

# STAT 3093 ASSIGNMENT #7

Q1. Ex 24, pg 506

$$CI = \bar{x} - \bar{y} \pm t_{\alpha/2, v} \sqrt{\frac{s_1^2}{m} + \frac{s_2^2}{n}}$$

$$v = \frac{\left(\frac{s_1^2}{m} + \frac{s_2^2}{n}\right)^2}{\frac{(s_1^2/m)^2}{m-1} + \frac{(s_2^2/n)^2}{n-1}} = \frac{\left(\frac{5.5^2}{28} + \frac{7.8^2}{31}\right)^2}{\frac{(3.5^2/28^2)}{28-1} + \frac{(7.8^2/31^2)}{31-1}} = 53.95$$

round down  $\rightarrow v = 53$

$$\alpha = 0.1, \quad t_{\alpha/2, v} = 1.67$$

$$CI = 91.5 - 88.3 \pm 1.67 \sqrt{\frac{5.5^2}{28} + \frac{7.8^2}{31}}$$

$$= (-0.28, 6.12)$$

For a 90% confidence interval, it suggests a difference.

For 95% CI,  $\alpha = 0.05$ ,  $t_{\alpha/2, v} = 2.01$

$$CI = (-0.299, 6.76)$$

no difference is suggested at CI level of 95%.



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Q2: EX 28, PG 547

$$H_0: \mu_1 = \mu_2$$

$\mu_1$  = mean for cola

$$H_a: \mu_1 - \mu_2 > 0$$

$\mu_2$  = mean for strawberry.

$$t = \frac{\bar{X} - \bar{Y} - \Delta_0}{\sqrt{\frac{s_1^2}{m} + \frac{s_2^2}{n}}} = \frac{554 - 540 - 0}{\sqrt{\frac{15^2}{15} + \frac{21^2}{15}}} = 2.10$$

$$df: v = \frac{\left(\frac{s_1^2}{m} + \frac{s_2^2}{n}\right)^2}{\frac{(s_1/m)^2}{m-1} + \frac{(s_2/n)^2}{n-1}} = 25$$

$$\text{Tail area} = 0.0229$$

$$P\text{-value} = 1 - \text{tail area} = 0.0229$$

The evidence shows that cola has a higher compression strength if one chooses to use a significance level  $\alpha > 0.0229$ .

The necessary assumptions are that the compression strength of both types of drink are normally distributed.



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Q3: Ex 38 b, c; Pg 509

b) No, it is necessary to have the sample standard deviations as well.

$$c) s_p^2 = \frac{m-1}{m+n-2} s_1^2 + \frac{n-1}{m+n-2} s_2^2$$

$$= \frac{15-1}{15+19-2} 19.5^2 + \frac{19-1}{15+19-2} 15.3^2 = 299.24$$

$$t = \frac{\bar{x} - \bar{y} - (m_1 - m_2)}{\sqrt{s_p^2 \left( \frac{1}{m} + \frac{1}{n} \right)}} = \frac{30.47 - 26.53}{\sqrt{299.24 \left( \frac{1}{15} + \frac{1}{19} \right)}} = 0.659$$

$$H_0 = \mu_1 - \mu_2 = 0$$

$$H_a = \mu_1 - \mu_2 > 0$$

$$\text{tail area} = 0.742 \text{ using } df = m + n - 2$$

$$P = 1 - 0.742 = 0.257$$

The evidence does not allow us to reject the null hypothesis, which states that there is no difference between the time consumers look at the products, unless a significance of  $> 0.257$  is acceptable.



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Q4: Ex 42 b, c pg 517

b)  $\bar{d} = 167.21$

$s_d = 228.21$

$$t = \frac{\bar{d} - \Delta_0}{s_d / \sqrt{n}} = \frac{167.21 - 0}{228.21 / \sqrt{14}} = 2.74$$

tail area = 0.9916

for 2 tailed t test ( $H_a: \mu_0 \neq \Delta_0$ )

$P = 2(1 - \text{tail area}) = 0.0168$

the P value indicates the null hypothesis could be rejected at  $\alpha = 0.05$  but not at  $\alpha = 0.01$ .

c) incorrect method

$$t = \frac{\bar{d} - \Delta_0}{\sqrt{\frac{s_1^2}{n} + \frac{s_2^2}{n}}} = \frac{167.21 - 0}{\sqrt{\frac{351.97^2}{14} + \frac{234.44^2}{14}}} = 1.48$$

$P = 2(1 - \text{tail area}) = 0.163$

If the procedure was used incorrectly we'd fail to reject null hypothesis when maybe we should have.



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Q5: Ex 54, Pg 525

$$\hat{p}_1 = \frac{104}{207} = 0.5024$$

$$\hat{p}_2 = \frac{109}{213} = 0.517$$

$$\begin{aligned} \hat{p} &= \frac{m}{m+n} \hat{p}_1 + \frac{n}{m+n} \hat{p}_2 = \frac{207}{207+213} \cdot \frac{104}{207} + \frac{213}{207+213} \cdot \frac{109}{213} \\ &= 0.507 \end{aligned}$$

$$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}(1-\hat{p})\left(\frac{1}{m} + \frac{1}{n}\right)}} = \frac{0.502 - 0.517}{\sqrt{0.507(1-0.507)\left(\frac{1}{207} + \frac{1}{213}\right)}} = -0.191$$

$$H_a: p_1 - p_2 < 0 \quad z = -0.191$$

$$P = \Phi(z) = 0.424$$

The null hypothesis cannot be rejected at a significance level  $\alpha = 0.10$ . The data does not support the researcher's hypothesis at this significance level.