

COMP1216

Coursework 2: Formal Modelling

Group #8

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INTRODUCTION

This report has been produced in order to satisfy the requirements of Coursework 2: Formal Modelling for the module COMP1206: Software Modelling and Design.

The members of the group that have worked on this coursework are the following:

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All members of this group have equally contributed to the realisation of this report by applying the knowledge gained throughout the semester to accomplish the tasks outlined in the coursework.

The class diagram shown in the following pages has been realised with Visual Paradigm and the event-B model has been developed by using the Rodin tool. Extension refinement has been used extensively, indeed, eight machines and seven contexts have been created.

The model developed does not violate any requirement listed in the coursework description. Furthermore, the model does not violate any additional requirement that we have opted to introduce in our model.

The model verification process has been conducted by using the model checker function of ProB.

Following this, we provide a list of additional requirements that have been introduced in our model.

Afterwards, the Event-B model developed with the Rodin tool will be presented and at the end of this paper the class diagram showing the main entities of the model will be shown.

ADDITIONAL REQUIREMENTS

- **REQ22:** After a user registers, he/she shall be logged out of the platform.
- **REQ23:** Every quiz shall have exactly one creator. The creator of the quiz shall be a registered user.
- **REQ24:** Every question shall belong exactly to one quiz.
- **REQ25:** A quiz can be shared to multiple registered users.
- **REQ26:** Every question shall be matched to a position so that a quiz contains a sequence of questions.
- **REQ27:** Different questions belonging to the same quiz shall be matched to different positions.
- **REQ28:** The creator of a quiz shall not be allowed to share the quiz to (him/her)self.
- **REQ29:** The creator a quiz shall be allowed to share the quiz only if the quiz contains at least one question.
- **REQ30:** A question added to a quiz shall be automatically inserted at the end of the sequence of the quiz's questions.
- **REQ31:** The creator of a quiz shall be allowed to deshare the quiz with a registered user.
- **REQ32:** Every answer shall belong to exactly one question.
- **REQ33:** The correct answer of a question shall belong to the question.
- **REQ34:** A question shall contain at least 2 **different** answers.
- **REQ35:** A quiz instance shall have exactly one host during any of its states .
- **REQ36:** A user (registered or unregistered) shall not be allowed to be playing in two or more quiz instances at a time.
- **REQ37:** A user shall be allowed to be playing in a quiz instance only if the quiz instance is not in the following states: quizCreated, finishedQuiz.
- **REQ38:** A quiz instance which is not in the finishedQuiz state shall be linked to a quiz which contains at least one question.

- **REQ39:** It shall not be necessary for a quiz instance in the finishedQuiz state to be linked to a quiz because if the quiz is deleted, the quiz instance should be deleted as well.
- **REQ40:** The host of an active quiz instance (not in the finishedQuiz state) shall not be allowed to be playing in the quiz instance he/she is hosting.
- **REQ41:** The host of an active quiz instance shall be constantly logged in.
- **REQ42:** A quiz instance in the questioning or questionSummary state shall be matched with the current question being played.
- **REQ43:** The current question being played in a quiz instance shall belong to the quiz linked to the quiz instance.
- **REQ44:** A quiz instance which is not in the quizCreated state shall be linked to the number of questions answered up to now.
- **REQ45:** The number of answered questions of a quiz instance in the questioning or questionSummary state shall not be greater than the number of questions of the quiz the quiz instance is linked to.
- **REQ46:** A player shall be allowed to answer only the current question being played in the quiz instance he/she is playing in.
- **REQ47:** A quiz instance in the questioning state shall being played by at least one player.
- **REQ48:** The host of an active quiz instance shall not be allowed to be playing in another quiz instance.
- **REQ49:** The host of an active quiz instance shall not be allowed to log out of the system.
- **REQ50:** The host of an active quiz instance shall not be allowed to create a quiz at the same time.
- **REQ51:** The host of an active quiz instance shall not be allowed to remove a quiz at the same time.
- **REQ52:** The creator of a quiz shall not be allowed to remove a quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
- **REQ53:** The host of an active quiz instance shall not be allowed to share a quiz at the same time.
- **REQ54:** The host of an active quiz instance shall not be allowed to add a question to a quiz at the same time.
- **REQ55:** The creator of a quiz shall not be allowed to add a question to the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
- **REQ56:** The host of an active quiz instance shall not be allowed to add an answer to a question of a quiz at the same time.
- **REQ57:** The creator of a quiz shall not be allowed to add an answer to a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
- **REQ58:** The host of an active quiz instance shall not be allowed to remove an answer from a question of a quiz at the same time.
- **REQ59:** The creator of a quiz shall not be allowed to remove an answer from a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
- **REQ60:** The host of an active quiz instance shall not be allowed to set the correct answer of a question of a quiz at the same time.
- **REQ61:** The creator of a quiz shall not be allowed to set the correct answer of a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.

- **REQ62:** The host of an active quiz instance shall not be allowed to update an answer of a question of a quiz at the same time.
- **REQ63:** The creator of a quiz shall not be allowed to update an answer of a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
- **REQ64:** The host of an active quiz instance shall not be allowed to remove a question of a quiz at the same time.
- **REQ65:** The creator of a quiz shall not be allowed to remove a question from the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
- **REQ66:** The host of an active quiz instance shall not be allowed to update a question of a quiz at the same time.
- **REQ67:** The creator of a quiz shall not be allowed to update a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
- **REQ68:** A player of a quiz instance shall be allowed to select an answer multiple times while the quiz instance is in the questioning state.
- **REQ69:** A player of a quiz instance shall not be allowed to select an answer when all other players have answered because the quiz instance passes to the questionSummary state.
- **REQ70:** The host of a quiz instance in the questioning state shall not be allowed to end prematurely a question if all players have answered because the quiz instance passes to the questionSummary state.
- **REQ71:** The host of a quiz instance in the questionSummary state shall have the possibility not to show the question summary to the players.
- **REQ72:** The host of a quiz instance in the questionSummary state shall be allowed to show the question summary only if at least 1 player is playing in the quiz instance.
- **REQ73:** The host of a quiz instance in the questionSummary state shall be allowed to proceed with the next question only if at least one player is playing AND there exists a next question.
- **REQ74:** The host of a quiz instance in the questionSummary state shall have the possibility not to show the quiz summary (report) to the players.
- **REQ75:** The host of a quiz instance in the quizSummary state shall be allowed to show the quiz summary (report) only if at least 1 player is playing in the quiz instance.
- **REQ76:** The creator of a quiz shall not be allowed to deshare a quiz with another registered user if the latter is hosting a quiz instance linked to the quiz.
- **REQ77:** The creator of a quiz shall not be allowed to deshare a quiz if he/she is hosting an active quiz instance.
- **REQ78:** The host of a quiz instance in the finishedQuiz state can remove the quiz instance only if he/she is not hosting any active quiz instance.
- **REQ79:** A quiz instance must be linked to exactly one report.
- **REQ80:** The statistics of the answered questions of a quiz instance not in the finishedQuiz state shall be stored in as many question summaries as the number of answered questions.
- **REQ81:** The final report of a quiz instance in the quizSummary state shall be generated by using the question summaries previously generated.
- **REQ82:** The question summaries shall be discarded when the quizInstance passes to the finishedQuiz state.
- **REQ83:** A question shall be matched to a time within which players can select an answer during a quiz instance.
- **REQ84:** The time of a question shall vary between 1 and 10 minutes.

- **REQ85:** A quiz instance in the questioning state shall be matched with the time when it has transitioned into the questioning state.
- **REQ86:** A quiz instance in the questioning state shall be matched with the time when it will transition into the questionSummary state.
- **REQ87:** The time n when a quiz instance in the questioning state transitions into the questionSummary state shall be equal to $\rightarrow n = \text{startingTime} + \text{question time of the current question being played}$
- **REQ88:** A player shall be allowed to answer a question only within the time of the question.
- **REQ89:** The host of a quiz instance in the questioning state shall be allowed to end a question prematurely only if the question time is not up.
- **REQ90:** A registered user that has lost access to a quiz, because the creator has unshared it, shall be allowed to have access to the quiz instances that has previously run on that quiz.
- **REQ91:** A user shall not be allowed to register into the platform if he/she is playing in a quiz instance.
- **REQ92:** A registered user shall not be allowed to log in the platform if he/she is playing in a quiz instance.
- **REQ93:** A registered user shall not be allowed to log out of the platform if he/she is playing in a quiz instance.

FURTHER EXPLANATIONS

- It is important to notice that while a quiz instance not in the finishedQuiz state must be matched to exactly one quiz, a quiz instance in the finishedQuiz state may be matched to 0 or 1 quiz. This choice has been made because if there existed a composition relation between a quiz and a quiz instance in the finishedQuiz state then the deletion of a quiz would lead to the deletion of all its associated quiz instances. However, this would lead to a loss of precious information as a quiz instance in the finishedQuiz state is the bridge through which a host can have access to the generated report.
- We have opted to split REQ18 into two requirements. Indeed, when a question is finished and its associated quiz instance transitions from the questioning state to the question summary state, a question summary is generated and shown to **only the host of the quiz instance**. We have not created a specific event for showing the question summary to the host as when a quiz instance transitions to the question summary state a question summary is generated and so shown to the host. Additionally, we have added an event that lets the host decide whether to show the question summary to the players or not. In other words, the system is capable of showing the question summary both on the host device and on the players' devices. The same holds for the final quiz summary which is shown when the quiz instance transitions to the quizSummary state.
- As it is possible to notice, a report does not have any direct relation with a quiz and all its components (questions and answers). This choice has been made because if a report was linked to a quiz and all its components then if a quiz or one of its components changed then the report would refer to erratic information. For example, if the answer text of one question changed then the report would refer to an answer that did not exist when the quiz instance was run. Thus, a report must not be dynamically generated when a host needs to analyze it but must be a static file. The decision of what type of file to use for the report should be postponed to later stages of software

development. It is possible to have access to a report by accessing a quiz instance that has been previously run as a report is associated with a quiz instance by mean of a one-to-one relation.

- A report is created when a quiz instance transitions to the quizSummary state. A report file is created by merging together the previously created question summaries which, each of them, collected the performance of the players on a specific question.
- The host of a running quiz instance can terminate the quiz instance at any given time. It is possible to directly transition from the quizCreated or the quizInit state to the finishedQuiz state. On the other hand, if a quiz instance is in the questioning state, the quiz instance cannot transition directly to the finishedQuiz state but must pass through the following states: questionSummary, quizSummary. A quiz instance in the
- questionSummary state can be terminated by the host but must transition to the quizSummary state before being In the finishedQuiz state.
- A quiz instance is in the quizCreated state immediately after a registered user having access to a quiz starts hosting.
- A quiz instance is in the quizInit state when players are allowed to join the quiz instance.
- A quiz instance is in the questioning state when players are allowed to answer a question.
- A quiz instance is in the questionSummary state immediately after a question has ended. A question summary is shown to the host. The host can decide to show the question summary to the players of the quiz instance.
- A quiz instance is in the quizSummary state whenever the host has decided to end the quiz instance or all questions of the quiz have been answered. A quiz summary is shown to the host. The host can decide to show the quiz summary to the players of the quiz instance.
- A quiz instance is in the finishedQuiz state immediately after the quizSummary state. In other words, a quiz instance in the finishedQuiz state is not active.

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CONTEXT c0**SETS**

USER

END

CONTEXT c1**EXTENDS** c0**SETS**

PASSWORD

END

CONTEXT *c2***EXTENDS** *c1***SETS**

QUIZ

QUESTION

CONSTANTS

POSITION

AXIOMS*axm21*;: $POSITION = \mathbb{N}$ **END**

CONTEXT c3

EXTENDS c2

SETS

ANSWER

END

CONTEXT c4

EXTENDS c3

SETS

INSTANCE_QUIZ

END

CONTEXT c5

EXTENDS c4

SETS

QUESTION_SUMMARY

REPORT

END

CONTEXT c6

EXTENDS c5

CONSTANTS

QUESTION_TIME

AXIOMS

axm61;
 $QUESTION_TIME \subseteq \mathbb{N}_1$

axm62;
 $QUESTION_TIME = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

The time of a question shall vary between 1 and 10 minutes.

END

MACHINE m1

SEES c0

VARIABLES

registeredUser Represents the set of registered users

INVARIANTS

inv1;
 $registeredUser \subseteq USER$

The registeredUser set must be a subset of the carrier set USER

EVENTS

Initialisation

begin

act1;
 $registeredUser := \emptyset$

end

Event REGISTER $\langle \text{ordinary} \rangle \hat{=}$

Event that lets a non-registered user register

any

u A user

where

grd1;
 $u \in USER \setminus registeredUser$

The user must not be already registered

then

act1;
 $registeredUser := registeredUser \cup \{u\}$

The user is added to the set of registered users

end

END

MACHINE m2**REFINES** m1**SEES** c1**VARIABLES**

registeredUser

password

INVARIANTSinv21;: $password \in registeredUser \rightarrow PASSWORD$

password is a total function from the set of registered users to the carrier set PASSWORD

EVENTS**Initialisation** ⟨extended⟩

begin

act1;: $registeredUser := \emptyset$ act21;: $password := \emptyset$

end

Event REGISTER ⟨ordinary⟩ $\hat{=}$ **extends** REGISTER

any

 u A user

p

where

grd1;: $u \in USER \setminus registeredUser$

The user must not be already registered

grd21;: $p \in PASSWORD$

then

act1;: $registeredUser := registeredUser \cup \{u\}$

The user is added to the set of registered users

act21;: $password(u) := p$

The password of user u is p

end

END

MACHINE m3**REFINES** m2**SEES** c1**VARIABLES**

registeredUser

password

loggedIn

loggedOut

INVARIANTS*inv31*:: *partition(registeredUser, loggedIn, loggedOut)*

All registered users must be either logged in or logged out

EVENTS**Initialisation** ⟨extended⟩**begin***act1*:: *registeredUser* := ∅*act21*:: *password* := ∅*act31*:: *loggedIn* := ∅*act32*:: *loggedOut* := ∅**end****Event** REGISTER ⟨ordinary⟩ ≐**extends** REGISTER**any***u* A user*p***where***grd1*:: *u* ∈ *USER* \ *registeredUser*

The user must not be already registered

grd21:: *p* ∈ *PASSWORD***then***act1*:: *registeredUser* := *registeredUser* ∪ {*u*}

The user is added to the set of registered users

act21:: *password*(*u*) := *p*The password of user *u* is *p**act31*:: *loggedOut* := *loggedOut* ∪ {*u*}When a user *u* registers, *u* is added to the set of loggedOut users**end****Event** LOGIN ⟨ordinary⟩ ≐

REQ3

any*u**p***where***inv31*:: *u* ∈ *loggedOut**inv32*:: *p* = *password*(*u*)*p* must be the password of *u***then***act31*:: *loggedIn* := *loggedIn* ∪ {*u*}The user *u* is added to the set of loggedIn users*act32*:: *loggedOut* := *loggedOut* \ {*u*}The user *u* is removed from the set of loggedOut users**end****Event** LOGOUT ⟨ordinary⟩ ≐

REQ4

any*u***where**

```
    inv31;:  $u \in \text{loggedIn}$   
        The user u mst be logged in  
  then  
    act31;:  $\text{loggedIn} := \text{loggedIn} \setminus \{u\}$   
        The user u is removed from the set of loggedIn users  
    act32;:  $\text{loggedOut} := \text{loggedOut} \cup \{u\}$   
        The user u is added to the set of loggedOut users  
  end  
END
```

MACHINE m4**REFINES** m3**SEES** c2**VARIABLES**

registeredUser
 password
 loggedIn
 loggedOut
 quizzes
 questions
 quizCreator
 belongingQuiz
 sharedTo
 questionPosition

INVARIANTS

inv41; $quizzes \subseteq QUIZ$
 quizzes is a subset of the carrier set QUIZ
inv42; $questions \subseteq QUESTION$
 questions is a subset of the carrier set QUESTION
inv43; $quizCreator \in quizzes \rightarrow registeredUser$
 quizCreator is a total function from quizzes to registeredUser because every quiz must be created by one registered user
inv44; $belongingQuiz \in questions \rightarrow quizzes$
 It is a total function because every question belongs to just one quiz
inv45; $sharedTo \in quizzes \leftrightarrow registeredUser$
 It is a many-to-many relation because a quiz can be shared to many registered users and a registered user can have access to many shared quizzes
inv46; $questionPosition \in questions \rightarrow POSITION$
 It is a total function because every question must have a position that indicates the position of the question inside the belonging quiz
inv47; $\forall a, b, c. (a \in questions \wedge b \in questions \wedge a \neq b \wedge a \notin \emptyset \wedge b \notin \emptyset \wedge c \in quizzes \wedge belongingQuiz(a) = c \wedge belongingQuiz(b) = c) \Rightarrow questionPosition(a) \neq questionPosition(b)$
 Different questions belonging to the same quiz shall be matched to different positions.
inv48; $\forall q, u. q \in quizzes \wedge u \in registeredUser \wedge q \mapsto u \in sharedTo \Rightarrow u \neq quizCreator(q)$
 The creator of a quiz shall not be allowed to share a quiz to (him/her)self

EVENTS**Initialisation** ⟨extended⟩**begin**

act1; $registeredUser := \emptyset$
act21; $password := \emptyset$
act31; $loggedIn := \emptyset$
act32; $loggedOut := \emptyset$
act41; $quizzes := \emptyset$
act42; $questions := \emptyset$
act43; $quizCreator := \emptyset$
act44; $belongingQuiz := \emptyset$
act45; $sharedTo := \emptyset$
act46; $questionPosition := \emptyset$

end**Event** REGISTER ⟨ordinary⟩ $\hat{=}$ **extends** REGISTER**any** u A user p **where**

```

    grd1::  $u \in USER \setminus registeredUser$ 
        The user must not be already registered
    grd21::  $p \in PASSWORD$ 
then
    act1::  $registeredUser := registeredUser \cup \{u\}$ 
        The user is added to the set of registered users
    act21::  $password(u) := p$ 
        The password of user u is p
    act31::  $loggedOut := loggedOut \cup \{u\}$ 
        When a user u registers, u is added to the set of loggedOut users
end
Event LOGIN ⟨ordinary⟩  $\hat{=}$ 
extends LOGIN
any
     $u$ 
     $p$ 
where
    inv31::  $u \in loggedOut$ 
    inv32::  $p = password(u)$ 
        p must be the pssword of u
then
    act31::  $loggedIn := loggedIn \cup \{u\}$ 
        The user u is added to the set of loggedIn users
    act32::  $loggedOut := loggedOut \setminus \{u\}$ 
        The user u is removed from the set of loggedOut users
end
Event LOGOUT ⟨ordinary⟩  $\hat{=}$ 
extends LOGOUT
any
     $u$ 
where
    inv31::  $u \in loggedIn$ 
        The user u mst be logged in
then
    act31::  $loggedIn := loggedIn \setminus \{u\}$ 
        The user u is removed from the set of loggedIn users
    act32::  $loggedOut := loggedOut \cup \{u\}$ 
        The user u is added to the set of loggedOut users
end
Event CREATEQUIZ ⟨ordinary⟩  $\hat{=}$ 
REQ5
any
     $u$ 
     $q$ 
where
    grd41::  $u \in loggedIn$ 
        A user must be logged in so that to create a quiz
    grd42::  $q \in QUIZ \setminus quizzes$ 
        The created quiz must not have been already created
then
    act41::  $quizzes := quizzes \cup \{q\}$ 
        The created quiz is added to the dynamic set quizzes
    act42::  $quizCreator(q) := u$ 
        the creator of the quiz q is u
end
Event REMOVEQUIZ ⟨ordinary⟩  $\hat{=}$ 
REQ10
any

```

```

    u
    q
  where
    grd41::  $q \in quizzes$ 
    grd42::  $u \in loggedIn$ 
      The user must be logged in so that to remove a quiz
    grd43::  $quizCreator(q) = u$ 
      Only the creator of the quiz can remove the quiz
  then
    act41::  $quizzes := quizzes \setminus \{q\}$ 
      the quiz is removed
    act42::  $quizCreator := \{q\} \triangleleft quizCreator$ 
      The quiz does not have anymore a creator because is removed
    act43::  $sharedTo := \{q\} \triangleleft sharedTo$ 
      All registered users that had access to the quiz, do not have access to it anymore because the quiz
      is removed
    act44::  $belongingQuiz := belongingQuiz \triangleright \{q\}$ 
      The questions of the quiz do not belong anymore to it
    act45::  $questions := questions \setminus \{quest | quest \in questions \wedge belongingQuiz(quest) = q\}$ 
      The questions of the quiz are removed
    act46::  $questionPosition := \{quest | quest \in questions \wedge belongingQuiz(quest) = q\} \triangleleft questionPosition$ 
      The position of the questions is removed
  end
Event SHAREQUIZ  $\langle ordinary \rangle \hat{=}$ 
REQ13
any
  u1
  u2
  q
  where
    grd41::  $u1 \in loggedIn$ 
      the user must be logged in so that to share the quiz
    grd42::  $u2 \in registeredUser$ 
      the other user that will have access to the quiz
    grd43::  $u1 \neq u2$ 
      the two users cannot be the same person
    grd44::  $q \in quizzes$ 
    grd45::  $quizCreator(q) = u1$ 
      u1 must be the creator of the quiz
    grd46::  $q \in ran(belongingQuiz)$ 
      The quiz must contain at least 1 question in order to be shared
    grd47::  $q \mapsto u2 \notin sharedTo$ 
      the quiz must not have already been shared with u2
  then
    act41::  $sharedTo := sharedTo \cup \{q \mapsto u2\}$ 
  end
Event CREATEQUESTION  $\langle ordinary \rangle \hat{=}$ 
REQ7
any
  quest
  q
  u
  p
  where
    grd41::  $quest \in QUESTION \setminus questions$ 
      The question must be a new question
    grd42::  $q \in quizzes$ 
    grd43::  $u \in loggedIn$ 
      The user must be logged in in order to create a new question

