## Algorithms Lab

 $Alberto\ Montes \\ malberto\@student.ethz.ch$ 

January 21, 2017

# Contents

1	Fundamentals			
	1.1	Introduction	3	
	1.2	Binary Search, Sliding Window, Graph Traversals, Greedy	10	
	1.3	CGAL	16	
	1.4	BGL	24	
2	Advanced Algorithms			
	2.1	Dynamic Programming, Brute Force, Split and List	34	
	2.2	BGL Flows	45	
	2.3	Linear/Quadratic Programing	53	
	2.4	Proximity Structures in CGAL	61	
	2.5	Advanced Flows	69	
3	Exa	am Preparation	<b>7</b> 9	

## Chapter 1

## **Fundamentals**

## 1.1 Introduction

## Build the sum

## Keywords-

```
#include <vector>
   #include <iostream>
   using namespace std;
   void do_sum(){
       int n; cin>> n;
       float sum = 0.0;
       float sumant;
       for (int i =0; i < n; i++) {</pre>
            cin >> sumant;
12
            sum += sumant;
13
14
        cout << sum << endl;</pre>
15
   }
16
17
   int main() {
18
       int T; cin >> T;
for (int t=0; t < T; t++){
19
20
            do_sum();
21
        }
   }
23
```

## **Even Pairs**

#### **Keywords**— Precompute

```
#include <vector>
   #include <iostream>
3
4
   using namespace std;
5
   void do_even_count(){
6
        int n; cin >> n;
        vector < int > bits(n);
        for (int i =0; i < n; i++)</pre>
9
             cin >> bits [i];
        // Precompute Si's
        vector<int> partial_sum(n);
        partial_sum[0] = bits[0];
        for (int i = 1; i < n; i++) {</pre>
15
16
             partial_sum[i] = partial_sum[i-1] + bits[i];
18
        vector < int > evens(n), odds(n);
evens[0] = 0; odds[0] = 0;
        if (bits[0] == 0)
             evens[0] = 1;
23
        else
            odds[0] = 1;
24
        for (int i = 1; i < n; i++) {
    evens[i] = evens[i-1];</pre>
26
             odds[i] = odds[i-1];
             if (partial_sum[i] % 2 == 0)
28
29
                  evens[i]++;
             else
                  odds[i]++;
31
32
        // Calculate the result
34
        int counter = 0;
if (bits[0] == 0)
36
37
            counter++;
        for (int i =1; i < n; i++){</pre>
38
             if (partial_sum[i] % 2 == 0)
39
                 counter += evens[i-1] + 1;
40
             else
41
42
                  counter += odds[i-1];
43
44
45
        cout << counter << endl;</pre>
   }
46
47
48
    int main() {
        int T; cin >> T;
49
        for (int t=0; t < T; t++){</pre>
50
             do_even_count();
   }
53
```

## **Dominoes**

## Keywords-

```
#include <vector>
   #include <iostream>
3
4
   using namespace std;
   void compute_dominoes_falling(){
6
        int n; cin >> n;
        vector < unsigned long int > dominoes_height(n);
        for (int i =0; i < n; i++)
9
10
            cin >> dominoes_height[i];
       int max = 1;
12
        for (int i = 0; i < n; i++) {</pre>
14
            if (i + dominoes_height[i] > max)
15
             max = i + dominoes_height[i];
else if (max == i + 1)
16
17
18
                 break;
19
        if (max > n)
            max = n;
        cout << max << endl;</pre>
23
24
   }
25
   int main() {
26
        ios_base::sync_with_stdio(false);
        int T; cin >> T;
for (int t=0; t < T; t++){</pre>
28
29
             compute_dominoes_falling();
30
31
   }
```

#### **Even Matrices**

#### **Keywords**— Precompute

```
#include <vector>
   #include <iostream>
   using namespace std;
6
   // Implementation in O(n^3) time
   void do_even_count_matrices(){
        int n; cin >> n;
9
        vector < vector < int > > M(n, vector < int > (n));
       for (int i = 0; i < n; i++)
  for (int j = 0; j < n; j++)</pre>
                 cin >> M[i][j];
        // Precompute pMi's
15
16
        vector < vector < int > > pM(n+1, vector < int > (n+1));
        for (int i = 0; i <= n; i++) {</pre>
            pM[i][0] = 0;
18
            pM[0][i] = 0;
        for (int i = 1; i <= n; i++) {</pre>
            for (int j = 1; j <= n; j++) {
                 pM[i][j] = pM[i-1][j] + pM[i][j-1] - pM[i-1][j-1] + M[i-1][j-1];
24
            }
26
        }
        int counter = 0;
28
        for (int i1 = 1; i1 <= n; i1++) {</pre>
29
            for (int i2 = i1; i2 <= n; i2++) {</pre>
31
                 \ensuremath{//} We reduce the probelm to one dimension
                                         // Do even pairs on array S
32
                 vector < int > S(n+1);
                                           // pS contains partial sums of S
                 vector < int > pS(n+1);
                 pS[0] = 0;
                 for (int k = 1; k <= n; k++) {</pre>
                     S[k] = pM[i2][k] - pM[i2][k-1] - pM[i1-1][k] + pM[i1-1][k-1];
36
                     pS[k] = pS[k-1] + S[k];
                 // Do even pairs O(n) algorithm on array S
40
                 int onedim_sol = 0;
41
42
                 int even = 0, odd = 0;
                 for (int j = 1; j <=n; j++) {</pre>
43
                     // even = # of partial sums of array (S[1], ..., S[j-1]) that are even.
44
45
                     // odd = # of partial sums of array (S[1], ..., S[j-1]) that are odd.
                     if (pS[j] % 2 == 0){
46
                          onedim_sol += even + 1;
47
48
                          even++;
                     }
50
                     else {
                          onedim_sol += odd;
                          odd++;
                     }
                 }
                 counter += onedim_sol;
            }
56
58
        cout << counter << endl;</pre>
59
   }
61
   int main() {
        ios_base::sync_with_stdio(false);
        int T; cin >> T;
64
        for (int t=0; t < T; t++){</pre>
66
            do_even_count_matrices();
67
   }
```

#### False Coin

#### Keywords— Tree Search

```
#include <vector>
   #include <iostream>
3
   using namespace std;
   void test_false_coin() {
       int n; cin >> n;
8
       vector < int > candidates(n, 0);
       vector < int > lw_coins(n, 0), hw_coins(n, 0);
       int num_trials; cin >> num_trials;
       for (int i = 0; i < num_trials; i++) {</pre>
            int num_per_side; cin >> num_per_side;
            vector<int> left_coins(n, false), right_coins(n, false);
            int left_pos, right_pos;
for (int j = 0; j < num_per_side; j++) {</pre>
18
                cin >> left_pos;
20
                left_coins[left_pos-1] = true;
            }
            for (int j = 0; j < num_per_side; j++) {</pre>
23
                cin >> right_pos;
25
                right_coins[right_pos-1] = true;
28
            char comparison; cin >> comparison;
            // For each trial eliminate all the possible candidates depending where on the balance
30
            // appear
31
            for (int j = 0; j < n; j++) {
                switch (comparison) {
                    case '=': {
                         if (left_coins[j] || right_coins[j])
36
                             candidates[j] = -1;
                         else if (candidates[j] == 0)
38
                             candidates[j] = 1;
39
                         break;
                    }
40
                     case '<': {
41
                         if (left_coins[j]) {
                             lw_coins[j]++;
43
44
                             if (hw_coins[j] > 0) {
                                 candidates[j] = -1;
45
                             } else if (candidates[j] == 0) {
46
                                 candidates[j] = 1;
47
                             }
48
                         } else if (right_coins[j]) {
49
50
                             hw_coins[j]++;
                             if (lw_coins[j] > 0) {
                                  candidates[j] = -1;
                             } else if (candidates[j] == 0) {
                                  candidates[j] = 1;
                             }
                         } else {
                             candidates[j] = -1;
                         }
58
                         break;
60
                    }
                     case '>': {
                        if (right_coins[j]) {
                             lw_coins[j]++;
                             if (hw_coins[j] > 0) {
                                  candidates[j] = -1;
66
                             } else if (candidates[j] == 0) {
                                  candidates[j] = 1;
67
                             7
68
                         } else if (left_coins[j]) {
                             hw_coins[j]++;
                             if (lw_coins[j] > 0) {
                                 candidates[j] = -1;
                             } else if (candidates[j] == 0) {
74
                                  candidates[j] = 1;
                             }
76
                         } else {
                             candidates[j] = -1;
```

```
}
78
                               break;
79
                         }
80
81
                         default: break;
                    }
82
              }
83
84
85
86
          int count_candidates = 0;
          int coin_id = 0;
for (int i = 0; i < n; i++) {
    if (candidates[i] == 1) {</pre>
87
88
89
                    count_candidates++;
90
                    coin_id = i + 1;
91
92
93
          ^{\prime\prime} If there is more than one candidate there is not an unique solution
94
          if (count_candidates > 1) {
95
               coin_id = 0;
96
97
          cout << coin_id << endl;</pre>
98
99
100
     }
     int main() {
102
          ios_base::sync_with_stdio(false);
          int T; cin >> T;
for (int t=0; t < T; t++){</pre>
104
105
               test_false_coin();
106
107
     }
108
```

## Deck of Cards

#### Keywords—Sliding Window

```
#include <vector>
   #include <iostream>
3
   #include <limits>
   #include <stdlib.h>
6
7
   using namespace std;
   // Implementation in O(n)
9
   void deck_of_cards(){
       long n; cin >> n;
       long k; cin >> k;
       vector <long > values(n);
       for (int i = 0; i < n; i++) {
15
16
            cin >> values[i];
18
       long i_r = 0, j_r = 0;
long start = 0, end = 0;
       long sum = values[0];
       long min_value = abs(k-sum);
23
       // Slide a window and keep track of the minimum difference between k and the sum of values
24
       while (start < n) {</pre>
            if (sum <= k) {</pre>
26
                if (end < n-1) {
                     sum += values[++end];
28
                } else { break; }
29
            } else {
                sum -= values[start++];
31
32
            if (abs(k-sum) < min_value) {</pre>
34
                 min_value = abs(k-sum);
                i_r = start;
j_r = end;
36
37
            }
38
39
        cout << i_r << ' ' << j_r << endl;
40
   }
41
42
   int main() {
43
       ios_base::sync_with_stdio(false);
44
45
        int T; cin >> T;
       for (int t=0; t < T; t++){</pre>
46
            deck_of_cards();
47
48
   }
49
```

## 1.2 Binary Search, Sliding Window, Graph Traversals, Greedy

## **Search Snippets**

Keywords—Sliding Window

```
Implementation sliding window.
2
   Hint: to improve the efficiency, instead of loop along all the appearance vector to see if all the
   words appear, keep up a counter and changing it with conditions. It is much more efficient and
       clean
   */
   #include <vector>
6
   #include <iostream>
   #include <algorithm>
   #include <math.h>
9
   #include <limits.h>
   using namespace std;
   struct word {
14
       int id;
16
       int position;
18
   void search_snippets() {
       int n; cin >> n;
       vector < int > m(n);
                                 // total word appearance
       int t = 0;
       for (int i = 0; i < n; i++) {</pre>
           cin >> m[i];
26
            t += m[i];
27
28
       vector<word > w; w.reserve(t);
29
       for (int i = 0; i < n; i++) {</pre>
           for (int j = 0; j < m[i]; j++) {</pre>
                word wo; wo.id = i;
32
                cin >> wo.position;
34
                w.push_back(wo);
35
       }
36
37
       sort(w.begin(), w.end(), [](word a, word b) {
           return a.position < b.position;</pre>
38
40
       vector < int > a(n, 0);
41
       int min_d = w[t-1].position - w[0].position + 1;
42
       int s = 0, e = 0, u = n; // start, end, and uncovered counter
43
       a[w[s].id]++; u--;
45
       // Sliding Window
       while (e != t) {
46
           while (e < t - 1 && u > 0) {
47
                if (a[w[e].id] == 0) u--;
50
                a[w[e].id]++;
           if (u != 0) break;
53
                a[w[s].id]--;
                if (a[w[s].id] == 0) ++u;
            } while (++s != e \&\& u==0);
                                              // Even you go out of the while loop, s will have been
                                              // incresed undiredbly
            min_d = min(min_d, w[e].position - w[s-1].position + 1);
58
59
       cout << min_d << endl;</pre>
61
   }
   int main() {
       ios_base::sync_with_stdio(false);
       int T; cin >> T;
       for (int t=0; t < T; t++){</pre>
67
            search_snippets();
       }
69
   }
```

#### **Boats**

#### **Keywords**— Interval Scheduling

```
Implementation using two fors to iterate
3
4
   Correct
5
   #include <vector>
6
7
   #include <iostream>
   #include <algorithm>
9
   using namespace std;
   void boats() {
       long n; cin >> n;
       vector < pair < long , long > > boats(n);
16
       for (int i = 0; i < n; i++) {</pre>
            cin >> boats[i].second;
            cin >> boats[i].first;
18
        sort(boats.begin(), boats.end(), [](pair<long, long> a, pair<long, long> b) {
            return a.first < b.first;</pre>
23
       });
24
       long current_last_position = boats[0].first;
26
        long number_boats = 1;
        long i = 1;
        while (i < n) {
28
29
            if (current_last_position > boats[i].first) {
                i++;
31
            } else if (boats[i].first - current_last_position > boats[i].second) {
32
                number_boats++;
                current_last_position = boats[i].first;
                i++;
            } else {
                long first_end = boats[i].second + current_last_position;
36
                long min_position = i;
                for (long j = i+1; j < n; j++) {</pre>
                     long end_position;
                     if (boats[j].first - current_last_position > boats[j].second) {
40
                         end_position = boats[j].first;
41
42
                     } else {
                         end_position = current_last_position + boats[j].second;
43
                     }
44
45
                     if (end_position < first_end) {</pre>
                         first_end = end_position;
46
47
                         min_position = j;
48
                     }
                }
50
                number_boats++;
                current_last_position = first_end;
                i = min_position + 1;
            }
       }
        cout << number_boats << endl;</pre>
56
58
59
   int main() {
61
       ios_base::sync_with_stdio(false);
        int T; cin >> T;
        for (int t=0; t < T; t++){</pre>
64
            boats();
        }
66
   }
67
```

## **Moving Books**

#### **Keywords**— Greedy

```
#include <vector>
   #include <set>
   #include <iostream>
   #include <algorithm>
   using namespace std;
   void moving_books() {
9
       long n; cin >> n;
       long m; cin >> m;
       vector < long > s(n), w(m);
       for (int i = 0; i < n; i++) {
            cin >> s[i];
15
16
       for (int i = 0; i < m; i++) {</pre>
18
            cin >> w[i];
       // Check if the heviest box can not be bringed by nobody
       int max_s = *max_element(s.begin(), s.end());
       int max_w = *max_element(w.begin(), w.end());
23
       if (max_w > max_s) {
24
            cout << "impossible\n";</pre>
26
            return;
28
29
       multiset < int , greater < int > > ws;
       sort(s.begin(), s.end(), greater<int>());
31
32
       for (int i = 0; i < m; i++) ws.insert(w[i]);</pre>
       int r = 0;
       while (!ws.empty()) {
34
           r++;
            for (int i = 0; i < n; i++) {</pre>
36
                auto j = ws.lower_bound(s[i]);
                if (j != ws.end()) {
39
                    ws.erase(j);
                } else {
40
                    break;
41
42
43
       }
44
45
       cout << 3*r-1 << endl;
46
   }
47
48
   int main() {
49
50
       ios_base::sync_with_stdio(false);
       int T; cin >> T;
       for (int t=0; t < T; t++){</pre>
            moving_books();
   }
```

#### **Evolution**

Keywords— DFS, Binary Search

```
#include <vector>
       #include <map>
       #include <iostream>
3
       #include <string>
       #include <algorithm>
       #include <unordered_map>
 8
       using namespace std;
9
       // Binary Search
       int binary(int b, vector<int>& path, vector<int>& age) {
                int 1 = 0; int r = path.size()-1;
                while(1 != r){
                         int m = (1+r)/2;
                         if (age[path[m]] > b) 1 = m+1; else r = m;
               return path[1];
18
       }
       \label{localization} \mbox{void dfs(int u, vector<int> } \& \mbox{ tree, vector<int>} \& \mbox{ path, vector<vector<pair<int,int> } > \& \mbox{ tree, vector<int>} \& \mbox{ tree, vector<int>} \& \mbox{ path, vector<vector<int>} & \mbox{ path, vector<int>} &
                query, vector < int > & result, vector < int > & age) {
                // process queries
24
               for (int i = 0; i < query[u].size(); i++) {</pre>
                        result[query[u][i].second] = binary(query[u][i].first,path,age);
26
27
                // continue search
                for (int i = 0; i < tree[u].size(); ++i){</pre>
                         int v = tree[u][i];
30
                         path.push_back(v);
32
                         dfs(v,tree,path,query,result,age);
                path.pop_back();
       }
35
       void evolution() {
38
               int n, q; cin >> n >> q;
40
               // Store the names and respective ages
                unordered_map < string, int > species_to_index;
41
               vector<string> species(n);
42
43
               vector < int > age(n);
               string name;
44
               for (int i = 0; i < n; i++) {</pre>
45
                        cin >> name;
46
                         species_to_index[name] = i;
47
48
                         species[i] = name;
                         cin >> age[i];
49
               // Find root
               int root = max_element(age.begin(), age.end()) - age.begin();
               // Read tree
               vector < vector < int > > tree(n);
                string child, parent;
                for (int i = 0; i < n - 1; i++) {</pre>
58
59
                         cin >> child >> parent;
                         tree[species_to_index[parent]].push_back(species_to_index[child]);
                // Read queries: for each species store a vector of queries consisting of the age b and the
                // index of the query i
64
65
                vector < vector < pair < int , int > > query(n);
               for (int i = 0; i < q; i++) {</pre>
66
67
                         cin >> name;
                         int b; cin >> b;
                         query[species_to_index[name]].push_back(make_pair(b, i));
                // Process queries in one tree transversal
                vector<int> path; path.push_back(root);
                vector<int> result(q);
                dfs(root, tree, path, query, result, age);
```

```
// Output result
77
             for (int i = 0; i < q; i++) {
    cout << species[result[i]];
    if ( i < q - 1 ) cout << " ";</pre>
78
79
80
             }
81
             cout << endl;</pre>
82
      }
83
84
      int main() {
85
            ios_base::sync_with_stdio(false);
int T; cin >> T;
for (int t=0; t < T; t++){</pre>
86
87
88
                    evolution();
89
90
91
     }
```

## Octopussy

#### **Keywords**— Greedy

```
#include <iostream>
   #include <vector>
   #include <queue>
   #include <algorithm>
6
   using namespace std;
   long find_minimum_time(vector<long> &t, long pos) {
9
        if (pos == 0) {
            return t[pos];
       long upper_pos = (pos % 2 == 1) ? (pos - 1) / 2 : (pos - 2) / 2;
       long next_pos = (pos % 2 == 1) ? pos + 1 : pos - 1;
       long min_upper_pos = find_minimum_time(t, upper_pos);
        // Check if the time limit of the pair bomb is more limiting or not.
       if (t[next_pos] <= min_upper_pos - 2) {</pre>
18
            return min(t[pos], min_upper_pos - 1);
19
       } else {
            return min(t[pos], min_upper_pos - 2);
   }
   void octopussy() {
       int n; cin >> n;
27
       vector < long > t(n);
       for (int i = 0; i < n; i++) {</pre>
28
            cin >> t[i];
29
       vector < bool > disarmed(n, false);
       auto cmp = [&t](pair<long, long> left, pair<long, long> right) {
   if ( left.second > right.second ) { return true; }
34
35
            else if ( left.second == right.second ) { return t[left.first] > t[right.first]; }
36
            else { return false; }
38
       priority_queue <pair <long , long > , vector <pair <long , long > > , decltype(cmp) > bombs_queue(cmp);
40
       for (long j = (n-3)/2+1; j < n; j++) {
41
42
            long min_time = find_minimum_time(t, j);
            bombs_queue.push(pair<long, long>(j, min_time));
43
44
45
       long t_time = 0;
46
        while( !bombs_queue.empty() ) {
47
            auto p_bomb = bombs_queue.top();
            bombs_queue.pop();
49
            // The most priority bomb has expired its time...B000M!
            long b_index = p_bomb.first;
            if (t[b_index] <= t_time) { break; }</pre>
            // Marked the bomb as disarmed
            disarmed[b_index] = true;
            t_time++;
            /* Now see if the bomb next to it has been desarmed to let the bomb standing over them to
            enter the priority queue. If not...too late...BOOOOOM!! */
            if (b_index == 0) { continue; } // The bomb at index 0 has no bomb standing over it.
58
            long next_b_index = (b_index % 2 == 1) ? b_index + 1 : b_index - 1;
            if ( disarmed[next_b_index] ) {
                long std_b_index = (b_index % 2 == 1) ? (b_index - 1) / 2 : (b_index - 2) / 2;
                bombs_queue.push(pair < long, long > (std_b_index, find_minimum_time(t, std_b_index)));
            }
        bool all_disarmed = all_of(disarmed.begin(), disarmed.end(), [](bool v){return v;});
        string response = (all_disarmed) ? "yes" : "no";
        cout << response << endl;</pre>
   }
69
   int main() {
       int t; cin >> t;
        for (int i = 0; i < t; i++) {</pre>
            octopussy();
   }
```

## 1.3 CGAL

## Hit

#### **Keywords**— Intersection

```
#include <CGAL/Exact_predicates_exact_constructions_kernel_with_sqrt.h>
2
   #include <iostream>
   typedef CGAL::Exact_predicates_exact_constructions_kernel_with_sqrt K;
   using namespace std;
   void compute_hit(int n) {
       long x, y, a, b;
       cin >> x >> y >> a >> b;
       K::Point_2 xy(x, y), ab(a, b);
14
       K::Ray_2 ray(xy, ab);
       bool hit = false;
16
       for (int i = 0; i < n; i++) {</pre>
            long r, s, t, u;
18
            cin >> r >> s >> t >> u;
19
            if (hit) {
20
                continue;
22
            K::Point_2 rs(r, s), tu(t, u);
K::Segment_2 seg(rs, tu);
25
            if (CGAL::do_intersect(ray, seg)) {
                hit = true;
            }
27
       }
28
        string result = (hit) ? "yes" : "no";
30
        cout << result << endl;</pre>
32
33
   }
35
36
    int main() {
       ios_base::sync_with_stdio(false);
38
       int nb_obstacles; cin >> nb_obstacles;
        while(nb_obstacles > 0) {
40
41
            compute_hit(nb_obstacles);
            cin >> nb_obstacles;
       }
43
       return 0;
44
   }
45
```

