pair searches. Despite having a lower cross-section than the previous final states with BR of 0.27% in the SM, it has the highest selection efficiency. This is due to the low backgrounds and the ability to reconstruct the photons fully. The dominant non-reducible background is QCD/QED production of $b\bar{b}\gamma\gamma$, which has a cross-section of $\sim 13\text{fb}$ at the 14 TeV LHC, more details about the backgrounds of this final states are shown in [Table 6.3](#).

Channel	LO σ [fb]	NLO K-fact	6 ab^{-1} [#evt @ NLO]
$b\bar{b}h, y_b^2$	0.0648	1.5	583
$b\bar{b}h, y_b y_t$	-0.00829	1.9	-95
$b\bar{b}h, y_t^2$	0.123	2.5	1,840
Zh	0.0827	1.3	645
$\sum b\bar{b}h$	0.262	-	2,970
$b\bar{b}\gamma\gamma$	12.9	1.5	116,000
$t\bar{t}h$	1.156	1.2	6,938

Table 6.3. SM cross-section for the main background processes at 14 TeV with 6 ab^{-1} data at the HL-LHC. For $b\bar{b}h$ production, the Higgs boson is decayed to a pair of photons. The total production of Higgs associated with $b\bar{b}$ is denoted by $\sum b\bar{b}h$ and is the sum of the top four channels.

Both ATLAS and CMS have published searches of this channel using BDT and NN analyses [\[226, 282\]](#). Though the ATLAS collaboration has reported the strongest 95% CL bound on κ_λ thus far, and their result was used in the comparisons in [Figure 5.11](#). In comparison, CMS has reported bounds on both κ_λ and κ_{2V} of $\kappa_\lambda \in [-3.3; 8.5]$ and $\kappa_{2V} \in [-1.3; 3.5]$.

6.4 Summary

The Higgs pair production is a missing critical measurement of the SM; it is essential to determine the Higgs potential by directly constraining the Higgs trilinear self-coupling. Moreover, this channel is sensitive to non-linear couplings of the Higgs. Due to the small cross-section of this channel, current searches obtain relatively weak bounds on κ_λ that are comparable with the perturbative unitarity bounds [\[107\]](#). Nonetheless, the HL-LHC is expected to result in an observation or even discovery of this process, particularly with the help of advanced machine learning techniques.

The observation of Higgs pair production is expected to provide a direct measurement of one of the two “difficult” couplings in the SM Higgs sector, the trilinear Higgs self-coupling. However, as we shall explore in the upcoming chapter, it could also provide a window for observing the Higgs coupling to light quarks, the second challenging coupling class we discussed earlier.

7 Higgs pair as a probe for light Yukawa couplings

The immense hierarchy of quark (and lepton) masses that illustrated in Figure 7.1 is one of the most peculiar aspects of the SM. One might wonder whether the Braut-Englert-Higgs mechanism is responsible for the light quark mass generation or if other physics beyond the SM also plays a role in this. In fact, one of S. Weinberg's last papers addressed this very question [283]. In this paper, Weinberg proposed that only the third generation fermions obtain their masses from Yukawa coupling, while the rest acquire theirs via loop-level interactions. Despite his model being only illustrative, his paper is a testament that even the pioneers of the SM theory still reflect upon this mystery.

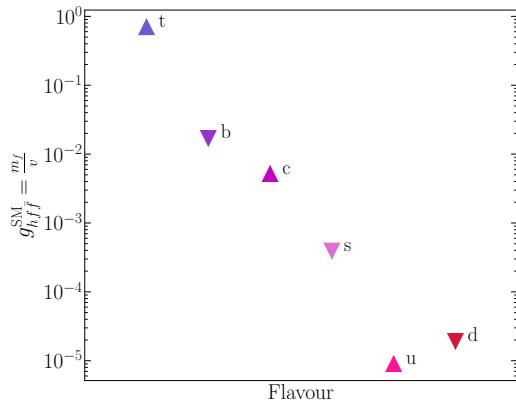


Figure 7.1. The SM Yukawa couplings are proportional to the quark masses because the Higgs Yukawa couplings span about six orders of magnitude. The SM cannot explain this large hierarchy.

The pragmatic approach to unravelling this puzzle would be to directly measure the Higgs interaction with light fermions. Ideally, this would be via Higgs decays to first and second-generation fermions. This is feasible for the muon case [284, 285] and rather challenging for the charm quarks [286–288]. However, it is nearly impossible with the current technologies for the electron, strange and first-generation quarks. Lepton colliders might have potential for *strange tagging* [289]. The difficulties here are twofold: First, the SM predicts that these couplings are extremely small, effectually making the respective rates vanish even at tens of ab^{-1} luminosity. Even if NP enhanced the Higgs coupling to these fermions, the resolution of the LHC would make reconstructing the

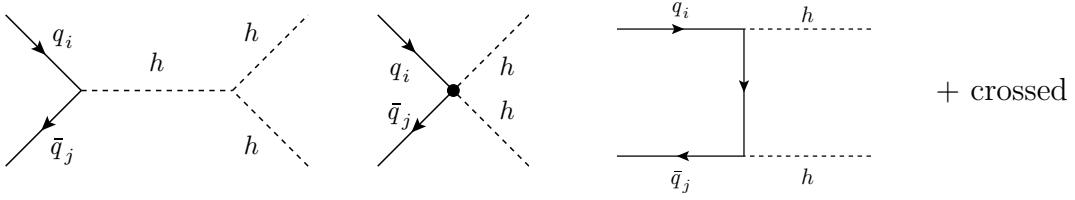


Figure 7.2. Feynman diagrams for the $q\bar{q}A$ Higgs pair production in the SMEFT paradigm. The middle diagram shows a contact $hhq\bar{q}$ interaction that constructively interfere with the s -channel topology. Combined with the PDF enhancement, Higgs pair production is significantly more sensitive to light Yukawa couplings compared to its single Higgs counterpart.

Higgs from electron pairs challenging compared to muons [290], and it is not possible to distinguish up, down, or gluon jets at the LHC from the overwhelming QCD background. Additionally, light quarks jets cannot be flavour-tagged with any current or foreseen advancements; this yields in degenerate constraints on enhanced light Yukawa couplings. This means that the search for these couplings ought to take a non-trivial path. Enhancements of light quark Yukawa couplings would open the tree-level quark anti-quark annihilation Higgs production channel $q\bar{q}A$, which is enhanced by the presence of light quarks in the PDFs. Furthermore, it could break the degeneracy amongst the strange up and down quarks by having a *production tagging* stemming from the different distributions of the PDFs per quark flavour [291]. For sufficiently large enhancement of the light quark Yukawa couplings, this channel would even become dominant over the loop-induced gluon fusion, as seen in Figure 7.3. Working strictly in the SMEFT paradigm, the $q\bar{q}A$ channel would contain a $hhq\bar{q}$ contact interaction illustrated in Figure 7.2; this interaction further enhances the Higgs pair production more than the single Higgs $q\bar{q}A$, by a constructive interference of this topology with the s -channel one. This effect is accompanied with large light-quark PDFs for large scattering energy of Higgs pair compared to single-Higgs production. These effects make Higgs pair production more sensitive to light quark Yukawa enhancement, as Figure 7.3 indicates.

Although the ggF Higgs pair production channel in SMEFT contains diagrams with contact $hhq\bar{q}$ interaction shown in Figure 7.4, the contribution of this diagram topology is suppressed by the kinematic mass of the quarks appearing inside the loops. The ggF channel hence shows effectively no dependence on the light quark Yukawa coupling.

This chapter aims to study the potential for Higgs pair production as a direct probe channel for light quark Yukawa interaction; focusing on the first generation quarks. I will start by introducing the inclusion of light quark couplings to the Higgs in the SMEFT framework in section 7.1. Then the NLO QCD calculation of the $q\bar{q}A$ channel is shown in section 7.2. I outline, in section 7.4, a cut-based analysis of the di-Higgs final state $b\bar{b}\gamma\gamma$ to estimate the sensitivity of this channel for the HL-LHC. Later, in section 7.5 an optimised approach for enhancing the sensitivity based on multi-variant analysis and interpretable machine learning is showcased. The results of both analysis techniques are discussed and compared in section 7.6. In section 7.7 I overview the other searches for

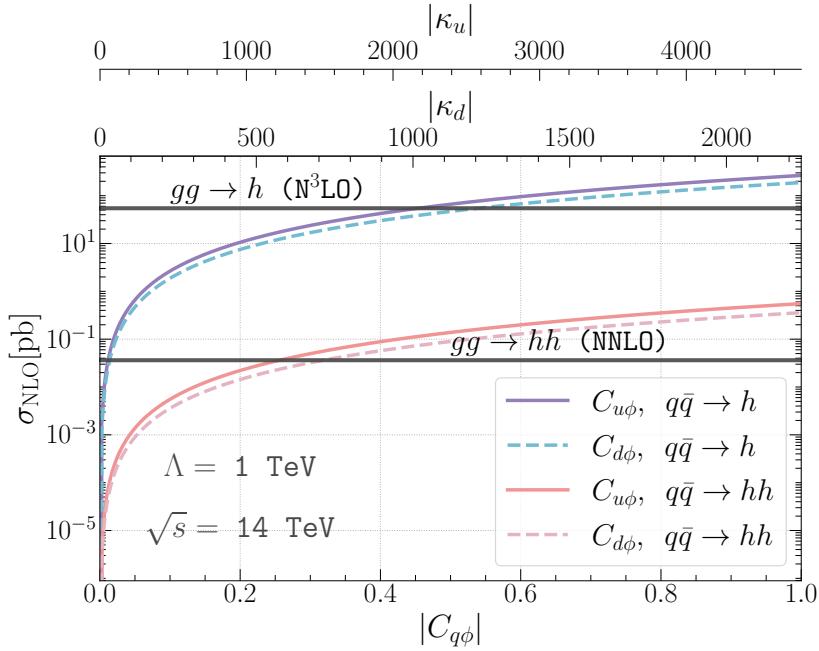


Figure 7.3. The production cross-section of single Higgs and di-Higgs at 14 TeV from the quark anti-quark annihilation $q\bar{q}A$ as a function of the Wilson coefficients $C_{u\phi}$ and $C_{d\phi}$ versus the SM gluon fusion cross-sections, the horizontal solid line for gluon fusion channels. One can observe that for values of $C_{u\phi} = 0.22$ (0.43) and $C_{d\phi} = 0.26$ (0.47) the $q\bar{q}A$ channel becomes the dominant di-Higgs (single Higgs) production channel. The NP scale is set to $\Lambda = 1$ TeV.

light Yukawa couplings, comparing them to the Higgs pair production sensitivity. This chapter is concluded in section 7.8.

The cut-based analysis has been published in [41], while the interpretable machine-learning one is an undergoing project with R. Gröber, C. Grojean, A. Paul, and Z. Qian, and expected to be published soon [227].

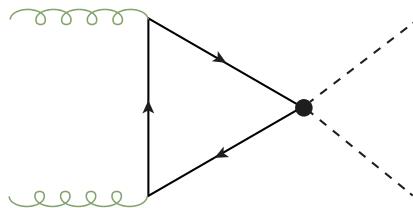


Figure 7.4. The new diagram for ggF emerging from the $hhq\bar{q}$ coupling appearing in SMEFT.

7.1 SMEFT and light Yukawa couplings

Within the SM, the Higgs couplings to quarks are described by the Lagrangian

$$\mathcal{L}_y = -y_{ij}^u \bar{Q}_L^i \tilde{\phi} u_R^j - y_{ij}^d \bar{Q}_L^i \phi d_R^j + h.c.. \quad (7.1)$$

with $\tilde{\phi} = i\sigma_2\phi^*$, σ_2 is the second Pauli matrix, ϕ denotes the Higgs doublet, Q_L^i the left-handed $SU(2)$ quark doublet of the i -th generation and u_R^j and d_R^j the right-handed up- and down-type fields of the j -th generation, respectively. Explicitly writing the flavour indices ij of the SMEFT operators and lifting the condition of their flavour universality, we could get light quark -Higgs coupling enhancement from the operators

$$\Delta\mathcal{L}_y = \frac{\phi^\dagger\phi}{\Lambda^2} \left(C_{u\phi}^{ij} \bar{Q}_L^i \tilde{\phi} u_R^j + C_{d\phi}^{ij} \bar{Q}_L^i \phi d_R^j + h.c. \right). \quad (7.2)$$

The mass matrices of the up-and down-type quarks obtained from the Yukawa and the new SMEFT coupling are

$$\begin{aligned} M_{ij}^u &= \frac{v}{\sqrt{2}} \left(y_{ij}^u - \frac{1}{2}(C_{u\phi})_{ij} \frac{v^2}{\Lambda^2} \right), \\ M_{ij}^d &= \frac{v}{\sqrt{2}} \left(y_{ij}^d - \frac{1}{2}(C_{d\phi})_{ij} \frac{v^2}{\Lambda^2} \right), \end{aligned} \quad (7.3)$$

where y_{ij}^q are the SM Yukawa matrix elements. Since the quark masses are measured quantities, one would naturally rotate to the mass basis using bi-unitary transformation represented by the matrices $\mathcal{V}_q, \mathcal{U}_q$, like in the SM. The Wilson coefficients matrix elements in the flavour space in the mass basis can be written as

$$\tilde{C}_{q\phi}^{ij} = (\mathcal{V}_q)_{ni}^* C_{q\phi}^{nm} (\mathcal{U}_q)_{mj}, \quad \text{with } q = u, d. \quad (7.4)$$

In order to match these Wilson coefficients to Higgs couplings to quarks, the Lagrangian operator describing these couplings, in the mass eigenbasis, is used

$$\mathcal{L} \supset g_{h\bar{q}_iq_j} \bar{q}_i q_j h + g_{h\bar{q}_iq_j} \bar{q}_i q_j h^2. \quad (7.5)$$

Then, one gets the matching results in identifying the SMEFT couplings of Higgs and quarks as

$$g_{h\bar{q}_iq_j} := \frac{m_{q_i}}{v} \delta_{ij} - \frac{v^2}{\Lambda^2} \frac{\tilde{C}_{q\phi}^{ij}}{\sqrt{2}}, \quad g_{hh\bar{q}_iq_j} := -\frac{3}{2\sqrt{2}} \frac{v}{\Lambda^2} \tilde{C}_{q\phi}^{ij}. \quad (7.6)$$

It is possible to observe that, in the general case, non-diagonal couplings can be generated. However, such couplings are strongly constraint by flavour observables, particularly

neutral meson mixing [292],

$$|\tilde{C}_{q\phi}^{12}| \lesssim 10^{-5} \Lambda^2/v^2 \quad |\tilde{C}_{d\phi}^{13/23}| \lesssim 10^{-4} \Lambda^2/v^2. \quad (7.7)$$

Due to these strong constraints, flavour violation (MFV) [293] is often implemented into SMEFT. In MFV, the SM Yukawa matrices y_q^{ij} are the only spurions breaking the global $SU(3)_Q \otimes SU(3)_U \otimes SU(3)_D \rightarrow U^6(1)$ flavour symmetry. This implies that the Wilson coefficients matrices in the mass basis are simultaneously diagonalisable with the SM Yukawa matrices and inherit their hierarchy. Therefore, MFV is not a viable scheme for considering significant enhancements to the couplings for first and second generations while keeping the third generation couplings unchanged.

In order to bypass the constraints of MFV and also avoid flavour changing neutral currents (FCNC) that are prohibited by flavour observables, one can turn to flavour alignment [294, 295] or its generalisation aligned flavour violation (AFV) [296]. With flavour alignment schemes, the NP flavour parameters (here the Wilson coefficients) are aligned with the SM Yukawa, such that both can be simultaneously diagonalised, thus preventing tree-level FCNCs. Contrary to MFV, the duress of making these new parameters proportional to the SM Yukawa couplings is lifted. This would induce radiative FCNCs, as this formalism is unstable under quantum corrections [297–299]. This alignment breaking would not be seen in the SMEFT but rather when UV-complete models are considered. AFV resolves this instability by ensuring that any NP Spurion breaking the flavour symmetry will transform trivially under the quark phases transformations $U^6(1)$, keeping the CKM matrix the only flavour object that has non-trivial transformations. Thereby the CKM will have physical flavour changing currents as well as a \mathcal{CP} -violating phase. This constraint on the NP flavour spurions k_q , allows them to be written as a series in powers of the CKM matrix, known as the alignment expansion

$$k_u = K_{0,u} + K_{1,u} V_{CKM}^* K_{2,u} V_{CKM}^T K_{3,u} + \mathcal{O}(V_{CKM}^4) + \dots, \quad (7.8)$$

$$(k_d)^\dagger = K_{0,d} + K_{1,d} V_{CKM}^T K_{2,d} V_{CKM}^* K_{3,d} + \mathcal{O}(V_{CKM}^4) + \dots, \quad (7.9)$$

where $K_{i,u}$ and $K_{i,d}$ are complex 3×3 diagonal matrices invariant under flavour transformations. This formalism is stable under renormalisation group evolution as any linear combinations, or tensor products of the spurions will remain flavour aligned.

For simplicity, I shall only consider the first term in the alignment expansion, such that only diagonal $C_{q\phi}$ are investigated, as the other terms are already CKM-suppressed and not of particular phenomenological interest for the considered processes. With this in mind, and using the translation between SMEFT and κ -formalism discussed in subsection 2.2.2, it is possible to identify the couplings in SMEFT with the κ 's

$$g_{h\bar{q}_iq_i} = \kappa_q g_{h\bar{q}_iq_i}^{\text{SM}}, \quad g_{hh\bar{q}_iq_i} = -\frac{3}{2} \frac{1-\kappa_q}{v} g_{h\bar{q}_iq_i}^{\text{SM}}, \quad (7.10)$$

in a slight abuse of language of the κ -formalism as the $hh\bar{q}\bar{q}$ coupling typically is not included in it.

Higgs pair production offers an extra advantage for probing light Yukawa interactions, as it is susceptible to the $hhq\bar{q}$ interaction; one could also consider the non-linear HEFT by extending it to include Wilson coefficients c_q and c_{qq} for the first and second-generation quarks, in analogy to ones defined for the top quark in eq. (2.8) [300]. The analysis performed on these HEFT parameters is published in [41].

7.2 Higgs pair production and Higgs decays with modified light Yukawa couplings

As we have briefly discussed in the introduction, the gluon fusion channel of Higgs pair production is affected by enhanced light Yukawa couplings in two ways: First is the inclusion of light quark loops in the triangle and box diagrams. Second, the new diagrams introduced by the contact $hhq\bar{q}$ coupling are shown in Figure 7.4. However, these effects are both negligible due to the mass-suppression of these diagrams by the light quark appearing in the loops. Therefore, effectively, one could consider the ggF channel as purely derived by third-generation quarks.

7.2.1 Higgs pair production via quark anti-quark annihilation

In the SM, the $q\bar{q}A$ channel is severely suppressed by the small Yukawa coupling of the first generation quarks. In fact, if these quarks are considered massless, like in the 5-flavour scheme, this channel vanishes in the SM. There are four-diagrams contributing to $q\bar{q}A$ shown in Figure 7.2. Computing the matrix-elements for them gives the differential partonic cross-section

$$\frac{d\hat{\sigma}_{q_i\bar{q}_j}}{d\hat{t}} = \frac{1}{16\pi} \frac{1}{12\hat{s}} \left[\left| 2g_{hhq_i\bar{q}_j} + \frac{g_{hhh} g_{hq_i\bar{q}_j}}{\hat{s} - m_h^2 - im_h\Gamma_h} \right|^2 + \mathcal{O}(g_{hq_i\bar{q}_j}^4) \right], \quad (7.11)$$

where the $\mathcal{O}(g_{hq_i\bar{q}_j}^4)$ terms stem from the \hat{t} - and \hat{u} -channel diagrams, and their contribution is typically only $\sim 0.1\%$ of the total cross-section.

The hadronic cross section is then obtained by

$$\sigma_{\text{hadronic}} = \int_{\tau_0}^1 d\tau \int_{\hat{t}_-}^{\hat{t}_+} d\hat{t} \sum_{i,j} \frac{d\mathcal{L}^{q_i\bar{q}_j}}{d\tau} \frac{d\hat{\sigma}_{q_i\bar{q}_j}}{d\hat{t}}, \quad (7.12)$$

with $\tau_0 = 4m_h^2/s$, $\hat{s} = \tau s$ and

$$\hat{t}_\pm = m_h^2 - \frac{\hat{s}(1 \mp \beta)}{2} \quad \text{and} \quad \beta = \sqrt{1 - \frac{4m_h^2}{\hat{s}}}. \quad (7.13)$$

The parton luminosity is given by

$$\frac{d\mathcal{L}^{q_i\bar{q}_j}}{d\tau} = \int_\tau^1 \frac{dx}{x} \left[f_{q_i}(x/\tau, \mu_F^2) f_{\bar{q}_j}(x, \mu_F^2) + f_{\bar{q}_j}(x/\tau, \mu_F^2) f_{q_i}(x, \mu_F^2) \right]. \quad (7.14)$$

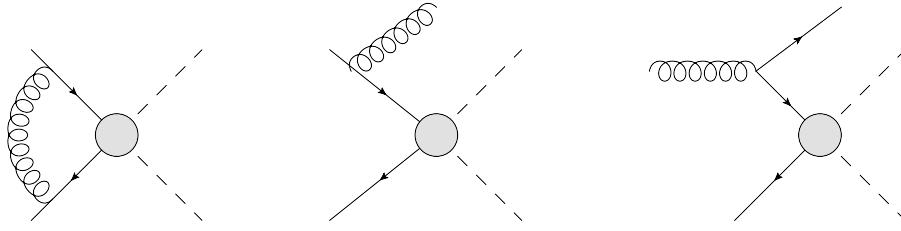


Figure 7.5. Generic form of the QCD corrections of order $\mathcal{O}(\alpha_s)$ to the $q\bar{q}A$ Higgs pair production.

All the kinematic masses were neglected, following the 5-flavour scheme of the PDFs, while the coupling of the Higgs boson to the light quarks (for flavour diagonal couplings) is

$$g_{hq_i\bar{q}_j} = \frac{m_q^{\overline{MS}}(\mu_R)}{v} \kappa_q \delta_{ij}, \quad (7.15)$$

and analogously for the $g_{hhq_i\bar{q}_j}$ coupling. It is worth noting that there is no inconsistency with such an assumption since, in scenarios of modified Yukawa couplings, the masses of the quarks need not be generated by electroweak symmetry breaking.

NLO QCD correction

Since the ggF NLO QCD corrections are sizeable, it is reasonable to assume that the same would apply to the $q\bar{q}A$ amplitude. Computing the NLO QCD corrections to this channel is a relatively straightforward task. More simplifications can be made by neglecting the NLO corrections of the \hat{t} and \hat{u} channels because they are strongly suppressed. This enables us to adapt the NLO QCD corrections results from $b\bar{b} \rightarrow h$ in the 5-flavour scheme [301–303], also for $b\bar{b}hh$ [304, 305], to the s -channel and contact term $q\bar{q}A$ diagrams. This is achieved by some adjustments taking into account the modified LO cross-section and the different kinematics of the process. The Feynman diagrams at NLO QCD are shown in Figure 7.5. The NLO corrections are given by [306]

$$\sigma(q\bar{q} \rightarrow h) = \sigma_{LO} + \Delta\sigma_{q\bar{q}} + \Delta\sigma_{qg}, \quad (7.16a)$$

$$\Delta\sigma_{q\bar{q}} = \frac{\alpha_s(\mu_R)}{\pi} \int_{\tau_0}^1 d\tau \sum_q \frac{d\mathcal{L}^{q\bar{q}}}{d\tau} \int_{\tau}^1 dz \hat{\sigma}_{LO}(Q^2 = z\tau s) \omega_{q\bar{q}}(z), \quad (7.16b)$$

$$\Delta\sigma_{qg} = \frac{\alpha_s(\mu_R)}{\pi} \int_{\tau_0}^1 d\tau \sum_{q,\bar{q}} \frac{d\mathcal{L}^{qg}}{d\tau} \int_{\tau}^1 dz \hat{\sigma}_{LO}(Q^2 = z\tau s) \omega_{qg}(z), \quad (7.16c)$$

and

$$\hat{\sigma}_{LO}(Q^2) = \int_{\hat{t}_-}^{\hat{t}_+} \frac{d\hat{\sigma}_{q_i\bar{q}_j}}{d\hat{t}}, \quad (7.17)$$

with $z = \tau_0/\tau$, $\sigma_{LO} = \sigma_{\text{hadronic}}$ of eq. (7.12), and the ω factors are given by

$$\begin{aligned}\omega_{q\bar{q}}(z) &= -P_{qq}(z) \ln \frac{\mu_F^2}{\tau s} + \frac{4}{3} \left\{ \left(2\zeta_2 - 1 + \frac{3}{2} \ln \frac{\mu_R^2}{M_{hh}^2} \right) \delta(1-z) \right. \\ &\quad \left. + (1+z^2) \left[2\mathcal{D}_1(z) - \frac{\ln z}{1-z} \right] + 1-z \right\},\end{aligned}\quad (7.18a)$$

$$\omega_{qg}(z) = -\frac{1}{2} P_{qg}(z) \ln \left(\frac{\mu_F^2}{(1-z)^2 \tau s} \right) - \frac{1}{8} (1-z)(3-7z), \quad (7.18b)$$

with $\zeta_2 = \frac{\pi^2}{6}$. The Altarelli Parisi splitting functions $P_{qq}(z)$ and $P_{qg}(z)$ [307–309] are given by

$$P_{qq}(z) = \frac{4}{3} \left[2\mathcal{D}_0(z) - 1 - z + \frac{3}{2} \delta(1-z) \right], \quad (7.19a)$$

$$P_{qg} = \frac{1}{2} \left[z^2 + (1-z)^2 \right], \quad (7.19b)$$

and the “plus” distribution is

$$\mathcal{D}_n(z) := \left(\frac{\ln(1-z)^n}{1-z} \right)_+. \quad (7.20)$$

The renormalisation scale $\mu_R = M_{hh}$ and the factorisation scale $\mu_F = M_{hh}/4$, were chosen as central values.

The NLO $q\bar{q}A$ cross-section as well as the LO ggF were implemented in a private FORTRAN code and NNPDF30 parton distribution functions (PDF’s)[269] available through the LHAPDF-6 package [310]. For the one-loop integrals appearing in the form-factors of the box and triangle diagrams, I have used the COLLIER library [311] to ensure numerical stability of the loop integral calculation for massless quarks inside the loops¹. The resulting NLO K -factor was found to be

$$K_{NLO} = \frac{\sigma_{NLO}}{\sigma_{LO}} = 1.28 \pm 0.02, \quad (7.21)$$

with the error denoting the theoretical uncertainty. The K -factor does not depend on the scaling of the couplings nor the flavour of the initial $q\bar{q}$ since the LO cross-section factors out (except for the different integration in the real contributions).

7.2.2 Higgs decays

The same way hh production acquires additional channels due to enhanced Yukawa couplings, also Higgs decays to light quarks will become significant compared to the SM

¹I have expanded the code to include other SMEFT operators, and it can be found in the GitHub repository https://github.com/Alasfar-lina/HH_XS_in_SMEFT.

scenario [262]. In addition, loops of light quarks will contribute to the decays $h \rightarrow \gamma\gamma/Z\gamma$ and $h \rightarrow gg$, though this effect is small. Since the $h \rightarrow q\bar{q}$ decay are near impossible to detect with the current technologies, the effect of opening these decay channels is reduction in the branching ratios of the Higgs final states of experimental interest, like $h \rightarrow b\bar{b}$ and $h \rightarrow \gamma\gamma$.

