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$$[(E)_{-1+V_{k+1}} + (H)_{-1+V_{k+1}} + (I)_{-1+V_{k+1}} + (0)_{-1+V_{k+1}}] \frac{1}{4} = (H)_{-1+V_{k+1}}$$

$$[(0)_{-1+V_{k+1}} + (0)_{-1+V_{k+1}} + (0)_{-1+V_{k+1}} + (0)_{-1+V_{k+1}}] \frac{1}{4} = (H)_{-1+V_{k+1}}$$

$$1 = (H)_{-1+V_{k+1}}$$

	↑		
←	A	B	C ✓
	D ✓	E	F
	G ✓	H	I ✓

0	1	1
1	1	1
0	1	0

Step 1:

	$V_k(0)$	$V_{k+1}(5)$
A	0	-1
B	0	-1
D	0	-1
E	0	-1
F	0	-1
H	0	-1

$$S = (LEFT, A)_{-1+V_k}$$

$$S = (RIGHT, A)_{-1+V_k}$$

$$S = (UP, A)_{-1+V_k}$$

$$S = (DOWN, A)_{-1+V_k}$$

$$S = (LEFT, B)_{-1+V_k}$$

$$S = (RIGHT, B)_{-1+V_k}$$

$$S = (UP, B)_{-1+V_k}$$

$$S = (DOWN, B)_{-1+V_k}$$

$$1. V_{k+1}(A) = \frac{1}{4} [(-1 + V_{k+1}(A)) + (-1 + V_{k+1}(B)) + (-1 + V_{k+1}(D)) + (-1 + V_{k+1}(H))]$$

$$V_{k+1}(A) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$V_{k+1}(A) = -1$$

$$2. V_{k+1}(B) = \frac{1}{4} [(-1 + V_{k+1}(A)) + (-1 + V_{k+1}(C)) + (-1 + V_{k+1}(E)) + (-1 + V_{k+1}(H))]$$

$$V_{k+1}(B) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$V_{k+1}(B) = -1$$

$$3. V_{k+1}(D) = \frac{1}{4} [(-1 + V_{k+1}(A)) + (-1 + V_{k+1}(E)) + (-1 + V_{k+1}(G)) + (-1 + V_{k+1}(H))]$$

$$V_{k+1}(D) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$V_{k+1}(D) = -1$$

$$4. V_{k+1}(E) = \frac{1}{4} [(-1 + V_{k+1}(D)) + (-1 + V_{k+1}(F)) + (-1 + V_{k+1}(H)) + (-1 + V_{k+1}(B))]$$

$$V_{k+1}(E) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$V_{k+1}(E) = -1$$

$$5. V_{k+1}(F) = \frac{1}{4} [(-1 + V_{k+1}(E)) + (-1 + V_{k+1}(G)) + (-1 + V_{k+1}(I)) + (-1 + V_{k+1}(C))]$$

$$V_{k+1}(F) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$V_{k+1}(F) = -1$$

$$6. V_{k+1}(F) = -1$$

$$6. V_{k+1}(H) = \frac{1}{4} [(-1 + V_{k+1}(G)) + (-1 + V_{k+1}(I)) + (-1 + V_{k+1}(H)) + (-1 + V_{k+1}(E))] \\ V_{k+1}(H) = \frac{1}{4} [(-1+0) + (-1+0) + (-1+0) + (-1+0)] \\ V_{k+1}(H) = -1$$

$$\begin{array}{|c|c|c|} \hline \swarrow & & \uparrow \\ \hline \searrow & & \swarrow \\ \hline \end{array}$$

A	B	C
D	E	F
G	H	I

7.

-1	-1	0
-1	-1	-1
0	-1	0

$V_{k+1}(Z)$	$V_k(Z)$	
-1	0	A
-1	0	B
-1	0	C
-1	0	D
-1	0	E
-1	0	F
-1	0	G

$$8. q_{k+1}(A, \text{LEFT}) = -2$$

$$9. q_{k+1}(A, \text{RIGHT}) = -2$$

$$10. q_{k+1}(A, \text{UP}) = -2$$

$$11. q_{k+1}(A, \text{DOWN}) = -2$$

$$12. \pi_{k+1}(A) = \{ \text{LEFT, RIGHT, UP, DOWN} \}$$

$$13. q_{k+1}(B, \text{LEFT}) = -2$$

$$14. q_{k+1}(B, \text{RIGHT}) = -1$$

$$15. q_{k+1}(B, \text{UP}) = -2 \quad [(-1+1) + (-1+1) + (-1+1) + (-1+1)] \frac{1}{4} = (A)_{k+1} V$$