#### First Hit

#### **Keywords**— Intersection

```
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
   #include <vector>
   #include <algorithm>
3
   #include <type_traits>
   #include <stdexcept>
   #include <limits>
8
   using namespace std;
   typedef CGAL::Exact_predicates_exact_constructions_kernel
   typedef result_of <K::Intersect_2(K::Ray_2,K::Segment_2)>::type
   // round down to next double
   double floor_to_double(const K::FT& x) {
14
       double a = floor(CGAL::to_double(x));
       while (a > x) a -= 1;
       while (a+1 <= x) a += 1;</pre>
       return a;
18
   }
   // read segment cin; as each coordinate can be represented as a
22
   // long, this is significantly faster than K::Segment_2 s; cin >> s;
   inline K::Segment_2 read_segment() {
23
       long x1, y1, x2, y2;
       cin >> x1 >> y1 >> x2 >> y2;
       return K::Segment_2(K::Point_2(x1,y1), K::Point_2(x2,y2));
   }
28
   // clip/set target of s to o
   void shorten_segment(K::Segment_2& s, const IT& o) {
       if (const K::Point_2* p = boost::get<K::Point_2>(&*o))
31
           s = K::Segment_2(s.source(), *p);
        else if (const K::Segment_2* t = boost::get<K::Segment_2>(&*o))
            // select endpoint of *t closer to s.source()
            if (CGAL::collinear_are_ordered_along_line (s.source(), t->source(), t->target()))
                s = K::Segment_2(s.source(), t->source());
36
            else
38
                s = K::Segment_2(s.source(), t->target());
            throw runtime_error("Strange segment intersection.");
40
41
   }
   void find_hit(size_t n) {
43
       // read input
44
       K::Ray_2 r;
45
46
       cin >> r:
       vector < K :: Segment_2 > segs;
47
       segs.reserve(n):
48
       for (size_t i = 0; i < n; ++i) segs.push_back(read_segment());</pre>
49
       random_shuffle(segs.begin(), segs.end());
50
       // clip the ray at each segment hit (cuts down on the number of
       // intersection points to be constructed: for a uniformly random
       // order of segments, the expected number of constructions is
       // logarithmic in the number of segments that intersect the initial // ray.)
       K::Segment_2 rc(r.source(), r.source());
        // find some segment hit by r
       for (size_t i; i < n; ++i)</pre>
60
            if (CGAL::do_intersect(segs[i], r)) {
                shorten_segment(rc, CGAL::intersection(segs[i], r));
                break:
       if (i == n) { cout << "no\n"; return; }</pre>
66
       // check remaining segments against rc
       while (++i < n)
67
            if (CGAL::do_intersect(segs[i], rc))
68
                shorten_segment(rc, CGAL::intersection(segs[i], r)); // not rc!
        cout << floor_to_double(rc.target().x()) << " " << floor_to_double(rc.target().y()) << "\n";</pre>
   }
73
74
   int main() {
76
       // sanity check
       if (numeric_limits<long>::digits < 51)</pre>
```

```
throw runtime_error("long has <51 bits mantissa");
ios_base::sync_with_stdio(false);
cout << setiosflags(ios::fixed) << setprecision(0);
for (size_t n; cin >> n && n > 0;)
find_hit(n);
return 0;

throw runtime_error("long has <51 bits mantissa");
setprecision(0);
for (size_t n; cin >> n && n > 0;)
find_hit(n);
return 0;
```

Keywords— Triangle Contains, Sliding Window

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
   #include <iostream>
   #include <vector>
3
   #include <algorithm>
   typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
   typedef K::Point_2
   typedef std::vector<P>
                                                                  Pts;
   typedef std::vector<int>
                                                                  Covered;
   typedef std::vector<Covered>
                                                                  Trs;
   typedef Covered::const_iterator
                                                                  Iterator:
   using namespace std;
   // Function to check whether a point is inside a triangle
   inline bool contains(const Pts& t, const P& p) {
       return !CGAL::right_turn(t[0],t[1],p) && !CGAL::right_turn(t[2],t[3],p) && !CGAL::right_turn(t
           [4],t[5],p);
   }
18
19
21
   void hiking_maps() {
       int m, n; cin >> m >> n;
       // Read the path
       Pts path(m);
26
       long x, y;
       for (int i = 0; i < m; i++) {</pre>
           cin >> x >> y;
           path[i] = P(x, y);
       // Read the triangles
32
       Trs triangles(n);
       for (int i = 0; i < n; ++i) {</pre>
35
           Pts t;
           for (std::size_t j = 0; j < 6; ++j) {</pre>
               P p;
                std::cin >> p;
                t.push_back(p);
40
           }
           // Ensure correct order for orientation tests
41
           for (int j = 0; j < 6; j+=2)
42
                if (CGAL::right_turn(t[j],t[j+1],t[(j+2)%6])) std::swap(t[j],t[j+1]);
           // Store which path segments are covered
44
           bool prev = contains(t,path[0]);
45
           for (int j = 1; j < m; ++j) {
46
                if (contains(t,path[j])) {
47
48
                    if (prev) triangles[i].push_back(j-1);
49
                    else prev = true;
               } else
                    prev = false;
           }
       // search for the cover by scanning through the sequence of triangles
       Covered covered(m-1,0); // #times i,i+1 is covered
       int uncovered = m-1; // #uncovered segments (covered[i]==0)
       int best = n; // size of best range so far
58
59
       for (int tb = 0, te = 0; tb != n;) {
            // Ensure covering
           for (; uncovered > 0 && te != n; te++) {
                for (Iterator j = triangles[te].begin(); j != triangles[te].end(); j++)
                    if (++covered[*j] == 1) --uncovered;
65
           if (uncovered != 0) break;
           // Can we remove tb?
67
           do {
                for (Iterator j = triangles[tb].begin(); j != triangles[tb].end(); j++)
                    if (--covered[*j] == 0) uncovered++;
           } while (++tb != te && uncovered == 0);
           best = min(best, te - tb + 1);
       cout << best << endl;</pre>
75
   }
76
```

```
int main() {
    ios_base::sync_with_stdio(false);
    int T; cin >> T;
    for (int t=0; t < T; t++) {
        hiking_maps();
    }
}</pre>
```

#### Antenna

#### Keywords — Minimum Circle

```
#include <CGAL/Exact_predicates_exact_constructions_kernel_with_sqrt.h>
   #include <CGAL/Min_circle_2.h>
3
   #include <CGAL/Min_circle_2_traits_2.h>
   #include <iostream>
   #include <vector>
6
   typedef CGAL::Exact_predicates_exact_constructions_kernel_with_sqrt K;
   typedef CGAL::Min_circle_2_traits_2<K> Traits;
9
   typedef CGAL::Min_circle_2<Traits> Min_circle;
   using namespace std;
   double ceil_to_double(const K::FT& x) {
15
16
       double a = ceil(CGAL::to_double(x));
       while (a+1 >= x) a -= 1;
18
       while (a < x) a += 1;
       return a;
   }
   void compute_antenna_radius(int n) {
       vector < K :: Point_2 > P(n);
23
       long x, y;
24
       for (int i = 0; i < n; i++) {</pre>
26
            cin >> x >> y;
           P[i] = K::Point_2(x, y);
       }
28
29
       Min_circle mc(P.begin(), P.end(), true);
31
       Traits::Circle c = mc.circle();
32
       cout << ceil_to_double(sqrt(c.squared_radius())) << endl;</pre>
   }
34
   int main() {
36
       int nb_population; cin >> nb_population;
       cout << fixed << setprecision(0);</pre>
39
       while(nb_population > 0) {
40
            compute_antenna_radius(nb_population);
41
42
            cin >> nb_population;
43
       return 0;
44
   }
```

#### Attack of the Clones

#### **Keywords**— Interval Scheduling

```
/*
   The algorithm to solve this problem consist in using the Interval Scheduling to place the maximum
   number of jedis along the perimeter. The problem begins when the range is continuouly cyncling so
3
   there is no reference point to start. The best point to use it, is the one with less jedis
       covering it (for the first two testsets there is ensure at least one segment without covering
       and on the last
   testset there is at least one with at most 10 jedis). This segment with minimum jedis covering
   should be found and then apply from there the Interval Scheduling algorithm for all combinations
6
   starting points (none segment is cutting the starting point, or picking each of the segments that
   is cutting the starting point and take the best result).
8
   #include <iostream>
   #include <vector>
   #include <map>
   #include <algorithm>
   #include <climits>
   using namespace std;
18
   void compute_jedis() {
       long N, M; cin >> N >> M;
20
       vector<pair<int, int> > jedis(N);
       // vector < pair < int , int > > nn_jedis , sum_jedis ;
       map<int, int> nn_jedis;
       map<int, int> sum_jedis;
       int a, b;
       for (int i = 0; i < N; i++) {</pre>
28
           cin >> a >> b;
           a--; b--;
                                                             // Re-index to 0-based index
           jedis[i] = make_pair(a, b);
           nn_jedis[a]++;
           if (b < a) nn_jedis[0]++;</pre>
           if (b < M - 1) nn_jedis[b+1]--;</pre>
       }
       // Find the position which no interval overlaps, or the one that less intervals overlap (at
38
       // most 10 by statement)
39
       int prev_sum = 0;
       int min_jedis = INT_MAX, min_jedis_pos = -1;
40
       for (auto nn_jedi : nn_jedis) {
41
           int pos = nn_jedi.first;
           sum_jedis[pos] = prev_sum + nn_jedi.second;
43
           prev_sum += nn_jedi.second;
44
            // cout << pos << "\t" << prev_sum << endl;
45
46
           if (prev_sum < min_jedis) {</pre>
               min_jedis = prev_sum;
47
               min_jedis_pos = pos;
48
           }
49
       // Separate the intervals between the ones that cut k_0 and the ones that not.
       int ai, bi;
       int k0 = min_jedis_pos;
       for (int i = 0; i < N; i++) {</pre>
           a = jedis[i].first;
           b = jedis[i].second;
ai = (a - k0 + M) % M;
58
           bi = (b - k0 + M) \% M;
           if (bi < ai) jedis_cutting.push_back(make_pair(bi, ai));</pre>
63
           else jedis_not_cutting.push_back(make_pair(bi, ai));
65
       // Sort by ending interval position
       sort(jedis_not_cutting.begin(), jedis_not_cutting.end());
67
       // Interval Scheduling for the non-cutting-min position intervals
       int result = 0, lastb = -1;
       for (int i = 0; i < jedis_not_cutting.size(); i++) {</pre>
           if (jedis_not_cutting[i].second > lastb) {
                result++;
74
               lastb = jedis_not_cutting[i].first;
```

```
}
75
76
78
        // Now the same algorithm of Interval Scheduling but for each of the interval that cut the min
        // jedis position
        int result_cutting;
80
        for (int j = 0; j < jedis_cutting.size(); j++) {</pre>
81
             result_cutting = 1;
82
83
             lastb = jedis_cutting[j].first;
             for (int i = 0; i < jedis_not_cutting.size(); i++) {</pre>
                 if (jedis_not_cutting[i].second > lastb && jedis_not_cutting[i].first < jedis_cutting[</pre>
85
                     j].second) {
                     result_cutting++;
86
                     lastb = jedis_not_cutting[i].first;
87
                 }
88
             }
89
90
             result = max(result, result_cutting);
92
93
        cout << result << endl;</pre>
    }
94
95
96
    int main() {
97
        ios_base::sync_with_stdio(false);
98
        int t; cin >> t;
99
100
        for (int i = 0; i < t; i++) {</pre>
             compute_jedis();
        }
103
        return 0;
104
    }
```

## 1.4 BGL

## First Steps BGL

Keywords — Minimum Spanning Tree, Dijkstra Shortest Path

```
// STL includes
   #include <vector>
3
   #include <iostream>
   #include <algorithm>
   #include <climits>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/strong_components.hpp>
9
   #include <boost/graph/dijkstra_shortest_paths.hpp>
   #include <boost/graph/prim_minimum_spanning_tree.hpp>
13
   // Namespaces
   using namespace std;
   using namespace boost;
   \ensuremath{//} Directed graph with integer weights on edges.
   typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_weight_t, int> > Graph;
   typedef graph_traits < Graph > :: vertex_descriptor Vertex;
   typedef graph_traits < Graph > :: edge_descriptor
                                                      Edge;
   typedef graph_traits < Graph > :: edge_iterator
                                                      EdgeIt;
   // Property map edge -> weight
   typedef property_map < Graph , edge_weight_t >: : type
                                                           WeightMap;
   void graphs() {
26
       int n, m;
       cin >> n >> m;
28
29
       // Initialize graph and weightmap
30
31
       Graph G(n);
       WeightMap weightmap = get(edge_weight, G);
       // Store the graph
       for (int i = 0; i < m; i++) {</pre>
36
            int u, v, w;
            cin >> u >> v >> w;
            Edge e; bool success;
38
39
            tie(e, success) = add_edge(v, u, G);
            weightmap[e] = w;
40
41
       // Find the Minimum Spanning Tree with Prim algorithm
43
       vector < int > predmap(n);
44
       Vertex start = 0;
       prim_minimum_spanning_tree(G, make_iterator_property_map(
46
47
            predmap.begin(), get(vertex_index, G)
       ), root_vertex(start));
48
       int w = 0;
49
50
       for (int j = 0; j < n; j++) {
            Edge e; bool success;
            tie(e, success) = edge(j, predmap[j], G);
            if ( success ) {
                w += weightmap[e];
            }
56
58
       // Compute shortest t-u path in G
       vector < int > distmap(n);
       vector < Vertex > predmap_d(n);
       dijkstra_shortest_paths(G, start,
            predecessor_map(make_iterator_property_map(
                predmap_d.begin(), get(vertex_index, G)
            distance_map(make_iterator_property_map(
66
                distmap.begin(), get(vertex_index, G)
       ):
       // Find the furthest vertex
       int max_distance = 0;
       for (int j = 1; j < n; j++) {</pre>
            if (distmap[j] < INT_MAX) {</pre>
74
                max_distance = max(max_distance, distmap[j]);
```

```
}
76
77
           cout << w << " " << max_distance << endl;</pre>
78
79
    }
80
81
    int main() {
82
         ios_base::sync_with_stdio(false);
int T; cin >> T;
for (int t=0; t < T; t++){</pre>
83
84
85
                graphs();
86
          }
87
    }
88
```

Keywords— Minimum Spanning Tree, Dijkstra Shortest Path

```
// STL includes
2
   #include <vector>
3
   #include <iostream>
   #include <algorithm>
   #include <climits>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/strong_components.hpp>
   #include <boost/graph/dijkstra_shortest_paths.hpp>
   #include <boost/graph/prim_minimum_spanning_tree.hpp>
   #include <boost/graph/graph_utility.hpp>
14
   // Namespaces
   using namespace std;
   using namespace boost;
   // Directed graph with integer weights on edges.
18
   typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_weight_t, int> > Graph;
19
   typedef graph_traits<Graph>::vertex_descriptor
                                                          Vertex;
   typedef graph_traits < Graph > :: edge_descriptor
                                                          Edge;
   typedef graph_traits < Graph > :: edge_iterator
                                                          EdgeIt;
   // Property map edge -> weight
23
   typedef property_map < Graph , edge_weight_t >: : type
                                                          WeightMap:
25
   void graphs() {
       int n, e, s, a, b;
28
       cin >> n >> e >> s >> a >> b;
30
       vector < Graph > Gs(s);
31
       vector < WeightMap > weightmaps(s);
       for (int i = 0; i < s; i++) {</pre>
            weightmaps[i] = get(edge_weight, Gs[i]);
       for (int i = 0; i < e; i++) {</pre>
38
            int u, v;
            cin >> u >> v;
40
41
            for (int j = 0; j < s; j++) {
                int w; cin >> w;
                Edge edge_to_add; bool success;
43
                tie(edge_to_add, success) = add_edge(u, v, Gs[j]);
44
                weightmaps[j][edge_to_add] = w;
45
           }
46
       }
47
48
49
       Graph G;
50
       WeightMap weightmap = get(edge_weight, G);
       // For every specie compute the Prim Minimum Spanning Tree and then add the edges into a
           global
       // graph
       for (int i = 0; i < s; i++) {</pre>
            int v; cin >> v;
            vector < Vertex > primpredmap(n);
            prim_minimum_spanning_tree(Gs[i], make_iterator_property_map(primpredmap.begin(), get(
                vertex_index, Gs[i])));
            Edge edge_s; bool success;
            Edge new_edge; bool new_success;
            for (int j = 0; j < n; j++) {
                if (j == primpredmap[j]) { continue; }
                Vertex source = j, target = primpredmap[j];
                tie(edge_s, success) = edge(source, target, Gs[i]);
                int weight = weightmaps[i][edge_s];
66
                tie(new_edge, new_success) = add_edge(j, primpredmap[j], G);
                weightmap[new_edge] = weight;
           }
       // Compute the dijkstra shortest path over the global graph
74
       vector < int > distmap(n);
       vector < Vertex > predmap(n);
```

```
Vertex start = a;
76
77
        Vertex end = b;
78
        {\tt dijkstra\_shortest\_paths(G, start,}
79
            predecessor_map(make_iterator_property_map(
                predmap.begin(), get(vertex_index, G)
80
            )).
81
            distance_map(make_iterator_property_map(
82
                 distmap.begin(), get(vertex_index, G)
83
84
        );
85
86
        cout << distmap[end] << endl;</pre>
87
   }
88
89
90
   int main() {
        ios_base::sync_with_stdio(false);
91
        int T; cin >> T;
92
        for (int t=0; t < T; t++){</pre>
93
            graphs();
94
95
   }
96
```

## Important Bridges

#### **Keywords**— Biconnected Components

```
// STL includes
2
   #include <vector>
3
   #include <iostream>
   #include <algorithm>
   #include <climits>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/strong_components.hpp>
   #include <boost/graph/dijkstra_shortest_paths.hpp>
   #include <boost/graph/prim_minimum_spanning_tree.hpp>
   #include <boost/graph/biconnected_components.hpp>
   // Namespaces
   using namespace std;
   namespace boost
18
     struct edge_component_t
        enum
       { num = 555 };
23
       typedef edge_property_tag kind;
25
     edge_component;
   using namespace boost;
28
30
   // Directed graph with integer weights on edges.
   typedef adjacency_list<vecS, vecS, undirectedS, no_property, property <edge_component_t, size_t> >
        Graph:
   typedef graph_traits < Graph > :: vertex_descriptor
                                                           Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
                                                           Edge;
   typedef graph_traits < Graph > :: edge_iterator
                                                           EdgeIt;
   // // Property map edge -> weight
   // typedef property_map < Graph , edge_weight_t >:: type
                                                           WeightMap;
   void important_bridges() {
40
       int n, m;
41
       cin >> n >> m;
42
       Graph G;
       vector<pair<int, int> > bridges(m), critical_bridges;
for (int i = 0; i < m; i++) {</pre>
44
45
46
            int u, v;
            cin >> u >> v;
47
            bridges[i] = pair<int, int>(u, v);
48
            Edge e; bool success;
49
            tie(e, success) = add_edge(u, v, G);
       property_map < Graph , edge_component_t >: : type
       component = get(edge_component, G);
       size_t num_comps = biconnected_components(G, component);
       // Agrupate all the Edges depending the component ID
58
59
       EdgeIt ei, ei_end;
       vector < vector < Edge > edge_components(num_comps, vector < Edge > (0));
       for (tie(ei, ei_end) = edges(G); ei != ei_end; ++ei) {
            int comp = component[*ei];
            edge_components[comp].push_back(*ei);
64
65
       // Store as result all the edges that are alone at its component
66
67
       for (int i = 0; i < num_comps; i++) {</pre>
            if (edge_components[i].size() > 1) {
                continue:
            Vertex s, t;
            s = source(edge_components[i][0], G);
            t = target(edge_components[i][0], G);
            if (s < t) {
                critical_bridges.push_back(pair<int, int>(s, t));
            } else {
```

```
critical_bridges.push_back(pair<int, int>(t, s));
77
              }
78
         }
79
80
         // Print number of critical bridges
81
         sort(critical_bridges.begin(), critical_bridges.end());
82
         cout << critical_bridges.size() << endl;</pre>
83
        for (int i = 0; i < critical_bridges.size(); i++) {
   cout << critical_bridges[i].first << " " << critical_bridges[i].second << endl;</pre>
84
85
86
87
    }
88
89
    int main() {
90
91
         ios_base::sync_with_stdio(false);
         int T; cin >> T;
for (int t=0; t < T; t++){</pre>
92
93
              important_bridges();
94
         }
95
    }
```

## **Buddy Selection**

Keywords— Maximum Cardinality Matching

```
// STL includes
2
   #include <vector>
3
   #include <string>
   #include <iostream>
   #include <unordered_map>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
8
   #include <boost/graph/max_cardinality_matching.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // Directed graph with integer weights on edges.
   typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_weight_t, int> > Graph;
                                                          Vertex;
   typedef graph_traits < Graph >:: vertex_descriptor
   typedef graph_traits < Graph > :: edge_descriptor
                                                          Edge;
18
   typedef graph_traits<Graph>::edge_iterator
                                                          EdgeIt;
19
   // Property map edge -> weight
   typedef property_map <Graph, edge_weight_t>::type
                                                          WeightMap;
23
   void buddy_selection() {
25
       int n, c, f;
       cin >> n >> c >> f;
       vector<vector<int> > adjacency_list(n, vector<int>(n, 0));
28
       /st Create the graph with all the edges that have higher weight than f and perform maximum
30
       cardinality matching to find a more optimal solution of the problem. If cardinality matching
           is
       equal to n/2 it means that the solution proposed 'f' is not the optimal */
       std::unordered_map<string, vector<int> > characteristics;
       string name;
35
       for (int i = 0; i < n; i++) {</pre>
            for (int j = 0; j < c; j++) {
                cin >> name:
                characteristics[name].push_back(i);
40
       }
41
       // Iterate over all characteristics and create vertex with weight
42
       for (auto it = characteristics.begin(); it != characteristics.end(); it++) {
            vector<int> people = it->second;
44
            int np = people.size(); // Number of people that share the same caracteristic
45
            if (np <= 1) continue;</pre>
46
47
            // Lets iterate over all people that share the same characteristic
48
            for (int i = 0; i < np; i++) {</pre>
49
                for (int j = i+1; j < np; j++) {
                    int p_i = people[i], p_j = people[j];
                    adjacency_list[p_i][p_j]++;
                    adjacency_list[p_j][p_i]++;
                }
           }
       }
       // Create final graph
58
59
       Graph G(n);
       WeightMap weightmap = get(edge_weight, G);
        // Now iterate over all edges and substract the edges with a weight less than 'f'
       for (int i = 0; i < n; i++) {</pre>
            for (int j = i + 1; j < n; j++) {</pre>
65
                int weight = adjacency_list[i][j];
                if (weight > f) {
66
67
                    Edge edg; bool success;
                    tie(edg, success) = add_edge(i, j, G);
                    weightmap[edg] = weight - f;
                }
           }
       }
       // Compute Matching
       vector < Vertex > matemap(n); // Use as an Exterior Property Map: Vertex -> Matc
76
       edmonds_maximum_cardinality_matching (
```

```
G,
77
78
             make_iterator_property_map(matemap.begin(), get(vertex_index , G))
        );
79
        // Look at the matching size
80
        int matchingsize = matching_size (
81
             G,
82
             make_iterator_property_map (matemap.begin(), get(vertex_index , G))
83
        );
84
85
        if (matchingsize == n/2) {
86
              cout << "not optimal" << endl;</pre>
87
88
         } else {
             cout << "optimal" << endl;</pre>
89
        }
90
91
    }
92
    int main() {
93
        ios_base::sync_with_stdio(false);
int T; cin >> T;
for (int t=0; t < T; t++){</pre>
94
95
96
             buddy_selection();
97
98
    }
99
```

#### Keywords— Binary Search, Minimum Circle

