92586 Computational Linguistics

8. "One" Neuron

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Previously

From Words to Topics

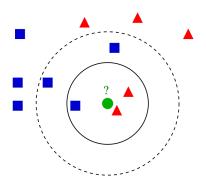
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- 1 There was Life Before Deep Learning
- 2 Some History
- 3 The Perceptron
- 4 More than One Neuron
- Chapter 5 of Lane et al. (2019)

(And Many Non-NN in-Production Models Prevail)

- Naïve Bayes
- k-nearest neighbors
- Random forests
- Support vector machines
- HMM
- Logistic Regression
- o . . .

k-Nearest Neighbours

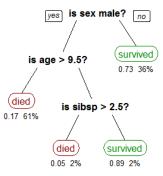


The class of \bullet is the same as the most frequent among its k neighbours

https://en.wikipedia.org/wiki/K-nearest_neighbors_algorithm > > > 000

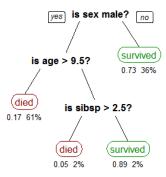
Random Forests

Titanic survivors



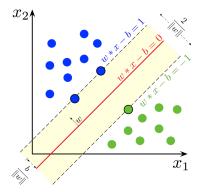
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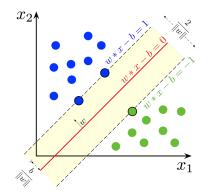


Multiple decision trees are learned and the final class is the **mode**

Support Vector Machines



Support Vector Machines

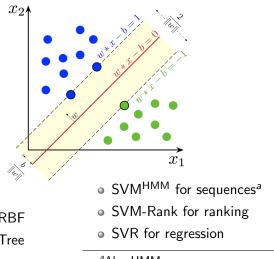


Kernels

Linear

- RBF
- Polynomial
- Tree

Support Vector Machines



Kernels

Linear

RBF

Polynomial

Tree

^aAlso HMM

There are many, many others

Often they are SoA (or close)

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- Some of them give explainable outcomes
- Representations have to be engineered

Some History

Some History

Opening paragraph of Rosenblatt (1957)'s **The Perceptron—a** perceiving and recognizing automaton

Since the advent of electronic computers and modern servo systems, an increasing amount of attention has been focused on the feasibility of constructing a device possessing such human-like functions as perception, recognition, concept formation, and the ability to generalize from experience. In particular, interest has centered on the idea of a machine which would be capable of conceptualizing inputs impinging directly from the physical environment of light, sound, temperature, etc. -- the "phenomenal world" with which we are all familiar -- rather than requiring the intervention of a human agent to digest and code the

necessary information.

Al Winters

1974–1980 First major winter 1987–1993 Second major winter

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1966 failure of MT

1970 abandonment of connectionism

1971–75 DARPA's frustration wrt CMU speech recognition research

1973 Lighthill report decreases AI research in the UK

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Al Winters

- 1974–1980 First major winter 1987–1993 Second major winter
 - 1966 failure of MT
 - 1970 abandonment of connectionism
 - 1971–75 DARPA's frustration wrt CMU speech recognition research
 - 1973 Lighthill report decreases AI research in the UK
 - 1973–74: DARPA's cutbacks to academic AI research
 - 1987 collapse of the LISP machine market
 - 1988 cancellation of new spending on AI by the Strategic Computing Initiative
 - 1993 resistance to expert systems deployment and maintenance
 - $1990s\,$ end of the Fifth Generation computer project's original goals

• Intended to be a machine able of recognising images

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- Rough idea:

Input: features of an image (small subsections)

Parameters: weights for each feature (measure of importance)

Output: Fire once all potentiometers pass a certain threshold

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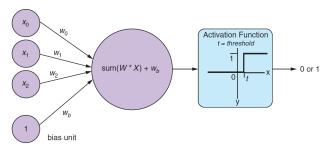
Parameters: weights for each feature (measure of importance)

