

## INTERNATIONAL A-LEVEL MATHEMATICS MA03

(9660/MA03) Unit P2 Pure Mathematics

Mark scheme

January 2022

Version: 1.0 Final



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## Key to mark scheme abbreviations

M Mark is for method

m Mark is dependent on one or more M marks and is for method

A Mark is dependent on M or m marks and is for accuracy

**B** Mark is independent of M or m marks and is for method and accuracy

E Mark is for explanation

√ or ft Follow through from previous incorrect result

**CAO** Correct answer only

**CSO** Correct solution only

**AWFW** Anything which falls within

**AWRT** Anything which rounds to

**ACF** Any correct form

AG Answer given

SC Special case

**oe** Or equivalent

A2, 1 2 or 1 (or 0) accuracy marks

**–x EE** Deduct x marks for each error

NMS No method shown

PI Possibly implied

**SCA** Substantially correct approach

**sf** Significant figure(s)

**dp** Decimal place(s)

Q		Answer	Marks	Comments
1(a)	0 0.75	$e^{-0^{2}} = 1$ $e^{-0.75^{2}} = 0.569782825$ $e^{-1.5^{2}} = 0.105399225$	B1 M1	All five correct $x$ values (and no extra used) <b>PI</b> by five correct $y$ values  At least four correct $y$ values in exact form or decimals, rounded or truncated
	1.5 2.25 3.0	$e^{-1.5^{2}} = 0.105399225$ $e^{-2.25^{2}} = 0.006329715$ $e^{-3^{2}} = 0.000123410$		to three dp <b>or</b> better (in table or formula) ( <b>PI</b> by <b>AWRT</b> correct answer)
		1+0.000123+4(0.56978 297)+2×0.105399]	m1	Correct sub into formula with $h = 0.75$ <b>oe</b> and at least four correct $y$ values either listed, with + signs, or totalled. ( <b>PI</b> by AWRT correct answer)
	= 0.879		A1	CAO, must see this value exactly and no error seen
			4	

Q	Answer	Marks	Comments
1(b)(i)	$f(x) = e^{-x^2} - 0.5x - 0.5$ $f(0.5) = e^{-0.5^2} - 0.25 - 0.5 = 0.0288$	M1	Or reverse  Both values rounded or truncated to at least 1sf
	$f(0.6) = e^{-0.6^2} - 0.3 - 0.5 = -0.102$ Change of sign, $0.5 < x < 0.6$	<b>A</b> 1	Must have both statement and interval in words or symbols or comparing 2 sides:
		2	at $0.5$ , $e^{-0.5^2} > 0.75$ ; at $0.6$ , $e^{-0.6^2} < 0.8 = 0.8(\cdots)$ (M1) Conclusion as before (A1)
		2	

Q	Answer	Marks	Comments
1(b)(ii)	$-x^2 = \ln\left(\frac{1}{2}(x+1)\right)$	M1	
	$x^2 = \ln\left(\frac{2}{(x+1)}\right)$		Must see a middle line
	$x = \sqrt{\ln\left(\frac{2}{(x+1)}\right)}$	<b>A</b> 1	<b>AG</b> Condone inclusion of $\pm$
		2	

Q	Answer	Marks	Comments
1(b)(iii)	$x_2 = 0.536$	B1	
	$x_3 = 0.514$	B1	If 0 scored then <b>SC1</b> for 0.54 AND 0.51
		2	

Question 1 Total	10	
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Q	Answer	Marks	Comments
2(a)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 8 \times 2(2x+1)^7 \cos 3x + (2x+1)^8 \times (-3\sin 3x)$	М1	$p(2x+1)^7 \cos 3x + (2x+1)^8 \times (-q \sin 3x)$
	$= 16(2x+1)^{7}\cos 3x - 3(2x+1)^{8}\sin 3x$	<b>A</b> 1	All correct
		2	

Q	Answer	Marks	Comments
2(b)	$\frac{dy}{dx} = \frac{(2x^3 + 5)9x^2 - (3x^3 - 1)6x^2}{(2x^3 + 5)^2}$	M1	$\frac{\left(2x^3+5\right)ax^2-\left(3x^3-1\right)bx^2}{\left(2x^3+5\right)^2}$
	$= \frac{51x^2}{(2x^3 + 5)^2}$	<b>A</b> 1	Must see use of differentiation
		2	

