# Increasing realism in models of biotic interactions:

# ecological and evolutionary consequences

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### 4 Abstract

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Interactions between organisms give rise to emergent properties of natural systems. This
underpins the ubiquity of biotic interactions in the study of ecological and evolutionary
dynamics. The representation of biotic interactions often requires models and simplifying
assumptions since it is impossible to account for all aspects of the world in a single model.
Critical choices, such as the number of species that can alter the interaction between a focal pair or which abiotic variables constitute the environment, are necessary when building ecological and evolutionary models. Such simplifying assumptions inevitably lead
to the omission of heterogeneities at various levels. Complexity that is unaccounted for
can, in turn, make the relationships between organisms appear noisy and fundamentally
change model-based predictions. Despite this, ecological and evolutionary studies often
lack appropriate frameworks that allow the inclusion of different levels of complexity in
representations of biotic interactions. Thus, it is unclear whether including more realistic
assumptions is warranted for the vast majority of natural systems. In this thesis, I explore

how incorporating complexity as abiotic and biotic modifiers, as well as different sources
of uncertainty, reveals potential explanatory generalities in natural systems. I also explore
how accounting for these variables changes predictions related to the maintenance of diversity at ecological and evolutionary scales. Throughout this thesis, I focus on different
types of interactions and organisms and propose mathematical and statistical frameworks
that can be used beyond the studied systems.

In Chapter 2, I explore how the presence of multiple species and different environmen-24 tal contexts change the strength of plant-pollinator interactions. I propose a framework for using pollinator functional responses to examine the role of pollinator-pollinator interactions and abiotic conditions in altering the time between floral visits of a focal pollinator. I show that both density dependent responses and abiotic conditions are necessary to explain the number of visits a pollinator makes. In Chapter 3, I explore how incorporating different sources of uncertainty changes predictions of species coexistence. I do this by simultaneously exploring how different model formulations, environmental contexts, and parameter uncertainty change the probability of predicting coexistence in an experimental system. I provide direct evidence that predictions of species coexistence 33 are likely to change given the models used to quantify density-dependence. I also provide a theoretical framework to explore predictions made with different models. Finally, in Chapter 4, I adopt an ecological framework to examine the evolutionary dynamics of sexually antagonistic alleles. I show that incorporating environmental fluctuations can substantially increase the amount of genetic diversity in a population under sexually antagonistic selection. Overall, the results of my thesis show that the assumptions adopted

- <sup>40</sup> by some ecological and evolutionary models tend to be oversimplifying. Here, I provide
- tools for ecologists and evolutionary biologists to explore more realistic representations
- of biotic interactions as well as their consequences for diversity maintenance.

## 43 Preface

- My thesis has been prepared as a collection of three standalone scientific articles. Each
- chapter is a standalone piece of research and, therefore, I only provide a general Introduc-
- tion and Conclusion chapters linking the three chapters together. In **Chapter 1**, I focus on
- describing how my three chapters are connected. In Chapter 5, I focus on summarising
- the results from each of my thesis chapters and their combined implications both in both
- 49 how we study interactions and their consequences for diversity maintenance. Finally, I
- 50 further expand on new ideas beyond those presented in the different chapters to discuss
- 51 about the future steps moving forward.
- At the time of thesis submission, each of these three articles are in different stages of
- the publication process.
- Chapter 2: "The context dependency of pollinator interference: how environmental
- 55 conditions and co-foraging species impact floral visitaion" was published in May 2021 in
- the journal *Ecology Letters* in volume 24, no. 7, pages 1443–1454.
- 57 Chapter 3: "The interplay of environmental conditions, parameter sensitivity and
- structural sensitivity in predictions of species coexistence" is in preparation for submis-
- sion to *Ecology Letters*.
- 60 **Chapter 4**: "Quantifying the relative contributions of environmental fluctuations to
- the maintenance of a sexually antagonistic polymorphism" is in preparation for submis-
- sion to The American Naturalist.

## **Solution** Chapter 1: General Introduction

#### 64 Models of biotic interactions

Interactions between organisms underpin the persistence of almost all life forms on Earth (Lawton, 1999). Furthermore, a large body of work has shown that biotic interactions determine emergent properties of natural systems, such as stability (May, 1972; Wootton & Stouffer, 2016; Song & Saavedra, 2018), resilience (Capdevila *et al.*, 2021), ecosystem functioning (Turnbull *et al.*, 2013; Godoy *et al.*, 2020), and the coexistence of multiple species (Chesson, 2000; Saavedra *et al.*, 2017). Unsurprisingly, numerous ecological and evolutionary concepts revolve around the effects that organisms exert on each other (Gause, 1934; MacArthur & Levins, 1967; Thompson, 1999; HilleRisLambers *et al.*, 2012; Chase & Leibold, 2009).