Output: Fire once all potentiometers pass a certain threshold

Fired: positive match in the image

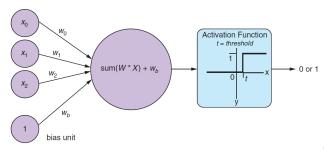
Did not fire: negative class

Numerical Perceptron¹



¹I am discarding any biological reference

Numerical Perceptron¹

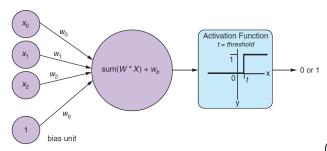


(Lane et al., 2019, p. 158)

• Feature vector: $X = [x_1, x_2, \dots, x_i, \dots, x_n]$

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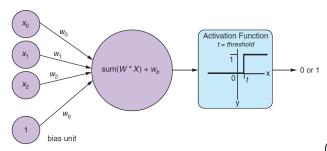
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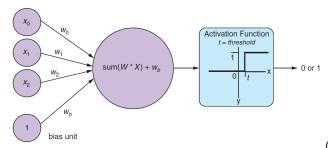
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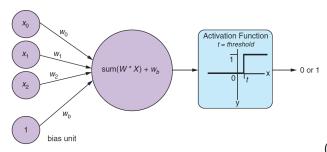
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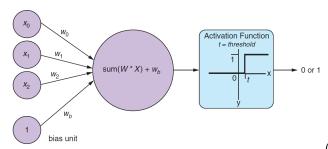
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- Bias: always-on input (resilientcy to inputs of all zeros)

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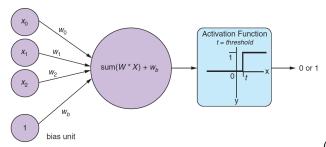
4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 4 | 1 |

Numerical Perceptron



$$f(\vec{x}) = \begin{cases} 1 & \text{if } \sum_{i=0}^{n} x_i w_i > \text{threshold} \\ 0 & \text{otherwise} \end{cases}$$
 (1)

Numerical Perceptron



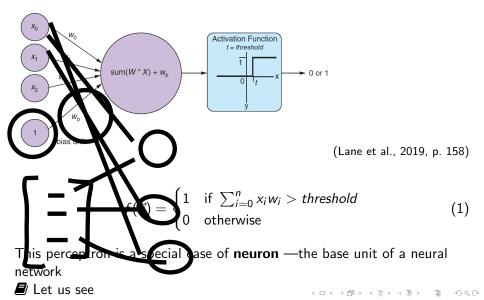
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This perceptron is a special case of **neuron** —the base unit of a neural network

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Numerical Perceptron



Without Bias

"The output of [a perceptron] is a linear function of the input" (Goodfellow et al., 2016, p. 105)

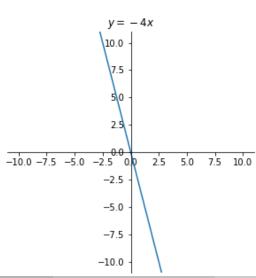
$$\hat{y} = w^T x \tag{2}$$

Without Bias

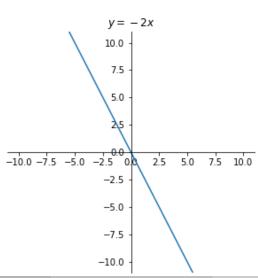
```
import matplotlib.pyplot as plt
import numpy as np
for i in range(-5, 5, 1):
    fig, ax = plt.subplots(figsize = (5,5))
    ax.spines['left'].set_position('center')
    ax.spines['bottom'].set_position('center')
    ax.spines['right'].set_color('none')
    ax.spines['top'].set_color('none')
    ax.set(title='$y=w^Tx$')
    x = np.arange(-5.0, 5.0, 0.01)
    plt.xlim((-5,+5))
    plt.ylim((-5,+5))
    ax.set(title='$y={}x$'.format(i))
    y = i*x #1 + np.sin(2 * np.pi * x)
    ax.plot(x, y)
    fig.savefig("linear_w{}.png".format(i))
   plt.show()
```