```
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
2
   #include <CGAL/Min_circle_2.h>
3
   #include <CGAL/Min_circle_2_traits_2.h>
   #include <iostream>
   #include <vector>
   typedef CGAL::Exact_predicates_exact_constructions_kernel
                                                                  K:
   typedef K::Point_2
                                                                  Р;
   typedef CGAL::Min_circle_2_traits_2<K>
                                                                  Traits;
   typedef CGAL::Min_circle_2<Traits>
                                                                  Min circle:
   using namespace std;
   double ceil_to_double(const K::FT& x) {
       double a = ceil(CGAL::to_double(x));
       while (a + 1 >= x) a -= 1;
18
       while (a < x) a += 1;
       return a;
   }
23
   pair < bool, K::FT > evaluate(int index, vector < K::FT > & distances, vector < P > & cities) {
25
        // Initialize the external circle with the furthest cities from 0 to index.
       Min_circle min_ex_circle(cities.begin(), cities.begin() + index + 1, true);
       Traits::Circle circle = min_ex_circle.circle();
28
       K::FT ex_radius = circle.squared_radius();
30
       K::FT tc_radius;
31
       if (index >= cities.size() - 1) tc_radius = 0;
       else tc_radius = distances[index + 1];
       bool eval = ex_radius >= tc_radius;
36
       K::FT max_radius = max(ex_radius, tc_radius);
38
       return make_pair(eval, max_radius);
39
   }
40
41
   int binary_search(int left, int right, vector<K::FT>& distances, vector<P>& cities) {
       if (left == right - 1) return left;
       int m = (right + left) / 2;
43
44
       K::FT max_rad; bool eval;
45
       tie(eval, max_rad) = evaluate(m, distances, cities);
46
       if (!eval) {
47
           return binary_search(m, right, distances, cities);
48
49
       } else {
           return binary_search(left, m, distances, cities);
   }
   void theev() {
       int n; cin >> n;
       // Read cities locations
       long x, y; cin >> x >> y;
       P their_city(x, y);
60
       P e_their_city(x, y);
       vector <P> cities(n-1);
       for (int i = 0; i < n-1; i++) {</pre>
            cin >> x >> y;
            cities[i] = P(x, y);
66
67
68
       // For the cas we have one or two cities where the min radius will be 0
       if (n <= 2) {
            cout << 0 << endl:
            return;
74
       // Sort all the cities depending on the distance to the capital with decreasing order
       sort(cities.begin(), cities.end(),
76
            [&their_city](Pa, Pb) {
                return CGAL::squared_distance(a, their_city) > CGAL::squared_distance(b, their_city);
```

```
}
78
79
80
81
         // Compute and store the distances to the capital
         vector <K::FT > distances(n-1);
82
         for (int i = 0; i < n - 1; i++) {
83
              distances[i] = squared_distance(cities[i], their_city);
84
85
86
         // Perform binary search
87
         int index = binary_search(0, n-1, distances, cities);
88
89
         K::FT rad_1 = evaluate(index, distances, cities).second;
K::FT rad_2 = evaluate(index + 1, distances, cities).second;
90
91
92
         K::FT result = min(rad_1, rad_2);
93
94
          cout << ceil_to_double(result) << endl;</pre>
95
    }
96
97
     int main() {
98
         int t; cin >> t;
99
100
         cout << fixed << setprecision(0);
for (int i = 0; i < t; i++) {</pre>
102
              theev();
104
105
          return 0;
    }
```

## Chapter 2

## Advanced Algorithms

## 2.1 Dynamic Programming, Brute Force, Split and List

## **Burning Coins**

**Keywords**— Dynamic Programming

```
#include <vector>
   #include <iostream>
   using namespace std;
   int play(vector<int>& coins_values, int left_idx, int right_idx, bool turn, vector<vector<int> >&
       mem) {
           turn = true -> Your turn
           turn = false -> Friend's turn */
       // Final case if no coins left
       if (left_idx == right_idx) {
           return 0;
       }
       if (mem[left_idx][right_idx-1] > -1) {
           return mem[left_idx][right_idx-1];
18
19
       // First take the left coins then the right one
       int left_result, right_result, result;
       if (turn) {
           left_result = coins_values[left_idx];
           left_result += play(coins_values, left_idx+1, right_idx, false, mem);
           right_result = coins_values[right_idx-1];
           right_result += play(coins_values, left_idx, right_idx-1, false, mem);
           result = (left_result > right_result) ? left_result : right_result;
           mem[left_idx][right_idx-1] = result;
28
           return result:
30
       } else {
           left_result = play(coins_values, left_idx+1, right_idx, true, mem);
           right_result = play(coins_values, left_idx, right_idx-1, true, mem);
           result = (left_result < right_result) ? left_result: right_result;</pre>
           mem[left_idx][right_idx-1] = result;
           return result;
36
   }
38
   void burning_coins() {
40
       int n; cin >> n;
41
43
       vector < int > coins_values(n);
       for (int i = 0; i < n; i++) {</pre>
44
           cin >> coins_values[i];
45
46
47
       // Add some memory storing the result for every pair of left and right indexes possible (
48
       vector < vector < int > > mem(n, vector < int > (n, -1));
49
       cout << play(coins_values, 0, n, true, mem) << endl;</pre>
53
   }
```

```
int main() {
    ios_base::sync_with_stdio(false);
    int T; cin >> T;
    for (int t=0; t < T; t++) {
        burning_coins();
    }
}</pre>
```

## Light Pattern

#### **Keywords**— Dynamic Programming

```
#include <vector>
    #include <iostream>
4
   using namespace std;
5
6
   void light_pattern() {
7
       int n, k, x;
       cin >> n >> k >> x;
9
                                 // p: number of patterns,
       int p, s, b;
       uint16_t q = 0x00;
                                 // q: desired pattern
       p = n / k;
16
        // Compute the desired pattern
       for (int i = 1; i <= k; i++) {</pre>
            q \mid = (x \& 1) << (k-i);
18
            x >>= 1;
       vector<uint16_t> bulbs_state(p);
        for (int i = 0; i < p; i++) {</pre>
23
            s = 0;
                                 // s to store the bulb state
24
            for (int j = 0; j < k; j++) {
                cin >> b;
                if (b == 1) s |= 1 << j;</pre>
28
29
            bulbs_state[i] = s;
31
32
        // Compute the diff state of each pattern with the desired one. The int represent the number
        \ensuremath{//} different bulbs at each of the patterns.
        vector < int > diff_state(p, 0);
       for (int i = 0; i < p; i++) {
            int diff = bulbs_state[i] ^ q;
36
            for (int j = 0; j < k; j++) {
                if ((diff & 1<<j) != 0) diff_state[i]++;</pre>
38
39
       }
40
41
       // Compute the accumulated in case the bulbs have been changed one by one or by block all the
43
        // previous ones
        vector < int > values_individual(p), values_block(p);
44
        values_individual[0] = diff_state[0];
45
        values_block[0] = k - diff_state[0] + 1;
46
47
       for (int i = 1; i < p; i++) {</pre>
            values\_individual[i] = min(values\_individual[i-1], values\_block[i-1]) + diff\_state[i];
48
49
            values_block[i] = min(values_block[i-1] + k - diff_state[i],
                                 values_individual[i-1] + k - diff_state[i] + 2);
52
        cout << min(values_individual[p-1], values_block[p-1]) << endl;</pre>
   }
   int main() {
        ios_base::sync_with_stdio(false);
        int T; cin >> T;
58
        for (int t=0; t < T; t++){</pre>
            light_pattern();
60
   }
```

# Light at the Museum

Keywords— Dynamic Programming, Split and List

```
#include <vector>
   #include <iostream>
   #include <algorithm>
3
   #include <climits>
   using namespace std;
                                                pair_int;
   typedef pair <int, int>
8
   typedef vector<vector<int> >
                                                 vecvec;
   typedef vector<pair<vector<int>,int> >
                                                vecpairvec;
   void create_subset(vecvec& state_on, vecvec& state_off, vecpairvec& F, int dbound, int ubound) {
       int N = ubound - dbound;
       int M = state_on[0].size();
       for (int k = 0; k < 1 << N; k++) {
           vector<int> tuple(M, 0);
           int count = 0;
18
           for (int i = 0; i < N; i++) {</pre>
               bool changed_state = (k & 1<<i) != 0;</pre>
               if (changed_state) count++;
23
               for (int j = 0; j < M; j++)
                    tuple[j] += (changed_state) ? state_off[i+dbound][j] : state_on[i+dbound][j];
25
           F.push_back(make_pair(tuple, count));
       }
28
   }
   struct Comp {
31
       bool operator() (pair<vector<int>, int> P, vector<int> V) {
           return P.first < V;</pre>
       bool operator() (vector<int> V, pair<vector<int>, int> P) {
           return V < P.first;</pre>
36
   };
38
   void light_at_the_museum() {
40
41
       int N, M; cin >> N >> M;
       vector < int > brightness(M);
43
       for (int i = 0; i < M; i++) cin >> brightness[i];
44
45
       46
       for (int j = 0; j < N; j++)
47
           for (int i = 0; i < M; i++) cin >> state_on[j][i] >> state_off[j][i];
48
49
       // Create all combinations for two subsets (divide and list)
       vecpairvec F1, F2;
       \label{eq:create_subset} create\_subset(state\_on, state\_off, F1, 0, N/2);
       create_subset(state_on, state_off, F2, N/2, N);
       sort(F2.begin(), F2.end());
       int min_changes = INT_MAX;
       for (int idx = 0; idx < F1.size(); idx++) {</pre>
58
           vector<int> missing = F1[idx].first;
           for (int i = 0; i < M; i++) {</pre>
               missing[i] = brightness[i] - missing[i];
           pair < vecpairvec :: iterator , vecpairvec :: iterator > it_pair;
           it_pair = equal_range(F2.begin(), F2.end(), missing, Comp());
66
           for (auto it = it_pair.first; it != it_pair.second; it++) {
67
68
                int count = it->second + F1[idx].second;
               min_changes = min(min_changes, count);
           }
       }
       if (min_changes == INT_MAX) cout << "impossible\n";</pre>
74
       else cout << min_changes << endl;</pre>
   }
   int main() {
```

```
ios_base::sync_with_stdio(false);
int T; cin >> T;
for (int t=0; t < T; t++){
    light_at_the_museum();
}
}
</pre>
```

#### The Great Game

Keywords— Dynamic Programming

```
#include <vector>
   #include <iostream>
   #include <climits>
3
   using namespace std;
6
   int max_(vector<vector<int> > &transitions, int start, int end,
8
9
       vector < int > &min_mem, vector < int > &max_mem);
   int min_(vector<vector<int> > &transitions, int start, int end,
            vector<int> &min_mem, vector<int> &max_mem) {
       if (start == end) {
           min_mem[start] = 0;
            return 0:
       }
18
       int min_dist = INT_MAX;
       for (int v : transitions[start]) {
            if (max_mem[v] == -1) {
                max_(transitions, v, end, min_mem, max_mem);
23
           min_dist = min(min_dist, max_mem[v]);
25
       min_mem[start] = min_dist + 1;
       return min_mem[start];
28
   }
30
   int max_(vector<vector<int> > &transitions, int start, int end,
31
       vector < int > &min_mem, vector < int > &max_mem) {
       if (start == end) {
           max mem[start] = 0:
36
            return 0;
38
39
       int max_dist = 0;
       for (int v : transitions[start]) {
40
41
           if (\min_{m \in [v]} == -1) {
                min_(transitions, v, end, min_mem, max_mem);
43
44
            max_dist = max(max_dist, min_mem[v]);
45
       max_mem[start] = max_dist + 1;
46
       return max_mem[start];
47
   }
48
49
   void great_game() {
50
       int n, m;
       cin >> n >> m;
       int r, b;
       cin >> r >> b;
       // set to O-index
       r--; b--;
       vector < vector < int > > transitions(n);
58
       for (int i = 0; i < m; i++) {</pre>
60
            int u, v;
            cin >> u >> v;
           // set to O-index
            u--; v--;
            transitions[u].push_back(v);
66
       // Create memory vectors
67
68
       vector < int > min_mem(n, -1), max_mem(n, -1);
       // For each of the starting possitions, check which one has minimum movements to win the game.
       int red_moves = min_(transitions, r, n-1, min_mem, max_mem);
       int black_moves = min_(transitions, b, n-1, min_mem, max_mem);
74
       cout << (black_moves < red_moves || (black_moves == red_moves && black_moves % 2 == 0)) <<
            endl:
   }
```

```
int main() {
    ios_base::sync_with_stdio(false);
    int T; cin >> T;
    int t=0; t < T; t++) {
        great_game();
    }
}</pre>
```

Keywords — Maximum Cardinality Matching, Dijkstra Shortest Path

```
// STL includes
   #include <vector>
3
   #include <string>
   #include <iostream>
   #include <unordered_map>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/max_cardinality_matching.hpp>
   #include <boost/graph/dijkstra_shortest_paths.hpp>
   // Namespaces
   using namespace std;
14
   using namespace boost;
   \ensuremath{//} Directed graph with integer weights on edges.
16
   typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_weight_t, int> > Graph;
   typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_weight_t, int> > DiGraph;
   typedef graph_traits < DiGraph >:: vertex_descriptor
                                                             Vertex:
   typedef graph_traits < DiGraph > :: edge_descriptor
                                                             Edge;
   typedef graph_traits < DiGraph > :: edge_iterator
                                                             EdgeIt;
   // Property map edge -> weight
23
   typedef property_map < DiGraph , edge_weight_t > :: type
                                                             WeightMap;
   void oh_her_majestys_secret_service() {
       int n, m, a, s, c, d;
       cin >> n >> m >> a >> s >> c >> d;
28
30
       DiGraph G(n);
31
       WeightMap weightmap = get(edge_weight, G);
        char w; int x, y, z;
       Edge edg; bool success;
       for (int i = 0; i < m; i++) {</pre>
            cin >> w >> x >> y >> z;
36
38
            tie(edg, success) = add_edge(x, y, G);
            weightmap[edg] = z;
            if (w == 'L') {
40
41
                tie(edg, success) = add_edge(y, x, G);
                weightmap[edg] = z;
            }
43
       }
44
45
46
       vector < int > agents(a), shelters(s);
       for (int i = 0; i < a; i++) cin >> agents[i];
47
       for (int i = 0; i < s; i++) cin >> shelters[i];
48
49
       // Compute one distance map per agent
       vector < vector < int > > distmap(a, vector < int > (n));
       for (int i = 0; i < a; i++) {</pre>
            dijkstra_shortest_paths(G, agents[i],
                distance_map(make_iterator_property_map(distmap[i].begin(), get(vertex_index, G))));
       // Represent G' as the pairwise distance matrix T from agents to shelters.
       vector < vector < int > > T(a, vector < int > (s, INT_MAX));
       for (int i = 0; i < a; i++) {</pre>
            for (int j = 0; j < s; j++) {
                T[i][j] = distmap[i][shelters[j]];
       }
        // Binary search for the smallest t
        int low = 0, high = INT_MAX;
       while (low < high) {</pre>
66
            int mid = low + (high-low)/2;
67
            // Regresent the model as a bipartite graph with all the agents as nodes in one side, and
68
            // all the shelters duplicated for each possible capacity and then compute the maximum
            // cardinality matching
            Graph GG(a + s*c);
            for (int i = 0; i < a; i++) {</pre>
                for (int j = 0; j < s; j++) {</pre>
74
                    if (T[i][j] == INT_MAX) continue;
                    for (int k = 0; k < c; k++) {
76
                         if (T[i][j] + (k + 1) * d <= mid) {</pre>
                             add_edge(i, a + k * s + j, GG);
```

```
}
78
                        }
79
                   }
80
81
              // Compute maximum cardinality
vector<Vertex> matemap(a + s * c); // Use as an Exterior Property Map: Vertex -> Matc
82
83
               edmonds_maximum_cardinality_matching (
84
85
                   make_iterator_property_map(matemap.begin(), get(vertex_index , G))
86
              );
87
              const Vertex NULL_VERTEX = graph_traits<Graph>::null_vertex();
88
              int matchingsize = 0;
for (int i = 0; i < a; i++) {
   matchingsize += (matemap[i] != NULL_VERTEX);</pre>
89
90
91
92
               if (matchingsize == a) high = mid;
94
              else low = mid + 1;
95
96
97
         cout << low << endl;</pre>
98
    }
99
100
    int main() {
          ios_base::sync_with_stdio(false);
102
         int T; cin >> T;
         for (int t=0; t < T; t++){</pre>
104
              oh_her_majestys_secret_service();
107
    }
```

# Poker Chips

#### **Keywords**— Dynamic Programming

```
#include <vector>
   #include <map>
2
   #include <iostream>
3
   #include <cmath>
   #include <stdexcept>
   #include <algorithm>
   using namespace std;
8
9
   double compute_award(double k) {
       if (k > 1) {
           return exp2(k-2);
       } else if (k == 1) {
           return 0;
       } else {
           throw runtime_error("k can not be less than 1.");
17
       }
   }
18
    int map_positions_into_vector(vector<int>& stack_heigh, vector<int>& stack_top) {
       int nb_stacks = stack_heigh.size();
23
        int accum = 1, pos = 0;
       for (int i = nb_stacks - 1; i >= 0; i--) {
25
            pos += accum * stack_heigh[i];
            accum *= stack_top[i] + 1;
       }
       return pos;
28
   }
30
    int play(vector<vector<int> >& stacks, vector<int>& nb_chips, vector<int>& turn_positions, vector<</pre>
31
       int>& memory) {
       // Check memory first
       int mem_pos = map_positions_into_vector(turn_positions, nb_chips);
35
       if (memory[mem_pos] != -1) return memory[mem_pos];
       // Check if there is not more chips at the stack (it is not necessary as memory[0] = 0)
       int nb_stacks = stacks.size();
40
       map<int, vector<int> > color_map;
       // Check at each of the stacks and see the next poker chips and group them by color
41
       for (int i = 0; i < nb_stacks; i++) {</pre>
42
43
            int next_position = turn_positions[i] - 1;
            if (next_position < 0) continue;</pre>
                                                // In case a stack is empty
44
45
            color_map[stacks[i][next_position]].push_back(i);
46
47
       // Iterate over all groups of colors, and compute the maximum award in DP achievable from this
48
49
       // stack positions
       int max_award = 0;
       for (auto it = color_map.begin(); it != color_map.end(); it++) {
            vector<int> chips_positions = it->second;
            int nb = chips_positions.size();
            /* Now compute all the possible combinations of extracting these chips (extract all the
            ones with the same colos is not allways the best strategy)
            Example:
            3 3 3 2 2 2 2
58
59
            2 2 2 X X 3 X
           If use the strategy to extract all the chips from the same color award = 10
61
            but if first is removed the 2 with a 3 at the bottom, then the award = 20
            for (int k = 1; k < 1<<nb; k++) {</pre>
65
                int count = 0;
66
67
                // Selecting the chips from the same color, see which is the award with the next
                    position
                vector < int > new_positions(turn_positions);
68
                for (int i = 0; i < nb; i++) {</pre>
                    if (k & (1<<i)) {</pre>
                         count++;
                        new_positions[chips_positions[i]]--;
74
                    }
                }
```

```
76
                 int new_award = compute_award(count);
78
79
                 int award = play(stacks, nb_chips, new_positions, memory);
                 max_award = max(max_award, award + new_award);
80
             }
81
83
84
        // Store result into memory
        memory[mem_pos] = max_award;
85
86
87
        return max_award;
    }
89
    void poker_chips() {
90
        int n; cin >> n;
92
        vector < int > nb_chips(n);
        vector < vector < int > > stacks(n);
94
        vector < int > initial_positions(n);
95
96
        for (int i = 0; i < n; i++) {</pre>
97
98
            cin >> nb_chips[i];
        }
        for (int i = 0; i < n; i++) {</pre>
100
             for (int j = 0; j < nb_chips[i]; j++) {</pre>
                 int c; cin >> c;
                 stacks[i].push_back(c);
105
             initial_positions[i] = nb_chips[i];
        }
106
        int N_memory = map_positions_into_vector(nb_chips, nb_chips) + 1;
108
        vector < int > memory(N_memory, -1);
109
        memory[0] = 0;
110
        int max_award = play(stacks, nb_chips, initial_positions, memory);
113
        cout << max_award << endl;</pre>
114
    }
116
    int main() {
118
        ios_base::sync_with_stdio(false);
119
        int T; cin >> T;
        for (int t=0; t < T; t++){</pre>
             poker_chips();
121
    }
```

## 2.2 BGL Flows

# Coin Tossing

```
#include <iostream>
   #include <vector>
3
   #include <algorithm>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
6
   #include <boost/graph/push_relabel_max_flow.hpp>
   #include <boost/graph/edmonds_karp_max_flow.hpp>
8
   // Namespaces
9
   using namespace std;
   using namespace boost;
13
   // BGL Graph definitions
14
   // ===========
   // Graph Type with nested interior edge properties for Flow Algorithms
   typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
18
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
       property<edge_capacity_t, long,</pre>
           property < edge_residual_capacity_t, long,</pre>
                property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
   // Interior Property Maps
   typedef property_map < Graph , edge_capacity_t >::type
                                                              EdgeCapacityMap;
   typedef property_map < Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph, edge_reverse_t>::type ReverseEdgeMap;
                                                             ReverseEdgeMap;
   typedef graph_traits < Graph >:: vertex_descriptor
                                                              Vertex;
26
   typedef graph_traits < Graph > :: edge_descriptor
                                                              Edge;
   // Custom Edge Adder Class, that holds the references
30
31
   // to the graph, capacity map and reverse edge map
   // -----
   class EdgeAdder {
       Graph &G;
       EdgeCapacityMap &capacitymap;
       ReverseEdgeMap &revedgemap;
38
39
       // to initialize the Object
40
       EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, ReverseEdgeMap &revedgemap):
            G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
41
       // to use the Function (add an edge)
43
       void addEdge(int from, int to, long capacity) {
44
            Edge e, reverseE;
45
            bool success;
46
           tie(e, success) = add_edge(from, to, G);
47
            tie(reverseE, success) = add_edge(to, from, G);
48
            capacitymap[e] = capacity;
49
50
            capacitymap[reverseE] = 0;
            revedgemap[e] = reverseE;
            revedgemap[reverseE] = e;
       }
   };
56
   void coin_tossing() {
       int n, m;
58
       cin >> n >> m;
       Graph G;
       EdgeCapacityMap capacitymap = get(edge_capacity, G);
       ReverseEdgeMap revedgemap = get(edge_reverse, G);
       ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
       EdgeAdder eaG(G, capacitymap, revedgemap);
66
       for (int i = 0; i < m; i++) {</pre>
68
           int a, b, c;
            cin >> a >> b >> c;
           if (c == 1) {
                eaG.addEdge(i, m+a, 1);
           } else if (c == 2) {
74
                eaG.addEdge(i, m+b, 1);
            } else {
```

```
eaG.addEdge(i, m+a, 1);
76
77
                  eaG.addEdge(i, m+b, 1);
             }
78
79
        }
80
81
         Vertex src = add_vertex(G);
82
        for (int i = 0; i < m; i++) {</pre>
83
84
             eaG.addEdge(src, i, 1);
85
         Vertex sink = add_vertex(G);
86
87
         long sum = 0;
         for (int j = m; j < m+n; j++) {</pre>
88
             int s; cin >> s;
89
90
             sum += s;
             eaG.addEdge(j, sink, s);
91
        }
92
        long flow = push_relabel_max_flow(G, src, sink);
94
95
        if (flow != m || flow != sum) {
    cout << "no" << endl;</pre>
96
97
98
         } else {
             cout << "yes" << endl;
         }
100
    }
    int main() {
         ios_base::sync_with_stdio(false);
105
         int T; cin >> T;
         for (int t=0; t < T; t++){</pre>
106
              coin_tossing();
         }
108
109
    }
```

# **Shopping Trip**

