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# COMMON FIXED POINT THEOREM IN INTUITIONISTIC FUZZY METRIC SPACES

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ABSTRACT. In this paper, a common fixed point theorem for R-weakly commuting maps in intuitionistic fuzzy metric spaces is proved.

# 1. Introduction and Preliminaries

In this section, using the idea of intuitionistic fuzzy metric spaces introduced by Park [5] we define the new notion of intuitionistic fuzzy metric spaces with the help of the notion of continuous t-representable.

**Definition 1.1.** A complete lattice is a partially ordered set in which every nonempty subset admits supremum and infimum.

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**Lemma 1.2.** ([2]) Consider the set  $L^*$  and operation  $\leq_{L^*}$  defined by:

$$L^* = \{(x_1, x_2) : (x_1, x_2) \in [0, 1]^2 \text{ and } x_1 + x_2 \le 1\},\$$

 $(x_1,x_2) \leq_{L^*} (y_1,y_2) \iff x_1 \leq y_1 \text{ and } x_2 \geq y_2, \text{ for every } (x_1,x_2), (y_1,y_2) \in L^*.$ Then  $(L^*,\leq_{L^*})$  is a complete lattice.

**Definition 1.3.** ([1]) An intuitionistic fuzzy set  $\mathcal{A}_{\zeta,\eta}$  in a universe U is an object  $\mathcal{A}_{\zeta,\eta} = \{(\zeta_{\mathcal{A}}(u),\eta_{\mathcal{A}}(u))|u\in U\}$ , where, for all  $u\in U,\ \zeta_{\mathcal{A}}(u)\in [0,1]$  and  $\eta_{\mathcal{A}}(u)\in [0,1]$  are called the membership degree and the non-membership degree, respectively, of u in  $\mathcal{A}_{\zeta,\eta}$ , and furthermore they satisfy  $\zeta_{\mathcal{A}}(u)+\eta_{\mathcal{A}}(u)\leq 1$ .

We denote its units by  $0_{L^*} = (0,1)$  and  $1_{L^*} = (1,0)$ . Classically, a triangular norm \* = T on [0,1] is defined as an increasing, commutative, associative mapping  $T: [0,1]^2 \longrightarrow [0,1]$  satisfying T(1,x) = 1 \* x = x, for all  $x \in [0,1]$ . A triangular conorm  $S = \diamond$  is defined as an increasing, commutative, associative mapping  $S: [0,1]^2 \longrightarrow [0,1]$  satisfying  $S(0,x) = 0 \diamond x = x$ , for all  $x \in [0,1]$ . Using the lattice  $(L^*, \leq_{L^*})$  these definitions can be straightforwardly extended.

**Definition 1.4.** ([2]) A triangular norm (t-norm) on  $L^*$  is a mapping  $\mathcal{T}:(L^*)^2 \longrightarrow L^*$  satisfying the following conditions:

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(\forall x \in L^*)(\mathcal{T}(x, 1_{L^*}) = x), \quad \text{(boundary condition)}
(\forall (x, y) \in (L^*)^2)(\mathcal{T}(x, y) = \mathcal{T}(y, x)), \quad \text{(commutativity)}
(\forall (x, y, z) \in (L^*)^3)(\mathcal{T}(x, \mathcal{T}(y, z)) = \mathcal{T}(\mathcal{T}(x, y), z)), \quad \text{(associativity)}
(\forall (x, x', y, y') \in (L^*)^4)(x \leq_{L^*} x' \text{ and } y \leq_{L^*} y' \implies \mathcal{T}(x, y) \leq_{L^*} \mathcal{T}(x', y')).
(monotonicity)
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If  $(L^*, \leq_{L^*}, \mathcal{T})$  is an Abelian topological monoid with unit  $1_{L^*}$  then  $\mathcal{T}$  is said to be a *continuous t*-norm.

**Definition 1.5.** ([2]) A continuous t-norm  $\mathcal{T}$  on  $L^*$  is called continuous t-representable if and only if there exist a continuous t-norm \* and a continuous t-conorm  $\diamond$  on [0,1] such that, for all  $x=(x_1,x_2),y=(y_1,y_2)\in L^*$ ,

$$\mathcal{T}(x,y) = (x_1 * y_1, x_2 \diamond y_2).$$

For example  $\mathcal{T}(a,b) = (a_1b_1, \min(a_2+b_2,1))$  for all  $a = (a_1,a_2)$  and  $b = (b_1,b_2)$  in  $L^*$  is a continuous t-representable.

