

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname _____

Forename(s) _____

Candidate signature _____

I declare this is my own work.

INTERNATIONAL AS FURTHER MATHEMATICS

(9665/FM01) Unit FP1 Pure Mathematics

Monday 8 May 2023

07:00 GMT

Time allowed: 1 hour 30 minutes

Materials

- For this paper you must have the Oxford International AQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphical calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
TOTAL	



J U N 2 3 F M 0 1 0 1

1

[6 marks]

[illegible]

Answer

6



2

$$I = \int_4^{\infty} x^{-3} \, dx$$

2 (a)

[1 mark]

2 (b)

[3 marks]

[illegible]

Answer

3 (a) Show that

$$(x+1)^3 - (x-1)^3 = 6x^2 + 2$$

[1 mark]

3 (b) Use the method of differences to show that

$$\sum_{r=15}^n (6r^2 + 2) = n^3 + (n+1)^3 - k$$

where k is a constant.

[4 marks]



- 4 (a)** Find the general solution of the equation

$$\sin\left(\frac{x}{3} + \frac{\pi}{6}\right) = -\frac{\sqrt{2}}{2}$$

Give your answer in terms of π

[4 marks]

Answer _____

- 4 (b)** Find the sum of the four smallest positive solutions of the equation

$$\sin\left(\frac{x}{3} + \frac{\pi}{6}\right) = -\frac{\sqrt{2}}{2}$$

Give your answer in terms of π

[3 marks]

Answer _____



5

$$z^2 - az + (b + i) = 0$$

where a and b are real constants, has two complex roots.

One of the roots of the equation is $2 + i$

Find the other root of the equation.

[5 marks]

[illegible]

Answer _____

5



A curve has equation $y = px^2 - 3x$ where p is a constant.

A line passes through two points on the curve, one where $x = 7$ and the other where $x = 7 + h$

Find the gradient of this line in terms of p and h

Give your answer in its simplest form.

[3 marks]

[illegible]

Answer _____

6 (b) The curve has a stationary point at the point where $x = 7$

Use your answer to **part (a)** to find the value of p

[2 marks]

Answer

5



7 The quadratic equation

$$3x^2 - 2x + 9 = 0$$

has roots α and β

7 (a) Write down the value of $\alpha + \beta$ and the value of $\alpha\beta$

[2 marks]

$$\alpha + \beta = \underline{\hspace{2cm}} \quad \alpha\beta = \underline{\hspace{2cm}}$$

7 (b) Hence show that $\alpha^2 + \beta^2 = -\frac{50}{9}$

[2 marks]



[4 marks]

[illegible]

Answer

8



IB/G/Jun23/FM01

8 The function f is defined by

$$f(x) = \frac{x^2}{(x-1)(x+2)}$$

8 (a) Write down the equations of the asymptotes of the graph of $y = f(x)$

[2 marks]

Answer _____

8 (b) It is given that the line $y = k$, where k is a constant, intersects the graph of $y = f(x)$
Find the set of possible values of k

[3 marks]

Answer _____

8 (c) Hence find the coordinates of the stationary points of the graph of $y = f(x)$

[3 marks]

