```
# This cell is used for creating a button that hides/unhides code
cells to quickly look only the results.
# Works only with Jupyter Notebooks.
from IPython.display import HTML
HTML('''<script>
code show=true;
function code toggle() {
if (code show){
$('div.input').hide();
} else {
$('div.input').show();
code show = !code show
$( document ).ready(code_toggle);
</script>
<form action="javascript:code toggle()"><input type="submit"</pre>
value="Click here to toggle on/off the raw code."></form>''')
<IPython.core.display.HTML object>
# Description:
   Exercise4 notebook.
# Copyright (C) 2018 Santiago Cortes, Juha Ylioinas
# This software is distributed under the GNU General Public
# Licence (version 2 or later); please refer to the file
# Licence.txt, included with the software, for details.
# Preparations
import os
from PIL import Image
from scipy.io import loadmat
import numpy as np
import matplotlib.pyplot as plt
import cv2
from itertools import compress
from scipy.ndimage import maximum filter
from scipy.ndimage import map coordinates
from scipy.ndimage import convolveld as conv1
from scipy.ndimage import convolve as conv2
from skimage.io import imread
from skimage.transform import ProjectiveTransform,
SimilarityTransform, AffineTransform
from skimage.measure import ransac
```

```
from utils import gaussian2, maxinterp, circle points
import time
# Select data directory
if os.path.isdir('/coursedata'):
    # JupyterHub
    course data dir = '/coursedata'
elif os.path.isdir('../../coursedata'):
    # Local installation
    course_data_dir = '../../coursedata'
else:
    # Docker
    course_data_dir = '/home/jovyan/work/coursedata/'
print('The data directory is %s' % course data dir)
data_dir = os.path.join(course_data_dir, 'exercise-04-data/')
print('Data stored in %s' % data dir)
The data directory is /coursedata
Data stored in /coursedata/exercise-04-data/
```

# CS-E4850 Computer Vision Exercise Round 4

The problems should be solved before the exercise session and solutions returned via MyCourses. Upload to MyCourses both: this Jupyter Notebook (.ipynb) file containing your solutions to the programming tasks and the exported pdf version of this Notebook file. If there are both programming and pen & paper tasks kindly combine the two pdf files (your scanned/LaTeX solutions and the exported Notebook) into a single pdf and submit that with the Notebook (.ipynb) file. Note that (1) you are not supposed to change anything in the utils.py and (2) you should be sure that everything that you need to implement should work with the pictures specified by the assignments of this exercise round.

NOTE: In order to avoid errors caused by running the cells in mixed order (which quite often happens while trying different things and debugging), while working on a particular cell be sure that you have freshly run all its preceding cells belonging to the same exercise.

Fill your name and student number below.

Name: Alberto Dian

Student number: 102383146

## Exercise 1 - Matching Harris corner points

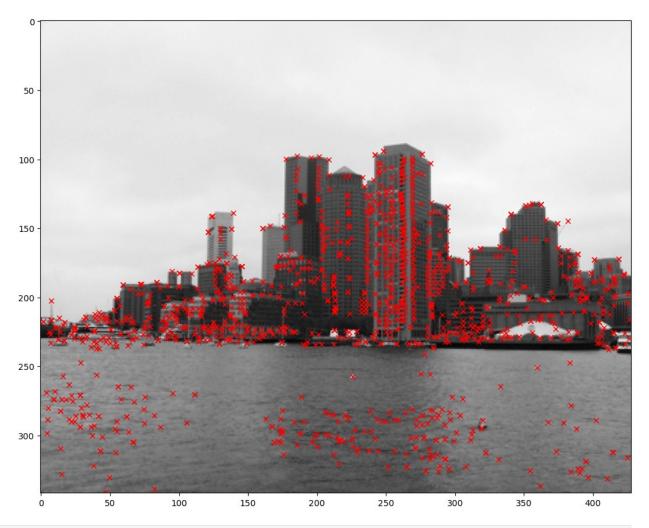
In this exercise, you will familiarize yourself with the method of Harris interest point detection. The aim is to first detect Harris corners from two images of the same scene. Then, image

patches of size 15x15 pixels around each detected corner point is extracted following a matching step where mutually nearest neighbors are found using the sum of squared differences (SSD) similarity measure. The SSD measure for two image patches, f and g, is defined as follows

so that the larger the SSD value the more dissimilar the patches are. Do the task (a) below and answer questions in (b):

```
## The first part uses OpenCV computer vision library to
## extract Harris corner points
## (source: https://docs.opencv.org/3.0-beta/doc/py tutorials/
## py feature2d/py features harris/py features harris.html)
I1 = imread(data dir+'Boston1.png');
R1 = cv2.cornerHarris(I1,2,3,0.04)
# Take only the local maxima of the corner response function
fp = np.ones((3,3))
fp[1,1] = 0
maxNR1 = maximum filter(R1, footprint=fp, mode='constant')
# Test if cornerness is larger than neighborhood
cornerI1 = R1>maxNR1
# Threshold for low value maxima
maxCV1 = np.amax(R1)
# Find centroids
ret, labels, stats, centroids =
cv2.connectedComponentsWithStats(np.uint8((R1>0.0001*maxCV1)*cornerI1)
# Define the criteria to stop and refine the corners
criteria = (cv2.TERM CRITERIA EPS + cv2.TERM CRITERIA MAX ITER, 100,
0.001)
corners = cv2.cornerSubPix(I1,np.float32(centroids),(5,5),(-1,-1),
criteria)
kp1=corners.T
# Display Harris keypoints
plt.figure(figsize=(20,10))
plt.imshow(I1, cmap='gray')
plt.plot([kp1[0]],[kp1[1]],'rx')
plt.suptitle("Harris Corners using OpenCV", fontsize=20)
plt.show()
```

## Harris Corners using OpenCV



```
## The previous part illustrated OpenCV's built-in capabilities.
## Let's try to do Harris corner extraction and matching using our own
## implementation in a less black-box manner.

## Familiarize yourself with the harris function
def harris(im, sigma=1.0, relTh=0.0001, k=0.04):
    im = im.astype(float) # Make sure im is float

# Get smoothing and derivative filters
g, _, _, _, _, _, = gaussian2(sigma)
    _, gx, gy, _, _, _, = gaussian2(np.sqrt(0.5))

# Partial derivatives
Ix = conv2(im, -gx, mode='constant')
Iy = conv2(im, -gy, mode='constant')
```