Q	Answer	Marks	Comments
2(c)	$2y^{2} + 4xy\frac{dy}{dx} = 6xy + 3x^{2}\frac{dy}{dx}\left[+\frac{dy}{dx}[1]\right]$	M1 A1	LHS or RHS correct implicit differentiation Both correct
	$\frac{dy}{dx} = \frac{6xy - 2y^2}{4xy - 3x^2 - 1}$	<b>A</b> 1	oe
		3	

Question 2 Total	7	
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Q	Answer	Marks	Comments
3(a)	$8[(0.5)^{3}] + a[(0.5)^{2}] + b[0.5] + 6 = 6$ $8[(-0.5)^{3}] + a[(-0.5)^{2}] + b[-0.5] + 6 = 9$	M1	One correct substitution or for M1 use of long division
	0.25a + 0.5b = -1	<b>A</b> 1	
	0.25a - 0.5b = 4	m1	Attempt to solve
	b = -5 $a = 6$	<b>A</b> 1	Both answers correct
		4	

Q	Answer	Marks	Comments
3(b)	$f(-1.5) = 8(-1.5)^3 + 6(-1.5)^2 - 5(-1.5) + 6$ $= -27 + 13.5 + 7.5 + 6$ $= 0$ As equal to 0, $(2x + 3)$ is a factor	E1	Must see working  Condone omission of statement
		1	

Q	Answer	Marks	Comments
3(c)	$\frac{8x^3 + 6x^2 - 5x + 6}{4x^2 + 4x - 3} = \frac{(2x+3)(4x^2 - 3x + 2)}{(2x-1)(2x+3)}$	B1ft B1	Numerator correct PI Denominator correct Accept long division, or other equivalent methods eg
	$=\frac{2x(2x-1)-0.5(2x-1)+1.5}{(2x-1)}$	М1	$ \frac{2x - 0.5}{4x^2 + 4x - 3 8x^3 + 6x^2 - 5x + 6} $ $ 8x^3 + 8x^2 - 6x $
	$=2x-\frac{1}{2}+\frac{3}{2(2x-1)}$	<b>A</b> 1	$     \begin{array}{r}       -2x^2 + x + 6 \\       -2x^2 - 2x + 1.5 \\     \end{array} $
			3x + 4.5
		4	

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Q	Answer	Marks	Comments
4(a)	$\int y^2 \mathrm{d}y = \int 2x  \mathrm{d}x$	M1	For attempt at integration after separating variables
	At (2, 3) $\frac{1}{3}y^3 = x^2 + 5$	<b>A</b> 1	ACF
		2	

Q	Answer	Marks	Comments
4(b)	$\int 2y  \mathrm{d}y = \int x^2  \mathrm{d}x$	M1	For attempt at integration after separating variables
	At (2, 3) $y^2 = \frac{1}{3}x^3 + \frac{19}{3}$	<b>A</b> 1	ACF
		2	

Q	Answer	Marks	Comments
4(c)	$\frac{dy}{dx} = \frac{4}{9}$	M1	Either gradient correct
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{4}{6} \left[ = \frac{2}{3} \right]$		
	$\tan \theta = \frac{\frac{4}{6} - \frac{4}{9}}{1 + \frac{4}{6} \times \frac{4}{9}}$	M1	Correct use of trig identity oe
	$\tan \theta = \frac{6}{35}$	<b>A</b> 1	
		3	

Question 4 To	al 7	
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Q	Answer	Marks	Comments
5(a)(i)	$[12\cos\theta - 5\sin\theta =]$ $R\cos\theta\cos\alpha - R\sin\theta\sin\alpha$	M1	PI
	R=13	<b>A</b> 1	
	$\alpha$ = 0.395	<b>A</b> 1	
		3	

Q	Answer	Marks	Comments
5(a)(ii)	$\cos(x+0.4+0.395) = \frac{6.5}{13}$ $\left[x+0.795 = \pm \frac{\pi}{3}  \text{oe}\right]$	M1	Ft their part (a)
	x = -1.84	<b>A</b> 1	One correct answer
	x = 0.25	<b>A</b> 1	2 <sup>nd</sup> correct answer and no extras Ignore answers outside range
		3	

