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Candidate number

Surname

Forename(s)

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I declare this is my own work.

INTERNATIONAL A-LEVEL

MATHEMATICS

(9660/MA04) Unit S2 Statistics

Tuesday 16 January 2024

07:00 GMT

Time allowed: 1 hour 30 minutes

Materials

- For this paper you must have the OxfordAQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphical calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



Answer **all** questions in the spaces provided.

- 1** The probability density function f for a continuous random variable X is given by

$$f(x) = \begin{cases} \frac{1}{7}e^{-\frac{1}{7}x} & x \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

- 1 (a)** State the name of the distribution of X

[1 mark]

Answer _____

- 1 (b)** Find the mean of X

[1 mark]

Answer _____

- 1 (c)** Find $P(2 < X < 7)$

Give your answer to four significant figures.

[2 marks]

Answer _____



1 (d) It is given that $P(X < a) = 0.8$

Find the value of a

Give your answer to four significant figures.

[2 marks]

Answer _____

1 (e) Find $P(X > 8 \mid X > 5)$

Give your answer to four significant figures.

[2 marks]

Answer _____

<hr/> 8

Turn over for the next question

Turn over ►



Assume that the population standard deviation is unchanged.

[7 marks]

[illegible]

[illegible]

[2 marks]



- 3** The continuous random variable X has probability density function $f(x)$ defined by

$$f(x) = \begin{cases} \frac{1}{8}x^2 & 0 \leq x < 1 \\ k(x-1) + \frac{1}{8} & 1 \leq x \leq 6 \\ 0 & \text{otherwise} \end{cases}$$

where k is a constant.

- 3 (a)** Find $P(X < 1)$

Give your answer in exact form.

[2 marks]

