

## Computer graphics

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## Second Graded Project

## 1. Voronoi diagram (Sec. 4.2 and 4.3, lab 6)

In lab6, we built a Voronoi diagram using Voronoi Parallel Linear Enumeration with Sutherland-Hodgman polygon clipping algorithm. Voronoi Parallel Linear Enumeration treats each Voronoi site independently and computes their Voronoi cell independently in parallel.

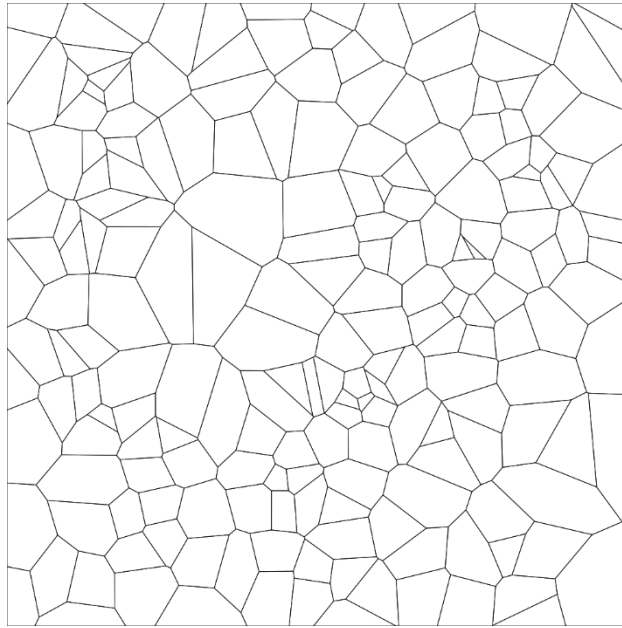
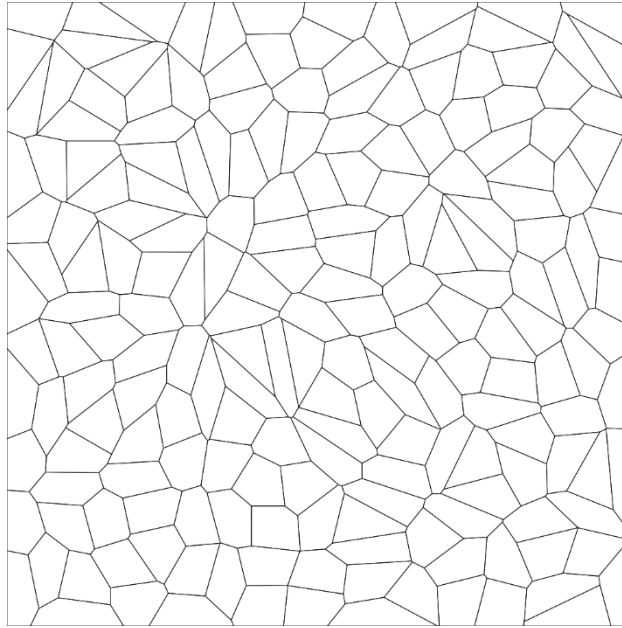


Figure 1: Voronoi diagram using Parallel Linear Enumeration with Sutherland-Hodgman polygon clipping algorithm with 200 cells. The rendering time is 18ms.

## 2. Power Diagram (Sec. 4.4.3, lab 7) and weights optimization using LBFGS (Sec 4.4.4, lab 7)

In lab 7, we extended our Voronoi diagrams to power diagrams, in which the size of the cells can be controlled using weights. Equal weights lead to a power diagram that corresponds to the Voronoi diagram. Moreover, increasing the value of a weight while keeping the others equal increases the area of the corresponding cell.

However, it is not easy to set the value of the weights to control the areas of the cells. Setting the weights can be seen as an optimal transport problem, where one wants to set the mass of the Voronoi cell according to the population density of the points. To find the optimal weights, we thus maximize a function using L-BFGS thanks to the libLBFGS library.

