NDCG@5

```
% Load data
load C:\Users\Andrea\Desktop\MAGISTRALE\Anno1-sem2\SearchEngines\HWS\seupd2021-goldr\RUN\RUN202
measure_ndcg5 = runtotonlyndcg5(1:49,:);
measure_ndcg5 = table2array(measure_ndcg5)
measure\_ndcg5 = 49 \times 5
         1.0000
                 1.0000
   1.0000
                           1.0000
                                    1.0000
   0.6844
          0.6844 0.6844
                           0.6844
                                    0.6992
         0.5258 0.5258 0.5920
                                    0.5920
   0.5258
   0.8688 0.7227 0.8688
                           0.1696
                                    0.1696
   0.6844 0.6844 0.6844
   0.4852 0.5087 0.4852
                           0.0848
                                    0.0848
   0.8539 0.7227 0.8539 0.6399
                                    0.6399
   0.4704 0.4704 0.4704
                              0
   0.8539 0.7227 0.8539
                           0.3601
                                    0.5296
   0.8539 0.6548 0.8539
                           0.3392
                                    0.6548
% remove the now useless ap matrix
clear runtotonlyndcg5;
% the significance level
alpha = 0.05;
% the mean for each run across the topics
m_avg_ndcg5 = mean(measure_ndcg5);
ogmyruns = "";
ogmyruns(1) = "run1";
ogmyruns(2) = "run2";
ogmyruns(3) = "run3";
ogmyruns(4) = "run4";
ogmyruns(5) = "run5";
myruns_ndcg5 = ogmyruns;
% sort in descending order of mean score
[~, idx] = sort(m_avg_ndcg5, 'descend');
% re-order runs by descending mean of the measure
measure_ndcg5 = measure_ndcg5(:, idx);
```

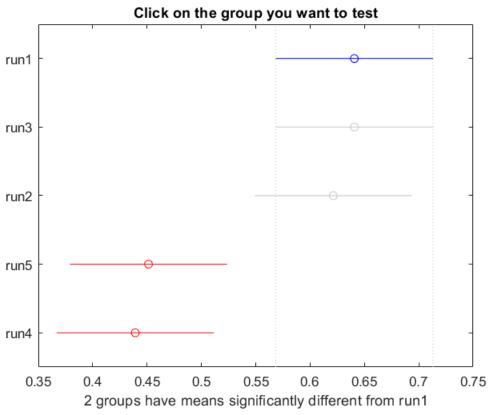
One way ANOVA

myruns_ndcg5 = myruns_ndcg5(:,idx);

```
% perform the ANOVA
[~, tbl_ndcg5, sts_ndcg5] = anova1(measure_ndcg5, myruns_ndcg5, 'off');
% display the ANOVA table
tbl_ndcg5
```

 $tbl_ndcg5 = 4 \times 6 cell$ 3 4 5 'F' 'SS' 'df' 'MS' 'Prob>F' 'Source' 2 4 7.6877 'Columns' 2.1162 0.5290 7.6237e-06 3 'Error' 16.5160 240 0.0688 [] [] 'Total' 18.6321 244 [] [] []

```
c = multcompare(sts_ndcg5, 'Alpha', alpha, 'Ctype', 'hsd');
```



```
C
c = 10 \times 6
                                                         1.0000
    1.0000
              2.0000
                        -0.1446
                                         0
                                              0.1446
              3.0000
                                                         0.9962
    1.0000
                        -0.1252
                                    0.0194
                                              0.1640
    1.0000
              4.0000
                         0.0448
                                    0.1894
                                              0.3339
                                                         0.0033
    1.0000
              5.0000
                         0.0570
                                    0.2016
                                              0.3461
                                                         0.0013
    2.0000
              3.0000
                        -0.1252
                                    0.0194
                                                         0.9962
                                              0.1640
    2.0000
              4.0000
                         0.0448
                                    0.1894
                                              0.3339
                                                         0.0033
    2.0000
              5.0000
                         0.0570
                                    0.2016
                                              0.3461
                                                         0.0013
    3.0000
              4.0000
                         0.0254
                                    0.1700
                                              0.3145
                                                         0.0117
    3.0000
              5.0000
                         0.0376
                                    0.1822
                                              0.3267
                                                         0.0053
    4.0000
              5.0000
                        -0.1324
                                    0.0122
                                              0.1568
                                                         0.9994
```

