

Big Data Analytics

Introduction to Complex System

Site percolation on the square lattice

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1 Introduction

The site percolation model simulation was written in Java in version 15 with usage of IntelliJ IDE (2021.1). All plots were generated by using python in version 3.8 and with usage of Pycharm IDE (2021.1). Computer used for all calculations has the following parameters:

- Intel® Core™ i5-7200U CPU @ 2.50GHz \times 4
- 16GB RAM memory
- 512GB of SSD storage
- Ubuntu 20.04.2 LTS 64 bit

With given parameters: $L = x$, $T = 100$, $p_0 = 0.0$, $p_k = 1.0$, $d_p = 0.001$ time needed to get result file is:

- 1, 55s for $x = 10$
- 23, 4s for $x = 50$
- 90, 3s for $x = 100$

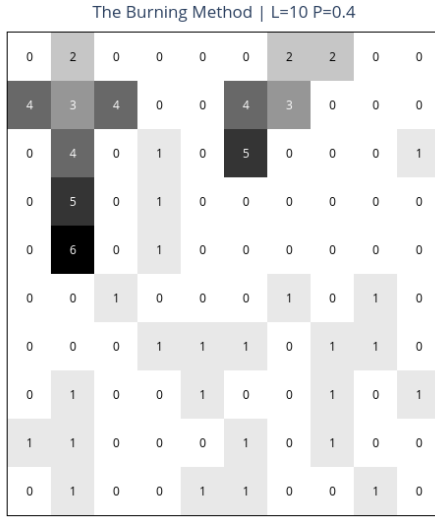
All simulations presented in this document were generated for $T = 10^4$ and $d_p = 0.001$

2 Presentation results

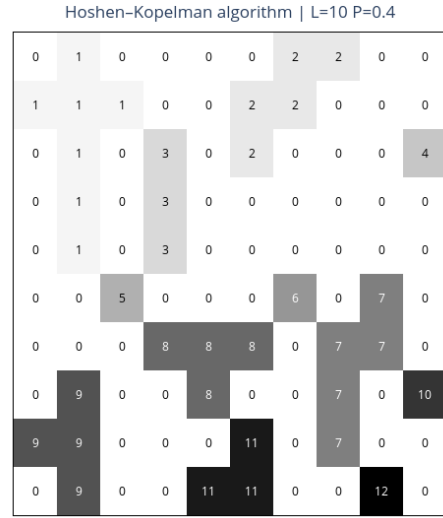
2.1 Part I

Visualize sample configurations for $L = 10$ and 3 values of $p = 0.4, 0.6, 0.8$ within two methods:

- (1) use the burning algorithm and describe each site by the number
- (2) use the HK algorithm and color each cluster with the different color.

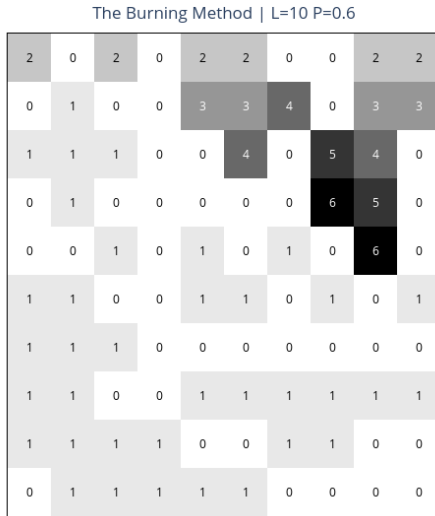


(a)

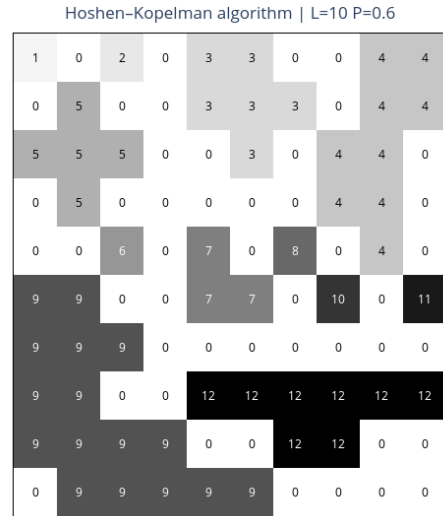


(b)