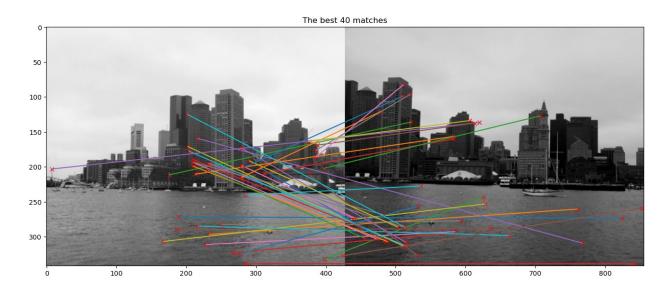
```
# Components of the second moment matrix
    Ix2Sm = conv2(Ix**2, g, mode='constant')
    Iy2Sm = conv2(Iy**2, g, mode='constant')
    IxIySm = conv2(Ix*Iy, q, mode='constant')
    # Determinant and trace for calculating the corner response
    detC = (Ix2Sm*Iy2Sm) - (IxIySm**2)
    traceC = Ix2Sm+Iy2Sm
    # Corner response function R
    # "Corner": R > 0
    # "Edge": R < 0
    # "Flat": |R| = small
    R = detC-k*traceC**2
    maxCornerValue = np.amax(R)
    # Take only the local maxima of the corner response function
    fp = np.ones((3,3))
    fp[1,1] = 0
    maxImg = maximum filter(R, footprint=fp, mode='constant')
    # Test if cornerness is larger than neighborhood
    cornerImg = R>maxImg
    # Threshold for low value maxima
    y, x = np.nonzero((R>relTh*maxCornerValue)*cornerImg)
    # Convert to float
    x = x.astype(float)
    y = y.astype(float)
    # Remove responses from image borders to reduce false corner
detections
    r, c = R.shape
    idx = np.nonzero((x<2)+(x>c-3)+(y<2)+(y>r-3))[0]
    x = np.delete(x,idx)
    y = np.delete(y,idx)
    # Parabolic interpolation
    for i in range(len(x)):
         ,dx=maxinterp((R[int(y[i]), int(x[i])-1], R[int(y[i]),
int(x[i])], R[int(y[i]), int(x[i])+1]))
         _,dy=maxinterp((R[int(y[i])-1, int(x[i])], R[int(y[i]),
int(x[i])], R[int(y[i])+1, int(x[i])]))
        x[i]=x[i]+dx
        y[i]=y[i]+dy
    return x, y, cornerImg
```

```
# Load images
I1 = imread(data dir+'Boston1.png')/255.
I2 = imread(data dir+'Boston2m.png')/255.
# Harris corner extraction, take a look at the source code above
x1, y1, cimg1 = harris(I1)
x2, y2, cimg2 = harris(I2)
## We pre-allocate the memory for the 15*15 image patches extracted
## around each corner point from both images
patch size=15
npts1=x1.shape[0]
npts2=x2.shape[0]
patches1=np.zeros((patch_size, patch_size, npts1))
patches2=np.zeros((patch size, patch size, npts2))
## The following part extracts the patches using bilinear
interpolation
k=(patch size-1)/2.
xv,yv=np.meshgrid(np.arange(-k,k+1),np.arange(-k,k+1))
for i in range(npts1):
    patch = map coordinates(I1, (yv + y1[i], xv + x1[i]))
    patches1[:,:,i] = patch
for i in range(npts2):
    patch = map_coordinates(I2, (yv + y2[i], xv + x2[i]))
    patches2[:,:,i] = patch
## We compute the sum of squared differences (SSD) of pixels'
intensities
## for all pairs of patches extracted from the two images
distmat = np.zeros((npts1, npts2))
for il in range(npts1):
    for i2 in range(npts2):
        distmat[i1,i2]=np.sum((patches1[:,:,i1]-patches2[:,:,i2])**2)
## Next we compute pairs of patches that are mutually nearest
neighbors
## according to the SSD measure
ss1 = np.amin(distmat, axis=1)
ids1 = np.argmin(distmat, axis=1)
ss2 = np.amin(distmat, axis=0)
ids2 = np.argmin(distmat, axis=0)
pairs = []
for k in range(npts1):
    if k == ids2[ids1[k]]:
        pairs.append(np.array([k, ids1[k], ss1[k]]))
pairs = np.array(pairs)
## We sort the mutually nearest neighbors based on the SSD
```

```
sorted ssd = np.sort(pairs[:,2], axis=0)
id ssd = np.argsort(pairs[:,2], axis=0)
## Estimate the geometric transformation between images
src=[]
dst=[]
for k in range(len(id_ssd)):
    l = id ssd[k]
    src.append([x1[int(pairs[l, 0])], y1[int(pairs[l, 0])]])
    dst.append([x2[int(pairs[l, 1])], y2[int(pairs[l, 1])]])
src=np.array(src)
dst=np.array(dst)
rthrs=2
tform, = ransac((src, dst), ProjectiveTransform, min_samples=4,
                               residual threshold=rthrs,
max trials=1000)
H1to2p = tform.params
## Next we visualize the 40 best matches which are mutual nearest
neiahbors
## and have the smallest SSD values
Nvis = 40
montage = np.concatenate((I1, I2), axis=1)
plt.figure(figsize=(16, 8))
plt.suptitle("The best 40 matches according to SSD measure",
fontsize=20)
plt.imshow(montage, cmap='gray')
plt.title('The best 40 matches')
for k in range(np.minimum(len(id ssd), Nvis)):
    l = id ssd[k]
    plt.plot(x1[int(pairs[l, 0])], y1[int(pairs[l, 0])], 'rx')
    plt.plot(x2[int(pairs[l, 1])] + I1.shape[1], y2[int(pairs[l, 1])],
'rx')
    plt.plot([x1[int(pairs[l, 0])], x2[int(pairs[l, 1])]+I1.shape[1]],
         [v1[int(pairs[l, 0])], v2[int(pairs[l, 1])]])
## Finally, since we have estimated the planar projective
transformation
## we can check that how many of the nearest neighbor matches actually
## are correct correspondences
p1to2=np.dot(H1to2p, np.hstack((src, np.ones((src.shape[0],1)))).T)
p1to2 = p1to2[:2,:] / p1to2[2,:]
p1to2 = p1to2.T
pdiff=np.sqrt(np.sum((dst-p1to2)**2, axis=1))
# The criterion for the match being a correct is that its
correspondence in
# the second image should be at most rthrs=2 pixels away from the
```

```
transformed
# location
n_correct = len(pdiff[pdiff<rthrs])
print("{} correct matches.".format(n_correct))
67 correct matches.</pre>
```

The best 40 matches according to SSD measure



# a) Matching points using normalized cross-correlation (NCC)

Implement the matching of mutually nearest neighbors using normalized cross-correlation (NCC) as the similarity measure instead of SSD.

