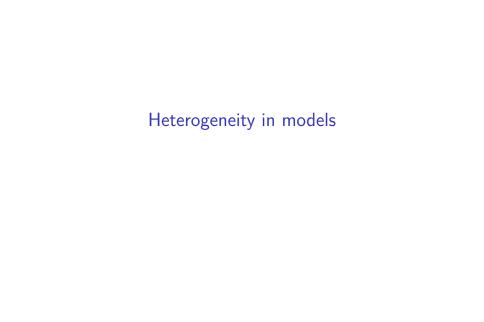
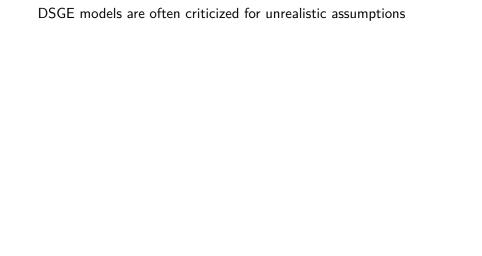
# Intro to Heterogeneity Macro II - Fluctuations - ENSAE, 2023-2024

Pablo Winant

2024-04-03





# DSGE models are often criticized for unrealistic assumptions

#### Example:

- Macroeconomic Policy in DSGE and Agent-Based Models from Revue de l'OFCE
- In that respect, the Great Recessions has revealed to be a natural experiment for economic analysis, showing the inadequacy of the predominant theoretical frameworks. Indeed, an increasing number of leading economists claim that the current ''economic crisis is a crisis for economic theory'' (Kirman, 2010; Colander et al., 2009; Krugman, 2009, 2011; Caballero, 2010; Stiglitz, 2011; Kay, 2011; Dosi, 2011; Delong, 2011). The basic assumptions of mainstream DSGE models, e.g. rational expectations, representative agents, perfect markets etc., prevent the understanding of basic phenomena underlying the current economic crisis

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#### But:

mainstream models typically incorporate many non classical

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<sup>&</sup>lt;sup>1</sup>check Household heterogeneity in macroeconomic models: A historical

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Is it a simplifying assumption?

Or is it actually equivalent to the aggregation of many optimization problems?

For the latter one needs a theory of aggregation<sup>1</sup>

 ... which quickly breaks down (for instance when utility fonction are heterogenous)

¹check Household heterogeneity in macroeconomic models: A historical

# Example with the Neoclassical Model

#### Let's consider three versions of the neoclassical model

- ▶ fully decentralized (many firms, many consumers)
- representative agent
- planner problem

#### Note:

- for the neoclassical model, there is a theory of aggregation for the production sector (firms are Cobb-Douglas)
- two assumptions are needed to aggregate consumers: log-utility and no uncertainty

# Heterogenous Agents

Some economists have recognized early the need to explicitly model heterogeneity.

- ▶ 1977: Bewley
  - idiosyncratic stochastic endowment
  - consumption-savings model with borrowing constraints
  - leads to ex-post heterogeneity (constrained/unconstrained) hence different reactions
- ► Huggett Economy (1993)
  - ▶ additional *ex-ante heterogeneity* in *idiosyncratic* income process
- ► Ayiagari Model (1994)
  - savings are invested to accumulate aggregate capital
  - consumption-savings model with borrowing constraints
  - idiosyncratic productivity shocks (salary)
- ► Krussell Smith Model (1998)
  - ► Ayagari + aggregate shocks

# Mean Field Games and Heterogenous Agents Models **2012** Ben Moll did a talk at IMA (UK)

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... TO HELP ME OUT WITH MY MATH PROBLEMS

**Result**: a new stream of heterogenous agents papers

- PDE Models in Macroeconomics (2014) with Achdou, Bueary, Lasry, Lions
- The Dynamics of Inequality (2016) with Gabaix, Lasry, Lions
- Monetary Policy According to HANK (2018) with Kaplan and Violante
  - that one was hugely successfull