In order to compute the Higgs partial widths and branching ratios (BR) at higher orders in QCD, I have modified the FORTRAN programme `HDECAY` [312, 313] to include the light fermion decay channels and loops in the above-mentioned decays². The overall change of the Higgs total width is given by

$$\Gamma_H \approx \Gamma_{\text{SM}} + \sum_{q=c,s,u,d} \frac{g_{h\bar{q}_iq_i}^2}{(g_{h\bar{q}_iq_i}^{\text{SM}})^2} \Gamma_q, \quad (7.22)$$

where Γ_q can be obtained at NLO QCD from the modified `HDECAY` code. Detailed results for the Branching ratios for the final states of interest have been published in [41].

In fig. 7.6 I show the branching ratios of phenomenological interest, denoted by \mathcal{B} . Once the light quark Yukawa couplings are increased (shown for the different quarks by the different coloured lines) the BRs to $b\bar{b}b\bar{b}$, $b\bar{b}\gamma\gamma$ and $b\bar{b}\tau^+\tau^-$ decrease due to the increased Higgs width. Instead the $\mathcal{B}(hh \rightarrow c\bar{c}\gamma\gamma)$ first increases with increasing κ_c , but starts decreasing after reaching a maximum around $\kappa_c \approx 8$, where the $\mathcal{B}(h \rightarrow c\bar{c})$ asymptotically reaches unity while the $\mathcal{B}(h \rightarrow \gamma\gamma)$ continues decreasing.

In order to have a preliminary estimate about the sensitivity of Higgs pair production to light Yukawa enhancements, it is important to consider both production and decay effects in terms of signal strength

$$\mu_i := \frac{\sigma \text{BR}_i}{\sigma^{\text{SM}} \text{BR}_i^{\text{SM}}}. \quad (7.23)$$

Comparing the production of single Higgs to Higgs pair signal strengths, for any final state of interest, we could see in Figure 7.7 that for first-generation $C_{q\phi} \lesssim 0.8$ Higgs pair production has a higher signal strength than single-Higgs production despite having double the reduction in the signal strength from the decays of two Higgs bosons as opposed to a single one. In fact, as we shall see in section 7.7, values of $C_{q\phi} > 0.4$ have been already excluded by multiple searches.

7.3 Event generation for the final state $hh \rightarrow b\bar{b}\gamma\gamma$

For this study, the final state $b\bar{b}\gamma\gamma$ is considered, as this channel has the most potential for Higgs pair searches [133]. It includes the small albeit “clean” $h \rightarrow \gamma\gamma$ decay, combined with the other Higgs decay to b -quark pair having the largest branching ratio $\sim 58\%$. Furthermore, the b -tagging capabilities for ATLAS and CMS are continuously improving.

²The modified `HDECAY` code can be found in the GitHub repository https://github.com/Alasfar-Lina/hdecay_lightflavour.

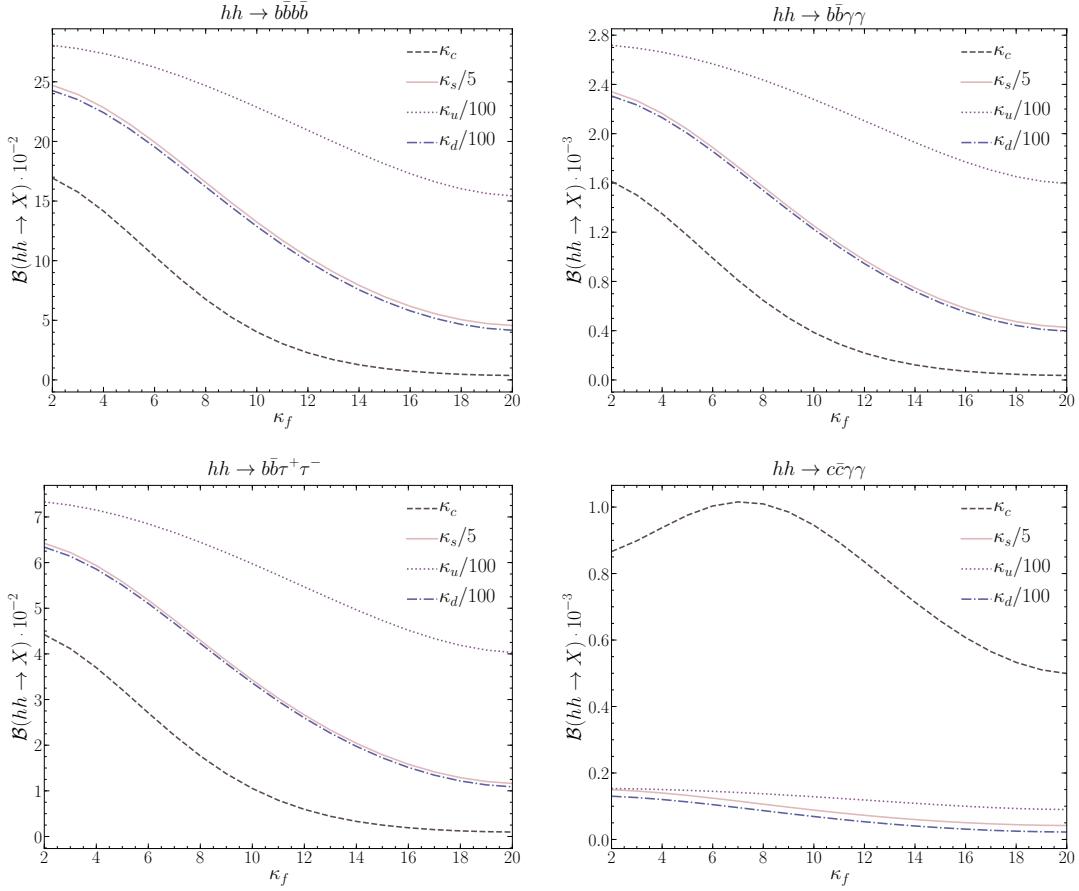


Figure 7.6. Different Higgs pair final states BRs including state-of-the-art QCD corrections as functions of the coupling modification factors κ_f . *Top left:* $hh \rightarrow b\bar{b}b\bar{b}$. *Top right:* $hh \rightarrow b\bar{b}\gamma\gamma$. *Bottom left:* $hh \rightarrow b\bar{b}\tau^+\tau^-$. *Bottom right:* $hh \rightarrow c\bar{c}\gamma\gamma$. This figure is published in [41].

For the cut-based analysis, the FORTRAN codes used to compute the hh cross-section and decay have been interfaced with **Pythia** 6.4 [314], where the $q\bar{q}A$ process was generated at NLO and the ggF at LO, then multiplied with the NLO K-factor. The generated events were written to a ROOT file via **RootTuple** tool [315] for further analysis. The backgrounds were not simulated for this analysis; rather, the results from [316] were used because we have used the same cuts as this reference.

For the multivariate analysis based on interpretable BDT, the backgrounds and signal events needed to be generated. The backgrounds described in Table 6.3 were generated using **MadGraph_aMC@NLO** [166], then showered via **Pythia** 8.3 [317] and a fast detector simulation is done using **Delphes** 3 [318], the QED/QCD background $b\bar{b}\gamma\gamma$, Zh and $b\bar{b}h$ events were taken from the analysis data of ref. [43], while $t\bar{t}h$ events were generated specifically for this analysis. In order to obtain the NLO cross-section for these processes, the events were multiplied by their respective K -factors that have been ob-

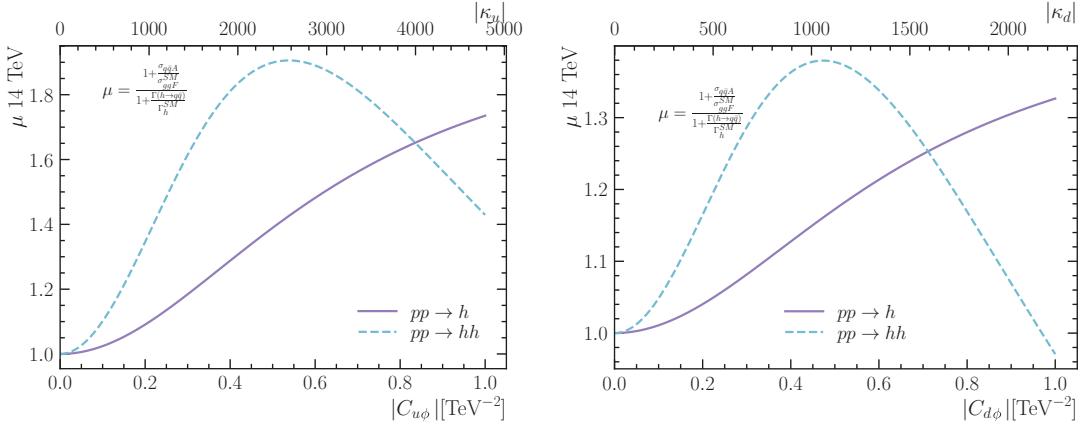


Figure 7.7. Signal strengths at 14 TeV LHC, of the single Higgs (purple solid line) vs. Higgs pair (blue dashed line) as functions of $C_{u\phi}$ (left) and $C_{d\phi}$ (right). Both plots show that for $C_{q\phi} \lesssim 0.8$ the signal strength of Higgs pair production is higher than the single Higgs one. This implies that Higgs pair production is more sensitive to enhancements of light quark Yukawa in SMEFT. This is independent of the final state (except for $h \rightarrow q\bar{q}$, where $q = u$ for the left plot and $q = d$ for the right one).

tained from $t\bar{t}h$ [319], $b\bar{b}\gamma\gamma$ [320], Zh [321] and the remaining part of the $b\bar{b}h$ processes from [322].

The Higgs pair signals were generated in a slightly different pipeline. The ggF channel events were simulated first using **POWHEG** [103, 256, 257], which has been modified to separate the individual contributions from the box, triangle, and their interference. This is done to easily scale by κ_λ (or C_ϕ), as the box does not depend on it, while the triangle and the interference have quadratic and linear dependence, respectively. The $q\bar{q}A$ channel events were generated via **MadGraph_aMC@NLO** using a model created with **FeynRules** [206]. Samples for both up-and down-quark initiated $q\bar{q}A$ processes have been generated. Parton showering and fast detector simulation for both Higgs pair processes were run through the same pipeline as the backgrounds. Events were multiplied with the K -factor at NLO ($q\bar{q}A$) and NNLO (ggF) after event generation. The Higgs bosons were decayed with the assumption of narrow width approximation, and the BR values were computed in the modified **HDECAY** code.

To be inclusive and to explore the capabilities and importance of the full detector coverage, no generator-level cuts were applied on these processes except for the $b\bar{b}\gamma\gamma$ to avoid divergences. These minimal generator-level cuts for $b\bar{b}\gamma\gamma$ are

$$\begin{aligned} Xp_T^b &> 20 \text{ GeV}, \\ \text{generator level cuts: } &\eta_\gamma < 4.2, \Delta R_{b\gamma} > 0.2, \\ &100 < m_{\gamma\gamma} (\text{GeV}) < 150. \end{aligned} \tag{7.24}$$

Here Xp_T^b implies a minimum p_T cut for at least one b -jet. After the showering and

Channel	LO σ [fb]	K -fact.	Order	6 ab^{-1} [#evt @ order]
$hh_{\text{tri}}^{\text{ggF}}$	$7.288 \cdot 10^{-3}$	2.28		96
$hh_{\text{box}}^{\text{ggF}}$	0.054	1.98	NNLO	680
$hh_{\text{int}}^{\text{ggF}}$	-0.036	2.15		-460
$u\bar{u}\text{A}$ ($C_{d\phi} = 0.1$)	2.753	1.29	NLO	28
$d\bar{d}\text{A}$ ($C_{u\phi} = 0.1$)	4.270	1.30		43

Table 7.1. The LO cross-section for Higgs pair production processes (including the decay $hh \rightarrow b\bar{b}\gamma\gamma$) for 6 ab^{-1} 14 TeV HL-LHC.

detector simulation, further basic selection cuts were applied to select events with

$$\begin{aligned} \text{basic cuts: } & n_{\text{eff}}^{b\text{jet}} \geq 1, \quad n_{\text{eff}}^{\gamma\text{jet}} \geq 2, \\ & p_T^{b\text{jet}} > 30 \text{ GeV}, \quad p_T^{\gamma\text{jet}} > 5 \text{ GeV}, \\ & \eta_{b\text{jet}, \gamma\text{jet}} < 4, \quad 110 \text{ GeV} < m_{\gamma_1\gamma_2} < 140 \text{ GeV}, \end{aligned} \quad (7.25)$$

and $n_{\text{eff}}^{b/\gamma\text{jet}}$ representing the number of b/γ -jets that pass the basic selection. The cross-section, K -factors, number of events with 6 ab^{-1} luminosity at 14 TeV are given in Table 6.3 for the background and in Table 7.1 for the Higgs pair signals.

Both analysis methods included sensitivity studies for the HL-LHC, i.e. 14 TeV and 6 ab^{-1} ³ luminosity and projections for a future hadron circular collider (FCC-hh), with 100 TeV and the luminosity of 30 ab^{-1} have been made for the ML-based analysis. The results for the FCC can be found in the Appendix C.

7.4 Cut-based analysis

A cut and count analysis has been performed mainly as a “proof of concept” to demonstrate the sensitivity of Higgs pair production for probing light quark Yukawa couplings. The analysis used the same cuts and m_{hh} binning as ref. [316] such that their background events counts can be used.

7.4.1 Analysis strategy

The number of expected background N_b and signal N_s events needs to be estimated from simulated events to derive sensitivity bounds. Since N_b is taken from [316], the task is to estimate N_s for the $q\bar{q}\text{A}$ process as a function of $C_{q\phi}$, and to reproduce N_s of the ggF SM process published in the reference as a cross-check.

Since the cross-section, branching fraction and the integrated luminosity are readily available, it is only needed to estimate the selection efficiency ϵ_{SEL} from the applied cuts

³In the published cut-based analysis [41] 3 ab^{-1} luminosity for the HL-LHC were used. However, here I used 6 ab^{-1} when reporting fit results

cut	ϵ_{cut}	$\delta\epsilon_{\text{cut}}$
Trigger-level in eq. (7.26) and (7.27)	0.71	0.04
p_T cuts in eq. (7.28)	0.35	0.07
ΔR cuts in eq. (7.29)	0.69	0.21
total	0.11	0.06

Table 7.2. The cuts used in the analysis with their efficiency ϵ_{cut} and uncertainties on these efficiencies $\delta\epsilon_{\text{cut}} = \sqrt{\epsilon(1-\epsilon)N}$, where N is the total number of events. The analysis was performed on 100K SM simulated events.

to obtain the number of signal events. The basic cuts of trigger-level selection are jets and photons with minimal p_T and maximal η ,

$$p_T(\gamma/j) > 25 \text{ GeV}, \quad |\eta(\gamma/j)| < 2.5. \quad (7.26)$$

Additionally, a veto on the events with hard leptons is applied

$$p_T(\ell) > 20 \text{ GeV}, \quad |\eta(\ell)| < 2.5. \quad (7.27)$$

Jets were clustered using `fastjet` [323] with the anti-kt algorithm with a radius parameter of $R = 0.5$.

The b -tagging efficiency of $\epsilon_b = 0.7$, as well as the photon identification efficiency $\epsilon_\gamma = 0.8$ have been simulated in accordance with the ATLAS and CMS performance [324–326, 326, 327]. The selection cuts we used are the same ones as in [316], starting with the cuts of the transverse momentum p_T of the photons and b -tagged jets. The two hardest photons/ b -tagged jets, with transverse momentum $p_{T>}$, and the softer ones with $p_{T<}$ are selected to satisfy

$$p_{T>}^>(b/\gamma) > 50 \text{ GeV}, \quad \text{and} \quad p_{T<}^>(b/\gamma) > 30 \text{ GeV}. \quad (7.28)$$

In order to ensure well-separation of the photons and b -jets, we required the following cuts on the jet radius,

$$\Delta R(b, b) < 2, \quad \Delta R(\gamma, \gamma) < 2, \quad \Delta R(b, \gamma) > 1.5. \quad (7.29)$$

The mass windows used are about three times the photon resolution of ATLAS and CMS [326, 327], such wide windows were used in order to avoid signal loss

$$105 \text{ GeV} < m_{b\bar{b}} < 145 \text{ GeV}, \quad 123 \text{ GeV} < m_{\gamma\gamma} < 130 \text{ GeV}. \quad (7.30)$$

The selection cuts are summarised in table [Table 7.2](#) with their corresponding efficiency.

The total selection efficiency for the ggF channel was found to be $\epsilon_{SEL}^{ggF} = 0.044$, consistent with the results of [316], while the $q\bar{q}A$ channel efficiency is slightly higher

$\epsilon_{SEL}^{qq} = 0.05 \pm 0.001$ for the up and down quark initiated $q\bar{q}A$, results for second generation quarks can be found in [41].

7.4.2 Statistical analysis

The likelihood ratio test statistic q_μ was used in order to estimate the HL-LHC sensitivity, and set projected limits on the SMEFT Wilson coefficients $C_{q\phi}$, with and without the modifier of the trilinear coupling C_ϕ ⁴. The likelihood function was constructed from the signal and background events in each bin of the m_{hh} distribution described in [316]

$$-\ln \mathcal{L}(\mu) = \sum_{i \in \text{bins}} (N_{bi} + \mu N_{si}) - n_i \ln(N_{bi} + \mu N_{si}), \quad (7.31)$$

with N_{bi} and N_{si} being the number of background and signal events in the i th m_{hh} distribution, respectively. In order to include the theoretical uncertainties on the expected number of signal events, the above likelihood was extended by a Gaussian distribution for N_{si} in which the mean equals to the central value of the bin values and standard deviation σ equals to its theoretical uncertainty. The signal strength μ was then estimated by minimising $-\ln \mathcal{L}(\mu)$ to obtain the estimator for $\hat{\mu}$ by injecting SM signal plus background events n_i . The test statistic is then given by

$$q_\mu = 2(\ln \mathcal{L}(\mu) - \ln \mathcal{L}(\hat{\mu})), \quad (7.32)$$

following the procedure described in [328], and using the Python package `pyhf` [329, 330]. The expected 6 ab^{-1} HL-LHC sensitivity for the signal strength at 95% (68%) CL is found to be $\mu = 1.5(1.1)$.

7.4.3 Charm-tagging and second generation bounds

In order to utilise Higgs pair production in setting bounds on the second generation Yukawa coupling, it is possible to use the method developed in [331, 332] that re-analyses final states with b -quarks based on the mistagging of c -jets as b -jets in associated VH production. The analysis relies on the current CMS [333] and ATLAS [334] working points for b -tagging, as illustrated in the Table 7.3. The signal strength estimator when considering the mistagging probability of b -jets to c -jets (i.e. c -jet contamination of b -tagged jets) $\epsilon_{b \rightarrow c}$ is

$$\hat{\mu} = \frac{\sigma_{hh} \mathcal{B}_b \epsilon_{b1} \epsilon_{b2} \epsilon_f + \sigma_{hh} \mathcal{B}_c \epsilon_{b \rightarrow c,1} \epsilon_{b \rightarrow c,2} \epsilon_f}{\sigma_{hh}^{\text{SM}} \mathcal{B}_b^{\text{SM}} \epsilon_{b1} \epsilon_{b2}}, \quad (7.33)$$

with ϵ_f being the efficiency of the aforementioned cuts. The above expression simplifies to

$$\hat{\mu} = \mu_b \epsilon_f + 0.05 \cdot \left(\epsilon_{c/b}^{\text{b-tag}} \right)^2 \epsilon_f \cdot \mu_c, \quad (7.34)$$

⁴Additionally the HEFT parameters c_q and c_{qq} were studied, the results can be found in the published paper [41].

Detector	Cuts (1st, 2nd) b -jets	$\epsilon_{c/b}^{\text{b-tag}}{}^2$
CMS	Med1-Med1	0.18
CMS	Med1-Loose	0.23
ATLAS	Med-Med	$8.2 \cdot 10^{-2}$
ATLAS	Tight-Tight	$5.9 \cdot 10^{-3}$

Table 7.3. The b -tagging working points used in the analysis, for CMS [333] and ATLAS [334]. This table is published in [41].

for $\mathcal{B}_c^{\text{SM}}/\mathcal{B}_b^{\text{SM}} \approx 0.05$. The signal strength modifier of the $b\bar{b}\gamma\gamma$ final state is denoted by μ_b and the one of the $c\bar{c}\gamma\gamma$ final state by μ_c . The ratio of tagging efficiencies is defined as

$$\left(\epsilon_{c/b}^{\text{b-tag}}\right)^2 = \frac{\epsilon_{b\rightarrow c,1}\epsilon_{b\rightarrow c,2}}{\epsilon_{b1}\epsilon_{b2}}. \quad (7.35)$$

One b -tagging working point could only constrain either μ_b or μ_c . In order to resolve the flat direction several b -tagging working points $\left(\epsilon_{c/b}^{\text{b-tag}}\right)^2$ are needed.

When the fit is performed on this signal strength with charm mistagging probability, we obtain the upper projected limit on the charm final state signal strength after profiling over μ_b ,

$$\mu_c(\text{up}) = 36.6 \text{ (68\% CL)}, \quad \mu_c(\text{up}) = 74.8 \text{ (95\% CL)}. \quad (7.36)$$

However, the obtained sensitivity is not sufficient to set any better limits at 95% CL than the existing ones (or projected ones in other channels) for the Yukawa coupling modifiers κ_c , and κ_s . Instead, it is possible to improve on them by introducing c -tagging working points $(\epsilon_{c/b}^{\text{c-tag}})^2$

$$\left(\epsilon_{c/b}^{\text{c-tag}}\right)^2 = \frac{\epsilon_{c1}\epsilon_{c2}}{\epsilon_{c\rightarrow b,1}\epsilon_{c\rightarrow b,2}}, \quad (7.37)$$

mixed with the b -tagging ones. We denote the contamination of c -jets with b -jets by $\epsilon_{c\rightarrow b}$. For mixed tagging, the signal strength estimator becomes

$$\hat{\mu} = \frac{\sigma_{hh}\mathcal{B}_b\epsilon_{b1}\epsilon_{b2}\epsilon_f + \sigma_{hh}\mathcal{B}_c\epsilon_{c1}\epsilon_{c2}\epsilon_f}{\sigma_{hh}^{\text{SM}}\mathcal{B}_b^{\text{SM}}\epsilon_{b1}\epsilon_{b2} + \sigma_{hh}^{\text{SM}}\mathcal{B}_c^{\text{SM}}\epsilon_{c1}\epsilon_{c2}}, \quad (7.38)$$

where now ϵ_b is either ϵ_b or $\epsilon_{c\rightarrow b}$ and ϵ_c either ϵ_c or $\epsilon_{b\rightarrow c}$. This simplifies to

$$\hat{\mu} = \frac{\mu_b + 0.05\epsilon_{c/b}^2\mu_c}{1 + 0.05\epsilon_{c/b}^2}\epsilon_f. \quad (7.39)$$

The working point $\epsilon_{c/b}^2$ could be the b -tagging or c -tagging working point.

Assuming that c -tagging and b -tagging are uncorrelated, and working with the methods discussed in [331, 335], i.e. combining the ATLAS medium cuts (med.) for b -tagging with the c -tagging working points in order to break the degeneracy, we could improve the 95% CL sensitivity on μ_c . We start by the c -tagging working point used by the ATLAS

<i>c</i> -tagging working point	ϵ_c	$\epsilon_{c \rightarrow b}$	μ_c (up)	95% CL
<i>c</i> -tag I [336, 337]	19%	13%		10.1
<i>c</i> -tag II [338, 339]	30%	20%		8.2
<i>c</i> -tag III [338, 339]	50%	20%		3.8

Table 7.4. The *c*-tagging working points with the expected 95% CL upper limit (sensitivity) of μ_c obtained after profiling over μ_b . This table is published in [41].

collaboration in Run I searches for top squarks decays to charm and neutralino [336, 337], which we refer to as *c*-tagging I.

Further *c*-tagging working points from the HL-LHC upgrade are used: with the expected insertable B-layer (IBL) sub-detector that is to be installed during the ATLAS HL-LHC upgrade [338, 339], the new *c*-tagging II and III points, as illustrated in Table 7.4, can be identified. In fig. ?? we used them to obtain in combination with the ATLAS med *b*-tagging expected 95% CL upper limits on μ_c for the HL-LHC from an analysis of the final state $b\bar{b}\gamma\gamma$.

7.5 Optimised search for Higgs pair via Interpretable machine learning

When dealing with a multivariate problem, such as separating the Higgs pair signal from its backgrounds, using “simple” cuts is not the most efficient method for accomplishing this task. This is mainly because the various features used in the classification correlate with each other in multivariate analyses, and making simple cuts, like in the previous section, would not capture this correlation. On the other hand, with a BDT or a random forest classifier, it is possible to capture these correlations and introduce highly non-trivial cuts. For this analysis the features are the kinematic distributions of the Higgs pair decay products and the backgrounds.

7.5.1 Constructing features

The simulated events of the signal and background described in the event selection section are required to contain at least two reconstructed photons and a *b*-tagged jet. From these events, the following high-level features were constructed

- $p_T^{b_1}, p_T^{b_2}, p_T^{\gamma_1}, p_T^{\gamma_2},$
- $\eta_{b_{j1}}, \eta_{b_{j2}}, \eta_{\gamma_1}, \eta_{\gamma_2},$
- $n_{bjet}, n_{jet}, \Delta R_{\min}^{b\gamma}, \Delta\varphi_{\min}^{bb},$
- $m_{\gamma\gamma}, m_{bb}, m_{b_1h}, m_{b\bar{b}h}, H_T.$

Here, $p_T^{b/\gamma_{1,2}}$ and $\eta^{b/\gamma_{1,2}}$ are the transverse momentum and pseudorapidity for the tagged leading and sub-leading *b*/ γ -jets (in this definition the subleading *b*-jet could be a null

four-vector since I require to only have at least one b -jet inclusive), n_{bj} is the number of tagged and passed b -jets. $\Delta R_{\min}^{b\gamma}$ and $\Delta\varphi_{\min}^{bb}$ are the minimum jet-distance and φ -angle between a tagged b -jet and a photon jet. The remaining variables are the invariant masses, and H_T is the scalar sum of the transverse mass of the system.

These features are the same as those studied in ref. [43] for $b\bar{b}h$. However, they are, by no means, unique. It is possible to run the analysis with another set of features and obtain the same results, as long as these features are independent and highly correlated. Figure 7.8 shows the distributions four most important features from this list, the $m_{\gamma\gamma}$ is very important in distinguishing the large $b\bar{b}\gamma\gamma$ background from the signal and $t\bar{t}h$ (or other background that contain $h \rightarrow \gamma\gamma$), while the rest, particularly H_T , distinguishes the different hh channels and also hh from other Higgs channels backgrounds.

