

Please write clearly in block capitals.

Centre number

--	--	--	--	--

Candidate number

--	--	--	--

Surname

--

Forename(s)

--

Candidate signature

--

I declare this is my own work.

INTERNATIONAL A-LEVEL FURTHER MATHEMATICS

(9665/FM04) Unit FS2 Statistics

Time allowed: 1 hour 30 minutes

Materials

- For this paper you must have the Oxford International AQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphic calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



1 The diameters of the metal discs produced by a machine have a normal distribution with standard deviation 1 millimetre.

The machine breaks down. After it is repaired, a random sample of 101 metal discs produced by the machine is taken.

The sample standard deviation is found to be 1.2 millimetres.

The owner of the machine is concerned that the population standard deviation may have increased.

Investigate whether the population standard deviation has increased, using the 1% level of significance.

[illegible]

[illegible]

A town has a weather station which measures the wind speed. The maximum daily wind speed at the station has a normal distribution with standard deviation 1.6 knots.

Emma uses a sample of size of n days.

[3 marks]

This image shows a blank sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Answer _____



2 (b) The total of the maximum daily wind speeds in Emma's sample is 2300 knots.

Find Emma's confidence interval, giving your values to two decimal places.

[3 marks]

Answer

6

Turn over for the next question

Turn over ►



At a particular company, a random sample of the employees was selected.

The results are shown in the following table.

	Satisfied	Not satisfied	Total
Male	21	19	40
Female	27	13	40
Total	48	32	80

[9 marks]

[illegible]

This image shows a single sheet of white paper with horizontal blue or grey ruling lines. The lines are evenly spaced and run across the width of the page. There are approximately 20 lines visible. The paper has a slight shadow on its right side, suggesting it's resting on a surface. There is no handwriting or other markings on the paper.

9

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Answer _____

- 4 (a) (ii) Find the power of Jane's hypothesis test, giving your answer to three decimal places.

[2 marks]

Answer _____

- 4 (b) State the critical region of Jane's hypothesis test.

[1 mark]

Answer _____

Turn over ►



Huang is investigating the weekly household income in a country.

Huang takes a random sample of 5 households.

Their weekly household income, in dollars, was recorded in a particular week in 2008 and then recorded again in 2018 in the corresponding week.

The results are shown in the following table.

Household	2008 (\$)	2018 (\$)
A	600	610
B	597	600
C	602	602
D	605	603
E	598	598

Huang claims that the mean weekly household income in 2018 has not changed compared with the mean weekly household income in 2008

Test Huang's claim, using the 10% level of significance.

[11 marks]

[illegible]

[illegible]

Justine is investigating the heights of women who play basketball.

She also takes a random sample of 300 women who do not play basketball and measures their heights, Y centimetres.

$$\sum x = 65\,760 \quad \text{and} \quad \sum x^2 = 10\,814\,020$$

$$\sum y = 49\,197 \quad \text{and} \quad \sum y^2 = 8\,070\,022$$

Justine claims that the mean height of women who play basketball is greater than the mean height of women who do not play basketball.

[12 marks]

[illegible]

[illegible]

12

- 7** The random variables B_i $\{i = 1, 2, \dots, k\}$ are independent and each have a binomial distribution with parameters n and p

- 7 (a)** Show that the random variable $R = \frac{B_1}{n}$ is an unbiased estimator of p

[2 marks]

- 7 (b)** Show that the random variable $T = \frac{1}{kn} \sum_{i=1}^k B_i$ is a consistent estimator.

[4 marks]



[5 marks]

[illegible]

11

Turn over ►



8 (a) Show that the moment generating function of X_i is given by

$$M_{X_i}(t) = \left(1 - \frac{t}{\lambda}\right)^{-1} \quad \text{where } t < \lambda$$

[illegible]
$$X = \sum_{i=1}^n X_i \quad \text{where } X_i \text{ and } X_j \text{ are independent for } i \neq j$$

Using moment generating functions, find $\text{Var}(X)$



[illegible]

Answer _____

Question 8 continues on the next page

8 (c) The random variable Y is such that $Y = 2\lambda X$ where λ is a constant

8 (c) (i) Find $E(Y)$

[2 marks]

Answer _____

8 (c) (ii) Find $\text{Var}(Y)$

[2 marks]

Answer _____

15

END OF QUESTIONS



There are no questions printed on this page

*Do not write
outside the
box*

**DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED**



*Do not write
outside the
box*

[illegible]

*Do not write
outside the
box*

[illegible]

*Do not write
outside the
box*

[illegible]

There are no questions printed on this page

*Do not write
outside the
box*

**DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED**

Copyright information

For confidentiality purposes, all acknowledgements of third-party copyright material are published in a separate booklet. This booklet is published after each live examination series and is available for free download from www.oxfordaqaexams.org.uk

Permission to reproduce all copyright material has been applied for. In some cases, efforts to contact copyright-holders may have been unsuccessful and Oxford International AQA Examinations will be happy to rectify any omissions of acknowledgements. If you have any queries please contact the Copyright Team.

Copyright © 2022 Oxford International AQA Examinations and its licensors. All rights reserved.