For two image patches of similar size it can be written as follows (also given in the slide 83 of

Lecture 2): 
$$NCC(f,g) = \frac{\sum\limits_{k,l} \big(g(k,l) - \acute{g}\big) \big(f(k,l) - \acute{f}\big)}{\sqrt{\sum\limits_{k,l} \big(g(k,l) - \acute{g}\big)^2 \sum\limits_{k,l} \big(f(k,l) - \acute{f}\big)^2}}$$
 where  $\acute{g}$  and  $\acute{f}$  are the mean intensity

values of patches g and f. The values of NCC are always between -1 and 1, and the larger the value the more similar the patches are.

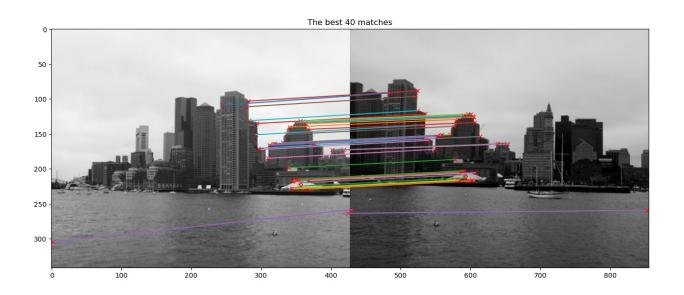
```
# Now, your task is to do matching in similar manner but using
normalised
## cross-correlation (NCC) instead of SSD. You should also report the
## number of correct correspondences for NCC as shown above for SSD.
##
## HINT: Compared to the previous SDD-based implementation, all you
need
## to do is to modify the lines performing the 'distmat' calculation
## from SSD to NCC.
```

```
## Thereafter, you can proceed as above but notice the following
details:
## You need to determine the mutually nearest neighbors by
## finding pairs for which NCC is maximized (i.e. not minimized like
SSD).
## Also, you need to sort the matches in descending order in terms of
NCC
## in order to find the best matches (i.e. not ascending order as with
SSD).
# Measure pairwise distances NCC
##-vour-code-starts-here-##
# Load images
I1 = imread(data dir+'Boston1.png')/255.
I2 = imread(data dir+'Boston2m.png')/255.
# Harris corner extraction, take a look at the source code above
x1, y1, cimg1 = harris(I1)
x2, y2, cimg2 = harris(I2)
## We pre-allocate the memory for the 15*15 image patches extracted
## around each corner point from both images
patch size=15
npts1=x1.shape[0]
npts2=x2.shape[0]
patches1=np.zeros((patch_size, patch_size, npts1))
patches2=np.zeros((patch size, patch size, npts2))
## The following part extracts the patches using bilinear
interpolation
k=(patch size-1)/2.
xv,yv=np.meshgrid(np.arange(-k,k+1),np.arange(-k,k+1))
for i in range(npts1):
    patch = map coordinates(I1, (yv + y1[i], xv + x1[i]))
    patches1[:,:,i] = patch
for i in range(npts2):
    patch = map coordinates(I2, (yv + y2[i], xv + x2[i]))
    patches2[:,:,i] = patch
## NCC
distmat = np.zeros((npts1, npts2))
for il in range(npts1):
    for i2 in range(npts2):
        distmat[i1,i2] = np.sum((patches1[:,:,i1]-
np.mean(patches1[:,:,i1]))*(patches2[:,:,i2]-
np.mean(patches2[:,:,i2])))/np.sqrt(np.sum(((patches1[:,:,i1]-
np.mean(patches1[:,:,i1]))**2))*np.sum((patches2[:,:,i2]-
```

```
np.mean(patches2[:,:,i2]))**2))
## Next we compute pairs of patches that are mutually nearest
neighbors
## according to the NCC measure
ss1 = np.amax(distmat, axis=1)
ids1 = np.argmax(distmat, axis=1)
ss2 = np.amax(distmat, axis=0)
ids2 = np.argmax(distmat, axis=0)
pairs = []
for k in range(npts1):
    if k == ids2[ids1[k]]:
        pairs.append(np.array([k, ids1[k], ss1[k]]))
pairs = np.array(pairs)
## We sort the mutually nearest neighbors based on the NCC
sorted ncc = np.sort(pairs[:,2], axis=0)[::-1]
id ncc = np.argsort(pairs[:,2], axis=0)[::-1]
## Estimate the geometric transformation between images
src=[]
dst=[]
for k in range(len(id ncc)):
    l = id ncc[k]
    src.append([x1[int(pairs[l, 0])], y1[int(pairs[l, 0])]])
    dst.append([x2[int(pairs[l, 1])], y2[int(pairs[l, 1])]])
src=np.array(src)
dst=np.array(dst)
rthrs=2
tform, = ransac((src, dst), ProjectiveTransform, min samples=4,
                               residual threshold=rthrs,
max trials=1000)
H1to2p = tform.params
## Next we visualize the 40 best matches which are mutual nearest
neighbors
## and have the biggest NCC values
Nvis = 40
montage = np.concatenate((I1, I2), axis=1)
plt.figure(figsize=(16, 8))
plt.suptitle("The best 40 matches according to NCC measure",
fontsize=20)
plt.imshow(montage, cmap='gray')
plt.title('The best 40 matches')
for k in range(np.minimum(len(id ncc), Nvis)):
    l = id ncc[k]
    plt.plot(x1[int(pairs[l, 0])], y1[int(pairs[l, 0])], 'rx')
    plt.plot(x2[int(pairs[l, 1])] + I1.shape[1], y2[int(pairs[l, 1])],
```

```
'rx')
   plt.plot([x1[int(pairs[l, 0])], x2[int(pairs[l, 1])]+I1.shape[1]],
         [y1[int(pairs[l, 0])], y2[int(pairs[l, 1])]])
## Finally, since we have estimated the planar projective
transformation
## we can check that how many of the nearest neighbor matches actually
## are correct correspondences
plto2=np.dot(H1to2p, np.hstack((src, np.ones((src.shape[0],1)))).T)
p1to2 = p1to2[:2,:] / p1to2[2,:]
p1to2 = p1to2.T
pdiff=np.sqrt(np.sum((dst-p1to2)**2, axis=1))
# The criterion for the match being a correct is that its
correspondence in
# the second image should be at most rthrs=2 pixels away from the
transformed
# location
n correct = len(pdiff[pdiff<rthrs])</pre>
print("{} correct matches.".format(n_correct))
##-vour-code-ends-here-##
293 correct matches.
```

The best 40 matches according to NCC measure



## b) Answer the questions below

1) How many correct correspondences do you get by using NCC instead of SSD? 2) Which one of the two similarity measures performs better in this case and why?