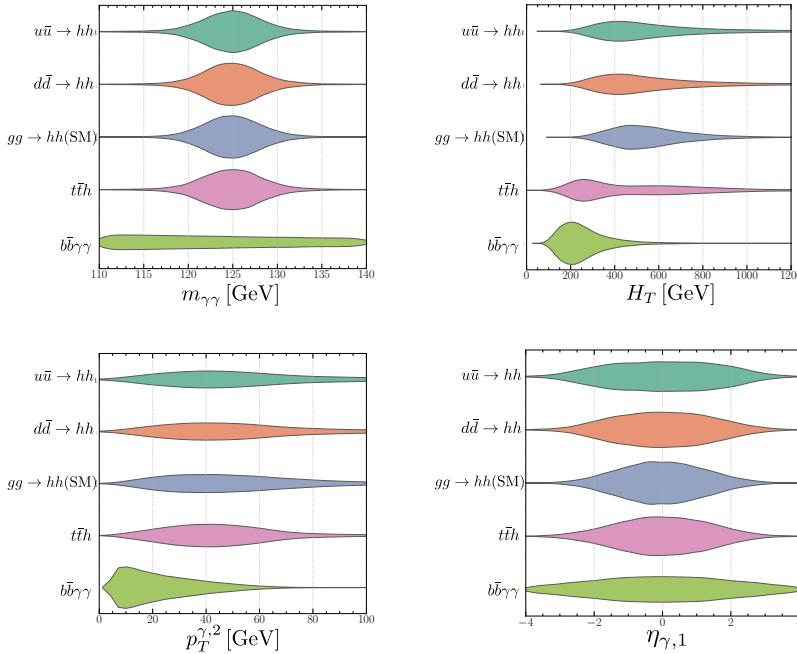


Figure 7.8. Violin plots showing the distributions of the most significant features used by the BDT classifier for the signal channels, and the two most significant backgrounds $b\bar{b}\gamma\gamma$.

7.5.2 Exploratory network analysis

The aim of this analysis is to explore how the kinematic variables constructed in the previous section are related to each other. Furthermore, we are interested in examining their variation across the channels. This can be achieved by calculating the intra-feature correlations stratified according to the signal types (ggF , $u\bar{u}A$, $d\bar{d}A$) or a background. This correlation will play the role of the effect measure of these features across the different channels. The correlations can be represented as network diagrams as seen

in of Figure 7.9. The Pearson’s correlation networks show some differences amongst the different signal strata⁵. These differences can be further investigated by a post-hoc hypothesis test, based on a linear mixed effects model for each pair of the features X_i, X_j stratified according to the processes (ggF , $u\bar{u}A$, $d\bar{d}A$ and background) S_k , given as follows

$$X_i = \beta_{ij} X_j + \beta_k S_k + \beta_0, \quad (7.40)$$

where β_{ij} , β_k and β_0 are the constants for the fit. The hypothesis test is therefore performed by taking the ratio of log likelihood for the linear model of eq. (7.40), defined as

$$t = \frac{\mathcal{L}(\beta_{ij}, \beta_k, \beta_0)}{\mathcal{L}(\beta_{ij}, \beta_k = 0, \beta_0)}. \quad (7.41)$$

This statistical test yields a p -value for each feature pair, these p -values are false discovery rate (FDR) corrected, and the correlation difference amongst the strata is considered significant if the FDR-corrected p -values pass the threshold $p < 0.01$. The result of these comparisons can be seen in Figure 7.10.

We can see that many of the features do not have significant variation across the strata. This indicates that these features are not important in separating the signal from the background. The most significant variation is between the ggF (equivalently $q\bar{q}A$) and the background. While for the $q\bar{q}A$ channels, the correlation patterns are almost identical except for the correlation between the observables related to the PDFs, which is expected since the only kinematic difference between the up-and down-initiated $q\bar{q}A$ emerges from the PDFs of the up and down quarks. This network analysis gives some

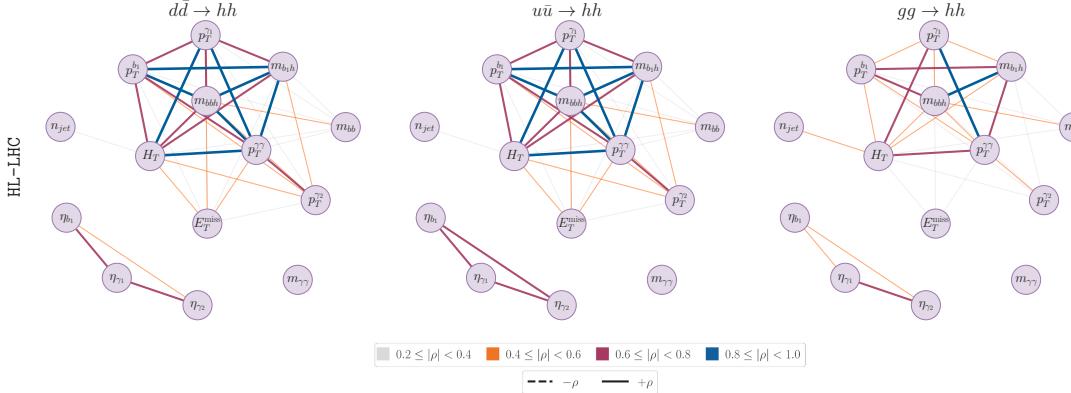


Figure 7.9. Network diagrams of the signal channels of their Pearson correlation (ρ) between the features, showing slightly different patterns of correlation amongst these channels.

insight of the feature set at hand. Namely, if we examine the intra-feature correlations across the channels, as seen in Figure 7.10, we would expect that the variable which do not vary much across the different channels will not play a major role in the classification procedure.

⁵For network plots of the backgrounds see [43].

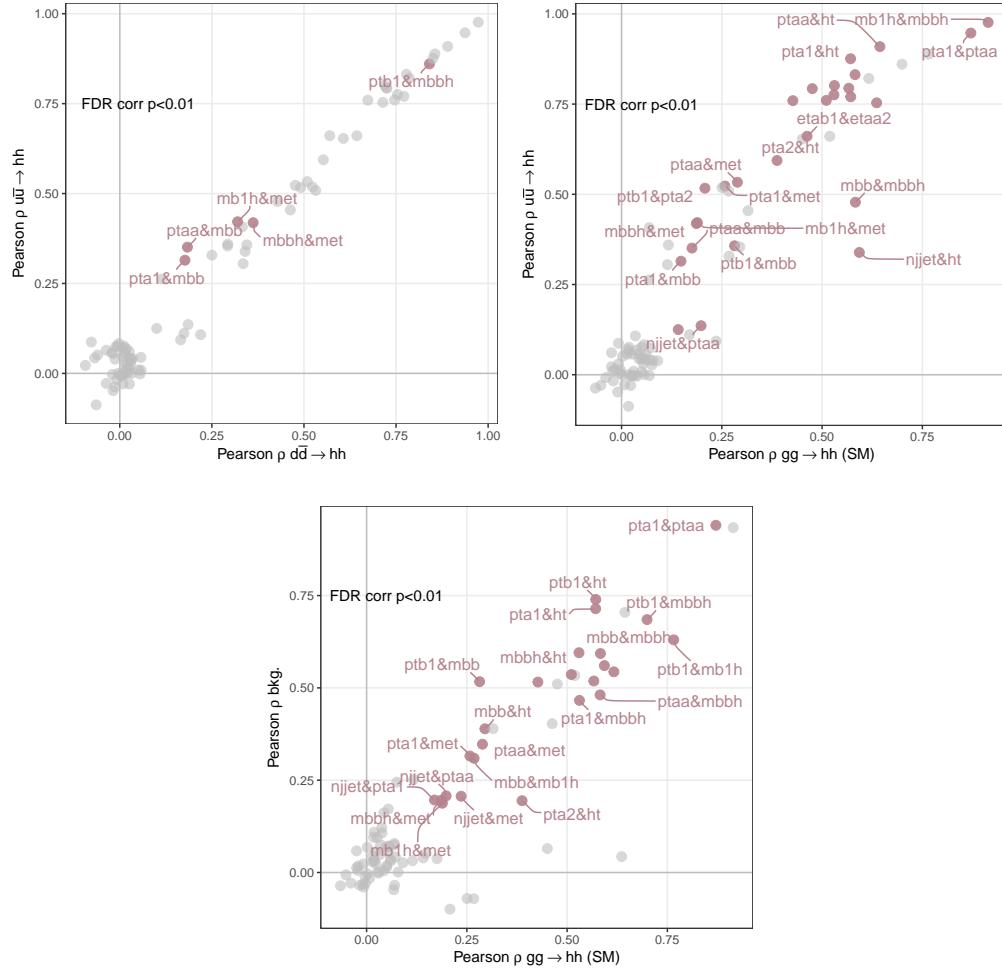


Figure 7.10. Pearson correlations plotted against each other for the different signals. The coloured and annotated variable pairs points indicate that the difference between the correlation passes the hypothesis testing FDR-corrected p -value threshold ($p < 0.01$).

7.5.3 Classification analysis

The network analysis merely offers a method to explore how the Higgs pair signal differs from the backgrounds. It is useful to reduce the dimensionality of the feature space and offer “hints” on which subset of features has the highest discriminant power. However, for analysis of the sensitivity and complete resolution of the signal against backgrounds, the golden standard is rule-based machine learning. BDTs and random forests in particle physics analysis have been explored since the early LHC days. Nowadays, it has become widespread, and its popularity becomes evident by simply examining the particle physics literature. Many recent Higgs experimental analyses were performed using some rule-

based ML algorithm⁶.

In this analysis, the extreme gradient BDT (XGBoost), with its Python implementation [340], has been used as the classifier algorithm. The standard procedure for training and testing the classifier was followed, starting with the complete list of features listed in subsection 7.5.1 and then the most important features were shortlisted to improve the efficiency and performance of the classifier. This was possible due to the introduction of interpretability to the ML analysis that provided variable importance measures, by which features with a low importance index can be removed.

Interpretability is achieved by incorporating a mathematically robust measure from Game Theory known as **Shapley values** [341]. This measure formulates an axiomatic prescription for fairly distributing the payoff of a game amongst the players in a n -player cooperative game. When applied to ML, Shapley values estimate the significance of the features used in the classification. The process naturally and mathematically lends itself to examining the correlations amongst the features used in the classification since all possible combinations of variables can be taken out of the game to check the outcome. Further information regarding the application of Shapley values in particle physics analysis can be found in refs. [43, 342, 343]. The same procedure described in [43] was followed for the Higgs pair production study. The importance of a variable in determining the outcome of classification will be quantified by the mean of the absolute Shapley value, $\overline{|S_v|}$, larger values signifying higher importance. The SHAP (Shapley Additive exPlanations) [344] package implemented in Python was used. This package computes the feature importance using Shapley values calculated exactly from tree-explainers [345, 346]. This analysis is to be published soon [227].

Classifier output

The trained BDTs outputs are extracted as confusion matrices, with number of events as entries. The diagonal elements of these matrices represent the true positive (TP) identification of the signal and true negative (TN) rejection of the background. In contrast, the upper triangular part represents the signal loss, or false-negative counts (FN). The lower triangular part shows the remaining background contamination of the signal, or the false-positive counts (FP). Using these counts, it is possible to estimate the accuracy score ACC of the classifiers

$$ACC = \frac{TP + TN}{TP + TN + FP + FN} \approx 0.7, \quad (7.42)$$

and the sensitivity $TP/P \approx 0.2$, which corresponds to the ϵ_{SEL} of the cut-based analysis. Here we see that the ML-based analysis yielded a three- to four-fold increase in ϵ_{SEL} compared to the cut and count method. Table 7.5 shows one of these matrices from the classification of the ggF SM signal separated into the topologies according to their dependence on C_ϕ . For up- and down-quark $q\bar{q}A$, the same matrices were constructed,

⁶Rule-based ML algorithms outperform deep neural networks (DNN) in terms of simplicity of implementation and computational requirements. In addition, rule-based algorithms, such as decision

Predicted no. of events at HL-LHC							
Actual no. of events	Channel	$hh_{\text{tri}}^{\text{ggF}}$	$hh_{\text{tri}}^{\text{ggF}}$	$hh_{\text{box}}^{\text{ggF}}$	$Q\bar{Q}h$	$b\bar{b}\gamma\gamma$	total
$hh_{\text{tri}}^{\text{ggF}}$		28	14	18	38	10	108
$hh_{\text{int}}^{\text{ggF}}$		89	80	129	178	41	517
$hh_{\text{box}}^{\text{ggF}}$		77	105	266	265	50	763
$Q\bar{Q}h$		177	98	191	5,457	1,835	7,758
$b\bar{b}\gamma\gamma$		1,743	845	1,074	30,849	287,280	321,791
\mathcal{Z}_j		0.61	2.37	6.49	28.45	534.1	

Table 7.5. The confusion matrix output of the trained BDT five-channel classifier. The separation between the ggF topologies allows for setting constraints on C_ϕ . The events shown are for the HL-LHC at 14 TeV and integrated luminosity of 6ab^{-1} , assuming the SM signal. The bottom-most row gives the signal significance

and since the number of events for these processes scale with $C_{q\phi}^2$, it is only required to produce one confusion matrix for each classification procedure, as for the ggF channel. For the fitting procedure, a Bayesian framework based on an MCMC method was used, analogous to the procedure described in section 5.2.

The full analysis code, including the BDT training and fits as well as the confusion matrices for the classification procedures performed can be found in the **Github** repository: <https://github.com/talismanbrandi/IML-diHiggs.git>.

Feature importance and Shapley values

Another output of the interpretable BDT is the SHAP scores for the features used in the classification. The $|S_v|$ values are used to order the features used for the classification. The most important features in different classifiers used in this analysis can be seen in Figure 7.11. Panel (a) shows the hierarchy of the features used for the separation of the SM ggF signal from the backgrounds. The BDT was able to distinguish between the different signals, a task cut-based analysis or unsupervised clustering are unable to fructify. Panel (b) shows the list of feature importance for the ggF vs $q\bar{q}A$ classification, while (c) demonstrates the full strength of the BDT in distinguishing $u\bar{u}A$ from $d\bar{d}A$ despite having very little variation of their kinematic distributions. As expected, $u\bar{u}A$ vs $d\bar{d}A$ classification, the features that appeared on top of the list are related to the different PDFs. Their ranking is though less intuitive because this classification is a genuine multivariate problem, where the intra-variable correlations and differences have been fully extorted.

7.6 Fit results

The fit from the cut-bases analysis was originally made for 3ab^{-1} and published in [41]. For a better comparison with the optimised BDT multivariate analysis, the fit for this

trees, are more transparent as far as the signal vs. background separation is concerned.

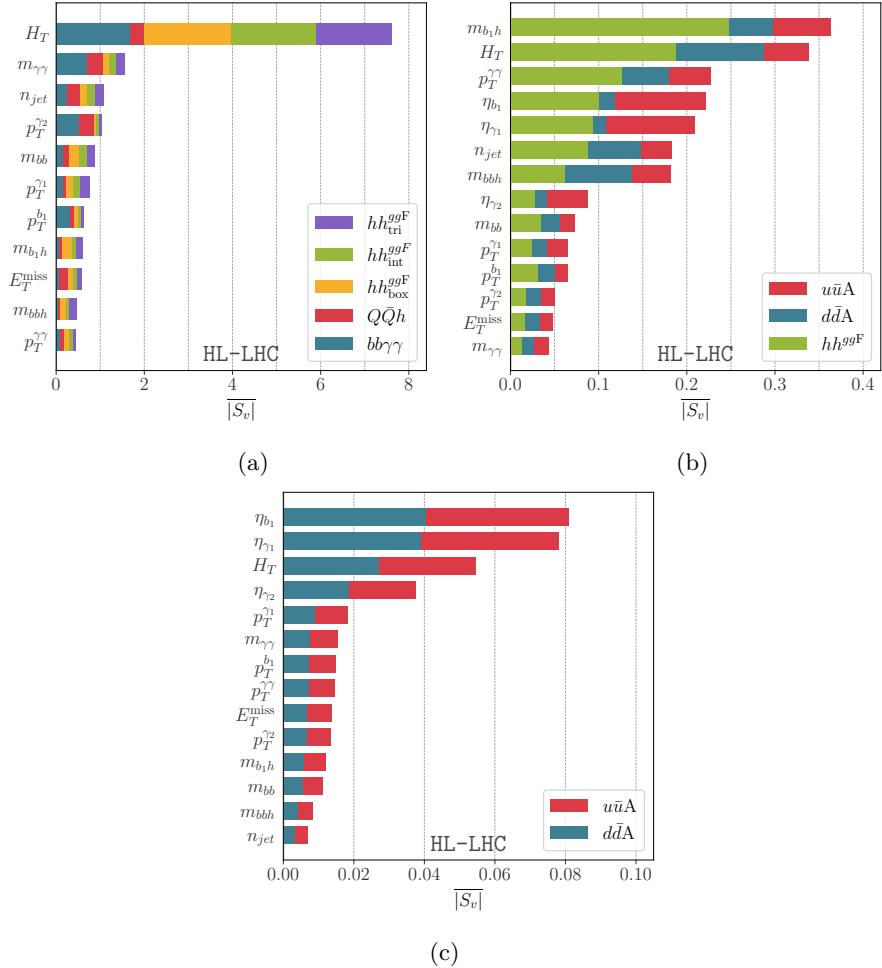


Figure 7.11. The feature importance output in terms of $\overline{|S_v|}$. The higher the value of $\overline{|S_v|}$, the more important the kinematic variable is in separating the different channels: (a) The hierarchy of variables important for the separation of hh^{ggF}_{tri} from hh^{ggF}_{int} events from hh^{ggF}_{box} , $Q\bar{Q}h$ and $b\bar{b}\gamma\gamma$ QCD-QED background. (b) The hierarchy of variables important for the separation of hh^{ggF} , $u\bar{u}A$ and $d\bar{d}A$ events. (c) The hierarchy of variables important for the separation of $u\bar{u}A$ from $d\bar{d}A$ events.

thesis was carried out again for 6 ab^{-1} , and with SMEFT Wilson coefficient parametrisation, thus harmonising it with the results of the other chapters. Two-parameter fits were done in the $(C_\phi, C_{q\phi})$ plane shown by the top plots of Figure 7.12. The low panel shows the fit in the $(C_{u\phi}, C_{d\phi})$ plane. We see that even with the traditional technique, two-parameter fits were possible. However, the bounds obtained on the trilinear self-coupling modifier are weaker than the projected bounds for the HL-LHC, made by ATLAS and CMS [222, 347, 348], which is expected due to the dilution of these bounds by adding light Yukawa coupling modifiers and the loss of some signal due to the analysis technique. For the $C_{u\phi} - C_{d\phi}$ combined fit, no correlation between the two parameters is

seen.

To demonstrate the power of multivariate (MV) analysis, we compare the fit results from single parameter fits of this analysis to the cut-and count technique (CC) for both up and down quark coupling modifiers at 68% CL/CI

$$\begin{aligned} C_{u\phi}^{MV}(\kappa_u^{MV}) &= [-0.09, 0.10] \text{ } ([-466, 454]), & C_{u\phi}^{CC}(\kappa_u^{CC}) &= [-0.18, 0.17] \text{ } ([-841, 820]), \\ C_{d\phi}^{MV}(\kappa_d^{MV}) &= [-0.16, 0.16] \text{ } ([-360, 360]), & C_{d\phi}^{CC}(\kappa_d^{CC}) &= [-0.18, 0.18] \text{ } ([-405, 405]). \end{aligned} \quad (7.43)$$

A significant improvement of the bounds from using MV analysis over CC is obtained

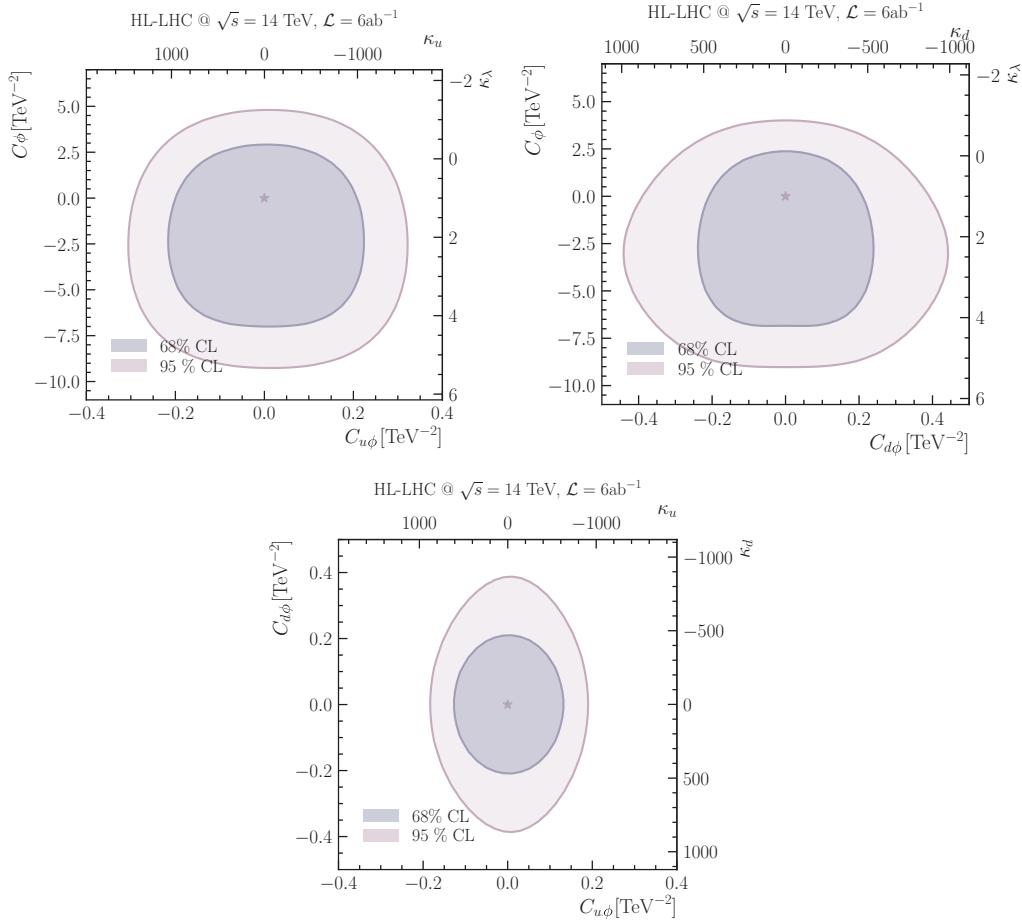


Figure 7.12. The 68% and 95% CL contours of the constraints on up and down Yukawa coupling modifiers as well as C_ϕ from two-parameter fits using the results of the cut-based analysis for the HL-LHC at 14 TeV and 6ab^{-1} integrated luminosity.

for $C_{u\phi}$, while in $C_{d\phi}$ on a mild improvement of $\mathcal{O}(10\%)$ is obtained.

To compare the ML multivariate analysis used to other sensitivity projections, the

projections on the trilinear coupling modifier C_ϕ are shown in Figure 7.13. These bounds are obtained by using a BDT classification showcased in Table 7.5, by showing the significance $\mathcal{Z} = \sqrt{q_\mu}$ functions for the linear, quadratic and combined dependence on C_ϕ . The constraints that we have obtained here are similar to or slightly better than the results quoted by the experimental sensitivity analysis quoted before. This was achieved by optimising the BDT by separating the signal and background channels, as well as the exclusion of less-important features. The projected 1σ bound on C_ϕ is $[-1.57, 1.00]$ at HL-LHC. Another advantage of the optimised multivariate analysis is the ability to

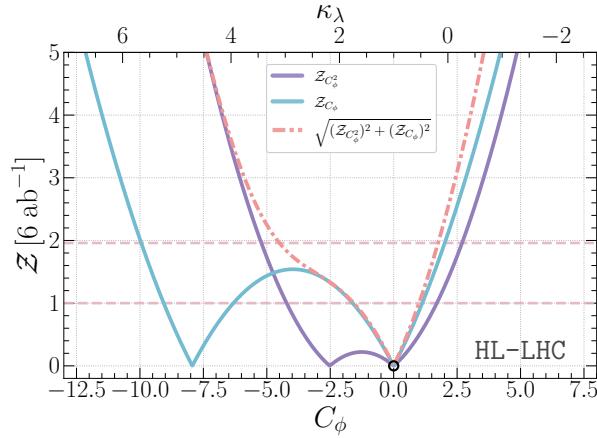


Figure 7.13. Bounds on C_ϕ (or κ_λ) at the HL-LHC from single parameter fit. The solid blue lines are the constraints from the $hh_{\text{int}}^{\text{ggF}}$ contribution, which scales linearly with the modified coupling. The solid purple line is from the $hh_{\text{tri}}^{\text{ggF}}$ contribution that scales quadratically with the modified coupling. The red dashed line is the combination of the quadratic and linear channels. The horizontal light red dashed lines mark the 68% and 95%CI's.

perform two-parameter fits in the same planes described above, shown in Figure 7.14 while maintaining the improvement over the cut-based one.

Since the BDT training achieved sufficient accuracy for the seven-channel classifier, including up and down $q\bar{q}A$, the different ggF topologies and the backgrounds, it was possible to resolve all of the signal channels strata and their parametric dependence on the three Wilson coefficients $C_{u\phi}$, $C_{d\phi}$ and C_ϕ . A three-parameter fit is possible without degeneracies, as seen in Figure 7.15. However, the posterior distribution of the three-parameter fit shows no marked correlations amongst the Wilson coefficients. In both two- and three-parameter fits, a degeneracy in the $C_{d\phi}$ direction is observed at 99.7% CI. This is due to the reduction of the Higgs pair signal when the $h \rightarrow d\bar{d}$ decay channel is opened, particularly for high values of this Wilson coefficient as highlighted by Figure 7.7. When this analysis is applied for the strange quark, the overall effect of enhanced the strange quark is a reduction in the $b\bar{b}\gamma\gamma$ signal, making this Higgs pair final state insensitive to the strange Yukawa enhancements; more details on this were discussed in ref. [41]. Comparing with the constraints on C_ϕ from a single parameter fit in Figure 7.13, it can be seen from the two- and three-parameter fits in Figure 7.14

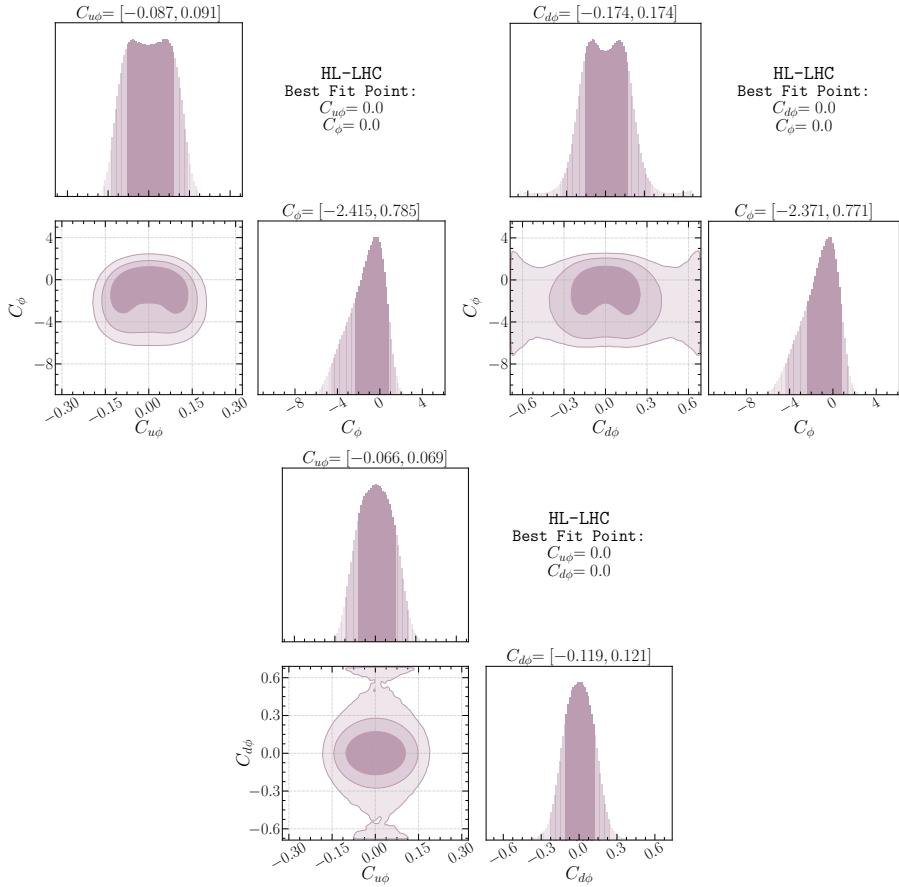


Figure 7.14. The 68%, 95% and 99.7% highest density posterior contours, for Bayesian fits preformed on pairs of Wilson coefficients for C_ϕ , $C_{u\phi}$ and $C_{d\phi}$ form the multi-variate analysis output. The quoted intervals on top of the panel correspond to the 68% CIs.