```

```

    grd44:: quizCreator(q) = u
        The creator of the quiz must be u
    grd45:: p ∈ POSITION
    grd46:: ∀z·z ∈ questions ∧ belongingQuiz(z) = q ⇒ p > questionPosition(z)
        The question must be added at the end of the question list of the quiz
then
    act41:: questions := questions ∪ {quest}
    act42:: belongingQuiz(quest) := q
        the question quest belongs to q
    act43:: questionPosition(quest) := p
        The position of the question quest is p inside the question list of the quiz
end
Event REMOVEQUESTION ⟨ordinary⟩ ≐
REQ9
any
    u
    quest
    q
where
    grd41:: u ∈ loggedIn
        The user must be logged in order to remove a question
    grd42:: q ∈ quizzes
    grd43:: quest ∈ questions
    grd45:: belongingQuiz(quest) = q
        q must be the belonging quiz of quest
    grd44:: quizCreator(q) = u
        The creator of the quiz q must be u
then
    act41:: questions := questions \ {quest}
    act42:: belongingQuiz := {quest} ⧸ belongingQuiz
    act43:: questionPosition := {quest} ⧸ questionPosition
        The position of the question is removed
end
Event UPDATE_QUESTION_OK ⟨ordinary⟩ ≐
REQ8 this event updates just the text of the question
any
    u
    quest
    q
    result
where
    grd41:: u ∈ loggedIn
    grd42:: q ∈ quizzes
    grd43:: quizCreator(q) = u
        Only the quiz creator of q can update the question
    grd44:: quest ∈ questions
    grd45:: result = TRUE
        The update has been successfully
    grd46:: belongingQuiz(quest) = q
        the question must belong to q
then
    skip
end
Event UPDATE_QUESTION_NOT_OK ⟨ordinary⟩ ≐
REQ8 this event updates just the text of the question
any
    u
    quest
    q

```

```

    result
  where
    grd41::  $u \in \text{loggedIn}$ 
    grd42::  $q \in \text{quizzes}$ 
    grd43::  $\text{quizCreator}(q) = u$ 
    grd1:  $\text{quest} \in \text{questions}$ 
    grd45::  $\text{belongingQuiz}(\text{quest}) = q$ 
    grd46::  $\text{result} = \text{FALSE}$ 
    The update has not been successfully. The previous text of the question is restored
  then
    skip
  end
Event UNSHARE_QUIZ  $\langle \text{ordinary} \rangle \triangleq$ 
  any
    u1
    u2
    q
  where
    grd41:  $u1 \in \text{registeredUser}$ 
    grd42:  $u2 \in \text{registeredUser}$ 
    grd43:  $u1 \in \text{loggedIn}$ 
    A registerd user can unshare only if he/she is online
    grd44:  $u1 \neq u2$ 
    grd45:  $q \mapsto u2 \in \text{sharedTo}$ 
    u2 had to have access to the quiz
    grd46:  $u1 = \text{quizCreator}(q)$ 
    Only the creator of the quiz can unshare a quiz
  then
    act41:  $\text{sharedTo} := \text{sharedTo} \setminus \{q \mapsto u2\}$ 
  end
END

```

MACHINE m5**REFINES** m4**SEES** c3**VARIABLES**

registeredUser
 password
 loggedIn
 loggedOut
 quizzes
 questions
 quizCreator
 belongingQuiz
 sharedTo
 questionPosition
 answers
 correctAnswer
 belongingQuestion

INVARIANTS**inv51**: $answers \subseteq ANSWER$ **inv52**: $finite(answers)$ **inv53**: $belongingQuestion \in answers \rightarrow questions$

Every answer shall belong to exactly one question.

inv54: $correctAnswer \in questions \rightarrow answers$

Every question must have a correct answer and an answer can be the correct answer of at most 1 question (TOTAL INJECTIVITY)

inv55: $\forall quest \cdot quest \in questions \Rightarrow card(\{a \mid a \in answers \wedge belongingQuestion(a) = quest\}) \geq 2 \wedge card(\{a \mid a \in answers \wedge belongingQuestion(a) = quest\}) \leq 4$

Every question must have at least 2 answers and at most 4 answers

inv56: $\forall a, quest \cdot a \in answers \wedge quest \in questions \wedge correctAnswer(quest) = a \Rightarrow belongingQuestion(a) = quest$

The correct answer of a question shall belong to the question.

inv58: $correctAnswer \subseteq belongingQuestion^{-1}$

Actually this is a redundant invariant that has the same meaning as the invariant above

EVENTS**Initialisation** $\langle \text{extended} \rangle$ **begin**

act1: $registeredUser := \emptyset$
act21: $password := \emptyset$
act31: $loggedIn := \emptyset$
act32: $loggedOut := \emptyset$
act41: $quizzes := \emptyset$
act42: $questions := \emptyset$
act43: $quizCreator := \emptyset$
act44: $belongingQuiz := \emptyset$
act45: $sharedTo := \emptyset$
act46: $questionPosition := \emptyset$
act51: $answers := \emptyset$
act52: $correctAnswer := \emptyset$
act53: $belongingQuestion := \emptyset$

end**Event** REGISTER $\langle \text{ordinary} \rangle \hat{=}$ **extends** REGISTER**any**

u A user
 p


```

where
  grd1::  $u \in USER \setminus registeredUser$ 
    The user must not be already registered
  grd21::  $p \in PASSWORD$ 
then
  act1::  $registeredUser := registeredUser \cup \{u\}$ 
    The user is added to the set of registered users
  act21::  $password(u) := p$ 
    The password of user u is p
  act31::  $loggedOut := loggedOut \cup \{u\}$ 
    When a user u registers, u is added to the set of loggedOut users
end
Event LOGIN  $\langle ordinary \rangle \hat{=}$ 
extends LOGIN
  any
     $u$ 
     $p$ 
  where
    inv31::  $u \in loggedOut$ 
    inv32::  $p = password(u)$ 
      p must be the pssword of u
  then
    act31::  $loggedIn := loggedIn \cup \{u\}$ 
      The user u is added to the set of loggedIn users
    act32::  $loggedOut := loggedOut \setminus \{u\}$ 
      The user u is removed from the set of loggedOut users
  end
Event LOGOUT  $\langle ordinary \rangle \hat{=}$ 
extends LOGOUT
  any
     $u$ 
  where
    inv31::  $u \in loggedIn$ 
      The user u mst be logged in
  then
    act31::  $loggedIn := loggedIn \setminus \{u\}$ 
      The user u is removed from the set of loggedIn users
    act32::  $loggedOut := loggedOut \cup \{u\}$ 
      The user u is added to the set of loggedOut users
  end
Event CREATEQUIZ  $\langle ordinary \rangle \hat{=}$ 
extends CREATEQUIZ
  any
     $u$ 
     $q$ 
  where
    grd41::  $u \in loggedIn$ 
      A user must be logged in so that to create a quiz
    grd42::  $q \in QUIZ \setminus quizzes$ 
      The created quiz must not have been already created
  then
    act41::  $quizzes := quizzes \cup \{q\}$ 
      The created quiz is added to the dynamic set quizzes
    act42::  $quizCreator(q) := u$ 
      the creator of the quiz q is u
  end
Event REMOVEQUIZ  $\langle ordinary \rangle \hat{=}$ 
extends REMOVEQUIZ

```

```

any
  u
  q
where
  grd41::  $q \in quizzes$ 
  grd42::  $u \in loggedIn$ 
    The user must be logged in so that to remove a quiz
  grd43::  $quizCreator(q) = u$ 
    Only the creator of the quiz can remove the quiz
then
  act41::  $quizzes := quizzes \setminus \{q\}$ 
    the quiz is removed
  act42::  $quizCreator := \{q\} \triangleleft quizCreator$ 
    The quiz does not have anymore a creator because is removed
  act43::  $sharedTo := \{q\} \triangleleft sharedTo$ 
    All registered users that had access to the quiz, do not have access to it anymore because the quiz
    is removed
  act44::  $belongingQuiz := belongingQuiz \triangleright \{q\}$ 
    The questions of the quiz do not belong anymore to it
  act45::  $questions := questions \setminus \{quest | quest \in questions \wedge belongingQuiz(quest) = q\}$ 
    The questions of the quiz are removed
  act46::  $questionPosition := \{quest | quest \in questions \wedge belongingQuiz(quest) = q\} \triangleleft questionPosition$ 
    The position of the questions is removed
  act54::  $correctAnswer := \{q2 | q2 \in questions \wedge belongingQuiz(q2) = q\} \triangleleft correctAnswer$ 
    The correct answer of all questions of the quiz must be removed
  act55::  $belongingQuestion := belongingQuestion \triangleright \{q2 | q2 \in questions \wedge belongingQuiz(q2) = q\}$ 
    The answers of the questions of the quiz do not belong to the questions anymore
  act56:  $answers := answers \setminus \{a1 | a1 \in answers \wedge belongingQuestion(a1) \in \{quest1 | quest1 \in$ 
     $questions \wedge belongingQuiz(quest1) = q\}\}$ 
    Removing a quiz involves removing all answers of the questions of the quiz
end
Event SHAREQUIZ ⟨ordinary⟩  $\hat{=}$ 
extends SHAREQUIZ
any
  u1
  u2
  q
where
  grd41::  $u1 \in loggedIn$ 
    the user must be logged in so that to share the quiz
  grd42::  $u2 \in registeredUser$ 
    the other user that will have access to the quiz
  grd43::  $u1 \neq u2$ 
    the two users cannot be the same person
  grd44::  $q \in quizzes$ 
  grd45::  $quizCreator(q) = u1$ 
    u1 must be the creator of the quiz
  grd46:  $q \in ran(belongingQuiz)$ 
    The quiz must contain at least 1 question in order to be shared
  grd47:  $q \mapsto u2 \notin sharedTo$ 
    the quiz must not have already been shared with u2
then
  act41::  $sharedTo := sharedTo \cup \{q \mapsto u2\}$ 
end
Event CREATEQUESTION ⟨ordinary⟩  $\hat{=}$ 
extends CREATEQUESTION
any
  quest

```

```

    q
    u
    p
    a
    b
where
  grd41:: quest ∈ QUESTION \ questions
    The question must be a new question
  grd42:: q ∈ quizzes
  grd43:: u ∈ loggedIn
    The user must be logged in in order to create a new question
  grd44:: quizCreator(q) = u
    The creator of the quiz must be u
  grd45:: p ∈ POSITION
  grd46::  $\forall z. z \in \text{questions} \wedge \text{belongingQuiz}(z) = q \Rightarrow p > \text{questionPosition}(z)$ 
    The question must be added at the end of the question list of the quiz
  grd51::  $(a \in \text{ANSWER} \setminus \text{answers}) \wedge (b \in \text{ANSWER} \setminus \text{answers})$ 
    The 2 answers must be new ones
  grd52: a ≠ b
    The 2 answers must be different
then
  act41:: questions := questions ∪ {quest}
  act42:: belongingQuiz(quest) := q
    the question quest belongs to q
  act43:: questionPosition(quest) := p
    The position of the question quest is p inside the question list of the quiz q
  act51:: answers := answers ∪ {a, b}
  act53:: correctAnswer(quest) := a
    The correct answer is a
  act54:: belongingQuestion := belongingQuestion ∪ {a ↦ quest, b ↦ quest}
    The 2 new answers belong to the question quest
end
Event ADDANSWER ⟨ordinary⟩ ≐
REQ7
any
  quest
  q
  u
  a
where
  grd51:: u ∈ loggedIn
    The user us must be logged in
  grd52:: q ∈ quizzes
  grd53:: a ∈ ANSWER \ answers
  grd54:: quest ∈ questions
  grd55:: quizCreator(q) = u
    The user u must be the creator of the quiz
  grd56:: belongingQuiz(quest) = q
  grd57::  $\text{card}(\{a1 | a1 \in \text{answers} \wedge \text{belongingQuestion}(a1) = \text{quest}\}) < 4$ 
    The current answers of the question must be less than 4
then
  act51:: answers := answers ∪ {a}
  act52:: belongingQuestion(a) := quest
end
Event REMOVENOTCORRECTANSWER ⟨ordinary⟩ ≐
any
  quest
  q
  u

```

```

    a
  where
    grd51::  $u \in \text{loggedIn}$ 
      The user  $u$  must be logged in
    grd52::  $q \in \text{quizzes}$ 
    grd53::  $\text{quest} \in \text{questions}$ 
    grd54::  $a \in \text{answers}$ 
    grd55::  $\text{card}(\{a1 | a1 \in \text{answers} \wedge \text{belongingQuestion}(a1) = \text{quest}\}) > 2$ 
      The number of current answers of the question must be more than 2
    grd56::  $\text{correctAnswer}(\text{quest}) \neq a$ 
      The answer to be removed must not be the correct answer of the question
    grd57:  $\text{quizCreator}(q) = u$ 
      The user  $u$  must be the creator of the quiz
    grd58:  $\text{belongingQuiz}(\text{quest}) = q$ 
    grd59:  $\text{belongingQuestion}(a) = \text{quest}$ 
      The anser must belong to the quiz  $q$ 
  then
    act51::  $\text{answers} := \text{answers} \setminus \{a\}$ 
    act52::  $\text{belongingQuestion} := \{a\} \triangleleft \text{belongingQuestion}$ 
  end
Event REMOVECORRECTANSWER  $\langle \text{ordinary} \rangle \hat{=}$ 
  any
    quest
    q
    u
    a1
    a2
  where
    grd51::  $u \in \text{loggedIn}$ 
      The user  $u$  must be logged in
    grd52::  $\text{quest} \in \text{questions}$ 
    grd53::  $q \in \text{quizzes}$ 
    grd54::  $a1 \in \text{answers}$ 
    grd55::  $a2 \in \text{answers}$ 
    grd56::  $\text{correctAnswer}(\text{quest}) = a1$ 
      The answer to be removed must be the correct answer of the question
    grd57::  $\text{belongingQuestion}(a2) = \text{quest}$ 
      The new correct answer must belong to the question
    grd58:  $\text{quizCreator}(q) = u$ 
      The user  $u$  must be the creator of the quiz
    grd59:  $\text{belongingQuiz}(\text{quest}) = q$ 
    grd60:  $\text{belongingQuestion}(a1) = \text{quest}$ 
    grd61:  $\text{card}(\{a | a \in \text{answers} \wedge \text{belongingQuestion}(a) = \text{quest}\}) > 2$ 
      The current number of answers of the question must be greater than 2
    grd62:  $a1 \neq a2$ 
  then
    act51::  $\text{answers} := \text{answers} \setminus \{a1\}$ 
    act52::  $\text{belongingQuestion} := \{a1\} \triangleleft \text{belongingQuestion}$ 
    act53::  $\text{correctAnswer} := \text{correctAnswer} \triangleleft \{\text{quest} \mapsto a2\}$ 
      the new coorrect answer is  $a2$ 
  end
Event SETCORRECTANSWER  $\langle \text{ordinary} \rangle \hat{=}$ 
  any
    u
    q
    quest
    a1
    a2
  where

```

```

    grd51::  $u \in \text{loggedIn}$ 
        The user  $u$  must be logged in
    grd52::  $q \in \text{quizzes}$ 
    grd53::  $\text{quest} \in \text{questions}$ 
    grd54::  $a1 \in \text{answers}$ 
    grd55::  $a2 \in \text{answers}$ 
    grd56::  $a1 \neq a2$ 
    grd57:  $\text{quizCreator}(q) = u$ 
        The user  $u$  must be the creator of the quiz
    grd58:  $\text{belongingQuiz}(\text{quest}) = q$ 
    grd59:  $\text{correctAnswer}(\text{quest}) = a1$ 
         $a1$  must be the current correct answer of the question
    grd60:  $\text{belongingQuestion}(a2) = \text{quest}$ 
         $a2$  must belong to the question
  then
    act51::  $\text{correctAnswer} := \text{correctAnswer} \triangleleft \{\text{quest} \mapsto a2\}$ 
  end
Event UPDATE_ANSWER_OK  $\langle \text{ordinary} \rangle \triangleq$ 
  any
    a
    q
    quest
    result
    u
  where
    grd51::  $u \in \text{loggedIn}$ 
    grd52::  $a \in \text{answers}$ 
    grd53::  $q \in \text{quizzes}$ 
    grd54::  $\text{quest} \in \text{questions}$ 
    grd55::  $\text{belongingQuestion}(a) = \text{quest}$ 
    grd56:  $\text{quizCreator}(q) = u$ 
    grd57:  $\text{belongingQuiz}(\text{quest}) = q$ 
    grd58:  $\text{result} = \text{TRUE}$ 
        The update has been successful
  then
    skip
  end
Event UPDATE_ANSWER_NOT_OK  $\langle \text{ordinary} \rangle \triangleq$ 
  The event updates only the text of an answer
  any
    a
    q
    quest
    result
    u
  where
    grd51::  $u \in \text{loggedIn}$ 
        the user  $u$  must be logged in
    grd52::  $a \in \text{answers}$ 
    grd53::  $\text{quest} \in \text{questions}$ 
    grd54::  $q \in \text{quizzes}$ 
    grd55::  $\text{belongingQuestion}(a) = \text{quest}$ 
    grd56::  $\text{quizCreator}(q) = u$ 
         $u$  must be the creator of the quiz
    grd58::  $\text{belongingQuiz}(\text{quest}) = q$ 
    grd57::  $\text{result} = \text{FALSE}$ 
        The update has not been successful. The previous text is restored
  then
    skip

```

```

end
Event REMOVEQUESTION ⟨ordinary⟩ ≐
extends REMOVEQUESTION
any
  u
  quest
  q
where
  grd41:: u ∈ loggedIn
    The user must be logged in order to remove a question
  grd42:: q ∈ quizzes
  grd43:: quest ∈ questions
  grd45:: belongingQuiz(quest) = q
    q must be the belonging quiz of quest
  grd44:: quizCreator(q) = u
    The creator of the quiz q must be u
then
  act41:: questions := questions \ {quest}
  act42:: belongingQuiz := {quest} ◁ belongingQuiz
  act43:: questionPosition := {quest} ◁ questionPosition
    The position of the question is removed
  act51:: answers := answers \ {a | a ∈ answers ∧ belongingQuestion(a) = quest}
    the answers of the question must be removed when the question is removed
  act52:: correctAnswer := {quest} ◁ correctAnswer
    The correct answer of quest is not the correct answer anymore
  act53:: belongingQuestion := belongingQuestion ▷ {quest}
    All answers of the question do not belong to it anymore
end
Event UPDATE_QUESTION_OK ⟨ordinary⟩ ≐
extends UPDATE_QUESTION_OK
any
  u
  quest
  q
  result
where
  grd41:: u ∈ loggedIn
  grd42:: q ∈ quizzes
  grd43:: quizCreator(q) = u
    Only the quiz creator of q can update the question
  grd44:: quest ∈ questions
  grd45:: result = TRUE
    The update has been successfully
  grd46:: belongingQuiz(quest) = q
    the question must belong to q
then
  skip
end
Event UPDATE_QUESTION_NOT_OK ⟨ordinary⟩ ≐
extends UPDATE_QUESTION_NOT_OK
any
  u
  quest
  q
  result
where
  grd41:: u ∈ loggedIn
  grd42:: q ∈ quizzes

```

```

    grd43:: quizCreator(q) = u
    grd1: quest ∈ questions
    grd45:: belongingQuiz(quest) = q
    grd46:: result = FALSE
    The update has not been successfully. The previous text of the question is restored
  then
    skip
  end
Event UNSHARE_QUIZ ⟨ordinary⟩ ≐
extends UNSHARE_QUIZ
  any
    u1
    u2
    q
  where
    grd41: u1 ∈ registeredUser
    grd42: u2 ∈ registeredUser
    grd43: u1 ∈ loggedIn
    A registerd user can unshare only if he/she is online
    grd44: u1 ≠ u2
    grd45: q ↦ u2 ∈ sharedTo
    u2 had to have access to the quiz
    grd46: u1 = quizCreator(q)
    Only the creator of the quiz can unshare a quiz
  then
    act41: sharedTo := sharedTo \ {q ↦ u2}
  end
END

```

MACHINE m8**REFINES** m5**SEES** c4**VARIABLES**

registeredUser
 password
 loggedIn
 loggedOut
 quizzes
 questions
 quizCreator
 belongingQuiz
 sharedTo
 questionPosition
 answers
 correctAnswer
 belongingQuestion
 quizInstances
 host
 playingIn
 instanceOfQuiz
 currentQuestion
 quizCreated
 quizInit
 questioning
 questionSummary
 quizSummary
 finishedQuiz
 answeredQuestions
 peopleAnswers
 peopleSelectedAnswer

INVARIANTS

inv61;
quizInstances \subseteq *INSTANCE_QUIZ*

inv62;
partition(*quizInstances*, *quizCreated*, *quizInit*, *questioning*, *questionSummary*, *quizSummary*, *finishedQuiz*)

It describes all the possible states of every quiz instance

inv63;
host \in *quizInstances* \rightarrow *registeredUser*

Every quiz instance must be hosted by exactly one registered user. Notice that this relations must exist for every possible state of a quiz instance

inv64;
playingIn \in *USER* \leftrightarrow *quizInstances* \setminus (*quizCreated* \cup *finishedQuiz*)

A USER (registerd or not) can play in at most one quiz instance at a time (PARTIAL FUNCTION).