$$16. q_{k+1}(B, \text{DOWN}) = -2 \quad [(0+1) + (0+1) + (0+1) + (0+1)] \frac{1}{4} = (A)_{k+1} V$$

$$17. \pi_{k+1}(B) = \{ \text{LEFT, RIGHT, UP, DOWN} \} \quad 1- = (A)_{k+1} V$$

$$18. q_{k+1}(D, \text{LEFT}) = -2 \quad [(-1+1) + (-1+1) + (-1+1) + (-1+1)] \frac{1}{4} = (B)_{k+1} V$$

$$19. q_{k+1}(D, \text{RIGHT}) = -2 \quad [(0+1) + (0+1) + (0+1) + (0+1)] \frac{1}{4} = (B)_{k+1} V$$

$$20. q_{k+1}(D, \text{UP}) = -2 \quad 1- = (B)_{k+1} V$$

$$21. q_{k+1}(D, \text{DOWN}) = -2 \quad [(-1+1) + (-1+1) + (-1+1) + (-1+1)] \frac{1}{4} = (D)_{k+1} V$$

$$22. \pi_{k+1}(D) = \{ \text{LEFT, RIGHT, UP, DOWN} \} \quad 1- = (D)_{k+1} V$$

$$23. q_{k+1}(E, \text{LEFT}) = -2 \quad 1- = (D)_{k+1} V$$

$$24. q_{k+1}(E, \text{RIGHT}) = -2 \quad [(-1+1) + (-1+1) + (-1+1) + (-1+1)] \frac{1}{4} = (E)_{k+1} V$$

$$25. q_{k+1}(E, \text{UP}) = -2 \quad [(0+1) + (0+1) + (0+1) + (0+1)] \frac{1}{4} = (E)_{k+1} V$$

$$26. q_{k+1}(E, \text{DOWN}) = -2 \quad 1- = (E)_{k+1} V$$

$$27. \pi_{k+1}(E) = \{ \text{LEFT, RIGHT, UP, DOWN} \} \quad 1- = (E)_{k+1} V$$

$$28. q_{k+1}(F, \text{LEFT}) = -2 \quad [(0+1) + (0+1) + (0+1) + (0+1)] \frac{1}{4} = (F)_{k+1} V$$

$$29. q_{k+1}(F, \text{RIGHT}) = -2 \quad 1- = (F)_{k+1} V$$

$$30. q_{k+1}(F, \text{UP}) = -1$$

$$31. q_{k+1}(F, \text{DOWN}) = -1$$

$$32. \pi_{k+1}(F) = \{ \text{UP, DOWN} \}$$

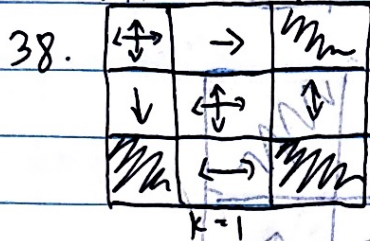
$$33. q_{k+1}(H, LEFT) = -1$$

$$34. q_{k+1}(H, RIGHT) = -1$$

$$35. q_{k+1}(H, UP) = -2$$

$$36. q_{k+1}(H, DOWN) = -2$$

$$37. \pi_{k+1}(H) = \{LEFT, RIGHT\}$$



$$39. V_*(A) = \frac{1}{4} [(-1 + V_{k+2}(A)) + (-1 + V_{k+2}(B)) + (-1 + V_{k+2}(C)) + (-1 + V_{k+2}(D))]$$

$$V_*(A) = \frac{1}{4} [(-1 + -1) + (-1 + -1) + (-1 + -1) + (-1 + -1)]$$

$$V_*(A) = -2$$

$$40. V_*(B) = \frac{1}{4} [(-1 + V_{k+2}(A)) + (-1 + V_{k+2}(C)) + (-1 + V_{k+2}(E)) + (-1 + V_{k+2}(D))]$$

