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# INTERNATIONAL AS MATHEMATICS MA02

(9660/MA02) Unit PSM1 Pure Mathematics, Statistics and Mechanics

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Mark scheme

January 2020

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Version: V1 Final Mark Scheme

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**Key to mark scheme abbreviations**

|                |  |
|----------------|--|
| <b>M</b>       | Mark is for method   |
| <b>m</b>       | Mark is dependent on one or more M marks and is for method         |
| <b>A</b>       | Mark is dependent on M or m marks and is for accuracy              |
| <b>B</b>       | Mark is independent of M or m marks and is for method and accuracy |
| <b>E</b>       | Mark is for explanation  |
| <b>✓ or ft</b> | Follow through from previous incorrect result                      |
| <b>CAO</b>     | Correct answer only  |
| <b>CSO</b>     | Correct solution only  |
| <b>AWFW</b>    | Anything which falls within  |
| <b>AWRT</b>    | Anything which rounds to   |
| <b>ACF</b>     | Any correct form   |
| <b>AG</b>      | Answer given   |
| <b>SC</b>      | Special case   |
| <b>oe</b>      | Or equivalent  |
| <b>A2, 1</b>   | 2 or 1 (or 0) accuracy marks                                       |
| <b>–x EE</b>   | Deduct x marks for each error                                      |
| <b>NMS</b>     | No method shown  |
| <b>PI</b>      | Possibly implied   |
| <b>SCA</b>     | Substantially correct approach                                     |
| <b>sf</b>      | Significant figure(s)  |
| <b>dp</b>      | Decimal place(s)   |

| Q    | Answer   | Marks  | Comments  |
|------|--|--|---|
| 1(a) | $p - q$  | B1   |   |
| 1(b) | $\log_3(5^2 \times 2)$<br>or<br>$\log_3(5 \times 5 \times 2)$<br>$2\log_3 5 + \frac{1}{2}\log_3 4$<br>or<br>$\log_3 5 + \log_3 5 + \frac{1}{2}\log_3 4$<br>$2p + \frac{1}{2}q$ | B1<br><br><br><br><br><br><br>M1<br><br><br><br>A1 | PI<br><br><br><br><br><br>Complete, correct application of log rules. |
|      | Total  | 4  |   |

| Q    | Answer   | Marks                  | Comments   |
|------|--|------------------------|--|
| 2(a) | $\frac{\sin \beta}{4} = \frac{3/7}{6}$ oe<br>and<br>$\sin \beta = 4 \times \frac{3/7}{6}$ oe<br>$\sin \beta = \frac{2}{7}$ | M1<br><br><br><br>A1   | Use of sine rule with values substituted and correct unsimplified rearrangement.<br><br><br>AG |
| 2(b) | $\cos^2 \beta + \sin^2 \beta = 1$<br>$\cos^2 \beta = \frac{45}{49}$<br>$\cos \beta = \frac{3\sqrt{5}}{7}$                  | M1<br><br>m1<br><br>A1 | Stated or used, PI<br><br>Correct substitution and rearrangement<br><br>CSO                    |
|      | Total  | 5                      |  |

| Q     | Answer  | Marks  | Comments  |
|-------|---|--|---|
| 3(a)  | $(\sqrt{17})^2 + (\sqrt{17})^2$<br>$((\sqrt{17})^2 + (\sqrt{17})^2 =) 34$<br>$(x-4)^2 + (y-1)^2 = 34$   | <b>M1</b><br><b>A1</b><br><b>B1</b><br><b>B1ft</b>   | oe<br><br>For correct LHS<br>ft their 34 provided M1 scored.<br>Equation must be in the correct form  |
| 3(b)  | $(x-1)^2 + (y-3)^2 = 34$  | <b>B2ft</b>  | B1 for each correct bracketed term in an equation of the correct form or<br>$(x-7)^2 + (y+1)^2$<br>ft their 34  |
| 3 (c) | $(x-6)^2 - 36 + (y-2)^2 - 4 + 2 = 0$<br>$((x-6)^2 + (y-2)^2 =) 38$<br>The two circles have different radii<br><br>(Hence) Jane is not correct | <b>M1</b><br><b>A1</b><br><b>E1</b><br><br><b>E1</b> | Completes the square twice<br><br>Finding correct radius squared for the circle. PI by correct radius.<br>E1 for comparing radii in the context of the question.<br>E1 for statement on Jane's claim.<br><br>Stating she is not correct and giving a correct reason.<br>No working seen scores E0E0 |
|       | <b>Total</b>  | <b>10</b>  |   |

