

A.I

Assignment - 1

Task 2:-

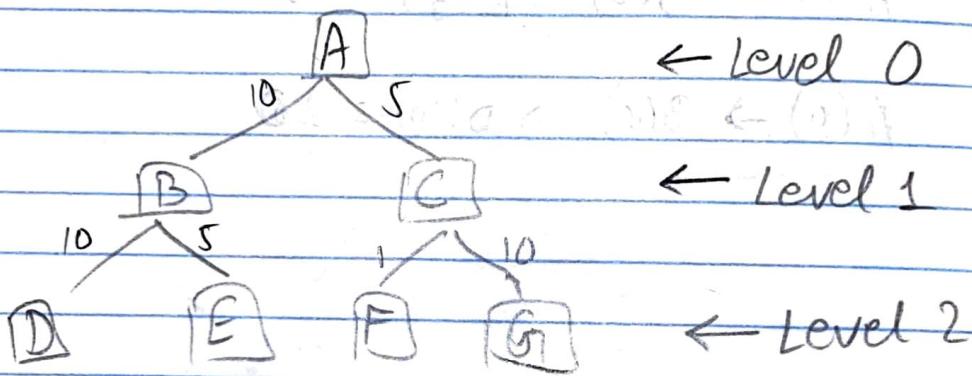
1. Breadth-first search

A, B, C, D, E, F, G.

2. Depth first search

A, B, D, E, C, F, G.

3. Iterative deepening search.



Step 1:- At level 0 :- A

Step 2:- At level 1 :- A, B, C

Step 3:- At level 2 :- A, B, D, E, C, F, G.

4. Uniform Cost Search:-

$$A(0) \rightarrow C(5) \rightarrow F(1) = 6$$

$$A(0) \rightarrow C(5) \rightarrow F(1) \rightarrow G(10) = 16$$

$$A(0) \rightarrow C(5) \rightarrow G(10) = 15 \quad \checkmark$$

$$A(0) \rightarrow B(10) \rightarrow D(10) \rightarrow E(5) = 25$$

$$A(0) \rightarrow B(10) \rightarrow E(5) = 15$$

$$A(0) \rightarrow B(10) \rightarrow D(10) = 20$$

A -> G (25) & A -> E (15)