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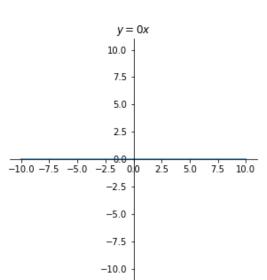
Without Bias



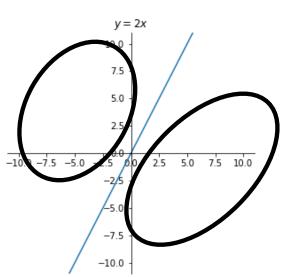
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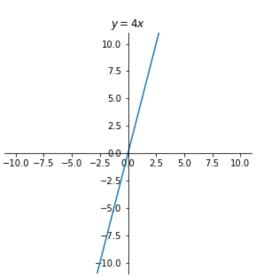
Without Bias



Without Bias

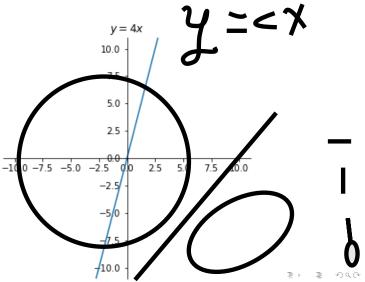


Without Bias



Without Bias

Plotting with different values of w do you see an issue?



With Bias

$$\hat{y} = \underline{w}^T \underline{x} + \underline{b} \tag{3}$$

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"[...] the mapping from parameters to predictions is still a linear function but the mapping from features to predictions is now an affine function" (Goodfellow et al., 2016, p. 107)

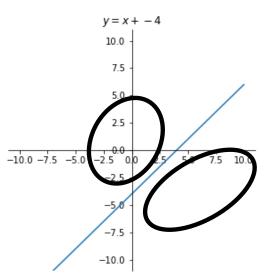
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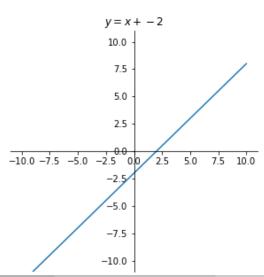
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(does not need to pass by the origin)

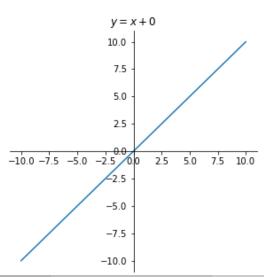
Without Bias



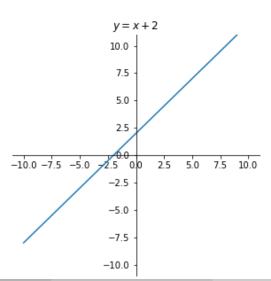
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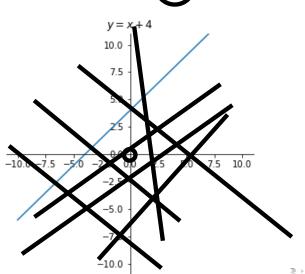
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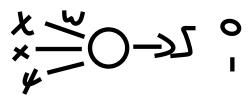


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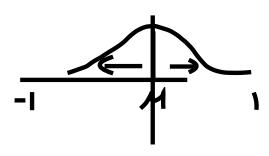
Typical Learning Process (1/2)

Given an annotated dataset...



• start with a random weight initialisation from a normal distribution

$$\vec{w} \sim \mathcal{N}(\mu, \sigma^2)$$
 with $\mu \sim 0$ (but do not use 0!)