Figure 1: An example of the burning method (a) and HK algorithm (b) for $p = 0.4$



(a)



(b)

Figure 2: An example of the burning method (a) and HK algorithm (b) for $p = 0.6$

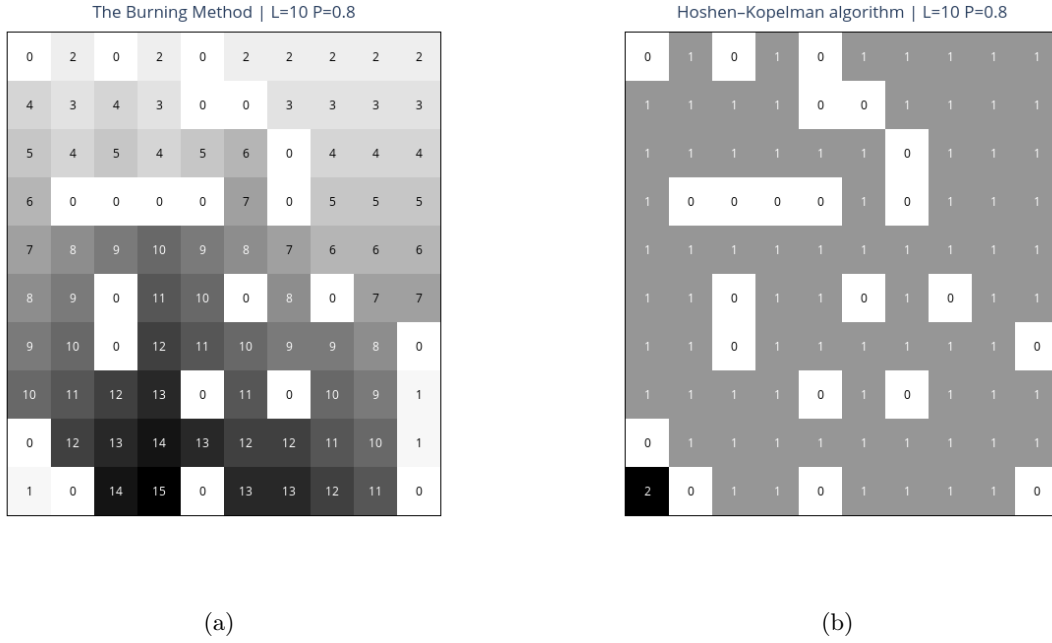


Figure 3: An example of the burning method (a) and HK algorithm (b) for $p = 0.8$

2.2 Part II

Present P_{flow} (that the path connecting the first and the last row exists) as a function of p for $L = 10, 50, 100$ and for $T = 10^4$.