This relation must exist for all quiz instances that are not in the following states: *quizCreated*, *finishedQuiz*

inv65;
instanceOfQuiz \in *quizInstances* \leftrightarrow *quizzes*

It shall not be necessary for a quiz instance in the *finishedQuiz* state to be linked to a quiz because if the quiz is deleted, the quiz instance should be deleted as well.

inv66;
 $\forall qi. qi \in (quizInstances \setminus finishedQuiz) \Rightarrow host(qi) \notin playingIn^{-1}[\{qi\}]$

The host of an active quiz instance (not in the *finishedQuiz* state) shall not be allowed to be playing in the quiz instance he/she is hosting.

inv67;
 $\forall qi, q. q \in quizzes \wedge qi \in quizInstances \wedge qi \notin finishedQuiz \wedge instanceOfQuiz(qi) = q \Rightarrow host(qi) \in (\{quizCreator(q)\} \cup sharedTo[\{q\}]) \wedge host(qi) \in loggedIn$

The host of an active quiz instance, which is linked to a quiz q, must be the creator of q or must have access to q. The host of an active quiz instance must always be logged in

- inv68:** $currentQuestion \in (questioning \cup questionSummary) \rightarrow questions$
 A quiz instance in the questioning or questionSummary state shall be matched with the current question being played.
- inv69:** $answeredQuestions \in (quizInstances \setminus quizCreated) \rightarrow \mathbb{N}$
 A quiz instance which is not in the quizCreated state shall be linked to the number of questions answered up to now.
- inv610:** $\forall qi, quest \cdot qi \in quizInstances \wedge qi \in (questioning \cup questionSummary) \wedge quest \in questions \wedge (qi \mapsto quest) \in currentQuestion \Rightarrow belongingQuiz(quest) = instanceOfQuiz(qi)$
 The current question of any quiz instance in the questioning and questionSummary states shall be a question of the quiz the quiz instance is linked to
- inv611:** $\forall qi, q \cdot qi \in (questioning \cup questionSummary) \wedge q \in quizzes \wedge instanceOfQuiz(qi) = q \Rightarrow answeredQuestions(qi) \leq card(belongingQuiz^{-1}[\{q\}])$
 The number of answered questions of a quiz instance in the questioning or questionSummary state shall not be greater than the number of questions of the quiz the quiz instance is linked to.
- inv612:** $peopleAnswers \in dom(playingIn) \leftrightarrow questioning$
 It is a partial function from the domain of playingIn to the set questioning.
 This function indicates which players have answered the current question of a quiz instance in the questioning state.
- inv613:** $peopleAnswers \subseteq playingIn$
 every player can answer only a question of the quiz instance he/she is playing in
- inv614:** $\forall qi \cdot qi \in quizInstances \wedge qi \in questioning \Rightarrow (card(playingIn^{-1}[\{qi\}]) > 0)$
 A quiz instance in the questioning state shall being played by at least one player.
- inv615:** $\forall qi, q \cdot qi \in quizInstances \wedge qi \notin finishedQuiz \wedge q \in quizzes \wedge instanceOfQuiz(qi) = q \Rightarrow belongingQuiz^{-1}[\{q\}] \neq \emptyset$
 Every active (not finished) quiz instance must be linked to a quiz which must contain at least 1 question
- inv616:** $quizInstances \setminus finishedQuiz \subseteq dom(instanceOfQuiz)$
- inv617:** $\forall u \cdot u \in registeredUser \wedge u \in loggedIn \wedge u \in host[quizInstances \setminus finishedQuiz] \Rightarrow u \notin dom(playingIn)$
 The host of an active quiz instance shall not be allowed to be playing in another quiz instance.
- inv618:** $peopleSelectedAnswer \in dom(playingIn) \leftrightarrow answers$
 It is a partial function from the domain of playinIn to answers. It indicates what answers the players of an active quiz instance have selected
- inv619:** $(\forall qi \cdot qi \in quizInstances \Rightarrow qi \notin questioning) \Rightarrow peopleSelectedAnswer = \emptyset$
 The function is defined only when a quiz instance is in the questioning state.
- inv620:** $\forall p, a \cdot p \in USER \wedge p \in dom(playingIn) \wedge a \in answers \wedge p \mapsto a \in peopleSelectedAnswer \Rightarrow a \in belongingQuestion^{-1}[\{currentQuestion(playingIn(p))\}]$
 The players must select an answer of the current question of the quiz instance

EVENTS

Initialisation (extended)

begin

```

act1:: registeredUser := ∅
act21:: password := ∅
act31:: loggedIn := ∅
act32:: loggedOut := ∅
act41:: quizzes := ∅
act42:: questions := ∅
act43:: quizCreator := ∅
act44:: belongingQuiz := ∅
act45:: sharedTo := ∅
act46:: questionPosition := ∅
act51:: answers := ∅
act52:: correctAnswer := ∅
act53:: belongingQuestion := ∅
act61:: quizInstances := ∅
act62:: host := ∅
act63:: playingIn := ∅

```

```

    act64:: instanceOfQuiz :=  $\emptyset$ 
    act65:: peopleAnswers :=  $\emptyset$ 
    act66: answeredQuestions :=  $\emptyset$ 
    act67: currentQuestion :=  $\emptyset$ 
    act68: finishedQuiz :=  $\emptyset$ 
    act69: questioning :=  $\emptyset$ 
    act611: questionSummary :=  $\emptyset$ 
    act612: quizCreated :=  $\emptyset$ 
    act613: quizInit :=  $\emptyset$ 
    act614: quizSummary :=  $\emptyset$ 
    act615: peopleSelectedAnswer :=  $\emptyset$ 
  end
Event REGISTER  $\langle$ ordinary $\rangle \hat{=}$ 
extends REGISTER
  any
    u A user
    p
  where
    grd1:: u  $\in$  USER \ registeredUser
      The user must not be already registered
    grd21:: p  $\in$  PASSWORD
    grd81: u  $\notin$  dom(playingIn)
  then
    act1:: registeredUser := registeredUser  $\cup$  {u}
      The user is added to the set of registered users
    act21:: password(u) := p
      The password of user u is p
    act31:: loggedOut := loggedOut  $\cup$  {u}
      When a user u registers, u is added to the set of loggedOut users
  end
Event LOGIN  $\langle$ ordinary $\rangle \hat{=}$ 
extends LOGIN
  any
    u
    p
  where
    inv31:: u  $\in$  loggedOut
    inv32:: p = password(u)
      p must be the pssword of u
    grd81: u  $\notin$  dom(playingIn)
  then
    act31:: loggedIn := loggedIn  $\cup$  {u}
      The user u is added to the set of loggedIn users
    act32:: loggedOut := loggedOut \ {u}
      The user u is removed from the set of loggedOut users
  end
Event LOGOUT  $\langle$ ordinary $\rangle \hat{=}$ 
extends LOGOUT
  any
    u
  where
    inv31:: u  $\in$  loggedIn
      The user u mst be logged in
    grd81: u  $\notin$  host[quizInstances \ finishedQuiz]
      The host of an active quiz instance shall not be allowed to log out of the system.
    grd82: u  $\notin$  dom(playingIn)
  then
    act31:: loggedIn := loggedIn \ {u}
      The user u is removed from the set of loggedIn users

```

```

    act32:: loggedOut := loggedOut  $\cup$  {u}
        The user u is added to the set of loggedOut users
    end
Event CREATEQUIZ  $\langle$ ordinary $\rangle \hat{=}$ 
extends CREATEQUIZ
    any
        u
        q
    where
        grd41:: u  $\in$  loggedIn
            A user must be logged in so that to create a quiz
        grd42:: q  $\in$  QUIZ  $\setminus$  quizzes
            The created quiz must not have been already created
        grd61:: u  $\notin$  host[quizInstances  $\setminus$  finishedQuiz]
            The host of an active quiz instance shall not be allowed to create a quiz at the same time.
    then
        act41:: quizzes := quizzes  $\cup$  {q}
            The created quiz is added to the dynamic set quizzes
        act42:: quizCreator(q) := u
            the creator of the quiz q is u
    end
Event REMOVEQUIZ  $\langle$ ordinary $\rangle \hat{=}$ 
extends REMOVEQUIZ
    any
        u
        q
    where
        grd41:: q  $\in$  quizzes
        grd42:: u  $\in$  loggedIn
            The user must be logged in so that to remove a quiz
        grd43:: quizCreator(q) = u
            Only the creator of the quiz can remove the quiz
        grd61:: u  $\notin$  host[quizInstances  $\setminus$  finishedQuiz]
            The host of an active quiz instance shall not be allowed to remove a quiz at the same time.
        grd62:  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 
            The creator of a quiz shall not be allowed to remove a quiz if there exists an active quiz instance,
            linked to the quiz, being hosted at the same time.
    then
        act41:: quizzes := quizzes  $\setminus$  {q}
            the quiz is removed
        act42:: quizCreator := {q}  $\Leftarrow$  quizCreator
            The quiz does not have anymore a creator because is removed
        act43:: sharedTo := {q}  $\Leftarrow$  sharedTo
            All registered users that had access to the quiz, do not have access to it anymore because the quiz
            is removed
        act44:: belongingQuiz := belongingQuiz  $\ni$  {q}
            The questions of the quiz do not belong anymore to it
        act45:: questions := questions  $\setminus$  {quest | quest  $\in$  questions  $\wedge$  belongingQuiz(quest) = q}
            The questions of the quiz are removed
        act46:: questionPosition := {quest | quest  $\in$  questions  $\wedge$  belongingQuiz(quest) = q}  $\Leftarrow$  questionPosition
            The position of the questions is removed
        act54:: correctAnswer := {q2 | q2  $\in$  questions  $\wedge$  belongingQuiz(q2) = q}  $\Leftarrow$  correctAnswer
            The correct answer of all questions of the quiz must be removed
        act55:: belongingQuestion := belongingQuestion  $\ni$  {q2 | q2  $\in$  questions  $\wedge$  belongingQuiz(q2) = q}
            The answers of the questions of the quiz do not belong to the questions anymore
        act56: answers := answers  $\setminus$  {a1 | a1  $\in$  answers  $\wedge$  belongingQuestion(a1)  $\in$  {quest1 | quest1  $\in$ 
            questions  $\wedge$  belongingQuiz(quest1) = q}}
            Removing a quiz involves removing all answers of the questions of the quiz

```

```

    act61: instanceOfQuiz := instanceOfQuiz  $\triangleright$  {q}
  end
Event SHAREQUIZ ⟨ordinary⟩  $\hat{=}$ 
extends SHAREQUIZ
  any
    u1
    u2
    q
  where
    grd41:: u1  $\in$  loggedIn
      the user must be logged in so that to share the quiz
    grd42:: u2  $\in$  registeredUser
      the other user that will have access to the quiz
    grd43:: u1  $\neq$  u2
      the two users cannot be the same person
    grd44:: q  $\in$  quizzes
    grd45:: quizCreator(q) = u1
      u1 must be the creator of the quiz
    grd46: q  $\in$  ran(belongingQuiz)
      The quiz must contain at least 1 question in order to be shared
    grd47: q  $\mapsto$  u2  $\notin$  sharedTo
      the quiz must not have already been shared with u2
    grd61:: u1  $\notin$  host[quizInstances \ finishedQuiz]
      The host of an active quiz instance shall not be allowed to share a quiz at the same time.
  then
    act41:: sharedTo := sharedTo  $\cup$  {q  $\mapsto$  u2}
  end
Event CREATEQUESTION ⟨ordinary⟩  $\hat{=}$ 
extends CREATEQUESTION
  any
    quest
    q
    u
    p
    a
    b
  where
    grd41:: quest  $\in$  QUESTION \ questions
      The question must be a new question
    grd42:: q  $\in$  quizzes
    grd43:: u  $\in$  loggedIn
      The user must be logged in in order to create a new question
    grd44:: quizCreator(q) = u
      The creator of the quiz must be u
    grd45:: p  $\in$  POSITION
    grd46::  $\forall z. z \in \text{questions} \wedge \text{belongingQuiz}(z) = q \Rightarrow p > \text{questionPosition}(z)$ 
      The question must be added at the end of the question list of the quiz
    grd51:: (a  $\in$  ANSWER \ answers)  $\wedge$  (b  $\in$  ANSWER \ answers)
      The 2 answers must be new ones
    grd52: a  $\neq$  b
      The 2 answers must be different
    grd61:: u  $\notin$  host[quizInstances \ finishedQuiz]
      The host of an active quiz instance shall not be allowed to add a question to a quiz at the same time.
    grd62:  $\forall qi. qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$ 
      The creator of a quiz shall not be allowed to add a question to a quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
  then

```

```

    act41:: questions := questions  $\cup$  {quest}
    act42:: belongingQuiz(quest) := q
           the question quest belongs to q
    act43:: questionPosition(quest) := p
           The position of the question quest is p inside the question list of the quiz q
    act51:: answers := answers  $\cup$  {a, b}
    act53:: correctAnswer(quest) := a
           The correct answer is a
    act54:: belongingQuestion := belongingQuestion  $\cup$  {a  $\mapsto$  quest, b  $\mapsto$  quest}
           The 2 new answers belong to the question quest
end
Event ADDANSWER  $\langle$ ordinary $\rangle \hat{=}$ 
  REQ7
extends ADDANSWER
any
  quest
  q
  u
  a
where
  grd51:: u  $\in$  loggedIn
           The user u must be logged in
  grd52:: q  $\in$  quizzes
  grd53:: a  $\in$  ANSWER  $\setminus$  answers
  grd54:: quest  $\in$  questions
  grd55:: quizCreator(q) = u
           The user u must be the creator of the quiz
  grd56:: belongingQuiz(quest) = q
  grd57:: card({a1 | a1  $\in$  answers  $\wedge$  belongingQuestion(a1) = quest}) < 4
           The current answers of the question must be less than 4
  grd61:: u  $\notin$  host[quizInstances  $\setminus$  finishedQuiz]
           The host of an active quiz instance shall not be allowed to add an answer to a question of a quiz
           at the same time.
  grd62::  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

           The creator of a quiz shall not be allowed to add an answer to a question of a quiz if there exists
           an active quiz instance, linked to the quiz, being hosted at the same time.
then
  act51:: answers := answers  $\cup$  {a}
  act52:: belongingQuestion(a) := quest
end
Event REMOVENOTCORRECTANSWER  $\langle$ ordinary $\rangle \hat{=}$ 
extends REMOVENOTCORRECTANSWER
any
  quest
  q
  u
  a
where
  grd51:: u  $\in$  loggedIn
           The user u must be logged in
  grd52:: q  $\in$  quizzes
  grd53:: quest  $\in$  questions
  grd54:: a  $\in$  answers
  grd55:: card({a1 | a1  $\in$  answers  $\wedge$  belongingQuestion(a1) = quest}) > 2
           The number of current answers of the question must be more than 2
  grd56:: correctAnswer(quest)  $\neq$  a
           The answer to be removed must not be the correct answer of the question

```

grd57: $quizCreator(q) = u$
 The user u must be the creator of the quiz
 grd58: $belongingQuiz(quest) = q$
 grd59: $belongingQuestion(a) = quest$
 The answer must belong to the quiz q
 grd61: $u \notin host[quizInstances \setminus finishedQuiz]$
 The host of an active quiz instance shall not be allowed to remove a non-correct answer from a question of a quiz at the same time.
 grd62: $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$
 The creator of a quiz shall not be allowed to remove a non-correct answer from a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.

then
 act51: $answers := answers \setminus \{a\}$
 act52: $belongingQuestion := \{a\} \triangleleft belongingQuestion$
 end

Event REMOVECORRECTANSWER $\langle ordinary \rangle \hat{=}$
extends REMOVECORRECTANSWER
 any
 $quest$
 q
 u
 $a1$
 $a2$
 where
 grd51: $u \in loggedIn$
 The user u must be logged in
 grd52: $quest \in questions$
 grd53: $q \in quizzes$
 grd54: $a1 \in answers$
 grd55: $a2 \in answers$
 grd56: $correctAnswer(quest) = a1$
 The answer to be removed must be the correct answer of the question
 grd57: $belongingQuestion(a2) = quest$
 The new correct answer must belong to the question
 grd58: $quizCreator(q) = u$
 The user u must be the creator of the quiz
 grd59: $belongingQuiz(quest) = q$
 grd60: $belongingQuestion(a1) = quest$
 grd61: $card(\{a \mid a \in answers \wedge belongingQuestion(a) = quest\}) > 2$
 The current number of answers of the question must be greater than 2
 grd62: $a1 \neq a2$
 grd61: $u \notin host[quizInstances \setminus finishedQuiz]$
 The host of an active quiz instance shall not be allowed to remove the correct answer from a question of a quiz at the same time.
 grd63: $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$
 The creator of a quiz shall not be allowed to remove the correct answer from a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.

then
 act51: $answers := answers \setminus \{a1\}$
 act52: $belongingQuestion := \{a1\} \triangleleft belongingQuestion$
 act53: $correctAnswer := correctAnswer \triangleleft \{quest \mapsto a2\}$
 the new correct answer is $a2$
 end

Event SETCORRECTANSWER $\langle ordinary \rangle \hat{=}$
extends SETCORRECTANSWER

```

any
  u
  q
  quest
  a1
  a2
where
  grd51:: u ∈ loggedIn
    The user u must be logged in
  grd52:: q ∈ quizzes
  grd53:: quest ∈ questions
  grd54:: a1 ∈ answers
  grd55:: a2 ∈ answers
  grd56:: a1 ≠ a2
  grd57: quizCreator(q) = u
    The user u must be the creator of the quiz
  grd58: belongingQuiz(quest) = q
  grd59: correctAnswer(quest) = a1
    a1 must be the current correct answer of the question
  grd60: belongingQuestion(a2) = quest
    a2 must belong to the question
  grd61:: u ∉ host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to set the correct answer of a question of a quiz at the same time.
  grd62:  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

    The creator of a quiz shall not be allowed to set the correct answer
    of a question of the quiz if there exists an active quiz instance, linked to the quiz,
    being hosted at the same time.
then
  act51:: correctAnswer := correctAnswer  $\Leftarrow$  {quest  $\mapsto$  a2}
end
Event UPDATE_ANSWER_OK ⟨ordinary⟩  $\hat{=}$ 
extends UPDATE_ANSWER_OK
any
  a
  q
  quest
  result
  u
where
  grd51:: u ∈ loggedIn
  grd52:: a ∈ answers
  grd53:: q ∈ quizzes
  grd54:: quest ∈ questions
  grd55:: belongingQuestion(a) = quest
  grd56: quizCreator(q) = u
  grd57: belongingQuiz(quest) = q
  grd58: result = TRUE
    The update has been successful
  grd61:: u ∉ host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to update an answer of a question of a quiz at the same time.
  grd62:  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

    The creator of a quiz shall not be allowed to update an answer of a
    question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the
    same time.
then

```

```

    skip
end
Event UPDATE_ANSWER_NOT_OK ⟨ordinary⟩ ≐
extends UPDATE_ANSWER_NOT_OK
any
    a
    q
    quest
    result
    u
where
    grd51:: u ∈ loggedIn
        the user u must be logged in
    grd52:: a ∈ answers
    grd53:: quest ∈ questions
    grd54:: q ∈ quizzes
    grd55:: belongingQuestion(a) = quest
    grd56:: quizCreator(q) = u
        u must be the creator of the quiz
    grd58:: belongingQuiz(quest) = q
    grd57:: result = FALSE
        The update has not been successful. The previous text is restored
    grd61: u ∉ host[quizInstances \ finishedQuiz]
        The host of an active quiz instance shall not be allowed to update an answer of a
        quiz at the same time.
    grd62: ∀qi·qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

        The creator of a quiz shall not be allowed to update an answer of a
        question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the
        same time.
then
    skip
end
Event REMOVEQUESTION ⟨ordinary⟩ ≐
extends REMOVEQUESTION
any
    u
    quest
    q
where
    grd41:: u ∈ loggedIn
        The user must be logged in order to remove a question
    grd42:: q ∈ quizzes
    grd43:: quest ∈ questions
    grd45:: belongingQuiz(quest) = q
        q must be the belonging quiz of quest
    grd44:: quizCreator(q) = u
        The creator of the quiz q must be u
    grd61: u ∉ host[quizInstances \ finishedQuiz]
        The host of an active quiz instance shall not be allowed to remove a question from a quiz at the
        same time.
    grd62: ∀qi·qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

        The creator of a quiz shall not be allowed to remove a question from the quiz if there exists an
        active quiz instance, linked to the quiz, being hosted at the same time.
then
    act41:: questions := questions \ {quest}
    act42:: belongingQuiz := {quest} ⧸ belongingQuiz

```



```

act43:: questionPosition := {quest}  $\Leftarrow$  questionPosition
    The position of the question is removed
act51:: answers := answers \ {a | a ∈ answers ∧ belongingQuestion(a) = quest}
    the answers of the question must be removed when the question is removed
act52:: correctAnswer := {quest}  $\Leftarrow$  correctAnswer
    The correct answer of quest is not the correct answer anymore
act53:: belongingQuestion := belongingQuestion  $\triangleright$  {quest}
    All answers of the question do not belong to it anymore

end
Event UPDATE_QUESTION_OK ⟨ordinary⟩  $\hat{=}$ 
extends UPDATE_QUESTION_OK
any
    u
    quest
    q
    result
where
    grd41:: u ∈ loggedIn
    grd42:: q ∈ quizzes
    grd43:: quizCreator(q) = u
        Only the quiz creator of q can update the question
    grd44:: quest ∈ questions
    grd45:: result = TRUE
        The update has been successfully
    grd46:: belongingQuiz(quest) = q
        the question must belong to q
    grd61:: u  $\notin$  host[quizInstances \ finishedQuiz]
        The host of an active quiz instance shall not be allowed to update a question of a quiz at the
        same time.
    grd62::  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

        The creator of a quiz shall not be allowed to update a question of the quiz if there exists an active
        quiz instance, linked to the quiz, being hosted at the same time.

then
    skip
end
Event UPDATE_QUESTION_NOT_OK ⟨ordinary⟩  $\hat{=}$ 
extends UPDATE_QUESTION_NOT_OK
any
    u
    quest
    q
    result
where
    grd41:: u ∈ loggedIn
    grd42:: q ∈ quizzes
    grd43:: quizCreator(q) = u
    grd1:: quest ∈ questions
    grd45:: belongingQuiz(quest) = q
    grd46:: result = FALSE
        The update has not been successfully. The previous text of the question is restored
    grd61:: u  $\notin$  host[quizInstances \ finishedQuiz]
        The host of an active quiz instance shall not be allowed to update a question of a quiz at the
        same time.
    grd62::  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

        The creator of a quiz shall not be allowed to update a question of the quiz if there exists an active
        quiz instance, linked to the quiz, being hosted at the same time.

then