| Q | Answer  | Marks  | Comments   |
|---|---|--|--|
| 4 | $3.6 = \frac{1}{2} \times r^2 \times 0.8$<br>$r = 3$<br>$OD = 12$<br>$(CD^2 =) 6^2 + 12^2 - 2 \times 6 \times 12 \times \cos 0.8$<br>$(CD^2 =) 79.674233...$<br>$(CD =) 8.93$ | <b>M1</b><br><b>A1</b><br><br><b>B1</b><br><br><b>M1</b><br><br><b>M1</b><br><br><b>A1</b> | oe. Use of $A = \frac{1}{2} r^2 \theta$<br><br><br>PI<br><br>Correct substitution into Cosine Rule<br><br>Correct order of evaluation to find $CD^2$<br><br>AWRT |
|   | <b>Total</b>  | <b>6</b>   |  |

| Q    | Answer  | Marks     | Comments   |
|------|---|-----------|--|
| 5(a) | Exponential curve and increasing function in the first and second quadrants with the correct form, asymptotic to the negative $x$ –axis from above. | <b>B1</b> |  |
|      | 15 marked on $y$ -intercept of curve on positive $y$ –axis.   | <b>B1</b> | Condone correct coordinates  |
| 5(b) | $\log_5(15 \times 7^x) = \log_5 625^{2x}$   | <b>M1</b> | Forms correct equation in $x$ .<br>Condone missing 5 in $\log_5$   |
|      | $\log_5 15 + \log_5 7^x$  | <b>M1</b> | Correct use of $\log(ab) = \log(a) + \log(b)$<br>Condone missing 5 in $\log_5$   |
|      | $x \log_5 7$<br>or<br>$2x \log_5 625$<br>or<br>$8x \log_5 5$<br>or<br>$4x \log_5 25$<br>or<br>$8x$  | <b>M1</b> | Correct use of $\log(a^b) = b \log(a)$ for at least 1 term.<br>Condone missing 5 in $\log_5$                                   |
|      | $1 + \log_5 3 + x \log_5 7 = 8x$  | <b>A1</b> | Completely correct unsimplified linear equation in $x$ with $\log_5 5$ replaced by 1<br>Condone missing 5 in $\log_5$          |
|      | $x(8 - \log_5 7) = 1 + \log_5 3$  | <b>M1</b> | Correct rearrangement of their equation with $x$ factorised out. Must be seen as an equation.<br>Condone missing 5 in $\log_5$ |
|      | $x = \frac{1 + \log_5 3}{8 - \log_5 7}$   | <b>A1</b> | Must see all 5s in $\log_5$  |
|      | <b>Total</b>  | <b>8</b>  |  |

| Q | Answer   | Marks                  | Comments   |
|---|--|------------------------|--|
| 6 | $5\sin x(3\cos x - 2)$<br>or<br>$4(3\cos x - 2)$<br>or<br>$4(2 - 3\cos x)$                   | <b>M1</b>              | Attempt at one factorisation.  |
|   | $5\sin x(3\cos x - 2) = 4(2 - 3\cos x)$<br>or<br>$5\sin x(3\cos x - 2) + 4(3\cos x - 2) = 0$ | <b>M1</b>              | Both sides of equation factorised correctly. Maybe sum of two brackets set equal to zero   |
|   | $(5\sin x + 4)(3\cos x - 2) = 0$   | <b>A1</b>              | Factorised form set equal to zero.<br>PI by $5\sin x + 4 = 0$<br>and $3\cos x = 2$   |
|   | $\sin x = -\frac{4}{5}$<br>$\cos x = \frac{2}{3}$  | <b>m1</b><br><b>A1</b> | <b>m1</b> for one correct<br><b>A1</b> for both correct<br>PI by $x = -0.927$ or $-2.214$ (or more accurate)<br>PI by $x = 0.841$ or $-0.841$ (or more accurate)   |
|   | $x = -0.927, -2.214, 0.841, -0.841$  | <b>B2</b>              | Condone more accurate answers.<br>( $-0.927295\dots, -2.21429\dots, \pm 0.841068\dots$ )<br><b>B2</b> for exactly 4 answers to the correct accuracy<br><b>B1</b> for at least 2 answers to the correct accuracy<br>Ignore answers outside of the interval. If more than two answers for each inside the interval, -1 for each extra from Bs to a min of 0. |
|   | <b>Total</b>   | <b>7</b>               |  |