From their origin as natural sciences, the disciplines of ecology and evolution have shifted from a descriptive towards a more predictive and quantitative approach. This shift brought with it the use of mathematical models to describe natural phenomena (Maynard-Smith, 1978; Rossberg *et al.*, 2019). Mathematical descriptions of interactions are "useful fictions" (Box *et al.*, 2011) in a twofold manner. First, they create a description of how organisms that coincide in space and time affect each other. Almost all known types of interactions can be described in the form of mathematical expressions that reproduce the observed data faithfully (Volterra, 1926; Holling, 1959; Holt, 1977; Adler *et al.*, 2018; Wood & Thomas, 1999; Holland *et al.*, 2002; Vázquez *et al.*, 2005; Stouffer & Novak, 2021) Second, models are practical tools with which to make predictions beyond the

phenomena they describe and thus, provide general insights into how natural systems operate (Evans *et al.*, 2012; Stouffer, 2019; Rossberg *et al.*, 2019).

## 86 The perils of simple models

Models that capture the effect of biotic interactions are abstractions of reality, and abstractions always reflect choices (Levins, 2006). Building models that include all aspects of reality is not only impractical but also unfeasible. Therefore, ecologists and evolutionary biologists have to continuously make choices regarding which variables to include in a model and which to omit (Evans *et al.*, 2012; Rossberg *et al.*, 2019). A common assumption when building models is that to achieve general insights, we should favor simple models (Evans *et al.*, 2013). Indeed there is a general belief in ecology and evolution that a good model should include as little as possible (Evans *et al.*, 2013; Orzack, 2012). This belief is often rooted in an implicit philosophical stance that one can not maximize generality (i.e., models that apply to more than one system) and realism (i.e., models that produce accurate predictions for a system) (Levins, 2006; Evans *et al.*, 2012).

Inevitably, model building in biology leads to a key question that will, in turn, modify the outcomes achieved by any model: when is a model "realistic" enough (Stouffer,
2019)? The answer to this question will depend on the purpose for which a model is
built. Models that capture the effect of biotic interactions tend to fall into the category of
"demonstration models". These types of models are often based on phenomenological
descriptions of processes and have the general aim to show that the modeled principles
are sufficient to produce the phenomena of interest (Evans *et al.*, 2013). Demonstration

models however, do not help decide whether the modelled principles are *necessary* (Evans *et al.*, 2013). The task to decide the necessary principles and thus the answer to the question of when a model is realistic enough becomes the modeler's responsibility. In many cases, the answer to this question can appear arbitrary or solely determined by the predominant paradigm regarding the studied system (Holland *et al.*, 2006; Bascompte *et al.*, 2006; Kokko & López-Sepulcre, 2007; AlAdwani & Saavedra, 2019; Mayfield & Stouffer, 2017; Martyn *et al.*, 2021).

Always favoring simple models in ecological and evolutionary studies can be prob-112 lematic from two perspectives. First, the assumption that more complex models do not 113 lead to general insights is seldomly tested. For example, most models that capture competitive interactions between plants have the implicit assumption that competitive effects 115 between individuals are always additive and direct (Schoener, 1974; Freckleton & Watkin-116 son, 2001; Kraft et al., 2015). However, when models and data collection were set up to 117 capture non-additive effects of interactions between individuals of co-occurring species, 118 the evidence overwhelmingly showed that including these levels of biotic complexity 119 was necessary to capture plant interactions accurately (Mayfield & Stouffer, 2017; Martyn 120 et al., 2021; Lai et al., 2021). Thus, in some cases, increasing complexity increases rather 121 than hampers the general insights obtained from models of biotic interactions. 122

Second, failing to include necessary levels of complexity can hinder our ability to predict how natural communities will react to novel conditions. Predictions of how natural systems will behave in the future are inherently challenging (Sutherland, 2006). Nevertheless, ignoring heterogeneities at various levels can further complicate rather than simplify predictions (Evans *et al.*, 2012). For instance, demographic models tend to treat ecological and evolutionary dynamics separately, despite the general understanding that both processes are often intertwined (MacArthur, 1962; Kokko & López-Sepulcre, 2007). Ignoring eco-evolutionary feedbacks leads to predictions that are inconsistent with empirical data and produce counterintuitive results in novel conditions (Kokko & López-Sepulcre, 2007). Thus, the implicit assumption that good models should include as little as possible should be treated with caution in ecological and evolutionary contexts (Evans *et al.*, 2013; Kokko & López-Sepulcre, 2007; Abrams, 2001).