**Definition 1.6.** A negator on  $L^*$  is any decreasing mapping  $\mathcal{N}: L^* \longrightarrow L^*$  satisfying  $\mathcal{N}(0_{L^*}) = 1_{L^*}$  and  $\mathcal{N}(1_{L^*}) = 0_{L^*}$ . If  $\mathcal{N}(\mathcal{N}(x)) = x$ , for all  $x \in L^*$ , then  $\mathcal{N}$  is called an involutive negator. A negator on [0,1] is a decreasing mapping  $N: [0,1] \longrightarrow [0,1]$  satisfying N(0) = 1 and N(1) = 0.  $N_s$  denotes the standard negator on [0,1] defined as, for all  $x \in [0,1]$ ,  $N_s(x) = 1-x$ . We define  $(N_s(\lambda), \lambda) = \mathcal{N}_s(\lambda)$ .

**Definition 1.7.** Let M, N are fuzzy sets from  $X^2 \times (0, +\infty)$  to [0, 1] such that  $M(x, y, t) + N(x, y, t) \leq 1$  for all  $x, y \in X$  and t > 0, in which, M is membership degree and N is non-membership degree of an intuitionistic fuzzy set. The triple  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  is said to be an *intuitionistic fuzzy metric space* if X is an arbitrary (non-empty) set,  $\mathcal{T}$  is a continuous t-representable and  $\mathcal{M}_{M,N}$  is a mapping  $X^2 \times (0, +\infty) \to L^*$  (an intuitionistic fuzzy set, see Definition 2.4) satisfying the following conditions for every  $x, y, z \in X$  and t, s > 0:

- (a)  $\mathcal{M}_{M,N}(x,y,t) >_{L^*} 0_{L^*}$ ;
- (b)  $\mathcal{M}_{M,N}(x,y,t) = 1_{L^*}$  if and only if x = y;

- (c)  $\mathcal{M}_{M,N}(x,y,t) = \mathcal{M}_{M,N}(y,x,t);$
- (d)  $\mathcal{M}_{M,N}(x,y,t+s) \geq_{L^*} \mathcal{T}(\mathcal{M}_{M,N}(x,z,t),\mathcal{M}_{M,N}(z,y,s));$
- (e)  $\mathcal{M}_{M,N}(x,y,\cdot):(0,\infty)\longrightarrow L^*$  is continuous.

In this case  $\mathcal{M}_{M,N}$  is called an intuitionistic fuzzy metric. Here,

$$\mathcal{M}_{M,N}(x,y,t) = (M(x,y,t), N(x,y,t)).$$

Let  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  be an intuitionistic fuzzy metric space. For t > 0, define the open ball B(x, r, t) with center  $x \in X$  and radius 0 < r < 1, as

$$B(x, r, t) = \{ y \in X : \mathcal{M}_{M,N}(x, y, t) >_{L^*} (N_s(r), r) = \mathcal{N}_s(r) \}.$$

A subset  $A \subseteq X$  is called *open* if for each  $x \in A$ , there exist t > 0 and 0 < r < 1 such that  $B(x,r,t) \subseteq A$ . Let  $\tau_{\mathcal{M}_{M,N}}$  denote the family of all open subset of X.  $\tau_{\mathcal{M}_{M,N}}$  is called the *topology induced by intuitionistic fuzzy metric*. A sequence  $\{x_n\}$  in an intuitionistic fuzzy metric space  $(X, \mathcal{M}_{M,N}, T)$  is called a *Cauchy sequence* if for each  $\varepsilon > 0$  and t > 0, there exists  $n_0 \in \mathbf{N}$  such that

$$\mathcal{M}_{M,N}(x_n, x_m, t) >_{L^*} \mathcal{N}_s(\varepsilon),$$

and for each  $n, m \geq n_0$ . The sequence  $\{x_n\}$  is said to be *convergent* to  $x \in V$  in the intuitionistic fuzzy metric space  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  and denoted by  $x_n \stackrel{\mathcal{M}_{M,N}}{\longrightarrow} x$  if  $\mathcal{M}_{M,N}(x_n, x, t) \longrightarrow 1_{L^*}$  whenever  $n \longrightarrow \infty$  for every t > 0. An intuitionistic fuzzy metric space is said to be *complete* if and only if every Cauchy sequence is convergent (see [3, 5]).

**Lemma 1.8.** ([3]) Let  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  be an intuitionistic fuzzy metric space. Then,  $\mathcal{M}_{M,N}(x,y,t)$  is nondecreasing with respect to t, for all x,y in X.