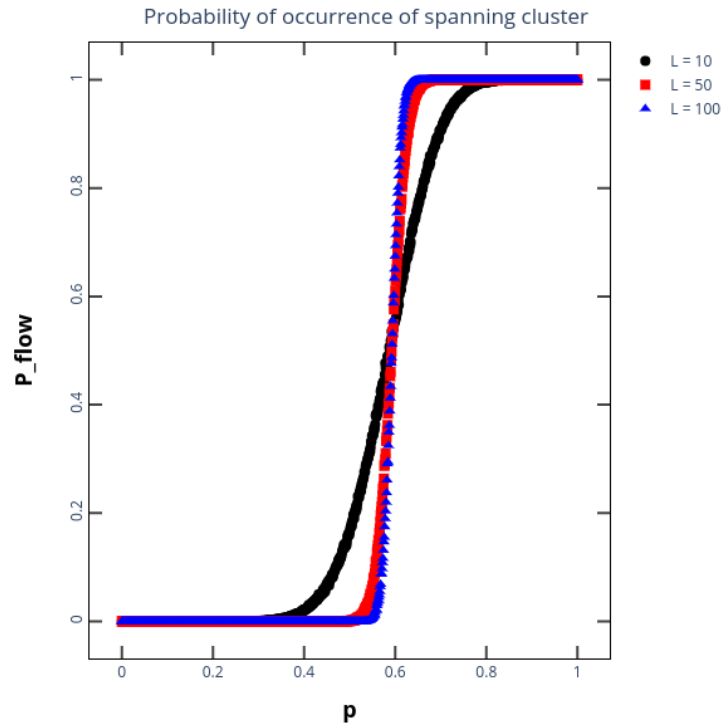


Figure 4: Probability P_{flow} that the path connecting the first and the last row exists as a function of p for $L = 10, 50, 100$

2.3 Part III

