

# Solution 1:

For every employee **b** choose **the single cheapest offer that makes someone supervise b**.

If an employee receives no offer, she must be the root.

If more than one employee has no offers, a rooted tree cannot be built.

## Algorithm ( $O(m)$ )

Step	Action
1	Read <code>n, m</code> , arrays <code>qual</code> , applications.
2	For each triple <code>(a, b, c)</code> with <code>qual[a] &gt; qual[b]</code> keep <code>best[b] = min(best[b], c)</code> .
3	<b>Feasibility</b> Exactly one employee must lack an entry in <code>best</code> . Condition <code>best.size() == n - 1</code> .
4	<b>Answer</b> Sum of all <code>best[b]</code> ; else <code>-1</code> .

## Why it's good

*Edges never point upward*, so any solution can replace its edge into `b` with the cheapest one without affecting the rest of the tree; thus picking all local minima is globally minimal.

## Corner cases

- `n = 1` (no edges needed)  $\rightarrow$  cost 0.
- Duplicate offers for same `b`  $\rightarrow$  keep the smallest.
- Malformed data with upward edges  $\rightarrow$  ignore (not in judge input, but harmless guard).

This was accepted on the first attempt