Type your answers here: 1) 67 correct matches using SSD vs 293 correct matches using NCC 2) In this case NCC performs better because it normalizes pixels value using mean and variance, ensuring the comparison to be more robust to local variations.

# Exercise 2 - Matching SURF regions

SURF (Speeded up robust features) is quite similar to SIFT which was presented in Lecture 3. In this implementation the descriptor vectors for the local regions have 64 elements (instead of 128 in SIFT) but Euclidean distance can still be used as a similarity measure in descriptor space. See the comments in the source code and do the following tasks:

- a) Sort the given nearest neighbor matches in ascending order based on the nearest neighbor distance ratio (NNDR), which is defined in Equation 4.18 in the course book (7.18 in the 2nd edition). Report the number of correct correspondences among the top 5 matches based on NNDR and compare it to the case where ordering is based on nearest neighbor distance.
- b) Answer some questions (see them below...)

```
## The first part uses OpenCV computer vision and scikit's image
processing
## libraries.
## SURF regions are extracted and matched and a similarity
transformation
## (i.e. rotation, translation and scale) between the views is
estimated
img1 = np.array(Image.open(data dir+'boat1.png'))
img2 = np.array(Image.open(data dir+'boat6.png'))
# Initiate SURF detector
surf = cv2.xfeatures2d.SURF create()
# Find the keypoints and descriptors with SURF detector
kp1, desc1 = surf.detectAndCompute(img1, None)
kp2, desc2 = surf.detectAndCompute(img2, None)
kps1 = np.array([p.pt for p in kp1])
kps2 = np.array([p.pt for p in kp2])
kps1_rad = np.array([p.size / 2 for p in kp1]) #rad==scale
kps2_rad = np.array([p.size / 2 for p in kp2])
## Sift should work this year -> Code below should not be needed.
##
## You may use the lines below if you do not have opency compiled with
opency-contrib
## (surf and sift are only part of that as they are patented)
```

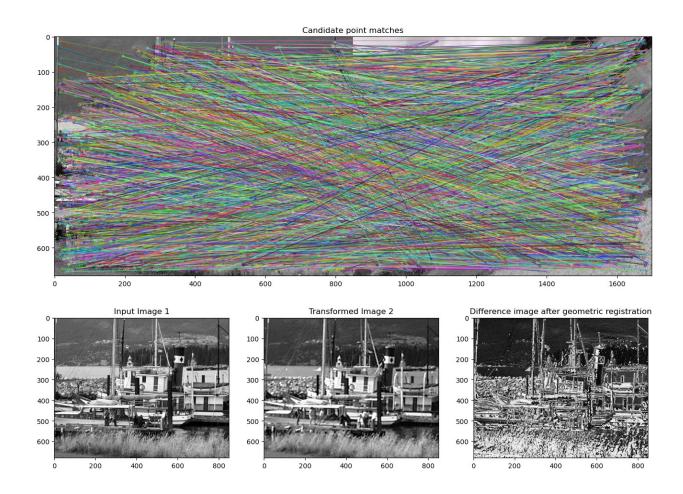
```
## Precomputed features and descriptors
## Using a trick to circumvent a bug in the new version of np.load
## save np.load
#np load old = np.load
# modify the default parameters of np.load
#np.load = lambda *a,**k: np load old(*a, allow pickle=True, **k)
# call load data with allow pickle implicitly set to true
#data1=np.load(data dir+"img1 surf kps descs.npy", encoding='latin1')
#data2=np.load(data_dir+"img2_surf_kps_descs.npy", encoding='latin1')
## restore np.load for future normal usage
#np.load = np load old
#kps1 = data1.item().get('keypoints')
#kps1 rad = data1.item().get('keypoint rads')
#desc1 = data1.item().get('descriptors')
#kps2 = data2.item().get('keypoints')
#kps2 rad = data2.item().get('keypoint rads')
#desc2 = data2.item().get('descriptors')
#kp1 = []
\#kp2 = []
#for i in range(kps1.shape[0]):
    p=cv2.KeyPoint()
   p.pt = (kps1[i,0], kps1[i,1]) \# coordinates of the keaypoints
#
    p.size = kps1 rad[i] * 2 # diameter of the blob feature
     kpl.append(p)
#for i in range(kps2.shape[0]):
   p=cv2.KeyPoint()
   p.pt = (kps2[i,0], kps2[i,1])
   p.size = kps2 \ rad[i] * 2
    kp2.append(p)
# Initiate BruteForce matcher with default params
bf = cv2.BFMatcher()
# Perform matching and save k=1 nearest neighbors for each descriptor
matches = bf.knnMatch(desc1, desc2, k=1)
# The candidate point matches can be visualized as follows:
img3 = cv2.drawMatchesKnn(img1,kp1,img2,kp2,matches,None,flags=2)
plt.figure(figsize=(16,8))
plt.suptitle('Feature matching using SURF', fontsize=20)
```

```
plt.imshow(img3)
plt.title('Candidate point matches')
plt.show()
## The estimation of geometric transformations is covered later in
lectures
## but it can be done as follows using scikit-image Python library:
# Collect feature points and scales from the match objects
source pts = []
target_pts = []
for match in matches:
    # Collect feature point coords and scale query (img1)
    x, y = kp1[match[0].queryIdx].pt
    source pts.append(np.array([x, y]))
    # Collect feature point coords and scale query (img2)
    x, y = kp2[match[0].trainIdx].pt
    target pts.append(np.array([x, y]))
source pts = np.array(source pts)
target pts = np.array(target pts)
## Estimate the geometric transformation between images
rthrs=10
tform, inliers = ransac((source pts, target pts), SimilarityTransform,
min samples=2,
                               residual threshold=rthrs,
max trials=1000)
H1to2p = tform.params
s in = source pts[inliers,:]
t in = target pts[inliers,:]
source pts aug = np.hstack((s in,np.ones((s in.shape[0],1))))
target pts aug = np.hstack((t in,np.ones((t in.shape[0],1))))
target = np.dot(H1to2p, source pts aug.T)
target = target [:2,:] / target [2,:]
target = target .T
xv, yv = np.meshgrid(np.arange(0,img1.shape[1]),
np.arange(0,img1.shape[0]))
src all = np.vstack((xv.flatten(), yv.flatten(), np.ones((1,
xv.size))))
target all = np.dot(H1to2p, src all)
target all = target all[:2,:] / target all[2,:]
xvt = target all [0,:].reshape(xv.shape[0], xv.shape[1])
yvt = target all [1,:].reshape(yv.shape[0], yv.shape[1])
img2t = map coordinates(img2, (yvt, xvt))
```

```
fig, axes = plt.subplots(nrows=1, ncols=3, figsize=(16,8))
ax = axes.ravel()
ax[0].imshow(img1, cmap='gray')
ax[0].set_title("Input Image 1")
ax[1].imshow(img2t, cmap='gray')
ax[1].set_title("Transformed Image 2")
ax[2].imshow(np.abs(img1-img2t), cmap='gray')
ax[2].set_title("Difference image after geometric registration")

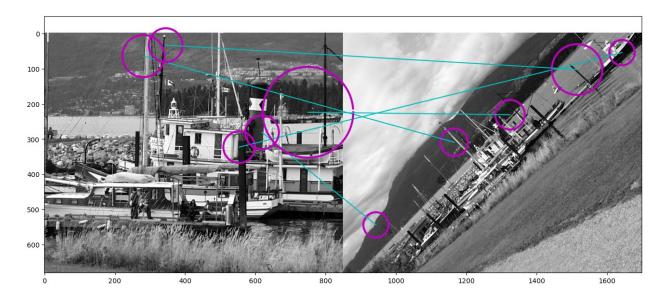
matches_in = list(compress(matches, inliers))
img3 = cv2.drawMatchesKnn(img1,kp1,img2,kp2,matches_in,None,flags=2)
plt.figure(figsize=(16,8))
plt.imshow(img3)
plt.title("Matched inlier points")
plt.show()
```