| Q    | Answer  | Marks        | Comments   |
|------|---|--------------|--|
| 7(a) | 0.251   | B1           | AWRT   |
| 7(b) | $P(W < 3) = P(W \leq 2)$<br>$= 0.167$   | M1<br>A1     | Attempts to find correct probability<br>Allow for 0.833<br>AWRT  |
| 7(c) | Not a good model, ...<br><br>Probability of winning unlikely to be constant from game to game | E1<br><br>E1 | Concludes not a good model and any reason, even incorrect<br><br>Comment about probability not being constant or winning in one match unlikely to be independent of winning in another match |
|      | Total   | 5            |  |

| Q    | Answer  | Marks                  | Comments   |
|------|---|------------------------|--|
| 8(a) | $E(Y^2) = (3 \times 1^2 + 1)^2 \times 0.4 +$<br>$(3 \times 2^2 + 2)^2 \times 0.25 +$<br>$(3 \times 3^2 + 3)^2 \times 0.35$<br><br>$\text{Var}(Y) = E(Y^2) - (E(Y))^2$<br>$= 370.4 - 15.6^2$<br><br>$= 127.04$ | M1<br><br>M1<br><br>A1 | Applies formula for $E(Y^2)$<br>Implied by sight of 370.4 or 1852/5 oe<br><br>Applies formula for $\text{Var}(Y)$<br>Condone applied to $X$ instead<br><br>Accept 3176/25 oe |
| 8(b) | $\text{Var}(0.5Y - 6) = 0.5^2 \text{Var}(Y)$<br><br>$= 31.76$   | M1<br><br>A1ft         | Applies formula for $\text{Var}(aY + b)$<br><br>Accept 794/25 oe<br>Follow through their $\text{Var}(Y)$   |
| 8(c) | $E\left(\sum_{i=1}^3 Y_i\right) = 3E(Y)$<br><br>$= 46.8$  | M1<br><br><br>A1       | Applies formula for $E\left(\sum_{i=1}^3 Y_i\right)$<br>PI   |
|      | Total   | 7                      |  |



| Q    | Answer  | Marks    | Comments  |
|------|---|----------|---|
| 9(a) | $P(B \cup S) = 0.7$<br>$P(S) = 0.4$   | B1       | States $P(B \cup S)$ and $P(S)$<br>Accept $P(B \cup S) = 7/10$ oe and $P(S) = 4/10$ oe<br>Also award for $P(S) = 0.4$ and number of customers going to the bank and supermarket is 35 (35 might be implied by Venn diagram) |
|      | $P(B \cap S) = 0.04$  | B1       | $P(B \cap S) = 2/50$ oe   |
|      | $P(B \cup S) = P(B) + P(S) - P(B \cap S)$<br>$0.7 = P(B) + 0.4 - 0.04$                  | M1       | Uses Addition formulae to find $P(B)$<br>Also award for number of customers going to the bank<br>$= 35 - 20 + 2 = 17$   |
|      | $P(B) = 0.34$   | A1       | Accept $17/50$ oe   |
|      | $P(B) \times P(S) = 0.34 \times 0.4 = 0.136$  | A1ft     | Multiplies $P(B)$ and $P(S)$<br>Follow through their $P(B)$ and $P(S)$  |
|      | $P(B \cap S) \neq P(B) \times P(S)$<br>Therefore events $B$ and $S$ are not independent | E1       | Mathematically statement of dependence and conclusion   |
| 9(b) | $P(S B') = \frac{20-2}{20-2+15} \text{ or } \frac{0.36}{0.66}$                          | M1       | Applies conditional probability formula   |
|      | $= \frac{6}{11}$  | A1       | OE<br>Do not accept rounded decimals  |
|      | <b>Total</b>  | <b>8</b> |   |

| Q  | Answer                                   | Marks | Comments  |
|----|--|-------|---|
| 10 | $10.4 = 0.4 \times v - 0.4 \times (-20)$ | M1    | Allow for $10.4 = 0.4 \times v - 0.4 \times (20)$ |
|    | $v = 6$                                  | A1    |   |
|    | Total                                    | 2     |   |