Present average size of the maximum cluster as a function of p for $L = 10, 50, 100$ and for $T = 10^4$.

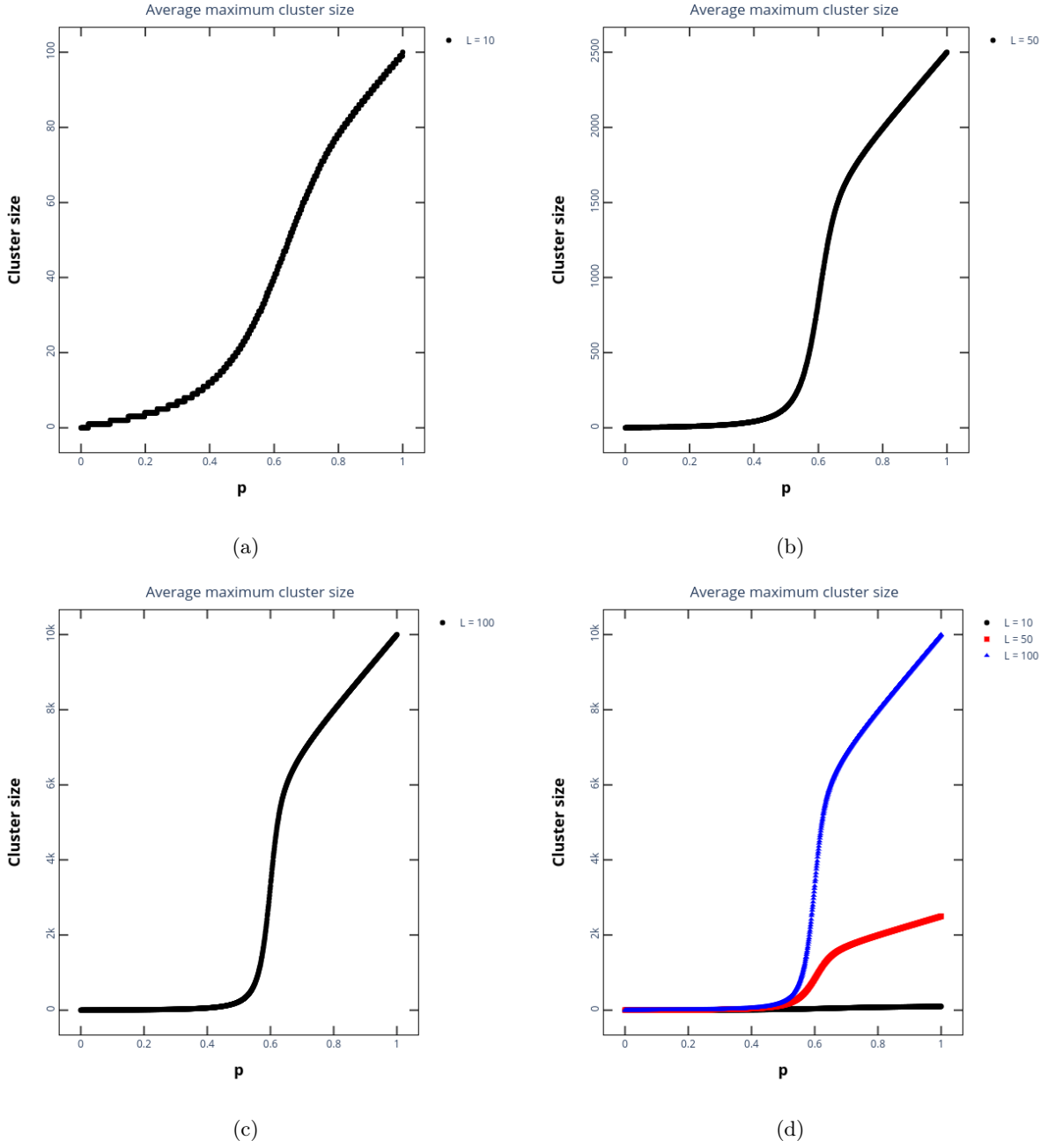
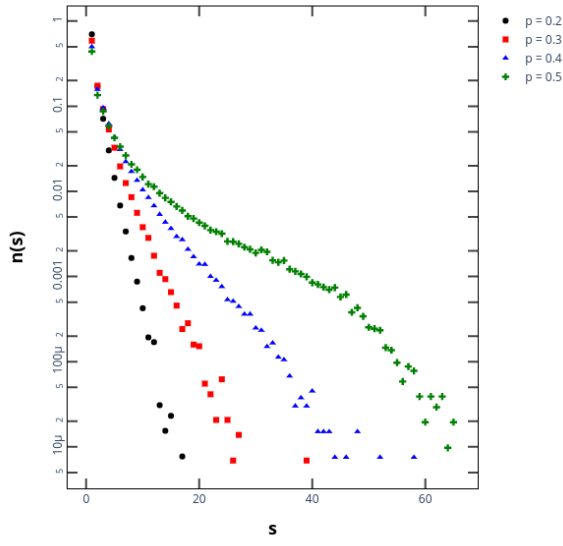