Two way ANOVA

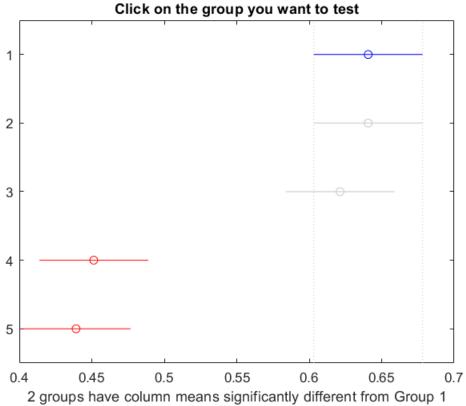
```
% perform the ANOVA
[~, tbl2_ndcg5, sts2_ndcg5] = anova2(measure_ndcg5, 1,'off');
% display the ANOVA table
tbl2_ndcg5
```

$tbl2_ndcg5 = 5 \times 6 cell$

c2

	1	2	3	4	5	6
1	'Source'	'SS'	'df'	'MS'	'F'	'Prob>F'
2	'Columns'	2.1162	4	0.5290	28.4808	1.3911e-18
3	'Rows'	12.9495	48	0.2698	14.5235	1.0785e-42
4	'Error'	3.5665	192	0.0186	[]	[]
5	'Total'	18.6321	244	[]	[]	[]

```
c2 = multcompare(sts2_ndcg5, 'Alpha', alpha, 'Ctype', 'hsd', "Estimate", "column");
```



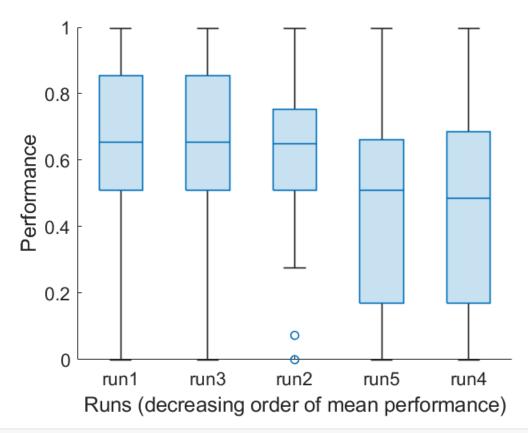
2 groups have column means significantly different from Group

```
c2 = 10 \times 6
    1.0000
                       -0.0751
              2.0000
                                             0.0751
                                                       1.0000
                                       0
   1.0000
              3.0000
                       -0.0557
                                             0.0945
                                                       0.9555
                                  0.0194
              4.0000
   1.0000
                        0.1142
                                  0.1894
                                             0.2645
                                                       0.0000
   1.0000
              5.0000
                        0.1265
                                  0.2016
                                                       0.0000
                                             0.2767
    2.0000
              3.0000
                      -0.0557
                                  0.0194
                                             0.0945
                                                       0.9555
    2.0000
              4.0000
                        0.1142
                                  0.1894
                                             0.2645
                                                       0.0000
    2.0000
              5.0000
                        0.1265
                                  0.2016
                                             0.2767
                                                       0.0000
```

```
4.0000
               0.0948
                        0.1700
3.0000
                                 0.2451
                                         0.0000
              0.1071
3.0000
        5.0000
                        0.1822
                                 0.2573
                                         0.0000
4.0000
        5.0000 -0.0629
                         0.0122
                                 0.0873
                                         0.9920
```

BoxPlot

```
% Compute the mean performance of each run across topics
m_ndcg5 = mean(measure_ndcg5);
myruns4 = ogmyruns;
% sort in descending order of mean score
[~, idx] = sort(m_ndcg5, 'descend');
% re-order runs by descending mean of the measure
% needed to have a more nice looking box plot
measure_ndcg5 = measure_ndcg5(:, idx);
myruns4 = myruns_ndcg5(:,idx);
figure
% show the box plot
boxchart(measure_ndcg5)
%hold on
% plot the mean on top of the box plot
%plot (m, ':x', "MarkerSize", 10, "LineWidth", 2)
% adjust tick labels on x-axis, y-axis range, and font size
ax = gca;
ax.FontSize = 14;
ax.XTickLabel = myruns4;
xlabel("Runs (decreasing order of mean performance)")
ylabel("Performance")
```

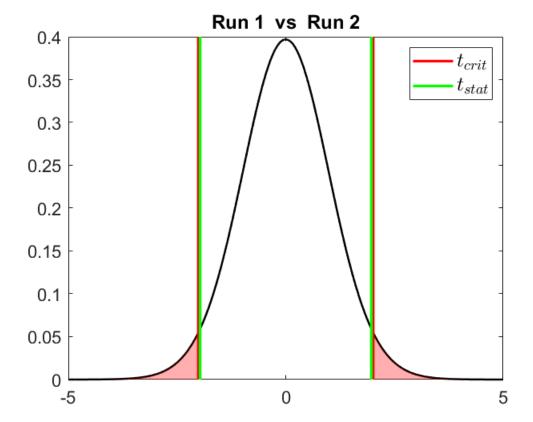


```
newmeasure_n = measure_ndcg5(:, [1,3,2,5,4]);
```