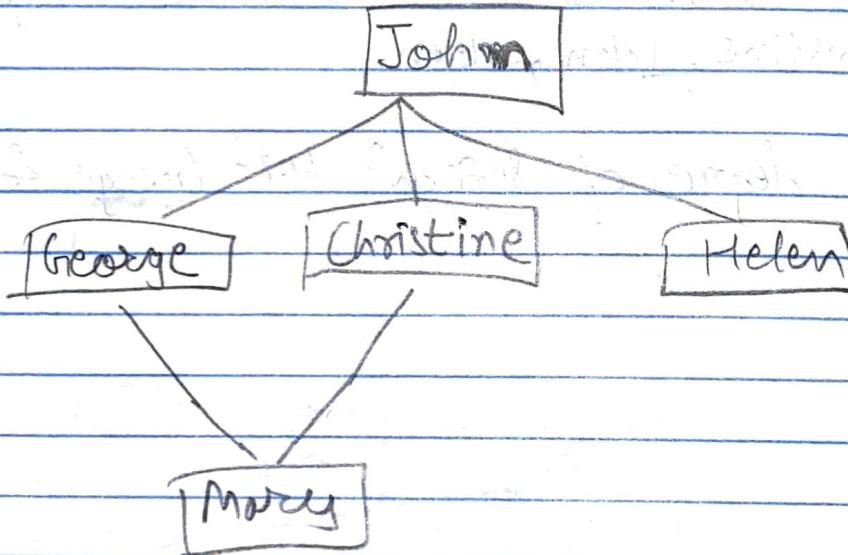
Each of it has in cost

Task 3 :-

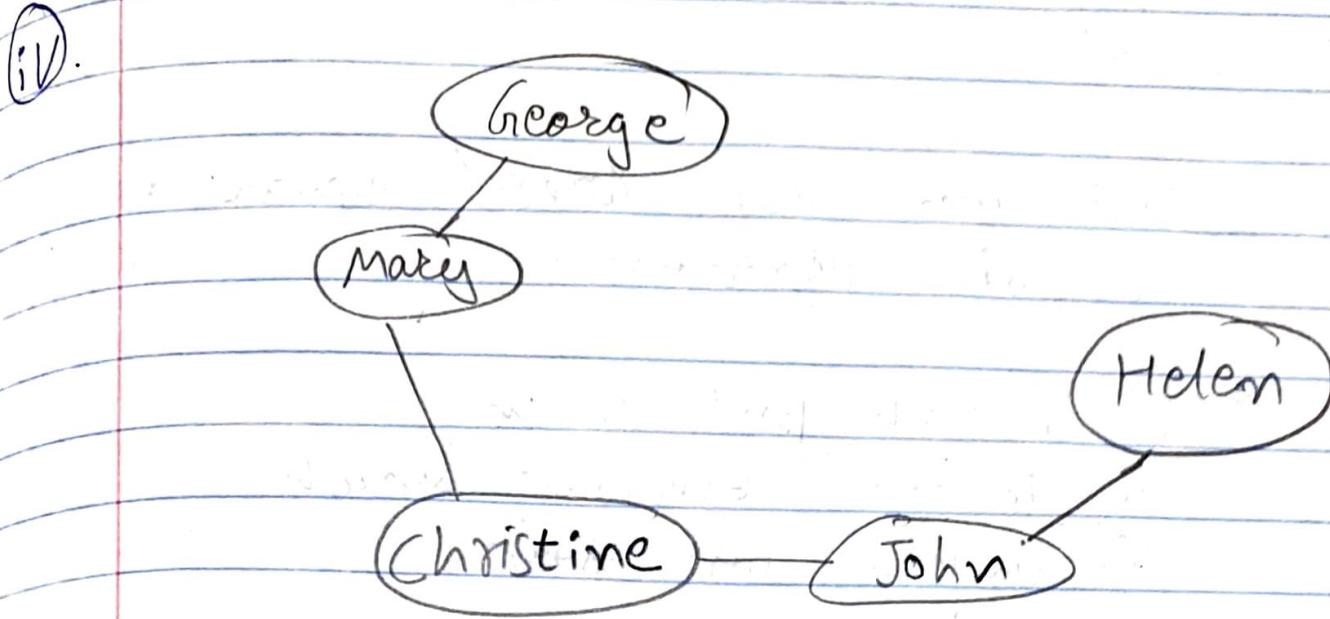
i). We can get correct number of following algorithms :-

- ④ i) Breadth first search
- ii) Iterative deepening search
- iii) Uniform Cost search

iii)