### Feature matching using SURF



```
## The previous part illustrated OpenCV's built-in brute force
matcher.
## Let's do the nearest neighbor matching for feature vectors in desc1
and desc2
## by using our own implementation.
## We compute the pairwise distances of feature vectors to matrix
'distmat'
## you can use the for-loop version or faster vectorized version
#distmat = np.zeros((desc1.shape[0], desc2.shape[0]))
#for i in range(desc1.shape[0]):
     for j in range(desc2.shape[0]):
         distmat[i, j] = np.linalg.norm(desc1[i,:] - desc2[j,:])
## Vectorized version: sqrt(xTx + yTy - 2xTy)
distmat = np.dot(desc1, desc2.T)
X terms = np.expand dims(np.diag(np.dot(desc1, desc1.T)), axis=1)
X terms = np.tile(X terms,(1,desc2.shape[0]))
Y terms = np.expand dims(np.diag(np.dot(desc2, desc2.T)), axis=0)
Y terms = np.tile(Y terms, (desc1.shape[0],1))
distmat = np.sqrt(Y_terms + X_terms - 2*distmat)
## We determine the mutually nearest neighbors
dist1 = np.amin(distmat, axis=1)
ids1 = np.argmin(distmat, axis=1)
dist2 = np.amin(distmat, axis=0)
ids2 = np.argmin(distmat, axis=0)
pairs = []
for k in range(ids1.size):
    if k == ids2[ids1[k]]:
        pairs.append(np.array([k, ids1[k], dist1[k]]))
```

```
pairs = np.array(pairs)
# We sort the mutually nearest neighbors based on the distance
snnd = np.sort(pairs[:,2], axis=0)
id_nnd = np.argsort(pairs[:,2], axis=0)
# We visualize the 5 best matches
Nvis = 5
plt.figure(figsize=(16, 8))
plt.suptitle("Top 5 mutual nearest neigbors of SURF features",
fontsize=20)
plt.imshow(np.hstack((img1, img2)), cmap='gray')
t = np.arange(0, 2*np.pi, 0.1)
# Display matches
for k in range(Nvis):
    pid1 = pairs[id nnd[k], 0]
    pid2 = pairs[id nnd[k], 1]
    loc1 = kps1[int(pid1)]
    r1 = 6*kps1 rad[int(pid1)]
    loc2 = kps2[int(pid2)]
    r2 = 6*kps2 rad[int(pid2)]
    plt.plot(loc1[0]+r1*np.cos(t), loc1[1]+r1*np.sin(t), 'm-',
linewidth=3)
    plt.plot(loc2[\frac{0}{2}]+r2*np.cos(t)+img1.shape[\frac{1}{2}], loc2[\frac{1}{2}]+r2*np.sin(t),
'm-', linewidth=3)
    plt.plot([loc1[0], loc2[0]+img1.shape[1]], [loc1[1], loc2[1]],
'c-')
# How many of the top 5 matches appear to be correct correspondences?
```