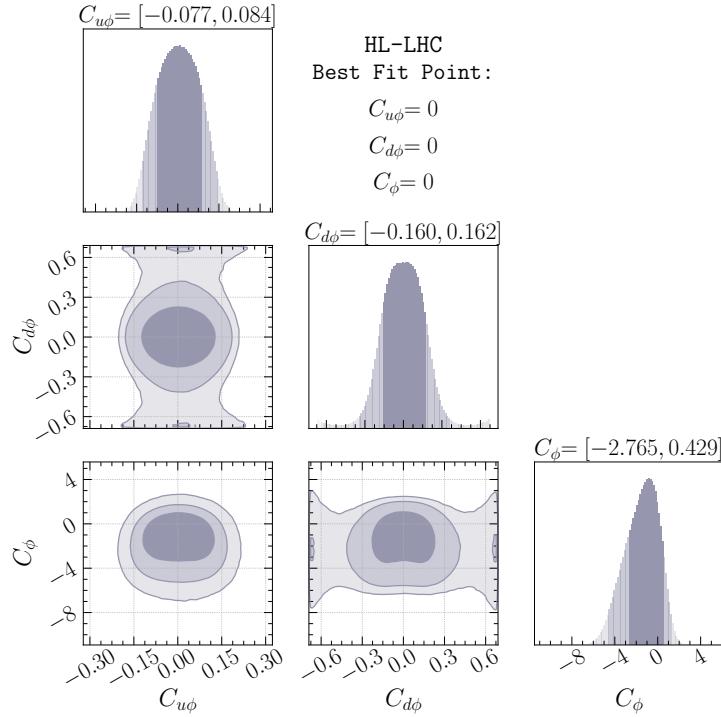


Figure 7.15. Three parameter Bayesian fits with $C_{u\phi}$, $C_{d\phi}$ and C_ϕ , the highest density posterior contours are the same as Figure 7.14.

and Figure 7.15, respectively, that, the constraints on C_ϕ become diluted when the light-quark Yukawa coupling modifiers $C_{q\phi}$ are taken into an account. This effect is somewhat more prominent for $C_{d\phi}$ than for $C_{u\phi}$ and stems from the fact that away from $C_{u\phi,d\phi} = 0$ larger negative values of C_ϕ are allowed by the crescent shaped curves of the highest density posterior contours. The bounds on $C_{u\phi}$ and $C_{d\phi}$ from the fit with two-parameters including C_ϕ remain the same as the bounds on these Wilson coefficient from the single parameter $C_{u\phi,d\phi}$ fits. The fit results are summarised in Table 7.6.

7.6.1 Second generation bounds

Fitting signal strengths obtained from b -mistagging of b -jets shown in eq. (7.34), and varying κ_c , κ_s for charm and beauty final states for constructing the likelihood $\mathcal{L}(\kappa_c, \kappa_s)$, we can set limits from the anticipated charm tagging working points as shown in Figure 7.16. These projected limits are an improvement compared to the current direct bound and prospects for HL-LHC, particularly for charm quark Yukawa modifications [331, 335].

Operators	$C_{u\phi}$	$C_{d\phi}$	C_ϕ		κ_u	κ_d	κ_λ
HL-LHC 14 TeV 6 ab^{-1} @ 68% CI							
\mathcal{O}_ϕ	—	—	[-1.57, 1.00]		—	—	[0.53, 1.73]
$\mathcal{O}_{u\phi}$	[-0.09, 0.10]	—	—		[-477, 431]	—	—
$\mathcal{O}_{d\phi}$	—	[-0.16, 0.16]	—		—	[-360, 360]	—
$\mathcal{O}_{u\phi}$ & \mathcal{O}_ϕ	[-0.087, 0.091]	—	[-2.42, 0.79]		[-434, 417]	—	[0.63, 2.13]
$\mathcal{O}_{d\phi}$ & \mathcal{O}_ϕ	—	[-0.17, 0.17]	[-2.73, 0.77]		—	[-381, 379]	[0.63, 2.27]
$\mathcal{O}_{u\phi}$ & $\mathcal{O}_{d\phi}$	[-0.065, 0.069]	[-0.12, 0.12]	—		[-331, 312]	[-268, 272]	—
All	[-0.077, 0.084]	[-0.160, 0.162]	[-2.77, 0.43]		[-400, 369]	[-362, 359]	[0.79, 2.30]

Table 7.6. Summary of the 68% projected bounds on $C_{u\phi}$, $C_{d\phi}$ and C_ϕ from single-, two- and three-parameter fits for HL-LHC with 6 ab^{-1} . The corresponding bounds on the rescaling of the effective couplings, κ_u , κ_d and κ_λ are presented on the right side of the table.

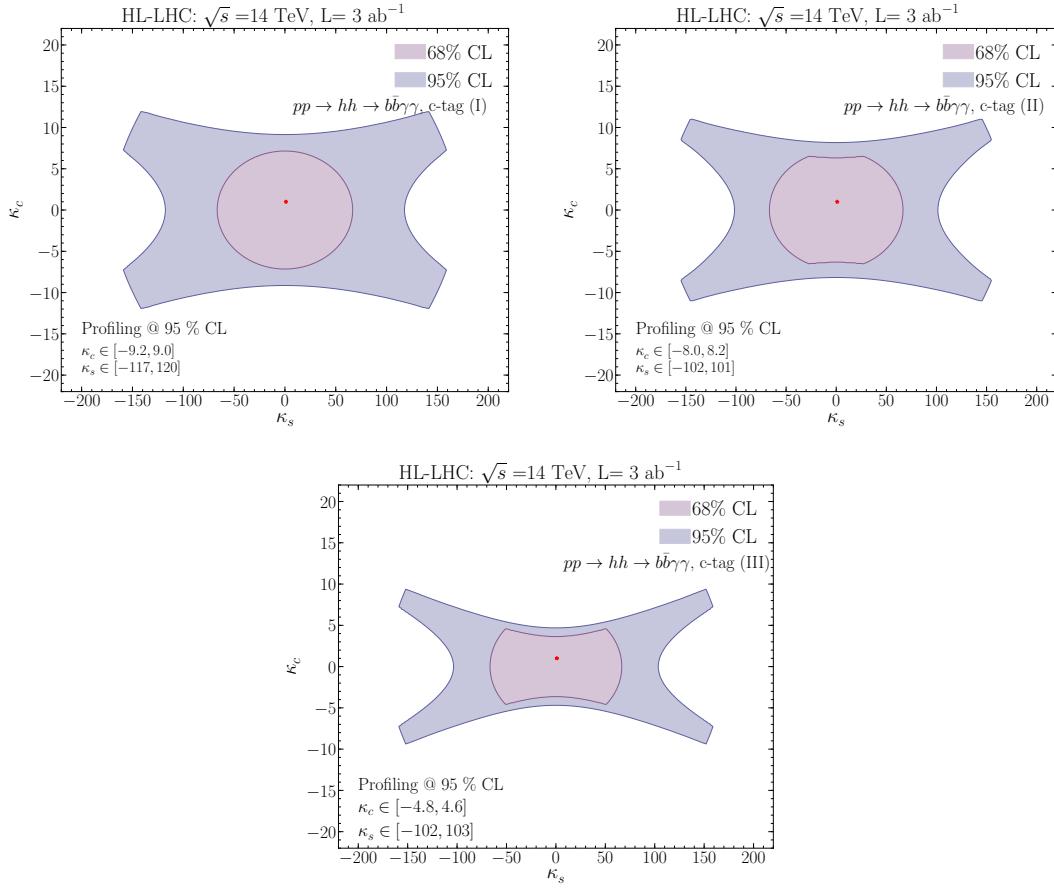


Figure 7.16. The expected sensitivity likelihood contours at 68% CL and 95% CL for an integrated luminosity $L = 3000 \text{ fb}^{-1}$ for modified second generation quark Yukawa couplings, using the c-tagging I (upper pannel, left), II (upper pannel, right) and III (lower pannel) working points.

7.7 Overview of Light Yukawa searches

Additional measurements of the light-quark Yukawa couplings might become relevant at HL-LHC or future hadron colliders like the FCC-hh, a careful study of which is beyond the scope of this thesis. Yet, I attempt to include a discussion here to provide a comparison with the study presented in this chapter and to put it into proper context or to serve as a proposal for further studies.

The channel $pp \rightarrow h + j$ has been proposed as a probe for charm Yukawa coupling [349] with charm-tagged jet having a potential bound of $\kappa_c \sim 1$ for the HL-LHC, depending on the charm-tagging scheme. This process could be used for the first and second generation Yukawa couplings by looking at the shapes of the kinematic distributions, the most important one being p_T [291, 350, 351]. The expected HL-LHC 95% CL bounds are $\kappa_c \in [-0.6, 3.0]$, $|\kappa_u| \lesssim 170$ and $|\kappa_d| \lesssim 990$. The use of the $h + j$ process along with other single Higgs processes have also been suggested as indirect probes for Higgs self coupling [29–33, 35], due to the contribution of the trilinear coupling to NLO electroweak corrections to these processes. In addition, experimental fits have been carried out for the trilinear coupling from single Higgs observables [93, 352].

It seems that for the HL-LHC, an optimal bound for the trilinear coupling can be obtained by combining both data from the single-Higgs process as well as Higgs pair production [92], with 68% CL bound on $\kappa_\lambda \in [0.1, 2.3]$, compared to the expected bound of $\kappa_\lambda \in [0.0, 2.5] \cup [4.9, 7.4]$ coming from using di-Higgs measurements alone. Moreover, single Higgs processes, namely Zh and $W^\pm h$ production, could also be useful in probing charm-Yukawa coupling utilising a mixture of b - and c -tagging schemes leveraging the mistagging probability of c -jets as b -jets in b -tagging working points, and vice-versa, to break the degeneracy in the signal strength [335]. This technique could probe $\kappa_c \sim 1$ in the FCC-hh. Of course, for the charm-Yukawa coupling, the constraints are set to improve significantly, as there has been a recent direct observation of $h \rightarrow c\bar{c}$ [286]. Therefore, from here on, I will mainly concentrate on the process with more potential for constraining Yukawa couplings of the first generation quarks.

Rare Higgs decays to mesons, $h \rightarrow M + V$, $M = \Upsilon, J/\Psi, \phi, \dots$, were suggested as a probe for light-quark Yukawa couplings [353–355], and there have been experimental searches for these decays [286, 356] with bounds on the branching ratios, $\mathcal{B}(h \rightarrow X, \gamma)$, $X = \Upsilon, J/\Psi, \dots$ $\sim 10^{-4} - 10^{-6}$ at 95% CL. It was shown in ref. [357], that the charge asymmetry of the process $pp \rightarrow hW^+$ vs $pp \rightarrow hW^-$ can be used as a probe for light-quark Yukawa couplings and to break the degeneracy amongst quark flavours. Moreover, the rare process $pp \rightarrow h\gamma$ is also a possible way to distinguish between enhancements of the up-and down-Yukawa couplings [358] where the authors have estimated the bounds on the up quark Yukawa coupling of $\kappa_u \sim 2000$ at the HL-LHC. Despite some processes appearing more sensitive than others, one should think of these processes as complementary.

One of the main features of the effective couplings $hhq\bar{q}$ and $hhhq\bar{q}$ emerging from SMEFT operator $\mathcal{O}_{q\phi}$, or the EWChL for that matter, is that these couplings are either free from propagator suppression for $hhq\bar{q}$ or scale with energy for $hhhq\bar{q}$ while

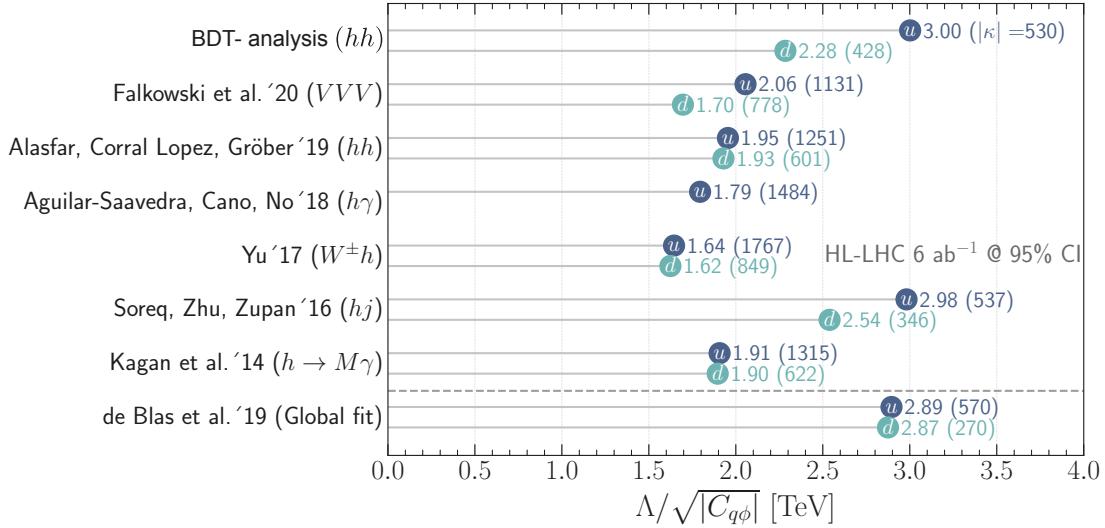


Figure 7.17. Summary of the 95% CI/CL sensitivity bounds on the SMEFT Wilson coefficients $C_{u\phi}$ (blue), and $C_{d\phi}$ (green). The bounds are interpreted in terms of the NP scale Λ that can be reached through the measurements of the Wilson coefficient at the HL-LHC at 6 ab^{-1} , the corresponding κ_q 's are shown inside the parentheses. Single parameter fit 95% CI bounds are used from this analysis for comparison with previous studies.

being safe from strong unitarity constraints. This feature gives processes with multiple Higgs and/or vector bosons $V = W^\pm, Z$ an advantage in constraining $\mathcal{O}_{q\phi}$. The latter constraints come from the longitudinal degrees of freedom of the gauge bosons, which can be understood from the Goldstone boson equivalence theorem. The use of the final state VV as a probe for $\mathcal{O}_{q\phi}$ is difficult due to the large SM background. However, the three-boson final state VVV gives strong projected bounds for light-quark Yukawa couplings for HL-LHC with 95% CL bounds on $\kappa_u \sim 1600$ and $\kappa_d \sim 1100$ [359]. A ten-fold improvement is expected at FCC-hh with bounds of order $\kappa_d \sim 30$. Higgs pair production has a smaller SM background compared to VV production. Still, it has a significantly smaller cross-section, too, even when compared to VVV , as the latter process has already been observed at the LHC [360, 361].

On the contrary, the LHC runs I-III do not have the sensitivity to probe the SM Higgs pair production, but it is potentially accessible at the HL-LHC [362] having a $\sigma \cdot BR \sim 1 \text{ fb}^{-1}$. However, Higgs pair production, particularly the channel $h \rightarrow b\bar{b}\gamma\gamma$, is of significant interest as it has unique features. The first is the ability to simultaneously constrain the trilinear and light-quark Yukawa couplings, as we have already seen in the previous sections. Secondly, Higgs pair production could probe non-linear relations between Yukawa interaction and $hhq\bar{q}$ couplings [363]. Lastly, Higgs pair production is expected to be significantly enhanced in specific models involving modification of light-quark Yukawa couplings (cf. [42, 364, 365]). I show in Figure 7.17 numerical comparisons of the strongest bounds from HL-LHC on the first-generation Yukawa couplings from the studies discussed above. Additionally, in the same figure these bounds are confronted

with the global fit bounds that have been obtained with no invisible or untagged Higgs decays allowed [366]. For $C_{d\phi}$, the most stringent bound comes from the global fit and the $h + j$ channel as a model-independent bound, while this analysis provides the second most stringent model-independent bound. For $C_{u\phi}$, the BDT analysis presented here provided the most stringent constraint, while the bound from $h + j$ and the global analysis are comparable. The figure is interpreted in terms of the reach of NP scale Λ that can be achieved by measuring these Wilson coefficients. For future colliders, like the FCC-hh at 100 TeV, in addition to Higgs pair production, triple Higgs production might be an interesting channel for constraining the operators with Wilson coefficient $C_{u\phi}$ and $C_{d\phi}$ due to the energy increase of a Feynman diagram coupling the quarks to three Higgs bosons.

For future colliders, like the FCC-hh at 100 TeV, in addition to Higgs pair production, triple Higgs production might be an interesting channel for constraining the operators with Wilson coefficient $C_{u\phi}$ and $C_{d\phi}$ due to the energy increase of a Feynman diagram coupling the quarks to three Higgs bosons. In this case, a similar study to this one should be performed to investigate this potential further, also, in this case, it will be essential to do a combined fit on the light quark Yukawa couplings together with the trilinear and quartic Higgs self-couplings⁷. Finally, it should be noted that there are also non-collider signatures for enhanced light-quark Yukawa couplings, manifesting in frequency shifts in atomic clocks from Higgs forces at the atomic level [368].

7.8 Discussion and conclusion

The chapter walked through the potential of Higgs pair production to glean information about the elusive Yukawa couplings of the first generation quarks from the final state $b\bar{b}\gamma\gamma$. This has been done in two different approaches: The first is the traditional cut and count method. Later on, I have showcased a significant improvement in the analysis by using interpretable machine learning. To maintain harmony with other chapters of this thesis, the enhancements of light Yukawa couplings were parametrised within the SMEFT framework.

Despite the limitations of the cut-based analysis for the Higgs pair, it was still possible to estimate notable sensitivity for both up-and down-type Yukawa coupling to the Higgs boson, comparable with other channels and the model-dependent global fit. Superior estimated bounds, particularly for the up quark, emanated from fully exploiting the kinematical shapes and their correlations in a multivariate analysis. This was achieved by using a high-level kinematical distribution as a feature in a BDT classification. The ML is interfaced with an explainer layer based on Shapley's values.

The precedence of using an interpretable ML framework over DNNs stems from optimising the training procedure by employing physics-motivated dimensionality reduction by excluding less important features. Interpretable ML not only outperforms black-box models but also provides a physics understanding of the processes at hand, pointing to

⁷In [367], it was shown that $\sim \mathcal{O}(1)$ bounds on the quartic Higgs self-coupling can be reached at the FCC-hh.

kinematic variables like H_T and $m_{\gamma\gamma}$ as being important variables that instrument this separation. Lastly, but most importantly, interpretable models provide higher confidence in the results of their classification or regression.

The use of a BDT classifier was not only beneficial for increasing the hh signal selection efficiency but also to classify the signal channels strata, such that it is possible to parametrise it in terms of C_ϕ , $C_{u\phi}$ and $C_{d\phi}$, by decomposing the ggF channel into its sub-topologies depending on their C_ϕ parametrisation. The outcome of this technique is the ability to perform two and three-parameter fits, including all of the Wilson coefficients in question.

With the HL-LHC Higgs pair searches, one can constrain the Higgs trilinear coupling to $\mathcal{O}(1)$ of the SM prediction. This result is matched by other sensitivity analyses based on ML analysis done by the CMS and ATLAS [222, 347, 348]. This highlights the desideratum of Higgs pair production observation for understanding the Higgs potential. Despite light Yukawa modifiers like $C_{q\phi}$ being typically overlooked when studying Higgs pair production, this study showed that they could dilute the bounds on the trilinear Higgs coupling. Thus these coefficients need to be considered in phenomenological studies of Higgs pair production. These Wilson coefficients are weakly bounded from other measurements, unlike other coefficients constrained from single-Higgs, EWPO or top quark data.

For the second generation quarks it was found that at the HL-LHC in the di-Higgs channel we will be able to set competitive bounds on the charm Yukawa coupling if final states with tagged charm quarks are considered. If one considers the final state $c\bar{c}\gamma\gamma$, one finds the expected sensitivity of $|\kappa_c| \lesssim 5$ and $|\kappa_s| \lesssim 100$, as shown in Figure 7.16, where the first prospective limit is comparable to the prospects from charm tagging in the Vh channel [335].

There exist a handful of potential UV-complete models in which both light Yukawa as well as the Higgs trilinear couplings are enhanced. For example, a model proposed in ref [364] based on vector-like quarks (VLQ) with AFV assumptions. The original assumption of this model is excluded, as the authors assumed an enhancement of all light quark-Higgs couplings to be equal to the beauty quark Yukawa. One could still get significant enhancement to light Yukawa from VLQ masses of ~ 2 TeV, which is well above the current direct searches excluding VLQ of masses $M_{VLQ} < 1.6$ TeV [369, 370] for the hadronic final state, and $M_{VLQ} < 1.2$ TeV for the leptonic one [371]. Due to the AFV manifested in this model, the VLQ could be made not to couple to the third generation quarks and evade the tree-level EWPO bounds [38]. In addition, the trilinear Higgs coupling could be modified by the inclusion of an additional scalar singlet cf. [107, 372, 373]. Another example of models with enhanced light Yukawa is a two-Higgs-doublet model (2HDM) model proposed in refs. [42, 374]. This model has a special kind of AFV, known as spontaneous flavour violation (SFV). Enhancements to light Yukawa couplings come from the second Higgs Yukawa couplings, which are made diagonal in the flavour space K_q ($q = u, d$). SFV has the constraint that either the up-type or the down-type couplings can be enhanced, while the couplings of the other type maintain the SM hierarchy.

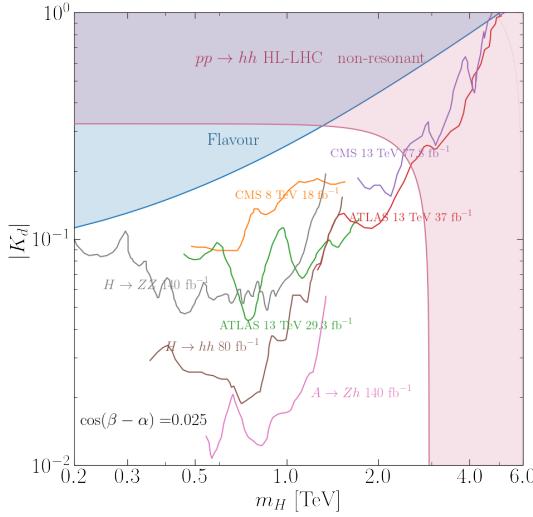


Figure 7.18. Example of constraints on the 2HDM with SFV presented in [42, 374] from flavour observables, LHC dijet , Zh, ZZ and resonant hh searches. The region shaded in red shows the bounds projected for the HL-LHC from the analysis presented in this chapter. This plot is based on the results quoted in ref. [42].

The addition of the second doublet modifies the Higgs potential, and consequently, the Higgs self-coupling will be modified as well. Like any other 2HDM, the parameter space is rather large. The bounds on this model will depend on the region of its parameter space we are interested in. Figure 7.18 shows the bounds on this model for a point near the alignment limit. For a small mass of the “heavy” Higgs H and large Yukawa coupling K_d flavour bounds dominate, while for larger m_H , the dijet searches [375–377] would dominate due to the decay $H \rightarrow d\bar{d}$. On the contrary, the decay $H \rightarrow hh$ would become dominant from smaller values of K_d and larger H mass, but still $m_H < 2$ TeV. In this regime, resonant Higgs pair searches give string constraints for light Yukawa enhancement [378, 379]. Similar light Yukawa bounds in this region of the parameter space could also be derived from Zh [380] and ZZ [381, 382] searches. Lastly, for $m_H > 2$ TeV, the non-resonant Higgs pair production will become the dominant bound on light Yukawa enhancement, coming from the analysis of this chapter.

Part IV

Flavour physics

8 Data-inspired models for $b \rightarrow s\ell\ell$ anomalies

Recent results from B -factories, including Belle and Babar, as well as the LHCb-experiment involving semileptonic decays of the beauty mesons B^0, B^\pm, B_s, \dots point to a marked deviation of $\sim 2.5\sigma$ from the SM prediction, particularly in the branching fractions ratios

$$R_{K^{(*)}} \equiv \frac{Br(B \rightarrow K^{(*)}\mu^+\mu^-)}{Br(B \rightarrow K^{(*)}e^+e^-)}, \quad (8.1)$$

in the high dilepton mass bins [44–48]¹. In addition, the results of the angular analysis of the decay $B \rightarrow K^*\mu^+\mu^-$ [383, 384], particularly the observable P'_5 , show similar deviation from the SM. With the most recent measurement was published by LHCb [385] in mind, and if the light cone sum rules for modelling the hadronic effects are considered, the deviation of the P'_5 observable would be comparable to or greater than the tension seen in $R_{K^{(*)}}$ cf. [386, 387]. Other observables derived from the branching fractions of semileptonic and full leptonic final states of B mesons decays, e.g. $B_s \rightarrow e^+e^-$, have shown deviations from the SM with the $2\sigma - 3\sigma$ range [49–52]. All of these observables involve the FCNC transition $b \rightarrow s\ell\ell$ ($\ell = e, \mu$), and are in conflict with the SM lepton universality of EW couplings. This tension could be translated into a strong case for the evidence of BSM physics with lepton flavour universality violation (LUV) [388–390].