Q	Answer	Marks	Comments
5(b)	$8\cot^2 y = 8\csc^2 y - 8  [= 2\csc y + 7]$	M1	Correct use of trig identity PI
	$8\csc^{2}y - 8 = 2\csc y + 7$ $8\csc^{2}y - 2\csc y - 15 = 0$ $(4\csc y + 5)(2\csc y - 3)[= 0]$	m1	Factorisation or correct use of formula PI
	$\csc y = -\frac{5}{4}, \frac{3}{2}$ or $\sin y = \frac{2}{3}, -0.8$	<b>A</b> 1	Both correct and no errors seen (May use cos/sin for first <b>M1</b> , <b>m1</b> , <b>A1</b> )
	$y = -127^{\circ}, -53^{\circ},$ $42^{\circ}, 138^{\circ}$	B1	Sight of <b>at least two</b> of these values correct
		B1	All 4 correct and no extras in interval (ignore answers outside interval)
		5	

Question 5 Tota	11	
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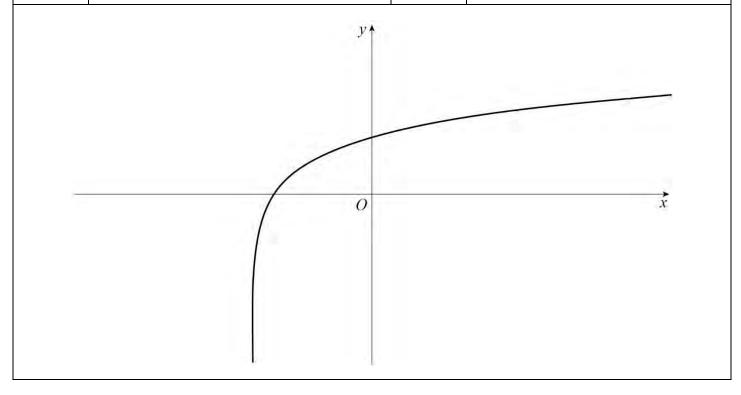
Q	Answer	Marks	Comments
6(a)	Translation $\begin{bmatrix} a \\ b \end{bmatrix}$	M1	Where at least one of <i>a</i> or <i>b</i> is non-zero
	$\begin{bmatrix} -2 \\ 1 \end{bmatrix}$	<b>A1</b>	Correct transformation and vector If <b>M0</b> scored <b>SC1</b> for $\begin{bmatrix} -2\\1 \end{bmatrix}$
		2	

Q	Answer	Marks	Comments
6(b)(i)	$y = \ln(x+2) + 1$		
	$x-1=\ln(y+2)$	M1	Swap $y$ and $x$
	$x-1 = \ln(y+2)$ $y+2 = e^{x-1}$ $f^{-1}(x) = e^{x-1} - 2$	M1	Attempt to isolate
	$f^{-1}(x) = e^{x-1} - 2$	<b>A</b> 1	Correct answer and no errors seen
		3	

Q	Answer	Marks	Comments
6(b)(ii)	Reflection in $y = x$	B1	
		1	

Q	Answer	Marks	Comments
6(b)(iii)	$[f^{-1}(x)] > -2$	B1	Do not allow $x > -2$
		1	

Q	Answer	Marks	Comments
6(c)(i)	See diagram below	B1	Correct shape and position
		B1	(0, 1+In2) stated or marked
		B1	$(e^{-1}-2,0)$ stated or marked
		3	



Q	Answer	Marks	Comments
6(c)(ii)	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{x+2}$	М1	
	At $(-1,1)$ $y-1=1(x-(-1))$ $[y=x+2]$	<b>A</b> 1	
		2	

Question 6 Total 12	2
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Q	Answer	Marks	Comments
7(a)	$\left[\frac{\mathrm{d}u}{\mathrm{d}x} = \right] 4e^{4x}$ $\mathrm{d}x = \frac{\mathrm{d}u}{4(u-1)}$	В1	
	$\left[\int \frac{1}{e^{4x} + 1} dx = \int \frac{dx}{u}\right]$	M1	All in terms of $\mathcal{U}$ , condone omission of $\mathrm{d} u$
	$=\int \frac{\mathrm{d}u}{4u(u-1)}$	<b>A</b> 1	Must see $du$ here, or earlier
	$\frac{1}{u(u-1)} = \frac{A}{u} + \frac{B}{u-1}$	M1	Use of partial fractions
	1 = A(u-1) + Bu $A = -1, B = 1$	<b>A</b> 1	
	$\int \frac{\mathrm{d}u}{4u(u-1)} = \frac{1}{4} \left( \ln(u-1) - \ln u \right)$	m1	Correct integration
	$[x]_0^{\ln 2} = [u]_2^{17}$	B1	Change of limits, maybe seen earlier (may change back to <i>x</i> and not change limits)
	$\int_{0}^{\ln 2} \frac{1}{e^{4x} + 1} dx = \frac{1}{4} \left[ \ln \frac{16}{17} - \ln \frac{1}{2} \right]$		
	$=\frac{1}{4}\ln\frac{32}{17}$	<b>A</b> 1	
		8	