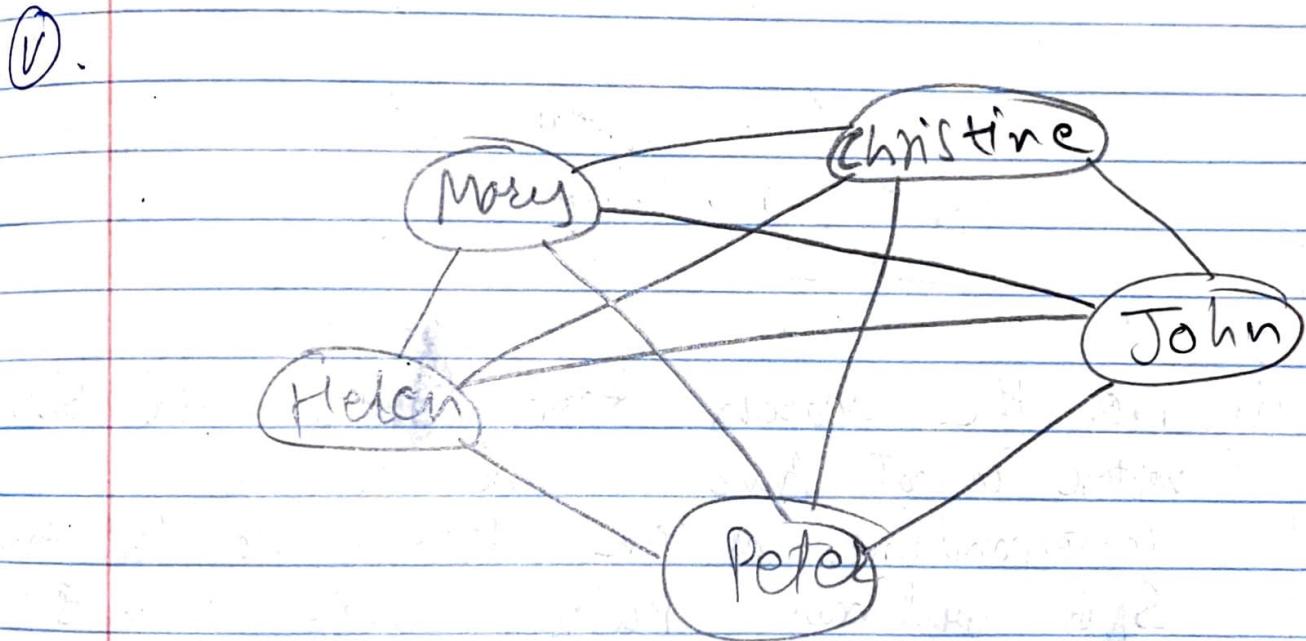


iii) No, the search tree nodes and SNG vertices cannot have a one to one correspondence as the tree generated from SNG will have nodes whose parents & children might repeat due to given condition that the algorithm does not try to avoid revisiting nodes. Also, there are nodes that have common connection. (I.E., If we draw tree, from perspective of George as root, Christine would be twice in the tree, once under Mary & again under John.)



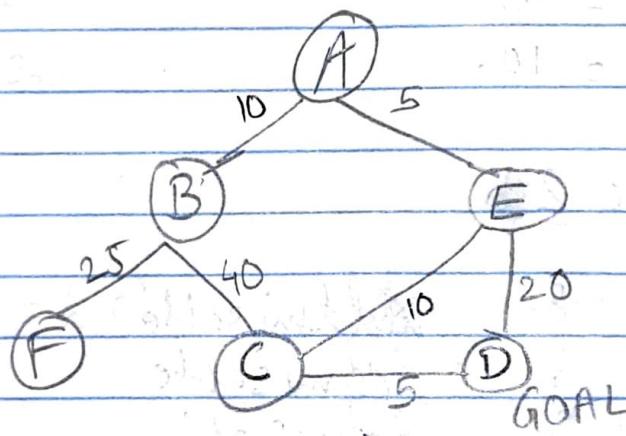
The above SNR has 5 people : George, Mary, Christine, John, Helen.

The degree of separaⁿ betⁿ George & Helen is 4.



⑥ As we know, 1 node is 1 KB & 1 million KB is 1 GB. We can modify BFS to avoid ~~re-visiting~~ re-visiting nodes as to reduce generation of duplicate nodes. This ensures that even in the worst case scenario we might explore all nodes but without creating duplicates and also wouldn't exceed the memory capacity.

Task 4:



$h^*(n)$ for $A \rightarrow 20$, $A \rightarrow E \rightarrow C \rightarrow D$

$h^*(n)$ for $B \rightarrow 30$, $B \rightarrow A \rightarrow E \rightarrow C \rightarrow D$

$h^*(n)$ for $C \rightarrow 5$, $C \rightarrow D$

$h^*(n)$ for $D \rightarrow 0$, $D \rightarrow D$

$h^*(n)$ for $E \rightarrow 15$, $E \rightarrow C \rightarrow D$

$h^*(n)$ for $F \rightarrow 55$, $F \rightarrow B \rightarrow A \rightarrow E \rightarrow C \rightarrow D$

Heuristic 1 : If $h(n) \leq h^*(n)$, admissible.

