

STAT 3493
ASSIGNMENT #7

Q5: Ex 54, Pg 525

$$\hat{p}_1 = \frac{104}{207} = 0.5024$$

$$\hat{p}_2 = \frac{109}{213} = 0.517$$

$$\begin{aligned} \hat{p} &= \frac{m}{m+n} \hat{p}_1 + \frac{n}{m+n} \hat{p}_2 = \frac{207}{207+213} \cdot \frac{104}{207} + \frac{213}{207+213} \cdot \frac{109}{213} \\ &= 0.507 \end{aligned}$$

$$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}(1-\hat{p})\left(\frac{1}{m} + \frac{1}{n}\right)}} = \frac{0.502 - 0.517}{\sqrt{0.507(1-0.507)\left(\frac{1}{207} + \frac{1}{213}\right)}} = -0.191$$

$$H_a: p_1 - p_2 < 0 \quad z = -0.191$$

$$P = \Phi(z) = 0.424$$

The null hypothesis cannot be rejected at a significance level $\alpha = 0.10$. The data does not support the researcher's hypothesis at this significance level.