

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

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Forename(s)

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Candidate signature

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I declare this is my own work.

INTERNATIONAL A-LEVEL MATHEMATICS

(9660/MA03) Unit P2 Pure Mathematics

Time allowed: 2 hours 30 minutes

Materials

- For this paper you must have the Oxford International AQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphic calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 120.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working: otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
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4	
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6	
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8	
9	
10	
11	
12	
13	
TOTAL	



J U N 2 2 M A 0 3 0 1

1 (a) Use the mid-ordinate rule with 4 strips to find an estimate for

$$\int_0^{0.8} \sin(e^x) dx$$

[4 marks]

[illegible]

Answer _____



1 (b) A curve has equation $y = \sin(e^x)$

The curve intersects the line $y = 3x - 2$ at a single point where $x = \alpha$

1 (b) (i) Show that α lies between 0.8 and 0.9

[2 marks]

1 (b) (ii) The equation $\sin(e^x) = 3x - 2$ can be rearranged into the form $x = \frac{\sin(e^x) + 2}{3}$

Use the iterative formula

$$x_{n+1} = \frac{\sin(e^{x_n}) + 2}{3}$$

with $x_1 = 0.8$ to find the values of x_2 and x_3

Give your answers to three decimal places.

[2 marks]

$x_2 =$ _____ $x_3 =$ _____



- 2 (a)** Given that $y = \frac{1-3x}{2x+5}$ show that $\frac{dy}{dx} = \frac{k}{(2x+5)^2}$ where k is a constant.

[2 marks]

- 2 (b)** Given that $y = \ln\left(\frac{1-3x}{2x+5}\right)$ find $\frac{dy}{dx}$

[2 marks]

Answer _____



[illegible]

5

4

where b and c are constants.

When $f(x)$ is divided by $(3x-1)$ the remainder is -5

[4 marks]

[illegible]
$$\mathcal{C} =$$


4 (a) (ii) Show that

$$f(x) = (2x+1)(px+q)(px-q)$$

where p and q are constants.

[2 marks]

4 (b) Hence show that

$$\frac{f(x)}{(3x+2)(x^2-2)} = k + \frac{g(x)}{x^2-2}$$

where k is a constant and g is a linear function.

[2 marks]

Turn over ►



[5 marks]

[illegible]

Answer _____



$$\frac{\sin 4x(1 - \cos 2x)}{\cos 2x(1 - \cos 4x)} = \tan x$$

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9

Turn over ►



- 6 (a)** Find the binomial expansion of $(1-x)^{-\frac{1}{3}}$ up to and including the term in x^3

[3 marks]

Answer _____

- 6 (b) (i)** Find the binomial expansion of $\frac{1}{\sqrt[3]{1-2x}}$ up to and including the term in x^3

[2 marks]

Answer _____



[2 marks]

Answer

[3 marks]

Answer

10

Turn over ►



[4 marks]

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7 (b) The function f is defined by

$$f(x) = \frac{1 + \cos x}{3} \quad \text{for } 0 \leq x \leq \pi$$

Find an expression for $f^{-1}(x)$

[2 marks]

Answer _____

6

Turn over for the next question

Turn over ►



$$\frac{6}{x^3 + x} = \frac{a}{x} + \frac{bx}{x^2 + 1}$$

[2 marks]

$$\int_1^2 \frac{6}{x^3 + x} dx = \ln k$$

[4 marks]



[2 marks]

$$\int_0^{0.5} \frac{u}{\sqrt{(1-u^2)^3}} du$$

[5 marks]

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Answer



- 9 (a) Express $\frac{1}{(30-x)(10-x)}$ in partial fractions.

[2 marks]

Answer _____

- 9 (b) A chemical experiment produces a substance.

The mass of the substance is x grams after time t minutes.