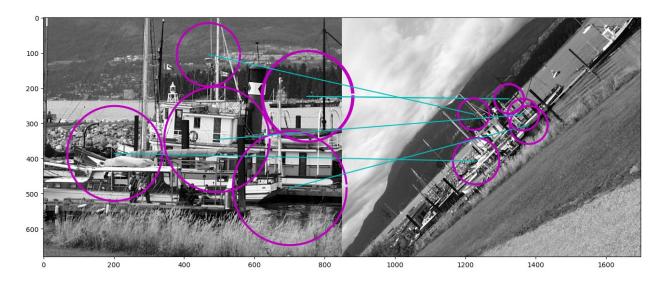


# a) Sorting matches according to the nearest neighbor distance ratio (NNDR)

```
## Now, your task is to compute and visualize the top 5 matches based
## the nearest neighbor distance ratio defined in Equation (4.18) in
the course book.
## How many of those are correct correspondences?
##-your-code-starts-here-##
## Vectorized version: sqrt(xTx + yTy - 2xTy)
distmat = np.dot(desc1, desc2.T)
X_terms = np.expand_dims(np.diag(np.dot(desc1, desc1.T)), axis=1)
X \text{ terms} = \text{np.tile}(X \text{ terms}, (1, \text{desc2.shape}[0]))
Y terms = np.expand dims(np.diag(np.dot(desc2, desc2.T)), axis=0)
Y terms = np.tile(Y terms, (desc1.shape[0],1))
distmat = np.sqrt(Y terms + X terms - 2*distmat)
## We determine the mutually nearest neighbors
nnd = np.sort(distmat, axis=1)
id_distmat = np.argsort(distmat, axis=1)
## Ratio of the nearest and second nearest neighbor distances
nndr list = nnd[:, 0] / nnd[:, 1]
pairs = []
for i in range(len(nndr list)):
    pairs.append(np.array([i, id distmat[i][0], nndr list[i]]))
pairs = np.array(pairs)
```

```
# We sort the mutually nearest neighbors based on the distance
nndr = np.sort(pairs[:, 2], axis=0)
id nndr = np.argsort(pairs[:, 2], axis=0)
# We visualize the 5 best matches
Nvis = 6
plt.figure(figsize=(16, 8))
plt.suptitle("Top 5 Nearest Neighbor Distance Ratio of NNRD features",
fontsize=20)
plt.imshow(np.hstack((img1, img2)), cmap='gray')
t = np.arange(0, 2 * np.pi, 0.1)
# Display matches
for k in range(Nvis):
    pid1 = pairs[id_nndr[k], 0]
    pid2 = pairs[id nndr[k], 1]
    loc1 = kps1[int(pid1)]
    r1 = 6*kps1 rad[int(pid1)]
    loc2 = kps2[int(pid2)]
    r2 = 6*kps2 rad[int(pid2)]
    plt.plot(loc1[0]+r1*np.cos(t), loc1[1]+r1*np.sin(t), 'm-',
linewidth=3)
    plt.plot(loc2[0]+r2*np.cos(t)+img1.shape[1], loc2[1]+r2*np.sin(t),
'm-', linewidth=3)
    plt.plot([loc1[0], loc2[0]+img1.shape[1]], [loc1[1], loc2[1]],
'c-')
##-your-code-ends-here-##
```

Top 5 Nearest Neighbor Distance Ratio of NNRD features



## b) Answer the questions below

1) What are the benefits of using SURF regions instead of Harris corners? 2) Why the matching approach of Exercise 1 (i.e. Harris corners and NCC based matching) would not work for the example images of Exercise 2? 3) In what kind of cases Harris corners may still be better than SURF and why?

Type your answers here: 1) First of all, SURF is optimized for speed while Harris can be computionally expensive. Secondly, SURF is invariant to scale and rotation compared to Harris that it isn't. To conclude, SURF not only detects keypoints but also computes feature descriptors that are robust to various transformations.

2) Because the two images are rotated and scaled with respect to each other, and Harris corners is not scale and rotation invariant. 3) If we are searching for matching points between two simple and planar scenes without scale or rotation, because the extra computation by SURF will not be needed and Harris technique will obtain a good result.

# Exercise 3 - Scale-space blob detection

The python lines below illustrate pre-computed blob detections obtained with a similar procedure as implemented in SIFT and described below. Here the task is to replace the pre-computed regions with regions computed by your own implementation. The result does not need to be exactly the same as the pre-computed one but similar. In summary, implement the scale-space blob detector as follows: a) Generate a Laplacian of Gaussian filter (you can set  $\sigma = 0.5$ ). b) Build a Laplacian scale space, starting with some initial scale and going for n iterations:

- filter image with scale-normalized Laplacian at current scale
- save square of Laplacian response for current level of scale space
- increase scale by factor k

c) Perform non-maximum suppression in scale space. d) Display resulting circles at their characteristic scales. Apply the blob detector to example images boat1.png and boat6.png as shown in the example script. Can you identify some corresponding regions? Note 1: Suitable values for k and n could be k = 1.19 and n = 18. Note 2: This task corresponds to Exercise 4.1 in the course book. A similar assignment has been used by Lazebnik at UIUC and their course page gives also more detailed instructions: http://slazebni.cs.illinois.edu/spring16/assignment2.html.

```
# Load images
imq1 = np.array(Image.open(data_dir+'boat1.png'))
img2 = np.array(Image.open(data_dir+'boat6.png'))
# Initiate SIFT detector
sift = cv2.SIFT create()
# Find the keypoints and descriptors with SIFT detector
kp1, desc1 = sift.detectAndCompute(img1, None)
kp2, desc2 = sift.detectAndCompute(img2, None)
## Sift should work this year. -> Code below should not be needed.
##
## The same song here as in the previous exercise, no sift and surf if
you dont compile
## with opency-contrib, sorry. :L
## Using the same trick to circumvent a bug in the new version of
np.load
## save np.load
#np load old = np.load
# modify the default parameters of np.load
#np.load = lambda *a,**k: np load old(*a, allow pickle=True, **k)
# call load data with allow pickle implicitly set to true
#data1=np.load(data_dir+"boat1_sift_kps_descs.npy", encoding='latin1')
#data2=np.load(data_dir+"boat6 sift kps descs.npy", encoding='latin1')
## restore np.load for future normal usage
#np.load = np load old
#kps1 = data1.item().get('keypoints')
#kps1 rad = data1.item().get('keypoint rads')
#desc1 = data1.item().get('descriptors')
#kps2 = data2.item().get('keypoints')
#kps2 rad = data2.item().get('keypoint rads')
#desc2 = data2.item().get('descriptors')
#kp1 = []
\#kp2 = []
```

```
#for i in range(kps1.shape[0]):
    p=cv2.KevPoint()
#
    p.pt = (kps1[i,0], kps1[i,1])
#
     p.size = kps1 \ rad[i] * 2
     kp1.append(p)
#for i in range(kps2.shape[0]):
    p=cv2.KeyPoint()
   p.pt = (kps2[i,0], kps2[i,1])
    p.size = kps2 \ rad[i] * 2
#
    kp2.append(p)
# Initiate BruteForce matcher with default params
bf = cv2.BFMatcher()
# Perform matching and save k=2 nearest neighbors for each descriptor
matches = bf.knnMatch(desc1, desc2, k=2)
# Apply Lowe's ratio test
good matches = []
for m,n in matches:
    if m.distance < 0.75*n.distance:
        good matches.append(m)
# Sort matches
good matches = sorted(good matches, key = lambda x:x.distance)
# Collect feature points and scales from the match objects
source pts = []
target pts = []
source radii = []
target radii = []
for match in good matches:
    # Collect feature point coords and scale query (img1)
    x, y = kp1[match.queryIdx].pt
    pt = np.array([np.round(x), np.round(y)]).astype(int)
    source pts.append(pt)
    radius = kp1[match.queryIdx].size / 2.
    source radii.append(radius)
    # Collect feature point coords and scale query (img2)
    x, y = kp2[match.trainIdx].pt
    pt = np.array([np.round(x), np.round(y)]).astype(int)
    target pts.append(pt)
    radius = kp2[match.trainIdx].size / 2.
    target radii.append(radius)
source pts = np.array(source pts)
source radii = np.array(source radii)
```

```
target pts = np.array(target pts)
target radii = np.array(target radii)
## Estimate the geometric transformation between images
rthrs=10
tform, = ransac((source pts, target pts), SimilarityTransform,
min samples=2,
                                 residual threshold=rthrs,
max trials=1000)
H1to2p = tform.params
s = np.sqrt(np.linalg.det(H1to2p[0:2,0:2]));
R = H1to2p[0:2,0:2] / s;
t = H1to2p[0:2,2];
# Plot
montage = np.concatenate((img1, img2), axis=1)
Nvis = 20
plt.figure(figsize=(16, 8))
plt.suptitle("Matching points using SIFT", fontsize=20)
plt.imshow(montage, cmap='gray')
plt.title('The best {} matches'.format(Nvis))
for k in range(0, Nvis):
    plt.plot([source pts[k,0], target pts[k,0]+img1.shape[1]],\
              [source pts[k,1], target pts[k,1]], 'r-')
    x,y=circle points(source pts[k,\frac{0}{0}], source pts[k,\frac{1}{1}],\
                       3*np.sqrt(2)*source radii[k])
    plt.plot(x, y, 'r', linewidth=1.5)
    x,y=circle points(target pts[k,\frac{0}{2})+img1.shape[\frac{1}{2}], target pts[k,\frac{1}{2}],\
                       3*np.sqrt(2)*target radii[k])
    plt.plot(x, y, 'r', linewidth=1.5)
```

