

Eksperimental Fysik 2 - Øvelse 2

The Michelson-Morley Interferometer

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Introduction

In this experiment we construct the Mach-Zender interferometer and use this setup to examine two distinct scenarios. In the first part we look at the effects of polarizing one of the beams. In the second part we examine the interference pattern as one of the beams passes is passed through a gas with varying pressure.

Theory

Waveplate and Polarization

We shall use the following notation to describe \hat{p} and \hat{s} -polarized waves, where these vectors describe orthogonal planes of polarization. The waves have frequency ω and phase ρ

$$\mathbf{E}_1 = \|E_1\| \hat{p} \cos(\omega t - \rho), \quad \mathbf{E}_2 = \|E_2\| \hat{s} \cos(\omega t - \rho).$$

and clearly,

$$\hat{p} \cdot \hat{p} = 1, \quad \hat{s} \cdot \hat{s} = 1, \quad \hat{s} \cdot \hat{p} = 0.$$

We can define the angle θ , to describe waves polarized somewhere in between \hat{p} and \hat{s} .

$$\mathbf{E} = \|E\| (\hat{p} \cos \theta + \hat{s} \sin \theta).$$

We are now interested in measuring the interference pattern two waves, where one wave is held fixed at $\theta = 0$ (\hat{p} -polarized) and the other wave is allowed to vary in θ . We assume that the waves have equal amplitude E . They need not however be in phase. We will denote their phases ρ_1, ρ_2 . The intensity of this wave is, as always, given by,

$$\begin{aligned} I &= c\epsilon_0 (\mathbf{E}_1 + \mathbf{E}_2)^2 \\ &= E^2 (\hat{p} \cdot \hat{p}) \cos^2(\omega t - \rho_1) + E^2 (\cos \theta \hat{p} + \sin \theta \hat{s})^2 \cos^2(\omega t - \rho_2) \\ &\quad + 2E^2 \hat{p} \cdot (\cos \theta \hat{p} + \sin \theta \hat{s}) \cos(\omega t - \rho_1) \cos(\omega t - \rho_2) \\ &= E^2 \cos^2(\omega t - \rho_1) + E^2 \cos^2(\omega t - \rho_2) \\ &\quad + 2E^2 \cos \theta \cos(\omega t - \rho_1) \cos(\omega t - \rho_2). \end{aligned}$$

We will only be able to measure the time-average of this intensity. The time average of a periodic function is given by the following function,

$$\langle f \rangle = \frac{1}{\tau} \int_0^\tau f d\tau.$$

Before continuing, we notice that the first 2 terms, both integrate to π over one cycle,

$$\begin{aligned} \langle I \rangle &= E^2 c\epsilon_0 \frac{1}{2\pi} \left(2\pi + \cos \theta \int_0^{2\pi} \cos(\omega t - \rho_1) \cos(\omega t - \rho_2) d(\omega t) \right) \\ &= E^2 c\epsilon_0 (1 + \cos \theta \cos(\Delta\rho)) \end{aligned}$$

Which gives us our main result. The amplitude of the interference should vary sinusoidally in θ .

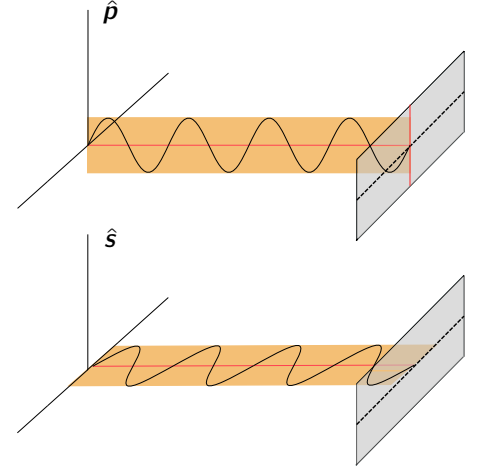


Figure 1: The two orthogonal polarizations of light; \hat{s} and \hat{p}

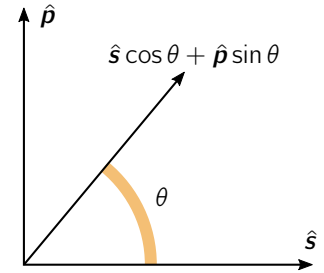


Figure 2: Light may also be polarized somewhere between \hat{s} and \hat{p} . We can describe these polarizations with an angle θ .

Waveplate

In the experiment we make use of a $\lambda/2$ -waveplate. This is a tool that allows us to rotate the polarization. The waveplate can be set to an angle θ_W , as the light passes through the plate, what happens can be visualized as the light being mirrored in a plane lying at θ_W . Fig 3 illustrates this. In practice, this functions as doubling the polarization angle. So,

$$\theta = 2\theta_W.$$

Combining this, with our knowledge from the previous section, we expect the amplitude of the interference pattern to vary in the following way,

$$A(\theta_W) = k \cos(2\theta_W + \rho).$$

Where k, ρ are constants.