Q	Answer	Marks	Comments
7(b)	$\left[ \int \frac{e^{4x}}{1 + 2e^{4x}} dx = \right] k \ln(1 + 2e^{4x}) [+c]$	M1	
	$= \frac{1}{8} \ln(1 + 2e^{4x}) + c$	<b>A</b> 1	
		2	

Question 7 Total	10	
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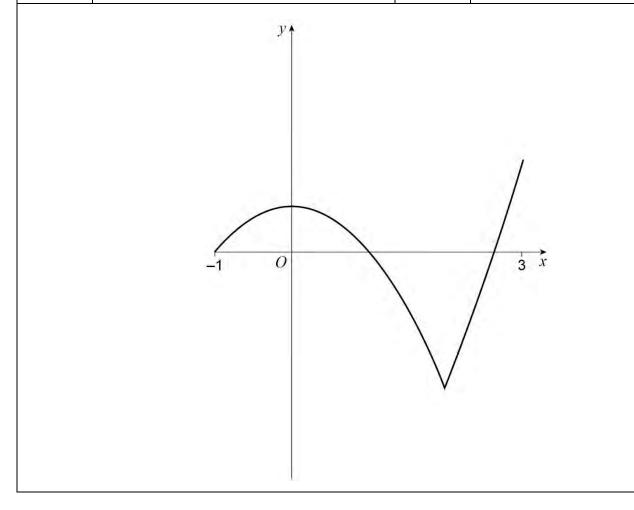
Q	Answer	Marks	Comments
8(a)	$\sec \theta = \frac{x}{a} \qquad \tan \theta = \frac{y}{b}$	M1	
	$\left(\frac{x}{a}\right)^2 = 1 + \left(\frac{y}{b}\right)^2$	<b>A</b> 1	ACF
		2	

Q	Answer	Marks	Comments
8(b)	When $\theta = \frac{\pi}{4}$ : $x = a\sqrt{2}$ , $y = b$	B1	PI
	Either		
	$\frac{\mathrm{d}x}{\mathrm{d}\theta} = a\sec\theta\tan\theta \qquad \frac{\mathrm{d}y}{\mathrm{d}\theta} = b\sec^2\theta$	M1	Either derivative correct
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{b\sec\theta}{a\tan\theta} = \left[\frac{b}{a}\csc\theta\right]$	<b>A</b> 1	
	or		
	$\frac{\mathrm{d}y}{\mathrm{d}x} = p(\frac{x^2}{a^2} - 1)^{-\frac{1}{2}} \times qx$	(M1)	Attempt at isolating y and chain rule
	$= b \frac{1}{2} \left( \frac{x^2}{a^2} - 1 \right)^{-\frac{1}{2}} \times \frac{2x}{a^2}$	(A1)	
	or		
	$\frac{2x}{a^2} = \frac{2y}{b^2} \frac{\mathrm{d}y}{\mathrm{d}x}$	(M1)	Attempt at implicit differentiation
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{xb^2}{ya^2}$	(A1)	
	When $\theta = \frac{\pi}{4}$ : $\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{b\sqrt{2}}{a}$ oe	<b>A</b> 1	
	Equation of normal		
	$y - b = -\frac{a}{b\sqrt{2}}(x - a\sqrt{2})$	<b>A</b> 1	All correct <b>ACF</b> eg $y = -\frac{\sqrt{2}a}{2t}x + \frac{a^2 + b^2}{t}$
			ACF eg $y = -\frac{1}{2b}x + \frac{1}{b}$
		5	