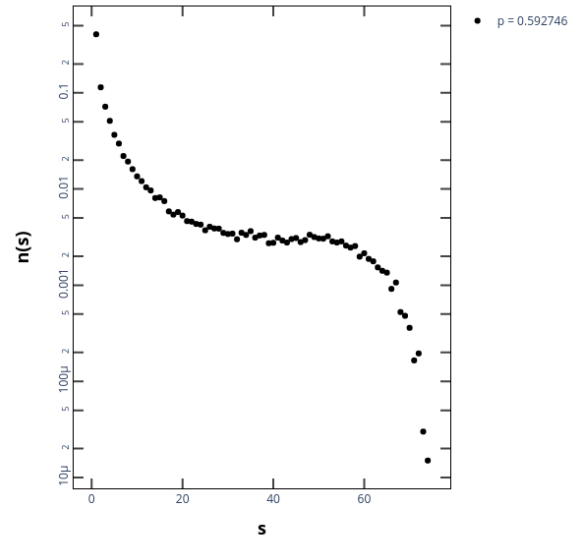
Figure 5: Graphs a, b, c show the average size of the maximum cluster size for $L = 10, L = 50, L = 100$ respectively. Graph d shows the overlapping graphs.

2.4 Part IV

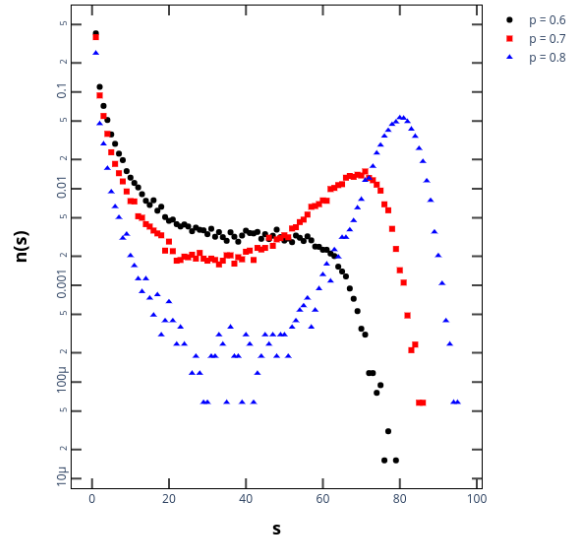
Present distribution of clusters $n(s, p, L)$ for a given $p : 0.2, 0.3, 0.4, 0.5, 0.592746, 0.6, 0.7, 0.8$.



(a)

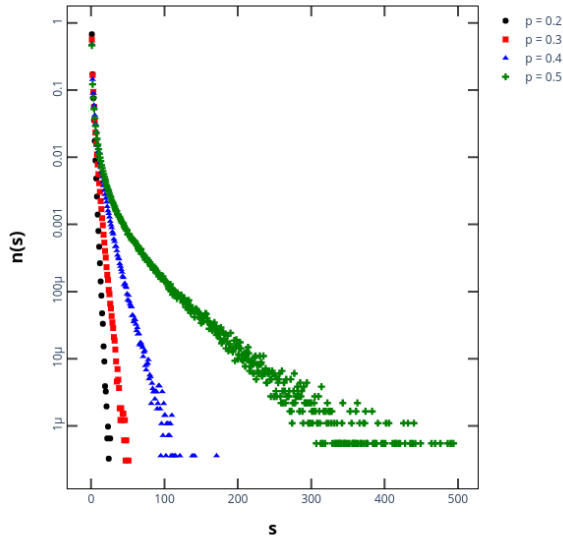


(b)

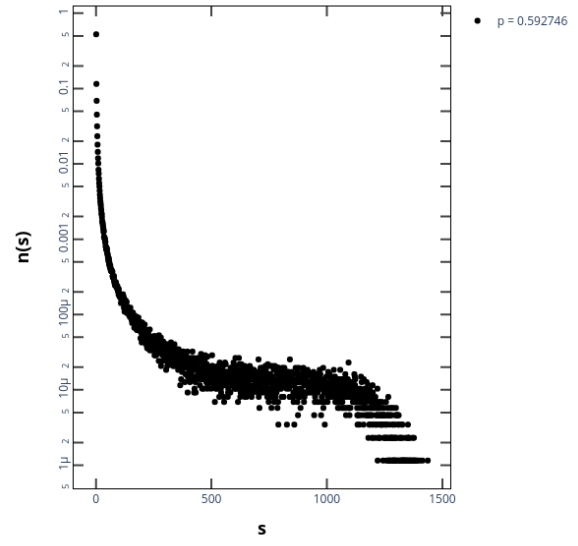


(c)

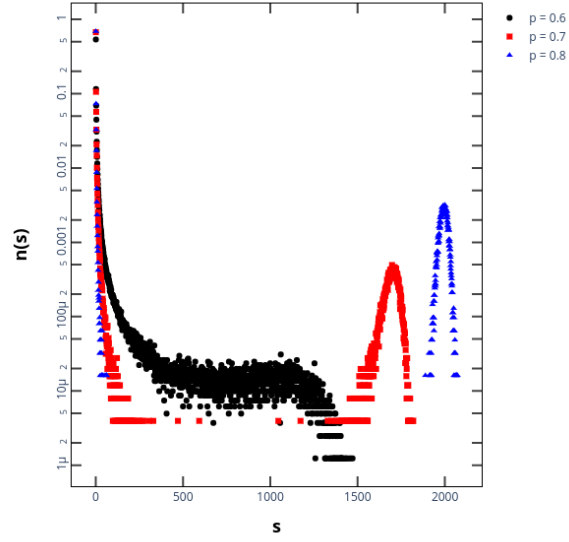
Figure 6: Cluster size distributions for square lattice, for $p < p_c$ (a), $p = p_c = 0.592746$ (b) and $p > p_c$ (c), with $L = 10$, averaged over $T = 10^4$ trials.



