

# 2020 Introduction to Massive Data Analysis

## Assignment 2

**Deadline: 2020/10/28 (WED) 23:59**

### Question: PageRank

Given a big matrix  $M$ . Specifically the column-normalized adjacency matrix where each column represents a webpage (vertex) and where it links to the non-zero entries. Write a program that calculates Google Matrix  $A$ :

$$A = \beta M + (1 - \beta) \begin{bmatrix} 1 \\ \vdots \\ 1 \end{bmatrix}_{N \times N}$$

With PageRank equation [Brin-Page, '98]

$$r_j = \sum_{i \rightarrow j} \beta \frac{r_i}{d_i} + (1 - \beta) \frac{1}{N}$$

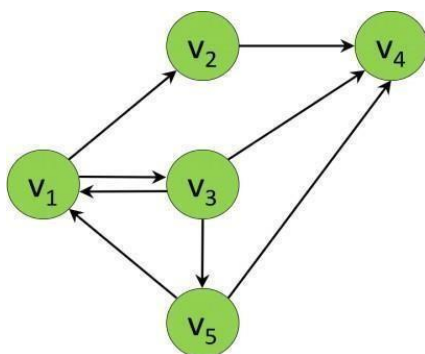
forming recursive problem:  $r = A \cdot r$

If  $M$  contains **dead-ends**, we have to renormalize  $r^{\text{new}}$ :

$$\forall j: r_j^{\text{new}} = r_j^{\text{new}} + \frac{1-S}{N} \quad \text{where: } S = \sum_j r_j^{\text{new}}$$

**NOTE: Please set  $\beta = 0.8$ , and initial PageRank value =  $1/N$  in this homework.**

**Example:**



$V = \{1, 2, 3, 4, 5\}$  and  $E = \{(1, 2), (1, 3), (2, 4), (3, 1), (3, 4), (3, 5), (5, 1), (5, 4)\}$

i	1	2	3	4	5
$r_i^1$	0.205	0.152	0.152	0.365	0.125

If we set  $\beta = 0.8$ , initial PageRank value =  $1/5$ , and run a single round of PageRank, we get the following values:

If we run 10 rounds of PageRank, we get the following values:

i	1	2	3	4	5
$r_i^{10}$	0.193	0.170	0.170	0.329	0.138

### Data format:

#### Input:

A file that contains one line for each link, and each line contains a pair of numbers that represent the vertices that are connected by the link.

1	2
1	3
2	4
3	1
3	4
3	5
5	1
5	4

#### Output:

There should be one line for each vertex, and each line should contain the vertex identifier and the PageRank values.

4	0.329
1	0.193
2	0.170
3	0.170
5	0.138

### Structure:

**[Mapper]** A node passes its PageRank “contributions” to the nodes it is connected to.

**[Reducer]** Each node sums up all PageRank contributions that have been passed to it.

## Assignment Requirements:

### Part1 Code (80%)

Please make sure that your .java file has the same name as your class name, which must be **PageRank**.

If you implement the algorithm with Python, please name your .ipynb file as **PageRank**, too.

### Part2 Report (20%)

- a. Final output. (We require **20** iterations result)  
Please show the **top 10 vertices** sorted by rank.
- b. Explain how you design your mapper and reducer.

If you implement with the algorithm Python, You can write your report in .ipynb file

Please pack above files into a zip file. Name it as "**MDA\_HW2\_studentID.zip**".