### HANK, HANK HANK, ...

- Monetary Policy According to HANK (2018), by Moll, Kaplan and Violante
  - ► HANK: Heterogenous Agents New Keynesian
  - > study unequal consequences of monetary policies
  - a new baseline model for central banks

<sup>&</sup>lt;sup>2</sup>the ones in the list are not necessary the most representative

<sup>&</sup>lt;sup>3</sup>pseudo representative new-keynesian model

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- ► Stimulated a whole literature<sup>2</sup>
  - Understanding HANK: Insights from a PRANK<sup>3</sup>
  - When HANK meets SAM
  - HANK beyond FIRE
  - Aggregate Demand: THANK (Tractable HANK) and TANK by Florin Bilbiie
    - main point: you don't need more than two agents to get the main insights

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Classically, we make the difference between two kinds of agents:

#### Ricardian Households

Agents who can freely reallocate consumption intertemporally.

They have a high marginal propensity to consume out of additional income.

Ricardian households choose not to consume more today, in order to consume more tomorrow.

#### i Keynesian Households

Agents whose consumption in the current period is limited by a binding credit constraint. Either they can't borrow at all or the amount they can borrow is limited today.

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Let's have a look at the MPC distribution for France.<sup>4</sup>

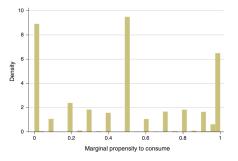


Figure 1: Self-Reported MPC from Transitory Income Shock

<sup>&</sup>lt;sup>4</sup>From From Fiscal Policy and MPC Heterogeneity, Tullio Jappelli and Luigi Pistaferri, American Economic Journal: Macroeconomics, 2014

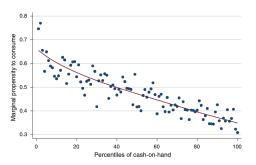


Figure 2: Average MPC by Cash-on-Hand Percentiles

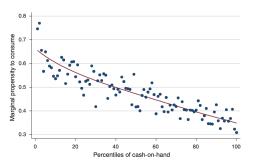


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Apparently MPC is well predicted by Cash-in-hand (amount of money left to household after having made all compulsory payments).

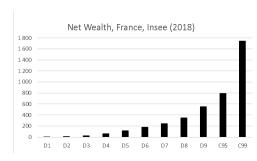


Figure 3: Wealth distribution

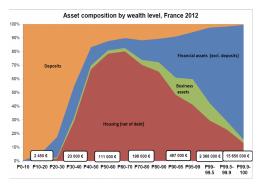


Figure 4: Wealth decomposition

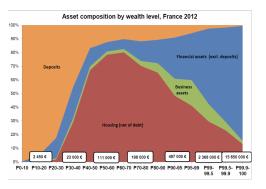


Figure 4: Wealth decomposition

Agents in the middle of the wealth distribution have a mortgage, whose interests leaves very little to spend after payments. They have lower cash-in-hand hence higher marginal propensity to consume (than rich agents).

# Wealthy Hand to Mouth agents

We have just seen that agents in the middle of the wealth distribution, hold a wider proportion of wealth in illiquid assets (housing)

- ► Their cash in hand (available for immediate purchase) is reduced. A sizable fraction of their income goes into repaying their loan...).
- ▶ They have higher MPC
- ▶ They also react to interest rates changes (notably those who have floating interest rates)
- "Monetary Policy According to HANK", 2018, Kaplan, Moll and Violante, stress out the role of "wealthy hand to mouth" and the need to take their existence to evaluate the influence of monetary policies.

► Specify several kinds of agents:

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- By using preference for wealth
  - coming next







Inequality, Leverage and Crisis, Kumhof, Rancière, Winant (2015)

The 2007 financial crisis, was initially as subprime mortgage crisis

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Ok, but from a macro perspective, what fueled such high levels of borrowing?