```

```

    skip
end
Event HOST_QUIZ_INSTANCE ⟨ordinary⟩ ≐
  REQ14
  any
    u
    q
    qi
  where
    grd61::  $u \in \text{loggedIn}$ 
      The user u must be logged in
    grd62::  $qi \in \text{INSTANCE\_QUIZ} \setminus \text{quizInstances}$ 
    grd63::  $q \in \text{quizzes}$ 
    grd65::  $u \notin \text{ran}((\text{finishedQuiz} \triangleleft \text{host}))$ 
      The user u must not be hosting any other active quiz instance
    grd66::  $u \in (\{\text{quizCreator}(q)\} \cup \text{sharedTo}[\{q\}])$ 
      The user u must be the creator or have access to the quiz
    grd67::  $\text{belongingQuiz}^{-1}[\{q\}] \neq \emptyset$ 
      The quiz must have at least 1 question
  then
    act61::  $\text{quizInstances} := \text{quizInstances} \cup \{qi\}$ 
    act62::  $\text{host}(qi) := u$ 
      The host of the quiz instance is u
    act63::  $\text{instanceOfQuiz}(qi) := q$ 
      The quiz instance is linked to the quiz q
    act64::  $\text{quizCreated} := \text{quizCreated} \cup \{qi\}$ 
      The quiz instance is in the quizCreated state
  end
Event BEGIN_QUIZ_INSTANCE ⟨ordinary⟩ ≐
  any
    u
    qi
  where
    grd61::  $u \in \text{loggedIn}$ 
      The user u must be logged in
    grd62::  $qi \in \text{quizCreated}$ 
      The quiz instance must be in the quizCreated state
    grd63::  $\text{host}(qi) = u$ 
      The host of the quiz instance must be u
  then
    act61::  $\text{quizCreated} := \text{quizCreated} \setminus \{qi\}$ 
      The quiz instance is not in the quizCreated state anymore
    act62::  $\text{quizInit} := \text{quizInit} \cup \{qi\}$ 
      The quiz instance becomes part of the quizInit state set
    act63::  $\text{answeredQuestions}(qi) := 0$ 
      No question has been answered so far
  end
Event START_QUIZ_INSTANCE ⟨ordinary⟩ ≐
  any
    u
    qi
    quest
  where
    grd61::  $u \in \text{loggedIn}$ 
      The user u must be logged in
    grd62::  $qi \in \text{quizInit}$ 
      The quiz instance must be in the quizInit state
    grd63::  $\text{host}(qi) = u$ 
      The host of the quiz instance must be u

```

grd64:: $\forall k \cdot \text{belongingQuiz}(k) = \text{instanceOfQuiz}(qi) \Rightarrow \text{questionPosition}(k) \geq \text{questionPosition}(\text{quest})$

The question of the quiz that will become the first question to be answered in the quiz instance must be the first one in the question list of the quiz

grd65: $qi \in \text{ran}(\text{playingIn})$
Some players must have joined the quiz during the quizInit state

then

act61:: $\text{quizInit} := \text{quizInit} \setminus \{qi\}$
The quiz is not in the quizInit state anymore

act62:: $\text{questioning} := \text{questioning} \cup \{qi\}$
The quiz instance is in the questioning state

act63:: $\text{currentQuestion}(qi) := \text{quest}$
The current question of the quiz instance is the first question of the question list of the quiz

end

Event JOIN_QUIZ_INSTANCE $\langle \text{ordinary} \rangle \hat{=}$

any

u
qi

where

grd61:: $u \in \text{USER}$
The player can be either regitered or unregistered

grd62:: $qi \in \text{quizInit}$
It is possible to join a quiz instanec only if it is in the quizInit state

grd63:: $u \neq \text{host}(qi)$
The player must not be the host of the quiz instance

grd64:: $u \notin \text{dom}(\text{playingIn})$
The player must not be playing in another quiz instance

grd1: $u \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$
The player cannot be any registered user that is hosting any active quiz instance

then

act64:: $\text{playingIn} := \text{playingIn} \cup \{u \mapsto qi\}$

end

Event ANSWER_QUESTION $\langle \text{ordinary} \rangle \hat{=}$

any

p
qi
quest
a

where

grd61:: $p \in \text{USER}$

grd62:: $qi \in \text{quizInstances}$

grd63:: $p \in \text{playingIn}^{-1}[\{qi\}]$
The player must be playing in the quiz instance

grd64:: $qi \in \text{questioning}$
The quiz instance must be in the questioning state

grd65: $\text{quest} \in \text{questions}$

grd66: $\text{currentQuestion}(qi) = \text{quest}$
The question the player is answering must be the current question

grd67: $a \in \text{answers}$

grd68: $a \in \text{belongingQuestion}^{-1}[\{\text{quest}\}]$
The answer being selected must belong to the current question of the quiz instance

grd69: $\text{card}(\text{peopleAnswers}^{-1}[\{qi\}]) < \text{card}(\text{playingIn}^{-1}[\{qi\}])$
A player of a quiz instance shall not be allowed to select an answer when all other players have answered because the quiz instance passes to the questionSummary state.

then

act61:: $\text{peopleAnswers} := \text{peopleAnswers} \cup \{p \mapsto qi\}$

act62: $\text{peopleSelectedAnswer} := \text{peopleSelectedAnswer} \Leftarrow \{p \mapsto a\}$

end

Event END_QUESTION_ALL_ANSWERED $\langle \text{ordinary} \rangle \hat{=}$

```

any
  qi
where
  grd61::  $qi \in \text{questioning}$ 
    The quiz instance must be in the questionig state
  grd62::  $\text{card}(\text{peopleAnswers}^{-1}[\{qi\}]) = \text{card}(\text{playingIn}^{-1}[\{qi\}])$ 
    All players must have answered
then
  act61::  $\text{questioning} := \text{questioning} \setminus \{qi\}$ 
    The quiz instance is not part of the questioning state anymore
  act62::  $\text{questionSummary} := \text{questionSummary} \cup \{qi\}$ 
    The quiz instance passes to the questionSummary state
  act63::  $\text{answeredQuestions}(qi) := \text{answeredQuestions}(qi) + 1$ 
    The number of answered questions is incremented by 1
  act64::  $\text{peopleAnswers} := \text{peopleAnswers} \triangleright \{qi\}$ 
    The players that have answered the question of the quiz instance are removed
  act65::  $\text{peopleSelectedAnswer} := \text{playingIn}^{-1}[\{qi\}] \triangleleft \text{peopleSelectedAnswer}$ 
    The answers select by the players of the quiz instance are removed
end
Event END_QUESTION_PREMATURATELY  $\langle \text{ordinary} \rangle \hat{=}$ 
any
  u
  qi
where
  grd61::  $qi \in \text{questioning}$ 
    The quiz instance must be in the question state
  grd62::  $u \in \text{loggedIn}$ 
    The user u must be logged in
  grd63::  $\text{host}(qi) = u$ 
    The host of the quiz instance must be u
  grd1:  $\text{card}(\text{peopleAnswers}^{-1}[\{qi\}]) \neq \text{card}(\text{playingIn}^{-1}[\{qi\}])$ 
    The host of a quiz instance in the questioning state
    shall not be allowed to end prematurely a question
    if all players have answered because the quiz instance passes to the questionSummary state.
then
  act61::  $\text{questioning} := \text{questioning} \setminus \{qi\}$ 
    The quiz instance is not in the questioning state anymore
  act62::  $\text{questionSummary} := \text{questionSummary} \cup \{qi\}$ 
    The quiz instance passes to the questionSummary state
  act63::  $\text{answeredQuestions}(qi) := \text{answeredQuestions}(qi) + 1$ 
    The number of answered questions of the quiz instance is incremebted by 1
  act64::  $\text{peopleAnswers} := \text{peopleAnswers} \triangleright \{qi\}$ 
    The players that have answered the question of the quiz instance are removed
  act65::  $\text{peopleSelectedAnswer} := \text{playingIn}^{-1}[\{qi\}] \triangleleft \text{peopleSelectedAnswer}$ 
    The answers select by the players of the quiz instance are removed
end
Event SHOW_QUESTION_SUMMARY_TO_PLAYERS  $\langle \text{ordinary} \rangle \hat{=}$ 
any
  u
  qi
where
  grd61::  $u \in \text{loggedIn}$ 
    The user u must be logged in
  grd62::  $qi \in \text{quizInstances}$ 
  grd63::  $\text{host}(qi) = u$ 
    The user u must be the host of the quiz instance
  grd63:  $qi \in \text{questionSummary}$ 
    The quiz instance must be in the questionSummary state

```

```

    grd64:  $qi \in \text{ran}(\text{playingIn})$ 
        The host of a quiz instance in the questionSummary state shall
        be allowed to show the question summary only if at least 1 player is playing in the quiz instance.
  then
    skip
  end
Event NEXT_QUESTION ⟨ordinary⟩ ≐
  any
    u
    qi
    quest
  where
    grd61:  $u \in \text{loggedIn}$ 
    grd62:  $qi \in \text{questionSummary}$ 
        The quiz instance must be in the questionSummary state
    grd63:  $\text{host}(qi) = u$ 
    grd64:  $\text{answeredQuestions}(qi) < \text{card}(\text{belongingQuiz}^{-1}[\{\text{instanceOfQuiz}(qi)\}])$ 
        There must be other questions to be answered
    grd65:  $qi \in \text{ran}(\text{playingIn})$ 
        At least 1 player must be playing in the quiz instance
    grd66:  $\text{quest} \in \text{questions}$ 
    grd67:  $\text{card}(\{\text{quests} \mid \text{quests} \in \text{questions} \wedge \text{quests} \in \text{belongingQuiz}^{-1}[\{\text{instanceOfQuiz}(qi)\}] \wedge$ 
         $\text{questionPosition}(\text{quests}) < \text{questionPosition}(\text{quest})\}) = \text{answeredQuestions}(qi)$ 
        The next question to be answered must be the successive one
  then
    act61:  $\text{questionSummary} := \text{questionSummary} \setminus \{qi\}$ 
        The quiz instance is not in the questionSummary state anymore
    act62:  $\text{questioning} := \text{questioning} \cup \{qi\}$ 
        The quiz instance passes to the questioning state
    act63:  $\text{currentQuestion}(qi) := \text{quest}$ 
        The current question is set to the successive question
  end
Event FINISH_QUIZ_INSTANCE ⟨ordinary⟩ ≐
  any
    u
    qi
  where
    grd61:  $u \in \text{loggedIn}$ 
        The user must be logged in
    grd62:  $qi \in \text{questionSummary}$ 
        The quiz instance must be in the questionSummary state
    grd63:  $\text{host}(qi) = u$ 
        The user u must be the host of the quiz instance
  then
    act61:  $\text{questionSummary} := \text{questionSummary} \setminus \{qi\}$ 
        The quiz instance is not in the questionSummary state anymore
    act62:  $\text{quizSummary} := \text{quizSummary} \cup \{qi\}$ 
        The quiz instance passes to the quizSummary state
    act63:  $\text{currentQuestion} := \{qi\} \triangleleft \text{currentQuestion}$ 
        The current question of the quiz instance is removed as it is not anymore in the questionSummary
        state
  end
Event SHOW_QUIZ_INSTANCE_SUMMARY_TO_PLAYERS ⟨ordinary⟩ ≐
  any
    qi
    u
  where
    grd61:  $qi \in \text{quizInstances}$ 

```

```

    grd62:  $qi \in quizSummary$ 
        The quiz instance must be in the quizSummary state
    grd63:  $u \in registeredUser$ 
    grd64:  $u \in loggedIn$ 
        The user u must be logged in
    grd65:  $host(qi) = u$ 
        The user u must be the host of the quiz instance
    grd66:  $qi \in ran(playingIn)$ 
        there must at least 1 player playing in the quiz instance
  then
    skip
  end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_SUMMARY_STATE  $\langle ordinary \rangle \triangleq$ 
  any
    u
    qi
  where
    grd61::  $u \in loggedIn$ 
        The user u must be logged in
    grd62::  $qi \in quizSummary$ 
        The quiz instance must be in the quizSummary state
    grd63::  $host(qi) = u$ 
        The user u must be the host of the quiz instance
  then
    act61::  $quizSummary := quizSummary \setminus \{qi\}$ 
        The quiz instance is not in the quizSummary state anymore
    act62::  $finishedQuiz := finishedQuiz \cup \{qi\}$ 
        The quiz instance passes to the finishedQuiz state
    act63:  $playingIn := playingIn \triangleright \{qi\}$ 
        The players of the quiz instance do not play anymore in the quiz instance
  end
Event LEAVE_QUIZ_INSTANCE_NOT_IN_QUESTIONING_STATE  $\langle ordinary \rangle \triangleq$ 
  any
    p
    qi
  where
    grd61:  $p \in USER$ 
    grd62:  $qi \in quizInstances \setminus (quizCreated \cup finishedQuiz \cup questioning)$ 
        The quiz instance must not be in the quiz created state, finishedQuiz or questioning state
    grd63:  $p \in playingIn^{-1}[\{qi\}]$ 
        The player must be playing in the quiz instance
  then
    act61:  $playingIn := \{p\} \triangleleft playingIn$ 
        The player does not play anymore in the quiz instance
  end
Event LEAVE_QUIZ_INSTANCE_LAST_ONE_IN_QUESTIONING_STATE  $\langle ordinary \rangle \triangleq$ 
  any
    p
    qi
  where
    grd61:  $p \in USER$ 
    grd62:  $qi \in questioning$ 
        The quiz instance must be in the questioning state
    grd63:  $p \in playingIn^{-1}[\{qi\}]$ 
        The player must be playing in the quiz instance
    grd64:  $card(playingIn^{-1}[\{qi\}]) = 1$ 
        The player must be the only player be playing in the quiz instance
  then

```

```

    act61: playingIn := {p}  $\triangleleft$  playingIn
        The player does not play anymore in the quiz instance
    act62: peopleAnswers := {p}  $\triangleleft$  peopleAnswers
        It is removed whether the player has answered the question or not
    act63: questioning := questioning \ {qi}
    act64: questionSummary := questionSummary  $\cup$  {qi}
        The quiz instance passes to the questionSummary state
    act65: peopleSelectedAnswer := {p}  $\triangleleft$  peopleSelectedAnswer
        The answer selected by the player is removed (if he/she has answered)
end
Event LEAVE_QUIZ_INSTANCE_NOT_LAST_ONE_IN_QUESTIONING_STATE  $\langle$ ordinary $\rangle \hat{=}$ 
any
    p
    qi
where
    grd61: p  $\in$  USER
    grd62: qi  $\in$  questioning
    grd63: p  $\in$  playingIn-1{qi}
    grd64: card(playingIn-1{qi}) > 1
        There must be at least 2 players be playing
then
    act61: playingIn := {p}  $\triangleleft$  playingIn
    act62: peopleAnswers := {p}  $\triangleleft$  peopleAnswers
    act63: peopleSelectedAnswer := {p}  $\triangleleft$  peopleSelectedAnswer
end
Event UNSHARE_QUIZ  $\langle$ ordinary $\rangle \hat{=}$ 
extends UNSHARE_QUIZ
any
    u1
    u2
    q
where
    grd41: u1  $\in$  registeredUser
    grd42: u2  $\in$  registeredUser
    grd43: u1  $\in$  loggedIn
        A registered user can unshare only if he/she is online
    grd44: u1  $\neq$  u2
    grd45: q  $\mapsto$  u2  $\in$  sharedTo
        u2 had to have access to the quiz
    grd46: u1 = quizCreator(q)
        Only the creator of the quiz can unshare a quiz
    grd81: u2  $\notin$  host[instanceOfQuiz-1{q} \ finishedQuiz]
        The creator of a quiz shall not be allowed to deshare a quiz
        with another registered user if the latter is hosting a quiz instance linked to the quiz.
    grd82: u1  $\notin$  host[quizInstances \ finishedQuiz]
        The creator of a quiz shall not be allowed to deshare a
        quiz if he/she is hosting an active quiz instance.
then
    act41: sharedTo := sharedTo \ {q  $\mapsto$  u2}
end
Event REMOVE_QUIZ_INSTANCE  $\langle$ ordinary $\rangle \hat{=}$ 
any
    u
    qi
where
    grd81: u  $\in$  registeredUser
    grd82: qi  $\in$  quizInstances
    grd83: qi  $\in$  finishedQuiz
        It is possible to remove a quiz instance only when it is in the finishedQuiz state

```

```

    grd84:  $u \in \text{loggedIn}$ 
           The user must be logged in
    grd85:  $\text{host}(qi) = u$ 
           The user  $u$  must be the host of the quiz instance
    grd86:  $u \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$ 
           The user must not be hosting any active quiz instance
  then
    act81:  $\text{quizInstances} := \text{quizInstances} \setminus \{qi\}$ 
           The quiz instance is removed
    act82:  $\text{finishedQuiz} := \text{finishedQuiz} \cup \{qi\}$ 
           The quiz instance is removed from the finishedQuiz state
    act83:  $\text{host} := \{qi\} \triangleleft \text{host}$ 
           The user is not the host of the quiz instance anymore
    act84:  $\text{instanceOfQuiz} := \{qi\} \triangleleft \text{instanceOfQuiz}$ 
           The quiz instance is not linked anymore to a quiz
    act85:  $\text{answeredQuestions} := \{qi\} \triangleleft \text{answeredQuestions}$ 
           The number of answered questions of the quiz instance is removed
  end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_CREATED_STATE  $\langle \text{ordinary} \rangle \triangleq$ 
  any
    u
    qi
  where
    grd91:  $u \in \text{registeredUser}$ 
    grd92:  $u \in \text{loggedIn}$ 
           The user  $u$  must be loggedIn
    grd93:  $qi \in \text{quizInstances}$ 
    grd94:  $qi \in \text{quizCreated}$ 
           The quiz instance must be in the quizCreated state
    grd95:  $\text{host}(qi) = u$ 
           The user  $u$  must be the host of the quiz instance
  then
    act91:  $\text{quizCreated} := \text{quizCreated} \setminus \{qi\}$ 
           The quiz instance is removed from the quizCreated state
    act92:  $\text{finishedQuiz} := \text{finishedQuiz} \cup \{qi\}$ 
           The quiz instance passes to the finishedQuiz state
    act93:  $\text{answeredQuestions}(qi) := 0$ 
           The number of answered questions is set to 0
  end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_INIT_STATE  $\langle \text{ordinary} \rangle \triangleq$ 
  any
    u
    qi
  where
    grd81:  $u \in \text{registeredUser}$ 
    grd82:  $u \in \text{loggedIn}$ 
           The user  $u$  must be loggedIn
    grd83:  $qi \in \text{quizInstances}$ 
    grd84:  $qi \in \text{quizInit}$ 
           The quiz instance must be in the quizInit state
    grd85:  $\text{host}(qi) = u$ 
           The user  $u$  must be the host of the quiz instance
  then
    act81:  $\text{quizInit} := \text{quizInit} \setminus \{qi\}$ 
           The quiz instance is not anymore in the quizInit state
    act82:  $\text{finishedQuiz} := \text{finishedQuiz} \cup \{qi\}$ 
           The quiz instance passes to the finishedQuiz state
    act83:  $\text{playingIn} := \text{playingIn} \triangleright \{qi\}$ 
           The players of the quiz instance do not play anymore in the quiz instance

```



```

end
Event END_QUESTION_TIME_IS_UP ⟨ordinary⟩ ≐
any
  qi
where
  grd61:  $qi \in quizInstances$ 
  grd62:  $qi \in questioning$ 
  The quiz instance must be in the questioning state
then
  act61:  $questioning := questioning \setminus \{qi\}$ 
  act62:  $questionSummary := questionSummary \cup \{qi\}$ 
  The quiz instance passes to the questionSummary state
  act63:  $answeredQuestions(qi) := answeredQuestions(qi) + 1$ 
  The number of answered questions of the quiz instance is incremented by 1
  act64:  $peopleAnswers := peopleAnswers \triangleright \{qi\}$ 
  act65:  $peopleSelectedAnswer := playingIn^{-1}[\{qi\}] \triangleleft peopleSelectedAnswer$ 
end
END

```

MACHINE m9**REFINES** m8**SEES** c5**VARIABLES**

registeredUser
 password
 loggedIn
 loggedOut
 quizzes
 questions
 quizCreator
 belongingQuiz
 sharedTo
 questionPosition
 answers
 correctAnswer
 belongingQuestion
 quizInstances
 host
 playingIn
 instanceOfQuiz
 currentQuestion
 quizInit
 questioning
 questionSummary
 quizSummary
 finishedQuiz
 answeredQuestions
 peopleAnswers
 quizCreated
 embeddedQuestions
 reports
 summaryFor
 reportedBy
 qSummary
 qReportedBy
 peopleSelectedAnswer

INVARIANTS

inv91: $embeddedQuestions \in quizInstances \setminus finishedQuiz \leftrightarrow questions$

Every quiz instance (not finished) must keep track of the questions
the quiz they are linked to contains

inv92: $qSummary \subseteq QUESTION_SUMMARY$

The set of summary of the questions

inv93: $reports \subseteq REPORT$

The set of reports

inv94: $summaryFor \in qSummary \mapsto embeddedQuestions$

every question summary must be the summary of a question in a certain quiz instance

inv95: $qReportedBy \in qSummary \rightarrow reports$

every question summary is linked to exactly one report

inv96: $reportedBy \in quizInstances \rightarrow reports$

(TOTAL SURJECTION) Every quiz instance must have exactly one report and a report must be
reporting
exactly one quiz instance

inv97: $(\forall qi. qi \in quizInstances \Rightarrow qi \in finishedQuiz) \Rightarrow qSummary = \emptyset$

The summaries of the questions of a quiz instance must exist only when the quiz instance is active (not finished).
These summaries will help construct the report of the whole quiz instance