### Matching points using SIFT



```
def scaleSpaceBlobs(img, N):
    start = time.time()
                     # The first sigma to start with
    sigma0 = 0.5
    k = 1.19
    Nscales = 18
                     # Number of scales in scalespace (noticable
effect on execution time, you can try different values)
    # Pre-allocate memory for the scale space, sigmas and filtered
images
    scalespace = np.zeros((img.shape[0], img.shape[1], Nscales))
    sigmas = np.zeros(Nscales)
    tmpxx = np.zeros(img.shape)
    tmpyy = np.zeros(img.shape)
    # Create a scalespace by...
    print("Creating a scalespace...")
    for i in range(Nscales):
        # Get the current sigma and generate gaussian filters
        sigmas[i] = (k ** i) * sigma0
        g,_,gxx,gyy,_, = gaussian2(sigmas[i])
        # filter the image with the scale-normalized Laplacian of
Gaussian
        # for each scale i and store the result to the variable
scalespace[:,:,i]
        ##-your-code-starts-here-##
        tmpxx = conv2(img, gxx, mode='constant')
```

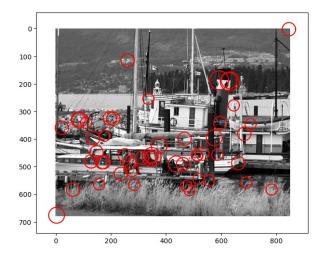
```
tmpyy = conv2(img, gyy, mode='constant')
        ##-vour-code-ends-here-##
        scalespace[:,:,i] = (sigmas[i]**2 * (tmpxx + tmpyy))**2
    # Selection of local maxima, each maxima defines a circular
region.
    print("Calculating local maxima...")
    # Pre-allocate memory for the local maxima images
    localmaxima = np.zeros(scalespace.shape)
    # Filter shape for calculating the local maxima
    footprint = np.ones((3,3))
    footprint[1,1] = 0
    for i in range(Nscales):
        # Calculate local maxima
        maxi = maximum filter(scalespace[:,:,i], footprint=footprint,
mode='constant')
        # test if pixel values are larger than neighborhood
        localmaxima[:,:,i] = scalespace[:,:,i] > maxi
    # In the end each row in 'blobs' encodes one circular region as
follows:.
    # [x, y, r, filter response]
    # where x and y are the column and row coordinates of the circle
center,
    # r is the radius of the circle, r=sqrt(2)*sigma (see slide 77 of
Lecture 3)
    # last column indicates the response of the Laplacian of Gaussian
filter
    blobs = None
    # Pre-allocate memory for consecutive scales
    scaleA = np.zeros(img.shape)
    scaleB = np.zeros(img.shape)
    scaleC = np.zeros(img.shape)
    print("Calculating detections...")
    for i in range(1,Nscales-1):
        # Consecutive scales
        scaleA = scalespace[:,:,i-1]
        scaleB = scalespace[:,:,i]
        scaleC = scalespace[:,:,i+1]
        # Indices of local maxima
        ri, ci = np.nonzero(localmaxima[:,:,i])
        # Compare the current level to the previous and next level
        idmax = np.nonzero((scaleA[ri,ci] < scaleB[ri,ci]) *</pre>
(scaleC[ri,ci] < scaleB[ri,ci]))[0]</pre>
        rlmax = ri[idmax]
```