Answer _____

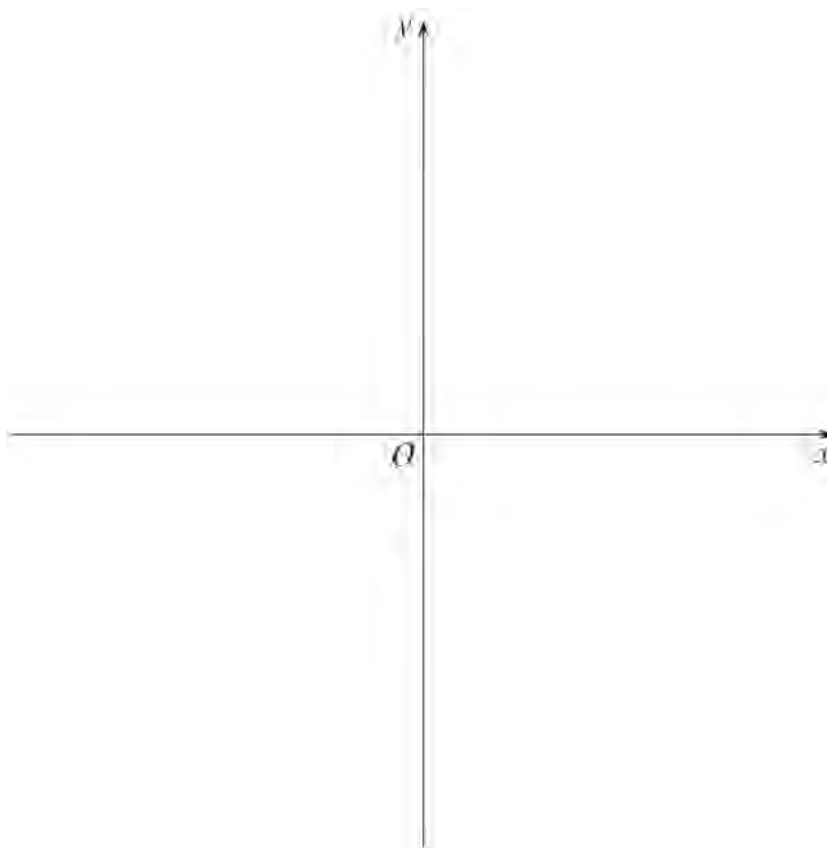


- 8 (d)** Show that the graph of $y = f(x)$ intersects its horizontal asymptote at one point.
Find the coordinates of this point.

[2 marks]

Answer _____

- 8 (e)** Sketch the graph of $y = f(x)$ on the axes below.
Show the coordinates of the stationary points
Show the coordinates of the point of intersection of the graph with its horizontal asymptote.

[3 marks]

$$\sum_{r=1}^n (r^3 + r^2) = \frac{1}{12} n(n+a)(n+b)(cn+a)$$

[4 marks]

[illegible]

[3 marks]

[illegible]

7

Turn over ►



- 10** The locus of a point P is such that the distance from P to the point $(1, 0)$ is equal to **half** the distance from P to the line $x = 4$

The locus of P is the curve E

- 10 (a)** Show that the equation of E is

$$\frac{x^2}{4} + \frac{y^2}{3} = 1$$

[3 marks]

- 10 (b)** The rectangular hyperbola H has equation

$$xy = \sqrt{3}$$

Find the coordinates of the two points of intersection of H and E

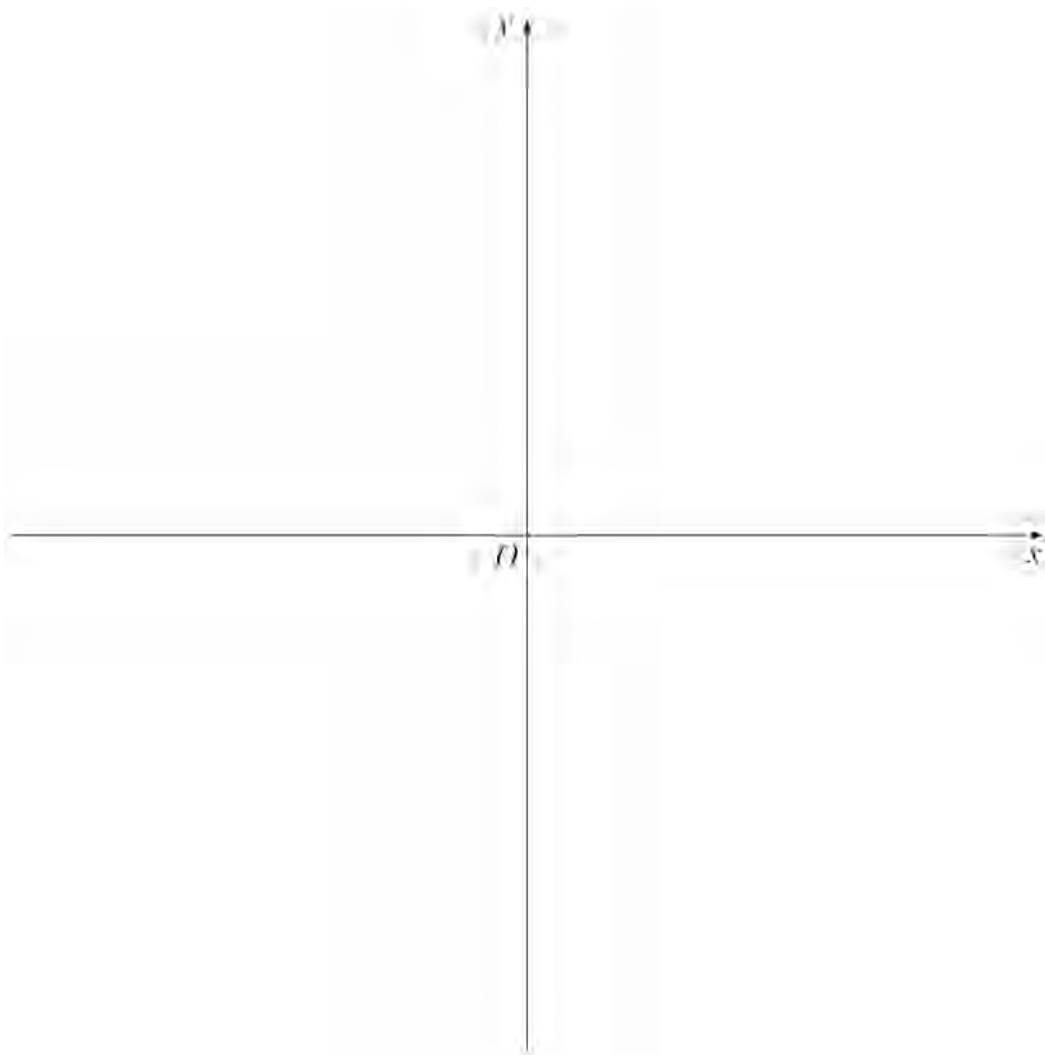
[4 marks]