(a)

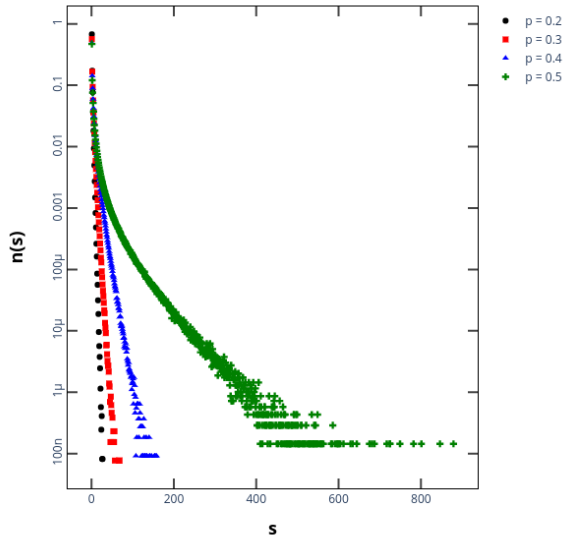


(b)

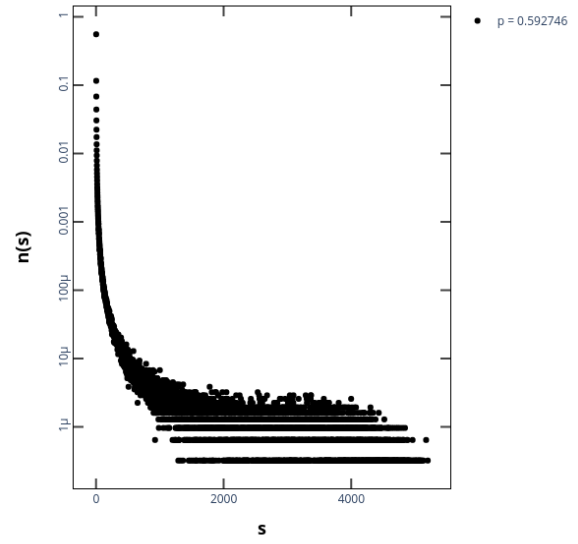


(c)

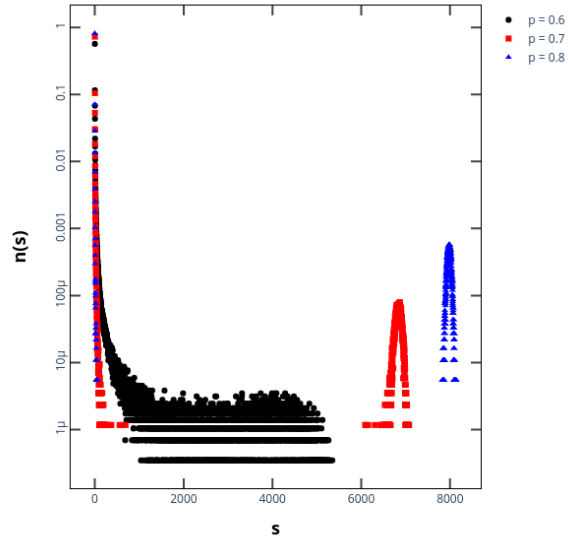
Figure 7: Cluster size distributions for square lattice, for $p < p_c$ (a), $p = p_c = 0.592746$ (b) and $p > p_c$ (c), with $L = 50$, averaged over $T = 10^4$ trials.



(a)



(b)



(c)

Figure 8: Cluster size distributions for square lattice, for $p < p_c$ (a), $p = p_c = 0.592746$ (b) and $p > p_c$ (c), with $L = 100$, averaged over $T = 10^4$ trials.