

Mark Scheme (Results)

October 2018

Pearson Edexcel International Advanced Level in Statistics S1 (WST01/01)

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### **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### **EDEXCEL IAL MATHEMATICS**

# **General Instructions for Marking**

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{\phantom{a}}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- 4. All A marks are `correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

Question Number	Scheme	Marks			
1.(a)	$S_{tt} = 1828 - \frac{(136)^2}{12} = 286.6$ o.e. awrt <u>287</u>	M1A1			
(b)	$r = \frac{S_{ht}}{\sqrt{S_{tt}S_{hh}}} = \frac{-236}{\sqrt{"286.6" \times 297}} \text{ or } \frac{-236}{\sqrt{85140}}; = -0.8088 \text{ awrt } \underline{-0.809}$	(2) M1A1			
(c)	Temperature decreases as height increases.	B1ft (1)			
(d)	$b = \frac{S_{ht}}{S_{hh}} = \frac{-236}{297} (= -0.7946)$ $a = \overline{t} - b\overline{h} = 11.3 + 0.7946 \times 9.33 = 18.7497$	M1 M1			
	t = 18.7 - 0.795h	A1 (3)			
(e) (f)	$t = 18.7 - 0.795 \times 5 = 14.7$ Unreliable as the data is from France not South Africa	M1 A1 (2) B1			
	Notes	(1) <b>Total 11</b>			
	Correct numerical answers in (a), (b), (d) or (e) score all the marks for tha	t part.			
(a)	M1 Correct expression for $S_{tt}$	· F ···			
	A1 awrt 287 allow exact fractions e.g. $\frac{860}{3}$ or $286\frac{2}{3}$				
(b)	M1 for attempt at correct formula, values must be substituted. Allow $\frac{-236}{\sqrt{287 \times 297}}$				
	A1 awrt $-0.809$ (allow $-0.808$ from a correct expression with 287 used)				
(c)	B1ft for a comment in context. Must see "height" (or h) and "temperature" (or t) Allow "as the temperature increases the height above sea level decreases" (or t)				
NB	If $ r  > 1$ score B0 in (c) Saying "sea level increases" (o.e.) is B0	<i>j</i>			
(d)	M1 Correct expression for b.				
	M1 Allow 11.3"their $b \times 9.33$ " [ $a = \frac{16706}{891}$ scores M1 but A0]				
	A1 $t = (18.75 \text{ or awrt } 18.7) - (\text{awrt } 0.795)h$ [No fractions and no $x, y$ ]				
(e)	M1 substitute $h = 5$ or 500 into <u>their</u> regression line answer in range [14.7, 14.8] (condone coming from $y$ , $x$ equation)				
(f)	B1 unreliable with a reason. [Use of 500 in (e) <u>and</u> stating "out of range" is B0] Must mention France or (S) Africa and at least imply the other				

Question Number						
2.(a)	$Q_2 = 54$	B1				
	$Q_1 = 45$	B1				
(b)	$Q_3 = 59$ Upper limit = $59 + 1.5 \times 14 = 80$	B1 (3) M1				
(b)	Lower limit = $45-1.5\times14=80$					
	Outlier 84					
		(3)				
	Males	B1				
(c)		B1				
(c)	* Females	D.1				
	20 30 40 50 60 70 80 90	B1				
	Weight (kg)					
(d)	Any two from: The females are heavier than the males (on average). The males have lower median than females. The males have a smaller IQR than the females. The females have a greater range than males. [Comments just about skewness are B0]	(3) B1 B1				
	Notes	Total 11				
(a)	$1^{\text{st}} B1  \text{for } Q_2 = 54$ $2^{\text{nd}} B1  \text{for } Q_1 = 45$ $3^{\text{rd}} B1  \text{for } Q_3 = 59$					
(b)	M1 correct expression for either limit ft their values in (a)  1 <sup>st</sup> A1 80 and 24  2 <sup>nd</sup> A1ft all outliers identified using their limits (must be stated in (b))					
(c)	1 <sup>st</sup> B1 Box with whiskers drawn and Q <sub>2</sub> and quartiles ft from(a), condone 2 whiskers on RHS 2 <sup>nd</sup> B1 For only one lower whisker to 32 and no outliers 3 <sup>rd</sup> B1 For upper whisker to 80 <b>or</b> 77 and an outlier at 84 <b>NB</b> If there are whiskers at both 77 and 80 it is 3 <sup>rd</sup> B0					
(d)	1 <sup>st</sup> B1 a correct comparison on location e.g. median or comment implying "on average" 2 <sup>nd</sup> B1 a second correct comparison on spread e.g. range or IQR (greater spread is B0)					