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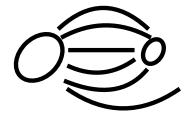
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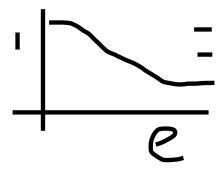
Each weight is adjusted by how much it contributed to the resulting error



Typical Learning Process (2/2)



- All instances in the training data are fed a number of times: epoch
- Typical stop criteria include
 - $error < \epsilon$ (convergence)
 - ► error stabilises
 - ► max number of epochs reached

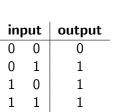


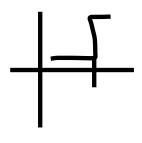
O

Example 1: Logical OR

in	out	output
0	0	0
0	1	1
1	0	1
1	1	1

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Mr. Perceptron can learn!

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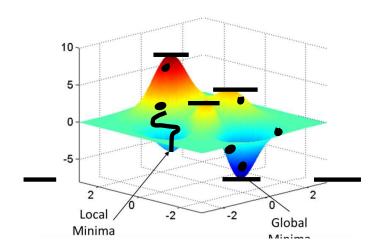
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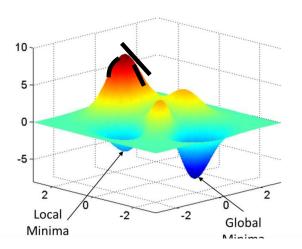
This learning model is called linear regression (another ML alternative)

Drawback: Local vs Global Minimum



Plot from M. Ryan's thesis (http://www.isni.org/isni/000000045916099%)

Drawback: Local vs Global Minimum



No guarantee that the model will reach the global optimal solution

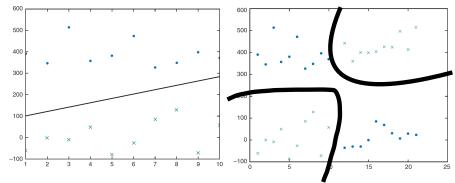
Plot from M. Ryan's thesis (http://www.isni.org/isni/000000045916099%) Alberto Barrón-Cedeño (DIT-UniBO)

Drawback: Linearly separable

The perceptron can only deal with linearly separable data

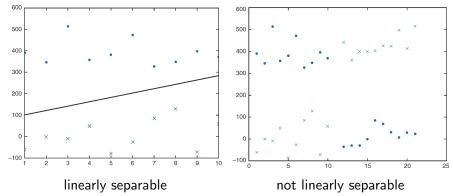
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Plots from (Lane et al., 2019, p. 164-165)

Example 2: Logical XOR

We have learned a logical OR function . . .

Can we learn a logical XOR?

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Let us see

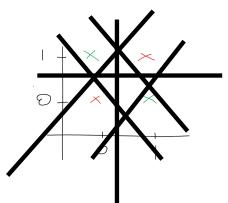
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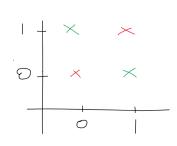


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Mr. Perceptron cannot learn!

... winter

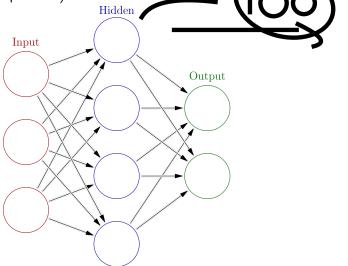
More than One Neuron

Neural Networks

A neural network is a combination of multiple perceptrons (and it can deal with more complex patterns)

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Input $x = [x_1, x_2, x_3, ..., x_k]$ Output $f(x)^2$ Answer y

 $^{^2}$ aka y'

³aka loss function

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Answer <u>y</u>

Cost Function³ Quantifier of the mismatch between actual and predicted output

$$err(x) = |y - f(x)| \tag{4}$$

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Training goal Minimising the cost function across all input samples

$$J(x) = \min_{i=1}^{n} \sum_{i=1}^{n} err(\underline{x_i})$$
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Next

- Backpropagation (briefly)
- Activation functions
- Keras



References

Goodfellow, I., Y. Bengio, and A. Courville 2016. *Deep Learning*. MIT Press. http://www.deeplearningbook.org.

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