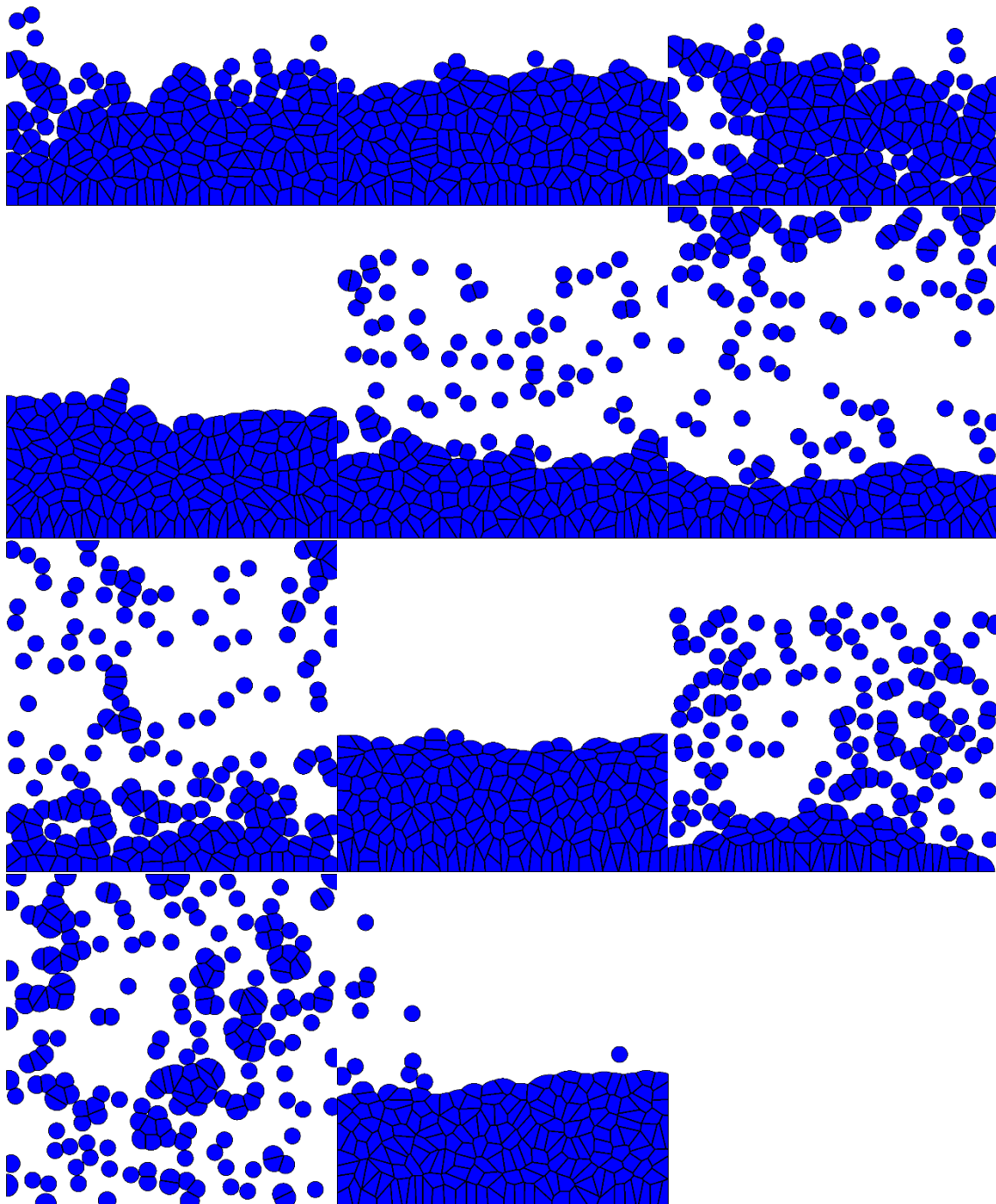


*Figure 2: Power diagram with 200 cells. The weight optimisation is achieved using LBFGS algorithm. The rendering time is 1800ms.*

### 3. Gallouet-Mérigot incompressible Euler scheme

In lab 7, we used semi-discrete optimal transport method to simulate fluids via incompressible Euler's equations, a simplification of Navier Stokes equations. We also added a spring force to each Laguerre's cells' centroid. We again use L-BFGS instead of a newton's optimizer, and our previous power diagram algorithm. Compared to lab 7, we are no longer optimizing  $N$  weights (each corresponding to each of the cell), but  $N+1$  weights, as we add a weight that is optimized such that the sum of all volumes of all Laguerre's cells remains constant (conservation of volume).

To obtain the following results (one frame every 50 time-step is displayed bellow), we used 500 frames, 200 cells, disks made out of polygons of 200 edges and a time-step of 0.004s. This took about 20 minutes due to the large number of edges. With 10 cells and using 500x500px frames, the computations take 7 minutes.



Comments on the class and suggestions for next year:

- I think that writing all the code on our own would make this course extremely demanding, and I don't even think that it would be feasible for us to do so, considering our engagement in other courses. I think it is a shame because everyone ends up heavily relying on your recordings and the live coding sessions. To be honest, I think that the assignments should be redesigned so that we can actually think about them and implement everything on our own. One possibility would be to ask us to fill existing functions and implement only some key components of the projects.
- Even with the help of the recordings and the live coding sessions, I tried to do as much as I could on my own and this took me more than 10 hours every week in average.
- It would also be great if we could get an introduction to debugging at the beginning of the course because we are not really familiar with that (in my case, I was not even familiar with c++ when I started the course).
- The content is really interesting, and it is probably one of the most applied CS courses we have here, so I was really glad that I took it. Personally, I had a hard semester as I was finalizing a paper at the beginning of the semester, and having interviews for PhD Programs, which did not let me a lot of time to work on this course.
- Concerning the attendance of the lectures, this is a problem in every course. Students generally prefer to study on their own and the fact that this is the last semester and that everyone is really tired and already got admitted in great schools for next years doesn't help.

I sincerely wanted to thank you for this semester. I particularly appreciated your reactivity in answering messages and the fact that you were always available to help on slack or answer questions during the tds. Thank you to Ellie as well for his help!