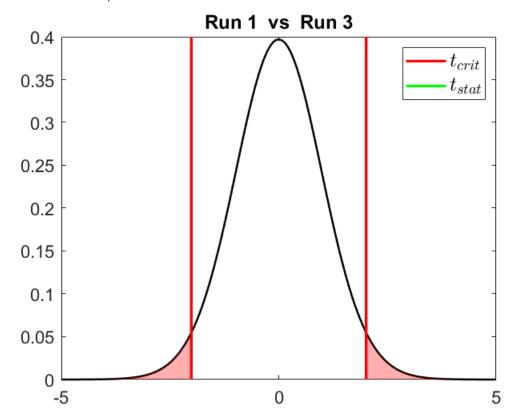
```
for r1 = 1:5
    for r2 = 1:5
        if r1 < r2
            %tstudnet comparisons
            [~, p] = ttest(newmeasure_n(:, r1), newmeasure_n(:, r2));
            %p(isnan(p))=0;
            fprintf("Run %s vs %s: p-value %f", ogmyruns(r1), ogmyruns(r2), p)
            df = length(newmeasure_n) - 1;
            tCrit = tinv(1 - 0.05/2, df);
            tRuns = tinv(1 - p/2, df);
            % if p == 0
            %
                 tRuns = 10;
            %else
                 tRuns = tinv(1 - p/2, df);
                %fprintf("tRuns: " + tRuns)
            %end
            % t distribution
            ar = -5:.01:5;
            ts = tpdf(ar, df);
            % find where we are above and below tCrit
            idx1 = ar >= tCrit;
            idx2 = ar <= -tCrit;
```

```
figure
             plot(ar, ts, "LineWidth", 1.5, "Color", "k");
             hold on
             % plot two vertical lines corresponding to tCrit
             h(1) = plot([tCrit tCrit], get(gca, "ylim"), "Color", "r", "LineWidth", 2, "LineSty
plot([-tCrit -tCrit], get(gca, "ylim"), "Color", "r", "LineWidth", 2, "LineStyle",
             % color the area under the t distribution above and below tCrit
             area(ar(idx1), ts(idx1) , "FaceColor", "r", "FaceAlpha", 0.3, "EdgeColor", "none");
             area(ar(idx2), ts(idx2), "FaceColor", "r", "FaceAlpha", 0.3, "EdgeColor", "none");
             h(2) = plot([tRuns tRuns], get(gca, "ylim"), "Color", "g", "LineWidth", 2, "LineSty
             plot([-tRuns -tRuns], get(gca, "ylim"), "Color", "g", "LineWidth", 2, "LineStyle",
%xline(tRuns, "Color", "g", "LineWidth", 2);
             ax = gca;
             ax.FontSize = 13;
             title(['Run ',num2str(r1),' vs Run ',num2str(r2)])
             lgnd = legend([h(1), h(2)], ["$t_{crit}$", "$t_{stat}$"], "Interpreter", "Latex");
             lgnd.FontSize = 15;
             %fprintf("%d - %d \n", r1, r2)
             if r2 == 5
                  break
             end
         end
    end
end
```