The mass of the substance increases at a rate directly proportional to $(30-x)(10-x)$

When $t = 0$, $x = 0$

When $t = 2$, $x = 6$

Find an expression for x in terms of t

[9 marks]



[illegible]

Answer _____

11

Turn over ►



10 (a) Show that $\frac{dy}{dx} = -\cot t$

[illegible]

Answer



The normal to the curve at P intersects the x -axis at the point A and intersects the y -axis at the point B

[6 marks]

[illegible]

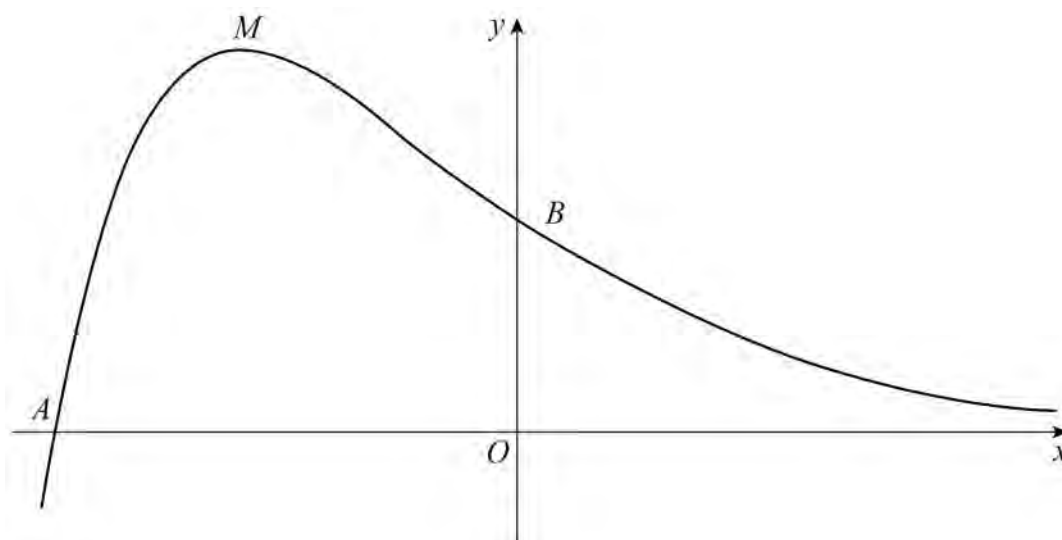
Answer _____

12



11

The diagram shows a sketch of the curve with equation $y = (5 + 2x)e^{-x}$



The curve crosses the axes at A and B and has a stationary point at M

11 (a) Find the coordinates of A and the coordinates of B

[1 mark]

Answer _____

11 (b) The curve $y = (5 + 2x)e^{-x}$ has a stationary point at M

11 (b) (i) Find $\frac{dy}{dx}$

[2 marks]

Answer _____



[2 marks]

Answer

[2 marks]

[6 marks]

[illegible]

Answer _____

A curve has equation $y = x \ln(x + y)$

$$\frac{dy}{dx} = \frac{x}{y} + \frac{y}{x} + 1$$

[6 marks]

[illegible]

Answer _____

6

Turn over ►



- 13 (a)** The point A has coordinates $(2, -3, 7)$. The point B has coordinates $(16, -1, -1)$.

Find the distance AB

[2 marks]

Answer _____

- 13 (b)** The line l has equation $\mathbf{r} = \begin{bmatrix} 9 \\ -2 \\ q \end{bmatrix} + \mu \begin{bmatrix} 5 \\ -4 \\ 5 \end{bmatrix}$

- 13 (b) (i)** The line l intersects the line AB

Find the value of q , where q is an integer.

[3 marks]

Answer _____



- 13 (b) (ii)** Find the acute angle between the line l and the line AB , giving your answer in degrees to three significant figures.

[4 marks]

Answer _____

- 13 (c)** The point D has coordinates $(-1, 2, 3)$.

The perpendicular from D to the line l meets l at the point C

Show that ABC is a right-angled triangle.

[6 marks]

Turn over ►



15

END OF QUESTIONS



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