

```

1 // the game in normal form, a n dimensional matrix of payoff vectors.
2 // - it is indexed by the strategies to make the code clearer
3 game = {
4   U: { L: [2, 6], C: [0, 4], R: [4, 4] },
5   M: { L: [3, 3], C: [0, 0], R: [1, 5] },
6   D: { L: [1, 1], C: [3, 5], R: [2, 3] },
7 }
8
9 // these are the parameters for each part of the question
10 // - player = the player for which to calculate best response
11 // - strategy = the probabilities in the other player's mixed strategy
12 questionParts = {
13   a: { player: 1, strategy: [ 1/6, 1/3, 1/2 ] },
14   b: { player: 2, strategy: [ 1/6, 1/3, 1/2 ] },
15   c: { player: 1, strategy: [ 1/4, 1/8, 5/2 ] },
16   d: { player: 1, strategy: [ 1/3, 1/3, 1/3 ] },
17   e: { player: 2, strategy: [ 1/2, 1/2, 0/1 ] },
18 }
19
20 // This function calculates the best response
21 function bestResponse({ game, strategy, player }) {
22   // this part of the code used to keep track of which strategies are best
23   brSet = []
24   maxPayoff = -99999
25   function updateBR({ payoff, s }) {
26     // add strategy to set of best responses if payoffs are equal:
27     if (payoff === maxPayoff) brSet.push(s)
28
29     // a new max payoff was found...
30     // the set of best responses is the current strategy:
31     if (payoff > maxPayoff) {
32       maxPayoff = payoff;
33       brSet = [s]
34     }
35   }
36
37   // This part of code calculates the payoffs
38   if (player === 1) {
39     // calculate player 1's payoff for each strategy s1 in S1
40     S1 = ['U', 'M', 'D']
41     for (s1 of S1) {
42       const payoff =
43         game[s1].L[0] * strategy[0] + // u1(s1,L) * probability s2 = L
44         game[s1].C[0] * strategy[1] + // u1(s1,C) * probability s2 = C
45         game[s1].R[0] * strategy[2] // u1(s1,R) * probability s2 = R
46
47       console.log(`u(${s1}, theta_2) = ${payoff}`) // log the payoff
48
49       // keep track of which responses 's' are best
50       updateBR({ payoff, s: s1 })
51     }
52   }
53
54   // calculate player 2's payoff for reach strategy s2 in S2
55   if (player === 2) {
56     S2 = ['L', 'C', 'R']
57     for (s2 of S2) {
58       payoff =
59         game.U[s2][1] * strategy[0] + // u2(U,s2) * probability s1 = U
60         game.M[s2][1] * strategy[1] + // u2(M,s2) * probability s1 = M

```

```
61     game.D[s2][1] * strategy[2]    // u2(D,s2) * probability s1 = D
62
63     console.log(`u(theta_1, ${s2}) = ${payoff}`) // log the payoff
64     updateBR({ payoff, s: s2 })
65
66 }
67 }
68 return brSet
69 }
70
71 // execute the code for each part of the problem
72 for (letter of Object.keys(questionParts)) {
73     console.log(`${letter}`)
74
75     // get set of best responses and output
76     br = bestResponse({ game, ...questionParts[letter] })
77     console.log(`BR is ${br.join(',')}`)
78 }
79
80 /*
81  * output:
82
83 a)
84 u(U, theta_2) = 2.3333333333333335
85 u(M, theta_2) = 1
86 u(D, theta_2) = 2.1666666666666667
87 BR is {U}
88
89 b)
90 u(theta_1, L) = 2.5
91 u(theta_1, C) = 3.1666666666666665
92 u(theta_1, R) = 3.833333333333333
93 BR is {R}
94
95 c)
96 u(U, theta_2) = 10.5
97 u(M, theta_2) = 3.25
98 u(D, theta_2) = 5.625
99 BR is {U}
100
101 d)
102 u(U, theta_2) = 2
103 u(M, theta_2) = 1.3333333333333333
104 u(D, theta_2) = 2
105 BR is {U,D}
106
107 e)
108 u(theta_1, L) = 4.5
109 u(theta_1, C) = 2
110 u(theta_1, R) = 4.5
111 BR is {L,R}
112
113 */
```