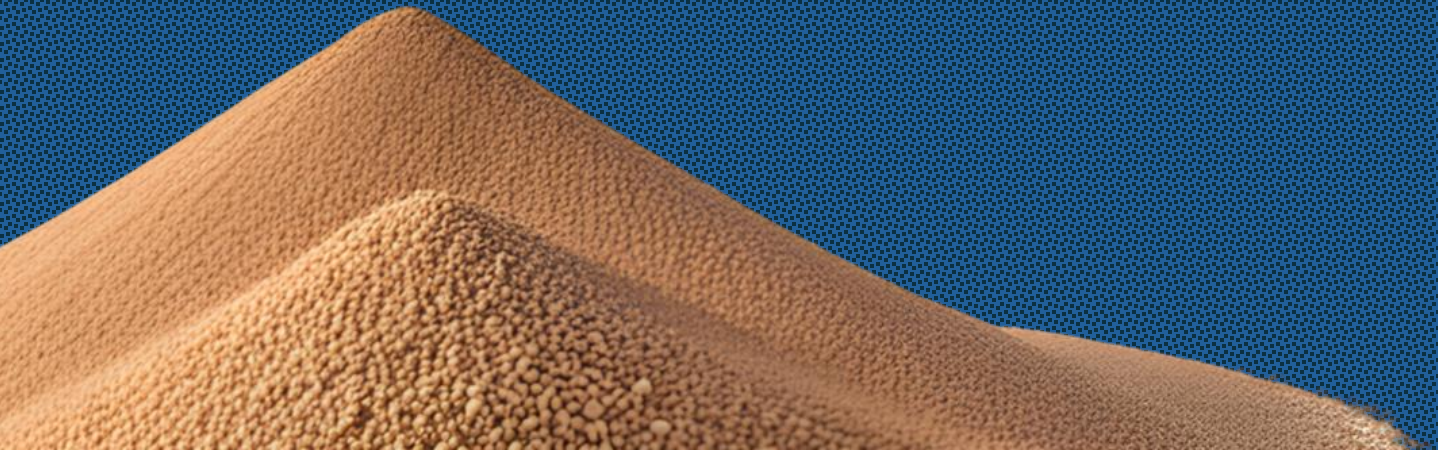


# A SIMPLE IMPLEMENTATION OF THE ABELIAN SANDPILE MODEL

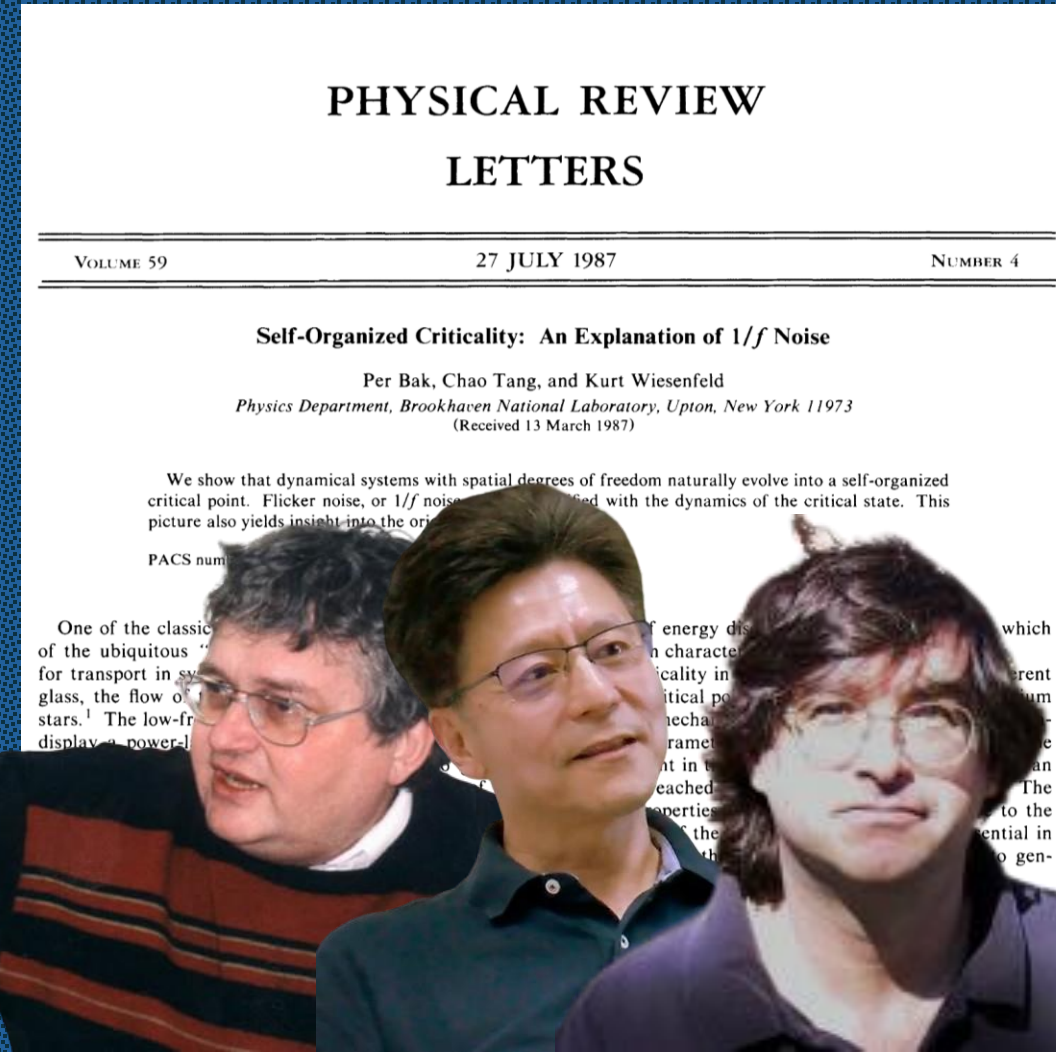
*Alberto Zaghini – Collegio Superiore*

*April 2024*



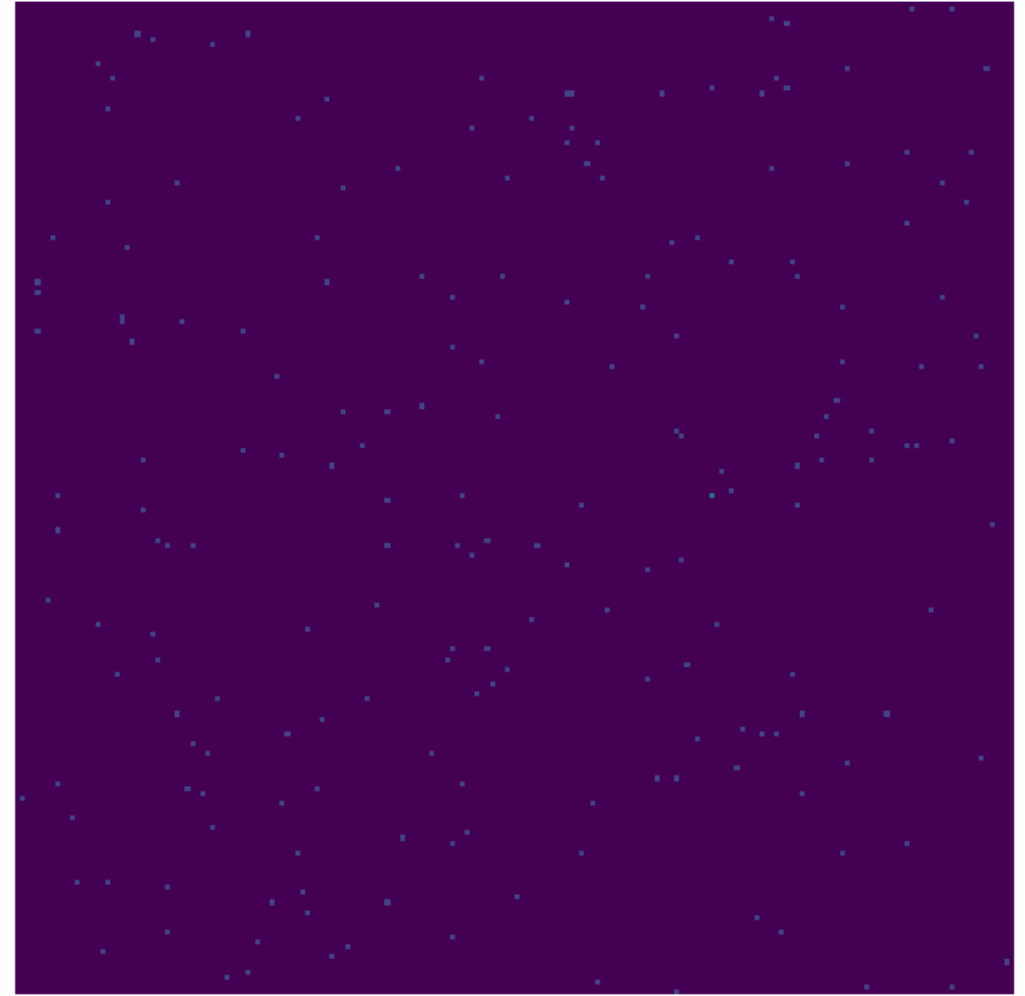
# BACKGROUND

- *Self-Organized Criticality (SOC):*  
*spontaneous evolution towards critical state*
- *No «fine tuning»*
- *Fractal structure, scale-free:*  
*power-law behaviour*
- *Cellular automaton*
  - *Abelian properties*