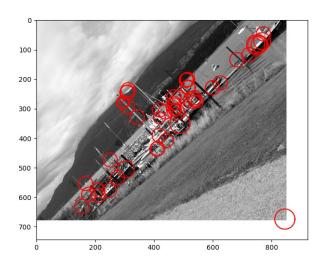
```
clmax = ci[idmax]
        # Add blob coordinates, circle radiuses and filter responses
to 'blobs'
        if blobs is not None:
            tmp = np.vstack((clmax, rlmax,
                      np.sqrt(2)*sigmas[i]*np.ones(len(rlmax)),
                      scaleB[rlmax, clmax])).T
            blobs = np.vstack((blobs, tmp))
        else:
            blobs = np.vstack((clmax, rlmax,
                      np.sqrt(2)*sigmas[i]*np.ones(len(rlmax)),
                      scaleB[rlmax, clmax])).T
    # Sort the blobs according to the response of Laplacian of
Gaussian.
    # Return N best detections.
    ids = np.argsort(blobs[:,3])
    sblobs = np.flipud(blobs[ids, :])
    blobsN = sblobs[0:min(N, sblobs.shape[0]), :]
    # Ouput the execution time
    print("Total time elapsed (s): " + str(time.time() - start) + "\
n")
    return blobsN
# The previous part illustrated OpenCV lib's built-in capabilities.
# Next, the task is to implement a similar blob detector as in SIFT.
# In the example below the detections are pre-computed.
# Since we now know the true geometric transformation H1to2p we can
# visualize those detections from both images which have large
overlap.
# Your task is to implement the function scaleSpaceBlobs.m so that it
# outputs similar circular regions as pre-computed in 'blobs1' and
'blobs2'.
# Replace 'blobs1' and 'blobs2' below with the output of the detector.
#data=np.load(data dir+'blobs data.npz', encoding='latin1')
#blobs1=data['blobs1']
#blobs2=data['blobs2']
# Each row in 'blobs1' and 'blobs2' defines a circular region as
follows:
# [x y r filter response]
# here x and y are the column and row coordinates of the circle center
# r is the radius of the circle, r=sqrt(2)*sigma (see slide 77 of
# last column indicates the response of the Laplacian of Gaussian
filter
# Below N is the number of strongest blobs that are returned.
```

```
# (strongest local maxima for the scale-normalized Laplacian of
Gaussian)
# Implement scaleSpaceBlobs.
# Everything should then work if you uncomment the following three
lines and
# turn on your
N=500:
blobs1 = scaleSpaceBlobs(img1, N)
blobs2 = scaleSpaceBlobs(img2, N)
# Show detected blob features
NVIS=50;
fig, axes = plt.subplots(nrows=1, ncols=2, figsize=(16,8))
plt.suptitle("Showing all detected blobs", fontsize=20)
ax = axes.ravel()
ax[0].imshow(img1, cmap='gray')
ax[1].imshow(img2, cmap='gray')
for k in range(0, NVIS):
    x, y = circle points(blobs1[k,0], blobs1[k,1],
3*np.sqrt(2)*blobs1[k,2])
    ax[0].plot(x, y, 'r', linewidth=1.5)
    x, y = circle points(blobs2[k,0], blobs2[k,1],
3*np.sqrt(2)*blobs2[k,2])
    ax[1].plot(x, y, 'r', linewidth=1.5)
plt.show()
# below we illustrate detected regions with high overlap
xy1to2=s*np.dot(R, blobs1[:,0:2].T)+np.tile(t,(blobs1.shape[0],1)).T
blobs1t=np.hstack((xy1to2.T, s*np.expand dims(blobs1[:,2],axis=1),
np.expand dims(blobs1[:,3], axis=1)))
distmat = np.zeros((blobs1.shape[0], blobs2.shape[0]))
for i in range(blobs1.shape[0]):
    for j in range(blobs2.shape[0]):
        distmat[i,j] = np.linalg.norm(blobs1t[i, 0:3] - blobs2[j,
0:31)
dist = np.amin(distmat, axis=0)
nnids = np.argmin(distmat, axis=0)
sdist = np.sort(dist)
sids = np.argsort(dist)
idlist = np.vstack((nnids[sids], sids, sdist)).T
# Visualize the 20 best matches
Nvis = 10
plt.figure(figsize=(16,8))
plt.suptitle("Blob detection and matching", fontsize=20)
```

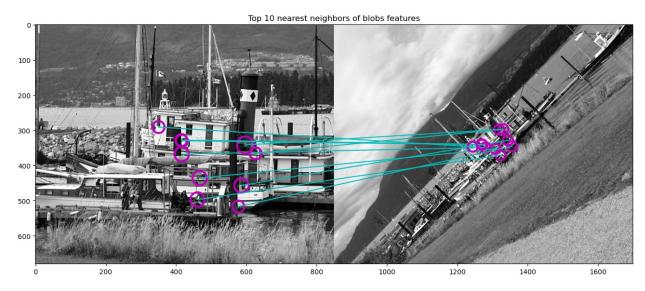
```
montage = np.concatenate((img1, img2), axis=1)
plt.imshow(montage, cmap='gray')
plt.title('Top {} nearest neighbors of blobs features'.format(Nvis))
t = np.arange(0, 2*np.pi+0.1, 0.1)
for k in range(Nvis):
    loc1 = blobs1[int(idlist[k, 0]), 0:2]
    r1 = 3*np.sqrt(2)*blobs1[int(idlist[k,0]), 2]
    loc2 = blobs2[int(idlist[k, 1]), 0:2]
    r2 = 3*np.sqrt(2)*blobs2[int(idlist[k,1]), 2]
    x1 = loc1[0]+r1*np.cos(t)
    y1 = loc1[1]+r1*np.sin(t)
    x2 = loc2[0]+r2*np.cos(t)+img1.shape[1]
    y2 = loc2[1]+r2*np.sin(t)
    plt.plot(x1, y1, 'm-', linewidth=3)
plt.plot(x2, y2, 'm-', linewidth=3)
    plt.plot([loc1[0], loc2[0]+img1.shape[1]],[loc1[1], loc2[1]],
'c-')
Creating a scalespace...
Calculating local maxima...
Calculating detections...
Total time elapsed (s): 57.15005874633789
Creating a scalespace...
Calculating local maxima...
Calculating detections...
Total time elapsed (s): 57.56558012962341
```

#### Showing all detected blobs





### Blob detection and matching



```
## This is just to convince you that the
## vectorized descriptor matching implementation
## illustrated above works correctly
X = np.random.randn(5, 10)
Y = np.random.randn(4, 10)
distmat = np.dot(X,Y.T)
X \text{ terms} = \text{np.expand dims(np.diag(np.dot(X, X.T)), axis=1)}
X \text{ terms} = \text{np.tile}(X \text{ terms}, (1,4))
Y terms = np.expand dims(np.diag(np.dot(Y, Y.T)), axis=0)
Y \text{ terms} = \text{np.tile}(Y \text{ terms}, (5,1))
distmat = np.sqrt(Y terms + X terms - 2*distmat)
print(distmat)
distmat2 = np.zeros((X.shape[0], Y.shape[0]))
for i in range(X.shape[0]):
    for j in range(Y.shape[0]):
        distmat2[i,j] = np.linalg.norm(X[i,:] - Y[j,:])
print(distmat2)
print(np.sum(distmat-distmat2))
[[3.66996523 3.32786774 3.48456468 4.39434007]
 [2.06205597 4.60621587 4.66308076 4.81479029]
 [3.80573201 3.9320217 4.7971086 3.74780005]
 [4.47020221 3.29847223 4.47538203 5.56756563]
 [4.86950253 4.17465633 5.46073414 5.557306 ]]
```

```
[[3.66996523 3.32786774 3.48456468 4.39434007]
[2.06205597 4.60621587 4.66308076 4.81479029]
[3.80573201 3.9320217 4.7971086 3.74780005]
[4.47020221 3.29847223 4.47538203 5.56756563]
[4.86950253 4.17465633 5.46073414 5.557306 ]]
-1.7763568394002505e-15
```