Answer _____

10 (c) Sketch H and E on the axes below, showing all significant features.

[4 marks]



- 11** The circle C is the locus of points on an Argand diagram such that

$$|z - 3| = 2$$

The point Q is the centre of C

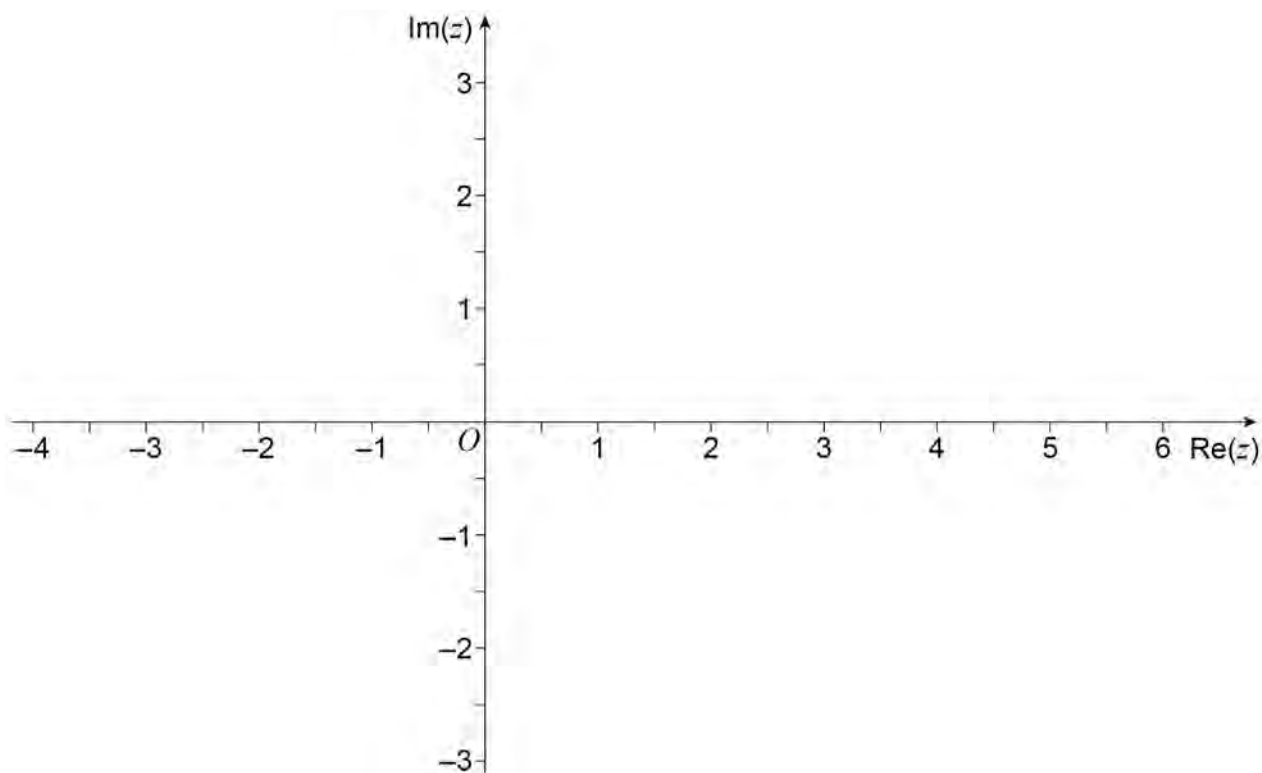
The line L is the locus of points on an Argand diagram such that

$$|z - 3| = |z + 3 - 3i|$$

The point P is the point on L which is closest to C

- 11 (a)** On the Argand diagram, draw C and L , and mark the points P and Q

[4 marks]



Find the exact area of the quadrilateral $PTQS$

[illegible]

Answer _____

9



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outside the
box*

**DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED**



[illegible]

Question number	<p style="text-align: center;">Additional page, if required. Write the question numbers in the left-hand margin.</p>
	<div style="border: 1px solid black; height: 550px; width: 100%;"></div>
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