**Example 1.9.** ([7]) Let (X, d) be a metric space. Denote  $\mathcal{T}(a, b) = (a_1b_1, \min(a_2 + b_2, 1))$  for all  $a = (a_1, a_2)$  and  $b = (b_1, b_2)$  in  $L^*$  and let M and N be fuzzy sets on  $X^2 \times (0, \infty)$  defined as follows:

$$\mathcal{M}_{M,N}(x,y,t)=(M(x,y,t),N(x,y,t))=(\frac{t}{t+md(x,y)},\frac{d(x,y)}{t+d(x,y)}),$$

in which m > 1. Then  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  is an intuitionistic fuzzy metric space.

Let  $\mathcal{T}$  be a continuous t-norm on  $L^*$  in which, for every  $\mu \in (0,1)$ , there exists  $\lambda \in (0,1)$  such that

(1.1) 
$$\mathcal{T}^{n-1}(\mathcal{N}_s(\lambda), ..., \mathcal{N}_s(\lambda)) >_{L^*} \mathcal{N}_s(\mu),$$

where  $\mathcal{N}_s$  is an standard negation. For more information see [6].

**Definition 1.10.** Let  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  be an intuitionistic fuzzy metric space.  $\mathcal{M}_{M,N}$  is said to be continuous on  $X \times X \times (0, \infty)$  if

$$\lim_{n \to \infty} \mathcal{M}_{M,N}(x_n, y_n, t_n) = \mathcal{M}_{M,N}(x, y, t)$$

whenever a sequence  $\{(x_n, y_n, t_n)\}$  in  $X \times X \times (0, \infty)$  converges to a point  $(x, y, t) \in X \times X \times (0, \infty)$  i.e.,  $\lim_n \mathcal{M}_{M,N}(x_n, x, t) = \lim_n \mathcal{M}_{M,N}(y_n, y, t) = 1_{L^*}$  and

$$\lim_{n} \mathcal{M}_{M,N}(x,y,t_n) = \mathcal{M}_{M,N}(x,y,t).$$

**Lemma 1.11.** Let  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  be an intuitionistic fuzzy metric space. Then  $\mathcal{M}_{M,N}$  is continuous function on  $X \times X \times (0, \infty)$ .

*Proof.* The proof is same as fuzzy metric spaces (see Proposition 1 of [4]).

#### 2. The Main Results

**Definition 2.1.** Let f and g be maps from an intuitionistic fuzzy metric space  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  into itself. The maps f and g are said to be weakly commuting if

$$\mathcal{M}_{M,N}((fog)(x),(gof)(x),t) \geq_{L^*} \mathcal{M}_{M,N}(f(x),g(x),t)$$

for each x in X and t > 0.

**Definition 2.2.** Let f and g be maps from an intuitionistic fuzzy metric space  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  into itself. The maps f and g are said to be R-weakly commuting if there exists some positive real number R such that

$$\mathcal{M}_{M,N}((fog)(x), (gof)(x), t) \ge_{L^*} \mathcal{M}_{M,N}(f(x), g(x), t/R)$$

for each x in X and t > 0.

Weak commutativity implies R-weak commutativity in intuitionistic fuzzy metric space. However, R-weak commutativity implies weak commutativity only when  $R \leq 1$ .

**Example 2.3.** Let  $X = \mathbf{R}$ . Let  $\mathcal{T}(a,b) = (a_1b_1, \min(a_2 + b_2, 1))$  for all  $a = (a_1, a_2), b = (b_1, b_2) \in L^*$  and let  $\mathcal{M}_{M,N}$  be the intuitionistic fuzzy set on  $X \times X \times [0, +\infty[$  defined as follows:

$$\mathcal{M}_{M,N}(x,y,t) = \left( \left( \exp\left(\frac{|x-y|}{t}\right) \right)^{-1}, \frac{\exp\left(\frac{|x-y|}{t}\right) - 1}{\exp\left(\frac{|x-y|}{t}\right)} \right),$$

for all  $t \in \mathbf{R}^+$ . Then  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  is an intuitionistic fuzzy metric space. Define f(x) = 2x - 1 and  $g(x) = x^2$ . Then,

$$\begin{split} &\mathcal{M}_{M,N}((fog)(x),(gof)(x),t) - \left( (\exp(2\frac{|x-1|^2}{t}))^{-1}, \frac{\exp(2\frac{|x-1|^2}{t})-1}{\exp(2\frac{|x-1|^2}{t})} \right) \\ & \left( (\exp(\frac{|x-1|^2}{t/2}))^{-1}, \frac{\exp(\frac{|x-1|^2}{t/2})-1}{\exp(\frac{|x-1|^2}{t/2})} \right) = \mathcal{M}_{M,N}(f(x),g(x),t/2) \\ &<_{L^*} \left( (\exp(\frac{|x-1|^2}{t}))^{-1}, \frac{\exp(\frac{|x-1|^2}{t/2})-1}{\exp(\frac{|x-1|^2}{t})} \right) = \mathcal{M}_{M,N}(f(x),g(x),t) \end{split}$$

Therefore, for R=2, f and g are R-weakly commuting. But f and g are not weakly commuting since exponential function is strictly increasing.