EVENTS

Initialisation \langle extended \rangle

begin

```
act1:: registeredUser :=  $\emptyset$ 
act21:: password :=  $\emptyset$ 
act31:: loggedIn :=  $\emptyset$ 
act32:: loggedOut :=  $\emptyset$ 
act41:: quizzes :=  $\emptyset$ 
act42:: questions :=  $\emptyset$ 
act43:: quizCreator :=  $\emptyset$ 
act44:: belongingQuiz :=  $\emptyset$ 
act45:: sharedTo :=  $\emptyset$ 
act46:: questionPosition :=  $\emptyset$ 
act51:: answers :=  $\emptyset$ 
act52:: correctAnswer :=  $\emptyset$ 
act53:: belongingQuestion :=  $\emptyset$ 
act61:: quizInstances :=  $\emptyset$ 
act62:: host :=  $\emptyset$ 
act63:: playingIn :=  $\emptyset$ 
act64:: instanceOfQuiz :=  $\emptyset$ 
act65:: peopleAnswers :=  $\emptyset$ 
act66:: answeredQuestions :=  $\emptyset$ 
act67:: currentQuestion :=  $\emptyset$ 
act68:: finishedQuiz :=  $\emptyset$ 
act69:: questioning :=  $\emptyset$ 
act611:: questionSummary :=  $\emptyset$ 
act612:: quizCreated :=  $\emptyset$ 
act613:: quizInit :=  $\emptyset$ 
act614:: quizSummary :=  $\emptyset$ 
act615:: peopleSelectedAnswer :=  $\emptyset$ 
act91:: embeddedQuestions :=  $\emptyset$ 
act92:: reports :=  $\emptyset$ 
act93:: summaryFor :=  $\emptyset$ 
act94:: reportedBy :=  $\emptyset$ 
act95:: qSummary :=  $\emptyset$ 
act96:: qReportedBy :=  $\emptyset$ 
```

end

Event REGISTER \langle ordinary $\rangle \hat{=}$

extends REGISTER

any

u A user

p

where

```
grd1::  $u \in USER \setminus registeredUser$ 
      The user must not be already registered
grd21::  $p \in PASSWORD$ 
grd81::  $u \notin dom(playingIn)$ 
```

then

```
act1:: registeredUser := registeredUser  $\cup \{u\}$ 
      The user is added to the set of registered users
act21:: password( $u$ ) :=  $p$ 
      The password of user  $u$  is  $p$ 
act31:: loggedOut := loggedOut  $\cup \{u\}$ 
      When a user  $u$  registers,  $u$  is added to the set of loggedOut users
```

```

    end
Event LOGIN ⟨ordinary⟩ ≐
extends LOGIN
  any
    u
    p
  where
    inv31:: u ∈ loggedOut
    inv32:: p = password(u)
             p must be the pssword of u
    grd81: u ∉ dom(playingIn)
  then
    act31:: loggedIn := loggedIn ∪ {u}
             The user u is added to the set of loggedIn users
    act32:: loggedOut := loggedOut \ {u}
             The user u is removed from the set of loggedOut users
  end
Event LOGOUT ⟨ordinary⟩ ≐
extends LOGOUT
  any
    u
  where
    inv31:: u ∈ loggedIn
             The user u mst be logged in
    grd81: u ∉ host[quizInstances \ finishedQuiz]
             The host of an active quiz instance shall not be allowed to log out of the system.
    grd82: u ∉ dom(playingIn)
  then
    act31:: loggedIn := loggedIn \ {u}
             The user u is removed from the set of loggedIn users
    act32:: loggedOut := loggedOut ∪ {u}
             The user u is added to the set of loggedOut users
  end
Event CREATEQUIZ ⟨ordinary⟩ ≐
extends CREATEQUIZ
  any
    u
    q
  where
    grd41:: u ∈ loggedIn
             A user must be logged in so that to create a quiz
    grd42:: q ∈ QUIZ \ quizzes
             The created quiz must not have been already created
    grd61:: u ∉ host[quizInstances \ finishedQuiz]
             The host of an active quiz instance shall not be allowed to create a quiz at the same time.
  then
    act41:: quizzes := quizzes ∪ {q}
             The created quiz is added to the dynamic set quizzes
    act42:: quizCreator(q) := u
             the creator of the quiz q is u
  end
Event REMOVEQUIZ ⟨ordinary⟩ ≐
extends REMOVEQUIZ
  any
    u
    q
  where
    grd41:: q ∈ quizzes

```

```

grd42:: u ∈ loggedIn
    The user must be logged in so that to remove a quiz
grd43:: quizCreator(q) = u
    Only the creator of the quiz can remove the quiz
grd61:: u ∉ host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to remove a quiz at the same time.
grd62:  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

    The creator of a quiz shall not be allowed to remove a quiz if there exists an active quiz instance,
    linked to the quiz, being hosted at the same time.
then
act41:: quizzes := quizzes \ {q}
    the quiz is removed
act42:: quizCreator := {q}  $\Leftarrow$  quizCreator
    The quiz does not have anymore a creator because is removed
act43:: sharedTo := {q}  $\Leftarrow$  sharedTo
    All registered users that had access to the quiz, do not have access to it anymore because the quiz
    is removed
act44:: belongingQuiz := belongingQuiz  $\ni$  {q}
    The questions of the quiz do not belong anymore to it
act45:: questions := questions \ {quest | quest ∈ questions ∧ belongingQuiz(quest) = q}
    The questions of the quiz are removed
act46:: questionPosition := {quest | quest ∈ questions ∧ belongingQuiz(quest) = q}  $\Leftarrow$  questionPosition

    The position of the questions is removed
act54:: correctAnswer := {q2 | q2 ∈ questions ∧ belongingQuiz(q2) = q}  $\Leftarrow$  correctAnswer
    The correct answer of all questions of the quiz must be removed
act55:: belongingQuestion := belongingQuestion  $\ni$  {q2 | q2 ∈ questions ∧ belongingQuiz(q2) = q}
    The answers of the questions of the quiz do not belong to the questions anymore
act56: answers := answers \ {a1 | a1 ∈ answers ∧ belongingQuestion(a1) ∈ {quest1 | quest1 ∈
    questions ∧ belongingQuiz(quest1) = q}}
    Removing a quiz involves removing all answers of the questions of the quiz
act61: instanceOfQuiz := instanceOfQuiz  $\ni$  {q}

end
Event SHAREQUIZ ⟨ordinary⟩  $\hat{=}$ 
extends SHAREQUIZ
any
    u1
    u2
    q
where
grd41:: u1 ∈ loggedIn
    the user must be logged in so that to share the quiz
grd42:: u2 ∈ registeredUser
    the other user that will have access to the quiz
grd43:: u1 ≠ u2
    the two users cannot be the same person
grd44:: q ∈ quizzes
grd45:: quizCreator(q) = u1
    u1 must be the creator of the quiz
grd46: q ∈ ran(belongingQuiz)
    The quiz must contain at least 1 question in order to be shared
grd47: q  $\mapsto$  u2 ∉ sharedTo
    the quiz must not have already been shared with u2
grd61:: u1 ∉ host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to share a quiz at the same time.
then
act41:: sharedTo := sharedTo ∪ {q  $\mapsto$  u2}
end

```

Event CREATEQUESTION $\langle \text{ordinary} \rangle \hat{=}$

extends CREATEQUESTION

any

quest

q

u

p

a

b

where

grd41:: *quest* $\in \text{QUESTION} \setminus \text{questions}$

The question must be a new question

grd42:: *q* $\in \text{quizzes}$

grd43:: *u* $\in \text{loggedIn}$

The user must be logged in in order to create a new question

grd44:: *quizCreator*(*q*) = *u*

The creator of the quiz must be u

grd45:: *p* $\in \text{POSITION}$

grd46:: $\forall z \cdot z \in \text{questions} \wedge \text{belongingQuiz}(z) = q \Rightarrow p > \text{questionPosition}(z)$

The question must be added at the end of the question list of the quiz

grd51:: $(a \in \text{ANSWER} \setminus \text{answers}) \wedge (b \in \text{ANSWER} \setminus \text{answers})$

The 2 answers must be new ones

grd52: *a* \neq *b*

The 2 answers must be different

grd61:: *u* $\notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$

The host of an active quiz instance shall not be allowed to add a question to a quiz at the same time.

grd62: $\forall qi \cdot qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$

The creator of a quiz shall not be allowed to add a question to a quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.

then

act41:: *questions* := *questions* \cup {*quest*}

act42:: *belongingQuiz*(*quest*) := *q*

the question *quest* belongs to *q*

act43:: *questionPosition*(*quest*) := *p*

The position of the question *quest* is *p* inside the question list of the quiz *q*

act51:: *answers* := *answers* \cup {*a*, *b*}

act53:: *correctAnswer*(*quest*) := *a*

The correct answer is *a*

act54:: *belongingQuestion* := *belongingQuestion* \cup {*a* \mapsto *quest*, *b* \mapsto *quest*}

The 2 new answers belong to the question *quest*

end

Event ADDANSWER $\langle \text{ordinary} \rangle \hat{=}$

REQ7

extends ADDANSWER

any

quest

q

u

a

where

grd51:: *u* $\in \text{loggedIn}$

The user *u* must be logged in

grd52:: *q* $\in \text{quizzes}$

grd53:: *a* $\in \text{ANSWER} \setminus \text{answers}$

grd54:: *quest* $\in \text{questions}$

grd55:: *quizCreator*(*q*) = *u*

The user *u* must be the creator of the quiz

```

    grd56:: belongingQuiz(quest) = q
    grd57:: card({a1|a1 ∈ answers ∧ belongingQuestion(a1) = quest}) < 4
        The current answers of the question must be less than 4
    grd61:: u ∉ host[quizInstances \ finishedQuiz]
        The host of an active quiz instance shall not be allowed to add an answer to a question of a quiz
        at the same time.
    grd62: ∀qi·qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

        The creator of a quiz shall not be allowed to add an answer to a question of a quiz if there exists
        an active quiz instance, linked to the quiz, being hosted at the same time.

then
    act51:: answers := answers ∪ {a}
    act52:: belongingQuestion(a) := quest
end

Event REMOVENOTCORRECTANSWER ⟨ordinary⟩ ≐
extends REMOVENOTCORRECTANSWER
any
    quest
    q
    u
    a
where
    grd51:: u ∈ loggedIn
        The user u must be logged in
    grd52:: q ∈ quizzes
    grd53:: quest ∈ questions
    grd54:: a ∈ answers
    grd55:: card({a1|a1 ∈ answers ∧ belongingQuestion(a1) = quest}) > 2
        The number of current answers of the question must be more than 2
    grd56:: correctAnswer(quest) ≠ a
        The answer to be removed must not be the correct answer of the question
    grd57: quizCreator(q) = u
        The user u must be the creator of the quiz
    grd58: belongingQuiz(quest) = q
    grd59: belongingQuestion(a) = quest
        The answer must belong to the quiz q
    grd61:: u ∉ host[quizInstances \ finishedQuiz]
        The host of an active quiz instance shall not be allowed to remove a non-correct answer from a
        question of a quiz at the same time.
    grd62: ∀qi·qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

        The creator of a quiz shall not be allowed to remove a non-correct answer from a question
        of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same
        time.

then
    act51:: answers := answers \ {a}
    act52:: belongingQuestion := {a} ⋈ belongingQuestion
end

Event REMOVECORRECTANSWER ⟨ordinary⟩ ≐
extends REMOVECORRECTANSWER
any
    quest
    q
    u
    a1
    a2
where
    grd51:: u ∈ loggedIn
        The user u must be logged in

```

```

grd52:: quest ∈ questions
grd53:: q ∈ quizzes
grd54:: a1 ∈ answers
grd55:: a2 ∈ answers
grd56:: correctAnswer(quest) = a1
    The answer to be removed must be the correct answer of the question
grd57:: belongingQuestion(a2) = quest
    The new correct answer must belong to the question
grd58:: quizCreator(q) = u
    The user u must be the creator of the quiz
grd59:: belongingQuiz(quest) = q
grd60:: belongingQuestion(a1) = quest
grd61:: card({a | a ∈ answers ∧ belongingQuestion(a) = quest}) > 2
    The current number of answers of the question must be greater than 2
grd62:: a1 ≠ a2
grd61:: u ∉ host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to remove the correct answer from a
    question of a quiz at the same time.
grd63:: ∀qi.qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

    The creator of a quiz shall not be allowed to remove the correct answer from a question
    of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same
    time
then
act51:: answers := answers \ {a1}
act52:: belongingQuestion := {a1} ⧸ belongingQuestion
act53:: correctAnswer := correctAnswer ⧸ {quest ↦ a2}
    the new coorrect answer is a2
end
Event SETCORRECTANSWER ⟨ordinary⟩ ≐
extends SETCORRECTANSWER
any
    u
    q
    quest
    a1
    a2
where
grd51:: u ∈ loggedIn
    The user u must be logged in
grd52:: q ∈ quizzes
grd53:: quest ∈ questions
grd54:: a1 ∈ answers
grd55:: a2 ∈ answers
grd56:: a1 ≠ a2
grd57:: quizCreator(q) = u
    The user u must be the creator of the quiz
grd58:: belongingQuiz(quest) = q
grd59:: correctAnswer(quest) = a1
    a1 must be the current correct answer of the question
grd60:: belongingQuestion(a2) = quest
    a2 must belong to the question
grd61:: u ∉ host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to set the correct answer of a question of
    a quiz at the same time.
grd62:: ∀qi.qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

    The creator of a quiz shall not be allowed to set the correct answer
    of a question of the quiz if there exists an active quiz instance, linked to the quiz,
    being hosted at the same time.

```



```

    then
      act51:: correctAnswer := correctAnswer  $\Leftarrow$  {quest  $\mapsto$  a2}
    end
Event UPDATE_ANSWER_OK  $\langle$ ordinary $\rangle \hat{=}$ 
extends UPDATE_ANSWER_OK
  any
    a
    q
    quest
    result
    u
  where
    grd51:: u  $\in$  loggedIn
    grd52:: a  $\in$  answers
    grd53:: q  $\in$  quizzes
    grd54:: quest  $\in$  questions
    grd55:: belongingQuestion(a) = quest
    grd56: quizCreator(q) = u
    grd57: belongingQuiz(quest) = q
    grd58: result = TRUE
    The update has been successful
    grd61:: u  $\notin$  host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to update an answer of a
    quiz at the same time.
    grd62:  $\forall qi \cdot qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$ 

    The creator of a quiz shall not be allowed to update an answer of a
    question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the
    same time.

  then
    skip
  end
Event UPDATE_ANSWER_NOT_OK  $\langle$ ordinary $\rangle \hat{=}$ 
extends UPDATE_ANSWER_NOT_OK
  any
    a
    q
    quest
    result
    u
  where
    grd51:: u  $\in$  loggedIn
    the user u must be logged in
    grd52:: a  $\in$  answers
    grd53:: quest  $\in$  questions
    grd54:: q  $\in$  quizzes
    grd55:: belongingQuestion(a) = quest
    grd56:: quizCreator(q) = u
    u must be the creator of the quiz
    grd58:: belongingQuiz(quest) = q
    grd57:: result = FALSE
    The update has not been successful. The previous text is restored
    grd61: u  $\notin$  host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to update an answer of a
    quiz at the same time.
    grd62:  $\forall qi \cdot qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$ 

    The creator of a quiz shall not be allowed to update an answer of a
    question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the
    same time.

```

```

    then
        skip
    end
Event REMOVEQUESTION ⟨ordinary⟩ ≐
extends REMOVEQUESTION
any
    u
    quest
    q
where
    grd41::  $u \in \text{loggedIn}$ 
        The user must be logged in order to remove a question
    grd42::  $q \in \text{quizzes}$ 
    grd43::  $\text{quest} \in \text{questions}$ 
    grd45::  $\text{belongingQuiz}(\text{quest}) = q$ 
        q must be the belonging quiz of quest
    grd44::  $\text{quizCreator}(q) = u$ 
        The creator of the quiz q must be u
    grd61:  $u \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$ 
        The host of an active quiz instance shall not be allowed to remove a question from a quiz at the
        same time.
    grd62:  $\forall qi \cdot qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$ 

        The creator of a quiz shall not be allowed to remove a question from the quiz if there exists an
        active quiz instance, linked to the quiz, being hosted at the same time.

    then
        act41::  $\text{questions} := \text{questions} \setminus \{\text{quest}\}$ 
        act42::  $\text{belongingQuiz} := \{\text{quest}\} \triangleleft \text{belongingQuiz}$ 
        act43::  $\text{questionPosition} := \{\text{quest}\} \triangleleft \text{questionPosition}$ 
            The position of the question is removed
        act51::  $\text{answers} := \text{answers} \setminus \{a \mid a \in \text{answers} \wedge \text{belongingQuestion}(a) = \text{quest}\}$ 
            the answers of the question must be removed when the question is removed
        act52::  $\text{correctAnswer} := \{\text{quest}\} \triangleleft \text{correctAnswer}$ 
            The correct answer of quest is not the correct answer anymore
        act53::  $\text{belongingQuestion} := \text{belongingQuestion} \triangleright \{\text{quest}\}$ 
            All answers of the question do not belong to it anymore
    end
Event UPDATE_QUESTION_OK ⟨ordinary⟩ ≐
extends UPDATE_QUESTION_OK
any
    u
    quest
    q
    result
where
    grd41::  $u \in \text{loggedIn}$ 
    grd42::  $q \in \text{quizzes}$ 
    grd43::  $\text{quizCreator}(q) = u$ 
        Only the quiz creator of q can update the question
    grd44::  $\text{quest} \in \text{questions}$ 
    grd45::  $\text{result} = \text{TRUE}$ 
        The update has been succesfully
    grd46::  $\text{belongingQuiz}(\text{quest}) = q$ 
        the question must belong to q
    grd61:  $u \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$ 
        The host of an active quiz instance shall not be allowed to update a question of a quiz at the
        same time.
    grd62:  $\forall qi \cdot qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$ 

```

The creator of a quiz shall not be allowed to update a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.

then

skip

end

Event UPDATE_QUESTION_NOT_OK $\langle \text{ordinary} \rangle \triangleq$

extends UPDATE_QUESTION_NOT_OK

any

u

quest

q

result

where

grd41:: $u \in \text{loggedIn}$

grd42:: $q \in \text{quizzes}$

grd43:: $\text{quizCreator}(q) = u$

grd1: $\text{quest} \in \text{questions}$

grd45:: $\text{belongingQuiz}(\text{quest}) = q$

grd46:: $\text{result} = \text{FALSE}$

The update has not been successfully. The previous text of the question is restored

grd61:: $u \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$

The host of an active quiz instance shall not be allowed to update a question of a quiz at the same time.

grd62: $\forall qi \cdot qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$

The creator of a quiz shall not be allowed to update a question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.

then

skip

end

Event HOST_QUIZ_INSTANCE $\langle \text{ordinary} \rangle \triangleq$

extends HOST_QUIZ_INSTANCE

any

u

q

qi

r

where

grd61:: $u \in \text{loggedIn}$

The user u must be logged in

grd62:: $qi \in \text{INSTANCE_QUIZ} \setminus \text{quizInstances}$

grd63:: $q \in \text{quizzes}$

grd65:: $u \notin \text{ran}((\text{finishedQuiz} \triangleleft \text{host}))$

The user u must not be hosting any other active quiz instance

grd66: $u \in (\{\text{quizCreator}(q)\} \cup \text{sharedTo}[\{q\}])$

The user u must be the creator or have access to the quiz

grd67: $\text{belongingQuiz}^{-1}[\{q\}] \neq \emptyset$

The quiz must have at least 1 question

grd91: $r \in \text{REPORT} \setminus \text{reports}$

A new report is created. Initially the report is an empty file. When the quiz instance terminates the report

will be populated with the information resulting from the content of the question summaries

then

act61:: $\text{quizInstances} := \text{quizInstances} \cup \{qi\}$

act62:: $\text{host}(qi) := u$

The host of the quiz instance is u

act63:: $\text{instanceOfQuiz}(qi) := q$

The quiz instance is linked to the quiz q

```

act64:: quizCreated := quizCreated  $\cup$  {qi}
    The quiz instance is in the quizCreated state
act91: embeddedQuestions := embeddedQuestions  $\cup$  ({qi}  $\times$  {quests | quests  $\in$  questions  $\wedge$  belongingQuiz(quests) =
    qi})
    The quiz instance is linked to the questions of the quiz
act92: reports := reports  $\cup$  {r}
    The report is added to the set of reports
act93: reportedBy(qi) := r
    The quiz instance is linked to the report
end
Event BEGIN_QUIZ_INSTANCE  $\langle$ ordinary $\rangle \hat{=}$ 
extends BEGIN_QUIZ_INSTANCE
any
    u
    qi
where
    grd61:: u  $\in$  loggedIn
        The user u must be logged in
    grd62:: qi  $\in$  quizCreated
        The quiz instance must be in the quizCreated state
    grd63:: host(qi) = u
        The host of the quiz instance must be u
then
    act61:: quizCreated := quizCreated  $\setminus$  {qi}
        The quiz instance is not in the quizCreated state anymore
    act62:: quizInit := quizInit  $\cup$  {qi}
        The quiz instance becomes part of the quizInit state set
    act63:: answeredQuestions(qi) := 0
        No question has been answered so far
end
Event START_QUIZ_INSTANCE  $\langle$ ordinary $\rangle \hat{=}$ 
extends START_QUIZ_INSTANCE
any
    u
    qi
    quest
where
    grd61:: u  $\in$  loggedIn
        The user u must be logged in
    grd62:: qi  $\in$  quizInit
        The quiz instance must be in the quizInit state
    grd63:: host(qi) = u
        The host of the quiz instance must be u
    grd64::  $\forall k \cdot \text{belongingQuiz}(k) = \text{instanceOfQuiz}(qi) \Rightarrow \text{questionPosition}(k) \geq \text{questionPosition}(\text{quest})$ 
        The question of the quiz that will become the first question to be answered in the quiz instance
        must be the first one in the question list of the quiz
    grd65: qi  $\in$  ran(playingIn)
        Some players must have joined the quiz during the quizInit state
then
    act61:: quizInit := quizInit  $\setminus$  {qi}
        The quiz is not in the quizInit state anymore
    act62:: questioning := questioning  $\cup$  {qi}
        The quiz instance is in the questioning state
    act63:: currentQuestion(qi) := quest
        The current question of the quiz instance is the first question of the question list of the quiz
end
Event JOIN_QUIZ_INSTANCE  $\langle$ ordinary $\rangle \hat{=}$ 
extends JOIN_QUIZ_INSTANCE

```

```

any
  u
  qi
where
  grd61::  $u \in USER$ 
    The player can be either registered or unregistered
  grd62::  $qi \in quizInit$ 
    It is possible to join a quiz instance only if it is in the quizInit state
  grd63::  $u \neq host(qi)$ 
    The player must not be the host of the quiz instance
  grd64::  $u \notin dom(playingIn)$ 
    The player must not be playing in another quiz instance
  grd1:  $u \notin host[quizInstances \setminus finishedQuiz]$ 
    The player cannot be any registered user that is hosting any active quiz instance
then
  act64::  $playingIn := playingIn \cup \{u \mapsto qi\}$ 
end
Event ANSWER_QUESTION  $\langle ordinary \rangle \hat{=}$ 
extends ANSWER_QUESTION
any
  p
  qi
  quest
  a
where
  grd61::  $p \in USER$ 
  grd62::  $qi \in quizInstances$ 
  grd63::  $p \in playingIn^{-1}[\{qi\}]$ 
    The player must be playing in the quiz instance
  grd64::  $qi \in questioning$ 
    The quiz instance must be in the questioning state
  grd65:  $quest \in questions$ 
  grd66:  $currentQuestion(qi) = quest$ 
    The question the player is answering must be the current question
  grd67:  $a \in answers$ 
  grd68:  $a \in belongingQuestion^{-1}[\{quest\}]$ 
    The answer being selected must belong to the current question of the quiz instance
  grd69:  $card(peopleAnswers^{-1}[\{qi\}]) < card(playingIn^{-1}[\{qi\}])$ 
    A player of a quiz instance shall not be allowed to select an answer when all other players
    have answered because the quiz instance passes to the questionSummary state.
then
  act61::  $peopleAnswers := peopleAnswers \cup \{p \mapsto qi\}$ 
  act62:  $peopleSelectedAnswer := peopleSelectedAnswer \Leftarrow \{p \mapsto a\}$ 
end
Event END_QUESTION_ALL_ANSWERED  $\langle ordinary \rangle \hat{=}$ 
extends END_QUESTION_ALL_ANSWERED
any
  qi
  qs
  r
where
  grd61::  $qi \in questioning$ 
    The quiz instance must be in the questionig state
  grd62::  $card(peopleAnswers^{-1}[\{qi\}]) = card(playingIn^{-1}[\{qi\}])$ 
    All players must have answered
  grd91:  $qs \in QUESTION\_SUMMARY \setminus qSummary$ 
    A question summary is generated. The question summary is populated with information about
    the performance of the players by using the information resulting
    from the relation peopleSelectedAnswer