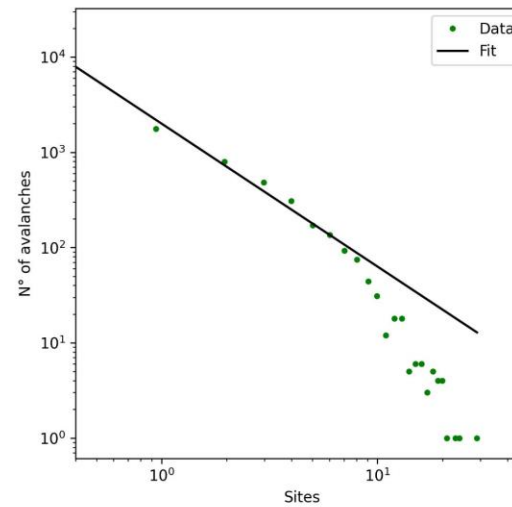
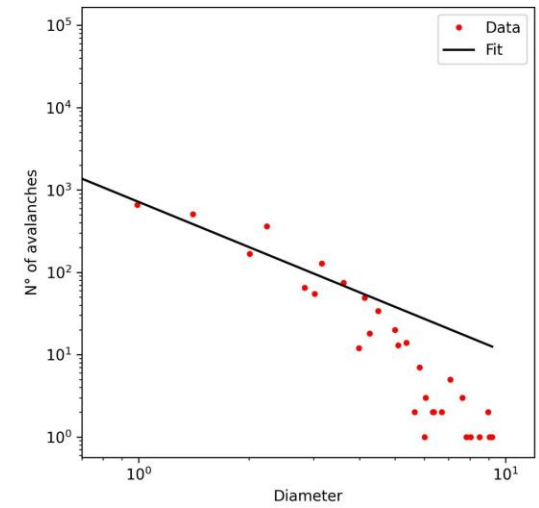
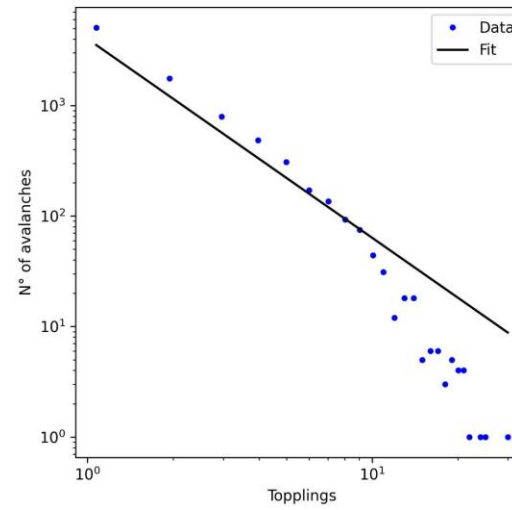
# SIMULATION

- *Numpy*
- *Matplotlib*



# ANALYSIS

## ■ *LMFit*





# REFERENCES

- D. Dhar. *The Abelian Sandpile and Related Models*, Physica A (1999)
- D.Dhar, *Theoretical studies of self-organized criticality*, Physica A (2006)
- M.E.J. Newman. *Power laws, Pareto distributions and Zipf's law*, Contemporary Physics (2005)
- V.Frette, K.Christensen, A.Malthe-Sørensen, J. Feder, T. Jøssang & P. Meakin. *Avalanche dynamics in a pile of rice*, Nature (1996)
- E.V. Ivashkevich, V.B. Priezzhev. *Introduction to the sandpile model*, Physica A (1998)
  - P.Bak, C.Tang, K.Wiesenfeld. *Self-organized criticality*, Physical Review A (1988)
    - P.Bak, C.Tang, K.Wiesenfeld. *Self-Organized Criticality: An Explanation of  $1/f$  Noise*, Physical Review Letters (1987)

