

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

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Forename(s)

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Candidate signature

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# INTERNATIONAL A-LEVEL MATHEMATICS

(9660/MA03) Unit P2 – Pure Mathematics

Wednesday 29 May 2019 07:00 GMT Time allowed: 2 hours 30 minutes

## Materials

- For this paper you must have the Oxford International AQA booklet of formulae and statistical tables (enclosed).
- You may use a graphics calculator.

## Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 120.

## Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks for method may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
<b>TOTAL</b>	



Answer **all** questions in the spaces provided.

- 1 (a)** Use Simpson's rule with 7 ordinates (6 strips), to find an estimate for  $\int_0^3 3^x dx$ , giving your answer to 3 decimal places.

**[4 marks]**

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Answer \_\_\_\_\_

- 1 (b)** A curve is defined by the equation  $y = 3^x$   
The curve intersects the line  $y = 12 - 4x$  at a single point where  $x = \alpha$

- 1 (b) (i)** Show that  $\alpha$  lies between 1.5 and 1.6

**[2 marks]**

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- 1 (b) (ii) The equation  $3^x = 12 - 4x$  can be rearranged into the form  $x = \frac{\ln(12 - 4x)}{\ln 3}$

Use the iterative formula

$$x_{n+1} = \frac{\ln(12 - 4x_n)}{\ln 3}$$

with  $x_1 = 1.5$  to find the values of  $x_2$  and  $x_3$ , giving your answers to 3 decimal places.

[2 marks]

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$$x_2 = \underline{\hspace{2cm}} \quad x_3 = \underline{\hspace{2cm}}$$

8

Turn over for the next question

Turn over ►



**2 (a)** The number of fish in Lake  $P$  decreases by 3% each year.

On 1 January 2019 there are 50 000 fish in this lake.

Calculate, to the nearest 100, the number of fish in this lake on

**2 (a) (i)** 1 January 2020,

**[1 mark]**

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Answer \_\_\_\_\_

**2 (a) (ii)** 1 January 2029,

**[2 marks]**

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Answer \_\_\_\_\_

**2 (a) (iii)** 1 January 2009.

**[2 marks]**

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Answer \_\_\_\_\_



**[4 marks]**

[illegible]

9



**3 (a)**

$$f(x) = 4x^3 + bx^2 + cx + 6$$

where  $b$  and  $c$  are constants.

When  $f(x)$  is divided by  $(2x - 3)$  the remainder is  $-6$

When  $f(x)$  is divided by  $(2x + 1)$  the remainder is 10

Find the value of  $b$  and the value of  $c$ .

**[4 marks]**

[illegible]

$$b = \underline{\hspace{2cm}} \qquad c = \underline{\hspace{2cm}}$$



**[4 marks]**

[illegible]

Answer \_\_\_\_\_

3

**Turn over ►**



- 4 (a) (i)** Express  $3 \cos \theta - 4 \sin \theta$  in the form  $R \cos (\theta + \alpha)$ , where  $R > 0$  and  $0 < \alpha < \frac{\pi}{2}$ , giving the value of  $\alpha$ , in radians, to 3 significant figures.

**[3 marks]**


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Answer \_\_\_\_\_

- 4 (a) (ii)** Hence solve the equation

$$3 \cos (y - 0.1) - 4 \sin (y - 0.1) = 2.5$$

giving all values of  $y$ , to 2 decimal places, in the interval  $-\pi < y < \pi$

**[3 marks]**


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Answer \_\_\_\_\_





**[5 marks]**

[illegible]

Answer

**[2 marks]**

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Answer \_\_\_\_\_

Express your answer in the form  $\frac{dy}{dx} = y f(x)$

**[3 marks]**

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Answer



$$2xy + y^2 = \frac{1}{x}$$

Find the coordinates of the stationary point of the curve.

[illegible]

Answer \_\_\_\_\_

**[3 marks]**

[illegible]

**[3 marks]**

[illegible]

Answer \_\_\_\_\_



**[2 marks]**

**[7 marks]**

Answer



$$x = \frac{1}{t+1} \quad \text{and} \quad y = 3t - t^2$$

**[5 marks]**

[illegible]

Answer



**[4 marks]**

[illegible]

Answer \_\_\_\_\_

9

**Turn over ►**



- 9 The function  $f$  is defined by

$$f(x) = |x^2 - 5| - 3 \quad \text{for } -5 \leq x \leq 5$$

- 9 (a) (i) Write down the range of  $f$ .