```
#include <iostream>
2
   #include <vector>
3
   #include <algorithm>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/push_relabel_max_flow.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
14
   // =============
   // Graph Type with nested interior edge properties for Flow Algorithms
   typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
16
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
       property < edge_capacity_t, long,</pre>
18
            property < edge_residual_capacity_t, long,</pre>
                property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
   // Interior Property Maps
   typedef property_map < Graph , edge_capacity_t >::type
                                                               EdgeCapacityMap;
   typedef property_map < Graph , edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph , edge_reverse_t>::type ReverseEdgeMap;
23
24
   typedef graph_traits < Graph >:: vertex_descriptor
                                                               Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
28
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map and reverse edge map
   // -----
31
   class EdgeAdder {
       Graph &G:
       EdgeCapacityMap &capacitymap;
       ReverseEdgeMap &revedgemap;
        // to initialize the Object
38
        EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, ReverseEdgeMap &revedgemap):
            G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
40
41
       // to use the Function (add an edge)
       void addEdge(int from, int to, long capacity) {
43
            Edge e, reverseE;
44
            bool success;
45
            tie(e, success) = add_edge(from, to, G);
46
            tie(reverseE, success) = add_edge(to, from, G);
47
            capacitymap[e] = capacity;
48
49
            capacitymap[reverseE] = 0;
            revedgemap[e] = reverseE;
50
            revedgemap[reverseE] = e;
       }
   };
   void shopping() {
       int n, m, s;
58
       cin >> n >> m >> s;
       Graph G;
        EdgeCapacityMap capacitymap = get(edge_capacity, G);
       ReverseEdgeMap revedgemap = get(edge_reverse, G);
       EdgeAdder eaG(G, capacitymap, revedgemap);
       vector < int > stores_locations(s);
66
       for (int i = 0; i < s; i++) {</pre>
            cin >> stores_locations[i];
67
68
       // Add street edges
       for (int i = 0; i < m; i++) {</pre>
            int a, b;
            cin >> a >> b;
74
            eaG.addEdge(a, b, 1);
            eaG.addEdge(b, a, 1);
       }
76
```

```
// Add edges from stores to sink
// Vertex src = add_vertex(G);
78
79
         Vertex sink = add_vertex(G);
80
         // eaG.addEdge(src, 0, s);
for (int i = 0; i < s; i++) {
81
82
               eaG.addEdge(stores_locations[i], sink, 1);
83
84
85
86
         long flow = push_relabel_max_flow(G, 0, sink);
87
         if (flow == s) {
88
               cout << "yes" << endl;
89
         } else {
90
               cout << "no" << endl;
91
92
93
    }
94
95
     int main() {
96
         ios_base::sync_with_stdio(false);
97
         int T; cin >> T;
for (int t=0; t < T; t++){</pre>
98
99
100
               shopping();
         }
    }
```

# Kingdom Defence

```
#include <iostream>
2
   #include <map>
3
   #include <algorithm>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/push_relabel_max_flow.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
14
   // =============
   // Graph Type with nested interior edge properties for Flow Algorithms
   typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
16
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
       property < edge_capacity_t, long,</pre>
18
            property < edge_residual_capacity_t , long ,</pre>
                property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
   // Interior Property Maps
   typedef property_map < Graph , edge_capacity_t >::type
                                                               EdgeCapacityMap;
   typedef property_map < Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph, edge_reverse_t>::type ReverseEdgeMap;
23
   typedef graph_traits < Graph >:: vertex_descriptor
                                                                Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
                                                                Edge;
   typedef graph_traits < Graph > :: edge_iterator
                                                                EdgeIt;
28
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map and reverse edge map
   class EdgeAdder {
       Graph &G;
       EdgeCapacityMap &capacitymap;
       ReverseEdgeMap &revedgemap;
36
38
   public:
        // to initialize the Object
       EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, ReverseEdgeMap &revedgemap):
40
41
            G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
       // to use the Function (add an edge)
43
       Edge addEdge(int from, int to, long capacity) {
44
            Edge e, reverseE;
45
            bool success:
46
            tie(e, success) = add_edge(from, to, G);
47
            tie(reverseE, success) = add_edge(to, from, G);
48
            capacitymap[e] = capacity;
49
50
            capacitymap[reverseE] = 0;
            revedgemap[e] = reverseE;
            revedgemap[reverseE] = e;
            return e;
       }
   };
   void kingdom_defence() {
58
       int 1, p;
       cin >> 1 >> p;
       Graph G(1+2):
        EdgeCapacityMap capacitymap = get(edge_capacity, G);
        ReverseEdgeMap revedgemap = get(edge_reverse, G);
        // ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
66
       EdgeAdder eaG(G, capacitymap, revedgemap);
68
       Vertex src = vertex(1, G);
       Vertex sink = vertex(1+1, G);
       long total_defenders = 0;
       long total_available = 0;
       for (int i = 0; i < 1; i++) {</pre>
74
            long g, d;
            cin >> g >> d;
76
            Vertex location = vertex(i, G);
            eaG.addEdge(src, location, g);
```

```
eaG.addEdge(location, sink, d);
78
             total_defenders += d;
79
80
             total_available += g;
81
82
        for (int i = 0; i < p; i++) {</pre>
83
             int f, t;
84
             long c, C;
85
86
             cin >> f >> t >> c >> C;
             eaG.addEdge(f, t, C - c);
87
             if (c > 0) {
88
89
                 eaG.addEdge(f, sink, c);
                 total_defenders += c;
90
                 eaG.addEdge(src, t, c);
total_available += c;
91
92
             }
93
        }
94
95
        long flow = push_relabel_max_flow(G, src, sink);
96
97
        bool result = flow == total_defenders;
98
99
100
         if (result) {
             cout << "yes" << endl;</pre>
102
         } else {
             cout << "no" << endl;
104
105
    }
107
    int main() {
108
         ios_base::sync_with_stdio(false);
110
         int T; cin >> T;
        for (int t=0; t < T; t++){</pre>
             kingdom_defence();
113
    }
```

#### **Keywords**— Dynamic Programming

```
#include <iostream>
2
   #include <vector>
3
   #include <map>
   #include <algorithm>
   using namespace std;
8
   struct center {
9
       center (int n) {
           sup = vector<uint16_t>(n, 0);
       vector < uint16_t > sup;
       map<uint16_t, map<int, int> > extsup;
       map<int, int> bestmap;
   };
18
   int best_stormtroopers(vector<center>& centers, int c, int mask, const int S) {
        auto bestit = centers[c].bestmap.find(mask);
       if (bestit != centers[c].bestmap.end())
            return bestit -> second;
23
       int best = 0;
       for (int k = 0; k < (0x1 << S); k++) {
25
            // Mask refers to the stormtroopers that can not be choosen because are being supervised
            if ((k & mask) != 0) continue;
28
            bool valid = true;
            // Check the validity looking if any of the stormtroopers supervise each other in this
30
            // configurations
31
            for (int i = 0; i < S && valid; i++) {</pre>
                if (((k & (0x1<<i)) != 0) && ((k & centers[c].sup[i]) != 0)) valid = false;
            }
            if (!valid) continue:
36
            int count = 0;
38
            // Count the strompers being sabotaged
            for (int i = 0; i < S; i++) {</pre>
                if (k & (0x1<<i)) count++;</pre>
40
41
            7
            // Now compute the mask (the stormtroopers that on the children centers are being
           // supervised by this configuration) and with DP count the maximum number of stormtroopers
43
44
            // that are not being supervised by each other.
           for (auto& esup : centers[c].extsup) {
45
                int nmask = 0;
46
                for (auto& p : esup.second) {
47
                    if (k & 0x1<<p.first) nmask |= p.second;</pre>
48
49
50
                count += best_stormtroopers(centers, esup.first, nmask, S);
            }
            best = max(best, count);
        centers[c].bestmap[mask] = best;
       return best;
   }
58
   void a_new_hope() {
       int K, S, M;
60
       cin >> K >> S >> M;
       vector < center > centers(K, center(S));
       int u, v, h, x, y;
       for (int i = 0; i < M; i++) {</pre>
66
            cin >> u >> v >> h;
            if (u == v) {
67
                for (int j = 0; j < h; j++) {
68
                    cin >> x >> y;
                    centers[u].sup[x] |= 0x1 << y;
                }
           }
            else {
74
                map < int , int > esup;
                for (int j = 0; j < h; j++) {</pre>
76
                    cin >> x >> y;
                    esup[x] \mid = 0x1 << y;
```

```
}
78
79
                       centers[u].extsup[v] = esup;
80
81
          }
82
83
          cout << best_stormtroopers(centers, 0, 0, S) << endl;</pre>
84
     }
85
86
87
     int main() {
          ios_base::sync_with_stdio(false);
int T; cin >> T;
for (int t=0; t < T; t++){
   a_new_hope();</pre>
88
89
90
91
92
    }
93
```

# 2.3 Linear/Quadratic Programing

### What is the maximum?

```
#include <iostream>
   #include <cassert>
   #include <cmath>
   #include <CGAL/basic.h>
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
   #include <CGAL/Gmpz.h>
   // choose exact integral type
9
   typedef CGAL::Gmpz ET;
   // program and solution types
   typedef CGAL::Quadratic_program <long > Program;
13
   typedef CGAL::Quadratic_program_solution <ET> Solution;
   using namespace std;
18
   void solve_1(int a, int b){
       Program qp (CGAL::SMALLER, true, 0, false, 0);
       const int X = 0;
       const int Y = 1;
       qp.set_a(X, 0, 1); qp.set_a(Y, 0, 1); qp.set_b(0, 4);
       qp.set_a(X, 1, 4); qp.set_a(Y, 1, 2); qp.set_b(1, a*b);
       qp.set_a(X, 2, -1); qp.set_a(Y, 2, 1); qp.set_b(2, 1);
qp.set_c(Y, -b);
       qp.set_d(X, X, 2*a);
26
       Solution s = CGAL::solve_quadratic_program(qp, ET());
28
       assert (s.solves_quadratic_program(qp));
29
       // cout << s << endl;
30
31
       if (s.is_infeasible()) {
            cout << "no" << endl;
       } else if (s.is_unbounded()) {
           cout << "unbounded" << endl;</pre>
       } else {
            assert (s.is_optimal());
            long result = floor(-CGAL::to_double(s.objective_value()));
38
39
            cout << result << endl;</pre>
40
   }
41
   void solve_2(int a, int b){
43
       Program qp (CGAL::LARGER, false, 0, true, 0);
44
       const int X = 0;
45
       const int Y = 1;
46
       const int Z2 = 2;
47
       qp.set_a(X, 0, 1); qp.set_a(Y, 0, 1); qp.set_b(0, -4);
48
       qp.set_a(X, 1, 4); \; qp.set_a(Y, 1, 2); \; qp.set_a(Z2, 1, 1); \; qp.set_b(1, -a*b); \\
49
       qp.set_a(X, 2, -1); qp.set_a(Y, 2, 1); qp.set_b(2, -1);
50
       qp.set_u(Z2, false, 0);
       qp.set_d(X, X, 2*a);
       qp.set_c(Y, b);
       qp.set_d(Z2, Z2, 2*1);
56
       Solution s = CGAL::solve_quadratic_program(qp, ET());
       assert (s.solves_quadratic_program(qp));
58
       // cout << s << endl;
       if (s.is_infeasible()) {
            cout << "no" << endl;
       } else if (s.is_unbounded()) {
            cout << "unbounded" << endl;</pre>
63
       } else if (s.is_optimal()){
            long result = ceil(CGAL::to_double(s.objective_value()));
            cout << result << endl;</pre>
66
       } else {
            cout << "no" << endl;
68
   }
   int main() {
74
       int p; cin >> p;
```

```
while (p > 0) {
   int a, b;
   cin >> a >> b;
   if (p == 1) solve_1(a, b);
   else if (p == 2) solve_2(a, b);
   cin >> p;
}
```

#### Diet

```
#include <iostream>
   #include <cassert>
   #include <cmath>
3
   #include <CGAL/basic.h>
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
6
   #include <CGAL/Gmpzf.h>
   // choose exact integral type
   typedef CGAL::Gmpzf ET;
   // program and solution types
12
   typedef CGAL::Quadratic_program <long > Program;
   typedef CGAL::Quadratic_program_solution<ET> Solution;
16
   using namespace std;
18
   void diet(int n, int m){
       Program lp (CGAL::LARGER, true, 0, false, 0);
       for (int i = 0; i < n; i++) {</pre>
            long c_min, c_max;
23
            cin >> c_min >> c_max;
24
26
            lp.set_b(i*2, c_min);
            lp.set_b(i*2+1, c_max);
            lp.set_r(i*2+1, CGAL::SMALLER);
28
29
31
       for (int j = 0; j < m; j++) {</pre>
32
            long p; cin >> p;
            lp.set_c(j, p);
34
            for (int i = 0; i < n; i++) {</pre>
                long C; cin >> C;
                lp.set_a(j, i*2, C);
36
                lp.set_a(j, i*2+1, C);
            }
       }
40
       Solution s = CGAL::solve_linear_program(lp, ET());
41
42
       assert (s.solves_linear_program(lp));
43
       if (s.is_infeasible() || s.is_unbounded()) {
44
45
            cout << "No such diet." << endl;</pre>
       } else {
46
            long result = floor(CGAL::to_double(s.objective_value()));
47
48
            cout << result << endl;</pre>
49
   }
50
   int main() {
       int n, m;
       cin >> n >> m;
       while (!(n==0 \&\& m==0)) {
56
            diet(n, m);
58
            cin >> n >> m;
       }
59
   }
```

#### **Portfolios**

```
#include <iostream>
   #include <cassert>
2
   #include <cmath>
3
   #include <CGAL/basic.h>
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
   #include <CGAL/Gmpzf.h>
   // choose exact integral type
   typedef CGAL::Gmpzf ET;
   // program and solution types
   typedef CGAL::Quadratic_program <long > Program;
   typedef CGAL::Quadratic_program_solution<ET> Solution;
14
   using namespace std:
   bool solve_case(vector<long>& c, vector<long>& r, vector<vector<long> >& v, long C, long R, long V
18
        , int n) {
19
        Program qp (CGAL::LARGER, true, 0, false, 0);
       for (int i = 0; i < n; i++) {</pre>
            qp.set_a(i, 0, r[i]);
            qp.set_a(i, 1, c[i]);
24
        qp.set_r(1, CGAL::SMALLER);
        qp.set_b(0, R);
        qp.set_b(1, C);
26
27
       for (int i = 0; i < n; i++) {</pre>
            for (int j = 0; j < n; j++) {</pre>
                qp.set_d(i, j, 2*v[i][j]);
30
       }
32
       Solution s = CGAL::solve_quadratic_program(qp, ET());
35
        assert (s.solves_quadratic_program(qp));
        if (s.is_infeasible() || s.is_unbounded()) {
38
        } else if (CGAL::to_double(s.objective_value()) <= V) {</pre>
40
            return true;
41
        } else {
            return false;
42
43
        7
44
   }
45
46
47
    void portfolios(int n, int m){
       vector < long > c(n), r(n);
49
       vector < vector < long > > v(n, vector < long > (n));
        for (int i = 0; i < n; i++) {</pre>
            cin >> c[i] >> r[i];
        for (int i = 0; i < n; i++) {</pre>
            for (int j = 0; j < n; j++) {</pre>
                 cin >> v[i][j];
58
59
       }
        for (int i = 0; i < m; i++) {</pre>
            long C, V, R;
            cin >> C >> R >> V;
62
            bool result = solve_case(c, r, v, C, R, V, n);
            if (result) {
65
                cout << "Yes." << endl;</pre>
            } else {
66
                 cout << "No." << endl;
67
        }
   }
72
   int main() {
76
        int n, m;
```

```
while (true) {
    cin >> n >> m;
    if (n == 0 && m == 0) { break; }
    portfolios(n, m);
}

80
81
82
}
```

#### Inball

```
#include <iostream>
   #include <cassert>
   #include <cmath>
3
   #include <CGAL/basic.h>
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
6
   #include <CGAL/Gmpz.h>
   // choose exact integral type
   typedef CGAL::Gmpz ET;
   // program and solution types
12
   typedef CGAL::Quadratic_program <long > Program;
   typedef CGAL::Quadratic_program_solution<ET> Solution;
16
   using namespace std;
18
   void inball(int n){
       int d; cin >> d;
       Program lp (CGAL::SMALLER, false, 0, false, 0);
23
       lp.set_c(d, -1);
       lp.set_l(d, true, 0);
24
       for (int i = 0; i < n; i++) {
26
            long norm = 0;
            for (int j = 0; j < d; j++) {</pre>
                long a; cin >> a;
28
29
                lp.set_a(j, i, a);
                norm += a * a;
31
32
            lp.set_a(d, i, sqrt(norm));
            long b; cin >> b;
34
            lp.set_b(i, b);
36
       Solution s = CGAL::solve_linear_program(lp, ET());
       assert (s.solves_linear_program(lp));
       if (s.is_infeasible()) {
40
            cout << "none" << endl;</pre>
41
       } else if (s.is_unbounded()) {
42
            cout << "inf" << endl;</pre>
43
       } else {
44
45
            long result = -CGAL::to_double(s.objective_value());
            cout << result << endl;</pre>
46
47
48
   }
49
50
   int main() {
       int n;
       while (true) {
           cin >> n;
            if (n == 0) { break; }
            inball(n);
56
       }
   }
```

# **Knights**

```
#include <iostream>
2
   #include <map>
3
   #include <algorithm>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/push_relabel_max_flow.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
14
   // ===========
   // Graph Type with nested interior edge properties for Flow Algorithms
   typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
        property < edge_capacity_t, long,</pre>
18
            property < edge_residual_capacity_t , long ,</pre>
                property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
   // Interior Property Maps
   typedef property_map < Graph , edge_capacity_t >::type
                                                                EdgeCapacityMap;
   typedef property_map < Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph, edge_reverse_t>::type ReverseEdgeMap;
23
   typedef graph_traits < Graph > :: vertex_descriptor
                                                                Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
                                                                 Edge;
   typedef graph_traits < Graph > :: edge_iterator
                                                                EdgeIt;
28
   \ensuremath{//} Custom Edge Adder Class, that holds the references
   // to the graph, capacity map and reverse edge map
   class EdgeAdder {
       Graph &G;
        EdgeCapacityMap &capacitymap;
        ReverseEdgeMap &revedgemap;
38
   public:
        // to initialize the Object
        EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, ReverseEdgeMap &revedgemap):
40
41
            G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
        // to use the Function (add an edge)
43
        Edge addEdge(int from, int to, long capacity) {
44
            Edge e, reverseE;
45
            bool success;
46
            tie(e, success) = add_edge(from, to, G);
47
            tie(reverseE, success) = add_edge(to, from, G);
48
49
            capacitymap[e] = capacity;
50
            capacitymap[reverseE] = 0;
            revedgemap[e] = reverseE;
            revedgemap[reverseE] = e;
            return e;
        7
   };
    void knights() {
58
       int m, n, k, c;
        cin >> m >> n >> k >> c;
        Graph G(2*m*n+2):
        EdgeCapacityMap capacitymap = get(edge_capacity, G);
        ReverseEdgeMap revedgemap = get(edge_reverse, G);
        EdgeAdder eaG(G, capacitymap, revedgemap);
66
        \ensuremath{//} Create graph representing the cave
67
68
        Vertex src = vertex(2*n*m, G);
        Vertex sink = vertex(2*n*m+1, G);
        for (int i = 0; i < n; i++) {</pre>
            for (int j = 0; j < m; j++) {</pre>
                int pos_out = i*m + j;
                int pos_in = pos_out + n*m;
                 int pos_out_right = pos_out + 1;
                int pos_in_right = pos_out_right + n*m;
76
                 int pos_out_down = pos_out + m;
                 int pos_in_down = pos_out_down + n*m;
```

```
78
                  // Conect inner node with outer node
                  eaG.addEdge(pos_in, pos_out, c);
80
                  if (j < m-1) {
                      // Connecting node with the one on the right
81
                      eaG.addEdge(pos_out, pos_in_right, 1);
eaG.addEdge(pos_out_right, pos_in, 1);
83
84
                  if (i < n-1) {
86
                      \ensuremath{//} Connecting node with the one on the bottom
                      eaG.addEdge(pos_out, pos_in_down, 1);
87
88
                      eaG.addEdge(pos_out_down, pos_in, 1);
89
                  if (i == 0 || i == n-1) {
90
                      // Connecting top and bottom nodes to sink
91
92
                      eaG.addEdge(pos_out, sink, 1);
                  if (j == 0 || j == m-1) {
94
                      // Connecting left and right nodes to sink
95
                      eaG.addEdge(pos_out, sink, 1);
96
97
                  }
             }
98
        }
99
100
         // Add edge from the source to the intersection representing the starting point of the knight
         for (int i = 0; i < k; i++) {</pre>
102
             int x, y; cin >> x >> y;
104
             int pos = y*m+x + n*m;
             eaG.addEdge(src, pos, 1);
107
         // Compute the maximum number of knights as maximum flow
108
         long flow = push_relabel_max_flow(G, src, sink);
         cout << flow << endl;</pre>
110
    }
    int main() {
         int T; cin >> T;
115
         for (int t=0; t < T; t++){</pre>
116
             knights();
118
    }
119
```

# 2.4 Proximity Structures in CGAL

## Graypes

**Keywords**— Delaunay Triangulation

```
#include <vector>
   #include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
   #include <CGAL/Delaunay_triangulation_2.h>
   typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
   typedef CGAL::Delaunay_triangulation_2 < K >
                                                                   Triangulation;
   typedef Triangulation::Finite_faces_iterator
                                                                   Face_iterator;
   typedef Triangulation::Edge_iterator
                                                                   EdgeIt;
   using namespace std;
14
   double ceil_to_double(const K::FT& x) {
       double a = ceil(CGAL::to_double(x));
       while (a+1 >= x) a -= 1;
16
       while (a < x) a += 1;</pre>
       return a;
18
   }
19
   void graypes(int n) {
       vector < K :: Point_2 > p(n);
       Triangulation t;
       for (int i = 0; i < n; i++) {</pre>
25
            long x, y;
            cin >> x >> y;
27
           p[i] = K::Point_2(x, y);
28
       t.insert(p.begin(), p.end());
30
       K::FT min_dist = t.segment(t.finite_edges_begin()).squared_length();
       for (EdgeIt e = t.finite_edges_begin(); e != t.finite_edges_end(); e++) {
33
            min_dist = min(min_dist, t.segment(e).squared_length());
35
36
       K::FT d = sqrt(min_dist * (100 * 100) / (2 * 2));
38
       cout << ceil_to_double(d) << endl;</pre>
   }
40
41
43
   int main() {
       int n;
44
       cout << fixed << setprecision(0);</pre>
45
46
       while (true) {
           cin >> n;
47
           if (n == 0) { break; }
48
49
            graypes(n);
   }
```

#### **Bistro**

#### Keywords— Delaunay Triangulation

