

Please write clearly in block capitals.

Centre number

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I declare this is my own work.

# INTERNATIONAL A-LEVEL MATHEMATICS

(9660/MA03) Unit P2 Pure Mathematics

Thursday 14 January 2021 07:00 GMT Time allowed: 2 hours 30 minutes

## Materials

- For this paper you must have the Oxford International AQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphical calculator.

## Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 120

## Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
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10	
11	
12	
13	
<b>TOTAL</b>	



J A N 2 1 M A 0 3 0 1

Answer **all** questions in the spaces provided.

- 1** The functions  $f$  and  $g$  are defined with their respective domains by

$$f(x) = x - 5 \quad \text{for all real values of } x$$

$$g(x) = \frac{25}{x+4} \quad \text{for all real values of } x, \quad x \neq -4$$

The composite function  $fg$  is denoted by  $h$

- 1 (a)** Find  $h(x)$  giving your answer as a single fraction.

**[2 marks]**

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Answer \_\_\_\_\_



**[3 marks]**

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**[1 mark]**

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Answer \_\_\_\_\_

2 The line  $l_1$  has equation  $\mathbf{r} = \begin{bmatrix} 4 \\ -2 \\ -3 \end{bmatrix} + \lambda \begin{bmatrix} -1 \\ 5 \\ 2 \end{bmatrix}$

The line  $l_2$  has equation  $\mathbf{r} = \begin{bmatrix} -1 \\ 5 \\ 11 \end{bmatrix} + \mu \begin{bmatrix} -1 \\ -4 \\ c \end{bmatrix}$

2 (a) In the case where  $l_1$  and  $l_2$  intersect, find

2 (a) (i) the value of  $c$

[3 marks]

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Answer \_\_\_\_\_

2 (a) (ii) the coordinates of the point of intersection.

[1 mark]

Answer \_\_\_\_\_

2 (b) In the case where  $l_1$  and  $l_2$  are perpendicular, find the value of  $c$

[3 marks]

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Answer \_\_\_\_\_



**3** It is given that  $y = 3\sin\theta - 3\cos\theta$

**3 (a)** Express  $y$  in the form  $R\sin(\theta - \alpha)$  where  $R$  is a surd and  $0^\circ < \alpha < 90^\circ$

**[2 marks]**

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Answer \_\_\_\_\_

**3 (b)** Hence find

**3 (b) (i)** the greatest value of  $y^2$

**[1 mark]**

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Answer \_\_\_\_\_

**3 (b) (ii)** the least value of  $y^2$

**[1 mark]**

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Answer \_\_\_\_\_

**3 (b) (iii)** the values of  $\theta$  in the interval  $-90^\circ < \theta < 90^\circ$  for which  $y = -\frac{3\sqrt{6}}{2}$

**[3 marks]**

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Answer \_\_\_\_\_



- 4 (a)** Describe a sequence of **two** geometrical transformations that maps the graph of  $y = \cos x$  onto the graph of  $y = 1 + 2\cos x$

[4 marks]

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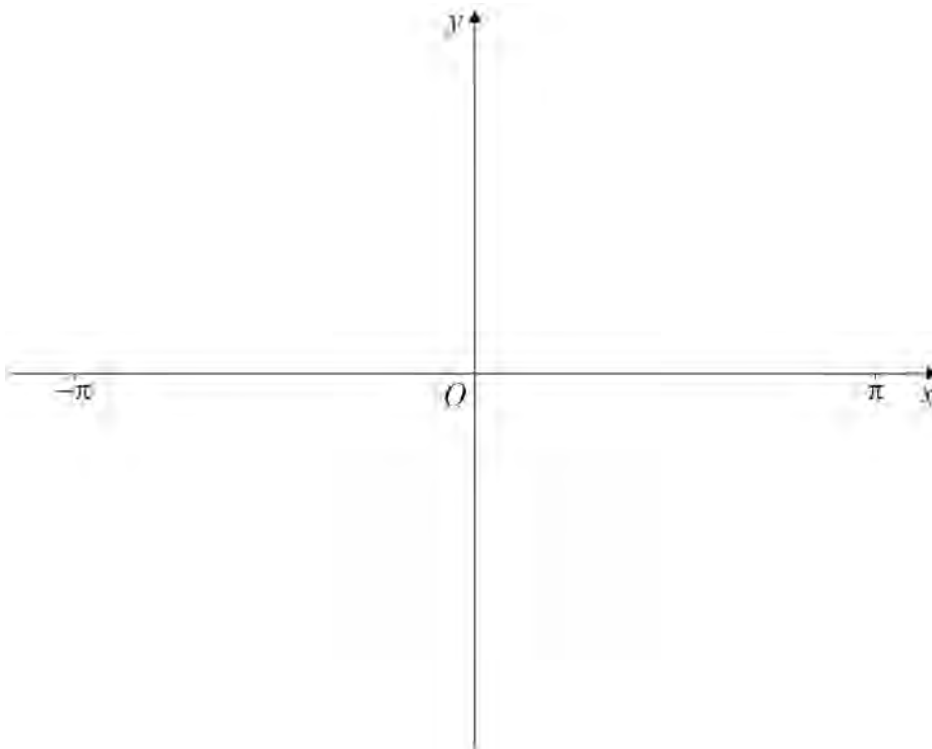
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- 4 (b)** Sketch the graph of the curve with equation