$h(A) = 5$ Admissible. 20.

$h(B) = 40$ not Admissible 30

$h(C) = 10$ not Admissible 5.

$h(D) = 0$ Admissible

$h(E) = 10$ Admissible

$h(F) = 0$ Admissible

$\therefore h(B) \& h(C) = \text{not Admissible}$ So we can
replace their values.

$$\therefore h^*(B) = 40$$

$$h^*(C) = 10.$$

Heuristic 2 :-

$h(A) = 8$ Admissible

$h(B) = 5$ Admissible

$h(C) = 3$ Admissible

$h(D) = 5$ not Admissible

$h(E) = 5$ Admissible

$h(F) = 0$ Admissible

~~$h(D)$~~

Here, $h(D)$ is not Admissible. So we can
replace its value.

$$h^*(D) = 5.$$

Heuristic 3 :-

| | |
|-------------|----------------|
| $h(A) = 35$ | Not Admissible |
| $h(B) = 30$ | Admissible |
| $h(C) = 20$ | Not Admissible |
| $h(D) = 0$ | Admissible |
| $h(E) = 0$ | Admissible |
| $h(F) = 50$ | Admissible |

Here, $h(A)$ & ~~$h(C)$~~ are not admissible.

$$h^*(A) = 35$$

$$h^*(C) = 20$$

Heuristic 4 :-

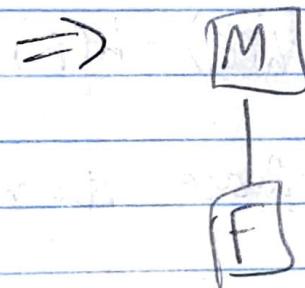
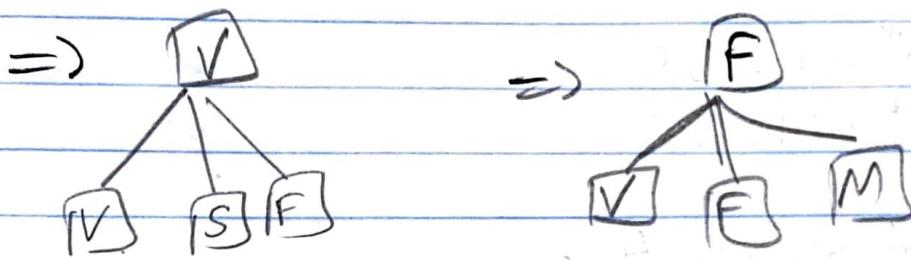
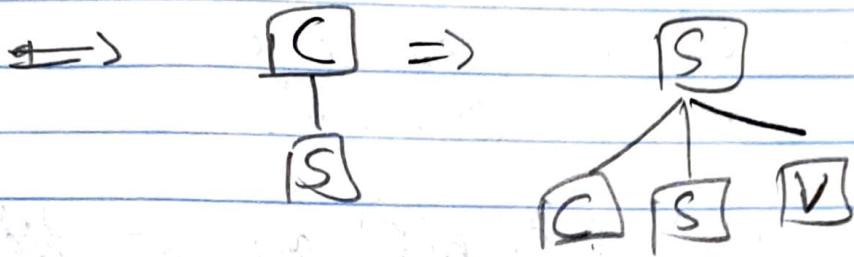
$$h(A) = h(B) = h(C) = h(D) = h(E) = h(F) = 0.$$

\therefore All the heuristics are admissible.