When these results are added to the measurements of differential dilepton branching fractions of B -mesons, grounds for the muons being the source of LUV are established, i.e. the NP degrees of freedom contain muon-flavoured couplings. However, the hadronic contributions in the decay amplitudes [391–395], that require non-perturbative QCD [396–399], make such conclusion debatable, see, e.g. [386, 387] and the most recent analysis, with the updated lepton flavour universality tests [400]. Another class of B decays involving the tree-level $b \rightarrow c\tau\nu_\tau$ transitions has shown similar tension with the SM [401–404]. Amongst other, the observable $R_{D^{(*)}} \equiv Br(B \rightarrow D^{(*)}\tau\nu)/Br(B \rightarrow D^{(*)}\ell\nu)$, originally found at Babar [405] and subsequently measured at Belle [406] and LHCb [407] has shown a $\sim 20\%$ deviation from the SM. All of the anomalous flavour observables are summarised in Figure 8.1 with their pull in σ 's shown in blue, compared the SM predictions with their uncertainties in orange.

The simultaneous resolution for the anomalies emerging from $b \rightarrow s\ell\ell$ and the semileptonic $b \rightarrow c$ transitions, requires models with complicated flavour structure [53–62], as they need to accommodate for similar deviations from the SM for both transitions albeit

¹The data from the most recent measurement of the R_{K^*} [48] has not been used in this work, as the fits shown in this chapter predates these results.

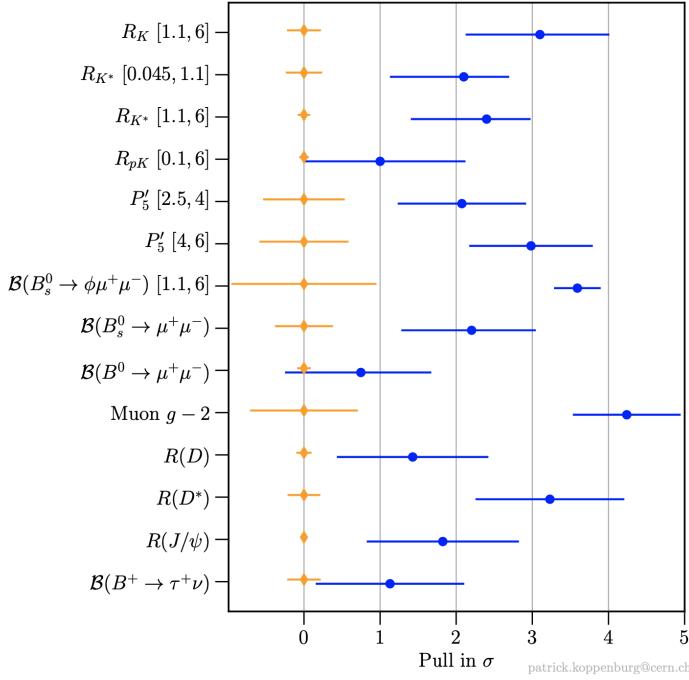


Figure 8.1. Forest plot summarising the flavour observables in tension with the SM predictions, the experimental pull in terms of standard deviations σ is shown in blue, while the SM prediction with the theoretical uncertainties is highlighted in orange. This figure is made by P. Koppenburg [408].

these two occur at different orders in the SM. Such models are often being at the edge of flavour physics constraints [230, 409] and collider bounds [410, 411]. On the other hand, most up-to-date measurements of $R_{D^{(*)}}$ from the Belle collaboration [412, 413] turn out to be in good agreement with the SM [414–417], thereby casting some doubt on the potential for NP lurking in $b \rightarrow c$ transitions. Furthermore, the ratios of branching fractions of decays involving the FCNC $b \rightarrow s\ell\ell$ transitions have a much lower dependence on the non-perturbative QCD effects than $g-2$ and differential distributions of semileptonic B -decays [418–421]. Therefore, the LUV information extracted from such “clean” observables have the highest potential for extracting LUV insights [422].

The $b \rightarrow s\ell\ell$ anomalies have been studied in a model-independent manner, in particular SMEFT framework in refs. [423–427] and more recently revisited in refs. [428–434]. Additionally, many UV-complete models were investigated, particularly lepto-quarks (LQ), like in refs. [435–439]. Another class of models of special interest are Z' models, in which the B anomalies can be realised at the loop level. The simplest of these models has been proposed in ref. [440], extending the SM with a single new $U(1)$ gauge group, together with the presence of top quark- and muon-partners, resulting in a top-philic Z' boson capable of evading present collider constraints [441] and responsible for the required LUV signatures. This model has the advantage of not introducing extra flavour spurions to the SM, i.e. similar to the MFV ansatz [293, 442, 443]. A more

general set of models with the same features can be found in ref. [444] and subsequently elaborated upon in greater detail in the phenomenological study of ref. [445].

While evading flavour constraints, models with topophilic Z' are in strong tension with the Z -pole measurements [445, 446]. In fact, it has been shown in [428], that despite large hadronic uncertainties for the amplitude of the $B \rightarrow K^* \mu^+ \mu^-$ decay, a tension of at the 3σ level at least would persist between B data and EWPO for muonic LUV effects, and an even stronger tension would be found in the case of LUV scenarios involving electron couplings. This elucidates the interplay between B -physics and EWPO [428, 429, 437–439, 444, 447, 448].

This chapter aims to review a global fit, including both EWPO and flavour observables related to the B -anomalies. The fit is based on SMEFT and based on two main assumptions

- i) Addressing the deviations in these FCNC processes with NP effects entering at one-loop level, as for SM amplitudes. This reduces the original multi-TeV domain of NP for B anomalies [449] to energies closer to present and future collider reach.
- ii) Avoiding the introduction of new sources of flavour violation beyond the SM Yukawa couplings, relaxing in this way, any restrictive flavour probe of NP in a fashion similar to what is predicted in Minimal Flavour Violation (MFV) [293, 442, 443].

Then I will present UV models that accommodate the resulting fit constraints and are based on those present in the literature [440, 441, 444]. This work is an extension of several studies done by some of my collaborators [386, 397, 426, 428, 450–452], and published in [453], which I have extended by contributing to the statistical analysis within SMEFT, and building UV complete models that explain the SMEFT fit results. This chapter is organised as follows: in section 8.1, the SMEFT analysis of the flavour anomalies is presented; in section 8.2, I discuss a viable Z' model in relation to our EFT results. After that, I present a possible alternative leptoquark scenarios in section 8.3. Lastly, the conclusions are summarised in section 8.4.

8.1 Flavour anomalies in SMEFT

8.1.1 Theoretical preamble

Global fits from $b \rightarrow s\ell\ell$ anomalies show that if the NP degrees of freedom enter at tree-level, they would have an energy scale $\Lambda \sim 10$ TeV [423–427]. Highlighting that for LHC phenomenology, the use of SMEFT is justified. The operators of interest for the explanation of these B anomalies are [428, 429, 444]:

$$\mathcal{O}_{LQ^{(1)}}^{\ell\ell 23}, (\mathcal{O}_{LQ}^{(1,3)})^{\ell\ell 23}, \mathcal{O}_{Qe}^{23\ell\ell}, \mathcal{O}_{Ld}^{\ell\ell 23}, \mathcal{O}_{ed}^{\ell\ell 23}. \quad (8.2)$$

Here, capitalised SM fields denote the quark or lepton left-handed doublets, while the lower-case ones stand for the right-handed singlets. The operator definitions in the

Warsaw basis are presented in [Table 2.1](#) are used. Current data permits both left- and right-handed operators, this is applicable when non-perturbative QCD effects are taken into account and while using light-cone sum rules [[428](#), [430–432](#)]. Nevertheless, the statistical significance for the right-handed $b \rightarrow s$ interaction remains small, coming only from $R_{K^*}/R_K \neq 1$ [[427](#), [428](#)]. Hence, one can only consider the left-handed operators $(\mathcal{O}_{LQ}^{(1,3)})^{2223}$ and \mathcal{O}_{Qe}^{2322} for addressing the flavour anomalies. Additionally, when conservative hadronic uncertainties are considered [[396–398](#)], the preference of NP coupling to the muons exclusively becomes mitigated and the inclusion of electron interactions is viable as well [[426](#)]. From these considerations, it can be concluded that the operator $(\mathcal{O}_{LQ}^{(1,3)})^{\ell\ell 23}$ with either or both $\ell = e, \mu$ offers the minimal resolution of these anomalies within the SMEFT framework [[428](#)].

Introducing these operators at tree-level will lead to flavour violation beyond the SM, as these operators are flavour spurions independent of the SM ones. This can be avoided if they get generated at loop-level from the RGE of operators involving leptons and the Higgs boson [[444](#)]

$$(\mathcal{O}_{\phi L}^{(1,3)})^{\ell\ell}, \quad \mathcal{O}_{\phi e}^{\ell\ell}, \quad (8.3)$$

or alternatively, from the semileptonic four-fermion (SL-4F) operators with right-handed top-quark currents:

$$\mathcal{O}_{Lu}^{\ell\ell 33}, \quad \mathcal{O}_{eu}^{\ell\ell 33}. \quad (8.4)$$

The leading log solutions of the RGE for these operators are [[85](#), [86](#)]

$$\begin{aligned} C_{LQ}^{(1)} \ell\ell 23 &= V_{ts}^* V_{tb} \left(\frac{y_t}{4\pi} \right)^2 \log \left(\frac{\Lambda}{\mu_{\text{EW}}} \right) \left(C_{Lu}^{\ell\ell 33} - C_{\phi L}^{(1)} \ell\ell \right), \\ C_{LQ}^{(3)} \ell\ell 23 &= V_{ts}^* V_{tb} \left(\frac{y_t}{4\pi} \right)^2 \log \left(\frac{\Lambda}{\mu_{\text{EW}}} \right) C_{\phi L}^{(3)} \ell\ell, \\ C_{Qe}^{23\ell\ell} &= V_{ts}^* V_{tb} \left(\frac{y_t}{4\pi} \right)^2 \log \left(\frac{\Lambda}{\mu_{\text{EW}}} \right) \left(C_{eu}^{\ell\ell 33} - C_{\phi e}^{\ell\ell} \right). \end{aligned} \quad (8.5)$$

These solutions pose the matching conditions for the left-handed quark-current operators in eq. [\(8.2\)](#) at the EW scale $\mu_{\text{EW}} \sim v$.²

In heavy quark physics, B decays are typically studied within the low energy weak effective theory [[456–458](#)], in which the vector and axial currents are defined as

$$\begin{aligned} \mathcal{O}_{9V,\ell} &= \frac{\alpha_e}{8\pi} (\bar{s}\gamma_\mu(1-\gamma_5)b)(\bar{\ell}\gamma^\mu\ell), \\ \mathcal{O}_{10A,\ell} &= \frac{\alpha_e}{8\pi} (\bar{s}\gamma_\mu(1-\gamma_5)b)(\bar{\ell}\gamma^\mu\gamma_5\ell); \end{aligned} \quad (8.6)$$

²Similar to the previous chapters, for one-loop effects, the NP scale is set to be $\Lambda = 1$ TeV. The renormalisation scale is set to $\mu_{\text{EW}} = m_t \simeq v/\sqrt{2}$ to minimise the matching-scale dependence with the inclusion of the NLO corrections [[454](#), [455](#)].

they are matched at the EW scale μ_{EW} with the SMEFT operators in eq. (8.3) - (8.4) follows:

$$\begin{aligned} C_{9,\ell}^{\text{NP}} &= \frac{\pi v^2}{\alpha \Lambda^2} \left(\frac{y_t}{4\pi} \right)^2 \log \left(\frac{\Lambda}{\mu_{\text{EW}}} \right) \left(C_{\phi L}^{(3)} \ell\ell - C_{\phi L}^{(1)} \ell\ell - C_{\phi e}^{\ell\ell} + C_{Lu}^{\ell\ell 33} + C_{eu}^{\ell\ell 33} \right), \\ C_{10,\ell}^{\text{NP}} &= \frac{\pi v^2}{\alpha \Lambda^2} \left(\frac{y_t}{4\pi} \right)^2 \log \left(\frac{\Lambda}{\mu_{\text{EW}}} \right) \left(C_{\phi L}^{(1)} \ell\ell - C_{\phi L}^{(1)} \ell\ell - C_{\phi e}^{\ell\ell} - s C_{Lu}^{\ell\ell 33} + C_{eu}^{\ell\ell 33} \right). \end{aligned} \quad (8.7)$$

The overall normalisation in the effective weak Hamiltonian follows the standard conventions adopted in refs. [397, 426, 428]. As anticipated, the set of operators relevant to the study of $R_{K^{(*)}}$ in eq. (8.5) is also sensitive to EWPO. The operators involving the Higgs field and lepton bilinears in the SMEFT induce tree-level modifications to EW-boson couplings. At the same time, modifications of the Z couplings to the leptons can also be induced via top quark loop contribution [459]. In the leading-log approximation and at the leading order in the top Yukawa coupling, LUV effects can be generated by:

$$\begin{aligned} \Delta g_{Z,L}^{\ell\ell} \Big|_{\text{LUV}} &= -\frac{1}{2} \left(C_{\phi L}^{(1)} \ell\ell + C_{\phi L}^{(3)} \ell\ell \right) \frac{v^2}{\Lambda^2} - 3 \left(\frac{y_t v}{4\pi \Lambda} \right)^2 \log \left(\frac{\Lambda}{\mu_{\text{EW}}} \right) C_{Lu}^{\ell\ell 33}, \\ \Delta g_{Z,R}^{\ell\ell} \Big|_{\text{LUV}} &= -\frac{1}{2} C_{\phi e}^{\ell\ell} \frac{v^2}{\Lambda^2} - 3 \left(\frac{y_t v}{4\pi \Lambda} \right)^2 \log \left(\frac{\Lambda}{\mu_{\text{EW}}} \right) C_{eu}^{\ell\ell 33}, \end{aligned} \quad (8.8)$$

where $\Delta g_{Z,L(R)}^{\ell\ell} \equiv g_{Z,L(R)}^{\ell\ell} - g_{Z,L(R)}^{\ell\ell,\text{SM}}$ is the deviation with respect to the left-handed (right-handed) leptonic couplings to the Z boson in the SM theory. Since EW couplings to leptons have been precisely measured at LEP/SLC, they provide an important test threshold for lepton universality [446, 460].

These observations motivate a global SMEFT fit of the operators explaining the B -anomalies and their interplay with EWPO. Assuming that the LUV effects are generated by NP via radiative effects, matching what is seen in eq. (8.7). Consequently, the NP will contribute to EWPO at the tree level, whilst other SMEFT operators from the REG mixing are assumed to be small or constrained from other processes. For these assumptions to be fulfilled within SMEFT, the operators modifying the EW coupling of the quarks need to be included as well

$$\mathcal{O}_{\phi Q}^{(1) \, qq}, \mathcal{O}_{\phi Q}^{(3) \, qq}, \mathcal{O}_{\phi u}^{qq}, \mathcal{O}_{\phi d}^{qq}, \quad (8.9)$$

where $q = 1, 2, 3$ identifies quark generations. These operators are considered to be flavour aligned, in a similar fashion to $C_{q\phi}$ of the previous chapter; in particular, they are assumed to be aligned with the down-quark basis. This is needed to avoid pathological tree-level FCNC [230]. The same holds for the leptonic operators, aligned with the charged lepton mass bases.

The EWPO have a degeneracy between the first and second-generation quarks, particularly in the down-type quarks sector. Therefore, it is natural to impose a $U(2)^3$ symmetry between first and second generation quark operators, thus imposing $C_{\phi Q}^{(1,3) \, 11} = C_{\phi Q}^{(1,3) \, 22}$, $C_{\phi u}^{11} = C_{\phi u}^{22}$. This also helps to suppress large FCNC contributions from these

operators. Additionally, the RGE boundary condition $C_{\phi u}^{33} = 0$ is assumed. This is motivated by the fact that this Wilson coefficient cannot be constrained by EWPO, as modifications to Z -coupling to right-handed top quarks cannot be probed by Z -pole measurements. Finally, for completeness, the four-lepton operator is also included in the fit:

$$O_{LL}^{1221} = (\bar{L}_1 \gamma^\mu L_2)(\bar{L}_2 \gamma_\mu L_1), \quad (8.10)$$

which contributes to the muon decay amplitude, and therefore alters the extraction of the Fermi constant, G_F , which is one of the inputs of the SM EW sector.

The operators in eqs. (8.3), (8.9) and (8.10), with the assumptions mentioned before, saturate all the 17 degrees of freedom, i.e. combinations of operators, that can be constrained in a fit to EWPO in the dimension-six SMEFT framework while keeping flavour changing neutral currents in the light quark sector under control. Together with the four SL-4F operators from eq. (8.4), this completes a total of 21 operators, which is included in the fit setup described in the next section.

8.1.2 SMEFT fit

The global fit combining both flavour observables related to the $b \rightarrow s\ell\ell$ anomalies and EWPO is carried out in a Bayesian statistical framework. The experimental observables are modelled via state-of-the-art theoretical information already implemented and described in ref. [428] for flavour physics and EW and Higgs physics in ref. [461] and, more recently, in ref. [460]. EWPO are extended by flavour non-universal SMEFT contributions described in ref. [446, 462]. The statistical and physics frameworks are available within the publicly available **HEPfit** [219] package. This package provides an MCMC framework that is built using the Bayesian Analysis Toolkit [463]³. The experimental input used for the global is summarised in the following, which are also implemented in **HEPfit** code:

- The fit with EWPO involves the set of EWPO including the Z -pole and W properties measurements from LEP and SLD, in addition to Tevatron and LHC measurements of EW bosons properties and rates [464–470]. The following EWPO are used in the fit

$$\begin{aligned} & M_H, m_t, \alpha_S(M_Z), \Delta\alpha_{\text{had}}^{(5)}(M_Z), \\ & M_Z, \Gamma_Z, R_{e,\mu,\tau}, \sigma_{\text{had}}, A_{FB}^{e,\mu,\tau}, A_{e,\mu,\tau}, A_{e,\tau}(P_\tau), R_{c,b}, A_{FB}^{c,b}, A_{s,c,b}, R_{u+c}, \\ & M_W, \Gamma_W, \text{BR}_{W \rightarrow e\nu, \mu\nu, \tau\nu}, \Gamma_{W \rightarrow cs}/\Gamma_{W \rightarrow ud+cs}, |V_{tb}|; \end{aligned}$$

- The angular distribution of the decay $B \rightarrow K^{(*)}\ell^+\ell^-$, this is including both the μ and e final states in the large $m_{\ell\ell}$ bins⁴. The data from ATLAS [471], Belle [420], CMS [472, 473] and LHCb [474, 475], in addition to the branching fractions from

³**HEPfit** is developed by some of my collaborators, who have co-authored this work.

⁴The measurements of $B \rightarrow K^{(*)}\ell^+\ell^-$ decays in the low di-lepton invariant mass region are plagued by large uncertainties for the J/ψ resonance, and thus not included in the fit.

- LHCb [476], the charged B^+ meson measured by LHCb [477], and the HFLAV average [478] for the branching fraction of the decay $B \rightarrow K^*\gamma$;
- The angular distribution of $B_s \rightarrow \phi\mu^+\mu^-$ [479] and the branching ratio of the decay $B_s \rightarrow \phi\gamma$ [480], measured by LHCb;
 - The LUV ratios R_K [46] and R_{K^*} [45] from LHCb and Belle [47];
 - Branching ratio of $B_{(s)} \rightarrow \mu^+\mu^-$ measured by LHCb [50], CMS [49], and ATLAS [51]; in addition to the upper bound on the decay $B_s \rightarrow e^+e^-$ reported by LHCb [52].

Modelling the decays of hadrons involves factorisable (i.e. the decay constant) and non-factorisable non-perturbative QCD effects. The non-factorisable effects emerge from long-distance hadronic contributions to QCD loops appearing in radiative corrections to these decays [391, 392, 396]. In this analysis, the $B \rightarrow K^*\ell^+\ell^-$ has two different scenarios to describe these hadronic effects, also discussed in other previous works of my collaborators [386, 426, 428, 450–452]. The first is a conservative approach (Phenomenological Data-Driven or PDD) as originally proposed in [397], and refined in ref. [386]. The second is more optimistic and based on the results of ref. [391] (Phenomenological Model Driven or PMD). The PDD scenario is based on a generic model of the hadronic effects, which is simultaneously fitted to $b \rightarrow s\ell\ell$ data alongside the NP effects. Adversely to the PDD approach, in the PMD scenario, the dispersion relations specified in [391] are used to constrain the hadronic contributions in the entire large-recoil region considered in the analysis. Ergo, PMD has smaller hadronic effects in the $B \rightarrow K^*\ell^+\ell^-$ amplitudes [450]. The choice of the hadronic uncertainties model significantly affects the outcome of the fits to the B -decays observables [428].

In order to be as general as possible, the SMEFT global fit is done for four different scenarios, described as follows:

- **EW:** Using EWPO data only with the assumptions discussed in section 8.1. This fit includes the operators in eqs. (8.3), (8.9), and (8.10), giving a total of 17 Wilson coefficients.
- **EW (SL-4F Only):** This refers to a fit done with the Wilson coefficients of the SL-4F operators involving the right-handed top current, reported in eq. (8.4). This scenario assumes that BSM enters the modifications of the Z couplings to muons and electrons through top-quark loops only.
- **EW & Flavour:** Wilson coefficients of all the 21 operators given in eq. (8.3), (8.9), and eq. (8.10), together with eq. (8.4) are varied.
All of the EW data and the flavour observables listed above are used. As explained above, this scenario comes in two varieties, PDD and PMD.
- **Flavour:** These fits exclusively include the Wilson coefficients of the *four operators* (both electrons and muons) appearing in eq. (8.4), and are done including only flavour data, i.e. excluding EW measurements. Results are again distinguished for the PDD and PMD cases. This fit is typically done when flavour anomalies

are discussed in the literature. Hence, it was included here to emphasise the importance of including EWPO.

8.1.3 Fit results

The fit was performed for each of the aforementioned scenarios, and the extracted average values of the Wilson coefficients and the corresponding 68% CI are summarised in Figure 8.2. The EW only fits, involving 17 out of the total 21 Wilson coefficients are shown in orange. The EWPO fit shows good agreements with the SM within 2σ level. Additionally, the Wilson coefficients involved in the fit seem to be highly correlated with the EWPO data as indicated by the correlation matrix in Figure 8.3. The impact of these operators on the $b \rightarrow s\ell\ell$ observables are shown in Figure 8.4, where it collects the mean and standard deviation on the shift in the Z coupling to light leptons w.r.t the SM, it should be noted that these deviations of the Z couplings are related to the LUV ratios $R_{K^{(*)}}$ in the dilepton-mass range [1.0, 6.0] GeV by:

$$\delta g_{Z,L(R)}^{ee(\mu\mu)} \equiv g_{Z,L(R)}^{ee(\mu\mu)}/g_{Z,L(R)}^{ee(\mu\mu),\text{SM}} - 1 , \quad \delta R_{K^{(*)}} \equiv R_{K^{(*)}} - R_{K^{(*)}}^{\text{SM}} , \quad (8.11)$$

which is tightly constraint by the EWPO data to per-mille level.

The other fit scenario only involves the **SL-4F** coefficients constraint from EWPO data, shown in yellow in Figure 8.2. Although EW data allows for more relaxed constraints on these operators, for example $\mathcal{O}_{Lu}^{\ell\ell 33}$ compared to the ones modifying Z couplings at tree-level e.g. $\mathcal{O}_{\phi L}$, the bounds remain compatible with the null (SM) Hypothesis and in ca. 3σ conflict with the experimental measurements on $R_{K^{(*)}}$ (indicated by the shaded red boxes in the right side of Figure 8.4).

We now move to the flavour data fits, with both ansätze for the hadronic contributions PDD highlighted in blue and PMD in pink. For this fit, deviations of the muonic C_{Lu}^{2233} show deviation from the SM hypothesis of 3σ for PDD and up to 6σ for the optimistic PMD scenario. The difference in the significance between the two cases stems from the interpretation of the angular analysis –namely the P'_5 observable– of the $B \rightarrow K^*\mu\mu$ decay. The PDD approach favours the fully left-handed NP coupling, i.e. $C_{9,\ell} = -C_{10,\ell}$, and allows for NP coupling to electrons, while the PMD exclusively predicts the muonic resolution [426, 428]. Flavour data seem to predict deviations in the Z coupling modifiers, implying a tension between the flavour fits and EWPO exacerbated by the PMD modelling of the long-distance QCD effects. This tension between B -anomalies and EW data reach $3(6)\sigma$ level for PDD(PMD). Of course, introducing a tree-level resolution of the $b \rightarrow s\ell\ell$ anomalies would decouple EW sensitive SMEFT operators from the four-fermion operators required for these anomalies. Still, it will not be compatible with the MFV ansatz. In fact, the size of flavour violation introduced by the tree-level resolution of the B anomalies brings any model with such structure to the brick of exclusion by other flavour observables [230, 409–411].

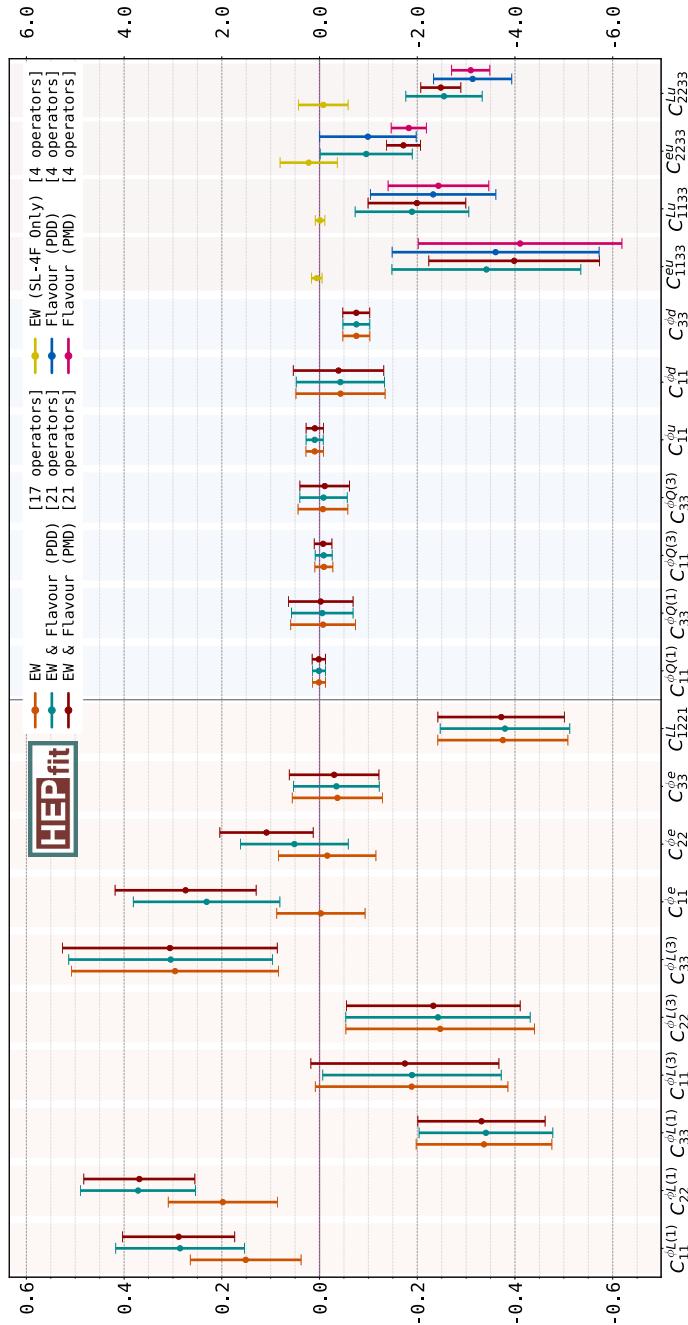


Figure 8.2. The marginalised fit results of the Wilson coefficients are considered in the scenarios detailed in subsection 8.1.2. The central points denote the mean of the marginalised posterior distribution, while the error bars are the 68% CI constraint of the Wilson coefficients. (Note the different scaling in the axes quantifying the size of the bounds presented in each half of the figure.) This figure is published in [453].