```
#include <vector>
   #include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
3
   #include <CGAL/Delaunay_triangulation_2.h>
   typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
6
   typedef CGAL::Delaunay_triangulation_2<K>
                                                                     Triangulation;
   typedef Triangulation::Finite_faces_iterator
                                                                     Face_iterator;
   {\tt typedef} \  \, {\tt Triangulation::Edge\_iterator}
                                                                     EdgeIt;
   typedef K::Point_2
                                                                     Point;
   using namespace std;
   double ceil_to_double(const K::FT& x) {
15
16
       double a = ceil(CGAL::to_double(x));
       while (a+1 >= x) a -= 1;
18
       while (a < x) a += 1;
       return a;
   }
   void bistro(int n) {
23
       int m;
       vector < Point > r(n);
24
       Triangulation t;
26
       for (int i = 0; i < n; i++) {</pre>
28
            long x, y;
29
            cin >> x >> y;
            r[i] = Point(x, y);
       }
31
32
       t.insert(r.begin(), r.end());
34
       cin >> m;
       for (int i = 0; i < m; i++) {</pre>
36
            long x, y;
            cin >> x >> y;
            Point p = Point(x,y);
39
            K::FT dist = CGAL::squared_distance(p, t.nearest_vertex(p)->point());
40
            cout << ceil_to_double(dist) << endl;</pre>
41
42
43
   }
44
45
46
   int main() {
47
48
       int n;
       cout << fixed << setprecision(0);</pre>
49
50
        while (true) {
            cin >> n;
            if (n == 0) { break; }
            bistro(n);
53
       }
   }
```

#### Keywords— Delaunay Triangulation

```
#include <vector>
   #include <map>
   #include <stack>
3
   #include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
   #include <CGAL/Delaunay_triangulation_2.h>
   typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
   typedef CGAL::Delaunay_triangulation_2 < K >
                                                                   Triangulation;
   typedef Triangulation::Finite_faces_iterator
                                                                   FaceIt;
   typedef Triangulation::Edge_iterator
                                                                   EdgeIt:
   typedef Triangulation::Face_handle
                                                                   FaceH;
   typedef Triangulation::Vertex_handle
                                                                   VertexH;
   typedef K::Point_2
                                                                   Point:
   typedef K::Segment_2
                                                                   Segment;
   using namespace std;
18
   double ceil_to_double(const K::FT& x) {
       double a = ceil(CGAL::to_double(x));
        while (a+1 >= x) a -= 1;
        while (a < x) a += 1;</pre>
23
       return a:
   }
25
   void h1n1(int n) {
28
       vector < Point > infected(n);
30
       Triangulation t;
31
       int m;
       for (int i = 0; i < n; i++) {</pre>
           long x, y;
            cin >> x >> y;
36
            infected[i] = Point(x, y);
       t.insert(infected.begin(), infected.end());
38
       cin >> m;
40
41
       for (int i = 0; i < m; i++) {</pre>
            long x, y, d;
            cin >> x >> y >> d;
43
44
           Point q(x, y);
45
            bool result = false;
46
47
            if (CGAL::squared_distance(q, t.nearest_vertex(q)->point()) < d) {</pre>
48
                cout << "n";
49
50
                continue;
            }
           FaceH face_1 = t.locate(q);
            map<FaceH, bool> face_seen;
            stack<FaceH> face_stack;
58
            face_stack.push(face_1);
            while(!face_stack.empty()) {
60
                FaceH face = face_stack.top();
                face_stack.pop();
                // If you are placed on an infinite face, as you are not closer from d to the nearest
                // point, you can escape from the infected
                if (t.is_infinite(face)) {
66
                    result = true;
67
                    break:
68
                face_seen[face] = true;
                for (int j = 0; j < 3; j++) {
                    Segment s = t.segment(face, j);
74
                    // The point can not escape from this face through this edge of the triangulation
76
                    if (s.squared_length() < d*4) { continue; }</pre>
```

```
// If can scape through, take the neighbour face
78
                       FaceH neighbour = face->neighbor(j);
// If it has been seen continue
79
80
81
                       if (face_seen[neighbour]) { continue; }
                       // Put to the queue of faces to study if scapatory
                       face_stack.push(neighbour);
83
                  }
84
             }
85
86
              if (result) {
87
                  cout << "y";
88
89
              } else {
                  cout << "n";
90
91
92
93
         cout << endl;</pre>
94
    }
95
96
97
    int main() {
98
         int n;
99
100
         cout << fixed << setprecision(0);</pre>
         while (true) {
              cin >> n;
102
              if (n == 0) { break; }
             h1n1(n);
104
         }
105
    }
106
```

Keywords— Delaunay Triangulation, Nearest Neighbor

```
#include <vector>
   #include <map>
   #include <stack>
3
   #include <algorithm>
   #include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
   #include <CGAL/Delaunay_triangulation_2.h>
   #include <CGAL/nearest_neighbor_delaunay_2.h>
   typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
   typedef CGAL::Delaunay_triangulation_2<K>
                                                                  Triangulation;
   typedef Triangulation::Finite_faces_iterator
                                                                  FaceIt;
   typedef Triangulation::Edge_iterator
                                                                  EdgeIt;
   typedef Triangulation::Finite_vertices_iterator
                                                                  VertexIt:
   typedef Triangulation::Face_handle
   typedef Triangulation::Vertex_handle
                                                                  VertexH:
   typedef K::Point_2
                                                                  Point:
   typedef K::Segment_2
                                                                  Segment;
18
   using namespace std;
   double ceil_to_double(const K::FT& x) {
23
       double a = ceil(CGAL::to_double(x));
25
       while (a+1 >= x) a -= 1;
       while (a < x) a += 1;
       return a:
   }
28
   void germs(int n) {
31
       long 1, b, r, t;
       cin >> 1 >> b >> r >> t;
       vector < Point > bacteries(n);
       vector < K :: FT > distances(n):
       for (int i = 0; i < n; i++) {</pre>
36
           long x, y;
38
            cin >> x >> y;
            bacteries[i] = Point(x, y);
40
41
       Triangulation tri;
       tri.insert(bacteries.begin(), bacteries.end());
43
44
       int i = 0;
45
       for (VertexIt vi = tri.finite_vertices_begin(); vi != tri.finite_vertices_end(); vi++) {
46
            VertexH vh = vi;
47
           Point p = vh->point();
48
49
            // Take the min distance to the neirest neighbour
           K::FT min_distance;
            if (tri.number_of_vertices() > 1) {
                VertexH vn = CGAL::nearest_neighbor(tri, vh);
                min_distance = CGAL::squared_distance(vh->point(), vn->point()) / 4;
            } else {
               // In the case the germ is alone, initialize \min distance with the distance to one
                // corner (it will allways be greater than the distance to any of the boundaries)
                min_distance = CGAL::squared_distance(vh->point(), Point(1, b));
58
            // check with every boundary if the distance is less than the minimum
           \label{eq:min_distance} \mbox{min_distance, (p.x() - 1) * (p.x() - 1));}
            min_distance = min(min_distance, (p.x() - r) * (p.x() - r));
            min_distance = min(min_distance, (p.y() - t) * (p.y() - t));
            min_distance = min(min_distance, (p.y() - b) * (p.y() - b));
66
            distances[i++] = min_distance;
67
68
       sort(distances.begin(), distances.end());
       vector < double > dead_time(n);
       for (int i = 0; i < n; i++) {</pre>
           K::FT d = distances[i];
74
            long ti = ceil_to_double(sqrt(sqrt(d) - .5));
            dead_time[i] = ti;
       }
76
```

```
// Print results
78
79
            \texttt{cout} \ << \ \texttt{dead\_time} \ [0] \ << \ \texttt{"} \ \texttt{"} \ << \ \texttt{dead\_time} \ [n/2] \ << \ \texttt{"} \ \texttt{"} \ << \ \texttt{dead\_time} \ [n-1] \ << \ \texttt{endl};
80
     }
81
82
83
84
     int main() {
85
           int n;
            cout << fixed << setprecision(0);
while (true) {</pre>
86
87
                  cin >> n;
if (n == 0) { break; }
88
89
                   germs(n);
90
            }
91
92
     }
```

# **Stamps**

```
#include <vector>
   #include <cmath>
2
3
   #include <CGAL/Exact_predicates_exact_constructions_kernel.h>
   #include <CGAL/basic.h>
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
   #include <CGAL/Gmpz.h>
   // Choose exact integral type
   typedef CGAL::Gmpzf ET;
   // Program and solution types
   typedef CGAL::Quadratic_program <ET> Program;
   typedef CGAL::Quadratic_program_solution<ET> Solution;
   // Geometric types
   {\tt typedef} \ {\tt CGAL::Exact\_predicates\_exact\_constructions\_kernel}
                                                                      Κ:
   typedef K::Point_2
                                                                      Р;
   typedef K::Segment_2
                                                                      S;
18
   using namespace std;
23
   void stamps() {
       int 1, s, w; cin >> 1 >> s >> w;
25
        vector <P> lamps(1), stamps(s);
        vector <long > M(s);
28
        vector <S> walls(w);
        // Read data
30
        for (int i = 0; i < 1; i++) {</pre>
31
            long x, y; cin >> x >> y;
lamps[i] = P(x, y);
        for (int i = 0; i < s; i++) {</pre>
            long x, y;
cin >> x >> y; stamps[i] = P(x, y);
36
            cin >> M[i];
38
39
        for (int i = 0; i < w; i++) {</pre>
40
41
            long x_a, y_a, x_b, y_b;
            cin >> x_a >> y_a >> x_b >> y_b;
42
            walls[i] = S(P(x_a, y_a), P(x_b, y_b));
43
44
        }
45
        // \ {\tt Define \ quadratic \ program}
46
        Program lp (CGAL::SMALLER, true, 1, true, 1<<12);</pre>
47
        for (int i = 0; i < s; i++) {</pre>
                                                       // stamp index
48
                                                        // lamp index
            for (int j = 0; j < 1; j++) {</pre>
49
                S l_s(lamps[j], stamps[i]);
                                                       // lamp to stamp segment
50
                bool blocked = false;
                for (int k = 0; k < w; k++) {
                     if (CGAL::do_intersect(walls[k], l_s)) {
                         blocked = true;
                         break;
                     }
                }
58
60
                if (!blocked) {
                     double d = CGAL::to_double(1 / l_s.squared_length());
                     lp.set_a(j, i, d);
                     lp.set_a(j, i+s, d);
            }
66
            lp.set_b(i, M[i]);
            lp.set_r(i, CGAL::SMALLER);
68
            lp.set_b(s+i, 1);
            lp.set_r(s+i, CGAL::LARGER);
       }
        // Get solution
        Solution sol = CGAL::solve_linear_program(lp, ET());
74
        assert (sol.solves_linear_program(lp));
76
        if (sol.is_infeasible()) {
            cout << "no" << endl;
```

```
} else {
79
             cout << "yes" << endl;</pre>
80
81
    }
82
83
84
    int main() {
   int t; cin >> t;
   for (int i = 0; i < t; i++) {</pre>
85
86
87
             stamps();
88
89
    }
90
```

## 2.5 Advanced Flows

#### Real Estate Market

Keywords — Max Flow Min Cost

```
#include <iostream>
   #include <vector>
3
   #include <algorithm>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
6
   #include <boost/graph/successive_shortest_path_nonnegative_weights.hpp>
   #include <boost/graph/find_flow_cost.hpp>
8
   // Namespaces
9
   using namespace std;
   using namespace boost;
13
   // BGL Graph definitions
14
   // ===========
   // Graph Type with nested interior edge properties for Cost Flow Algorithms
   typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
18
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
        property < edge_capacity_t, long,</pre>
            property < edge_residual_capacity_t , long ,</pre>
                 property < edge_reverse_t , Traits::edge_descriptor ,</pre>
                     property <edge_weight_t, long> > > > Graph;
   // Interior Property Maps
   typedef property_map < Graph, edge_capacity_t >:: type
typedef property_map < Graph, edge_weight_t >:: type
                                                                  EdgeCapacityMap;
                                                                 EdgeWeightMap;
   typedef property_map < Graph, edge_residual_capacity_t >::type ResidualCapacityMap;
26
   {\tt typedef} \hspace{0.2cm} {\tt property\_map} < {\tt Graph} \hspace{0.1cm}, \hspace{0.2cm} {\tt edge\_reverse\_t>} : : {\tt type}
                                                                 ReverseEdgeMap;
   typedef graph_traits < Graph >:: vertex_descriptor
28
                                                                 Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
                                                                 Edge;
   typedef graph_traits < Graph > :: out_edge_iterator
                                                                  OutEdgeIt; // Iterator
30
31
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map, weight map and reverse edge map
   class EdgeAdder {
        Graph &G;
        EdgeCapacityMap &capacitymap;
38
39
        EdgeWeightMap &weightmap;
40
        ReverseEdgeMap &revedgemap;
41
   public:
        EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, EdgeWeightMap &weightmap, ReverseEdgeMap &
43
            revedgemap)
            : G(G), capacitymap(capacitymap), weightmap(weightmap), revedgemap(revedgemap) {}
45
        void addEdge(int u, int v, long c, long w) {
46
            Edge e, reverseE;
47
            tie(e, tuples::ignore) = add_edge(u, v, G);
48
49
            tie(reverseE, tuples::ignore) = add_edge(v, u, G);
            capacitymap[e] = c;
            weightmap[e] = w;
            capacitymap[reverseE] = 0;
            weightmap[reverseE] = -w;
            revedgemap[e] = reverseE;
            revedgemap[reverseE] = e;
        }
   };
58
   void real_estate() {
       int N, M, S;
63
        cin >> N >> M >> S;
65
        const int MAX = 100;
        Graph G(N+M+S+2):
        EdgeCapacityMap capacitymap = get(edge_capacity, G);
        EdgeWeightMap weightmap = get(edge_weight, G);
        ReverseEdgeMap revedgemap = get(edge_reverse, G);
        ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
        EdgeAdder eaG(G, capacitymap, weightmap, revedgemap);
        Vertex src = vertex(N+M+S, G);
```

```
75
        Vertex sink = vertex(N+M+S+1, G);
76
        // Store the graph
78
        for (int i = 0; i < N; i++) { eaG.addEdge(src, i, 1, 0); }</pre>
        for (int i = 0; i < S; i++) {
    long l; cin >> l;
80
             eaG.addEdge(N+M+i, sink, 1, 0);
81
        }
82
83
        for (int i = 0; i < M; i++) {</pre>
             int s; cin >> s;
84
             eaG.addEdge(N+i, N+M+s-1, 1, 0);
85
86
        for (int i = 0; i < N; i++) {</pre>
87
             for (int j = 0; j < M; j++) {</pre>
88
89
                 long b; cin >> b;
                 eaG.addEdge(i, N+j, 1, MAX-b);
90
             }
91
        successive_shortest_path_nonnegative_weights(G, src, sink);
94
        int cost = find_flow_cost(G);
        int flow = 0;
96
97
        // Iterate over all edges leaving the source to sum up the flow values.
        OutEdgeIt e, eend;
98
        for(tie(e, eend) = out_edges(vertex(src,G), G); e != eend; ++e) {
99
            flow += capacitymap[*e] - rescapacitymap[*e];
        cost = flow*MAX - cost;
         cout << flow << " " << cost << endl;</pre>
104
105
    }
107
    int main() {
        ios_base::sync_with_stdio(false);
        int T; cin >> T;
        for (int t=0; t < T; t++){</pre>
112
             real_estate();
113
    }
```

Keywords— Maximum Flow, Bipartite Matchings, DFS

```
#include <iostream>
2
   #include <vector>
3
   #include <queue>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/push_relabel_max_flow.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
14
   // Graph Type with nested interior edge properties for Flow Algorithms
   typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
16
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
        property < edge_capacity_t, long,</pre>
18
            property < edge_residual_capacity_t, long,</pre>
                property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
   // Interior Property Maps
   typedef property_map < Graph , edge_capacity_t >::type
                                                                EdgeCapacityMap;
   typedef property_map < Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph, edge_reverse_t>::type ReverseEdgeMap;
23
   typedef graph_traits < Graph >:: vertex_descriptor
                                                                Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
                                                                Edge;
   typedef graph_traits < Graph > :: out_edge_iterator
                                                                OutEdgeIt;
28
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map and reverse edge map
   class EdgeAdder {
       Graph &G;
        EdgeCapacityMap &capacitymap;
        ReverseEdgeMap &revedgemap;
36
38
   public:
        // to initialize the Object
        EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, ReverseEdgeMap &revedgemap):
40
41
            G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
       // to use the Function (add an edge)
43
        void addEdge(int from, int to, long capacity) {
44
            Edge e, reverseE;
45
            bool success;
46
            tie(e, success) = add_edge(from, to, G);
47
            tie(reverseE, success) = add_edge(to, from, G);
48
            capacitymap[e] = capacity;
49
50
            capacitymap[reverseE] = 0;
            revedgemap[e] = reverseE;
            revedgemap[reverseE] = e;
   };
   void satellites() {
58
       int g, s, 1;
       cin >> g >> s >> 1;
        Graph G(g+s+2);
        EdgeCapacityMap capacitymap = get(edge_capacity, G);
        ReverseEdgeMap revedgemap = get(edge_reverse, G);
        ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
        EdgeAdder eaG(G, capacitymap, revedgemap);
66
        Vertex src = vertex(g+s, G);
67
68
        Vertex sink = vertex(g+s+1, G);
       int from, to;
        for (int i = 0; i < 1; i++) {</pre>
            cin >> from >> to;
            eaG.addEdge(from, g + to, 1);
74
        for (int i = 0; i < g; i++) {
76
            eaG.addEdge(src, i, 1);
```

```
78
         for (int i = g; i < g + s; i++) {</pre>
              eaG.addEdge(i, sink, 1);
80
81
         push_relabel_max_flow(G, src, sink);
83
         // BFS to find vertex set {\tt S}
84
         \label{lem:vector} \mbox{vector} \mbox{<} \mbox{int} \mbox{>} \mbox{vis}(\mbox{g+s+2}, \mbox{ false}); \mbox{ // visited flags}
86
         std::queue<int> Q; // BFS queue (from std:: not boost::)
         vis[src] = true; // Mark the source as visited
87
88
         Q.push(src);
         while (!Q.empty()) {
89
              const int u = Q.front();
90
91
              Q.pop();
              OutEdgeIt ebeg, eend;
              for (tie(ebeg, eend) = out_edges(u, G); ebeg != eend; ++ebeg) {
                   const int v = target(*ebeg, G);
94
                   // Only follow edges with spare capacity
                   if (rescapacitymap[*ebeg] == 0 || vis[v]) continue;
96
97
                   vis[v] = true;
                   Q.push(v);
98
              }
99
100
         int count_g = 0, count_s = 0;
         vector<int> result;
         for (int i = 0; i < g; i++) {</pre>
              if (!vis[i]) {
                  count_g++;
                   result.push_back(i);
              }
108
         for (int i = g; i < g + s; i++) {</pre>
              if (vis[i]) {
                   count_s++;
                   result.push_back(i - g);
              }
         }
115
116
         cout << count_g << " " << count_s << endl;
for (int i = 0; i < result.size(); i++) {</pre>
118
              cout << result[i] << " ";</pre>
119
              if (i == result.size() - 1) cout << endl;</pre>
121
         }
    }
124
    int main() {
126
         ios_base::sync_with_stdio(false);
         int T; cin >> T;
         for (int t=0; t < T; t++){</pre>
128
              satellites();
129
    }
```

Keywords— Max Flow Min Cut, DFS

```
#include <iostream>
2
   #include <vector>
3
   #include <algorithm>
   #include <climits>
   #include <queue>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
8
   #include <boost/graph/cycle_canceling.hpp>
   #include <boost/graph/push_relabel_max_flow.hpp>
   #include <boost/graph/successive_shortest_path_nonnegative_weights.hpp>
   #include <boost/graph/find_flow_cost.hpp>
   // Namespaces
14
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
18
19
   // Graph Type with nested interior edge properties for Flow Algorithms
   typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
23
       property < edge_capacity_t, long,</pre>
           property < edge_residual_capacity_t, long,</pre>
               property < edge_reverse_t, Traits::edge_descriptor> > > Graph;
   // Interior Property Maps
   typedef property_map < Graph , edge_capacity_t >:: type
                                                             EdgeCapacityMap;
   typedef property_map < Graph , edge_residual_capacity_t >::type ResidualCapacityMap;
   typedef property_map < Graph , edge_reverse_t >::type
                                                             ReverseEdgeMap;
   typedef graph_traits < Graph >:: vertex_descriptor
30
                                                             Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
                                                             OutEdgeIt;
   typedef graph_traits < Graph > :: out_edge_iterator
   // Custom Edge Adder Class, that holds the references
   \ensuremath{//} to the graph, capacity map and reverse edge map
   // -----
36
   class EdgeAdder {
38
       Graph &G;
       EdgeCapacityMap &capacitymap;
       ReverseEdgeMap &revedgemap;
40
41
       // to initialize the Object
43
       {\tt EdgeAdder(Graph \& G, EdgeCapacityMap \& capacitymap, ReverseEdgeMap \& revedgemap):}
44
           G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
45
46
       // to use the Function (add an edge)
47
       void addEdge(int from, int to, long capacity) {
48
49
            Edge e, reverseE;
            bool success;
            tie(e, success) = add_edge(from, to, G);
            tie(reverseE, success) = add_edge(to, from, G);
            capacitymap[e] = capacity;
            capacitymap[reverseE] = 0;
            revedgemap[e] = reverseE;
            revedgemap[reverseE] = e;
       }
   };
58
   void algocoon() {
       int n, m; cin >> n >> m;
       Graph G(n);
       EdgeCapacityMap capacitymap = get(edge_capacity, G);
66
       ReverseEdgeMap revedgemap = get(edge_reverse, G);
       ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
67
68
       EdgeAdder eaG(G, capacitymap, revedgemap);
       for (int i = 0; i < m; i++) {</pre>
            int from, to, cost;
            cin >> from >> to >> cost;
            eaG.addEdge(from, to, cost);
74
76
       int best_src = -1, best_sink = -1, best_value = numeric_limits<int>::max();
       int flow;
```

```
78
        for (int i = 1; i < n; i++) {</pre>
             flow = push_relabel_max_flow(G, 0, i);
             if (flow < best_value) {</pre>
80
                 best_value = flow; best_src = 0; best_sink = i;
81
             flow = push_relabel_max_flow(G, i, 0);
83
             if (flow < best_value) {</pre>
84
                 best_value = flow; best_src = i; best_sink = 0;
86
        }
87
88
        flow = push_relabel_max_flow(G, best_src, best_sink);
89
90
        // BFS to find vertex set {\tt S}
91
        vector < bool > vis(n, false); // visited flags
        std::queue <int > Q; // BFS queue (from std:: not boost::)
        vis[best_src] = true; // Mark the source as visited
94
        Q.push(best_src);
        while (!Q.empty()) {
96
             const int u = Q.front();
97
             Q.pop();
98
99
             OutEdgeIt ebeg, eend;
             for (tie(ebeg, eend) = out_edges(u, G); ebeg != eend; ++ebeg) {
100
                 const int v = target(*ebeg, G);
102
                 // Only follow edges with spare capacity
                 if (rescapacitymap[*ebeg] == 0 || vis[v]) continue;
                 vis[v] = true;
                 Q.push(v);
             }
        }
108
        cout << flow << endl;</pre>
        cout << count(vis.begin(), vis.end(), true);</pre>
110
        for (int i = 0; i < n; ++i) {</pre>
             if (vis[i]) cout << " " << i;</pre>
113
        }
        cout << endl;</pre>
114
    }
115
116
    int main() {
118
        ios_base::sync_with_stdio(false);
        int T; cin >> T;
        for (int t=0; t < T; t++){</pre>
121
             algocoon();
    }
```

#### Canteen

## Keywords— Max Flow Min Cost

