

**Problem 1** (1). For the map  $\phi(x) = x \sin(x)$  of the real line to itself, what are the regular values?

*Proof.*

□

**Problem 2** (3). For the map  $\phi(x, y) = \sin(x^2 + y^2)$  of the plane to the line, what are the regular values?

*Proof.*

□

**Problem 3** (5). Let  $\gamma : \mathbb{R} \rightarrow \mathbb{R}^2$  be a smooth curve in the plane. Let  $K$  be the set of all  $r \in \mathbb{R}$  such that the circle of radius  $r$  about the origin is tangent to the curve  $\gamma$  at some point. Show that  $K$  has empty interior in  $\mathbb{R}$ .

*Proof.*

□

**Problem 4** (6). If  $C$  is a circle embedded smoothly in  $\mathbb{R}^4$ , show that there exists a three-dimensional hyperplane  $H$  such that the orthogonal projection of  $C$  to  $H$  is an embedding.

*Proof.*

□