Introduction to Intelligent Systems '19/'20 Lab 2

Useful matlab functions: load, plot, hold on, hist, bar, length, find, rand, char, sum, xor, normpdf

Instructions

You should hand in a brief report, in which you provide answers to all the problems, with the same structure of the present document (Assignment 1, Assignment 2, etc.). The code developed to solve the problems has to be included in the report, commented, and opportunely referenced.

The plots have to be self-consistent, with clear title, labels and captions. They have to be sufficiently commented in the text.

The grading will be based on the following aspects (ordered acc. to importance):

- completeness of the report and correctness/plausibility of the results
- readability, layout, formatting of the text
- appearance of the plot, e.g. axis labels, quality of the caption
- language/English issues

A grade equal to 10 can be achieved by solving all the problems correctly and matching the above conditions. The bonus assignment 3 can be evaluated to compensate for eventual deficits of above conditions.

Assignment 1

class conditional probabilities, priors, posterior probabilities, Bayes decision rule, minimum error classification.

Let's assume we obtained the class conditional probability of salmon and sea bass, describing the distribution of the length of the two classes. These are given by p_salmon and p_seabass at length 1 (in cm), all in the file lab3_1.mat.

- 1. Given that sea bass is caught 3 times as often as salmon, calculate the posterior probabilities (don't forget to normalize to 1 for all lengths) and plot them.
- 2. Now a new fish is measured, which turns out to have a length of 8 cm. According to your posterior probabilities, how would you classify this fish? And what if it's length is 20 cm?

Assignment 2

normal distribution.

62.3468

Consider the following two sets of observed 1D data (feature values) coming from objects of two different classes (read the data from the file lab3_1.mat):

```
S1 = [-30.8508]
                   23.6509
                              -15.4613
                                          -0.0466
                                                     26.5835
                                                                41.1727
  -23.5292
              47.8198
                         29.8043
                                   7.9640
                                                       3.4718
                                             4.1434
  0.9068
            10.6914
                      11.5387
                                 34.7819
                                            55.8093
                                                       24.0074
  3.7086
            28.7557
                      15.4968
                                 -20.8930
                                                        19.2119
                                             38.4767
  14.0552
             25.4574
                       17.8422
                                   -18.2446
                                              5.1299
                                                        5.61847
S2 = [44.6799]
                 66.8210
                            41.2427
                                       45.1618
                                                 42.8800
                                                            38.2579
  48.0776
             47.2593
                       65.3007
                                  47.5098
                                             39.3579
                                                        66.0346
```

and the following test set of data points that need to be classified:

34.9384]

```
T = [5 \quad 23 \quad 40 \quad 70 \quad 95]
```

47.7037

- 1. Plot the elements of the two sets S1 and S2 on the x-axis of a Fig. 1: the elements of S1 as blue circles (bo) and the elements of the set S2 as red circles (ro). Plot in the same Fig. 1 the points of the test set T as black squares (ks).
- 2. Let's assume S1 and S2 are drawn from normal distributions. Compute the parameters (mean and standard deviation) of the two distributions, using maximum estimation. Create a Fig.2 in which you plot the two Gaussian functions, one in blue the other in red, together with the points of the two training data sets S1 and S2. The two functions are the class conditional probability densities $p(x|\omega_1)$ and $p(x|\omega_2)$ that the two classes produce a value x of the considered feature. Comment on the use of the functions, in comparison to using the rugged data.
- 3. Estimate the prior probabilities $P(\omega_1)$ and $P(\omega_2)$.
- 4. Create a Fig. 3 in which you plot the two products $P(\omega_1)p(x|\omega_1)$ and $P(\omega_2)p(x|\omega_2)$, together with the points of the two training data sets S1 and S2 and the test set T.

- 5. Substitute the values of the prior probabilities and the class conditional probability densities determined above in the equation $P(\omega_1)p(x|\omega_1) = P(\omega_2)p(x|\omega_2)$ and solve the resulting equation for x in order to determine the value(s) of the decision criterion that we should use for classification.
- 6. Using the thus obtained value(s) of the decision criterion, determine the classes of the points in the test set [5 23 40 70 95]. Create a Fig. 4 which copies Fig. 3 and adds to it a specification of which domain on the x-axis belongs to class 1 (blue) and which complementary domain corresponds to class 2 (red).
- 7. Evaluate the misclassification rate of the created classifier for each of the two classes. (For this, you can for instance use the error function erf, familiar from the iris recognition assignment in the first week.)

Assignment 3 (BONUS)

Let us consider two one-dimensional normal distributions with mean $m_1 = 1$ and $m_2 = -3$, with standard deviations $s_1 = s_2 = \sqrt{2}$. The two distributions have same prior probability $P(w_1) = P(w_2) = 0.5$. Compute the value of the decision criterion x*. Briefly comment on the approach that you take and report the main steps of the calculations.