$$y = 1 + 2\cos x \quad \text{for} \quad -\pi < x < \pi$$

indicating the value of  $y$  where the curve crosses the  $y$ -axis.

[2 marks]



- [6 marks]**

[illegible]

Answer \_\_\_\_\_



**[2 marks]**

$$\int_0^{0.5} \sqrt{(1+x^2)} \, dx$$

**[4 marks]**

Answer





$$\int_0^{0.5} \sqrt{(1+x^2)} \, dx$$

**[4 marks]**

[illegible]

Answer

10

**Turn over ►**



**6** It is given that  $\alpha + \beta = 45^\circ$  where  $\alpha$  and  $\beta$  are both positive.

**6 (a)** Find  $\tan \beta$  in terms of  $\tan \alpha$

**[2 marks]**

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Answer \_\_\_\_\_

**6 (b)** Show that  $(1 + \tan \alpha)(1 + \tan \beta) = 2$

**[2 marks]**

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**6 (c)** Find the exact value of  $\tan 22.5^\circ$

**[3 marks]**

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Answer \_\_\_\_\_

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7

**Turn over for the next question**

**Turn over ►**



The curve intersects the line  $y = 3 - 4x$  at a single point where  $x = \alpha$

**[2 marks]**

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$$x_{n+1} = \frac{3 - \sin(\ln(2x_n))}{4}$$

Give your answers to three decimal places.

**[2 marks]**

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$$x_2 = \quad \quad \quad x_3 =$$

Find the coordinates of a stationary point of the curve.

**[3 marks]**

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Answer



Show that  $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = 0$

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8 (a) Given that  $\cot x = \frac{\cos x}{\sin x}$ , use the quotient rule to show that

$$\frac{d}{dx}(\cot x) = -\operatorname{cosec}^2 x$$

[2 marks]

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**8 (b) (i)** Find  $\frac{dx}{dy}$  giving your answer in terms of  $y$

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Answer

**[3 marks]**

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Answer



9 (a) Given that  $x^3 + y^3 = 3xy$  show that  $\frac{dy}{dx} = \frac{y - x^2}{y^2 - x}$

[2 marks]

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9 (b) A curve has the equation  $x^3 + y^3 = 3xy$

9 (b) (i) Find the coordinates of the stationary point of the curve in the interval  $0 < x < 2^{\frac{2}{3}}$

Give your answer in exact form.

[3 marks]

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Answer \_\_\_\_\_





**[4 marks]**

[illegible]

Answer \_\_\_\_\_

9



When  $t = 5$  the temperature of the object is  $70^\circ\text{C}$

**[1 mark]**

**10 (b)** Find the temperature of the object when  $t = 15$  giving your answer to one decimal place  
[6 marks]



**10 (c)** Find the value of  $t$  when the temperature of the object is  $40^{\circ}\text{C}$  giving your answer to one decimal place.

Answer \_\_\_\_\_

9

**11 (a)** Find the exact value of  $\int_0^6 x e^{-0.5x} dx$

**[5 marks]**

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Answer \_\_\_\_\_

**11 (b)** Use the substitution  $u^2 = x+1$  to find

$$\int_8^{15} \frac{\sqrt{x+1}}{x-3} dx$$

giving your answer in the form  $a \ln b$  where  $a$  and  $b$  are constants.

**[9 marks]**

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Answer \_\_\_\_\_

**[4 marks]**

[illegible]

Answer

**[2 marks]**

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Answer



**12 (c)**

for small values of  $x$ , stating the rational values of  $D$ ,  $E$  and  $F$

**[4 marks]**

[illegible]

10

**Turn over ►**



13

$$x = ct, \quad y = \frac{c}{t} \quad \text{where } t > 0 \text{ and } c \text{ is a constant.}$$

The tangent at the point  $P\left(cp, \frac{c}{p}\right)$  on the curve meets the  $x$ -axis at  $A$  and the  $y$ -axis at  $B$

The normal at the point  $P$  meets the line  $y = x$  at  $C$  and the line  $y = -x$  at  $D$

**13 (a)**

**[1 mark]**

Answer

**13 (b)**

**[7 marks]**





**[3 marks]**

11



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ANSWER IN THE SPACES PROVIDED**



[illegible]

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