```

```

    grd92:  $r \in \text{reports}$ 
    grd93:  $\text{reportedBy}(qi) = r$ 
            $r$  must be the report of the quiz instance
  then
    act61:  $\text{questioning} := \text{questioning} \setminus \{qi\}$ 
           The quiz instance is not part of the questioning state anymore
    act62:  $\text{questionSummary} := \text{questionSummary} \cup \{qi\}$ 
           The quiz instance passes to the questionSummary state
    act63:  $\text{answeredQuestions}(qi) := \text{answeredQuestions}(qi) + 1$ 
           The number of answered questions is incremented by 1
    act64:  $\text{peopleAnswers} := \text{peopleAnswers} \triangleright \{qi\}$ 
           The players that have answered the question of the quiz instance are removed
    act65:  $\text{peopleSelectedAnswer} := \text{playingIn}^{-1}[\{qi\}] \triangleleft \text{peopleSelectedAnswer}$ 
           The answers select by the players of the quiz instance are removed
    act91:  $qSummary := qSummary \cup \{qs\}$ 
    act92:  $\text{summaryFor}(qs) := (qi \mapsto \text{currentQuestion}(qi))$ 
           The summary is linked to the quiz instance and current question of the quiz instance
    act93:  $qReportedBy(qs) := r$ 
           The question summary is linked to the report of the quiz instance
  end
Event END_QUESTION_PREMATURATELY  $\langle \text{ordinary} \rangle \hat{=}$ 
extends END_QUESTION_PREMATURATELY
any
   $u$ 
   $qi$ 
   $qs$ 
   $r$ 
where
  grd61:  $qi \in \text{questioning}$ 
           The quiz instance must be in the question state
  grd62:  $u \in \text{loggedIn}$ 
           The user  $u$  must be logged in
  grd63:  $\text{host}(qi) = u$ 
           The host of the quiz instance must be  $u$ 
  grd1:  $\text{card}(\text{peopleAnswers}^{-1}[\{qi\}]) \neq \text{card}(\text{playingIn}^{-1}[\{qi\}])$ 
           The host of a quiz instance in the questioning state
           shall not be allowed to end prematurely a question
           if all players have answered because the quiz instance passes to the questionSummary state.
  grd91:  $qs \in \text{QUESTION\_SUMMARY} \setminus qSummary$ 
  grd92:  $r \in \text{reports}$ 
  grd93:  $\text{reportedBy}(qi) = r$ 
  then
    act61:  $\text{questioning} := \text{questioning} \setminus \{qi\}$ 
           The quiz instance is not in the questioning state anymore
    act62:  $\text{questionSummary} := \text{questionSummary} \cup \{qi\}$ 
           The quiz instance passes to the questionSummary state
    act63:  $\text{answeredQuestions}(qi) := \text{answeredQuestions}(qi) + 1$ 
           The number of answered questions of the quiz instance is incremebted by 1
    act64:  $\text{peopleAnswers} := \text{peopleAnswers} \triangleright \{qi\}$ 
           The players that have answered the question of the quiz instance are removed
    act65:  $\text{peopleSelectedAnswer} := \text{playingIn}^{-1}[\{qi\}] \triangleleft \text{peopleSelectedAnswer}$ 
           The answers select by the players of the quiz instance are removed
    act91:  $qSummary := qSummary \cup \{qs\}$ 
    act92:  $\text{summaryFor}(qs) := qi \mapsto \text{currentQuestion}(qi)$ 
    act93:  $qReportedBy(qs) := r$ 
  end
Event SHOW_QUESTION_SUMMARY_TO_PLAYERS  $\langle \text{ordinary} \rangle \hat{=}$ 
extends SHOW_QUESTION_SUMMARY_TO_PLAYERS
any

```

```

    u
    qi
    qs
  where
    grd61:: u ∈ loggedIn
      The user u must be logged in
    grd62:: qi ∈ quizInstances
    grd63:: host(qi) = u
      The user u must be the host of the quiz instance
    grd63: qi ∈ questionSummary
      The quiz instance must be in the questionSummary state
    grd64: qi ∈ ran(playingIn)
      The host of a quiz instance in the questionSummary state shall
      be allowed to show the question summary only if at least 1 player is playing in the quiz instance.
    grd91: summaryFor(qs) = qi ↦ currentQuestion(qi)
      The summary to show must be the
      summary linked to the quiz instance and current question
      of the quiz instance

  then
    skip
  end
Event NEXT_QUESTION ⟨ordinary⟩ ≐
extends NEXT_QUESTION
  any
    u
    qi
    quest
  where
    grd61:: u ∈ loggedIn
    grd62:: qi ∈ questionSummary
      The quiz instance must be in the questionSummary state
    grd63:: host(qi) = u
    grd64:: answeredQuestions(qi) < card(belongingQuiz-1[{instanceOfQuiz(qi)}])
      There must be other questions to be answered
    grd65: qi ∈ ran(playingIn)
      At least 1 player must be playing in the quiz instance
    grd66: quest ∈ questions
    grd67: card({quests|quests ∈ questions ∧ quests ∈ belongingQuiz-1[{instanceOfQuiz(qi)}] ∧
      questionPosition(quests) < questionPosition(quest)}) = answeredQuestions(qi)
      The next question to be answered must be the successive one

  then
    act61:: questionSummary := questionSummary \ {qi}
      The quiz instance is not in the questionSummary state anymore
    act62:: questioning := questioning ∪ {qi}
      The quiz instance passes to the questioning state
    act63: currentQuestion(qi) := quest
      The current question is set to the successive question
  end
Event FINISH_QUIZ_INSTANCE ⟨ordinary⟩ ≐
extends FINISH_QUIZ_INSTANCE
  any
    u
    qi
  where
    grd61:: u ∈ loggedIn
      The user must be logged in
    grd62:: qi ∈ questionSummary
      The quiz instance must be in the questionSummary state

```

```

    grd63:: host(qi) = u
        The user u must be the host of the quiz instance
    then
    act61:: questionSummary := questionSummary \ {qi}
        The quiz instance is not in the questionSummary state anymore
    act62:: quizSummary := quizSummary ∪ {qi}
        The quiz instance passes to the quizSummary state
    act63:: currentQuestion := {qi} ◁ currentQuestion
        The current question of the quiz instance is removed as it is not anymore in the questionSummary
        state
    end
Event SHOW_QUIZ_INSTANCE_SUMMARY_TO_PLAYERS ⟨ordinary⟩ ≐
extends SHOW_QUIZ_INSTANCE_SUMMARY_TO_PLAYERS
any
    qi
    u
    r
where
    grd61:: qi ∈ quizInstances
    grd62: qi ∈ quizSummary
        The quiz instance must be in the quizSummary state
    grd63: u ∈ registeredUser
    grd64: u ∈ loggedIn
        The user u must be logged in
    grd65: host(qi) = u
        The user u must be the host of the quiz instance
    grd66: qi ∈ ran(playingIn)
        there must at least 1 player playing in the quiz instance
    grd91: r ∈ reports
    grd92: reportedBy(qi) = r
        the report to show must be the report of the quiz instance
    then
        skip
    end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_SUMMARY_STATE ⟨ordinary⟩ ≐
extends TERMINATE_QUIZ_INSTANCE_QUIZ_SUMMARY_STATE
any
    u
    qi
where
    grd61:: u ∈ loggedIn
        The user u must be loggedin
    grd62:: qi ∈ quizSummary
        The quiz instance must be in the quizSummary state
    grd63:: host(qi) = u
        The user u must be the host of the quiz instance
    then
    act61:: quizSummary := quizSummary \ {qi}
        The quiz instance is not in the quizSummary state anymore
    act62:: finishedQuiz := finishedQuiz ∪ {qi}
        The quiz instance passes to the finishedQuiz state
    act63: playingIn := playingIn ▷ {qi}
        The players of the quiz instance do not play anymore in the quiz instance
    act91: embeddedQuestions := {qi} ◁ embeddedQuestions
        The quiz instance is not linked anymore to the questions of the quiz instance
    act92: summaryFor := summaryFor ▷ ({qi} ◁ embeddedQuestions)
        The question summaries do not report anymore a specific question of the quiz instance
    act93: qSummary := qSummary \ summaryFor-1[{qi} ◁ embeddedQuestions]
        All the summaries of the quiz instance built so far must be deleted

```


act94: $qReportedBy := qReportedBy \triangleright reportedBy[\{qi\}]$
 The question summaries are not linked anymore to the report of the quiz instance

end

Event LEAVE_QUIZ_INSTANCE_LAST_ONE_IN_QUESTIONING_STATE $\langle \text{ordinary} \rangle \hat{=}$

extends LEAVE_QUIZ_INSTANCE_LAST_ONE_IN_QUESTIONING_STATE

any

p
 qi
 qs
 r

where

grd61: $p \in USER$
 grd62: $qi \in questioning$
 The quiz instance must be in the questioning state
 grd63: $p \in playingIn^{-1}[\{qi\}]$
 The player must be playing in the quiz instance
 grd64: $card(playingIn^{-1}[\{qi\}]) = 1$
 The player must be the only player be playing in the quiz instance
 grd91: $qs \in QUESTION_SUMMARY \setminus qSummary$
 A question summary is generated
 grd92: $r \in reports$
 grd93: $reportedBy(qi) = r$
 Thw question summary is linked to the report of the quiz instance

then

act61: $playingIn := \{p\} \triangleleft playingIn$
 The player does not play anymore in the quiz instance
 act62: $peopleAnswers := \{p\} \triangleleft peopleAnswers$
 It is removed whether the player has answered the question or not
 act63: $questioning := questioning \setminus \{qi\}$
 act64: $questionSummary := questionSummary \cup \{qi\}$
 The quiz instance passes to the questionSummary state
 act65: $peopleSelectedAnswer := \{p\} \triangleleft peopleSelectedAnswer$
 The answer selected by the player is removed (if he/she has naswered)
 act91: $qSummary := qSummary \cup \{qs\}$
 act92: $summaryFor(qs) := qi \mapsto currentQuestion(qi)$
 act93: $qReportedBy(qs) := r$

end

Event LEAVE_QUIZ_INSTANCE_NOT_IN_QUESTIONING_STATE $\langle \text{ordinary} \rangle \hat{=}$

extends LEAVE_QUIZ_INSTANCE_NOT_IN_QUESTIONING_STATE

any

p
 qi

where

grd61: $p \in USER$
 grd62: $qi \in quizInstances \setminus (quizCreated \cup finishedQuiz \cup questioning)$
 The quiz instance must not be in the quiz created state, finishedQuiz or questioning state
 grd63: $p \in playingIn^{-1}[\{qi\}]$
 The player must be playing in the quiz instance

then

act61: $playingIn := \{p\} \triangleleft playingIn$
 The player does not play anymore in the quiz instance

end

Event LEAVE_QUIZ_INSTANCE_NOT_LAST_ONE_IN_QUESTIONING_STATE $\langle \text{ordinary} \rangle \hat{=}$

extends LEAVE_QUIZ_INSTANCE_NOT_LAST_ONE_IN_QUESTIONING_STATE

any

p
 qi

where

```

    grd61:  $p \in USER$ 
    grd62:  $qi \in questioning$ 
    grd63:  $p \in playingIn^{-1}[\{qi\}]$ 
    grd64:  $card(playingIn^{-1}[\{qi\}]) > 1$ 
    There must be at least 2 players be playing
  then
    act61:  $playingIn := \{p\} \triangleleft playingIn$ 
    act62:  $peopleAnswers := \{p\} \triangleleft peopleAnswers$ 
    act63:  $peopleSelectedAnswer := \{p\} \triangleleft peopleSelectedAnswer$ 
  end
Event UNSHARE_QUIZ  $\langle ordinary \rangle \hat{=}$ 
extends UNSHARE_QUIZ
  any
     $u1$ 
     $u2$ 
     $q$ 
  where
    grd41:  $u1 \in registeredUser$ 
    grd42:  $u2 \in registeredUser$ 
    grd43:  $u1 \in loggedIn$ 
    A registerd user can unshare only if he/she is online
    grd44:  $u1 \neq u2$ 
    grd45:  $q \mapsto u2 \in sharedTo$ 
     $u2$  had to have access to the quiz
    grd46:  $u1 = quizCreator(q)$ 
    Only the creator of the quiz can unshare a quiz
    grd81:  $u2 \notin host[instanceOfQuiz^{-1}[\{q\}] \setminus finishedQuiz]$ 
    The creator of a quiz shall not be allowed to deshare a quiz
    with another registered user if the latter is hosting a quiz instance linked to the quiz.
    grd82:  $u1 \notin host[quizInstances \setminus finishedQuiz]$ 
    The creator of a quiz shall not be allowed to deshare a
    quiz if he/she is hosting an active quiz instance.
  then
    act41:  $sharedTo := sharedTo \setminus \{q \mapsto u2\}$ 
  end
Event REMOVE_QUIZ_INSTANCE  $\langle ordinary \rangle \hat{=}$ 
extends REMOVE_QUIZ_INSTANCE
  any
     $u$ 
     $qi$ 
  where
    grd81:  $u \in registeredUser$ 
    grd82:  $qi \in quizInstances$ 
    grd83:  $qi \in finishedQuiz$ 
    It is possible to remove a quiz instance only when it is in the finishedQuiz state
    grd84:  $u \in loggedIn$ 
    The user must be logged in
    grd85:  $host(qi) = u$ 
    The user u must be the host of the quiz instance
    grd86:  $u \notin host[quizInstances \setminus finishedQuiz]$ 
    The user must not be hosting any active quiz instance
  then
    act81:  $quizInstances := quizInstances \setminus \{qi\}$ 
    The quiz instance is removed
    act82:  $finishedQuiz := finishedQuiz \setminus \{qi\}$ 
    The quiz instance is removed from the finishedQuiz state
    act83:  $host := \{qi\} \triangleleft host$ 
    The user is not the host of the quiz instance anymore

```

```

act84: instanceOfQuiz := {qi}  $\triangleleft$  instanceOfQuiz
      The quiz instance is not linked anymore to a quiz
act85: answeredQuestions := {qi}  $\triangleleft$  answeredQuestions
      The number of answered questions of the quiz instance is removed
act91: reportedBy := {qi}  $\triangleleft$  reportedBy
      The report of the quiz instance is removed
act92: reports := reports \ {reportedBy(qi)}
      The report is not machted anymore to the quiz instance
end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_CREATED_STATE  $\langle$ ordinary $\rangle \hat{=}$ 
extends TERMINATE_QUIZ_INSTANCE_QUIZ_CREATED_STATE
any
  u
  qi
where
  grd91: u  $\in$  registeredUser
  grd92: u  $\in$  loggedIn
      The user u must be loggedIn
  grd93: qi  $\in$  quizInstances
  grd94: qi  $\in$  quizCreated
      The quiz instance must be in the quizCreated state
  grd95: host(qi) = u
      The user u must be the host of the quiz instance
then
  act91: quizCreated := quizCreated \ {qi}
      The quiz instance is removed from the quizCreated state
  act92: finishedQuiz := finishedQuiz  $\cup$  {qi}
      The quiz instance passes to the finishedQuiz state
  act93: answeredQuestions(qi) := 0
      The number of answered questions is set to 0
  act94: embeddedQuestions := {qi}  $\triangleleft$  embeddedQuestions
      The quiz instance is not linked anymore to the questions of the quiz instance
end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_INIT_STATE  $\langle$ ordinary $\rangle \hat{=}$ 
extends TERMINATE_QUIZ_INSTANCE_QUIZ_INIT_STATE
any
  u
  qi
where
  grd81: u  $\in$  registeredUser
  grd82: u  $\in$  loggedIn
      The user u must be loggedin
  grd83: qi  $\in$  quizInstances
  grd84: qi  $\in$  quizInit
      The quiz instance must be in the quizInit state
  grd85: host(qi) = u
      The user u must be the host of the quiz instance
then
  act81: quizInit := quizInit \ {qi}
      The quiz instance is not anymore in the quizInit state
  act82: finishedQuiz := finishedQuiz  $\cup$  {qi}
      The quiz instance passes to the finishedQuiz state
  act83: playingIn := playingIn  $\triangleright$  {qi}
      The players of the quiz instance do not play anymore in the quiz instance
  act91: embeddedQuestions := {qi}  $\triangleleft$  embeddedQuestions
      The quiz instance is not linked anymore to the questions of the quiz instance
end
Event END_QUESTION_TIME_IS_UP  $\langle$ ordinary $\rangle \hat{=}$ 
extends END_QUESTION_TIME_IS_UP

```

```

any
  qi
  qs
  r
where
  grd61: qi ∈ quizInstances
  grd62: qi ∈ questioning
    The quiz instance must be in the questioning state
  grd91: qs ∈ QUESTION_SUMMARY \ qSummary
  grd92: r ∈ reports
  grd93: reportedBy(qi) = r
then
  act61: questioning := questioning \ {qi}
  act62: questionSummary := questionSummary ∪ {qi}
    The quiz instance passes to the questionSummary state
  act63: answeredQuestions(qi) := answeredQuestions(qi) + 1
    The number of answered questions of the quiz instance is incremented by 1
  act64: peopleAnswers := peopleAnswers ▷ {qi}
  act65: peopleSelectedAnswer := playingIn-1[{qi}] ⋈ peopleSelectedAnswer
  act91: qSummary := qSummary ∪ {qs}
  act92: summaryFor(qs) := (qi ↦ currentQuestion(qi))
  act93: qReportedBy(qs) := r
end
END

```

MACHINE m10**REFINES** m9**SEES** c6**VARIABLES**

registeredUser
 password
 loggedIn
 loggedOut
 quizzes
 questions
 quizCreator
 belongingQuiz
 sharedTo
 questionPosition
 answers
 correctAnswer
 belongingQuestion
 quizInstances
 host
 playingIn
 instanceOfQuiz
 currentQuestion
 quizInit
 questioning
 questionSummary
 quizSummary
 finishedQuiz
 answeredQuestions
 peopleAnswers
 quizCreated
 embeddedQuestions
 reports
 summaryFor
 reportedBy
 qSummary
 qReportedBy
 peopleSelectedAnswer
 time
 questionTime
 questionEndsAt
 questionStartedAt

INVARIANTS**inv101:** $time \in \mathbb{N}$

This variable indicates the time expressed in minutes. For example, if $time = 1$ then 1 minute is passed from time 0

inv103: $questionTime \in questions \rightarrow QUESTION_TIME$

A question shall be matched to a time within which players can select an answer during a quiz instance.

inv104: $questionEndsAt \in questioning \rightarrow \mathbb{N}$

A quiz instance in the questioning state shall be matched with the time when it will transition into the questionSummary state.

inv105: $questionStartedAt \in questioning \rightarrow \mathbb{N}$

A quiz instance in the questioning state shall be matched with the time when it has transitioned into the questioning state

inv106: $\forall qi, t, n. qi \in quizInstances \wedge qi \in questioning \wedge t \in \mathbb{N} \wedge qi \mapsto t \in questionEndsAt \wedge n \in \mathbb{N} \wedge n = questionTime(currentQuestion(qi)) \Rightarrow t = questionStartedAt(qi) + n$
 A quiz instance passes from the questionig state to the questionSummary state
 after time n from when it has started where n=question time of the current question
 of the quiz instance