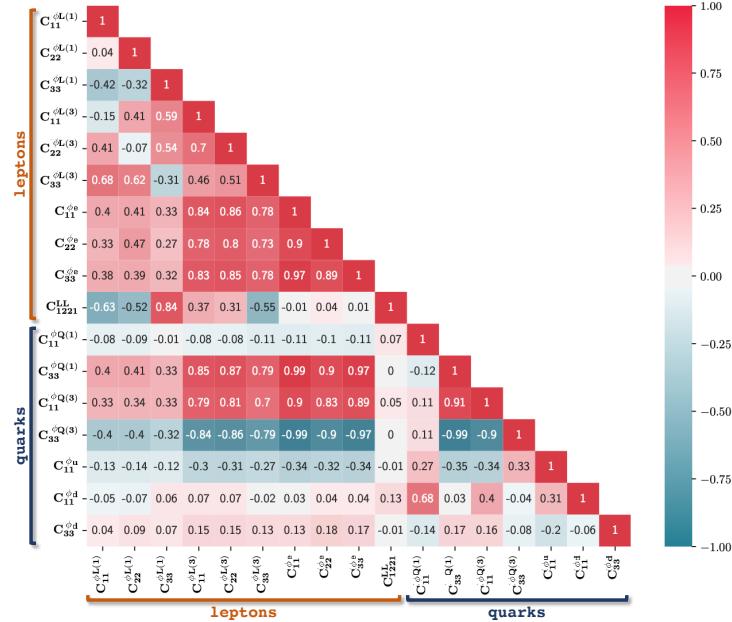


Figure 8.3. The correlation matrix resulting from the Bayesian fit of the Wilson coefficient of the operators listed in eqs. (8.3), (8.9), (8.10) in the **EW** scenario introduced in subsection 8.1.2. The two distinct groups of Wilson coefficients associated to leptonic and quark interactions are remarked as “leptons” and “quarks”, respectively. This figure is published in [453].

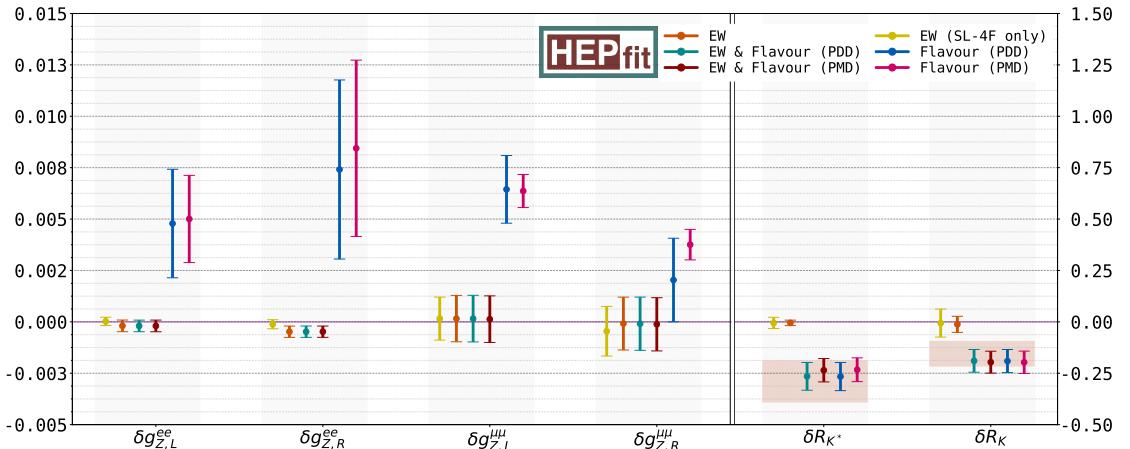


Figure 8.4. Fit results following the same convention as Figure 8.2 for the Z boson coupling modifiers for the muons and electrons, as well as the lepton universality violating ratios, see eq. (8.11), with the red boxes indicating the region selected by the experimental measurements of $R_{K,(K^*)}$. This figure is published in [453].

A global fit with the 21 coefficients, combining both flavour and EW data, is the way to reach consensus between what is required by $b \rightarrow s\ell\ell$ observations resolution and EW precision tests. Similarly to the flavour scenario, the fit is performed for PDD in teal

and PMD in red in [Figure 8.2](#) and [Figure 8.4](#). In these scenarios, the tension between EWPO and flavour data is lifted as the deviation from the SM Z -couplings remains within the EW data predictions. Also, the LUV generated by the Wilson coefficients matches the experimental observations. The resolution comes from deviation of $C_{\phi L(e)}^{\ell\ell}$ and the four-fermion operators $\mathcal{O}_{(L)eu}^{\ell\ell 33}$ from the SM hypothesis.

Another interesting observation from the global fit can be seen in the network graphs in [Figure 8.5](#), wherein the EW only fits the SL-4F Wilson coefficients are degenerate with the Higgs-lepton bilinear currents $C_{\phi L(e)}^{\ell\ell}$, having Pearson's correlation of $\rho \sim -1.0$. This degeneracy is broken once both EW and flavour data are taken into account, as seen in the lower panels of this figure. The breaking of the degeneracy is the reason for the observed shifts in the posterior distributions of $C_{\phi L(e)}^{\ell\ell}$ from the SM hypothesis.

It is not necessary to invoke all of the 21 SMEFT operators considered in the EW & Flavour scenario to have a resolution for the flavour anomalies and EWPO. A simpler picture using two or four operators satisfies the experimental need to explain LUV and respect EW measurements. This picture contains the fully left-handed operator, $\mathcal{O}_{LQ}^{\ell\ell 23}$ and $\mathcal{O}_{\phi L}^{(1)\ell\ell}$. The former operator would be generated at a loop-level by $\mathcal{O}_{Lu}^{\ell\ell 33}$, while the latter at the tree level. This minimalist SMEFT approach would then include only $\mathcal{O}_{\phi L}^{(1)\ell\ell}$ and $\mathcal{O}_{Lu}^{\ell\ell 33}$, and $\ell = \mu, e$. The model could involve either muons, electrons or both of them.

In [Figure 8.6](#), the EWPO (grey), flavour with PDD (orange) and combined (magenta) fits for this minimal SMEFT model. For the muonic solution, see [Appendix D](#) for the electronic solution. We observe that the tension between the aforementioned EWPO and $b \rightarrow s\ell\ell$ data if individual fits were performed, which is resolved in the combined fit. However, this induces a correlation between the four-fermion operator $\mathcal{O}_{Lu}^{\ell\ell 33}$ and the one involving the Higgs-doublet and lepton bilinears. This model also obeys MFV assumptions, protecting it from other flavour observables. However, as mentioned earlier, the B anomalies have to be explained at the one-loop level. Finally, note that the role played here by $\mathcal{O}_{Lu}^{\ell\ell 33}$ could be shared, in part, with $\mathcal{O}_{eu}^{\ell\ell 33}$, depending on how much departure is required from the fully left-handed solution to B anomalies. As already noted, this fact critically depends on the information stemming from the angular analysis of $B \rightarrow K^* \mu\mu$ [428]. On general grounds, to relieve the bounds from EWPO, the presence of $\mathcal{O}_{eu}^{\ell\ell 33}$ would also necessitate sizeable NP effects from $\mathcal{O}_{\phi e}^{\ell\ell}$, thus leaving us with a maximum of four needed operators to explain the flavour anomalies without being excluded by EWPO or including complex flavour structures.

8.2 Z' with vector-like partners

Exhilarated by the SMEFT fit and the consequent simplified model discussed in the previous section, I present some UV-complete models that explain the B -anomalies at the loop level; without adding extra flavour violation; and abide by the EWPO constraints. The first model that satisfies these requirements is based on a Z' model published in ref. [440]. This model is a simple extension of the SM gauge group by an additional

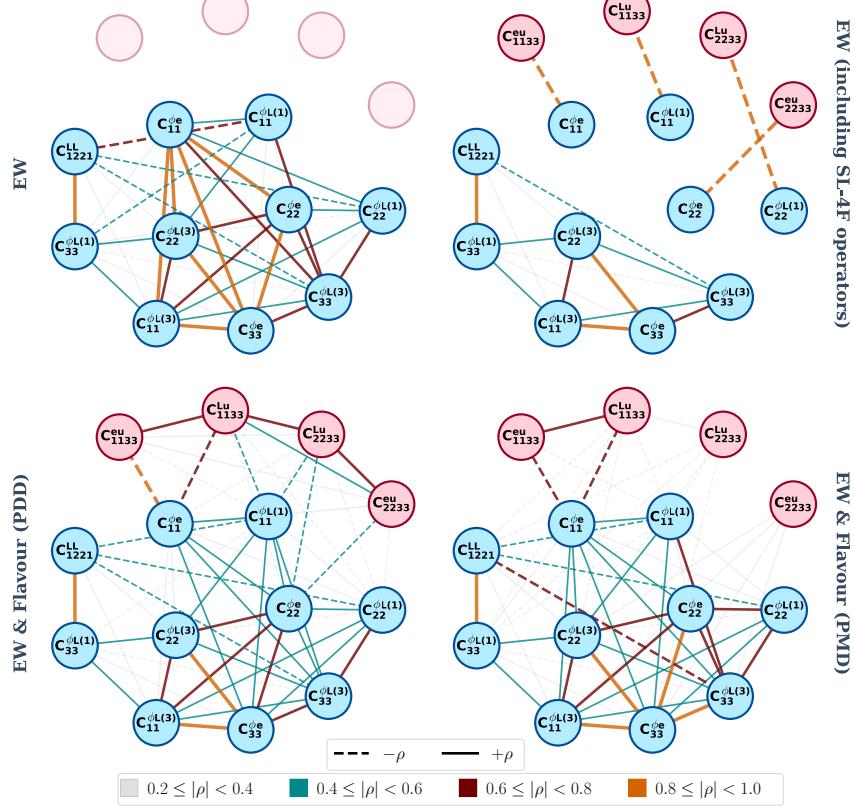


Figure 8.5. Network plot of the correlation between the Wilson coefficients considered in this study. The upper left panel shows the correlations from the **EW** fit, the upper right panel for the same fit but with the SL-4F Wilson coefficients included in the fit. The lower panel includes the flavour anomalies data in the **EW+Flavour** scenario, in which the degeneracy is broken. The lower left panel is for the PDD hadronic effects, while the lower right one is for the PMD case. This figure is published in [453].

Abelian group $U(1)_X$ with a corresponding gauge boson X_μ identified as the Z' . The SM fields have no X charge. This gauge symmetry is spontaneously broken by a vev of an additional scalar singlet S , which gives a mass to the Z' boson $m_{Z'} = g_X \langle S \rangle$. A top-quark T and a muon M VLQ partners are added as well. These two fields mix with the top u_3 and muon L_2 via Yukawa interaction terms with the scalar field S . Kinematic mixing between the Z' and the SM Z boson, as well as between the Higgs and the new scalar are assumed to be negligible. The new fields and their representation under the SM plus the new gauge group are summarised in Table 8.1.

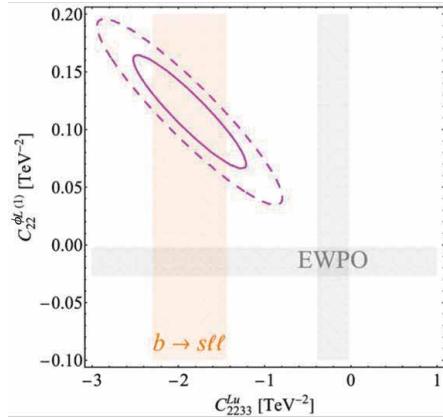


Figure 8.6. A minimal solution for the flavour anomalies within SMEFT while respecting EWPO for the four-fermion operators involving the muon. EWPO fits are the grey regions, while the $b \rightarrow s\ell\ell$ measurements fits with PDD ansatz are highlighted by the orange bands. The combined fit's 1 and 2σ contours are magenta coloured. This plot has been published in [453].

This model is completely characterized by eight new parameters: the gauge coupling g_X , the mass μ_S and quartic λ_S of the renormalizable potential of S , the new Yukawa couplings $Y_{T,M}$, here taken to be real, and the vector-like mass-term parameters $M_{T,M}$. The Lagrangian of the model contains the following terms:

$$\begin{aligned} \mathcal{L} = & M_T \bar{T}_R T_L + M_M \bar{M}_R M_L + Y_t \bar{u}_3 \tilde{\phi}^\dagger Q_3 \\ & + Y_T \bar{u}_3 T_L S + Y_\mu \bar{e}_2 \phi^\dagger L_2 + Y_M \bar{M}_R L_2 S + \text{h.c.} . \end{aligned} \quad (8.12)$$

From this Lagrangian, one can read off the mixing terms between the SM fields and

Particle/Field	$G_{\text{SM}} \otimes U(1)_X$ multiplicity
VL fermions	
T	$(\mathbf{3}, \mathbf{2})_{Y=\frac{1}{6}, X=-1}$
M	$(\mathbf{1}, \mathbf{2})_{\frac{1}{2}, -1}$
Gauge boson	
X_μ	$(\mathbf{1}, \mathbf{1})_{0,0}$
Scalar	
S	$(\mathbf{1}, \mathbf{1})_{0,1}$

Table 8.1. The added fields of this model and their representation under the SM gauge group and the new $U(1)_X$. Note that the new charge assignment here is not unique, and the model would produce the same phenomenology with different but consistent assignment.

vector-like partners.⁵ The spontaneous symmetry breaking of $U(1)_X$ is achieved by a non-vanishing vev $\langle S \rangle^2 = -\mu_S^2/(2\lambda_S) \equiv \eta^2 \neq 0$, that implies the following fermionic mixing patterns:

$$\begin{aligned} \text{top sector: } & \left(\begin{array}{cc} \bar{u}_3 & \bar{\mathbf{T}}_R \end{array} \right) \left(\begin{array}{cc} \frac{Y_t v}{\sqrt{2}} & \frac{Y_{\mathbf{T}} \eta}{\sqrt{2}} \\ 0 & M_{\mathbf{T}} \end{array} \right) \left(\begin{array}{c} U_3 \\ \mathbf{T}_L \end{array} \right) + \text{h.c.}, \\ \text{muon sector: } & \left(\begin{array}{cc} \bar{e}_2 & \bar{\mathbf{M}}_R \end{array} \right) \left(\begin{array}{cc} \frac{Y_\mu v}{\sqrt{2}} & 0 \\ \frac{Y_{\mathbf{M}} \eta}{\sqrt{2}} & M_{\mathbf{M}} \end{array} \right) \left(\begin{array}{c} L_2 \\ \mathbf{M}_L \end{array} \right) + \text{h.c.}, \end{aligned} \quad (8.13)$$

where U_i (E_i) indicates the Q_i -component (L_i -component) with weak isospin $1/2$ ($-1/2$). Using the determinant and trace of the squared mass matrices, one can easily show that the eigenvalues $m_{t,\mathbf{T}}$ and $m_{\mu,\mathbf{M}}$ must satisfy [440]:

$$\begin{aligned} m_{t(\mu)} m_{\mathbf{T}(\mathbf{M})} &= \frac{1}{\sqrt{2}} Y_{t(\mu)} v M_{\mathbf{T}(\mathbf{M})}, \\ m_{t(\mu)}^2 + m_{\mathbf{T}(\mathbf{M})}^2 &= M_{\mathbf{T}(\mathbf{M})}^2 + \frac{1}{2}(Y_{t(\mu)} v)^2 + \frac{1}{2}(Y_{\mathbf{T}(\mathbf{M})} \eta)^2, \end{aligned} \quad (8.14)$$

which in the decoupling limit clearly yield: $m_{t(\mu)} \simeq Y_{t(\mu)} v / \sqrt{2}$, $m_{\mathbf{T}(\mathbf{M})} \simeq M_{\mathbf{T}(\mathbf{M})}$. Defining for the top sector the rotation matrix from the interaction to the mass basis following the convention:

$$\left(\begin{array}{c} t_{R(L)} \\ \mathbf{T}'_{R(L)} \end{array} \right) = \left(\begin{array}{cc} \cos \theta_{R(L)}^t & -\sin \theta_{R(L)}^t \\ \sin \theta_{R(L)}^t & \cos \theta_{R(L)}^t \end{array} \right) \left(\begin{array}{c} u_3(U_3) \\ \mathbf{T}_{R(L)} \end{array} \right), \quad (8.15)$$

and doing similarly for the muonic sector, the mixing angles between SM fields, t and μ , and their partner mass eigenstates, \mathbf{T}' and \mathbf{M}' , can be conveniently expressed in terms of the dimensionless ratios $\xi_{\mathbf{T},\mathbf{M}}$ and $\varepsilon_{t,\mu}$:

$$\begin{aligned} \tan 2\theta_R^t &= \frac{2\xi_{\mathbf{T}}}{\xi_{\mathbf{T}}^2 - \varepsilon_t^2 - 1}, \quad \tan 2\theta_L^t = \frac{2\varepsilon_t}{\xi_{\mathbf{T}}^2 - \varepsilon_t^2 + 1}, \text{ with } \varepsilon_t \equiv \frac{Y_t v}{Y_{\mathbf{T}} \eta}, \quad \xi_{\mathbf{T}} \equiv \frac{\sqrt{2} M_{\mathbf{T}}}{\eta Y_{\mathbf{T}}}; \\ \tan 2\theta_R^\mu &= \frac{2\varepsilon_\mu}{\xi_{\mathbf{M}}^2 - \varepsilon_\mu^2 + 1}, \quad \tan 2\theta_L^\mu = \frac{2\xi_{\mathbf{M}}}{\xi_{\mathbf{M}}^2 - \varepsilon_\mu^2 - 1}, \text{ with } \varepsilon_\mu \equiv \frac{Y_\mu v}{Y_{\mathbf{M}} \eta}, \quad \xi_{\mathbf{M}} \equiv \frac{\sqrt{2} M_{\mathbf{M}}}{\eta Y_{\mathbf{M}}}. \end{aligned} \quad (8.16)$$

Perturbatively expanding in $\varepsilon_{t,\mu}$, eq. (8.16) will illustrate that the mixing in the top sector proceeds mainly through $\tan \theta_R^t \simeq 1/\xi_{\mathbf{T}}$, while in the muonic sector one has $\tan \theta_L^\mu \simeq 1/\xi_{\mathbf{M}}$ and negligible $\tan \theta_R^\mu$. Hence, for $\varepsilon_{t,\mu}/\xi_{\mathbf{T},\mathbf{M}} = Y_{t,\mu} v / \sqrt{2} M_{\mathbf{T},\mathbf{M}} < 1$, the leading couplings of the Z' boson to the SM fields correspond to right-handed top-quarks

⁵Note that upon an opposite $U(1)_X$ charge assignment for the vector-like fermionic partners than the one implicitly assumed, one should replace in eq. (8.12) S with S^\dagger .

and to left-handed muons as well as neutrinos, these couplings are given by

$$g_{Z't_R} = g_X \sin^2 \theta_R^t = \frac{g_X}{1 + \xi_T^2} + \mathcal{O}\left(\varepsilon_t^2/\xi_T^2\right), \quad (8.17)$$

$$g_{Z'\mu_L(\nu)} = g_X \sin^2 \theta_L^\mu = \frac{g_X}{1 + \xi_M^2} + \mathcal{O}\left(\varepsilon_\mu^2/\xi_M^2\right), \quad (8.18)$$

with $g_{Z't_L(\mu_R)}$ contributing only at order $\varepsilon_{t(\mu)}/\xi_{T(M)}^2$. The $b \rightarrow s\ell\ell$ anomalies can be ex-

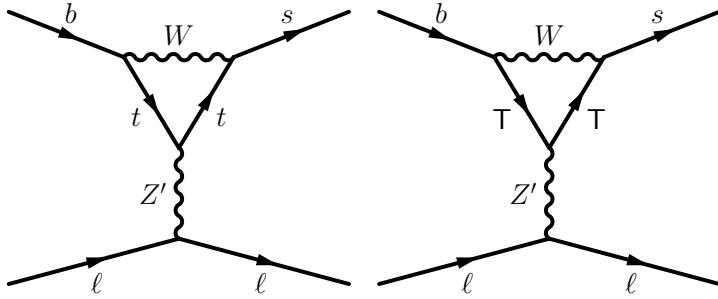


Figure 8.7. FCNC penguins with LUV emerging from the Z' model, explaining the $b \rightarrow s\ell\ell$ anomalies at loop-level. The penguin diagrams with the top-partners in the loop are the dominant ones.

plained in this model via penguin (also box) diagrams with LUV as shown in Figure 8.7. Since the Z' couples to the muons and not the electrons, LUV is generated at loop-level.

8.2.1 SMEFT matching and constraints

Integrating out the Z' generates the operator \mathcal{O}_{Lu}^{2233} with the matching condition:

$$C_{Lu}^{2233} = -\frac{g_{Z't_R} g_{Z'\mu_L}}{m_{Z'}^2} \simeq -\frac{1}{(1 + \xi_T^2)(1 + \xi_M^2)\eta^2}, \quad (8.19)$$

Together with four-fermion operators built of t_R or μ_L, ν fields that can be potentially probed at collider and by experimental signatures like ν -trident production. From eq. (8.19), it is clear that in order to have $|C_{Lu}^{2233}| \sim 2 \text{ TeV}^{-2}$ as required by the fit in Figure 8.6, the SSB of the new gauge group needs to happen at a scale close to the EW, namely $\eta \lesssim \text{TeV}$;⁶ for $m_{Z'} \sim \text{TeV}$ this leads to a natural coupling $g_X \gtrsim 1$.

The main collider constraints come from the resonant di-muon searches [481] followed by the production of top-quark pair $pp \rightarrow Z' \rightarrow t\bar{t}$ [482]. In Figure 8.8, these searches are projected onto this model, with the choice of $\eta = 1 \text{ TeV}$ and other parameters chosen to be preferred by the B anomalies observables, we see that the constraints on this model are dominated by the resonant di-muon searches. The theoretical prediction of the resonant

⁶Note that even for masses as low as $\mu_S \sim \mathcal{O}(v)$, for $\eta \simeq v$ and $\lambda_S \sim \mathcal{O}(1)$, the interactions of S do not alter the phenomenology discussed here since the largest S -generated effects are still suppressed as $\mathcal{O}(\varepsilon_t^2/\xi_T^2)$.

top-quark pair and di-muon production via gluon fusion $gg \rightarrow Z' \rightarrow t\bar{t}/\mu\mu$, in this model, has been calculated at NLO using the two-loop triangle calculations presented in chapter 4.

Figure 8.9 collects the constraints on this model, starting with the 1σ region corresponding to the explanation of B anomalies via eq. (8.19) in the parameter space $\xi_{T(M)}$. The gauge coupling g_X is fixed to $g_X = m_{Z'}/\eta$ for a tentative Z' gauge boson at the TeV scale and the vev of the new scalar field S is set to $\eta = 250$ GeV and $\eta = 500$ GeV in the left and right panel, respectively. In the same plot, the collider searches are also presented, re-interpreted from the results presented in ref. [445].

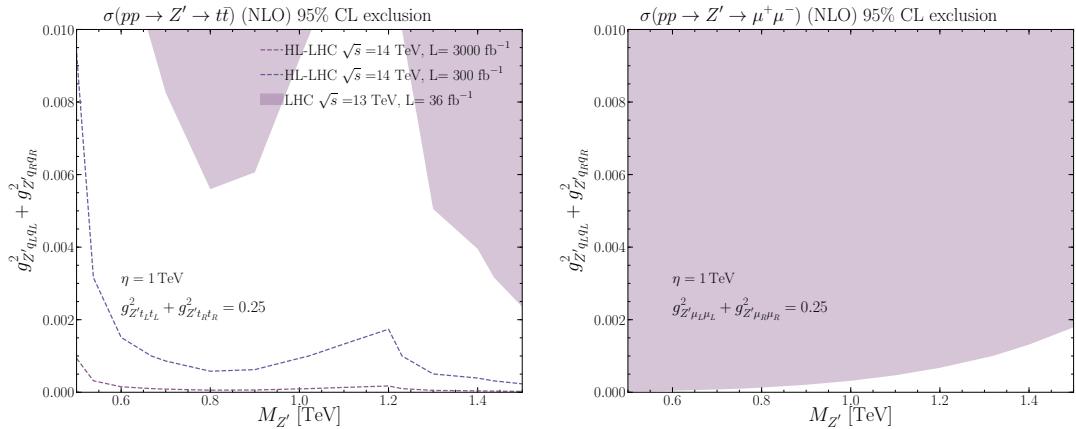


Figure 8.8. Direct searches for Z' using top-quark pair production [482] and di-muon searches [482]. The gluon fusion cross-sections for this model were calculated at NLO using the results of the two-loop triangle calculations of the process $gg \rightarrow Z^*$ preformed in chapter 4.

The bounds from neutrino-trident production performed in [483] constrain small ξ_M , where the 95 %CL bounds are shown in the orange band of the plot. The top-phillic Z' is predominantly produced at tree-level in association with top-quark pair. In the blue region, the 95% high- p_T constraint stemming from the recasting of the $pp \rightarrow \mu^- \mu^+ t\bar{t}$ is shown using the search conducted by ATLAS [481, 484]. The cyan contours are constraints coming from four-top production analysis from CMS [485], see ref. [445] for more details. The prospects constraining this model at the early runs of the HL-LHC with integrated luminosity 300 fb^{-1} are also explored and indicated with the dashed lines. The model benchmark that is shown in the right panel of Figure 8.9 shows a promising potential for discovery at the HL-LHC.

In the same figure, fixing the partner Yukawa coupling to $\mathcal{O}(1)$ values as reported in the two panels, I mark in grey the region corresponding to the bound on the mass of the vector-like partner observed from collider searches, taken to be $m_T = 1.4$ TeV from the search at ATLAS in ref. [486], and $m_M = 0.8$ TeV from the CMS analysis of ref. [487].