**Theorem 2.4.** Let  $(X, \mathcal{M}_{M,N}, \mathcal{T})$  be a complete intuitionistic fuzzy metric space and let f and g be R-weakly commuting self-mappings of X satisfying the following conditions:

- (a)  $f(X) \subseteq g(X)$ ;
- (b) f or g is continuous;
- (c)  $\mathcal{M}_{M,N}(f(x), f(y), t) \geq_{L^*} \mathcal{C}(\mathcal{M}_{M,N}(g(x), g(y), t))$ , where  $\mathcal{C}: L^* \longrightarrow L^*$  is a continuous function such that  $\mathcal{C}(a) >_{L^*} a$  for each  $a \in L^* \setminus \{0_{L^*}, 1_{L^*}\}$ . Then f and g have a unique common fixed point.

*Proof.* Let  $x_0$  be an arbitrary point in X. By (a), choose a point  $x_1$  in X such that  $f(x_0) = g(x_1)$ . In general choose  $x_{n+1}$  such that  $f(x_n) = g(x_{n+1})$ . Then for t > 0

$$\mathcal{M}_{M,N}(f(x_n), f(x_{n+1}), t) \geq_{L^*} \mathcal{C}(\mathcal{M}_{M,N}(g(x_n), g(x_{n+1}), t))$$

$$= \mathcal{C}(\mathcal{M}_{M,N}(f(x_{n-1}), f(x_n), t))$$

$$>_{L^*} \mathcal{M}_{M,N}(f(x_{n-1}), f(x_n), t)$$

Thus  $\{\mathcal{M}_{M,N}(f(x_n), f(x_{n+1}), t); n \geq 0\}$  is increasing sequence in  $L^*$ . Therefore, tends to a limit  $a \leq_{L^*} 1_{L^*}$ . We claim that  $a = 1_{L^*}$ . For if  $a <_{L^*} 1_{L^*}$  on making  $n \longrightarrow \infty$  in the above inequality we get  $a \geq_{L^*} \mathcal{C}(a) >_{L^*} a$ , a contradiction. Hence  $a = 1_{L^*}$ , i.e.,

$$\lim_{n} \mathcal{M}_{M,N}(f(x_n), f(x_{n+1}), t) = 1_{L^*}.$$

If we define

(2.1) 
$$c_n(t) = \mathcal{M}_{M,N}(f(x_n), f(x_{n+1}), t)$$

then  $\lim_{n\to\infty} c_n(t) = 1_{L^*}$ . Now, we prove that  $\{f(x_n)\}$  is a Cauchy sequence in f(X). Suppose that  $\{f(x_n)\}$  is not a Cauchy sequence in f(X). For convenience, let  $y_n = fx_n$  for  $n = 1, 2, 3, \cdots$ . Then there is an  $\epsilon \in L^* \setminus \{0_{L^*}, 1_{L^*}\}$  such that for each integer k, there exist integers m(k) and n(k) with  $m(k) > n(k) \ge k$  such that

(2.2) 
$$d_k(t) = \mathcal{M}_{M,N}(y_{n(k)}, y_{m(k)}, t) \leq_{L^*} \mathcal{N}_s(\epsilon) \text{ for } k = 1, 2, \cdots.$$

We may assume that

(2.3) 
$$\mathcal{M}_{M,N}(y_{n(k)}, y_{m(k)-1}, t) >_{L^*} \mathcal{N}_s(\epsilon),$$

by choosing m(k) be the smallest number exceeding n(k) for which (2.2) holds. Using (2.1), we have

$$\mathcal{N}_{s}(\epsilon) \geq_{L^{*}} d_{k}(t) 
\geq_{L^{*}} \mathcal{T}(\mathcal{M}_{M,N}(y_{n(k)}, y_{m(k)-1}, t/2), \mathcal{M}_{M,N}(y_{m(k)-1}, y_{m(k)}, t/2)) 
\geq_{L^{*}} \mathcal{T}(c_{k}(t/2), \mathcal{N}_{s}(\epsilon))$$

Hence,  $d_k(t) \longrightarrow \mathcal{N}_s(\epsilon)$  for every t > 0 as  $k \longrightarrow \infty$ .

