

## TOPOLOGICAL SORTING

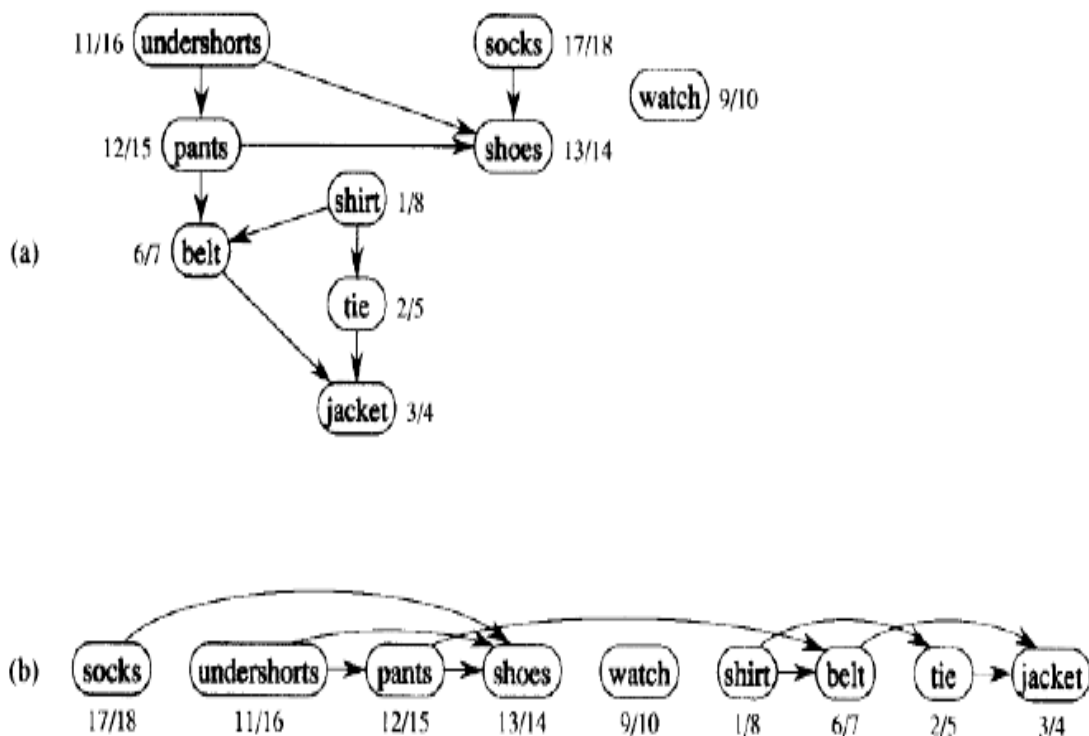
- A cycle in a diagram or directed graph  $G$  is a set of edges,  $\{(v_1, v_2), (v_2, v_3), \dots, (v_{r-1}, v_r)\}$  where  $v_1 = v_r$ . A diagram is acyclic if it has no cycles. Such a graph is often referred to as a directed acyclic graph, or DAG
- Topological sorting for Directed Acyclic Graph (DAG)  $G=(V,E)$  is a linear ordering of all its vertices such that if  $G$  contains an edge  $(u,v)$ , then vertex  $u$  comes before  $v$  in the ordering.
- Topological Sorting for a graph is not possible if the graph is not a DAG.
- We can view a Topological Sort of a graph as an ordering of its vertices along a horizontal line so that all directed edges go from left to right.

### Algorithm

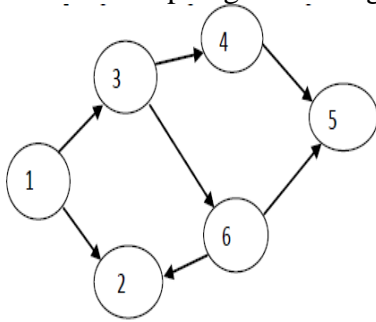
#### TOPOLOGICAL-SORT( $G$ )

1. Call DFS( $G$ ) to compute finishing times  $f[v]$  for all  $v$  in  $V$
2. as each vertex is finished, insert it onto the front of a linked list
3. **return** the linked list of vertices

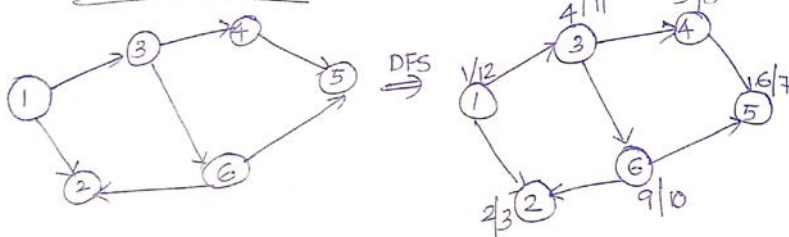
- **Time complexity:** We can perform a topological sort in time ,  $O(V+E)$  , since depth-first search takes  $O(V+E)$  time and it takes  $O(1)$  time to insert each of the  $V$  vertices on to the front of the linked list.



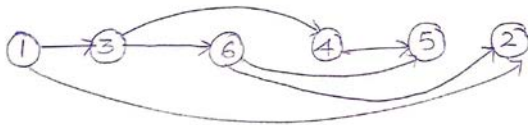
1. Write the topological sorting for the DAG given below [December 2019-2marks]



topological sorting



topological ordering



CS Scanned with CamScanner

topological sorting 1-3-6-4-5-2