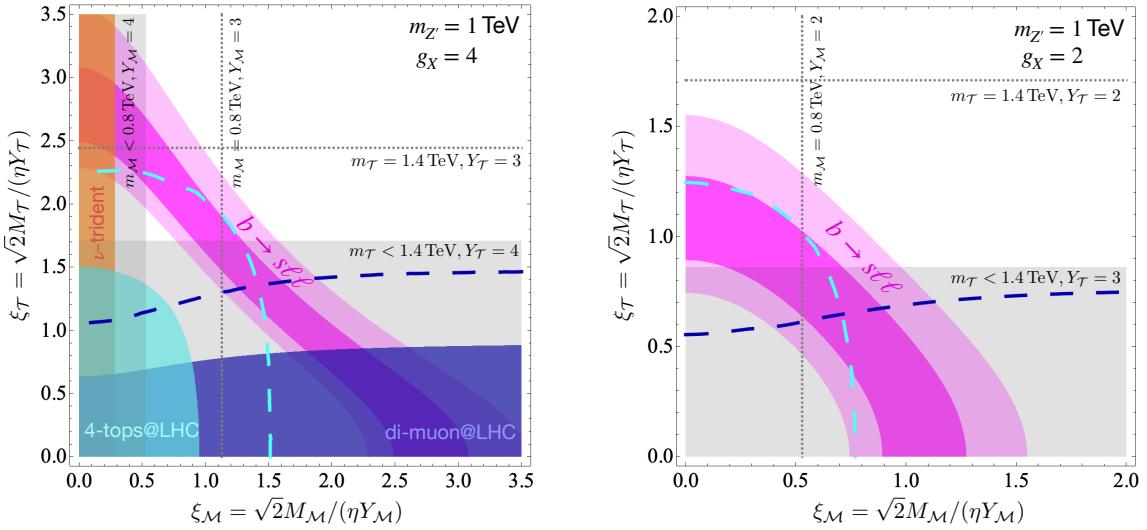


Figure 8.9. Collective of the constraints on the Z' model is presented: The magenta regions show the 68% and 95% CL constraints from $b \rightarrow sll$ anomalies, while the rest are the collider searches re-interpreted from the ones in ref. [445]. The projections for the early HL-LHC (at 300 fb^{-1}) constraints are shown as dashed lines. Grey regions underlie the parameter space where the mass of the vector-like partner lies below current collider limits for a fixed Yukawa coupling as explicitly reported. The dashed lines show the corresponding shift of the limit due to a smaller value of the same type of Yukawa coupling. The left panel is for $\eta = m'_Z/4$ and the right panel is for $\eta = m'_Z/2$. This figure is published in [453].

8.2.2 Expanding the model

For this model to survive EWPO constraints, it needs to induce $\mathcal{O}_{\phi L}^{(1) 22}$ with the same correlation patterns observed in [Figure 8.6](#). In principle, it is possible to achieve that by inducing tree-level $z - Z'$ mixing by charging S under $U_Y(1)$ in addition to $U_X(1)$, thereby inducing some misalignment in the weak hypercharge Y . However, this will create a tree-level (Drell Yan-like) resonant di-muon production enhancement, far beyond what is allowed by current collider searches [481]. Therefore, this mechanism is not possible. In order to accommodate for EW precision constraints, this model needs to be expanded further by including new vector-like leptonic states, like the ones discussed in refs. [488, 489]. These new degrees of freedom are interesting by their own merit, in particular with resolving the anomaly associated with $(g-2)_\mu$ [490, 491], also as neutrino mass source and interesting collider phenomenology [492, 493].

The simplest resolution can be accomplished by the inclusion of two new vector-like muonic partners: a singlet under $SU(2)_L$, S_Y , and a triplet of $SU(2)_L$, T_Y , where in both cases the subscript Y denotes the hypercharge of the fermion. Since they are vector-like fermions, they have a mass term, thus adding new parameters M_{S_Y, T_Y} . Their mixing with the SM leptons comes -like M- from the Yukawa term, which for $Y = 0$ is given by

$$\mathcal{Y}_{S_0} \bar{S}_{0,R} \tilde{\phi}^\dagger L_2 + \mathcal{Y}_{T_0} \bar{T}_{0,R}^A \tau^A \tilde{\phi}^\dagger L_2 + \text{h.c.} . \quad (8.20)$$

Another possibility of interest may be the one of replacing in eq. (8.20) $\tilde{\phi}$ with the Higgs doublet, ϕ , and then the pair of vector-like partners with hypercharge $Y = 1$. The matching condition for these new fields produces the needed SMEFT operators, and the values and sign of the corresponding Wilson coefficients are given by the interplay between these fields [489, 490] of the form:

$$\begin{aligned} C_{\phi L}^{(1) 22} &= \frac{\mathcal{Y}_{S_0}^2}{4M_{S_0}^2} - \frac{\mathcal{Y}_{S_1}^2}{4M_{S_1}^2} + \frac{3\mathcal{Y}_{T_0}^2}{4M_{T_0}^2} - \frac{3\mathcal{Y}_{T_1}^2}{4M_{T_1}^2} , \\ C_{\phi L}^{(3) 22} &= -\frac{\mathcal{Y}_{S_0}^2}{4M_{S_0}^2} - \frac{\mathcal{Y}_{S_1}^2}{4M_{S_1}^2} + \frac{\mathcal{Y}_{T_0}^2}{4M_{T_0}^2} + \frac{\mathcal{Y}_{T_1}^2}{4M_{T_1}^2} . \end{aligned} \quad (8.21)$$

In order to obtain the needed value and sign of $C_{\phi L}^{(1) 22} \sim 0.1$ but also vanishing or negligible $C_{\phi L}^{(3) 22}$ some tuning between the singlet and the $Y = 0$ triplet is needed. This tuning is stable under the RGE running once generated at the NP scale.

8.3 Leptoquark scenarios

Leptoquark models are generically predicted in grand unified theories (GUTs) [494, 495]. They typically generate a baryon violating process that leads to proton decay, which is severely constrained. However, in light of the simplified SMEFT model discussed earlier [Figure 8.6](#), it is possible to introduce leptoquarks (LQ) that couple non-universally to quark and lepton generations. These LQs are within reach of colliders and not pushed

to the GUT scale like their flavour-universal counterparts. Actually, they are potential candidates for explaining the flavour anomalies [445, 496]. Such models typically involve a highly non-trivial flavour structure. For a comprehensive survey of LQ models, see for instance [232, 436, 497–499].

In this section, I only discuss LQs that generate $C_{Lu}^{\ell\ell 33}$ and $C_{eu}^{\ell\ell 33}$, and introduce LUV in $b \rightarrow s\ell\ell$ transition at loop-level in accordance with the two main assumptions stated in the introduction, as shown in Figure 8.10. With that in mind, only a handful of LQs models remain; they are summarised in Table 8.2. From this table, it is possible to

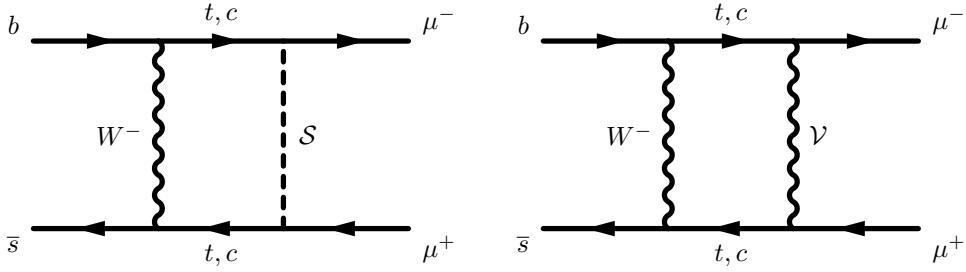


Figure 8.10. Box diagrams generated by scalar \mathcal{S} (left) and vector \mathcal{V} LQs, of the $b \rightarrow s\ell\ell$ transition with LUV.

Vector LQ: \mathcal{V}^μ	$SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$	Comments
$\bar{L}_\ell \gamma_\mu (\tau^A) Q_3 \mathcal{V}^{\mu(A)}$	$(\bar{\mathbf{3}}, \mathbf{1} \text{ or } \mathbf{3})_{-\frac{2}{3}}$	not of interest
$(\mathcal{V}^\mu)^\dagger \bar{e}_\ell^c \gamma_\mu Q_3$	$(\bar{\mathbf{3}}, \mathbf{2})_{\frac{5}{6}}$	not of interest
$\bar{L}_\ell^c \gamma_\mu u_3 i\tau^2 \mathcal{V}^\mu$	$(\bar{\mathbf{3}}, \mathbf{2})_{-\frac{1}{6}}$	generates $C_{\ell\ell 33}^{Lu} > 0$
$\bar{e}_\ell \gamma_\mu u_3 \mathcal{V}^\mu$	$(\bar{\mathbf{3}}, \mathbf{1})_{-\frac{5}{3}}$	generates $C_{\ell\ell 33}^{eu} < 0$
Scalar LQ: \mathcal{S}		
$\bar{L}_\ell (\tau^A) (i\tau^2) Q_3^c \mathcal{S}^{\dagger(A)}$	$(\bar{\mathbf{3}}, \mathbf{1} \text{ or } \mathbf{3}, 1/3)$	not of interest
$\bar{e}_\ell Q_3 i\tau^2 \mathcal{S}$	$(\bar{\mathbf{3}}, \mathbf{2})_{-\frac{7}{6}}$	not of interest
$\bar{L}_\ell u_3 \mathcal{S}$	$(\bar{\mathbf{3}}, \mathbf{2})_{-\frac{7}{6}}$	generates $C_{\ell\ell 33}^{Lu} < 0$
$\bar{e}_\ell^c u_3 \mathcal{S}$	$(\bar{\mathbf{3}}, \mathbf{1})_{\frac{1}{3}}$	generates $C_{\ell\ell 33}^{eu} > 0$

Table 8.2. Scalar and vector LQ interactions under scrutiny: LQs of interest for this analysis have to generate the dimension-six operators $\mathcal{O}_{Lu,eu}^{\ell\ell 33}$. Models that generate operators chirality structures other than Lu and eu are not of interest. This table is published in [453].

recognise the suitable models that explain the B anomalies at one loop as predicted in Figure 8.6. Unlike the Z' model, there are distinct cases for NP coupling to the electron or the muon: the case of the vector LQ $\mathcal{V}^\mu \sim (\bar{\mathbf{3}}, \mathbf{2}, -1/6)$ for LUV effects originating from electron couplings, and the scalar $\mathcal{S} \sim (\bar{\mathbf{3}}, \mathbf{2}, -7/6)$ for the ones associated to

muons. The interaction terms of interest are:

$$\mathcal{L}_{V\bar{f}f} = \tilde{\lambda}_{te} \bar{L}_1^c \gamma_\mu u_3 i\tau^2 V^\mu + \text{h.c.}, \quad \mathcal{L}_{S\bar{f}f} = \lambda_{t\mu} \bar{L}_2 u_3 S + \text{h.c..} \quad (8.22)$$

When the LQs are integrated out, we arrive to the matching to SMEFT

$$C_{Lu}^{1133} = +\frac{|\tilde{\lambda}_{te}|^2}{M_V^2}, \quad C_{Lu}^{2233} = -\frac{|\lambda_{t\mu}|^2}{2M_S^2}. \quad (8.23)$$

The sign difference between the vector and scalar LQs stems from the Fierz transformations used during the SMEFT matching. The LQ models are simpler in terms of added fields and parameters than the Z' counterpart, this also reflects on their collider constraints. The scalar LQ with muonic coupling is only constrained by $pp \rightarrow t\bar{t}\mu\mu$, while the vector electro-philic LQ is constrained from $t\bar{t}2\nu$ searches. In Figure 8.11, I show these bounds taken from the study of ref. [500]. The magenta regions show where the model predicts the correct $b \rightarrow s\ell\ell$ anomalies. These LQs generate $C_{\phi L}^{(1)} \ell\ell$ only at

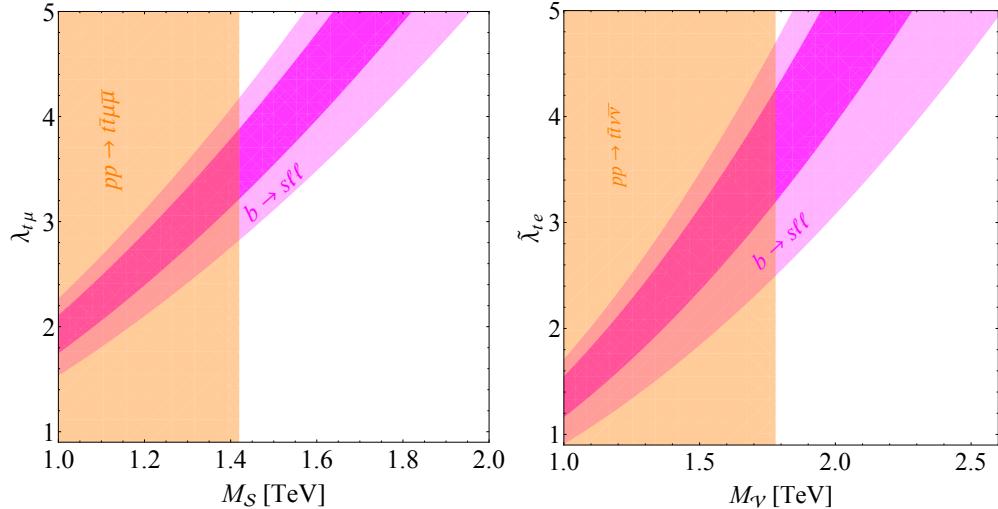


Figure 8.11. Constraints on the mass and LQ coupling with the muon for the scalar LQ model \mathcal{S} on the left panel; while on the right panel the vector electro-philic LQ model parameters constraints are shown. The orange band shown the collider bounds based on the comprehensive analysis found in ref. [500] The magenta regions show the models phase space at 68% and 95% CL that explains the flavour anomalies at one-loop.

loop-level, see Figure 8.12, which is insufficient to fulfil the requirements of both the flavour and EWPO fit, as it would generate $C_{\phi L}$ of order $\mathcal{O}(10^{-3})$, which is too small according to Figure 8.6. Hence, the addition of the extra singlet and triplet leptonic partners discussed in the previous section is again needed to fulfil the EWPO constraints.

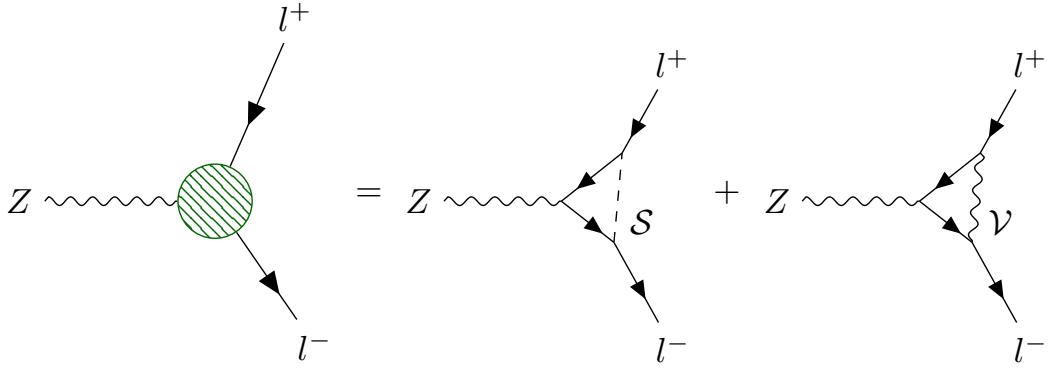


Figure 8.12. The LQs considered can only generate $C_{\phi L}^{(1)} \ell\ell$ via loop matching.

8.4 Conclusion

This chapter addressed the recent $b \rightarrow s\ell\ell$ anomalies in terms of NP models that fall under the assumptions of MFV, which required that LUV effects to be generated at the loop level. The interplay between EWPO and these anomalies in terms of the SMEFT was portrayed in Figure 8.2 and supported with Figure 8.4.

The global SMEFT fit hints that a unifying solution for EWPO and LUV anomalies can be achieved by including the right operators. Indeed only two operators either for the muons or electrons are strictly necessary, see Figure 8.6 and Appendix D. Like any multivariate analysis, the correlation amongst the coefficients played an essential role in finding the proper resolution of the EWPO and flavour observables conundrum.

Inspired by the simplified SMEFT model, I have discussed a top-philic Z' model with top and muon vector-like partners. Moreover, an alternative, simpler model based on leptoquarks can also produce the B anomalies at the loop level. Both models can be amended to include muonic or electronic solutions in the SMEFT simplified scenario. For the Z' model, the top-quark and lepton partners need to have the same X charge for the muon case, while they need to carry an opposite charge for the electronic NP coupling. The LQ models are different for the muonic and electronic cases; the former is compatible with a scalar and the latter with a vector LQ. Both of these models required the inclusion of correlated pairs of vector-like leptons, a $SU(2)_L$ singlet and a triplet to realise the minimal EFT scenario depicted on Figure 8.6. The existence of these particles may be independently motivated by the heavy new dynamics underlying the origin of neutrino masses and/or by a tentative explanation of the $(g - 2)_\mu$ anomaly [490, 491].

Future measurements of B decays by the LHCb and Belle-II are expected to reach a precision regime in the upcoming years [422, 501]. These measurements, in addition to high-energy ones at linear colliders [366, 462] will reveal more about the nature of these anomalies and their connection with Higgs physics. This is already hinted at by the global fits done here with the current data predicting NP Higgs operators like $C_{\phi L/e}$. Understanding how observables from different sectors correlate is essential to understanding the nature of NP underlying these anomalies, amongst others.

9 Conclusion

Constraints on Higgs observables are deeply intertwined with the top quark and flavour physics. This has been highlighted throughout the entirety of this thesis and the literature reviewed within. The era of Higgs precision measurements is on the horizon, prompting the inclusion of higher-order corrections to Higgs processes, which requires improved techniques for their calculation. An example of these techniques is the p_T expansion, first employed to obtain an analytic form for the Higgs pair virtual corrections [11]. This technique was used in chapter 4 for obtaining the QCD two-loop corrections of the gluon fusion component of Zh , which constitutes the main source of theoretical uncertainty on the associated production of the Higgs boson with a Z boson. The true power of this method is seen when combined with Padé approximants to bridge it with other expansions to obtain an analytic form for the virtual corrections covering the entire invariant mass spectrum [171].

The use of higher-order calculations in SMEFT opened the potential for probing the Higgs trilinear self-coupling [30–33, 35], and show connections between four-top operators and EWPO [39]. The nexus between the SMEFT four-heavy quark operators and the Higgs self-coupling is explored in chapter 5, via the inclusion of NLO SMEFT effects in single-Higgs rates.

Precision Higgs measurements will not be complete without observing Higgs pair production, the aspired jewel process of the HL-LHC, which carries the most potential for measuring the elusive Higgs self-coupling, consequently revealing the shape of the Higgs potential.

In chapter 7, I have demonstrated the potential of this process in constraining other “difficult” Higgs observable; its interaction with light quarks. Higgs pair production is treated as a multivariate problem and aspects of interpretable machine learning were employed to increase the selection efficiency [43]. Using a BDT-classifier interfaced with Shapley values as an interpretability layer, it was possible to constrain the trilinear coupling along with the up-and down-quark Yukawa coupling enhancements within SMEFT. The interpretability allowed for an optimised classifier and added physics understanding and confidence. The constraints projected for HL-LHC on up-quark Yukawa coupling enhancement obtained from this analysis are the most stringent amongst all other probes [291, 357–359], and even the global analysis [366].

I discussed in chapter 8 the recent flavour anomalies within the SMEFT framework. When these anomalies are confronted with EWPO, a marked tension of up to 6σ is observed between the data from B decays and EWPO, further highlighting the interplay between these anomalies and EWPO [428, 429, 437–439, 444, 447, 448].

This conundrum can be resolved by a global fit involving EW and flavour data. A minimalist SMEFT model, assuming no new flavour spurions are involved, would gener-

ate LUV at the loop level and involves semi-leptonics operators from the top and Higgs sectors, namely and $C_{L/eu}$ and $C_{\phi L/e}$. I have then showcased UV-complete models ascertained from this fit to explain these flavour anomalies based on a top-phillic Z' and leptoquarks.

Appendices

A Details of Zh calculation

A.1 Orthogonal Projectors in $gg \rightarrow ZH$

In this appendix, I present the explicit expressions of the projectors $\mathcal{P}_i^{\mu\nu\rho}$ appearing in eq.(4.2). The projectors are all normalized to unity.

$$\mathcal{P}_1^{\mu\nu\rho} = \frac{m_Z}{\sqrt{2}s'p_T^2} \left[p_1^\nu \epsilon^{\mu\rho p_1 p_2} - p_2^\mu \epsilon^{\nu\rho p_1 p_2} + q_t^\mu \epsilon^{\nu\rho p_2 p_3} \right. \quad (\text{A.1})$$

$$\left. + q_u^\nu \epsilon^{\mu\rho p_1 p_3} + s' \epsilon^{\mu\nu\rho p_2} - s' \epsilon^{\mu\nu\rho p_1} \right], \quad (\text{A.2})$$

$$\mathcal{P}_2^{\mu\nu\rho} = \frac{1}{\sqrt{2}s'p_T} \left[q_u^\nu \epsilon^{\mu\rho p_1 p_3} + q_t^\mu \epsilon^{\nu\rho p_2 p_3} \right], \quad (\text{A.3})$$

$$\begin{aligned} \mathcal{P}_3^{\mu\nu\rho} = & \frac{\sqrt{3}}{2s'p_T} \left[s' \epsilon^{\mu\nu\rho p_1} + s' \epsilon^{\mu\nu\rho p_2} - p_1^\nu \epsilon^{\mu\rho p_1 p_2} - p_2^\mu \epsilon^{\nu\rho p_1 p_2} \right. \\ & + (q_u^\nu \epsilon^{\mu\rho p_1 p_3} - q_t^\mu \epsilon^{\nu\rho p_2 p_3}) \left(\frac{1}{3} + \frac{m_Z^2}{p_T^2} \right) \\ & \left. + \frac{m_Z^2}{p_T^2} (q_t^\mu \epsilon^{\nu\rho p_2 p_1} - q_u^\nu \epsilon^{\mu\rho p_1 p_2}) \right], \end{aligned} \quad (\text{A.4})$$

$$\mathcal{P}_4^{\mu\nu\rho} = \frac{m_Z}{\sqrt{2}s'p_T^2} \left[q_t^\mu (\epsilon^{\nu\rho p_2 p_1} - \epsilon^{\nu\rho p_2 p_3}) - q_u^\nu (\epsilon^{\mu\rho p_1 p_2} - \epsilon^{\mu\rho p_1 p_3}) \right], \quad (\text{A.5})$$

$$\mathcal{P}_5^{\mu\nu\rho} = \frac{1}{\sqrt{6}s'p_T} \left[q_t^\mu \epsilon^{\nu\rho p_2 p_3} - q_u^\nu \epsilon^{\mu\rho p_1 p_3} \right], \quad (\text{A.6})$$

$$\begin{aligned} \mathcal{P}_6^{\mu\nu\rho} = & \frac{1}{s'p_T} \left[g^{\mu\nu} \epsilon^{\rho p_1 p_2 p_3} + s' \epsilon^{\mu\nu\rho p_3} + p_1^\nu \epsilon^{\mu\rho p_2 p_3} - p_2^\mu \epsilon^{\nu\rho p_1 p_3} - \frac{s'}{2} \epsilon^{\mu\nu\rho p_2} \right. \\ & + \frac{1}{2} (p_1^\nu \epsilon^{\mu\rho p_1 p_2} + p_2^\mu \epsilon^{\nu\rho p_1 p_2} + q_u^\nu \epsilon^{\mu\rho p_1 p_3} - q_t^\mu \epsilon^{\nu\rho p_2 p_3} - s' \epsilon^{\mu\nu\rho p_1}) \\ & \left. + \frac{m_Z^2}{2p_T^2} (q_t^\mu \epsilon^{\nu\rho p_2 p_1} - q_u^\nu \epsilon^{\mu\rho p_1 p_2} + q_u^\nu \epsilon^{\mu\rho p_1 p_3} - q_t^\mu \epsilon^{\nu\rho p_2 p_3}) \right], \end{aligned} \quad (\text{A.7})$$

where $q_t^\mu = (p_3^\mu - \frac{t'}{s'} p_2^\mu)$ and $q_u^\nu = (p_3^\nu - \frac{u'}{s'} p_1^\nu)$ are defined and the shorthand notation $\epsilon^{\mu\nu\rho p_2} \equiv \epsilon^{\mu\nu\rho\sigma} p_2^\sigma$ is used.

