

Data: high dimensional data $\mathbf{X} = \{\mathbf{x}_1, \dots, \mathbf{x}_N\} \subseteq \mathbb{R}^D$, Target Perplexity P , Number of iterations T

Result: low dimensional data $\mathbf{Y} = \{\mathbf{y}_1, \dots, \mathbf{y}_N\} \subseteq \mathbb{R}^d$ such that $d \ll D$ (usually $d = 2$ or 3)

subtract mean $\forall i = 0..N \quad \mathbf{x}_i = \mathbf{x}_i - \bar{\mathbf{x}}$;

recalc data $\forall i = 0..N, k = 0..D \quad (\mathbf{x}_i)_k = (\mathbf{x}_i)_k / \max_{i', k'} (\mathbf{x}_{i'})_{k'}$;

compute squared euclidian distances $d_{ij} = \|\mathbf{x}_i - \mathbf{x}_j\|^2$;

for $i = 0..N$ **do**

initialize σ_i ;

repeat

$\forall j = 0..N \quad p_{j|i} = \frac{\exp(-d_{ij}/2\sigma_i^2)}{\sum_{k \neq i} \exp(-d_{ik}/2\sigma_i^2)}$;

$\text{per}_i = 2^{\sum_j p_{j|i} \log_2 p_{j|i}}$;

until $\text{per}_i = P$;

end

symmetrize $p_{ij} = \frac{p_{j|i} + p_{i|j}}{2N}$;

sample initial $\mathbf{Y}^{(0)} = \{\mathbf{y}_1^{(0)}, \dots, \mathbf{y}_N^{(0)}\}$ from gaussian distribution;

for $t = 1..T$ **do**

compute $\forall i, j = 0..N \quad q_{ij} = \frac{(1 + \|\mathbf{y}_i^{(t-1)} - \mathbf{y}_j^{(t-1)}\|^2)^{-1}}{\sum_{k \neq i} (1 + \|\mathbf{y}_k^{(t-1)} - \mathbf{y}_i^{(t-1)}\|^2)^{-1}}$;

compute $\forall i = 0..N \quad \frac{\partial C}{\partial \mathbf{y}_i^{(t-1)}} = 4 \sum_j (p_{ij} - q_{ij})(\mathbf{y}_i^{(t-1)} - \mathbf{y}_j^{(t-1)})(1 + \|\mathbf{y}_i^{(t-1)} - \mathbf{y}_j^{(t-1)}\|^2)^{-1}$;

update $\forall i = 0..N \quad \mathbf{y}_i^{(t)} = \mathbf{y}_i^{(t-1)} + \eta \frac{\partial C}{\partial \mathbf{y}_i^{(t-1)}} + \alpha(t)(\mathbf{y}_i^{(t-1)} - \mathbf{y}_i^{(t-2)})$;

subtract mean $\forall i = 0..N \quad \mathbf{y}_i^{(t-1)} = \mathbf{y}_i^{(t-1)} - \bar{\mathbf{y}}^{(t-1)}$;

end

Algorithm 1: t-SNE Algorithm