```
#include <iostream>
2
   #include <vector>
3
   #include <algorithm>
   #include <string>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/successive_shortest_path_nonnegative_weights.hpp>
   #include <boost/graph/find_flow_cost.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
16
   // Graph Type with nested interior edge properties for Cost Flow Algorithms
   typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
18
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
       property < edge_capacity_t, long,</pre>
           property < edge_residual_capacity_t, long,</pre>
               property < edge_reverse_t , Traits::edge_descriptor ,</pre>
23
                   property <edge_weight_t, long> > > > Graph;
   // Interior Property Maps
24
   typedef property_map < Graph , edge_capacity_t >:: type
                                                           EdgeCapacityMap;
   typedef property_map < Graph , edge_reverse_t >: : type
                                                           ReverseEdgeMap;
   typedef graph_traits < Graph > :: vertex_descriptor
                                                           Vertex;
30
   typedef graph_traits < Graph > :: edge_descriptor
                                                           Edge;
   typedef graph_traits < Graph >:: out_edge_iterator
                                                           OutEdgeIt; // Iterator
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map, weight map and reverse edge map
   // -----
36
   class EdgeAdder {
38
       Graph &G;
       EdgeCapacityMap &capacitymap;
       EdgeWeightMap &weightmap:
40
41
       ReverseEdgeMap &revedgemap;
   public:
43
       EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, EdgeWeightMap &weightmap, ReverseEdgeMap &
44
           revedgemap)
           : \ G(G) \ , \ capacitymap(capacitymap) \ , \ weightmap(weightmap) \ , \ revedgemap(revedgemap) \ \{\}
45
46
       void addEdge(int u, int v, long c, long w) {
47
48
           Edge e, reverseE;
           tie(e, tuples::ignore) = add_edge(u, v, G);
49
           tie(reverseE, tuples::ignore) = add_edge(v, u, G);
           capacitymap[e] = c;
           weightmap[e] = w;
           capacitymap[reverseE] = 0;
           weightmap[reverseE] = -w;
           revedgemap[e] = reverseE;
           revedgemap[reverseE] = e;
       }
   };
58
59
   void canteen() {
       int n; cin >> n;
64
65
       const int MAX_PRICE = 20;
66
67
       vector < int > a(n), c(n), s(n), p(n), v(n-1), e(n-1);
       for (int i = 0; i < n; i++) { cin >> a[i] >> c[i]; }
       for (int i = 0; i < n; i++) { cin >> s[i] >> p[i]; }
       for (int i = 0; i < n-1; i++) { cin >> v[i] >> e[i]; }
       // Create Graph and Maps
       Graph G(n+2);
       EdgeCapacityMap capacitymap = get(edge_capacity, G);
       EdgeWeightMap weightmap = get(edge_weight, G);
       ReverseEdgeMap revedgemap = get(edge_reverse, G);
```

```
77
        ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
78
        EdgeAdder eaG(G, capacitymap, weightmap, revedgemap);
79
        Vertex src = n, sink = n+1;
80
        for (int i = 0; i < n; i++) {</pre>
81
            eaG.addEdge(src, i, a[i], c[i]);
82
            eaG.addEdge(i, sink, s[i], MAX_PRICE-p[i]);
            if (i < n-1) { eaG.addEdge(i, i+1, v[i], e[i]); }</pre>
84
85
86
        // Compute flow and cost
87
        successive_shortest_path_nonnegative_weights(G, src, sink);
88
        int cost = find_flow_cost(G);
89
        int flow = 0;
90
91
        for (int i = 0; i < n; i++) {</pre>
93
            Edge ee; bool success;
            tie(ee, success) = edge(i, sink, G);
            int f = capacitymap[ee] - rescapacitymap[ee];
            flow += f;
96
            cost -= f * MAX_PRICE;
97
        }
98
99
        cost = -cost;
        int total_s = accumulate(s.begin(), s.end(), 0);
        string text = (total_s == flow) ? "possible " : "impossible ";
        cout << text << flow << " " << cost << endl;
103
    }
104
106
    int main() {
        ios_base::sync_with_stdio(false);
        int T; cin >> T;
        for (int t=0; t < T; t++){</pre>
109
            canteen();
    }
112
```

## Casino Royale

**Keywords**— Max Flow Min Cost

```
#include <iostream>
   #include <vector>
3
   #include <algorithm>
   #include <string>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/successive_shortest_path_nonnegative_weights.hpp>
   #include <boost/graph/find_flow_cost.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
16
   // Graph Type with nested interior edge properties for Cost Flow Algorithms
   typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
18
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
       property < edge_capacity_t, long,</pre>
           property < edge_residual_capacity_t, long,</pre>
               property < edge_reverse_t , Traits::edge_descriptor ,</pre>
                   property <edge_weight_t, long> > > > Graph;
   // Interior Property Maps
24
   typedef property_map < Graph , edge_capacity_t >:: type
                                                           EdgeCapacityMap;
   typedef property_map < Graph , edge_reverse_t >: : type
                                                           ReverseEdgeMap;
   typedef graph_traits < Graph > :: vertex_descriptor
                                                           Vertex;
30
   typedef graph_traits < Graph > :: edge_descriptor
                                                           Edge;
   typedef graph_traits < Graph >:: out_edge_iterator
                                                           OutEdgeIt; // Iterator
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map, weight map and reverse edge map
   // -----
36
   class EdgeAdder {
38
       Graph &G;
       EdgeCapacityMap &capacitymap;
       EdgeWeightMap &weightmap:
40
41
       ReverseEdgeMap &revedgemap;
   public:
43
       EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, EdgeWeightMap &weightmap, ReverseEdgeMap &
44
           revedgemap)
           : G(G), capacitymap(capacitymap), weightmap(weightmap), revedgemap(revedgemap) {}
45
46
       Edge addEdge(int u, int v, long c, long w) {
47
48
           Edge e, reverseE;
           tie(e, tuples::ignore) = add_edge(u, v, G);
49
           tie(reverseE, tuples::ignore) = add_edge(v, u, G);
           capacitymap[e] = c;
           weightmap[e] = w;
           capacitymap[reverseE] = 0;
           weightmap[reverseE] = -w;
           revedgemap[e] = reverseE;
           revedgemap[reverseE] = e;
           return e;
58
   };
   void casino_royale() {
       int n, m, 1;
       cin >> n >> m >> 1;
65
       const int MAX_PRIORITY = 1<<7;</pre>
66
67
       // Create Graph and Maps
       Graph G(n+2);
       EdgeCapacityMap capacitymap = get(edge_capacity, G);
       EdgeWeightMap weightmap = get(edge_weight, G);
       ReverseEdgeMap revedgemap = get(edge_reverse, G);
       ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
       EdgeAdder eaG(G, capacitymap, weightmap, revedgemap);
       Vertex v_source = n, v_target = n + 1;
       for (int i = 0; i < n-1; i++) { eaG.addEdge(i, i+1, 1, MAX_PRIORITY); }</pre>
```

```
eaG.addEdge(v_source, 0, 1, 0);
77
        eaG.addEdge(n-1, v_target, 1, 0);
78
79
80
        // Add the missions edges
        int x, y, q;
for (int i = 0; i < m; i++) {</pre>
81
82
             cin >> x >> y >> q;
83
             eaG.addEdge(x, y, 1, (MAX_PRIORITY*(y-x) - q));
84
85
86
        // Find MaxFlowMinCost
87
88
         successive_shortest_path_nonnegative_weights(G, v_source, v_target);
        int cost = find_flow_cost(G), flow = 0;
89
        OutEdgeIt e, eend;
90
91
        for(tie(e, eend) = out_edges(vertex(v_source,G), G); e != eend; ++e) {
             flow += capacitymap[*e] - rescapacitymap[*e];
        }
93
        cost -= MAX_PRIORITY * (n-1) * flow;
        cout << -cost << endl;</pre>
95
    }
96
97
    int main() {
98
99
        ios_base::sync_with_stdio(false);
        int T; cin >> T;
for (int t=0; t < T; t++){</pre>
             casino_royale();
        }
103
    }
104
```

## Chapter 3

# **Exam Preparation**

## **Odd Route**

```
// STL includes
   #include <vector>
   #include <iostream>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/dijkstra_shortest_paths.hpp>
   // Namespaces
9
   using namespace std;
   using namespace boost;
   // Directed graph with integer weights on edges.
13
   typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_weight_t, int> > Graph;
14
15
   typedef graph_traits < Graph >:: vertex_descriptor
                                                          Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
16
   // Property map edge -> weight
   typedef property_map <Graph, edge_weight_t>::type
                                                          WeightMap;
18
   void odd_route() {
       int n, m; cin >> n >> m;
       int s, t; cin >> s >> t;
       Graph G(4*n):
26
       WeightMap weightmap = get(edge_weight, G);
28
       Split all vertices u, 0 \le u \le V(G) into 4 parts
       4*u (even length , even weight)
30
       4*u+1 (even length, odd weight)
       4*u+2 (odd length, even weight)
       4*u+3 (odd length, odd weight)
34
       */
36
       Edge e;
       int u, v, w;
       for (int i = 0; i < m; i++) {</pre>
38
            cin >> u >> v >> w;
            tie(e, tuples::ignore) = add_edge(4*u,
                                                        4*v + 2 + w%2, G); weightmap[e] = w;
40
            tie(e, tuples::ignore) = add_edge(4*u + 1, 4*v + 3 - w%2, G); weightmap[e] = w;
41
42
            tie(e, tuples::ignore) = add_edge(4*u + 2, 4*v + w%2,
                                                                         G); weightmap[e] = w;
            tie(e, tuples::ignore) = add_edge(4*u + 3, 4*v + 1 - w%2, G); weightmap[e] = w;
43
44
45
       vector<int> dist(4 * n), pred(4 * n);
46
47
       dijkstra_shortest_paths(G, 4*s,
48
                                 predecessor_map(make_iterator_property_map(pred.begin(),
49
                                 get(vertex_index, G)))
                                   .distance_map(make_iterator_property_map(dist.begin(),
                                     get(vertex_index, G))
       if (dist[4*t + 3] == INT_MAX)
         cout << "no" << endl;
56
         cout << dist[4*t + 3] << endl;</pre>
58
```

```
60
61
61    int main() {
62        ios_base::sync_with_stdio(false);
63        int T; cin >> T;
64        for (int t=0; t < T; t++){
65             odd_route();
66        }
67</pre>
```

## Light the Stage

```
#include <vector>
   #include <iostream>
   #include <algorithm>
   #include <limits>
   #include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
6
   #include <CGAL/Delaunay_triangulation_2.h>
   {\tt typedef} \ {\tt CGAL::Exact\_predicates\_inexact\_constructions\_kernel}
                                                                          K;
   typedef CGAL::Delaunay_triangulation_2<K>
                                                                          Triangulation;
   typedef K::Point_2
   using namespace std;
16
   void light_the_stage() {
       int m, n, h;
        cin >> m >> n;
18
       vector <P> l(n), p(m);
       vector<int> r(m);
       vector < int > dead_time(m, INT_MAX);
       // Read input
       int x, y;
        for (int i = 0; i < m; i++) {</pre>
            cin >> x >> y;
            p[i] = P(x, y);
28
29
            cin >> r[i];
       }
31
        cin >> h;
32
       for (int i = 0; i < n; i++) {</pre>
            cin >> x >> y;
            1[i] = P(x, y);
36
        // Create triangulation for the lamps points
       Triangulation tri;
        tri.insert(l.begin(), l.end());
40
        \ensuremath{//} Iterate over all participants and look for the closest lamp
41
42
        for (int i = 0; i < m; i++) {</pre>
            P v = tri.nearest_vertex(p[i])->point();
43
            double d_2 = CGAL::squared_distance(v, p[i]);
44
            double d = (r[i] + h);
45
            double d_max = d * d;
46
47
48
            if (d_max <= d_2) continue;</pre>
50
            for (int j = 0; j < n; j++) {</pre>
                 double dist = CGAL::squared_distance(p[i], 1[j]);
                 if (d_max > dist) {
                     dead_time[i] = j;
                     break;
                }
            }
56
        int winner_time = *std::max_element(dead_time.begin(), dead_time.end());
        // Print result
61
        for (int i = 0; i < m; i++) {</pre>
            if (dead_time[i] == winner_time) cout << i << " ";</pre>
64
        cout << endl;
   }
66
67
69
   int main() {
        std::ios_base::sync_with_stdio(false);
        int t; cin >> t;
        for (int i = 0; i < t; i++) {</pre>
            light_the_stage();
74
   }
```

## Bonus Level

```
// Includes
   // ======
   // STL includes
3
   #include <iostream>
   #include <cstdlib>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/successive_shortest_path_nonnegative_weights.hpp>
   #include <boost/graph/find_flow_cost.hpp>
   // Namespaces
   using namespace boost;
   using namespace std;
   // BGL Graph definitions
   // =========
   // Graph Type with nested interior edge properties for Cost Flow Algorithms
   typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
18
       property < edge_capacity_t, long,
            property<edge_residual_capacity_t, long,</pre>
                property < edge_reverse_t , Traits::edge_descriptor ,</pre>
                    property <edge_weight_t, long> > > > Graph;
23
   // Interior Property Maps
   typedef property_map < Graph , edge_capacity_t >:: type
                                                               EdgeCapacityMap:
   typedef property_map < Graph , edge_weight_t >::type
                                                               EdgeWeightMap;
   typedef property_map < Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph, edge_reverse_t>::type ReverseEdgeMap;
   typedef graph_traits < Graph >:: vertex_descriptor
                                                               Vertex;
28
   typedef graph_traits < Graph > :: edge_descriptor
                                                               Edge;
   typedef graph_traits<Graph>::out_edge_iterator OutEdgeIt; // Iterator
30
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map, weight map and reverse edge map
   // ==========
   class EdgeAdder {
       Graph &G;
       EdgeCapacityMap &capacitymap;
       EdgeWeightMap &weightmap;
       ReverseEdgeMap &revedgemap;
40
   public:
41
       EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, EdgeWeightMap &weightmap, ReverseEdgeMap &
           revedgemap)
            : G(G), capacitymap(capacitymap), weightmap(weightmap), revedgemap(revedgemap) {}
44
       void addEdge(int u, int v, long c, long w) {
45
            Edge e, reverseE;
46
            tie(e, tuples::ignore) = add_edge(u, v, G);
47
            tie(reverseE, tuples::ignore) = add_edge(v, u, G);
48
            capacitymap[e] = c;
49
            weightmap[e] = w;
            capacitymap[reverseE] = 0;
            weightmap[reverseE] = -w;
            revedgemap[e] = reverseE;
            revedgemap[reverseE] = e;
   };
   void bonus_level() {
58
59
       int n; cin >> n;
       const int MAX_COST = 100;
       // Create Graph and Maps
       Graph G(3 * n * n);
       EdgeCapacityMap capacitymap = get(edge_capacity, G);
65
       EdgeWeightMap weightmap = get(edge_weight, G);
       ReverseEdgeMap revedgemap = get(edge_reverse, G);
67
       EdgeAdder eaG(G, capacitymap, weightmap, revedgemap);
       Vertex src = add_vertex(G);
       Vertex sink = add_vertex(G);
       int a, pos;
       for (int i = 0; i < n; i++) {</pre>
            for (int j = 0; j < n; j++) {</pre>
                cin >> a;
                pos = 3 * j + 3 * n * i;
```

```
eaG.addEdge(pos, pos + 1, 1, MAX_COST - a);
eaG.addEdge(pos, pos + 2, 1, MAX_COST);
if (i != n - 1) {
77
 78
 79
                             eaG.addEdge(pos + 1, pos + 3 * n, 1, 0);
 80
                             eaG.addEdge(pos + 2, pos + 3 * n, 1, 0);
 81
                       }
 82
                       if (j != n -1) {
                             eaG.addEdge(pos + 1, pos + 3, 1, 0);
eaG.addEdge(pos + 2, pos + 3, 1, 0);
 84
 85
 86
                 }
 87
 88
           eaG.addEdge(src, 0, 2, 0);
 89
           eaG.addEdge(3 * n * n - 1, sink, 1, 0);
eaG.addEdge(3 * n * n - 2, sink, 1, 0);
90
91
           successive_shortest_path_nonnegative_weights(G, src, sink);
93
           int cost = find_flow_cost(G);
cout << - cost + 2 * (2 * n - 1) * MAX_COST << endl;</pre>
94
95
96
     }
97
98
99
     int main() {
           int T; cin >> T;
for (int t = 0; t < T; t++){</pre>
                 bonus_level();
103
     }
104
```

```
// Includes
   // ======
   // STL includes
3
   #include <iostream>
   #include <vector>
   #include <algorithm>
   #include <climits>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/connected_components.hpp>
   // CGAL
   #include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
   #include <CGAL/Delaunay_triangulation_2.h>
   #include <CGAL/Triangulation_vertex_base_with_info_2.h>
   // Namespaces
   using namespace std;
   using namespace boost;
18
   // Directed graph with integer weights on edges.
   typedef adjacency_list<vecS, vecS, undirectedS,</pre>
       no_property , property <edge_weight_t , int> >
                                                              Graph;
                                                              Vertex; // Vertex type
23
   typedef graph_traits < Graph > :: vertex_descriptor
   typedef graph_traits < Graph >:: edge_descriptor
                                                              Edge; // Edge type
   typedef graph_traits < Graph > :: edge_iterator
                                                              EdgeIt; // Edge iterator
   // Property map edge -> weight
   typedef property_map < Graph , edge_weight_t >::type
                                                              WeightMap:
28
   typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
30
   typedef K::Point_2
                                                                  Vb:
   typedef CGAL::Triangulation_vertex_base_with_info_2 <int, K>
                                                                  Fb;
   typedef CGAL::Triangulation_face_base_2 <K>
   typedef CGAL::Triangulation_data_structure_2 < Vb , Fb >
                                                                  Tds;
                                                                  Triangulation:
   typedef CGAL::Delaunay_triangulation_2 < K, Tds >
   typedef Triangulation::Edge_iterator
                                                                  Edge_iterator;
   typedef Triangulation::Vertex_handle
                                                                  VertexH;
   int get_k_planets(int t, vector<pair<P, int> >& planets, const int r, const int n) {
       assert(t > 0):
40
41
       assert(t < n):
       int n_not_conquered = n - t;
43
       Graph G(n_not_conquered);
44
45
46
       Triangulation tr;
       tr.insert(planets.begin(), planets.begin() + n_not_conquered);
47
48
49
       for (Edge_iterator e = tr.finite_edges_begin(); e != tr.finite_edges_end(); e++) {
           VertexH v1 = e->first->vertex((e->second + 1) % 3);
           VertexH v2 = e->first->vertex((e->second + 2) % 3);
           double dist = CGAL::squared_distance(v1->point(), v2->point());
           double rr = r;
           double min_dist = rr * rr;
           if (dist <= min_dist) {</pre>
                add_edge(v1->info(), v2->info(), G);
           }
       // Analyze components
       vector < int > component(n_not_conquered);
       int n_components = connected_components(G, &component[0]);
       vector<int> sizes(n_components, 0);
       int largest = -1;
       for (int i = 0; i < n_not_conquered; i++) {</pre>
           int c = component[i];
66
           sizes[c]++;
           largest = max(largest, sizes[c]);
68
       return min(t, largest);
   }
74
   int search_t(int begin, int end, vector<pair<P, int> >& planets, const int r, const int n) {
       if (begin + 1 == end)
76
           return max(get_k_planets(begin, planets, r, n), get_k_planets(end, planets, r, n));
       else {
```

```
int middle = (begin + end) / 2;
78
              int b = get_k_planets(middle, planets, r, n);
if (b == middle) return search_t(middle, end, planets, r, n);
79
80
81
              else return search_t(begin, middle, planets, r, n);
         }
82
    }
83
84
    void sith() {
85
86
         int n, r; cin >> n >> r;
87
         vector<pair<P, int> > p(n);
88
         long x, y;
for (int i = n-1; i >= 0; i--) {
89
90
              cin >> x >> y;
91
92
              p[i] = make_pair(P(x, y), i);
93
94
         int t = search_t(0, n/2, p, r, n);
95
         cout << t << endl;
96
97
    }
98
99
100
    int main() {
         int T; cin >> T;
for (int t = 0; t < T; t++){</pre>
102
              sith();
104
    }
```

## Clues

```
#include <vector>
   #include <map>
   #include <stack>
3
   #include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
   #include <CGAL/Delaunay_triangulation_2.h>
   #include <CGAL/Triangulation_vertex_base_with_info_2.h>
   using namespace std;
   // CGAL typedefs
   typedef CGAL::Exact_predicates_inexact_constructions_kernel
   typedef pair<int, bool>
                                                                          info_t;
   typedef CGAL::Triangulation_vertex_base_with_info_2 < info_t, K>
                                                                          Vb:
   typedef CGAL::Triangulation_data_structure_2 < Vb >
                                                                          Tds;
   typedef CGAL::Delaunay_triangulation_2 < K, Tds >
                                                                          Triangulation:
   typedef Triangulation::Finite_faces_iterator
                                                                          FaceIt:
   typedef Triangulation::Edge_iterator
                                                                          EdgeIt;
   typedef Triangulation::Face_handle
                                                                          FaceH:
   typedef Triangulation::Vertex_handle
                                                                          VertexH;
   typedef Triangulation::Vertex_circulator
                                                                          VertexCirculator;
   typedef K::Point_2
                                                                          Point:
   typedef K::Segment_2
                                                                          Segment:
   typedef K::Triangle_2
                                                                          Triangle:
   bool has_interference(Triangulation const & trg, K::FT const & rr) {
       for (auto e = trg.finite_edges_begin(); e != trg.finite_edges_end(); e++)
28
           if (trg.segment(*e).squared_length() <= rr) return true;</pre>
       return false;
   }
31
   bool try_two_colors(Triangulation & trg, K::FT const & rr) {
      for (auto v = trg.finite_vertices_begin(); v != trg.finite_vertices_end(); v++)
           v->info() = { 0, false };
       int components = 0;
       Triangulation trg0, trg1;
38
       for (auto v = trg.finite_vertices_begin(); v != trg.finite_vertices_end(); v++) {
           if (v->info().first == 0) {
40
41
                v->info().first = ++components;
                vector < VertexH > stack(1, v);
43
                do {
                    VertexH h = stack.back();
44
                    stack.pop_back();
45
                    VertexCirculator c = trg.incident_vertices(h);
46
                    do if (!trg.is_infinite(c) && CGAL::squared_distance(h->point(), c->point()) <= rr</pre>
47
                        ) {
                        if (c->info() == h->info()) return false;
                        if (c->info().first == 0) {
49
                            stack.push_back(c);
                            c->info() = { components, !h->info().second };
                    } while (++c != trg.incident_vertices(h));
                } while (!stack.empty());
           if (v->info().second) trg1.insert(v->point());
           else trg0.insert(v->point());
58
59
       7
       return !has_interference(trg0, rr) && !has_interference(trg1, rr);
   }
   void clues() {
65
       int n, m;
       long r;
       cin >> n >> m >> r;
       K::FT rr(r*r);
       vector < Point > stations(n);
       for (int i = 0; i < n; i++) cin >> stations[i];
       Triangulation trg;
       trg.insert(stations.begin(), stations.end());
       bool success = try_two_colors(trg, rr);
```