Q	Answer	Marks	Comments
8(c)	$x = 0,  y - b = -\frac{a}{b\sqrt{2}}(-a\sqrt{2})$		
	$x = 0,  y - b = -\frac{a}{b\sqrt{2}}(-a\sqrt{2})$ $y = \frac{a^2 + b^2}{b}$	M1	Attempt to find A and B
	$y = 0, -b = -\frac{a}{b\sqrt{2}}(x - a\sqrt{2})$		
	$x = \frac{\left(a^2 + b^2\right)\sqrt{2}}{a}$	<b>A</b> 1	Both correct
	$y = 0,  -b = -\frac{a}{b\sqrt{2}}(x - a\sqrt{2})$ $x = \frac{\left(a^2 + b^2\right)\sqrt{2}}{a}$ $Area = \frac{\left(a^2 + b^2\right)^2}{\sqrt{2}ab}$	<b>A</b> 1	ое
		3	

Question 8 Tota	10
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Q	Answer	Marks	Comments
9(a)(i)	See diagram below	B1 B1 B1	y-intercept at a max point [1 or (0, 1)]  Correct for $-1 \le x \le 2$ Correct for $2 \le x \le 3$ , curvature at $x = 2$ and nothing for $x > 3$
		3	



Q	Answer	Marks	Comments
9(a)(ii)	$-3 \le f(x) \le 2$	B1	Condone use of $y$ , f, etc
		1	

Q	Answer	Marks	Comments
9(a)(iii)	$\left 4-x^2\right =1$	M1	PI
	$x = \sqrt{5} \qquad x = \sqrt{3}$	<b>A</b> 1	Both correct values and no extras
		2	

Q	Answer	Marks	Comments
9(b)	$\left  4 - \frac{1}{(x-1)^2} \right  - 3 = -2$	M1	PI
	$x = 1 \pm \frac{1}{\sqrt{3}}$ , $x = 1 \pm \frac{1}{\sqrt{5}}$	A2,1,0	Answers must be in exact form  A1: at least two correct oe  A2: all correct and no extras oe
		3	

Question 9 Tot	9	
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Q	Answer	Marks	Comments
10(a)	$\cos(2\theta + \theta) = \cos 2\theta \cos \theta - \sin 2\theta \sin \theta$	B1	
	$= (2\cos^2\theta - 1)\cos\theta - 2\sin\theta\cos\theta\sin\theta$	М1	Correct use of double angle formulae and $\sin^2 \theta = 1 - \cos^2 \theta$
	$= 2\cos^3\theta - \cos\theta - 2\cos\theta \left(1 - \cos^2\theta\right)$		
	$=4\cos^3\theta-3\cos\theta$	<b>A</b> 1	AG, no errors seen
		3	

Q	Answer	Marks	Comments
10(b)	$\cos^3 2x = \frac{1}{4} (3\cos 2x + \cos 6x)$	B1	PI
	$\int x \cos^3 2x  dx$		
	$= \frac{1}{4}x \left(\frac{3}{2}\sin 2x + \frac{1}{6}\sin 6x\right)$ $-\frac{1}{4}\int \left(\frac{3}{2}\sin 2x + \frac{1}{6}\sin 6x\right) dx$	M1 A1	Correct use of parts formula Correct integral of $\cos 2x + \cos 6x$
	$4\int \left(2^{\sin 2x} + 6^{\sin 6x}\right)^{4x}$	<b>A</b> 1	All correct
	$=\frac{3}{8}x\sin 2x+\frac{1}{24}x\sin 6x$	M1	Correct integration
	$+\frac{3}{16}\cos 2x + \frac{1}{144}\cos 6x  [+c]$	<b>A</b> 1	All correct
		6	

Question 10 Tota	9	
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Q	Answer	Marks	Comments
11(a)	$f(x) = \frac{A}{2-x} + \frac{B}{(1-2x)} + \frac{C}{(1-2x)^2}$		
	$12 = A(1-2x)^2 + B(2-x)(1-2x) + C(2-x)$	B1	Correctly eliminating fractions
	$x = 2$ , $12 = 9A$ , $A = \frac{4}{3}$	M1	Attempt at finding one constant
	$x = 0.5,  12 = \frac{3}{2}C,  C = 8$	<b>A</b> 1	Two constants correct
	$x = 0$ , $12 = \frac{4}{3} + 2B + 16$ , $B = -\frac{8}{3}$		
	$f(x) = \frac{4}{3(2-x)} - \frac{8}{3(1-2x)} + \frac{8}{(1-2x)^2}$	<b>A</b> 1	All correct Allow equivalent methods
		4	

