

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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**Monday 8 June 2020**

Morning (Time: 1 hour 30 minutes)

Paper Reference **WFM03/01**

**Mathematics**

**International Advanced Subsidiary/Advanced Level**  
**Further Pure Mathematics F3**

**You must have:**

Mathematical Formulae and Statistical Tables (Blue), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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- (b) Hence determine the exact coordinates of the points of intersection of the curve with equation  $y = \sinh 3x$  and the curve with equation  $y = 19 \sinh x$ , giving your answers as simplified logarithms where necessary. (5)

Question 1 continued

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(Total 7 marks)

Q1



2. Determine

$$(i) \int \frac{1}{3x^2 + 12x + 24} dx \quad (4)$$

$$(ii) \int \frac{1}{\sqrt{27 - 6x - x^2}} dx \quad (4)$$

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Question 2 continued

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Question 2 continued

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(Total 8 marks)

Q2

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Question 3 continued

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**Question 3 continued**

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**(Total 9 marks)**

**Q3**



4.

$$I_n = \int x^n \cos x \, dx$$

(a) Show that, for  $n \geq 2$

$$I_n = x^n \sin x + nx^{n-1} \cos x - n(n-1)I_{n-2} \quad (4)$$

(b) Hence find the functions  $f(x)$  and  $g(x)$  such that

$$\int x^4 \cos x \, dx = f(x) \sin x + g(x) \cos x + c$$

where  $c$  is an arbitrary constant.

(5)

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Question 4 continued

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### Question 4 continued

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Question 4 continued

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(Total 9 marks)

Q4







**Question 5 continued**

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Question 5 continued

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Q5

(Total 12 marks)



$$\mathbf{A} = \begin{pmatrix} 1 & -1 & 1 \\ 1 & 1 & 1 \\ 1 & 2 & a \end{pmatrix} \quad a \neq 1$$

(4)

$$\mathbf{B} = \begin{pmatrix} 1 & -1 & 1 \\ 1 & 1 & 1 \\ 1 & 2 & 4 \end{pmatrix}$$

$$(\mathbf{r} - (12\mathbf{i} + 4\mathbf{j} + 6\mathbf{k})) \times (-6\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}) = \mathbf{0}$$

(4)



Question 6 continued

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### Question 6 continued

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Question 6 continued

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(Total 8 marks)

Q6

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**Question 7 continued**

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**Question 7 continued**

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**Q7**

**(Total 12 marks)**



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$$x - 5y + 3z = 11$$

$$3x - 2y + 2z = 7$$

- (a) Find a vector equation for  $l$ , giving your answer in the form  $\mathbf{r} = \mathbf{a} + \lambda \mathbf{b}$  where  $\mathbf{a}$  and  $\mathbf{b}$  are constant vectors and  $\lambda$  is a scalar parameter.

(5)

- (b) Find, in exact simplified form, the shortest distance between  $m$  and  $n$ .

(5)



Question 8 continued

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### Question 8 continued

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Question 8 continued

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Q8

(Total 10 marks)

END

TOTAL FOR PAPER: 75 MARKS