```
for (int i = 0; i < m; i++) {</pre>
77
             Point holmes, watson;
78
             cin >> holmes >> watson;
79
80
             if (success) {
81
                 if (CGAL::squared_distance(holmes, watson) <= rr) {</pre>
82
                      cout << "y"; continue;</pre>
                 }
84
85
                 auto holmes_station = trg.nearest_vertex(holmes);
86
                 auto watson_station = trg.nearest_vertex(watson);
87
88
                  if (holmes_station->info().first == watson_station->info().first &&
                      CGAL::squared_distance(holmes_station->point(), holmes) <= rr &&
89
                      CGAL::squared_distance(watson_station->point(), watson) <= rr)</pre>
90
91
                 {
                      cout << "y"; continue;</pre>
                 }
93
             cout << "n";
95
96
        cout << endl;</pre>
97
98
99
    }
    int main() {
        ios_base::sync_with_stdio(false);
103
104
         int T; cin >> T;
        for (int t = 0; t < T; t++) {</pre>
106
             clues();
        }
    }
```

## Punch

```
#include <iostream>
   #include <cassert>
   #include <CGAL/basic.h>
3
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
   #include <CGAL/Gmpz.h>
6
   // choose exact integral type
   typedef CGAL::Gmpz ET;
9
   // program and solution types
   typedef CGAL::Quadratic_program <int> Program;
   typedef CGAL::Quadratic_program_solution<ET> Solution;
15
   using namespace std;
16
   void punch(){
18
       int n, k; cin >> n >> k;
       Program qp (CGAL::EQUAL, true, 0, false, 0);
       int c, v;
       for (int i = 0; i < n; i++) {</pre>
            cin >> c >> v;
23
            qp.set_c(i, c);
24
            qp.set_a(i, 0, v);
26
            // qp.set_d(i, i, 1);
       qp.set_b(0, k);
28
29
       Solution s = CGAL::solve_linear_program(qp, ET());
31
       assert(s.solves_linear_program(qp));
32
       assert(s.is_optimal());
       // CGAL::Quadratic_program_solution<ET>::Variable_value_iterator opt = s.variable_values_begin
34
           ();
       // int value = 0;
       // for (; opt != s.variable_values_end(); opt++) {
36
               int tmp = int(CGAL::to_double(*(opt)));
if (tmp > 0) value++;
       //
       //
38
       // }
39
       // cout << value << endl;
40
41
        cout << CGAL::to_double(s.objective_value()) << endl;</pre>
   }
43
44
45
   int main() {
46
47
       ios_base::sync_with_stdio(false);
       int T; cin >> T;
48
49
       for (int i = 0; i < T; i++) {</pre>
            punch();
       }
52
   }
```

## Carsharing

```
#include <iostream>
   #include <vector>
   #include <set>
3
   #include <map>
   // BGL include
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/successive_shortest_path_nonnegative_weights.hpp>
   #include <boost/graph/find_flow_cost.hpp>
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
   // Graph Type with nested interior edge properties for Cost Flow Algorithms
   typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
       property < edge_capacity_t, long,</pre>
18
           property < edge_residual_capacity_t , long ,</pre>
               property < edge_reverse_t , Traits::edge_descriptor ,</pre>
                   property <edge_weight_t, long> > > > Graph;
   // Interior Property Maps
23
   typedef property_map < Graph , edge_capacity_t >:: type
                                                             EdgeCapacityMap;
   typedef property_map < Graph , edge_weight_t >::type
                                                             EdgeWeightMap;
   typedef property_map < Graph , edge_residual_capacity_t >:: type ResidualCapacityMap;
   typedef property_map < Graph , edge_reverse_t >: : type
                                                             ReverseEdgeMap;
   typedef graph_traits < Graph >:: vertex_descriptor
                                                             Vertex:
   typedef graph_traits < Graph > :: edge_descriptor
                                                             Edge;
   typedef graph_traits < Graph > :: out_edge_iterator
                                                             OutEdgeIt; // Iterator
30
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map, weight map and reverse edge map
   class EdgeAdder {
       Graph &G;
       EdgeCapacityMap &capacitymap;
       EdgeWeightMap &weightmap;
38
       ReverseEdgeMap &revedgemap;
   public:
40
41
       EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, EdgeWeightMap &weightmap, ReverseEdgeMap &
           revedgemap)
           : G(G), capacitymap(capacitymap), weightmap(weightmap), revedgemap(revedgemap) {}
42
       void addEdge(int u, int v, long c, long w) {
44
45
           Edge e, reverseE;
           tie(e, tuples::ignore) = add_edge(u, v, G);
46
           tie(reverseE, tuples::ignore) = add_edge(v, u, G);
47
48
           capacitymap[e] = c;
           weightmap[e] = w;
49
           capacitymap[reverseE] = 0;
           weightmap[reverseE] = -w;
           revedgemap[e] = reverseE;
           revedgemap[reverseE] = e;
       }
   };
   struct Booking {
       int s, t, d, a, p;
58
59
   };
   void carsharing() {
61
       int N, S;
       cin >> N >> S;
65
       const int MAXL = 100, MAXT = 100000, MAXP = 100;
       const int INF = MAXL*S;
67
       // Define variables to store data
       vector<int> L(S):
       vector < Booking > B;
       vector<set<int> > times(S);
       vector < map < int , int > > M(S);
       vector < int > psum(S+1);
       // Read data
76
       for (int i = 0; i < S; i++) {</pre>
```

```
cin >> L[i];
             times[i].insert(0); times[i].insert(MAXT);
78
79
        7
80
        int s, t, d, a, p;
for (int i = 0; i < N; i++) {</pre>
81
82
            cin >> s >> t >> d >> a >> p;
             s--; t--;
             times[s].insert(d); times[t].insert(a);
            B.push_back({s,t,d,a,p});
86
        7
87
88
        for (int s = 0; s < S; s++) {</pre>
89
             int i = 0;
             for (auto &t : times[s]) {
                 M[s][t] = i;
                 i++;
             psum[s+1] = psum[s] + M[s].size();
        }
96
97
        int T = psum.back();
98
        int v_source = T, v_target = T + 1;
99
        Graph G(T+2);
        EdgeCapacityMap capacitymap = get(edge_capacity, G);
        EdgeWeightMap weightmap = get(edge_weight, G);
        ReverseEdgeMap revedgemap = get(edge_reverse, G);
104
        ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
        {\tt EdgeAdder\ eaG(G,\ capacitymap,\ weightmap,\ revedgemap);}
        for (int i = 0; i < S; i++) {</pre>
             eaG.addEdge(v_source, psum[i], L[i], 0);
108
             eaG.addEdge(psum[i+1]-1, v_target, INF, 0);
109
             int it = -1, lastt = 0;
             for (auto &t : times[i]) {
                 if (it != -1) {
                     eaG.addEdge(psum[i]+it, psum[i]+it+1, INF, MAXP*(t-lastt));
                 }
114
                 it++; lastt = t;
            }
        }
118
        for (int i = 0; i < N; i++) {</pre>
             eaG.addEdge(psum[B[i].s] + M[B[i].s][B[i].d],
120
                         psum[B[i].t] + M[B[i].t][B[i].a],
                         1, ((B[i].a - B[i].d) * MAXP) - B[i].p);
        successive_shortest_path_nonnegative_weights(G, v_source, v_target);
        int flow = 0;
        // Iterate over all edges leaving the source to sum up the flow values.
        OutEdgeIt e, eend;
128
        for(tie(e, eend) = out_edges(vertex(v_source,G), G); e != eend; ++e) {
            flow += capacitymap[*e] - rescapacitymap[*e];
        }
        int cost = MAXP * MAXT * flow - find_flow_cost(G);
        cout << cost << endl;</pre>
    }
    int main() {
136
        ios_base::sync_with_stdio(false);
138
        int T; cin >> T;
        for (int t = 0; t < T; t++) {</pre>
139
             carsharing();
        }
141
    }
```

## **Planks**

```
#include <algorithm>
   #include <vector>
   #include <iostream>
   using namespace std;
6
   typedef vector<vector<int> > vecvec;
   void back_track(vector<int>& planks, vecvec& assignent, vecvec& F, int id, int ubound) {
9
        if (id >= ubound) {
            vector < int > tuple(4, 0);
            for (int i = 0; i < 4; i++) {</pre>
                for (int j = 0; j < assignent[i].size(); j++)</pre>
                    tuple[i] += planks[assigment[i][j]];
15
16
            F.push_back(tuple);
            return;
18
       }
       for (int side = 0; side < 4; side++) {</pre>
            assigment[side].push_back(id);
            back_track(planks, assigment, F, id+1, ubound);
23
            assigment[side].pop_back();
24
   }
   void planks() {
       int n; cin >> n;
28
29
       vector < int > planks(n);
31
       int sum = 0;
32
       long long n_sol = 0;
       for (int i = 0; i < n; i++) { cin >> planks[i]; sum += planks[i]; }
34
       if (sum % 4 != 0) {
36
            cout << 0 << endl;
            return:
       }
40
       vecvec F1, F2, assignent1(4), assignent2(4);
41
42
       back_track(planks, assigment1, F1, 0, n/2);
       back_track(planks, assigment2, F2, n/2, n);
43
       sort(F2.begin(), F2.end());
44
45
       for (int idx = 0; idx < F1.size(); idx++) {</pre>
46
            vector<int> member = F1[idx];
47
48
            for (int i = 0; i < 4; i++)</pre>
                member[i] = sum/4 - member[i];
50
            pair < vecvec :: iterator , vecvec :: iterator > bounds ;
            bounds = equal_range(F2.begin(), F2.end(), member);
            n_sol += distance(bounds.first, bounds.second);
        cout << n_sol / 24 << endl;
56
   }
58
   int main() {
       ios_base::sync_with_stdio(false);
        int T; cin >> T;
61
       for (int t=0; t < T; t++){</pre>
63
            planks();
       }
64
   }
```

## New Tiles

```
#include <iostream>
   #include <vector>
3
   #include <algorithm>
   using namespace std;
6
   void new_tiles() {
9
10
       int h, w;
        cin >> h >> w;
^{12}
        vector < uint32_t > floor_plan(h, 0);
        int p;
        for (int i = 0; i < h; i++) {
15
            for (int j = 0; j < w; j++) {
16
                 cin >> p;
if (p == 1) floor_plan[i] |= 0x01<<j;</pre>
17
18
19
        }
20
21
22
23
24
   }
25
   int main() {
26
        ios_base::sync_with_stdio(false);
27
        int T; cin >> T;
for (int t=0; t < T; t++){</pre>
28
29
            new_tiles();
30
31
   }
32
```

## Golden Eye

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
   #include <CGAL/Delaunay_triangulation_2.h>
2
   #include <CGAL/Triangulation_vertex_base_with_info_2.h>
3
   #include <CGAL/Triangulation_face_base_2.h>
   #include <vector>
   #include <boost/pending/disjoint_sets.hpp>
   {\tt typedef} \ \ {\tt CGAL::Exact\_predicates\_inexact\_constructions\_kernel}
                                                                       K:
8
   typedef K::Point_2
                                                                       P;
   typedef CGAL::Triangulation_vertex_base_with_info_2 < int , K >
                                                                       Vb:
   typedef CGAL::Triangulation_face_base_2 <K>
                                                                       Fb:
   typedef CGAL::Triangulation_data_structure_2 < Vb , Fb >
                                                                       Tds;
   typedef CGAL::Delaunay_triangulation_2<K,Tds>
                                                                       Delaunay;
   typedef Delaunay::Vertex_handle
                                                                       VertexH:
   typedef Delaunay::Finite_edges_iterator
                                                                       EI;
   typedef std::pair<P,int>
                                                                       IPoint:
   typedef boost::disjoint_sets_with_storage<>
                                                                       Uf:
18
   using namespace std;
   struct Edge {
        Edge(int u_, int v_, K::FT sql_) : u(u_), v(v_), sql(sql_) {}
23
       int u. v:
                       // endpoints
                        // squared length
25
       K::FT sql;
   }:
   inline bool operator<(const Edge& e, const Edge& f) { return e.sql < f.sql; }</pre>
28
   void goldeneye() {
31
       int n, m; double p;
       cin >> n >> m >> p;
       // Read jammers and build Delaunay
       vector < IPoint > jammers(n);
       long x, y;
       for (int i = 0; i < n; i++) {</pre>
            cin >> x >> y;
38
            jammers[i] = IPoint(P(x, y), i);
40
41
       Delaunay t;
42
       t.insert(jammers.begin(), jammers.end());
43
       // Extract edges and sort by length
44
       vector < Edge > edges;
45
46
        edges.reserve(3*n);
       for (EI e = t.finite_edges_begin(); e != t.finite_edges_end(); e++) {
47
            edges.push_back(Edge(e->first->vertex((e->second+1)%3)->info(),
48
                                  e->first->vertex((e->second+2)%3)->info(),
49
50
                                  t.segment(e).squared_length()));
       sort(edges.begin(), edges.end());
       // Compute components with power consumption p
       Uf ufp(n);
       typedef vector < Edge > :: const_iterator ECI;
       for (ECI e = edges.begin(); e != edges.end() && e->sql <= p; e++)</pre>
            ufp.union_set(e->u, e->v);
60
       // Handle missions
       K::FT a = 0, b = 0;
       Uf ufa(n), ufb(n);
       ECI ai = edges.begin(), bi = edges.begin();
       int x0, y0, x1, y1;
       for (int i = 0; i < m; i++) {</pre>
66
            cin >> x0 >> y0 >> x1 >> y1;
            P p0(x0, y0), p1(x1, y1);
67
            VertexH v0 = t.nearest_vertex(p0), v1 = t.nearest_vertex(p1);
68
            K::FT d = 4 * max(CGAL::squared_distance(p0, v0->point()),
                               CGAL::squared_distance(p1, v1->point()));
            if (d <= p && ufp.find_set(v0->info()) == ufp.find_set(v1->info())) {
                // mission possible with power p \rightarrow also with b
                cout << "y";
                if (d > b) b = d;
76
                for (; bi != edges.end() &&
                         ufb.find_set(v0->info()) != ufb.find_set(v1->info()); bi++)
```

```
78
                      ufb.union_set(bi->u, bi->v);
            } else cout << "n";</pre>
79
             // ensure it is possible at power a
80
81
            if (d > a) a = d;
            for (; ai != edges.end() &&
82
                     ufa.find_set(v0->info()) != ufa.find_set(v1->info()); ai++)
83
                 ufa.union_set(ai->u, ai->v);
84
85
86
        if (ai != edges.begin() && (ai-1)->sql > a) a = (ai-1)->sql;
87
        if (bi != edges.begin() && (bi-1)->sql > b) b = (bi-1)->sql; cout << endl << a << endl << b << endl;
88
89
   }
90
91
92
    int main() {
        ios_base::sync_with_stdio(false);
93
        cout << setiosflags(ios::fixed) << setprecision(0);</pre>
94
        int T; cin >> T;
95
        for (int t = 0; t < T; t++) {</pre>
96
97
            goldeneye();
98
   }
```

## Corbusier

```
#include <vector>
   #include <iostream>
3
4
   using namespace std;
   void corbusier() {
6
       int n, i, k;
        cin >> n >> i >> k;
9
        vector < int > disks(n);
        vector < vector < bool > > T(n, vector < bool > (k, false));
        for (int j = 0; j < n; j++) cin >> disks[j];
        int h;
15
16
        for (int d = 0; d < n; d++) {</pre>
            h = disks[d];
18
            T[d][h%k] = true;
if (d > 0) {
                 for (int j = 0; j < k; j++) {</pre>
                     if (T[d-1][j]) {
                          T[d][j] = true;
23
                          T[d][(j+h)%k] = true;
24
                     }
                 }
26
28
29
            if (T[d][i]) {
                 cout << "yes\n";</pre>
31
                 return;
32
        cout << "no\n";
37
    int main() {
38
        ios_base::sync_with_stdio(false);
39
        int T; cin >> T;
40
        for (int t = 0; t < T; t++) {
41
             corbusier();
42
43
   }
44
```

## **Placing Knights**

```
#include <iostream>
   #include <map>
3
   #include <algorithm>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
6
   #include <boost/graph/max_cardinality_matching.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
   typedef adjacency_list<vecS, vecS, undirectedS> Graph;
15
   typedef graph_traits < Graph > :: edge_descriptor Edge;
   typedef graph_traits < Graph >:: vertex_descriptor Vertex;
    void add_connection(Graph& G, vector < vector < bool > > & chessboard, int n, int i, int j, int new_i,
        int new_j) {
        if (new_i >= n || new_i < 0) return;</pre>
        if (new_j >= n || new_j < 0) return;</pre>
        if ( !chessboard[new_i][new_j] ) return;
        \verb"add_edge(i*n + j, new_i*n + new_j, G);
   }
28
   void placing_knights() {
30
        int n; cin >> n;
31
        vector < vector < bool > > chessboard(n, vector < bool > (n));
        // Read chessboardx
        int c = 0;
        for (int i = 0; i < n; i++) {</pre>
             for (int j = 0; j < n; j++) {</pre>
36
                  bool p; cin >> p;
38
                  chessboard[i][j] = p;
                  if ( p ) c++;
39
             }
40
41
        }
        Graph G(n*n);
43
44
        for (int i = 0; i < n; i++) {</pre>
45
             for (int j = 0; j < n; j++) {
46
47
                  if (chessboard[i][j]) {
                       \verb|add_connection(G, chessboard, n, i, j, i-1, j-2);|\\
48
                      add_connection(G, chessboard, n, i, j, i-1, j+2); add_connection(G, chessboard, n, i, j, i+1, j-2); add_connection(G, chessboard, n, i, j, i+1, j+2);
49
                       add\_connection(G, chessboard, n, i, j, i-2, j-1);
                      add_connection(G, chessboard, n, i, j, i-2, j+1);
add_connection(G, chessboard, n, i, j, i+2, j-1);
                       add_connection(G, chessboard, n, i, j, i+2, j+1);
                  }
56
             }
58
        vector < Vertex > mate(n*n);
        checked_edmonds_maximum_cardinality_matching(G, &mate[0]);
        int matches = matching_size(G, &mate[0]);
63
        cout << c - matches << endl;</pre>
   }
65
66
   int main() {
        ios_base::sync_with_stdio(false);
        int T; cin >> T;
        for (int t=0; t < T; t++){</pre>
             placing_knights();
        }
   }
```

## Radiation

```
#include <iostream>
   #include <vector>
2
   #include <cassert>
3
   #include <cmath>
   #include <CGAL/basic.h>
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
   #include <CGAL/Gmpz.h>
   // choose exact integral type
   typedef CGAL::Gmpz ET;
   // program and solution types
   typedef CGAL::Quadratic_program <long > Program;
   typedef CGAL::Quadratic_program_solution<ET> Solution;
   using namespace std;
   bool solve(vector<vector<long> > > & coefficients, const int h, const int t, const int d) {
       int nb_coeff = coefficients[0][d].size();
23
       Program lp (CGAL::SMALLER, false, 0, false, 0);
25
       CGAL::Quadratic_program_options options;
       options.set_pricing_strategy(CGAL::QP_BLAND);
                                                          // Bland's rule
       for (int i = 0; i < (h + t); i++) {</pre>
28
            for (int k = 0; k < nb_coeff; k++) {</pre>
30
                lp.set_a(k, i, coefficients[i][d][k]);
31
            lp.set_b(i, 0);
            if (i >= h) lp.set_a(nb_coeff, i, 1); // Epsilon
       }
36
       lp.set_c(nb_coeff, -1);
       lp.set_l(nb_coeff, true, 0);
38
       Solution s = CGAL::solve_linear_program(lp, ET(), options);
       return s.is unbounded():
40
41
   }
43
   void radiation(){
44
       int h, t;
45
       cin >> h >> t:
46
47
       const int D = 30;
48
49
50
       vector<vector<long> > health(h, vector<long>(3)), tumor(t,vector<long>(3));
       for (int i = 0; i < h; i++) cin >> health[i][0] >> health[i][1] >> health[i][2];
       for (int i = 0; i < t; i++) cin >> tumor[i][0] >> tumor[i][1] >> tumor[i][2];
       vector<vector<long> > >coefficients(h+t, vector<vector<long> >(D+1));
       for (int i = 0; i < (h + t); i++) {</pre>
            vector<long> cell = (i < h) ? health[i]: tumor[i-h];</pre>
60
            for (int d = 1; d <= D; d++) {</pre>
                long coef_x = 1;
                for (int x = 0; x \le d; x++) {
                    long coef_y = 1;
                    for (int y = 0; y <= d; y++) {</pre>
                        long coef_z = 1;
66
                        for (int z = 0; z <= d; z++) {
                            if (x + y + z > d) continue;
67
68
                            if (i >=h) coefficients[i][d].push_back(coef_x * coef_y * coef_z);
                            else coefficients[i][d].push_back(-coef_x * coef_y * coef_z);
                            coef_z *= cell[2];
                        coef_y *= cell[1];
                    }
74
                    coef_x *= cell[0];
               }
           }
76
       }
```

```
78
          int upper = 1;
79
          while (!solve(coefficients, h, t, upper) && upper <= D) upper *= 2;</pre>
80
81
          if (upper > D) cout << "impossible" << endl;</pre>
82
 83
          int low = upper / 2;
84
          while (low + 1 != upper) {
  int mid = low + (upper - low) / 2;
  if (solve(coefficients, h, t, mid)) {
85
 86
87
                upper = mid;
} else low = mid;
88
89
90
91
92
          cout << upper << endl;</pre>
     }
93
94
95
     int main() {
96
          int T; cin >> T;
97
          for (int t = 0; t < T; t++) {
    radiation();</pre>
98
99
100
     }
```