EVENTS

Initialisation ⟨extended⟩

begin

act1;: *registeredUser* := \emptyset
 act21;: *password* := \emptyset
 act31;: *loggedIn* := \emptyset
 act32;: *loggedOut* := \emptyset
 act41;: *quizzes* := \emptyset
 act42;: *questions* := \emptyset
 act43;: *quizCreator* := \emptyset
 act44;: *belongingQuiz* := \emptyset
 act45;: *sharedTo* := \emptyset
 act46;: *questionPosition* := \emptyset
 act51;: *answers* := \emptyset
 act52;: *correctAnswer* := \emptyset
 act53;: *belongingQuestion* := \emptyset
 act61;: *quizInstances* := \emptyset
 act62;: *host* := \emptyset
 act63;: *playingIn* := \emptyset
 act64;: *instanceOfQuiz* := \emptyset
 act65;: *peopleAnswers* := \emptyset
 act66;: *answeredQuestions* := \emptyset
 act67;: *currentQuestion* := \emptyset
 act68;: *finishedQuiz* := \emptyset
 act69;: *questioning* := \emptyset
 act611;: *questionSummary* := \emptyset
 act612;: *quizCreated* := \emptyset
 act613;: *quizInit* := \emptyset
 act614;: *quizSummary* := \emptyset
 act615;: *peopleSelectedAnswer* := \emptyset
 act91;: *embeddedQuestions* := \emptyset
 act92;: *reports* := \emptyset
 act93;: *summaryFor* := \emptyset
 act94;: *reportedBy* := \emptyset
 act95;: *qSummary* := \emptyset
 act96;: *qReportedBy* := \emptyset
 act616;: *time* := 0
 act617;: *questionTime* := \emptyset
 act618;: *questionEndsAt* := \emptyset
 act619;: *questionStartedAt* := \emptyset

end

Event REGISTER ⟨ordinary⟩ $\hat{=}$

extends REGISTER

any

u A user

p

where

grd1;: $u \in USER \setminus registeredUser$
 The user must not be already registered
 grd21;: $p \in PASSWORD$
 grd81;: $u \notin dom(playingIn)$

then

act1;: *registeredUser* := *registeredUser* $\cup \{u\}$
 The user is added to the set of registered users

```

    act21:: password(u) := p
        The password of user u is p
    act31:: loggedOut := loggedOut ∪ {u}
        When a user u registers, u is added to the set of loggedOut users
end
Event LOGIN ⟨ordinary⟩ ≐
extends LOGIN
any
    u
    p
where
    inv31:: u ∈ loggedOut
    inv32:: p = password(u)
        p must be the pssword of u
    grd81: u ∉ dom(playingIn)
then
    act31:: loggedIn := loggedIn ∪ {u}
        The user u is added to the set of loggedIn users
    act32:: loggedOut := loggedOut \ {u}
        The user u is removed from the set of loggedOut users
end
Event LOGOUT ⟨ordinary⟩ ≐
extends LOGOUT
any
    u
where
    inv31:: u ∈ loggedIn
        The user u mst be logged in
    grd81: u ∉ host[quizInstances \ finishedQuiz]
        The host of an active quiz instance shall not be allowed to log out of the system.
    grd82: u ∉ dom(playingIn)
then
    act31:: loggedIn := loggedIn \ {u}
        The user u is removed from the set of loggedIn users
    act32:: loggedOut := loggedOut ∪ {u}
        The user u is added to the set of loggedOut users
end
Event CREATEQUIZ ⟨ordinary⟩ ≐
extends CREATEQUIZ
any
    u
    q
where
    grd41:: u ∈ loggedIn
        A user must be logged in so that to create a quiz
    grd42:: q ∈ QUIZ \ quizzes
        The created quiz must not have been already created
    grd61:: u ∉ host[quizInstances \ finishedQuiz]
        The host of an active quiz instance shall not be allowed to create a quiz at the same time.
then
    act41:: quizzes := quizzes ∪ {q}
        The created quiz is added to the dynamic set quizzes
    act42:: quizCreator(q) := u
        the creator of the quiz q is u
end
Event REMOVEQUIZ ⟨ordinary⟩ ≐
extends REMOVEQUIZ
any

```

u
 q
where
 grd41:: $q \in quizzes$
 grd42:: $u \in loggedIn$
 The user must be logged in so that to remove a quiz
 grd43:: $quizCreator(q) = u$
 Only the creator of the quiz can remove the quiz
 grd61:: $u \notin host[quizInstances \setminus finishedQuiz]$
 The host of an active quiz instance shall not be allowed to remove a quiz at the same time.
 grd62: $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$
 The creator of a quiz shall not be allowed to remove a quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same time.
then
 act41:: $quizzes := quizzes \setminus \{q\}$
 the quiz is removed
 act42:: $quizCreator := \{q\} \triangleleft quizCreator$
 The quiz does not have anymore a creator because is removed
 act43:: $sharedTo := \{q\} \triangleleft sharedTo$
 All registered users that had access to the quiz, do not have access to it anymore because the quiz is removed
 act44:: $belongingQuiz := belongingQuiz \triangleright \{q\}$
 The questions of the quiz do not belong anymore to it
 act45:: $questions := questions \setminus \{quest | quest \in questions \wedge belongingQuiz(quest) = q\}$
 The questions of the quiz are removed
 act46:: $questionPosition := \{quest | quest \in questions \wedge belongingQuiz(quest) = q\} \triangleleft questionPosition$
 The position of the questions is removed
 act54:: $correctAnswer := \{q2 | q2 \in questions \wedge belongingQuiz(q2) = q\} \triangleleft correctAnswer$
 The correct answer of all questions of the quiz must be removed
 act55:: $belongingQuestion := belongingQuestion \triangleright \{q2 | q2 \in questions \wedge belongingQuiz(q2) = q\}$
 The answers of the questions of the quiz do not belong to the questions anymore
 act56: $answers := answers \setminus \{a1 | a1 \in answers \wedge belongingQuestion(a1) \in \{quest1 | quest1 \in questions \wedge belongingQuiz(quest1) = q\}\}$
 Removing a quiz involves removing all answers of the questions of the quiz
 act61: $instanceOfQuiz := instanceOfQuiz \triangleright \{q\}$
 act101: $questionTime := belongingQuiz^{-1}[\{q\}] \triangleleft questionTime$
 When removing a quiz, it is necessary to remove the question time of each of its questions
end
Event SHAREQUIZ $\langle ordinary \rangle \hat{=}$
extends SHAREQUIZ
any
 $u1$
 $u2$
 q
where
 grd41:: $u1 \in loggedIn$
 the user must be logged in so that to share the quiz
 grd42:: $u2 \in registeredUser$
 the other user that will have access to the quiz
 grd43:: $u1 \neq u2$
 the two users cannot be the same person
 grd44:: $q \in quizzes$
 grd45:: $quizCreator(q) = u1$
 u1 must be the creator of the quiz
 grd46: $q \in ran(belongingQuiz)$
 The quiz must contain at least 1 question in order to be shared
 grd47: $q \mapsto u2 \notin sharedTo$
 the quiz must not have already been shared with u2


```

    grd61::  $u1 \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$ 
        The host of an active quiz instance shall not be allowed to share a quiz at the same time.
  then
    act41::  $\text{sharedTo} := \text{sharedTo} \cup \{q \mapsto u2\}$ 
  end
Event CREATEQUESTION  $\langle \text{ordinary} \rangle \hat{=}$ 
extends CREATEQUESTION
  any
    quest
    q
    u
    p
    a
    b
    t
  where
    grd41::  $\text{quest} \in \text{QUESTION} \setminus \text{questions}$ 
        The question must be a new question
    grd42::  $q \in \text{quizzes}$ 
    grd43::  $u \in \text{loggedIn}$ 
        The user must be logged in in order to create a new question
    grd44::  $\text{quizCreator}(q) = u$ 
        The creator of the quiz must be u
    grd45::  $p \in \text{POSITION}$ 
    grd46::  $\forall z. z \in \text{questions} \wedge \text{belongingQuiz}(z) = q \Rightarrow p > \text{questionPosition}(z)$ 
        The question must be added at the end of the question list of the quiz
    grd51::  $(a \in \text{ANSWER} \setminus \text{answers}) \wedge (b \in \text{ANSWER} \setminus \text{answers})$ 
        The 2 answers must be new ones
    grd52:  $a \neq b$ 
        The 2 answers must be different
    grd61::  $u \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$ 
        The host of an active quiz instance shall not be allowed to add a question to a quiz at the same
        time.
    grd62:  $\forall qi. qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$ 
        The creator of a quiz shall not be allowed to add a question to a quiz if there exists an active
        quiz instance, linked to the quiz, being hosted at the same time.
    grd101:  $t \in \text{QUESTION\_TIME}$ 
  then
    act41::  $\text{questions} := \text{questions} \cup \{\text{quest}\}$ 
    act42::  $\text{belongingQuiz}(\text{quest}) := q$ 
        the question quest belongs to q
    act43::  $\text{questionPosition}(\text{quest}) := p$ 
        The position of the question quest is p inside the question list of the quiz q
    act51::  $\text{answers} := \text{answers} \cup \{a, b\}$ 
    act53::  $\text{correctAnswer}(\text{quest}) := a$ 
        The correct answer is a
    act54::  $\text{belongingQuestion} := \text{belongingQuestion} \cup \{a \mapsto \text{quest}, b \mapsto \text{quest}\}$ 
        The 2 new answers belong to the question quest
    act101:  $\text{questionTime}(\text{quest}) := t$ 
        When creatig a question, it is neccèssary to match it with a time
  end
Event ADDANSWER  $\langle \text{ordinary} \rangle \hat{=}$ 
REQ7
extends ADDANSWER
  any
    quest
    q
    u

```

```

    a
  where
    grd51:: u ∈ loggedIn
      The user u must be logged in
    grd52:: q ∈ quizzes
    grd53:: a ∈ ANSWER \ answers
    grd54:: quest ∈ questions
    grd55:: quizCreator(q) = u
      The user u must be the creator of the quiz
    grd56:: belongingQuiz(quest) = q
    grd57:: card({a1 | a1 ∈ answers ∧ belongingQuestion(a1) = quest}) < 4
      The current answers of the question must be less than 4
    grd61:: u ∉ host[quizInstances \ finishedQuiz]
      The host of an active quiz instance shall not be allowed to add an answer to a question of a quiz
      at the same time.
    grd62:  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

      The creator of a quiz shall not be allowed to add an answer to a question of a quiz if there exists
      an active quiz instance, linked to the quiz, being hosted at the same time.

  then
    act51:: answers := answers ∪ {a}
    act52:: belongingQuestion(a) := quest
  end

Event REMOVENOTCORRECTANSWER ⟨ordinary⟩ ≐
extends REMOVENOTCORRECTANSWER
any
  quest
  q
  u
  a
  where
    grd51:: u ∈ loggedIn
      The user u must be logged in
    grd52:: q ∈ quizzes
    grd53:: quest ∈ questions
    grd54:: a ∈ answers
    grd55:: card({a1 | a1 ∈ answers ∧ belongingQuestion(a1) = quest}) > 2
      The number of current answers of the question must be more than 2
    grd56:: correctAnswer(quest) ≠ a
      The answer to be removed must not be the correct answer of the question
    grd57: quizCreator(q) = u
      The user u must be the creator of the quiz
    grd58: belongingQuiz(quest) = q
    grd59: belongingQuestion(a) = quest
      The answer must belong to the quiz q
    grd61:: u ∉ host[quizInstances \ finishedQuiz]
      The host of an active quiz instance shall not be allowed to remove a non-correct answer from a
      question of a quiz at the same time.
    grd62:  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

      The creator of a quiz shall not be allowed to remove a non-correct answer from a question
      of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same
      time.

  then
    act51:: answers := answers \ {a}
    act52:: belongingQuestion := {a} ≪ belongingQuestion
  end

Event REMOVECORRECTANSWER ⟨ordinary⟩ ≐
extends REMOVECORRECTANSWER

```

```

any
  quest
  q
  u
  a1
  a2
where
  grd51::  $u \in \text{loggedIn}$ 
    The user u must be logged in
  grd52::  $quest \in \text{questions}$ 
  grd53::  $q \in \text{quizzes}$ 
  grd54::  $a1 \in \text{answers}$ 
  grd55::  $a2 \in \text{answers}$ 
  grd56::  $\text{correctAnswer}(quest) = a1$ 
    The answer to be removed must be the correct answer of the question
  grd57::  $\text{belongingQuestion}(a2) = quest$ 
    The new correct answer must belong to the question
  grd58:  $\text{quizCreator}(q) = u$ 
    The user u must be the creator of the quiz
  grd59:  $\text{belongingQuiz}(quest) = q$ 
  grd60:  $\text{belongingQuestion}(a1) = quest$ 
  grd61:  $\text{card}(\{a \mid a \in \text{answers} \wedge \text{belongingQuestion}(a) = quest\}) > 2$ 
    The current number of answers of the question must be greater than 2
  grd62:  $a1 \neq a2$ 
  grd61::  $u \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$ 
    The host of an active quiz instance shall not be allowed to remove the correct answer from a
    question of a quiz at the same time.
  grd63:  $\forall qi \cdot qi \in \text{quizInstances} \wedge qi \in \text{instanceOfQuiz}^{-1}[\{q\}] \Rightarrow qi \notin (\text{quizInstances} \setminus \text{finishedQuiz})$ 
    The creator of a quiz shall not be allowed to remove the correct answer from a question
    of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the same
    time
then
  act51::  $\text{answers} := \text{answers} \setminus \{a1\}$ 
  act52::  $\text{belongingQuestion} := \{a1\} \triangleleft \text{belongingQuestion}$ 
  act53::  $\text{correctAnswer} := \text{correctAnswer} \triangleleft \{quest \mapsto a2\}$ 
    the new correct answer is a2
end

```

Event SETCORRECTANSWER $\langle \text{ordinary} \rangle \hat{=}$

extends SETCORRECTANSWER

```

any
  u
  q
  quest
  a1
  a2
where
  grd51::  $u \in \text{loggedIn}$ 
    The user u must be logged in
  grd52::  $q \in \text{quizzes}$ 
  grd53::  $quest \in \text{questions}$ 
  grd54::  $a1 \in \text{answers}$ 
  grd55::  $a2 \in \text{answers}$ 
  grd56::  $a1 \neq a2$ 
  grd57:  $\text{quizCreator}(q) = u$ 
    The user u must be the creator of the quiz
  grd58:  $\text{belongingQuiz}(quest) = q$ 
  grd59:  $\text{correctAnswer}(quest) = a1$ 
    a1 must be the current correct answer of the question

```

```

    grd60: belongingQuestion(a2) = quest
           a2 must belong to the question
    grd61:: u ∉ host[quizInstances \ finishedQuiz]
           The host of an active quiz instance shall not be allowed to set the correct answer of a question of
           a quiz at the same time.
    grd62: ∀qi·qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

           The creator of a quiz shall not be allowed to set the correct answer
           of a question of the quiz if there exists an active quiz instance, linked to the quiz,
           being hosted at the same time.

  then
    act51:: correctAnswer := correctAnswer ⇐ {quest ↦ a2}
  end
Event UPDATE_ANSWER_OK ⟨ordinary⟩ ≐
extends UPDATE_ANSWER_OK
  any
    a
    q
    quest
    result
    u
  where
    grd51:: u ∈ loggedIn
    grd52:: a ∈ answers
    grd53:: q ∈ quizzes
    grd54:: quest ∈ questions
    grd55:: belongingQuestion(a) = quest
    grd56:: quizCreator(q) = u
    grd57: belongingQuiz(quest) = q
    grd58: result = TRUE
           The update has been successful
    grd61:: u ∉ host[quizInstances \ finishedQuiz]
           The host of an active quiz instance shall not be allowed to update an answer of a question of a
           quiz at the same time.
    grd62: ∀qi·qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

           The creator of a quiz shall not be allowed to update an answer of a
           question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the
           same time.

  then
    skip
  end
Event UPDATE_ANSWER_NOT_OK ⟨ordinary⟩ ≐
extends UPDATE_ANSWER_NOT_OK
  any
    a
    q
    quest
    result
    u
  where
    grd51:: u ∈ loggedIn
           the user u must be logged in
    grd52:: a ∈ answers
    grd53:: quest ∈ questions
    grd54:: q ∈ quizzes
    grd55:: belongingQuestion(a) = quest
    grd56:: quizCreator(q) = u
           u must be the creator of the quiz

```

```

    grd58:: belongingQuiz(quest) = q
    grd57:: result = FALSE
    The update has not been successful. The previous text is restored
    grd61: u ∉ host[quizInstances \ finishedQuiz]
    The host of an active quiz instance shall not be allowed to update an answer of a
    quiz at the same time.
    grd62: ∀qi·qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

    The creator of a quiz shall not be allowed to update an answer of a
    question of the quiz if there exists an active quiz instance, linked to the quiz, being hosted at the
    same time.

  then
    skip
  end
Event REMOVEQUESTION ⟨ordinary⟩ ≐
extends REMOVEQUESTION
any
  u
  quest
  q
where
  grd41:: u ∈ loggedIn
  The user must be logged in order to remove a question
  grd42:: q ∈ quizzes
  grd43:: quest ∈ questions
  grd45:: belongingQuiz(quest) = q
  q must be the belonging quiz of quest
  grd44:: quizCreator(q) = u
  The creator of the quiz q must be u
  grd61: u ∉ host[quizInstances \ finishedQuiz]
  The host of an active quiz instance shall not be allowed to remove a question from a quiz at the
  same time.
  grd62: ∀qi·qi ∈ quizInstances ∧ qi ∈ instanceOfQuiz-1[{q}] ⇒ qi ∉ (quizInstances \ finishedQuiz)

  The creator of a quiz shall not be allowed to remove a question from the quiz if there exists an
  active quiz instance, linked to the quiz, being hosted at the same time.

then
  act41:: questions := questions \ {quest}
  act42:: belongingQuiz := {quest} ⋈ belongingQuiz
  act43:: questionPosition := {quest} ⋈ questionPosition
  The position of the question is removed
  act51:: answers := answers \ {a | a ∈ answers ∧ belongingQuestion(a) = quest}
  the answers of the question must be removed when the question is removed
  act52:: correctAnswer := {quest} ⋈ correctAnswer
  The correct answer of quest is not the correct answer anymore
  act53:: belongingQuestion := belongingQuestion ▷ {quest}
  All answers of the question do not belong to it anymore
  act101: questionTime := {quest} ⋈ questionTime
  When removing a question it is necessary to remove its time
end
Event UPDATE_QUESTION_OK ⟨ordinary⟩ ≐
extends UPDATE_QUESTION_OK
any
  u
  quest
  q
  result
where
  grd41:: u ∈ loggedIn

```

```

    grd42::  $q \in quizzes$ 
    grd43::  $quizCreator(q) = u$ 
    Only the quiz creator of q can update the question
    grd44::  $quest \in questions$ 
    grd45::  $result = TRUE$ 
    The update has been succesfully
    grd46::  $belongingQuiz(quest) = q$ 
    the question must belong to q
    grd61::  $u \notin host[quizInstances \setminus finishedQuiz]$ 
    The host of an active quiz instance shall not be allowed to update a question of a quiz at the
    same time.
    grd62:  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

    The creator of a quiz shall not be allowed to update a question of the quiz if there exists an active
    quiz instance, linked to the quiz, being hosted at the same time.
  then
    skip
  end
Event UPDATE_QUESTION_NOT_OK ⟨ordinary⟩  $\hat{=}$ 
extends UPDATE_QUESTION_NOT_OK
any
  u
  quest
  q
  result
where
  grd41::  $u \in loggedIn$ 
  grd42::  $q \in quizzes$ 
  grd43::  $quizCreator(q) = u$ 
  grd1:  $quest \in questions$ 
  grd45::  $belongingQuiz(quest) = q$ 
  grd46::  $result = FALSE$ 
  The update has not been successfully. The previous text of the question is restored
  grd61::  $u \notin host[quizInstances \setminus finishedQuiz]$ 
  The host of an active quiz instance shall not be allowed to update a question of a quiz at the
  same time.
  grd62:  $\forall qi \cdot qi \in quizInstances \wedge qi \in instanceOfQuiz^{-1}[\{q\}] \Rightarrow qi \notin (quizInstances \setminus finishedQuiz)$ 

  The creator of a quiz shall not be allowed to update a question of the quiz if there exists an active
  quiz instance, linked to the quiz, being hosted at the same time.
then
  skip
end
Event HOST_QUIZ_INSTANCE ⟨ordinary⟩  $\hat{=}$ 
extends HOST_QUIZ_INSTANCE
any
  u
  q
  qi
  r
where
  grd61::  $u \in loggedIn$ 
  The user u must be logged in
  grd62::  $qi \in INSTANCE_QUIZ \setminus quizInstances$ 
  grd63::  $q \in quizzes$ 
  grd65::  $u \notin ran((finishedQuiz \triangleleft host))$ 
  The user u must not be hosting any other active quiz instance
  grd66:  $u \in (\{quizCreator(q)\} \cup sharedTo[\{q\}])$ 
  The user u must be the creator or have access to the quiz

```

```

    grd67: belongingQuiz-1[{q}] ≠ ∅
        The quiz must have at least 1 question
    grd91: r ∈ REPORT \ reports
        A new report is created. Initially the report is an empty file. When the quiz instance terminates
        the report
        will be populated with the information resulting from the content of the question summaries
then
    act61: quizInstances := quizInstances ∪ {qi}
    act62: host(qi) := u
        The host of the quiz instance is u
    act63: instanceOfQuiz(qi) := q
        The quiz instance is linked to the quiz q
    act64: quizCreated := quizCreated ∪ {qi}
        The quiz instance is in the quizCreated state
    act91: embeddedQuestions := embeddedQuestions ∪ ({qi} × {quests | quests ∈ questions ∧ belongingQuiz(quests) =
        q})
        The quiz instance is linked to the questions of the quiz
    act92: reports := reports ∪ {r}
        The report is added to the set of reports
    act93: reportedBy(qi) := r
        The quiz instance is linked to the report
end
Event BEGIN_QUIZ_INSTANCE ⟨ordinary⟩ ≐
extends BEGIN_QUIZ_INSTANCE
any
    u
    qi
where
    grd61: u ∈ loggedIn
        The user u must be logged in
    grd62: qi ∈ quizCreated
        The quiz instance must be in the quizCreated state
    grd63: host(qi) = u
        The host of the quiz instance must be u
then
    act61: quizCreated := quizCreated \ {qi}
        The quiz instance is not in the quizCreated state anymore
    act62: quizInit := quizInit ∪ {qi}
        The quiz instance becomes part of the quizInit state set
    act63: answeredQuestions(qi) := 0
        No question has been answered so far
end
Event START_QUIZ_INSTANCE ⟨ordinary⟩ ≐
extends START_QUIZ_INSTANCE
any
    u
    qi
    quest
where
    grd61: u ∈ loggedIn
        The user u must be logged in
    grd62: qi ∈ quizInit
        The quiz instance must be in the quizInit state
    grd63: host(qi) = u
        The host of the quiz instance must be u
    grd64:  $\forall k. \text{belongingQuiz}(k) = \text{instanceOfQuiz}(qi) \Rightarrow \text{questionPosition}(k) \geq \text{questionPosition}(\text{quest})$ 
        The question of the quiz that will become the first question to be answered in the quiz instance
        must be the first one in the question list of the quiz