[1 mark]

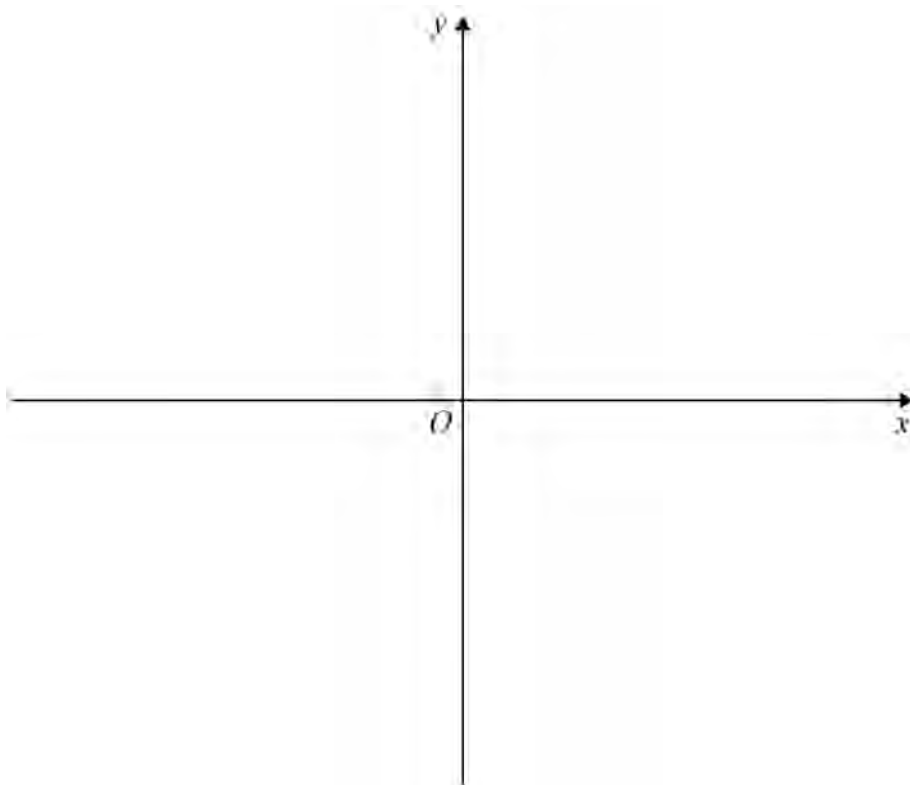
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Answer \_\_\_\_\_

- 9 (a) (ii) Sketch the graph of  $y = f(x)$ , indicating the value where the curve crosses the  $y$ -axis.

[3 marks]





**9 (a) (iii)** Solve  $f(x) = 1$

**[3 marks]**

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Answer \_\_\_\_\_

**9 (b)** The function  $g$  is defined by

$$g(x) = \frac{1}{x} \quad \text{where } x \neq 0$$

**9 (b) (i)** Find an expression for  $fg(x)$ .

**[1 mark]**

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Answer \_\_\_\_\_

**9 (b) (ii)** Solve  $fg(x) < 0$

**[3 marks]**

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Answer \_\_\_\_\_



10

$$\frac{dy}{dx} = \frac{y}{\sqrt{2x-1}} \quad \text{where } x > 0.5$$

**10 (a)**

**[4 marks]**

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Answer \_\_\_\_\_

**10 (b)**

**[2 marks]**

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Answer

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**[5 marks]**

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Answer

**[1 mark]**

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Answer



**11 (c)**

for small values of  $x$ , stating the values of  $D$ ,  $E$  and  $F$ .

**[6 marks]**

[illegible]

Answer

12

**Turn over ►**



The region bounded by the curve  $y = xe^{-1.5x}$ , the line  $x = 1$  and the  $x$ -axis from  $x = 0$  to  $x = 1$ , is rotated through  $2\pi$  radians about the  $x$ -axis to form a solid.

Use integration by parts twice to find the exact value of the volume of the solid generated, giving your answer in the form  $\pi (p + q e^{-3})$ , where  $p$  and  $q$  are rational.

[illegible]

[illegible]

Answer \_\_\_\_\_

7

**13** The line  $l_1$  has equation  $\mathbf{r} = \begin{bmatrix} -4 \\ 1 \\ -5 \end{bmatrix} + \lambda \begin{bmatrix} -3 \\ -4 \\ -5 \end{bmatrix}$

and the line  $l_2$  has equation  $\mathbf{r} = \begin{bmatrix} 6 \\ 10 \\ c \end{bmatrix} + \mu \begin{bmatrix} 4 \\ 1 \\ 1 \end{bmatrix}$

- 13 (a)** Given that the two lines intersect, find the value of  $c$  and the coordinates of the point of intersection.

**[4 marks]**

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$c =$  \_\_\_\_\_ and ( \_\_\_\_\_ , \_\_\_\_\_ )

- 13 (b)** Find the cosine of the acute angle between the two lines.

**[4 marks]**

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Answer \_\_\_\_\_





Find the coordinates of  $B$ .

**[5 marks]**

[illegible]

Answer

**END OF QUESTIONS**

13



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[illegible]

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