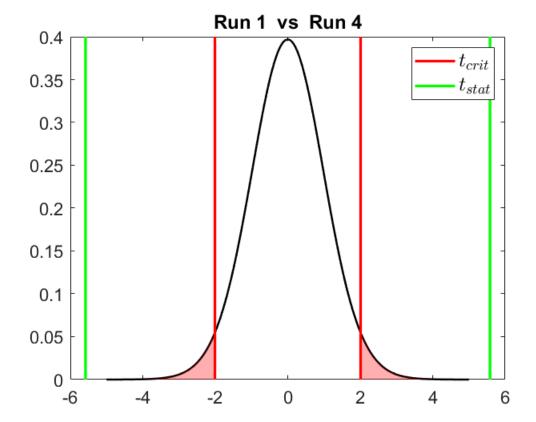
Run run1 vs run2: p-value 0.054621



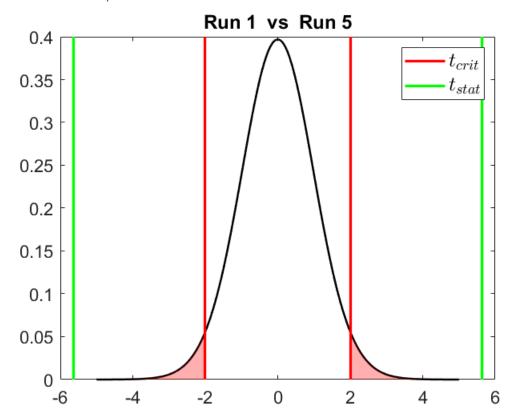
Run run1 vs run3: p-value NaN



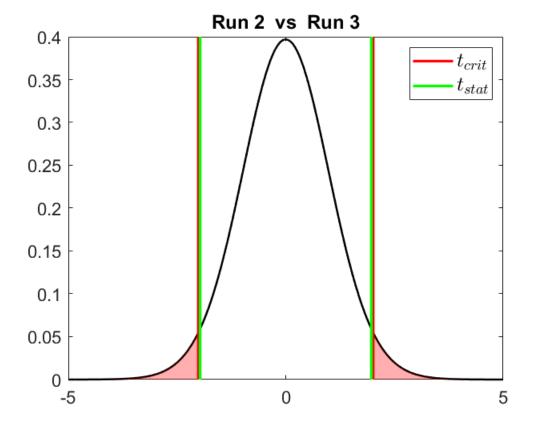
Run run1 vs run4: p-value 0.000001



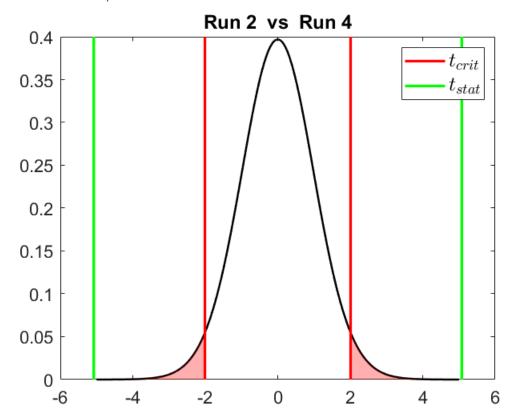
Run run1 vs run5: p-value 0.000001



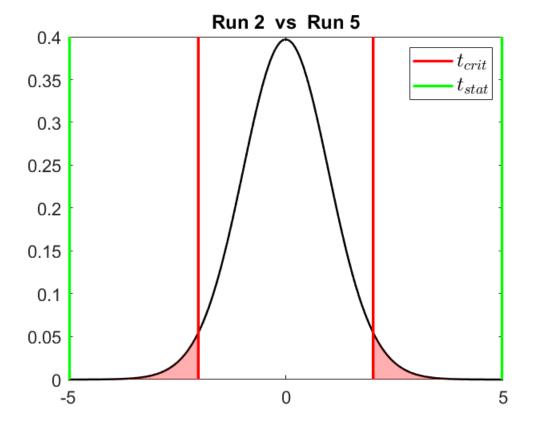
Run run2 vs run3: p-value 0.054621



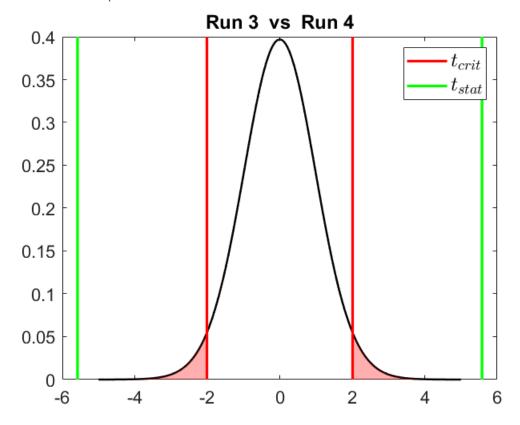
Run run2 vs run4: p-value 0.000006



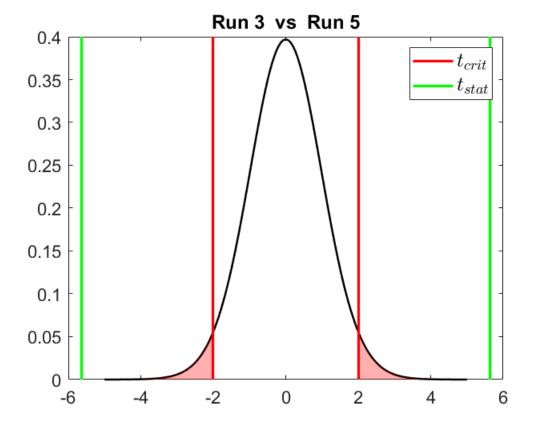
Run run2 vs run5: p-value 0.000009



Run run3 vs run4: p-value 0.000001



Run run3 vs run5: p-value 0.000001



Run run4 vs run5: p-value 0.143588