```

```

    grd65:  $qi \in \text{ran}(\text{playingIn})$ 
        Some players must have joined the quiz during the quizInit state
  then
    act61:  $\text{quizInit} := \text{quizInit} \setminus \{qi\}$ 
        The quiz is not in the quizInit state anymore
    act62:  $\text{questioning} := \text{questioning} \cup \{qi\}$ 
        The quiz instance is in the questioning state
    act63:  $\text{currentQuestion}(qi) := \text{quest}$ 
        The current question of the quiz instance is the first question of the question list of the quiz
    act101:  $\text{questionStartedAt}(qi) := \text{time}$ 
    act102:  $\text{questionEndsAt}(qi) := \text{time} + \text{questionTime}(\text{quest})$ 
  end
Event JOIN_QUIZ_INSTANCE  $\langle \text{ordinary} \rangle \hat{=}$ 
extends JOIN_QUIZ_INSTANCE
  any
     $u$ 
     $qi$ 
  where
    grd61:  $u \in \text{USER}$ 
        The player can be either registered or unregistered
    grd62:  $qi \in \text{quizInit}$ 
        It is possible to join a quiz instance only if it is in the quizInit state
    grd63:  $u \neq \text{host}(qi)$ 
        The player must not be the host of the quiz instance
    grd64:  $u \notin \text{dom}(\text{playingIn})$ 
        The player must not be playing in another quiz instance
    grd1:  $u \notin \text{host}[\text{quizInstances} \setminus \text{finishedQuiz}]$ 
        The player cannot be any registered user that is hosting any active quiz instance
  then
    act64:  $\text{playingIn} := \text{playingIn} \cup \{u \mapsto qi\}$ 
  end
Event ANSWER_QUESTION  $\langle \text{ordinary} \rangle \hat{=}$ 
extends ANSWER_QUESTION
  any
     $p$ 
     $qi$ 
     $\text{quest}$ 
     $a$ 
  where
    grd61:  $p \in \text{USER}$ 
    grd62:  $qi \in \text{quizInstances}$ 
    grd63:  $p \in \text{playingIn}^{-1}[\{qi\}]$ 
        The player must be playing in the quiz instance
    grd64:  $qi \in \text{questioning}$ 
        The quiz instance must be in the questioning state
    grd65:  $\text{quest} \in \text{questions}$ 
    grd66:  $\text{currentQuestion}(qi) = \text{quest}$ 
        The question the player is answering must be the current question
    grd67:  $a \in \text{answers}$ 
    grd68:  $a \in \text{belongingQuestion}^{-1}[\{\text{quest}\}]$ 
        The answer being selected must belong to the current question of the quiz instance
    grd69:  $\text{card}(\text{peopleAnswers}^{-1}[\{qi\}]) < \text{card}(\text{playingIn}^{-1}[\{qi\}])$ 
        A player of a quiz instance shall not be allowed to select an answer when all other players
        have answered because the quiz instance passes to the questionSummary state.
    grd101:  $\text{time} < \text{questionEndsAt}(qi)$ 
        A player shall be allowed to answer a question only within the time of the question.
  then
    act61:  $\text{peopleAnswers} := \text{peopleAnswers} \cup \{p \mapsto qi\}$ 
    act62:  $\text{peopleSelectedAnswer} := \text{peopleSelectedAnswer} \Leftarrow \{p \mapsto a\}$ 

```



```

end
Event END_QUESTION_ALL_ANSWERED ⟨ordinary⟩ ≐
extends END_QUESTION_ALL_ANSWERED
any
  qi
  qs
  r
where
  grd61:: qi ∈ questioning
    The quiz instance must be in the questionig state
  grd62::  $\text{card}(\text{peopleAnswers}^{-1}[\{qi\}]) = \text{card}(\text{playingIn}^{-1}[\{qi\}])$ 
    All players must have answered
  grd91: qs ∈ QUESTION_SUMMARY \ qSummary
    A question summary is generated. The question summary is populated with information about
    the performance of the players by using the information resulting
    from the relation peopleSelectedAnswer
  grd92: r ∈ reports
  grd93: reportedBy(qi) = r
    r must be the report of the quiz instance
  grd101: time < questionEndsAt(qi)
    this event can be used only if all players have
    answered the question within its time. Otherwise,
    the even END_QUESTION_TIME_IS_UP must be used
then
  act61:: questioning := questioning \ {qi}
    The quiz instance is not part of the questioning state anymore
  act62:: questionSummary := questionSummary ∪ {qi}
    The quiz instance passes to the questionSummary state
  act63:: answeredQuestions(qi) := answeredQuestions(qi) + 1
    The number of answered questions is incremented by 1
  act64:: peopleAnswers := peopleAnswers ▷ {qi}
    The players that have answered the question of the quiz instance are removed
  act65: peopleSelectedAnswer := playingIn-1[{qi}] ≲ peopleSelectedAnswer
    The answers select by the players of the quiz instance are removed
  act91: qSummary := qSummary ∪ {qs}
  act92: summaryFor(qs) := (qi ↦ currentQuestion(qi))
    The summary is linked to the quiz instance and current question of the quiz instance
  act93: qReportedBy(qs) := r
    The question summary is linked to the report of the quiz instance
  act101: questionStartedAt := {qi} ≲ questionStartedAt
  act102: questionEndsAt := {qi} ≲ questionEndsAt
end
Event END_QUESTION_PREMATURATELY ⟨ordinary⟩ ≐
extends END_QUESTION_PREMATURATELY
any
  u
  qi
  qs
  r
where
  grd61:: qi ∈ questioning
    The quiz instance must be in the question state
  grd62:: u ∈ loggedIn
    The user u must be logged in
  grd63:: host(qi) = u
    The host of the quiz instance must be u
  grd1:  $\text{card}(\text{peopleAnswers}^{-1}[\{qi\}]) \neq \text{card}(\text{playingIn}^{-1}[\{qi\}])$ 
    The host of a quiz instance in the questioning state
    shall not be allowed to end prematurely a question
    if all players have answered because the quiz instance passes to the questionSummary state.

```

```

    grd91:  $qs \in QUESTION\_SUMMARY \setminus qSummary$ 
    grd92:  $r \in reports$ 
    grd93:  $reportedBy(qi) = r$ 
    grd101:  $time < questionEndsAt(qi)$ 
    The host of a quiz instance in the questioning state shall be allowed to end a question prematurely only if the question time is not up.
  then
    act61:  $questioning := questioning \setminus \{qi\}$ 
    The quiz instance is not in the questioning state anymore
    act62:  $questionSummary := questionSummary \cup \{qi\}$ 
    The quiz instance passes to the questionSummary state
    act63:  $answeredQuestions(qi) := answeredQuestions(qi) + 1$ 
    The number of answered questions of the quiz instance is incremented by 1
    act64:  $peopleAnswers := peopleAnswers \triangleright \{qi\}$ 
    The players that have answered the question of the quiz instance are removed
    act65:  $peopleSelectedAnswer := playingIn^{-1}[\{qi\}] \triangleleft peopleSelectedAnswer$ 
    The answers select by the players of the quiz instance are removed
    act91:  $qSummary := qSummary \cup \{qs\}$ 
    act92:  $summaryFor(qs) := qi \mapsto currentQuestion(qi)$ 
    act93:  $qReportedBy(qs) := r$ 
    act101:  $questionStartedAt := \{qi\} \triangleleft questionStartedAt$ 
    act102:  $questionEndsAt := \{qi\} \triangleleft questionEndsAt$ 
  end
Event SHOW_QUESTION_SUMMARY_TO_PLAYERS  $\langle ordinary \rangle \triangleq$ 
extends SHOW_QUESTION_SUMMARY_TO_PLAYERS
  any
     $u$ 
     $qi$ 
     $qs$ 
  where
    grd61:  $u \in loggedIn$ 
    The user u must be logged in
    grd62:  $qi \in quizInstances$ 
    grd63:  $host(qi) = u$ 
    The user u must be the host of the quiz instance
    grd63:  $qi \in questionSummary$ 
    The quiz instance must be in the questionSummary state
    grd64:  $qi \in ran(playingIn)$ 
    The host of a quiz instance in the questionSummary state shall be allowed to show the question summary only if at least 1 player is playing in the quiz instance.
    grd91:  $summaryFor(qs) = qi \mapsto currentQuestion(qi)$ 
    The summary to show must be the summary linked to the quiz instance and current question of the quiz instance
  then
    skip
  end
Event NEXT_QUESTION  $\langle ordinary \rangle \triangleq$ 
extends NEXT_QUESTION
  any
     $u$ 
     $qi$ 
     $quest$ 
  where
    grd61:  $u \in loggedIn$ 
    grd62:  $qi \in questionSummary$ 
    The quiz instance must be in the questionSummary state
    grd63:  $host(qi) = u$ 

```

```

    grd64:: answeredQuestions(qi) < card(belongingQuiz-1{instanceOfQuiz(qi)})
        There must be other questions to be answered
    grd65: qi ∈ ran(playingIn)
        At least 1 player must be playing in the quiz instance
    grd66: quest ∈ questions
    grd67: card({quests|quests ∈ questions ∧ quests ∈ belongingQuiz-1{instanceOfQuiz(qi)} ∧
        questionPosition(quests) < questionPosition(quest)} ) = answeredQuestions(qi)
        The next question to be answered must be the successive one
then
    act61:: questionSummary := questionSummary \ {qi}
        The quiz instance is not in the questionSummary state anymore
    act62:: questioning := questioning ∪ {qi}
        The quiz instance passes to the questioning state
    act63: currentQuestion(qi) := quest
        The current question is set to the successive question
    act101: questionStartedAt(qi) := time
    act102: questionEndsAt(qi) := time + questionTime(quest)
end
Event FINISH_QUIZ_INSTANCE ⟨ordinary⟩ ≐
extends FINISH_QUIZ_INSTANCE
any
    u
    qi
where
    grd61:: u ∈ loggedIn
        The user must be logged in
    grd62:: qi ∈ questionSummary
        The quiz instance must be in the questionSummary state
    grd63:: host(qi) = u
        The user u must be the host of the quiz instance
then
    act61:: questionSummary := questionSummary \ {qi}
        The quiz instance is not in the questionSummary state anymore
    act62:: quizSummary := quizSummary ∪ {qi}
        The quiz instance passes to the quizSummary state
    act63:: currentQuestion := {qi} ≺ currentQuestion
        The current question of the quiz instance is removed as it is not anymore in the questionSummary
        state
end
Event SHOW_QUIZ_INSTANCE_SUMMARY_TO_PLAYERS ⟨ordinary⟩ ≐
extends SHOW_QUIZ_INSTANCE_SUMMARY_TO_PLAYERS
any
    qi
    u
    r
where
    grd61:: qi ∈ quizInstances
    grd62: qi ∈ quizSummary
        The quiz instance must be in the quizSummary state
    grd63: u ∈ registeredUser
    grd64: u ∈ loggedIn
        The user u must be logged in
    grd65: host(qi) = u
        The user u must be the host of the quiz instance
    grd66: qi ∈ ran(playingIn)
        there must at least 1 player playing in the quiz instance
    grd91: r ∈ reports
    grd92: reportedBy(qi) = r
        the report to show must be the report of the quiz instance

```

```

    then
        skip
    end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_SUMMARY_STATE ⟨ordinary⟩ ≐
extends TERMINATE_QUIZ_INSTANCE_QUIZ_SUMMARY_STATE
any
    u
    qi
where
    grd61: u ∈ loggedIn
        The user u must be logged in
    grd62: qi ∈ quizSummary
        The quiz instance must be in the quizSummary state
    grd63: host(qi) = u
        The user u must be the host of the quiz instance
    then
        act61: quizSummary := quizSummary \ {qi}
            The quiz instance is not in the quizSummary state anymore
        act62: finishedQuiz := finishedQuiz ∪ {qi}
            The quiz instance passes to the finishedQuiz state
        act63: playingIn := playingIn ▷ {qi}
            The players of the quiz instance do not play anymore in the quiz instance
        act91: embeddedQuestions := {qi} ◁ embeddedQuestions
            The quiz instance is not linked anymore to the questions of the quiz instance
        act92: summaryFor := summaryFor ▷ ({qi} ◁ embeddedQuestions)
            The question summaries do not report anymore a specific question of the quiz instance
        act93: qSummary := qSummary \ summaryFor-1[{qi} ◁ embeddedQuestions]
            All the summaries of the quiz instance built so far must be deleted
        act94: qReportedBy := qReportedBy ▷ reportedBy[{qi}]
            The question summaries are not linked anymore to the report of the quiz instance
    end
Event LEAVE_QUIZ_INSTANCE_LAST_ONE_IN_QUESTIONING_STATE ⟨ordinary⟩ ≐
extends LEAVE_QUIZ_INSTANCE_LAST_ONE_IN_QUESTIONING_STATE
any
    p
    qi
    qs
    r
where
    grd61: p ∈ USER
    grd62: qi ∈ questioning
        The quiz instance must be in the questioning state
    grd63: p ∈ playingIn-1[{qi}]
        The player must be playing in the quiz instance
    grd64: card(playingIn-1[{qi}]) = 1
        The player must be the only player be playing in the quiz instance
    grd91: qs ∈ QUESTION_SUMMARY \ qSummary
        A question summary is generated
    grd92: r ∈ reports
    grd93: reportedBy(qi) = r
        Thw question summary is linked to the report of the quiz instance
    grd101: time < questionEndsAt(qi)
        A player can leave during the questioning state only if the question time is not up
    grd102: card(peopleAnswers-1[{qi}]) < card(playingIn-1[{qi}])
        A player can only leave if not all other players have already answered
    then
        act61: playingIn := {p} ◁ playingIn
            The player does not play anymore in the quiz instance

```

```

act62: peopleAnswers := {p}  $\Leftarrow$  peopleAnswers
    It is removed whether the player has answered the question or not
act63: questioning := questioning \ {qi}
act64: questionSummary := questionSummary  $\cup$  {qi}
    The quiz instance passes to the questionSummary state
act65: peopleSelectedAnswer := {p}  $\Leftarrow$  peopleSelectedAnswer
    The answer selected by the player is removed (if he/she has answered)
act91: qSummary := qSummary  $\cup$  {qs}
act92: summaryFor(qs) := qi  $\mapsto$  currentQuestion(qi)
act93: qReportedBy(qs) := r
act101: questionStartedAt := {qi}  $\Leftarrow$  questionStartedAt
act102: questionEndsAt := {qi}  $\Leftarrow$  questionEndsAt
end

Event LEAVE_QUIZ_INSTANCE_NOT_IN_QUESTIONING_STATE  $\langle$ ordinary $\rangle \hat{=}$ 
extends LEAVE_QUIZ_INSTANCE_NOT_IN_QUESTIONING_STATE
any
    p
    qi
where
    grd61: p  $\in$  USER
    grd62: qi  $\in$  quizInstances \ (quizCreated  $\cup$  finishedQuiz  $\cup$  questioning)
        The quiz instance must not be in the quiz created state, finishedQuiz or questioning state
    grd63: p  $\in$  playingIn-1{qi}
        The player must be playing in the quiz instance
    then
        act61: playingIn := {p}  $\Leftarrow$  playingIn
            The player does not play anymore in the quiz instance
    end

Event LEAVE_QUIZ_INSTANCE_NOT_LAST_ONE_IN_QUESTIONING_STATE  $\langle$ ordinary $\rangle \hat{=}$ 
extends LEAVE_QUIZ_INSTANCE_NOT_LAST_ONE_IN_QUESTIONING_STATE
any
    p
    qi
where
    grd61: p  $\in$  USER
    grd62: qi  $\in$  questioning
    grd63: p  $\in$  playingIn-1{qi}
    grd64: card(playingIn-1{qi}) > 1
        There must be at least 2 players be playing
    grd101: time < questionEndsAt(qi)
        A player can leave during the questioning state only if the question time is not up
    grd102: card(peopleAnswers-1{qi}) < card(playingIn-1{qi})
        A player can only leave if not all other players have already answered
    then
        act61: playingIn := {p}  $\Leftarrow$  playingIn
        act62: peopleAnswers := {p}  $\Leftarrow$  peopleAnswers
        act63: peopleSelectedAnswer := {p}  $\Leftarrow$  peopleSelectedAnswer
    end

Event UNSHARE_QUIZ  $\langle$ ordinary $\rangle \hat{=}$ 
extends UNSHARE_QUIZ
any
    u1
    u2
    q
where
    grd41: u1  $\in$  registeredUser
    grd42: u2  $\in$  registeredUser
    grd43: u1  $\in$  loggedIn
        A registered user can unshare only if he/she is online

```

```

    grd44:  $u1 \neq u2$ 
    grd45:  $q \mapsto u2 \in sharedTo$ 
             u2 had to have access to the quiz
    grd46:  $u1 = quizCreator(q)$ 
             Only the creator of the quiz can unshare a quiz
    grd81:  $u2 \notin host[instanceOfQuiz^{-1}[\{q\}] \setminus finishedQuiz]$ 
             The creator of a quiz shall not be allowed to deshare a quiz
             with another registered user if the latter is hosting a quiz instance linked to the quiz.
    grd82:  $u1 \notin host[quizInstances \setminus finishedQuiz]$ 
             The creator of a quiz shall not be allowed to deshare a
             quiz if he/she is hosting an active quiz instance.
  then
    act41:  $sharedTo := sharedTo \setminus \{q \mapsto u2\}$ 
  end
Event REMOVE_QUIZ_INSTANCE  $\langle ordinary \rangle \triangleq$ 
extends REMOVE_QUIZ_INSTANCE
any
   $u$ 
   $qi$ 
where
  grd81:  $u \in registeredUser$ 
  grd82:  $qi \in quizInstances$ 
  grd83:  $qi \in finishedQuiz$ 
             It is possible to remove a quiz instance only when it is in the finishedQuiz state
  grd84:  $u \in loggedIn$ 
             The user must be logged in
  grd85:  $host(qi) = u$ 
             The user u must be the host of the quiz instance
  grd86:  $u \notin host[quizInstances \setminus finishedQuiz]$ 
             The user must not be hosting any active quiz instance
  then
    act81:  $quizInstances := quizInstances \setminus \{qi\}$ 
             The quiz instance is removed
    act82:  $finishedQuiz := finishedQuiz \setminus \{qi\}$ 
             The quiz instance is removed from the finishedQuiz state
    act83:  $host := \{qi\} \triangleleft host$ 
             The user is not the host of the quiz instance anymore
    act84:  $instanceOfQuiz := \{qi\} \triangleleft instanceOfQuiz$ 
             The quiz instance is not linked anymore to a quiz
    act85:  $answeredQuestions := \{qi\} \triangleleft answeredQuestions$ 
             The number of answered questions of the quiz instance is removed
    act91:  $reportedBy := \{qi\} \triangleleft reportedBy$ 
             The report of the quiz instance is removed
    act92:  $reports := reports \setminus \{reportedBy(qi)\}$ 
             The report is not macthed anymore to the quiz instance
  end
end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_CREATED_STATE  $\langle ordinary \rangle \triangleq$ 
extends TERMINATE_QUIZ_INSTANCE_QUIZ_CREATED_STATE
any
   $u$ 
   $qi$ 
where
  grd91:  $u \in registeredUser$ 
  grd92:  $u \in loggedIn$ 
             The user u must be loggedIn
  grd93:  $qi \in quizInstances$ 
  grd94:  $qi \in quizCreated$ 
             The quiz instance must be in the quizCreated state

```

```

    grd95: host(qi) = u
           The user u must be the host of the quiz instance
  then
    act91: quizCreated := quizCreated \ {qi}
           The quiz instance is removed from the quizCreated state
    act92: finishedQuiz := finishedQuiz ∪ {qi}
           The quiz instance passes to the finishedQuiz state
    act93: answeredQuestions(qi) := 0
           The number of answered questions is set to 0
    act94: embeddedQuestions := {qi} ⋈ embeddedQuestions
           The quiz instance is not linked anymore to the questions of the quiz instance
  end
Event TERMINATE_QUIZ_INSTANCE_QUIZ_INIT_STATE ⟨ordinary⟩ ≐
extends TERMINATE_QUIZ_INSTANCE_QUIZ_INIT_STATE
any
  u
  qi
where
  grd81: u ∈ registeredUser
  grd82: u ∈ loggedIn
           The user u must be loggedin
  grd83: qi ∈ quizInstances
  grd84: qi ∈ quizInit
           The quiz instance must be in the quizInit state
  grd85: host(qi) = u
           The user u must be the host of the quiz instance
  then
    act81: quizInit := quizInit \ {qi}
           The quiz instance is not anymore in the quizInit state
    act82: finishedQuiz := finishedQuiz ∪ {qi}
           The quiz instance passes to the finishedQuiz state
    act83: playingIn := playingIn ▷ {qi}
           The players of the quiz instance do not play anymore in the quiz instance
    act91: embeddedQuestions := {qi} ⋈ embeddedQuestions
           The quiz instance is not linked anymore to the questions of the quiz instance
  end
Event INCREASE_TIME ⟨ordinary⟩ ≐
when
  grd101:  $\forall qi. qi \in quizInstances \wedge qi \in questioning \Rightarrow card(peopleAnswers^{-1}[\{qi\}]) < card(playingIn^{-1}[\{qi\}])$ 
           It is possible to increase the time only if in all quiz instances in the questioning state
           not all players have answered
  grd102:  $\forall qi. qi \in quizInstances \wedge qi \in questioning \Rightarrow time < questionEndsAt(qi)$ 
           It is possible to increase the time only if the ending time of each quiz instance in the questioning
           state is strictly greater than the current time
  then
    act101: time := time + 1
           Time is increased by 1
  end
Event END_QUESTION_TIME_IS_UP ⟨ordinary⟩ ≐
extends END_QUESTION_TIME_IS_UP
any
  qi
  qs
  r
where
  grd61: qi ∈ quizInstances
  grd62: qi ∈ questioning
           The quiz instance must be in the questioning state

```

```

    grd91:  $qs \in QUESTION\_SUMMARY \setminus qSummary$ 
    grd92:  $r \in reports$ 
    grd93:  $reportedBy(qi) = r$ 
    grd101:  $time = questionEndsAt(qi)$ 
        The time must be equal to the ending time of the quiz instance
    then
        act61:  $questioning := questioning \setminus \{qi\}$ 
        act62:  $questionSummary := questionSummary \cup \{qi\}$ 
            The quiz instance passes to the questionSummary state
        act63:  $answeredQuestions(qi) := answeredQuestions(qi) + 1$ 
            The number of answered questions of the quiz instance is incremented by 1
        act64:  $peopleAnswers := peopleAnswers \triangleright \{qi\}$ 
        act65:  $peopleSelectedAnswer := playingIn^{-1}[\{qi\}] \triangleleft peopleSelectedAnswer$ 
        act91:  $qSummary := qSummary \cup \{qs\}$ 
        act92:  $summaryFor(qs) := (qi \mapsto currentQuestion(qi))$ 
        act93:  $qReportedBy(qs) := r$ 
        act101:  $questionStartedAt := \{qi\} \triangleleft questionStartedAt$ 
        act102:  $questionEndsAt := \{qi\} \triangleleft questionEndsAt$ 
    end
END

```


CLASS DIAGRAM

