# Typesetting Order Theory Under LATEX

#### Author

Andrew Lincoln Burrow albcorp@gmail.com

#### **Abstract**

The AlbOrderTheory package provides a single alb-order-theory LATEX package to provide markup for set and order theory. It is designed to make the LATEX input more readable, to allow the actual symbols to be adjusted from a single file, to enable the typesetting of set and order theoretic constructions to be designed in the context of the entire suite of required markup commands, and to place the extended markup in the alb namespace. Therefore, the package provides a large collection of math commands to markup operators, relations, and functions. The package is supported by an emacs lisp file customising AUCTEX, which provides command name completion and argument prompting.

### Copyright

Copyright © 1999–2006, 2013 Andrew Lincoln Burrow.

This program may be distributed and/or modified under the conditions of the LATEX Project Public License, either version 1.3 of this license or (at your option) any later version.

The latest version of this license is in

```
http://www.latex-project.org/lppl.txt
```

and version 1.3 or later is part of all distributions of LaTeX version 2005/12/01 or later.

This work has the LPPL maintenance status 'author-maintained'.

This work consists of the files

```
alb-algorithms.sty, alb-avm.sty, alb-latex.cls, alb-float-tools.sty, alb-graph-theory.sty, alb-journal.cls, alb-order-theory.sty, alb-proofs.sty, alb-theorems.sty, alb-thesis.cls, alb-algorithms.tex, alb-avm.tex, alb-latex.tex, alb-float-tools.tex, alb-graph-theory.tex, alb-journal.tex, alb-order-theory.tex, alb-proofs.tex, alb-theorems.tex, alb-thesis.tex. alb-journal-glossary.ist, alb-journal-index.ist, alb-thesis-glossary.ist, and alb-thesis-index.ist.
```

#### **Version Information**

Revision Date

## 1 Introduction

The alb-order-theory LaTeX package is designed to typeset order theory. In practice, this means that it supplies a large collection of simple math commands. The main benefit is consistency, and the ability to easily change a decision about typesetting for all documents.

## 2 Using the Commands and Environments

The commands and environments of the alb-order-theory LATEX package are divided into mathematical groups. They are all used within math mode.

## 2.1 Logical Connectives

In lattice theory we use the vee and the wedge for join and meet. Therefore, we lack an obvious symbol for the logical connectives. The current solution is just to use text labels.

\albNot x	$\operatorname{not} x$
x \albAnd y	x and $y$
x \albOr y	x  or  y

## 2.2 Set Theory

Commands accepting arguments and generating set theory mathematical construc-

\albSingleton{x}	$\{x\}$
\albCardinality{X}	X
\albTuple{x, y, z}	$\langle x, y, z \rangle$
\albPowerset{X}	$\mathcal{P}(X)$
$\albBinaryRelation\{R\}\{X\}\{Y\}$	$R \subseteq X \times Y$
\albPartialMap{\alpha}{X}{Y}	$\alpha:X\to Y$
$\albTotalMap{\alpha}{X}{Y}$	$\alpha:X\mapsto Y$
\albDomain{\alpha}	$domain(\alpha)$
\albRange{\alpha}	$range(\alpha)$
f \albCompose g	$f \circ g$

#### 2.3 Standard Sets

Commands without arguments representing the standard sets of arithmetic.

\albNaturals	$\mathbb{N}$
\albReals	$\mathbb{R}$

### 2.4 Order Theory

Commands accepting arguments and generating order theory mathematical constructions.

```
x \albIncomparable y x \parallel y x \albCoveredBy y x \prec y x \albCovers y x \succ y
```

\albEquivClass{x} \albDual{P}	$egin{array}{c} [x] \ P^{\partial} \end{array}$
<pre>\albOver{P}{x} \albUnder{P}{x} \albMax{A} \albMin{A} \albHeads{P} \albTails{P} \albWidth{P}</pre>	over(P, x) under(P, x) max(A) min(A) heads(P) tails(P) width(P)
<pre>\albHeight{P} x \albJoin y \albJoinOf{A} \albJoinInOf{P}{A} x \albMeet y \albMeetOf{A} \albMeetInOf{P}{A}</pre>	$\begin{array}{l} \operatorname{height}(P) \\ x \vee y \\ \bigvee A \\ \bigvee_P A \\ x \wedge y \\ \bigwedge A \\ \bigwedge_P A \end{array}$
<pre>\alb0rderEmbedding{\alpha}{0}{P} 0 \alb0rderIsomorphic P</pre>	$\alpha: O \hookrightarrow P$ $O \cong P$
\albDown{A} \albUp{A} \albDownInOf{P}{A} \albUpInOf{P}{A}	$ \downarrow A  \uparrow A  \downarrow_P A  \uparrow_P A $
\albLower{A} \albUpper{A} \albLowerInOf{P}{A} \albUpperInOf{P}{A}	
<pre>\albDownSets{P} \albRise{P}{x} \albFall{P}{x} \albDM{P} \albCD{P} \albExtenders{P}{A} \albRetractors{P}{A}</pre>	$\mathcal{O}(P)$ $\mathrm{rise}(P,x)$ $\mathrm{fall}(P,x)$ $\mathrm{DM}(P)$ $\mathrm{CD}(P)$ $\mathrm{extenders}(P,A)$ $\mathrm{retractors}(P,A)$

## 2.5 Notation for the Growth of Functions

Commands accepting arguments and generating expressions for the growth of functions.

\albBigOh{f}	O(f)
\albBigOmega{f}	$\Omega(f)$
\albBigTheta{f}	$\Theta(f)$

# 3 AUCT<sub>E</sub>X Customisations

Under AUCTEX the file alb-order-theory.el is automatically loaded whenever the alb-order-theory package is used. The customisation adds the math commands to AUCT<sub>E</sub>X. This provides the simple prompting for all the supplied math commands.

In addition, alb-order-theory.el causes a special equation number counter to be stored as a local variable. alb-LaTeX-equation-counter counts numbers assigned to labels for equations. This ensures dirty numbers are not reissued, as reissuing a number could make stale references hard to detect.

## 4 Makefile Targets

The AlbLaTeXDocumentTemplate makefile provides a target to relabel equations. The alb-relabel-eq target edits the LATEX source in an attempt to match equation labels to equation numbers. Labels of the form eq: identifier: number are processed. number is rewritten to the last part of the equation number. This is helpful in proof reading.