Answer _____

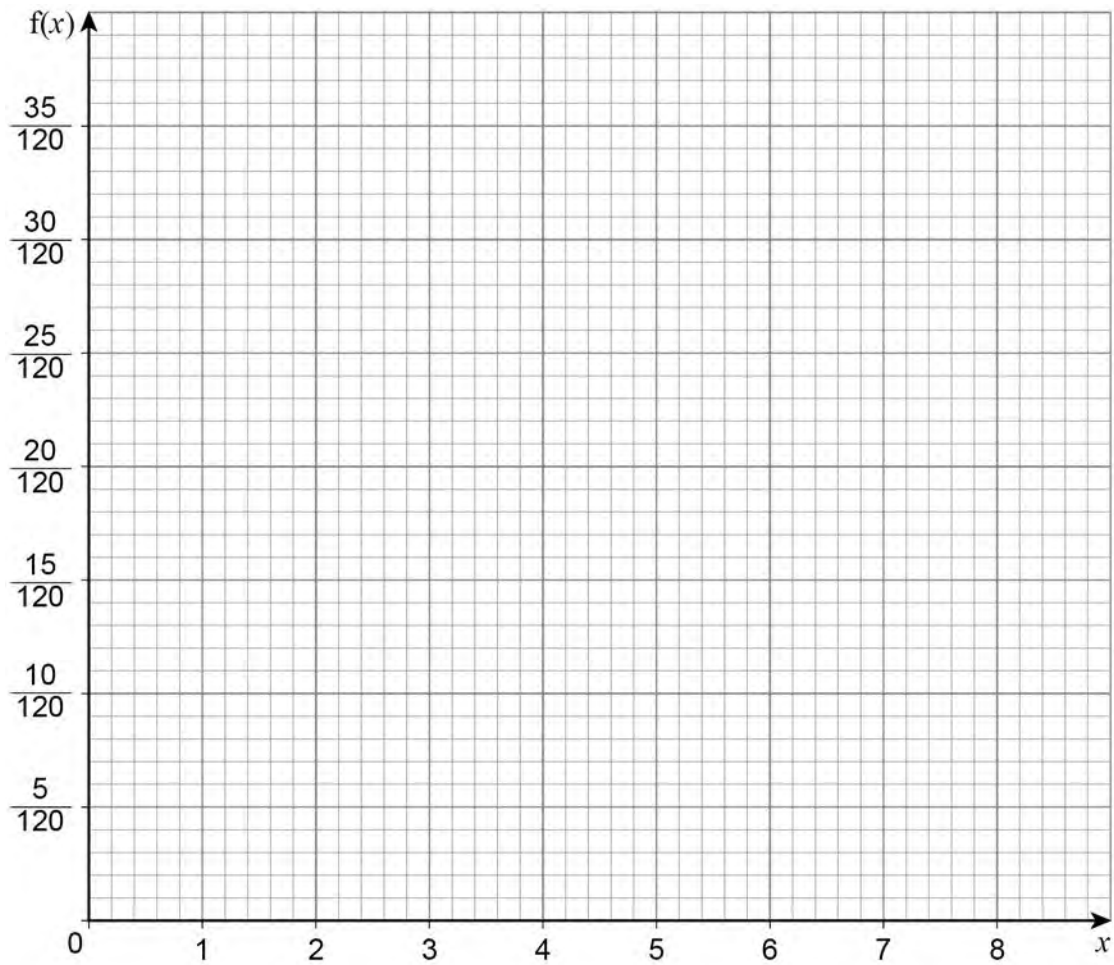
- 3 (b)** Show that $k = \frac{2}{75}$

[3 marks]



3 (c) Draw the graph of $y = f(x)$ for $0 \leq x \leq 8$

[3 marks]



Question 3 continues on the next page

Turn over ►



You are given that $F(x) = 1$ for $x > 6$

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$$F(x) = \begin{cases} 1 & x > 6 \end{cases}$$

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- 4 (a)** The random variables C , D , E and F are all binomially distributed, as shown in the table.

Distribution
$C \sim B(10, 0.04)$
$D \sim B(200, 0.51)$
$E \sim B(400, 0.91)$
$F \sim B(100, 0.05)$

State, with a reason, which one of these distributions would be most suitable to approximate by a Poisson distribution.

[2 marks]

Distribution _____

Reason _____

Question 4 continues on the next page

Turn over ►



- 4 (b)** In any given hour the number of aeroplanes which fly over an island can be modelled as a Poisson distribution with a mean of 1.8

- 4 (b) (i)** Find the probability that exactly 3 aeroplanes fly over the island between 9.00 am and 10.00 am on a randomly selected day.

Give your answer to three significant figures.

[2 marks]

Answer _____

- 4 (b) (ii)** Find the probability that more than 1 and less than 4 aeroplanes fly over the island in a given 20 minute period on a randomly selected day.

Give your answer to three significant figures.

[4 marks]

Answer _____



- 4 (c)** A different Poisson distribution is used to model the number of helicopters flying over the island in any given hour. The mean of this distribution is 2.7

Assume that the number of helicopters and the number of aeroplanes flying over the island in any given hour are independent random variables.

The random variable G represents the total number of helicopters and aeroplanes flying over the island in any given hour.

- 4 (c) (i)** Write down the parameter of G

[1 mark]

Answer

- 4 (c) (ii)** It is given that $P(G < a) > 0.95$ where a is an integer.

By considering probabilities, find the smallest possible value of a

[3 marks]

Answer



$$\sum x = 129.5 \quad \text{and} \quad \sum x^2 = 1677.05$$

- [10 marks]**

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Suggest one possible difference in Benga's hypothesis test.

Turn over ►



- 6** The mass V grams of flour in a bag can be modelled by a normal distribution with mean 502 grams and standard deviation 2.7 grams.

A bakery purchases 30 bags of flour.

The masses of the bags are independent and each bag is selected at random.

- 6 (a)** Find the probability that the mean mass of the 30 bags is less than 501 grams.

Give your answer to four decimal places.

[4 marks]

Answer _____

- 6 (b)** Find the probability that the mass of flour in each of the 30 bags is more than 496 grams.

Give your answer to three decimal places.

[4 marks]

Answer _____



$$F(x) = \begin{cases} 0 & x < 2 \\ \frac{1}{2} - \frac{2}{x^2} & 2 \leq x \leq 4 \\ \frac{1}{96}(x^2 + 3x + 8) & 4 < x \leq 8 \\ 1 & x > 8 \end{cases}$$

[7 marks]

[illegible]

[2 marks]

Answer

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Turn over ►



[6 marks]

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END OF QUESTIONS



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