### Challenges and consequences of increasing realism

Despite arguments in favor of increasing realism in models of biotic interactions, doing so remains a challenge in many ecological and evolutionary studies. One of those challenges 137 arises from the lack of theoretical frameworks that allow incorporating intricate empirical 138 observations into models (Abrams, 1983). Such is the case of competition between pollinators that forage for the same resources (Thomson & Page, 2020). An overwhelmingly 140 amount of empirical evidence shows that pollinators modify their foraging behavior in 141 the presence of other foraging species (Morse, 1977; Inouye, 1978; Thompson et al., 2006; Brosi & Briggs, 2013; Briggs, 2016), however, incorporating these behavioral changes into 143 population dynamics remains elusive (Thomson & Page, 2020). Furthermore, density-144 dependent responses could themselves depend on the abiotic conditions pollinators experience, as many studies have shown that environmental conditions can drastically change 146 how pollinators behave while foraging (Heinrich, 1976; Thomson et al., 1987; Cnaani et al., 147

2006; Westphal et al., 2006; Briggs et al., 2018; Classen et al., 2020). A coherent framework with which to incorporate both abiotic and biotic drivers into plant–pollinator interac-149 tions was lacking. To this end, in **Chapter 2** I develop a general framework to show how 150 pollinator functional responses can be used to incorporate biotic and abiotic drivers into 15 floral visitation rates. Furthermore, I show the empirical relevance of this framework by 152 parameterizing different models that incorporated pollinator-pollinator interactions and 153 environmental conditions when predicting observed data from a highly controlled foraging chamber experiment. Results from this chapter have substantial implications related 155 to our understanding of how species loss and environmental change might affect mutu-156 alistic communities.

Another theoretical challenge emerges when alternative models to represent biotic in-158 teractions are used interchangeably. Such is the case of phenomenological models of plant competition, where more than one mathematical form can faithfully reproduce empirical data (Levine & HilleRisLambers, 2009; Godoy & Levine, 2014; Godoy et al., 2014; May-161 field & Stouffer, 2017; Bimler et al., 2018). The effect biotic and abiotic drivers have in 162 model based predictions can be dramatically different due to uncertainty associated with 163 phenomenological models (Jørgensen & Bendoricchio, 2001; Flora et al., 2011; Aldebert 164 Clement & Stouffer Daniel B., 2018). To understand the interplay between uncertainty 165 and abiotic complexity, in Chapter 3 I introduce a mathematical and statistical framework to simultaneously explore how different phenomenological models of plant competition, 167 environmental contexts, and parameter uncertainty determine predictions of species co-168 existence. Additionally, I use this framework to make predictions around a pairwise competition experiment between annual plants, where I show that the effect of abiotic conditions in predictions of species coexistence is not independent of the model formulation used to describe species interactions.

Finally, it is not only important to understand whether increasing realism changes predictions, but it is also essential to understand how. For instance, theoretical studies have shown that environmental fluctuations can substantially increase the levels of genetic di-175 versity in populations that experience sexually antagonistic selection (Connallon & Clark, 2012; Connallon et al., 2019; Patten et al., 2010; Jordan & Charlesworth, 2012). However, 177 there are no approaches that directly quantify how environmental fluctuations promote 178 genetic diversity in populations that experience sexual conflict. Hence, in **Chapter 4** I adopt an ecological framework that allows the quantification of the relative contributions 180 of environmental fluctuations using simulations to capture the effect of environmental 181 fluctuations in evolutionary dynamics. In this chapter I show that incorporating environ-182 mental heterogeneity is essential to fully understand the effect of when and how sexually 183 antagonistic selection can maintain genetic diversity. 184

## Concluding remarks

In this thesis, I propose theoretical and statistical frameworks that allow increasing realism in models of biotic interactions with the aim to understand when higher levels
of complexity are justified. Furthermore, I also explore the consequences of increasing
model realism in predictions related to diversity maintenance at ecological and evolutionary scales. The individual chapters of this thesis are thematically broad as they are

focused on different types of interactions and organisms, but all address in a different way the challenges and consequences of incorporating biotic and abiotic complexity in the study of biotic interactions.

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