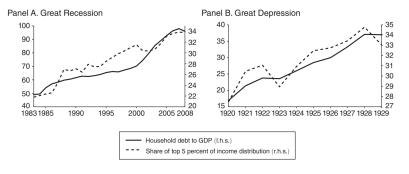


Figure 5: Leverage and Inequality

A similar pattern emerged before the great recession and before the great depression:<sup>5</sup>

parallel increases in income inequality and debt over income ratios

<sup>&</sup>lt;sup>5</sup>inequality data from Saez and Zucman

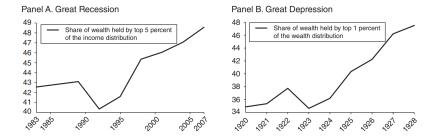
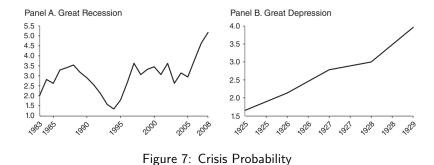


Figure 6: Wealth Inequality

Increase in wealth inequality is consistent.



Econometric measures of household default risk <sup>6</sup> rose consistently.

<sup>&</sup>lt;sup>6</sup>From Schularick and Taylor (2014)

# Model

What could link rising income inequality to increased borrowing by bottom-earners?

#### Intuition:

- top-earners have higher marginal propensity to save
- when their income increases they lend to bottom earners
- and rising debt increases the risk of default

Let's see how to model that in DSGE fashion (ommiting default risk for the sake of simplicity)

#### **Endowments**

We consider and endowment economy:

▶ Total output

$$y_t = (1-\rho_y)\overline{y} + \rho_y y_{t-1} + \epsilon_{y,t}$$

Inequality shock

$$z_t = (1-\rho_z)\overline{z} + \rho_z z_{t-1} + \epsilon_{z,t}$$

#### Comments:

- $\triangleright$   $z_t$  is the fraction of the total output that is received by top-earners. The rest is received by bottom earners.
- $\blacktriangleright$  We assume there is a faction  $\chi$  of top earners.
- $\blacktriangleright$  our goal is to study the effect of a persistent inequality shock (with  $\rho_z=1)$

# Top Earners

We choose the following utility function for top earners:

$$U_t = E_t \sum_{k \geq 0}^{\infty} \beta_{\tau}^k \left\{ \frac{\left(c_{t+k}^{\tau}\right)^{1-\frac{1}{\sigma}}}{1-\frac{1}{\sigma}} + \varphi \frac{\left(1+b_{t+k}\frac{1-\chi}{\chi}\right)^{1-\frac{1}{\eta}}}{1-\frac{1}{\eta}} \right\}$$

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Consumption:

$$c_t^\tau = y_t z_t \frac{1}{\chi} + (b_{t-1} - b_t p_t) \frac{1-\chi}{\chi}$$

where  $\boldsymbol{b}_t$  is debt holdings and  $\boldsymbol{p}_t$  the price of it  $1/r_t$ 

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Optimality condition from  $\max U_t$ 

$$p_t = \beta_\tau E_t \left[ \left( \frac{c_{t+1}^\tau}{c_t^\tau} \right)^{-\frac{1}{\sigma}} \right] + \varphi \frac{\left( 1 + b_t \frac{1-\chi}{\chi} \right)^{-\frac{1}{\eta}}}{\left( c_t^\tau \right)^{-\frac{1}{\sigma}}}$$

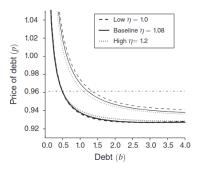
# Preference for Wealth

The preference for wealth can be justified as:

- ▶ a preference for social status
- capitalist spirit

It implies a steady-state supply of lending for any income level:

$$\frac{\beta_b - \beta_\tau}{\varphi} = \frac{\left(\overline{y}\overline{z}\frac{1}{\chi} + \overline{b}(1 - \beta_b)\frac{(1 - \chi)}{\chi}\right)^{\frac{1}{\sigma}}}{\left(1 + \overline{b}\frac{(1 - \chi)}{\chi}\right)^{\frac{1}{\eta}}}$$



Which in turn implies non-zero marginal propensity to save from a permanent income shock (in the short and the long run)

Parameters  $\eta$  and  $\varphi$  are not observed, but can be chosen in order

# **Bottom Earners**

Bottom earners are standard:

$$V_t = E_t \sum_{k \ge 0}^{\infty} \beta_b^k \left( \frac{\left(c_{t+k}^b\right)^{1 - \frac{1}{\sigma}}}{1 - \frac{1}{\sigma}} \right)$$

Budget constraint:

$$c_t^b = y_t(1 - z_t) \frac{1}{1 - \gamma} + (b_t p_t - b_{t-1})$$

Optimality condition from  $\max V_t$ 

$$p_t = \beta^b E_t \left[ \left( \frac{c_{t+1}^b}{c_t^b} \right)^{-\frac{1}{\sigma}} \right]$$

|   | Source/target              | Implied values               |
|---|----------------------------|------------------------------|
| Panel A. Directly calibrated parameters                   |                            |                              |
| Steady-state output level                                 | Normalization              | $\overline{y} = 1$           |
| Population share of top earners                           | 5 percent                  | $\chi = 0.05$                |
| Steady-state real interest rate                           | Literature                 | $\beta_b = 1.04^{-1}$        |
| Ies in consumption  | Literature                 | $\sigma = 0.5$               |
| Panel B. Indirectly calibrated parameters                 |                            |                              |
| Top earners' weight on wealth in utility                  | MPS of top earners         | $\varphi = 0.05$             |
| Top earners' wealth elasticity                            | MPS of top earners         | $\eta = 1.09$                |
| Steady-state top 5 percent income share $\overline{\tau}$ | Data: 21.8 percent in 1983 | $\frac{\dot{z}}{z} = 0.1807$ |
| Steady-state debt-to-income ratio $\overline{\lambda}$    | Data: 62.3 percent in 1983 | $\beta_{\tau} = 0.912$       |
| Panel C. Exogenous stochastic processes                   |                            |                              |
| Output  | Estimated                  | $\rho_{\rm y} = 0.669$       |
|   |                            | $\sigma_{\rm v} = 0.012$     |
| Output shares   | Estimated                  | $\rho_z = 1$                 |
|   |                            | $\sigma_z = 0.008$           |

Figure 8: Calibration

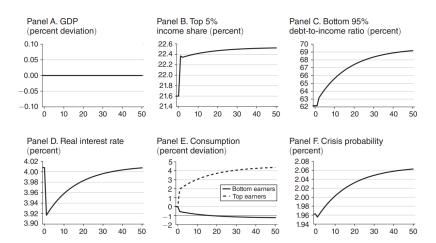


Figure 9: Inequality Shock

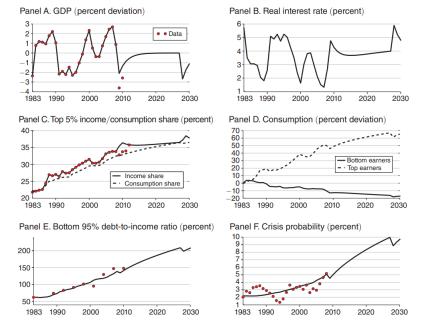


Figure 10: Pseudo-Historical Simulation

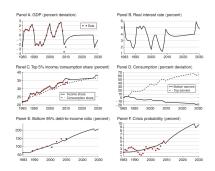


Figure 11: Pseudo-Historical Simulation

In the simulation we use historical values for the driving shocks (output and inequality). What is the predictive power of the model:

we match *one* moment: the evolution of debt/gdep from 1983 to 2010