Q	Answer	Marks	Comments
11(b)	$(2-x)^{-1} = \frac{1}{2} \left( 1 - \frac{1}{2}x \right)^{-1} = \frac{1}{2} + \frac{1}{4}x + \frac{1}{8}x^2$	B1	
		1	

Q	Answer	Marks	Comments
11(c)	f(x):		
	$\frac{4}{3}(2-x)^{-1} = \frac{4}{3}\left(\frac{1}{2} + \frac{1}{4}x + \frac{1}{8}x^2\right)$		
	$(1-2x)^{-1} = 1+2x+4x^{2}$ $(1-2x)^{-2} = 1+4x+12x^{2}$	M1	Expansion in the form $1+ax+bx^2$
		A1 A1	One mark for each correct expansion
	f(x):		
	$\left  \frac{4}{3} \left( \frac{1}{2} + \frac{1}{4}x + \frac{1}{8}x^2 \right) - \frac{8}{3} (1 + 2x + 4x^2) \right $	M1	
	$+8(1+4x+12x^2)$		
	$f(x) = 6 + 27x + 85.5x^2$	<b>A</b> 1	Allow equivalent methods
		5	

Question 11 Total	10	
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Q	Answer	Marks	Comments
12	Coords of $P(-2+3p, 3+4p, -1-5p)$	B1	
	Direction $AP \begin{bmatrix} 3p \\ 5+4p \\ -4-5p \end{bmatrix}$	M1	Seen or used
	$\begin{bmatrix} 3p \\ 5+4p \\ -4-5p \end{bmatrix} \begin{bmatrix} 3 \\ 4 \\ -5 \end{bmatrix} [=0]$		OR $AP^2 = (3p)^2 + (5+4p)^2 + (4+5p)^2$ $(X) = 50p^2 + 80p + 41$
	50 p = -40 $p = -0.8$	<b>A</b> 1	$\frac{dX}{dp} = 100 p + 80,  p = -0.8$
	Dist = $\sqrt{(-4.4+2)^2 + (-0.2+2)^2 + (3-3)^2}$	М1	$\frac{\mathrm{d}^2 X}{\mathrm{d}p^2} = 100 > 0  \text{MIN}$
	= 3	<b>A</b> 1	CSO
		6	

Question 12 Total	6
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Q	Answer	Marks	Comments
13(a)	$t = 0, M = 10$ $10 = \frac{A}{1+2}$		
	A = 30	B1	
	$t = 1, M = 15$ $15 = \frac{30}{1 + 2e^k}$ $1 + 2e^k = 2$ $e^k = 0.5$ $k = -\ln 2$		
	$1+2e^k=2$	M1	Attempt to find k
	$e^k = 0.5$		
	$k = -\ln 2$	<b>A1</b>	oe
		3	

Q	Answer	Marks	Comments
13(b)	$M = \frac{30}{1 + 2e^{-5\ln 2}}$	M1	
	M = 28	<b>A</b> 1	
		2	

Q	Answer	Marks	Comments
13(c)	$18 = \frac{30}{1 + 2e^{-t \ln 2}}$ $1 + 2e^{-t \ln 2} = \frac{5}{3}$ $e^{-t \ln 2} = \frac{1}{3}$		
	$1 + 2e^{-t \ln 2} = \frac{5}{3}$		
	$e^{-t\ln 2} = \frac{1}{3}$	M1	
	$-t\ln 2 = -\ln 3$		
	$t = \frac{\ln 3}{\ln 2}$	<b>A</b> 1	ое
		2	

Q	Answer	Marks	Comments
13(d)	$M = A \left( 1 + 2e^{kt} \right)^{-1}$		
	$M = A \left( 1 + 2e^{kt} \right)^{-1}$ $\frac{dM}{dt} = -A \left( 1 + 2e^{kt} \right)^{-2} \times 2ke^{kt}$	M1 A1ft	ft their $\boldsymbol{A}$ and $\boldsymbol{k}$
	When $t = 4$ $\frac{dM}{dt} = -30(1 + 2e^{-4\ln 2})^{-2} \times 2 \times (-\ln 2) \times e^{-4\ln 2}$		Note that $e^k = \frac{1}{2}$ for the correct value of $k$
	$\frac{\mathrm{d}M}{\mathrm{d}t} = \frac{80}{27} \ln 2$	A1ft	ое
		3	

		10	Question 13 Total
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