Using these projectors, it is possible to derive the relations between the form-factors

\mathcal{A}_i defined in eq.(4.2) and those defined in section 2 of ref.[143]:

$$\mathcal{A}_1 = \frac{p_T^2}{2\sqrt{2}m_Z(p_T^2 + m_Z^2)} \left[(t' + u')F_{12}^+ - (t' - u')F_{12}^- \right], \quad (\text{A.8})$$

$$\begin{aligned} \mathcal{A}_2 &= -\frac{p_T}{2\sqrt{2}(p_T^2 + m_Z^2)} \left[(t' + u')F_{12}^+ - (t' - u')F_{12}^- \right. \\ &\quad \left. - \frac{p_T^2 + m_Z^2}{2s'} ((t' + u')F_3^+ - (t' - u')F_3^-) \right], \end{aligned} \quad (\text{A.9})$$

$$\begin{aligned} \mathcal{A}_3 &= \frac{p_T}{2\sqrt{3}(p_T^2 + m_Z^2)} \left[(t' + u')F_{12}^- - (t' - u')F_{12}^+ \right. \\ &\quad \left. + (p_T^2 + m_Z^2)(F_2^- + F_4) \right], \end{aligned} \quad (\text{A.10})$$

$$\begin{aligned} \mathcal{A}_4 &= -\frac{m_Z}{2\sqrt{2}(p_T^2 + m_Z^2)} \left[(t' + u')F_{12}^- - (t' - u')F_{12}^+ \right. \\ &\quad \left. + (p_T^2 + m_Z^2) \left((1 - \frac{p_T^2}{m_Z^2})F_2^- + 2F_4 \right) \right], \end{aligned} \quad (\text{A.11})$$

$$\begin{aligned} \mathcal{A}_5 &= \frac{p_T}{2\sqrt{6}(p_T^2 + m_Z^2)} \left[(t' + u')F_{12}^- - (t' - u')F_{12}^+ \right. \\ &\quad \left. + (p_T^2 + m_Z^2) \left(4(F_2^- + F_4) + \frac{3}{2s'} \left((t' + u')F_3^- - (t' - u')F_3^+ \right) \right) \right], \end{aligned} \quad (\text{A.12})$$

$$\mathcal{A}_6 = \frac{p_T}{2} F_4. \quad (\text{A.13})$$

A.2 One-loop form-factors

The p_T -expanded one-loop form-factors up to $\mathcal{O}(p_T^2)$ are given by

$$\mathcal{A}_2^{(0,\Delta)} = -\frac{p_T}{\sqrt{2}(m_z^2 + p_T^2)}(\hat{s} - \Delta_m)m_t^2 C_0^+, \quad (\text{A.14})$$

$$\begin{aligned} \mathcal{A}_2^{(0,\square)} &= \frac{p_T}{\sqrt{2}(m_z^2 + p_T^2)} \left\{ \right. \\ &\quad \left(m_t^2 - m_z^2 \frac{\hat{s} - 6m_t^2}{4\hat{s}} - p_T^2 \frac{12m_t^4 - 16m_t^2\hat{s} + \hat{s}^2}{12\hat{s}^2} \right) B_0^+ \\ &\quad - \left(m_t^2 - \Delta_m \frac{m_t^2}{(4m_t^2 + \hat{s})} + m_z^2 \frac{24m_t^4 - 6m_t^2\hat{s} - \hat{s}^2}{4\hat{s}(4m_t^2 + \hat{s})} - \right. \\ &\quad \left. p_T^2 \frac{48m_t^6 - 68m_t^4\hat{s} - 4m_t^2\hat{s}^2 + \hat{s}^3}{12\hat{s}^2(4m_t^2 + \hat{s})} \right) B_0^- \\ &\quad + \left(2m_t^2 - \Delta_m + m_z^2 \frac{3m_t^2 - \hat{s}}{\hat{s}} + p_T^2 \frac{3m_t^2\hat{s} - 2m_t^4}{\hat{s}^2} \right) m_t^2 C_0^- \\ &\quad + \left(\hat{s} - 2m_t^2 + m_z^2 \frac{\hat{s} - 3m_t^2}{\hat{s}} + p_T^2 \frac{2m_t^4 - 3m_t^2\hat{s} + \hat{s}^2}{\hat{s}^2} \right) m_t^2 C_0^+ \\ &\quad + \log \left(\frac{m_t^2}{\mu^2} \right) \frac{m_t^2}{(4m_t^2 + \hat{s})} \left(\Delta_m + 2m_z^2 + p_T^2 \frac{2\hat{s} - 2m_t^2}{3\hat{s}} \right) \\ &\quad \left. - \Delta_m \frac{2m_t^2}{(4m_t^2 + \hat{s})} + m_z^2 \frac{\hat{s} - 12m_t^2}{4(4m_t^2 + \hat{s})} + p_T^2 \frac{8m_t^4 - 2m_t^2\hat{s} + \hat{s}^2}{4\hat{s}(4m_t^2 + \hat{s})} \right\}, \end{aligned} \quad (\text{A.15})$$

and

$$\mathcal{A}_6^{(0,\Delta)} = 0, \quad (\text{A.16})$$

$$\begin{aligned} \mathcal{A}_6^{(0,\square)} &= \frac{\hat{t} - \hat{u}}{\hat{s}^2} p_T \left[\frac{m_t^2}{2} (B_0^- - B_0^+) - \frac{\hat{s}}{4} \right. \\ &\quad \left. - \frac{2m_t^2 + \hat{s}}{2} m_t^2 C_0^- + \frac{2m_t^2 - \hat{s}}{2} m_t^2 C_0^+ \right]. \end{aligned} \quad (\text{A.17})$$

The NLO amplitude can be written in terms of three contributions, namely the two-loop 1PI triangle, the two-loop 1PI box and the reducible double-triangle diagrams,

$$\mathcal{A}_i^{(1)} = \mathcal{A}_i^{(1,\Delta)} + \mathcal{A}_i^{(1,\square)} + \mathcal{A}_i^{(1,\bowtie)}. \quad (\text{A.18})$$

A.3 Two-loop Results

The exact analytic results for the triangle and double triangle topologies are presented. The two-loop triangle results are:

$$\mathcal{A}_1^{(1,\Delta)} = \frac{p_T^2 (\hat{s} - \Delta_m)}{4\sqrt{2}m_Z} \frac{\mathcal{K}_t^{(2l)}}{(p_T^2 + m_Z^2)}, \quad (\text{A.19})$$

$$\mathcal{A}_2^{(1,\Delta)} = -\frac{p_T (\hat{s} - \Delta_m)}{4\sqrt{2}} \frac{\mathcal{K}_t^{(2l)}}{(p_T^2 + m_Z^2)}, \quad (\text{A.20})$$

$$\mathcal{A}_3^{(1,\Delta)} = \frac{p_T (\hat{t} - \hat{u})}{4\sqrt{3}} \frac{\mathcal{K}_t^{(2l)}}{(p_T^2 + m_Z^2)}, \quad (\text{A.21})$$

$$\mathcal{A}_4^{(1,\Delta)} = -\frac{m_Z (\hat{t} - \hat{u})}{4\sqrt{2}} \frac{\mathcal{K}_t^{(2l)}}{(p_T^2 + m_Z^2)}, \quad (\text{A.22})$$

$$\mathcal{A}_5^{(1,\Delta)} = -\frac{p_T (\hat{t} - \hat{u})}{4\sqrt{6}} \frac{\mathcal{K}_t^{(2l)}}{(p_T^2 + m_Z^2)}, \quad (\text{A.23})$$

$$\mathcal{A}_6^{(1,\Delta)} = 0, \quad (\text{A.24})$$

where the $\mathcal{K}_t^{(2l)}$ function is defined in eq.(4.11) of ref.[176], while the double-triangle form-factors are found to be

$$\mathcal{A}_1^{(1,\bowtie)} = -\frac{m_t^2 p_T^2}{4\sqrt{2} m_Z (m_Z^2 + p_T^2)^2} \left[F_t(\hat{t}) \left(G_t(\hat{t}, \hat{u}) - G_b(\hat{t}, \hat{u}) \right) + (\hat{t} \leftrightarrow \hat{u}) \right], \quad (\text{A.25})$$

$$\mathcal{A}_2^{(1,\bowtie)} = \frac{m_t^2 p_T}{4\sqrt{2} (m_Z^2 + p_T^2)^2} \left[F_t(\hat{t}) \left(G_t(\hat{t}, \hat{u}) - G_b(\hat{t}, \hat{u}) \right) + (\hat{t} \leftrightarrow \hat{u}) \right], \quad (\text{A.26})$$

$$\mathcal{A}_3^{(1,\bowtie)} = \frac{m_t^2 p_T}{4\sqrt{3} \hat{s} (m_Z^2 + p_T^2)^2} \left[\left(m_h^2 - \hat{t} \right) F_t(\hat{t}) \left(G_t(\hat{t}, \hat{u}) - G_b(\hat{t}, \hat{u}) \right) - (\hat{t} \leftrightarrow \hat{u}) \right], \quad (\text{A.27})$$

$$\begin{aligned} \mathcal{A}_4^{(1,\bowtie)} = & -\frac{m_t^2}{4\sqrt{2} m_Z \hat{s}^2 (m_Z^2 + p_T^2)^2} \left[\left(m_Z^2 \left(m_h^2 - \hat{t} \right)^2 \right. \right. \\ & \left. \left. - \hat{t} \left(m_Z^2 - \hat{u} \right)^2 \right) F_t(\hat{t}) \left(G_t(\hat{t}, \hat{u}) - G_b(\hat{t}, \hat{u}) \right) - (\hat{t} \leftrightarrow \hat{u}) \right], \end{aligned} \quad (\text{A.28})$$

$$\begin{aligned} \mathcal{A}_5^{(1,\bowtie)} = & -\frac{m_t^2 p_T}{4\sqrt{6} \hat{s} (m_Z^2 + p_T^2)^2} \left[\left(4m_Z^2 - \hat{s} - 4\hat{u} \right) F_t(\hat{t}) \left(G_t(\hat{t}, \hat{u}) - G_b(\hat{t}, \hat{u}) \right) \right. \\ & \left. - (\hat{t} \leftrightarrow \hat{u}) \right], \end{aligned} \quad (\text{A.29})$$

$$\mathcal{A}_6^{(1,\bowtie)} = 0, \quad (\text{A.30})$$

where

$$\begin{aligned}
 F_t(\hat{t}) &= \frac{1}{(m_h^2 - \hat{t})^2} \left[2\hat{t} \left(B_0(\hat{t}, m_t^2, m_t^2) - B_0(m_h^2, m_t^2, m_t^2) \right) \right. \\
 &\quad \left. + (m_h^2 - \hat{t}) \left((m_h^2 - 4m_t^2 - \hat{t}) C_0(0, m_h^2, \hat{t}, m_t^2, m_t^2, m_t^2) - 2 \right) \right], \tag{A.31}
 \end{aligned}$$

$$\begin{aligned}
 G_x(\hat{t}, \hat{u}) &= (m_z^2 - \hat{u}) \left[m_z^2 \left(B_0(\hat{t}, m_x^2, m_x^2) - B_0(m_z^2, m_x^2, m_x^2) \right) \right. \\
 &\quad \left. + (\hat{t} - m_z^2) \left(2m_x^2 C_0(0, \hat{t}, m_z^2, m_x^2, m_x^2, m_x^2) + 1 \right) \right]. \tag{A.32}
 \end{aligned}$$

B Two-parameter fits of four-fermion operators and C_ϕ for HL-LHC

I present here in Figure B.1 and Figure B.2, the fit results for the SMEFT four heavy quark operators with the Higgs trilinear self-coupling modifier C_ϕ for the HL-LHC projections by CMS [216, 222] as an extension of the results presented in chapter 5.

The expected constraints improve from the Run-II ones by a factor of

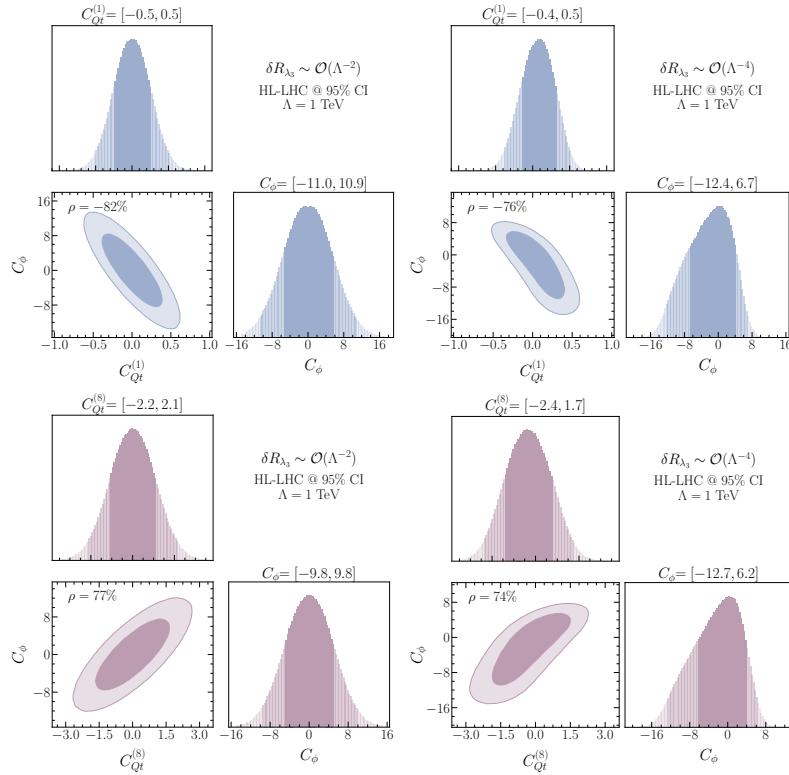


Figure B.1. The posterior distributions of the HL-LHC projections fits for C_ϕ with $C_{Qt}^{(1)}$ (up) and C_ϕ with $C_{Qt}^{(8)}$ (down). With 68% and 95% highest density posterior contours are indicated. The limits shown on top of the plots indicate the 95% CI's. Plots on the left are made for the fully linearised δR_{λ_3} , while the ones on the right include the quadratic effects.

$$\sim \sqrt{\frac{\mathcal{L}_{\text{HL-LHC}}}{\mathcal{L}_{\text{Run-II}}}}, \quad (\text{B.1})$$

as expected, from statistical analysis. This comes from the adaptation of the S_2 uncertainties scheme [133].

The linear fits show similar correlation patterns to the ones from the Run-II in [Figure 5.5](#) and [Figure 5.6](#). However, the quadratic R_{λ_3} scheme shows strong correlation between C_ϕ and the four-heavy quark Wilson coefficients, while this is not seen in the Run-II fits.

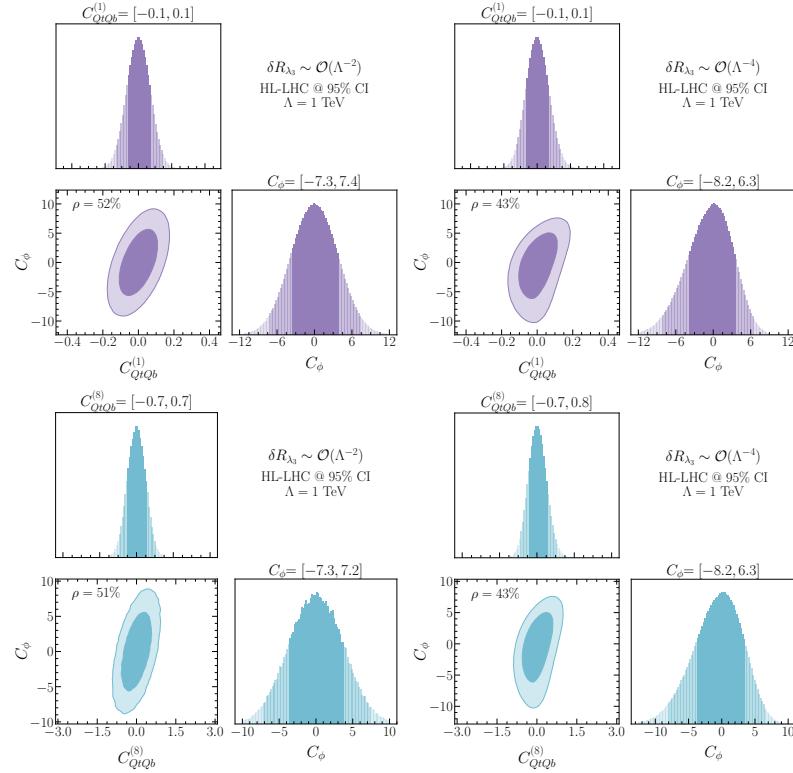


Figure B.2. The posterior distributions of the HL-LHC projections fits for C_ϕ with $C_{QtQb}^{(1)}$ (up) and C_ϕ with $C_{QtQb}^{(8)}$ (down), with the same annotations as in [Figure B.1](#).

C Prospects for Higgs pair production at the FCC

The analysis done in section 7.5 for Higgs pair at the HL-LHC can be repeated for the future hadron circular collider (FCC-hh), with centre-of-mass energy of 100 TeV and integrated luminosity of 30 ab^{-1} . The Higgs pair events and the backgrounds were generated in the same manner for the FCC-hh as for the HL-LHC. Moreover, the ML analysis and the consequent statistical framework were also identical to the ones done for the HL-LHC, with the caveat of using the 14 TeV K -factors for the 100 TeV cross-section scaling, as the 100 TeV K -factors were not available for all processes. We have explicitly checked that at least within the SM, for Higgs pair production via gluon fusion the difference is of $\mathcal{O}(1\%)$ [117] and hence small. An example output of the BDT-classifier for the FCC-hh is shown for the SM signal as a confusion matrix in Table C.1.

Performing a single-parameter fit on the light Yukawa modifiers, we see the projected bounds on these operators at FCC-hh are given by

$$\begin{aligned} C_{u\phi}^{MV}(\kappa_u^{MV}) &= [-0.012, 0.011] \quad([-57.8, 54.7]), \\ C_{d\phi}^{MV}(\kappa_d^{MV}) &= [-0.012, 0.012] \quad([-26.3, 28.4]). \end{aligned} \quad (\text{C.1})$$

These projected bounds for FCC-hh are an order of magnitude better than those for HL-LHC. In addition, the bounds on $C_{u\phi}$ and $C_{d\phi}$ are numerically the same displaying a much greater improvement in the bounds on $C_{d\phi}$ than on $C_{u\phi}$ at the higher energy collider. The results of the FCC-hh analysis are summarised in Table C.2

From this table, we observe that the constraints on the trilinear self-coupling reach the precision-level of $\sim 4\%$ at 68% CI. As for light Yukawa couplings, the up-type will reach $\mathcal{O}(50)$ times the SM value showing significant improvement over the HL-LHC,

Predicted no. of events at FCC-hh							
Actual no. of events	Channel	$hh_{\text{tri}}^{\text{ggF}}$	$hh_{\text{tri}}^{\text{ggF}}$	$hh_{\text{box}}^{\text{ggF}}$	$Q\bar{Q}h$	$b\bar{b}\gamma\gamma$	total
	$hh_{\text{tri}}^{\text{ggF}}$	3,579	1,303	2,372	4,697	337	12,288
	$hh_{\text{int}}^{\text{ggF}}$	13,602	7,300	17,075	24,716	1523	64,216
	$hh_{\text{box}}^{\text{ggF}}$	14,534	11,416	35,988	415,26	1,996	105,460
	$Q\bar{Q}h$	29,611	12,355	23,279	1,238,266	214,564	1,518,075
	$b\bar{b}\gamma\gamma$	45,574	22,290	26,213	150,935	227,142	24,317,657
	Z_j	10.95	31.22	111.1	737.7	4,743	

Table C.1. The confusion matrix output of the trained BDT five-channel classifier for the FCC-hh analysis. This table is analogous to for the HL-LHC Table 7.5

Operators	$C_{u\phi}$	$C_{d\phi}$	C_ϕ		κ_u	κ_d	κ_λ
\mathcal{O}_ϕ	—	—	[-0.066, 0.064]		—	—	[0.97, 1.03]
$\mathcal{O}_{u\phi}$	[-0.012, 0.011]	—	—		[-57.8, 54.7]	—	—
$\mathcal{O}_{d\phi}$	—	[-0.012, 0.011]	—		—	[-26.3, 28.4]	—
$\mathcal{O}_{u\phi} \& \mathcal{O}_\phi$	[-0.010, 0.011]	—	[-0.091, 0.042]		[-52, 49]	—	[0.98, 1.04]
$\mathcal{O}_{d\phi} \& \mathcal{O}_\phi$	—	[-0.010, 0.012]	[-0.092, 0.041]		—	[-24, 26]	[0.98, 1.04]
$\mathcal{O}_{u\phi} \& \mathcal{O}_{d\phi}$	[-0.008, 0.009]	[-0.008, 0.009]	—		[-42, 39]	[-19, 19]	—
All	[-0.009, 0.010]	[-0.009, 0.010]	[-0.105, 0.023]		[-47, 44]	[-21, 21]	[0.99, 1.05]

Table C.2. The 1σ bounds on $C_{u\phi}$, $C_{d\phi}$ and C_ϕ from one-, two- and three-parameter fits for FCC-hh with 30 ab^{-1} integrated luminosity.

and $\mathcal{O}(20 - 30)$ for the down Yukawa couplings. The posterior distributions for the two-parameter fits are shown in Figure C.1, while the three-parameter analysis in Figure C.2. These plots show more significant correlation patterns between C_ϕ and $C_{u\phi}$ or $C_{d\phi}$ compared to the HL-LHC fits in Figure 7.14 and Figure 7.15.s

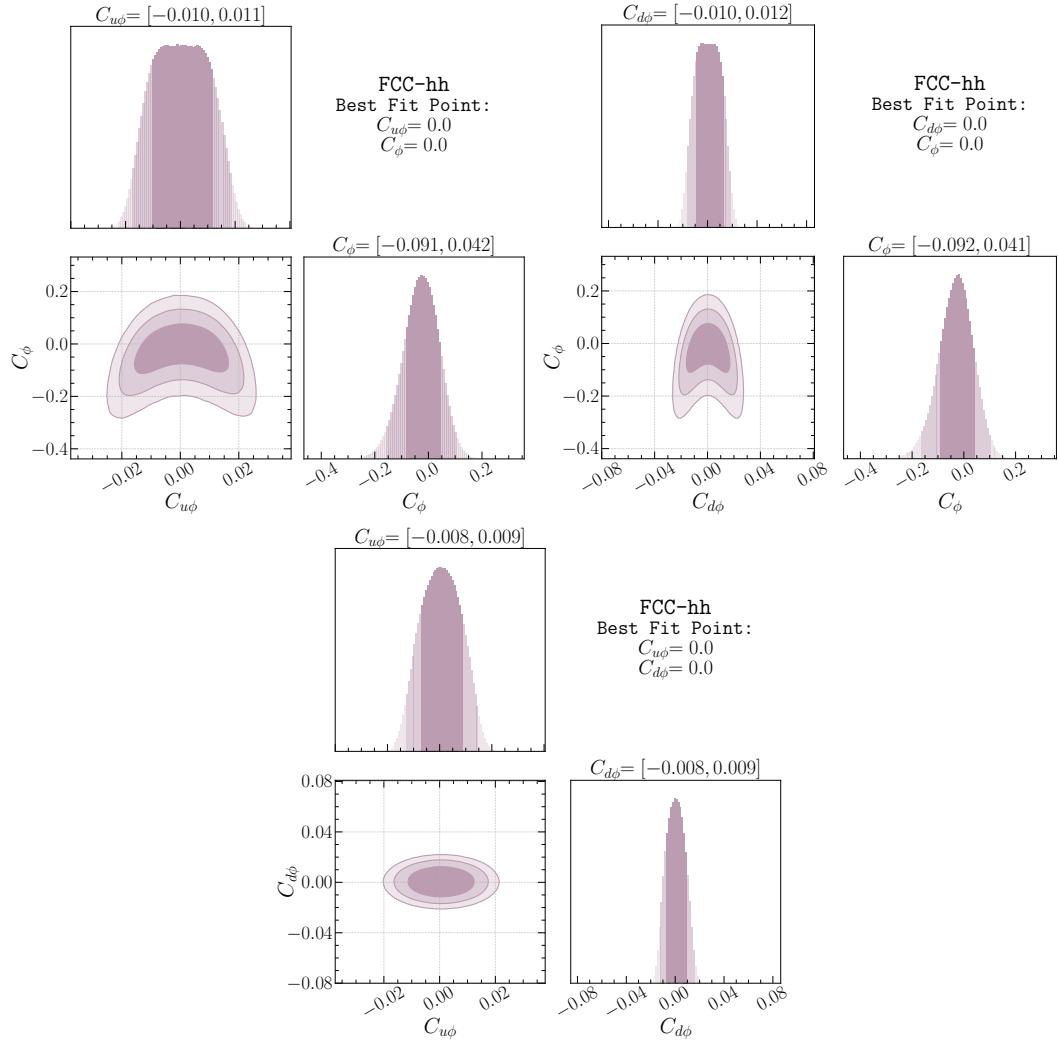


Figure C.1. Constraints on pairs of Wilson coefficients for C_ϕ , $C_{u\phi}$ and $C_{d\phi}$ for FCC-hh with 30 ab^{-1} integrated luminosity.

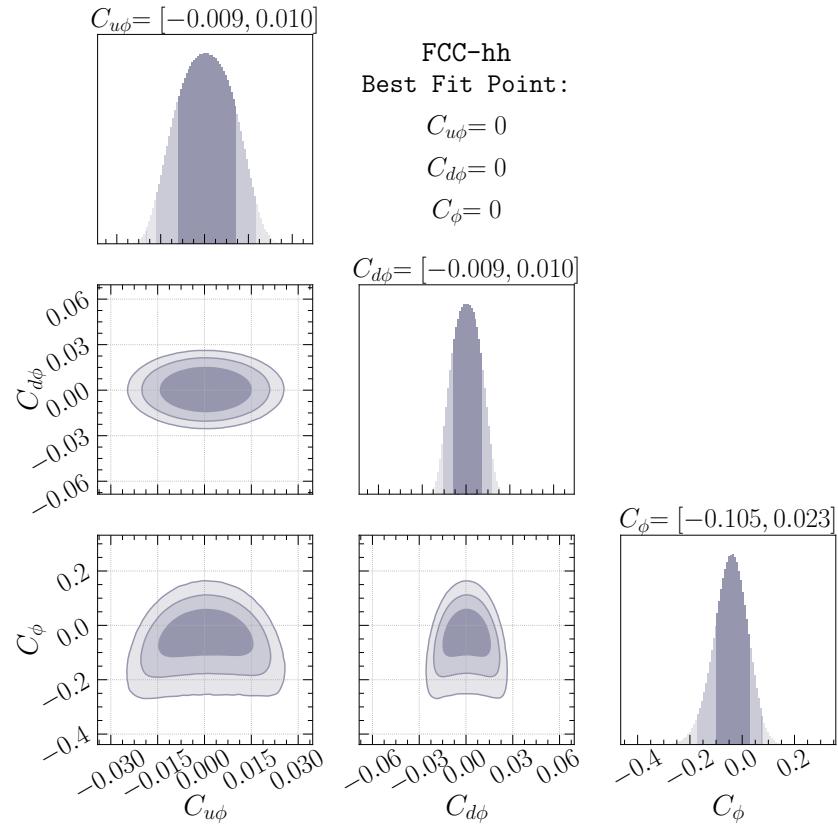


Figure C.2. Three parameter fits with $C_{u\phi}$, $C_{d\phi}$ and C_ϕ , for FCC-hh with 30 ab^{-1} integrated luminosity.

D Alternative simplified models for the flavour anomalies

Working under the PDD ansatz, it is possible to consider that the model would couple to the electron instead of the muon. Not much would change in terms of the particle content of this model, except for opposite charge assignment to get correct signs for the Wilson coefficients of \mathcal{O}^{Lu} and $\mathcal{O}_{\phi L}^{(1)}$ seen in the right panel off Figure 8.6. The electron and top partners need opposite X charges in this case. A final comment is needed for the electron scenario reported in Figure D.1, that involves opposite signs for the Wilson coefficients of \mathcal{O}^{Lu} and $\mathcal{O}_{\phi L}^{(1)}$ discussed so far. For the former, it should be noted that the sign highlighted in the matching in eq. (8.19) follows from having assumed the same sign for the charge of the vector-like top and muon partners under $U(1)_X$. For what concerns the generation of $C_{\phi L}^{(1) \ 11} < 0$, according to eq. (8.21) one needs to correlate once again the contribution stemming from S_0 , or from S_1 , with the effect coming from a $SU(2)_L$ triplet, that now needs to be identified with T_1 , namely the triplet of hypercharge $Y = 1$. Eventually, we wish also to comment on the possible role

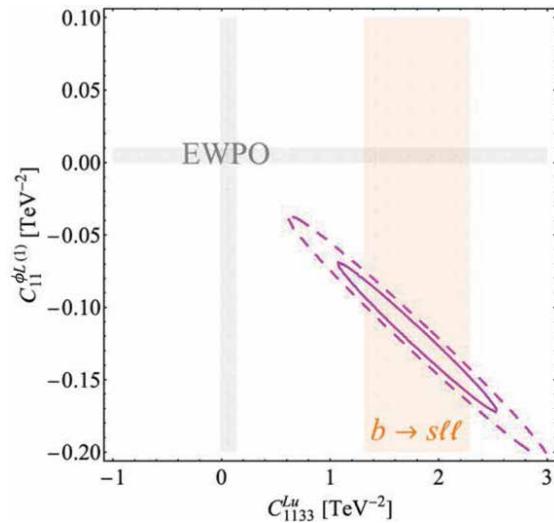


Figure D.1. A minimal solution for the flavour anomalies within SMEFT while respecting EWPO for the four-fermion operators involving the electron. EWPO fits are the grey regions, while the $b \rightarrow s l \ell$ measurements fits with PDD ansatz are highlighted by the orange bands. The combined fit's 1 and 2σ contours are magenta coloured. This plot has been published in [453].

of the \mathcal{O}_{eu} operator, so far neglected in this discussion, but of potential relevance more

in general. As mentioned earlier, the presence of \mathcal{O}_{eu} would be particularly needed in the case where hadronic corrections entering in the amplitude of $B \rightarrow K^* \ell \ell$ would be of the size originally estimated in [391]. In that case, a solution to flavour anomalies would be preferred in the muonic channel with NP Wilson coefficient C_{eu}^{2233} also substantially deviating from 0. Then, one would need to involve also the operator $C_{\phi e}^{22}$ to relieve possible tensions with EW precision. In a general picture, the required NP effects from $\mathcal{O}_{\phi e}^{11,22}$ can be obtained by integrating out heavy vector-like $SU(2)_L$ leptonic doublets.

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