$$d_{k}(t) = \mathcal{M}_{M,N}(y_{n(k)}, y_{m(k)}, t)$$

$$\geq_{L^{*}} \mathcal{T}^{2}(\mathcal{M}_{M,N}(y_{n(k)}, y_{n(k)+1}, t/3), \mathcal{M}_{M,N}(y_{n(k)+1}, y_{m(k)+1}, t/3), \mathcal{M}_{M,N}(y_{m(k)+1}, y_{m(k)}, t/3))$$

$$\geq_{L^{*}} \mathcal{T}^{2}(c_{k}(t/3), \mathcal{C}(\mathcal{M}_{M,N}(y_{n(k)}, y_{m(k)}, t/3)), c_{k}(t/3))$$

$$\mathcal{T}^{2}(c_{k}(t/3), \mathcal{C}(d_{k}(t/3)), c_{k}(t/3)).$$

Thus, as  $k \longrightarrow \infty$  in the above inequality we have

$$\mathcal{N}_s(\epsilon) \geq_{L^*} \mathcal{C}(\mathcal{N}_s(\epsilon)) >_{L^*} \mathcal{N}_s(\epsilon)$$

which is a contradiction. Thus,  $\{f(x_n)\}_n$  is Cauchy and by the completeness of X,  $\{f(x_n)\}_n$  converges to z in X. Also  $\{g(x_n)\}_n$  converges to z in X. Let us suppose that the mapping f is continuous. Then  $\lim_n (f \circ f)(x_n) = f(z)$  and  $\lim_n (f \circ g)(x_n) = f(z)$ . Further we have since f and g are R-weakly commuting

$$\mathcal{M}_{M,N}((fog)(x_n), (gof)(x_n), t) >_{L^*} \mathcal{M}_{M,N}(f(x_n), g(x_n), t/R).$$

On letting  $n \to \infty$  in the above inequality we get  $\lim_n (gof)(x_n) = f(z)$ , by Lemma 1.11. We now prove that z = f(z). Suppose  $z \neq f(z)$  then  $\mathcal{M}_{M,N}(z, f(z), t) <_{L^*} 1_{L^*}$ . By (c)

$$\mathcal{M}_{M,N}(f(x_n),(f\circ f)(x_n),t) \geq_{L^*} \mathcal{C}(\mathcal{M}_{M,N}(g(x_n),(g\circ f)(x_n),t)).$$

On making  $n \to \infty$  in the above inequality we get

$$\mathcal{M}_{M,N}(z, f(z), t) \ge_{L^*} \mathcal{C}(\mathcal{M}_{M,N}(z, f(z), t)) >_{L^*} \mathcal{M}(z, f(z), t),$$

a contradiction. Therefore, z = f(z). Since  $f(X) \subseteq g(X)$  we can find  $z_1$  in X such that  $z = f(z) = g(z_1)$ . Now,

$$\mathcal{M}((fof)(x_n), f(z_1), t) \ge_{L^*} \mathcal{C}(\mathcal{M}_{M,N}((gof)(x_n), g(z_1), t)).$$

Taking limit as  $n \to \infty$  we get

$$\mathcal{M}_{M,N}(f(z), f(z_1), t) \ge_{L^*} \mathcal{C}(\mathcal{M}_{M,N}(f(z), g(z_1), t)) = 1_{L^*}$$

since  $C(1_{L^*}) = 1_{L^*}$ , which implies that  $f(z) = f(z_1)$ , i.e.,  $z = f(z) = f(z_1) = g(z_1)$ . Also for any t > 0,

$$\mathcal{M}_{M,N}(f(z),g(z),t) = \mathcal{M}((fog)(z_1),(gof)(z_1),t) \geq_{L^*} \mathcal{M}_{M,N}(f(z_1),g(z_1),t/R) = 1_{L^*}$$

which again implies that f(z) = g(z). Thus z is a common fixed point of f and g.

Now to prove uniqueness let if possible  $z' \neq z$  be another common fixed point of f and g. Then there exists t > 0 such that  $\mathcal{M}(z, z', t) <_L 1_{\mathcal{L}}$ , and

$$\mathcal{M}_{M,N}(z, z', t) = \mathcal{M}_{M,N}(f(z), f(z'), t)$$

$$\geq_{L^*} \mathcal{C}(\mathcal{M}_{M,N}(g(z), g(z'), t)) = \mathcal{C}(\mathcal{M}_{M,N}(z, z', t))$$

$$>_{L^*} \mathcal{M}_{M,N}(z, z', t)$$

which is contradiction. Therefore, z=z', i.e., z is a unique common fixed point of f and g.

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