$$V_*(B) = \frac{1}{4} [(-1 + -1) + (-1 + 0) + (-1 + -1) + (-1 + -2)]$$

$$V_*(B) = -1.75$$

$$41. V_*(D) = \frac{1}{4} [(-1 + V_{k+2}(D)) + (-1 + V_{k+2}(E)) + (-1 + V_{k+2}(G)) + (-1 + V_{k+2}(A))]$$

$$V_*(D) = \frac{1}{4} [(-1 + -1) + (-1 + -1) + (-1 + 0) + (-1 + -1)]$$

$$V_*(D) = -1.75$$

$$42. V_*(E) = \frac{1}{4} [(-1 + V_{k+2}(D)) + (-1 + V_{k+2}(F)) + (-1 + V_{k+2}(H)) + (-1 + V_{k+2}(B))]$$

$$V_*(E) = \frac{1}{4} [(-1 + -1) + (-1 + -1) + (-1 + -1) + (-1 + -1)]$$

$$V_*(E) = -2$$

$$43. V_*(F) = \frac{1}{4} [(-1 + V_{k+2}(E)) + (-1 + V_{k+2}(F)) + (-1 + V_{k+2}(I)) + (-1 + V_{k+2}(C))]$$

$$V_*(F) = \frac{1}{4} [(-1 + -1) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$V_*(F) = -1.5$$

$$44. V_*(H) = \frac{1}{4} [(-1 + V_{k+2}(G)) + (-1 + V_{k+2}(I)) + (-1 + V_{k+2}(H)) + (-1 + V_{k+2}(E))]$$

$$V_*(H) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + -1) + (-1 + -1)]$$

$$45. q_{k+2}(A, LEFT) = -4$$

$$q_{k+2}(A, RIGHT) = -3.75$$

$$q_{k+2}(A, UP) = -4$$

$$q_{k+2}(A, DOWN) = -3.75$$

$$\pi_{k+2}(A) = \{RIGHT, DOWN\}$$

46. $q_{k+2}(B, \text{LEFT}) = -3.75$
 $q_{k+2}(B, \text{RIGHT}) = -1.75$
 $q_{k+2}(B, \text{UP}) = -3.5$
 $q_{k+2}(B, \text{DOWN}) = -3.75$
 $\pi_{k+2}(B) = \{\text{RIGHT}\}$

57.

-2	-1.75	
-1.75	-2	-1.5
	1.5	

47. $q_{k+2}(D, \text{LEFT}) = -3.5$
 $q_{k+2}(D, \text{RIGHT}) = -3.75$
 $q_{k+2}(D, \text{UP}) = -3.75$
 $q_{k+2}(D, \text{DOWN}) = -1.75$
 $\pi_{k+2}(D) = \{\text{DOWN}\}$

58.

48. $q_{k+2}(E, \text{LEFT}) = -3.75$
 $q_{k+2}(E, \text{RIGHT}) = -3.5$
 $q_{k+2}(E, \text{UP}) = -3.75$
 $q_{k+2}(E, \text{DOWN}) = -3.5$
 $\pi_{k+2}(E) = \{\text{RIGHT, DOWN}\}$

49. $q_{k+2}(F, \text{LEFT}) = -3.5$
 $q_{k+2}(F, \text{RIGHT}) = -3$
 $q_{k+2}(F, \text{UP}) = -1.5$
 $q_{k+2}(F, \text{DOWN}) = -1.5$
 $\pi_{k+2}(F) = \{\text{UP, DOWN}\}$

50. $q_{k+2}(H, \text{LEFT}) = -1.5$

$q_{k+2}(H, \text{RIGHT}) = -1.5$
 $q_{k+2}(H, \text{UP}) = -3.5$
 $q_{k+2}(H, \text{DOWN}) = -3$

$\pi_{k+2}(H) = \{\text{LEFT, RIGHT}\}$

51. $\pi_*(A) = \{\text{RIGHT, DOWN}\}$

52. $\pi_*(B) = \{\text{RIGHT}\}$

53. $\pi_*(D) = \{\text{DOWN}\}$

54. $\pi_*(E) = \{\text{RIGHT, DOWN}\}$

55. $\pi_*(F) = \{\text{UP, DOWN}\}$

56. $\pi_*(H) = \{\text{LEFT, RIGHT}\}$