## The Empire Strikes Back

```
#include <vector>
   #include <iostream>
   #include <algorithm>
3
   #include <limits.h>
   #include <CGAL/basic.h>
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
   #include <CGAL/Gmpzf.h>
   #include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
   #include <CGAL/Delaunay_triangulation_2.h>
   // LP
   typedef CGAL::Gmpzf ET;
   typedef CGAL::Quadratic_program <double > Program;
   typedef CGAL::Quadratic_program_solution <ET> Solution;
   // Delaunav
   typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
   typedef CGAL::Delaunay_triangulation_2 < K >
                                                                  Triangulation;
18
   typedef K::Point_2
                                                                  Point:
   using namespace std;
23
   void strikes_back() {
       int a, s, b, e;
25
       cin >> a >> s >> b >> e;
       vector < Point > asteroid(a), shooting_points(s), bounty_hunters(b);
       vector < int > asteroid_densities(a);
28
       long x, y;
30
       // Read data
       for (int i = 0; i < a; i++) {</pre>
31
            cin >> x >> y;
            asteroid[i] = Point(x, y);
            cin >> asteroid_densities[i];
       }
       for (int i = 0; i < s; i++) {</pre>
36
            cin >> x >> y;
            shooting_points[i] = Point(x, y);
38
       for (int i = 0; i < b; i++) {</pre>
40
41
            cin >> x >> y;
            bounty_hunters[i] = Point(x, y);
43
44
       // Create a triangulation for the bounty hunters to find the closest one at each shooting
45
           point
       Triangulation bh;
       bh.insert(bounty_hunters.begin(), bounty_hunters.end());
47
        // Initialize linear program
49
       Program lp (CGAL::LARGER, true, 0, false, 0);
       double max_d = LONG_MAX;  // Distance to the closest bounty hunters
       double d;
       for (int i = 0; i < s; i++) {
                                    // In case the set ob bounty hunters are empty
            if (b > 0) {
                Point cl_bh = bh.nearest_vertex(shooting_points[i])->point();
                max_d = CGAL::to_double(CGAL::squared_distance(cl_bh, shooting_points[i]));
           }
58
59
            for (int j = 0; j < a; j++) {</pre>
                // Compute the distance of every shooting point to each asteroid
                d = CGAL::to_double(CGAL::squared_distance(shooting_points[i], asteroid[j]));
                // If the closests bounty hunter is nearer than the asteroid, then to this no energy
                // will arrive
65
                if(d >= max_d) continue;
66
67
                // If arrives compute the coefficient
                double coef = 1 / ((double) max(1., d));
                lp.set_a(i, j, coef);
           lp.set_c(i, 1);
                                    // Minimize the sum of energy at each shot
                                    // (*) Set a last inequality upbounding the total amount of energy
           lp.set_a(i, a, 1);
                                     // used
       lp.set_b(a, e);
                                         // (*)
       lp.set_r(a, CGAL::SMALLER);
```

```
// Set a lower limit to the amount of energy that must arrive to each asteroid
77
          for (int j = 0; j < a; j++) {
    lp.set_b(j, asteroid_densities[j]);</pre>
78
79
80
81
          // Solve LP
82
          Solution sol = CGAL::solve_linear_program(lp, ET());
83
          assert (sol.solves_linear_program(lp));
84
85
         // If exists solution then its possible to do it
if (sol.is_optimal()) cout << "y" << endl;
else cout << "n" << endl;</pre>
86
87
88
89
    }
90
91
    int main() {
92
         int T; cin >> T;
for (int i = 0; i < T; i++) {</pre>
93
94
                strikes_back();
95
96
97
    }
```

## Bob's Burden

```
// Includes
   // ======
   // STL includes
3
   #include <iostream>
   #include <vector>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
8
   #include <boost/graph/dijkstra_shortest_paths.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
   // =========
   // Graph Type, OutEdgeList Type, VertexList Type, (un)directedS
   typedef adjacency_list<vecS, vecS, directedS,</pre>
                                                         // Use vecS for the VertexList! Choosing setS
       for the OutEdgeList disallows parallel edges.
                                         // interior properties of vertices
18
           no_property,
19
           property < edge_weight_t , int >
                                                // interior properties of edges
                               Graph;
   typedef graph_traits<Graph>::edge_descriptor
                                                         Edge;
                                                                      // Edge Descriptor: an object that
        represents a single edge.
   typedef graph_traits < Graph > :: vertex_descriptor
                                                         Vertex;
                                                                     // Vertex Descriptor: with vecS
       vertex list, this is really just an int in the range [0, num\_vertices(G)).
   typedef graph_traits < Graph > :: edge_iterator
                                                     EdgeIt;
                                                                  // to iterate over all edges
                                                         OutEdgeIt; // to iterate over all outgoing
   typedef graph_traits < Graph > :: out_edge_iterator
       edges of a vertex
                                                         WeightMap; // property map to access the
   typedef property_map < Graph , edge_weight_t >:: type
       interior property edge_weight_t
   void bobs_burden() {
       int k; cin >> k;
30
       int N = k * (k+1) / 2;
       Graph G(2 * N);
       WeightMap weightmap = get(edge_weight, G);
       int pos_in, pos_out, v;
36
       Edge e; bool success;
       for (int i = 0; i < k; i++) {</pre>
            for (int j = 0; j <= i; j++) {</pre>
38
                pos_in = i * (i + 1) / 2 + j;
39
                pos_out = pos_in + N;
40
41
                cin >> v;
                tie(e, success) = add_edge(pos_in, pos_out, G);
                weightmap[e] = v;
43
44
                if (j > 0) {
45
                    int pos_left_in = pos_in - 1, pos_left_out = pos_out - 1;
                    add_edge(pos_left_out, pos_in, G);
46
47
                    add_edge(pos_out, pos_left_in, G);
48
49
                if (i < k - 1) {
                    int pos_down_left_in = pos_in + (i + 1);
                    int pos_down_left_out = pos_down_left_in + N;
                    int pos_down_right_in = pos_down_left_in + 1;
                    int pos_down_right_out = pos_down_right_in + N;
                    add_edge(pos_out, pos_down_left_in, G);
                    add_edge(pos_down_left_out, pos_in, G);
                    add_edge(pos_out, pos_down_right_in, G);
                    add_edge(pos_down_right_out, pos_in, G);
               }
           }
61
       vector < vector < int > distmap(3, vector < int > (N*2));
       // Compute the distance map for the three point (0,0), (k,0), (k,k)
       dijkstra_shortest_paths(G, N,
            distance_map(make_iterator_property_map(distmap[0].begin(), get(vertex_index, G))));
       dijkstra_shortest_paths(G, 2*N - k,
            distance_map(make_iterator_property_map(distmap[1].begin(), get(vertex_index, G))));
       dijkstra_shortest_paths(G, 2*N - 1,
69
            distance_map(make_iterator_property_map(distmap[2].begin(), get(vertex_index, G))));
       int minimum_burden = INT_MAX;
       for (int i = 0; i < k; i++) {</pre>
```

```
for (int j = 0; j <= i; j++) {
   pos_in = i * (i + 1) / 2 + j;
   if (pos_in == 0 || pos_in == N - k || pos_in == N - 1)</pre>
73
74
75
76
                            continue;
                      tie(e, success) = edge(pos_in, pos_in+N, G);
minimum_burden = min(minimum_burden,
78
                           distmap[0][pos_in] + distmap[1][pos_in] + distmap[2][pos_in] + weightmap[e]);
79
                }
80
81
82
          cout << minimum_burden << endl;</pre>
83
84
    }
85
86
87
     int main() {
          ios_base::sync_with_stdio(false);
88
          int T; cin >> T;
for (int t=0; t < T; t++){</pre>
89
90
                bobs_burden();
91
92
    }
93
```

#### DHL

```
#include <vector>
   #include <climits>
   #include <iostream>
3
   #include <algorithm>
   using namespace std;
6
9
   int dp(vector<vector<int> >& sum, int pos_a, int pos_b, vector<vector<int> >& memory) {
        // Check memory first
       if (memory[pos_a][pos_b] != -1) return memory[pos_a][pos_b];
       // Look for the best combination to reduce the cost given an specific position of the two
            stacks
       int pick_a, pick_b, new_cost, cost = INT_MAX;
       // Separate the iteration, first look at the first stack and take the first volume
       pick_a = sum[0][pos_a] - sum[0][pos_a-1];
       for(int i = pos_b - 1; i >= 0; i--) {
            if ((pos_a-1 == 0 && i > 0) || (pos_a-1 > 0 && i == 0)) continue;
20
            pick_b = sum[1][pos_b] - sum[1][i];
            new_cost = (memory[pos_a-1][i] != -1) ? memory[pos_a-1][i] : dp(sum, pos_a-1, i, memory);
23
            cost = min(cost, new_cost + pick_a*pick_b);
25
       pick_b = sum[1][pos_b] - sum[1][pos_b-1];
28
        for(int i = pos_a - 1; i >= 0; i--) {
           if ((i == 0 && pos_b-1 > 0) || (i > 0 && pos_b-1 == 0)) continue;
            pick_a = sum[0][pos_a] - sum[0][i];
31
            new_cost = (memory[i][pos_b-1] != -1) ? memory[i][pos_b-1] : dp(sum, i, pos_b-1, memory);
            cost = min(cost, new_cost + pick_a*pick_b);
       memory[pos_a][pos_b] = cost;
36
       return cost;
38
   }
39
40
41
   void dhl() {
       int n; cin >> n;
43
       vector < vector < int > > sum(2, vector < int > (n+1));
44
       sum[0][0] = 0; sum[1][0] = 0;
45
46
47
       int v;
       for (int i = 0; i < 2; i++) {</pre>
48
49
            for (int j = 0; j < n; j++) {
                cin >> v; v--;
                sum[i][j+1] = sum[i][j] + v;
            }
       }
       int pos_a = n, pos_b = n;
56
       // Build memory matrix
       vector < vector < int > > memory(n+1, vector < int > (n+1, -1));
58
       memory[0][0] = 0;
       int cost = dp(sum, pos_a, pos_b, memory);
61
        cout << cost << endl;</pre>
63
   }
65
   int main() {
66
       ios_base::sync_with_stdio(false);
67
        int T; cin >> T;
       for (int t=0; t < T; t++){</pre>
            dh1():
       }
   }
```

## Sweepers

```
#include <iostream>
2
   #include <map>
3
   #include <algorithm>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/push_relabel_max_flow.hpp>
   #include <boost/graph/connected_components.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
   // BGL Graph definitions
   // ==========
   // Graph Type with nested interior edge properties for Flow Algorithms
16
   typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
18
       property < edge_capacity_t, long,</pre>
           property < edge_residual_capacity_t , long ,</pre>
                property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
   // Interior \overline{P}roperty Maps
   typedef property_map < Graph , edge_capacity_t >: : type
23
                                                               EdgeCapacityMap;
   {\tt typedef} \  \  {\tt property\_map} < {\tt Graph} \ , \  \  {\tt edge\_residual\_capacity\_t} > : : {\tt type} \  \  {\tt ResidualCapacityMap};
   typedef property_map < Graph , edge_reverse_t > : : type
                                                              ReverseEdgeMap;
   typedef graph_traits < Graph > :: vertex_descriptor
   typedef graph_traits<Graph>::edge_descriptor
                                                              Edge:
   typedef graph_traits < Graph > :: edge_iterator
                                                              EdgeIt;
28
30
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map and reverse edge map
   class EdgeAdder {
       Graph &G:
36
       EdgeCapacityMap &capacitymap;
       ReverseEdgeMap &revedgemap;
38
       // to initialize the Object
40
41
       EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, ReverseEdgeMap &revedgemap):
42
            G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
43
       // to use the Function (add an edge)
44
       Edge addEdge(int from, int to, long capacity) {
45
46
            Edge e, reverseE;
47
            bool success;
            tie(e, success) = add_edge(from, to, G);
48
            tie(reverseE, success) = add_edge(to, from, G);
49
            capacitymap[e] = capacity;
50
            capacitymap[reverseE] = 0;
            revedgemap[e] = reverseE;
           revedgemap[reverseE] = e;
            return e;
       }
   };
58
   void sweepers() {
60
       int n, m, s, p;
       cin >> n >> m >> s;
       Graph G(n+2);
       EdgeCapacityMap capacitymap = get(edge_capacity, G);
       ReverseEdgeMap revedgemap = get(edge_reverse, G);
66
       EdgeAdder eaG(G, capacitymap, revedgemap);
       Vertex v_source = n, v_target = n + 1;
68
       vector<int> degree(n, 0);
       vector < bool > has_edges(n, false);
       has_edges[n] = true; has_edges[n+1];
       for (int i = 0; i < s; i++) {</pre>
74
            cin >> p;
            eaG.addEdge(v_source, p, 1);
76
            degree[p]++;
            has_edges[p] = true;
```

```
78
        for (int i = 0; i < s; i++) {</pre>
            cin >> p;
80
             eaG.addEdge(p, v_target, 1);
81
             degree[p]++;
            has_edges[p] = true;
83
84
86
        int x, y;
        for (int i = 0; i < m; i++) {</pre>
87
             cin >> x >> y;
88
             eaG.addEdge(x, y, 1);
89
             eaG.addEdge(y, x, 1);
90
             degree[x]++; degree[y]++;
91
            has_edges[x] = true; has_edges[y] = true;
94
        int flow = push_relabel_max_flow(G, v_source, v_target);
96
        vector < Vertex > componentmap(n+2);
97
        connected_components(G, make_iterator_property_map(componentmap.begin(), get(vertex_index, G))
98
            );
99
        bool result = flow == s;
                                          // First check if the flow is equal the number of sweepers
        // Now check the degree of all the nodes
        for (int i = 0; i < n; i++)</pre>
            if (degree[i] % 2 != 0) result = false;
104
        // Now check that all the nodes from the same component that source, are the ones that have
            the
        // edges -> the edges are reachable.
        int ref_component = componentmap[n];
        for (int i = 0; i < n; i++) {
            if (has_edges[i] && componentmap[i] != ref_component) result = false;
108
110
        if (result) cout << "yes" << endl;</pre>
        else cout << "no" << endl;</pre>
113
    }
114
    int main() {
116
        ios_base::sync_with_stdio(false);
118
        int T; cin >> T;
        for (int t=0; t < T; t++){</pre>
119
            sweepers();
        }
121
    }
```

## Portfolios revisited

```
#include <iostream>
   #include <cassert>
   #include <cmath>
3
   #include <CGAL/basic.h>
   #include <CGAL/QP_models.h>
   #include <CGAL/QP_functions.h>
   #include <CGAL/Gmpz.h>
   // choose exact integral type
   typedef CGAL::Gmpz ET;
   // program and solution types
   typedef CGAL::Quadratic_program <int > Program;
   typedef CGAL::Quadratic_program_solution<ET> Solution;
   using namespace std:
18
   void portfolios(int n, int m){
        // Quadratic Programming
       Program qp(CGAL::SMALLER, true, 0, false, 0);
       const int COST = 0;
23
       const int RETURN = 1;
25
       int c, r, v;
       vector < int > returns(n);
       qp.set_r(RETURN, CGAL::LARGER);
28
       for (int i = 0; i < n; i++) {</pre>
            cin >> c >> r;
30
            qp.set_a(i, COST, c);
31
            qp.set_a(i, RETURN, r);
returns[i] = r;
       }
       for (int i = 0; i < n; i++) {</pre>
36
            for (int j = 0; j < n; j++) {
                cin >> v;
                if (j <= i) qp.set_d(i, j, 2*v);</pre>
38
39
40
       for (int i = 0; i < m; i++) {</pre>
41
            long C, V;
            cin >> C >> V;
43
44
            qp.set_b(COST, C);
45
46
            int lower = 0, upper = INT_MAX, middle;
47
            double best_return = 0;
48
49
            // Binary search
            while (lower + 1 != upper) {
50
                middle = lower + (upper - lower) / 2;
                qp.set_b(RETURN, middle);
                Solution s = CGAL::solve_nonnegative_quadratic_program(qp, ET());
                if (s.is_optimal() && CGAL::to_double(s.objective_value()) <= V) {</pre>
                    lower = middle;
                    // Compute return
58
                    double total_return = 0;
                    int indx = 0:
60
                    for (auto it = s.variable_values_begin(); it != s.variable_values_end(); it++) {
                         total_return += returns[indx++] * CGAL::to_double(*it);
                    best_return = max(best_return, total_return);
                } else {
                    upper = middle;
66
68
            cout << best_return << endl;</pre>
       }
   }
74
   int main() {
76
       ios_base::sync_with_stdio(false);
       int n, m;
```

## The Phantom Menace

```
/****
   Given a directed graph find how many vertex need to be removed to disconect one set of vertex with
   another set.
3
   This is solve creating a graph with an income and outcome node for each vertex. All the edges must
   have capacity one and then finding the mincut of the graph is possible to find the number of
       vertex
   required to disconnect the two sets of vertex. The mincut is found computing the maximum flow.
6
   // Includes
9
   // ======
   // STL includes
   #include <iostream>
   #include <cstdlib>
   // BGL includes
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/push_relabel_max_flow.hpp>
   // Namespaces
   using namespace boost;
18
19
   using namespace std;
   // BGL Graph definitions
   // Graph Type with nested interior edge properties for Cost Flow Algorithms
   typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
       property < edge_capacity_t, long,</pre>
26
            property<edge_residual_capacity_t, long,</pre>
                property<edge_reverse_t , Traits::edge_descriptor> > > Graph;
   // Interior Property Maps
   {\tt typedef} \  \  {\tt property\_map} < {\tt Graph} \;, \;\; {\tt edge\_capacity\_t} > : : {\tt type}
                                                                EdgeCapacityMap;
   typedef property_map < Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph, edge_reverse_t>::type ReverseEdgeMap;
   typedef graph_traits < Graph > :: vertex_descriptor
                                                                Vertex;
   typedef graph_traits < Graph > : : edge_descriptor
                                                                Edge;
   typedef graph_traits < Graph >:: out_edge_iterator
                                                                OutEdgeIt;
   // Custom Edge Adder Class, that holds the references
   // to the graph, capacity map, weight map and reverse edge map
40
   class EdgeAdder {
        Graph &G;
41
        EdgeCapacityMap &capacitymap;
42
        ReverseEdgeMap &revedgemap;
44
45
   public:
        // to initialize the Object
46
        EdgeAdder(Graph & G, EdgeCapacityMap &capacitymap, ReverseEdgeMap &revedgemap):
47
48
            G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
49
        // to use the Function (add an edge)
        void addEdge(int from, int to, long capacity) {
            Edge e, reverseE;
            bool success;
            tie(e, success) = add_edge(from, to, G);
            tie(reverseE, success) = add_edge(to, from, G);
            capacitymap[e] = capacity;
            capacitymap[reverseE] = 0;
            revedgemap[e] = reverseE;
58
59
            revedgemap[reverseE] = e;
   }:
61
   void phantom_menace() {
64
65
       int n, m, s, d;
        cin >> n >> m >> s >> d;
66
67
        // Create Graph and Maps
                           // Input nodes: [0, n) Output nodes: [n, 2*n)
        Graph G(2*n+2);
        EdgeCapacityMap capacitymap = get(edge_capacity, G);
        ReverseEdgeMap revedgemap = get(edge_reverse, G);
        EdgeAdder eaG(G, capacitymap, revedgemap);
        Vertex src = 2 * n, sink = 2 * n + 1;
        // Reading graphs edges
```

```
77
         int i, j;
         for (int k = 0; k < m; k++) {</pre>
78
              cin >> i >> j;
79
80
              eaG.addEdge(n + i, j, 1);
         }
81
         for (int k = 0; k < n; k++) eaG.addEdge(k, n + k, 1);</pre>
82
         // Read starting vertex
for (int k = 0; k < s; k++) {
    cin >> i;
83
84
85
               eaG.addEdge(src, i, 1);
86
87
         // Read ending vertex
88
         for (int k = 0; k < d; k++) {
    cin >> j;
89
90
91
               eaG.addEdge(n + j, sink, 1);
         // Compute the min cut as max flow
93
         int flow = push_relabel_max_flow(G, src, sink);
cout << flow << endl;</pre>
94
95
96
97
    }
98
99
     int main() {
         int T; cin >> T;
         for (int i = 0; i < T; i++) {</pre>
              phantom_menace();
103
104
    }
```

## Cantonal Courier

```
#include <vector>
   #include <iostream>
2
   // BGI. includes
3
   #include <boost/graph/adjacency_list.hpp>
   #include <boost/graph/push_relabel_max_flow.hpp>
   // Namespaces
   using namespace std;
   using namespace boost;
9
   // BGL Graph definitions
   // ==========
   // Graph Type with nested interior edge properties for Flow Algorithms
typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
14
   typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
        property < edge_capacity_t , long ,</pre>
            property < edge_residual_capacity_t, long,</pre>
                property < edge_reverse_t, Traits::edge_descriptor > > > Graph;
18
   // Interior \overline{P}roperty Maps
19
   typedef property_map < Graph , edge_capacity_t >::type
                                                                 EdgeCapacityMap;
   {\tt typedef} \  \  {\tt property\_map} < {\tt Graph} \;, \; {\tt edge\_residual\_capacity\_t} > :: {\tt type} \; \; {\tt ResidualCapacityMap} \;;
   typedef property_map < Graph , edge_reverse_t > : : type
                                                                 ReverseEdgeMap;
   typedef graph_traits < Graph >:: vertex_descriptor
   typedef graph_traits < Graph >:: edge_descriptor
                                                                 Edge;
25
   // Custom Edge Adder Class, that holds the references
   \ensuremath{//} to the graph, capacity map and reverse edge map
28
   // -----
   class EdgeAdder {
31
        Graph &G;
        EdgeCapacityMap &capacitymap;
        ReverseEdgeMap &revedgemap;
   public:
       // to initialize the Object
        {\tt EdgeAdder(Graph \& G, EdgeCapacityMap \& capacitymap, ReverseEdgeMap \& revedgemap):}
            G(G), capacitymap(capacitymap), revedgemap(revedgemap){}
38
        // to use the Function (add an edge)
40
41
        void addEdge(int from, int to, long capacity) {
            Edge e, reverseE;
            bool success:
43
            tie(e, success) = add_edge(from, to, G);
44
            tie(reverseE, success) = add_edge(to, from, G);
45
            capacitymap[e] = capacity;
46
            capacitymap[reverseE] = 0;
47
            revedgemap[e] = reverseE;
48
49
            revedgemap[reverseE] = e;
        }
50
   };
   void courier() {
       int Z, J; cin >> Z >> J;
        Graph G(Z + J);
        EdgeCapacityMap capacitymap = get(edge_capacity, G);
58
        ReverseEdgeMap revedgemap = get(edge_reverse, G);
        // ResidualCapacityMap rescapacitymap = get(edge_residual_capacity, G);
60
        EdgeAdder eaG(G, capacitymap, revedgemap);
        Vertex src = add_vertex(G), sink = add_vertex(G);
        // Read zone costs
        int c;
66
        for (int i = 0; i < Z; i++) {</pre>
            cin >> c:
67
68
            eaG.addEdge(J+i, sink, c);
        // Read jobs profits
        int total_revenue = 0;
        for (int i = 0; i < J; i++) {</pre>
74
            cin >> c;
            eaG.addEdge(src, i, c);
76
            total_revenue += c;
```

```
78
         // Read jobs and zones connections for (int i = 0; i < J; i++) {
79
80
              int N; cin >> N;
81
              for (int j = 0; j < N; j++) {
   int z; cin >> z;
82
83
                   eaG.addEdge(i, J+z, INT_MAX);
84
              }
85
         }
86
87
         long flow = push_relabel_max_flow(G, src, sink);
88
89
         cout << total_revenue - flow << endl;</pre>
90
    }
91
92
    int main() {
93
         ios_base::sync_with_stdio(false);
94
         int T; cin >> T;
for (int t = 0; t < T; t++) {</pre>
95
96
              courier();
97
98
    }
99
```

# Index

Binary Search, 13, 32 Delaunay Triangulation, 61-63 Nearest Neighbor, 65 DFS, 13, 63, 71, 73 Dynamic Programming, 34, 36, 39, 43, 51 Split and List, 37 Geometry Intersection, 16, 17 Minimum Circle, 21, 32 Triangle Contains, 19 Graphs Biconnected Components, 28 Bipartite Matchings, 71 Dijkstra Shortest Path, 24, 26, 41  $Max\ Flow\ Min\ Cost,\ 69,\ 75,\ 77$ Max Flow Min Cut, 73 Maximum Cardinality Matching, 30, 41 Maximum Flow, 45, 47, 49, 59, 71 Minimum Spanning Tree, 24, 26 Greedy, 12, 15 Interval Scheduling, 11, 22 LP/QP, 53, 55, 56, 58, 67 Sliding Window, 9, 10, 19 Tricks Precompute, 4, 6 Tree Search, 7