Alberto Franzin, Fabio Palese

Sistemi Intelligenti

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SpamBayes

Introduction

Bayesian networks Definition Naive Bayes

SpamBayes

RESULTS Frame 1

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(B|A)P(A)}{P(B)}$$

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- ► This has led to two different interpretations of the theorem.

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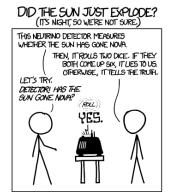
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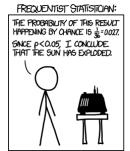
- ▶ P(A|B) is the *a posteriori* probability
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- ▶ P(B|A)P(A) is the *prior* probability
- ► $P(B) = \sum_{a \in A} P(B|A = a)P(A = a)$ is the *total* probability

Frequentists vs. Bayesians



from http://xkcd.com/1132, see also http://en.wikipedia.org/wiki/Sunrise_problem

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The frequentist relies on the theoretical probability of the events.

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The bayesian observes the past events occurred, and adapts the probability accordingly.

WHAT IT IS

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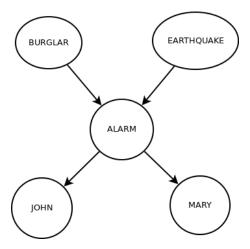
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- ► (Directed) Edges = causal relationship
- ► Two nodes are connected by an edge: the child of an arc is influenced by its ancestor in a probabilistic way

AN EXAMPLE



CONDITIONAL INDEPENDENCE

▶ If

$$P(A|B,C) = P(A|B)$$

then we say that *B* and *C* are *conditionally independent*.

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- ▶ Note that conditional independence \neq independence
- ► Explaining away: if we know that one possible cause of the event has happened, this may explain away the event, being all the other causes less probable once we know the one that happened.

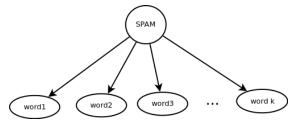
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- ► It is called *naive*, since it's often unrealistic, but it yields good results.
- ► In spam classification:



Python, to use Ply and BeautifulSoup dataset: SpamAssassin archive

FRAME 1