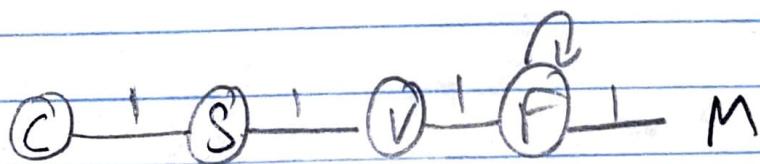
Task 5 :-

→ Given :-

City = C Village = V Mountain = M.
 Suburb = S Farmland = F.



\Rightarrow According to the given statements:-



\Rightarrow Therefore:-

$h(n)$:-

$$h(C) = 4, \quad h(V) = 2, \quad h(M) = 0.$$

$$h(S) = 3, \quad h(F) = 1$$

\therefore Thus $h(M)$ is goal state.

TASK 6 :-

→ Here, the greedy search algorithm is represented as $h(n)$ which is Euclidian distance.

⇒ A* algorithm is represented as $f(n)$.

$$f(n) = g(n) + h(n)$$

where, $h(n)$ is euclidian distance
and $g(n)$ is minimum distance between nodes.

From figure 5, we assume that it starts from $(5,0)$ and ends on $(5,3)$.

- Heuristic values of following items:-

$$h(5,0) = 6.9$$

$$h(4,2) = 6.2$$

$$h(4,0) = 6.8$$

$$h(6,2) = 6.1$$

$$h(6,0) = 6.7$$

$$h(5,3) = 0.$$

$$h(5,1) = 6.6$$

$$h(4,1) = 6.5$$

$$h(6,1) = 6.4$$

$$h(5,2) = 6.3$$

Q
→ Greedy Algorithm:- Start node $(S, 0)$ it has 3 ways from which $(S, 1)$ is shortest value where $(S, 1) = 6.6$.

Now, it has four options & it will select $(S, 2)$ or its shortest $h(S, 2) = 6.3$

Similarly, now it will select the shortest path having the shortest value.

where $A(S, 3) = 0$. which is goal node.

⇒ A* algorithm:- It works similarly to greedy algorithm and also it will follow the same path & result will also be same as greedy algo.

→ Here, we can say that greedy search algo performs better or same as A* algorithm.

→ Solution for fig 6c - ~~start node~~

Considering, start node = $(3, 1)$
End node = $(3, 2)$

$$h(3, 1) = 1$$

$$h(3, 0) = 2$$

$$h(2, 0) = 2 \cdot 23$$

$$h(1, 0) = 2 \cdot 23$$

Considering $(3, 1)$ as start node, in greedy search, the algo will have just one option. (i.e) $h(3, 0)$ with value 2.

In iteration 2, the node $(3,0)$ will have three options namely $n(2,0)$, $h(4,0)$ and $(3,0)$ with values of (2.23) , 2.23 & 1 .

The algorithm will select $h(3,1)$ and go there.

→ A^* algorithm will find $f(n)$ (i.e).

$$f(n) = h(n) + g(n)$$

$$\text{Here, } f(3,1) = 1 + 0 = 1.$$

$$f(3,0) = 2 + 1 = 3.$$

$$f(4,0) = 2 \cdot 23 + 2 = 4 \cdot 23.$$

$$f(4,1) = 1 \cdot 4 + 3 = 4 \cdot 4.$$

$$f(4,2) = 1 + 4 = 5.$$

$$f(3,2) = 0 + 5 = 5.$$

The A^* algorithm will follow the following path $(3,1) \rightarrow (3,0) \rightarrow (4,0) \rightarrow (4,1) \rightarrow (4,2) \rightarrow (3,2)$ as it has the lowest $f(n)$ value.

At $(4,1)$ for Eg. the algo. has 3 options.

$(4,0)$, $(5,1)$ & $(4,2)$ with values 4.23 .

$$(2.23 + 4) = 6.23. \text{ and } 5.$$

Here, it will not go back to $(4,0)$ as it has already visited it. Out of $(5,1)$ and $(4,2)$ it will go to $(4,2)$ as it has the lower $f(n)$ value.

- Greedy search always performs worse than or same as A* depending on start & end state.