| Q     | Answer                                      | Marks | Comments   |
|-------|---|-------|--|
| 11(a) | $2 + 36t - 6t^2$                            | B2    | Three term expression with one error scores B1.  |
| 11(b) | $36 - 12t = 0$                              | M1    | Differentiating their $v$ and setting equal to zero or attempt to complete the square to obtain $a(t - 3)^2 + b$ . |
|       | $t = 3$                                     | A1ft  | For value of $t$ for which $v$ is a maximum.<br>ft their $v$ from part (a) provided B1 scored.                     |
|       | $7 + 2(3) + 18(3^2) - 2(3^3) \quad (= 121)$ | M1    | Substituting their $t = 3$ into the expression for the displacement  |
|       | $121 - 7$                                   | M1    | Subtracting 7 from their displacement at $t = 3$   |
|       | 114   | A1    | CAO  |
|       | Total                                       | 7     |  |

| Q                | Answer   | Marks   | Comments  |
|------------------|--|---|---|
| <b>12(a)</b>     | $R - 2g = 10$<br>$R = 206$   | <b>M1</b><br><b>A1</b>  | Three term equation of motion ignoring signs with $20g$ or $196$ and $20 \times 0.5$ or $10$<br>For correct $R$   |
| <b>12(b)</b>     | $11000 - (900 + 20x)g = 0.5(900 + 20x)$<br>or<br>$11000 - (900 + 20x)g \geq 0.5(900 + 20x)$<br><br>$10x + 20gx = 11000 - 900g - 450$<br>or<br>$10x + 20gx \leq 10550 - 900g$<br><br>$(x =) 8.39...$<br>or<br>$x \leq 8.39...$<br><br>8 boxes | <b>M1</b><br><br><b>A1</b><br><br><b>M1</b><br><br><br><b>A1</b><br><br><b>E1</b> | oe.<br>Equation of motion, ignoring signs, including consideration of total mass of lift and $x$ boxes.<br>May be seen as an inequality, ignoring signs. Condone $>$<br>Correct equation or inequality. Condone $>$<br><br>oe. Simplification of their equation or inequality isolating terms in $x$ on one side and constant terms on the other. Condone $<$<br>AWR 8.4 Condone truncated to 8.3 PI by 8 in correct concluding statement<br>If working with inequalities correct inequality must be seen here. Condone $<$<br>Correct statement including whole number of boxes dependent upon correct working seen. |
| <b>12(b) ALT</b> | $11000 - Mg = 0.5M$<br>or<br>$11000 - Mg \geq 0.5M$<br><br>$(M =) 1067.96...$<br>or<br>$(M \leq) 1067.96...$<br><br>$(x =) 8.39...$<br>or<br>$x \leq 8.39...$<br><br>8 boxes   | <b>M1</b><br><br><b>A1</b><br><br><b>M1</b><br><br><br><b>A1</b><br><br><b>E1</b> | oe.<br>Equation of motion, ignoring signs, including consideration of total mass of lift and boxes $M$ .<br>May be seen as an inequality, ignoring signs. Condone $>$<br>Correct equation or inequality. Condone $>$<br><br>AWR 1068<br>Solving equation or inequality for $M$<br><br>AWR 8.4 For number of boxes unrounded. Condone truncated to 8.3 PI by 8 in correct concluding statement<br>If working with inequalities correct inequality must be seen here. Condone $<$<br>Correct statement including whole number of boxes dependent upon correct working seen.   |
|                  | <b>Total</b>   | <b>7</b>  |   |

| Q  | Answer  | Marks   | Comments  |
|----|---|---|---|
| 13 | <p>(Displacement =) <math>-75</math> or <math>75</math></p> $3 \times 10 + \frac{1}{2} \times a \times 10^2 = 75$ <p>or</p> $3 \times 10 + \frac{1}{2} \times a \times 10^2 = -75$ <p><math>a = 0.9</math></p> <p><math>a = -2.1</math></p> | <p><b>B1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>A1</b></p> | <p>Both values.<br/>PI by later working.<br/>Recognises that displacement could be <math>\pm 75</math></p> <p>Use of constant acceleration formula to gain at least one correct equation. Values substituted but need not be evaluated.</p> <p>oe</p> <p>oe</p> |
|    | <b>Total</b>  | <b>4</b>  |   |