Question	C.h	N/I 1			
Number	Scheme	Mark	KS		
3(a)	Width = 3 cm $1 \text{cm}^2$ represents 2 cars or $0.5 \text{cm}^2$ represents 1 car or their $h \times w = 6$ or area = 6	B1 M1			
	$Height = \frac{6}{3} = 2 \text{ cm}$	A1			
	30-28 $30.5-28$		(3)		
<b>(b)</b>	Median = $(2) + \frac{30 - 28}{15} \times 2$ or $(2) + \frac{30.5 - 28}{15} \times 2$ (o.e.)	M1			
	= 2.266 (or 2.33)	A1	(2)		
(c)	$\begin{bmatrix} \bar{t} = \end{bmatrix} \frac{182}{60} = 3.03$ $[\sigma_t = ] \sqrt{\frac{883}{60} - \bar{t}^2} = \sqrt{5.5155}$ $= 2.3485  (s = 2.3683)$ Mean > median	B1			
	$[\sigma_t = ] \sqrt{\frac{883}{60} - \bar{t}^2} = \sqrt{5.5155}$	M1			
	= 2.3485  (s = 2.3683)	A1	(3)		
(d)	Mean > median Positive skew	B1ft dB1	(3)		
	rositive skew	uD1	(2)		
(e)	[75 mins = 1.25 hours]		( )		
	$(>75 \text{ mins}) = 5 + 12 + 15 + \frac{3}{4} \times 18 = 45.5 \text{ or } (<75) = 10 + \frac{1}{4} \times 18 \text{ or } 28 - \frac{3}{4} \times 18$	M1			
	$P(T > 1.25) = \frac{45.5}{60}$ or e.g. $1 - \frac{14.5}{60}$	M1			
	0.7583 awrt <u>0.758</u>				
	Notes Total 13				
(a)	B1 3 only M1 may be implied by correct height A1 correct height of 2(cm) and correct width of 3 (cm)				
(b)	M1 for any correct equation leading to correct fraction as part of $m =$ or $(m - [2]) =$ Ignore incorrect end point and watch out for "working down"  A1 awrt 2.27 allow exact fraction e.g. $\frac{34}{15}$ (allow awrt 2.33 [ or $\frac{7}{3}$ ] if $n + 1$ used)				
(c)	B1 awrt 3.03 (allow exact fraction e.g. $\frac{91}{30}$ ) M1 A correct expression A1 awrt 2.35 or 2.37				
(d)	1 <sup>st</sup> B1 ft their mean and median (Allow "larger frequencies at the start of table"  Do not allow comparison of quartiles unless correct values are seen (2sf cor $Q_1 = 1.28$ or $\frac{23}{18}$ [ $(n+1) = 1.29$ ] $Q_3 = 4.33$ or $\frac{13}{3}$ [ $(n+1) = 4.42$ ] e.g. $2.1 > 0.99$ or $2^{\text{nd}}$ dB1 dependent on previous B1 being awarded.	npariso			

(e) 1<sup>st</sup> M1 for a correct expression for no. of cars longer than 75 mins or shorter than 75 mins

 $2^{\text{nd}} \text{ M1 } \frac{k}{60} \text{ where } 44 \leqslant k < 46$ 

A1 awrt 0.758 allow  $\frac{91}{120}$  (o.e.)

NB

Any use of the normal distribution is M0M0A0

Question	Scheme	Marks		
Number	0.13	B1		
4.(a)	0.13	(1)		
(b)	$P(A) \times P(C) = P(A \cap C)$	(1)		
(6)	0.05			
	$0.2 \times (0.08 + p) = 0.05  \underline{\mathbf{or}}  P(C) = \frac{0.05}{0.10 + 0.05 + 0.01 + 0.04}  \underline{\mathbf{or}}  \frac{0.05}{0.2}  \underline{\mathbf{or}}  0.25$	M1		
	p = 0.17	A1		
	P(no faults) = $1 - (0.1 + 0.05 + 0.01 + 0.04 + 0.08 + 0.03 + "0.17")$	M1		
	or $1 - [\text{``P(C)''} + 0.10 + 0.05 + 0.08]$	1411		
	q = 0.52	A1		
Ans only	They can get $q$ without finding $p$ so a correct answer to $q$ scores $4/4$			
		(4)		
(c)	P(Fault B but not fault C   Has fault A) = $\frac{0.05}{0.2}$	M1		
(c)				
	= 0.25	A1		
		(2)		
<b>(d)</b>	P(exactly 2 defects) = $0.12$ or $\frac{3}{25}$	B1		
	P(both have 2 defects) = $0.12^2$	M1		
	$= \underline{0.0144} \qquad \underline{\text{or}}  \frac{9}{625}$	A1		
		(3) <b>Total 10</b>		
(a)	Notes B1 0.13 only			
(a)				
(h)	1 <sup>st</sup> M1 using $P(A) \times P(C) = P(A \cap C)$ allow one addition error in $P(A)$ e.g. $P(A) = 0$	0.11		
(2)	1 <sup>st</sup> A1 0.17 only	-		
	$2^{\text{nd}}$ M1 $1-(0.10+0.05+0.01+0.04+0.08+0.03+\text{"their }0.17\text{"})$ allow letter $p$ for	or 0.17		
	or $1 - ["P(C)" + 0.10 + 0.05 + 0.08]$ but need a value for $P(C)$ [M0A0M1A0]			
	$2^{\text{nd}} \overline{\text{A1}}$ 0.52 only (correct answer of 0.52 with no incorrect working is 4/4)	. ,		
(c)	M1 for attempt at $P(B \cap C'   A)$ allow for $\frac{0.06}{0.2}$ or $\frac{0.05}{0.2}$ allow ft of their $P(A)$ use	ed in part(b)		
(C)	$\frac{1}{0.2}$ or attempt at $\frac{1}{0.2}$ (B) (B) (B) allow for $\frac{1}{0.2}$ or $\frac{1}{0.2}$ allow it of their $\frac{1}{0.2}$ (A) use	ca in part(b)		
	A1 0.25			
2 %				
(d)	B1 sight of 0.12 or $(0.05 + 0.03 + 0.04)$ only NB e.g. $0.12 \times 2$ is B1M0A0			
	M1 ("0.12") <sup>2</sup> where $0.1 <$ "0.12" $< 0.2$ May see attempt at $(0.05 + 0.03 + 0.04)^2$ multiplied out but must have $\ge 4$ corre	et products		
	r iviav see aucindi ai iv.v.j + v.v.j + v.v+) inuindheu our dur must nave 🥢 4 coffe	ci broducis		

A1 0.0144 (o.e.) (correct answer only scores 3/3)

Question	Scheme				Marks			
Number	Scheme				IVIAI KS			
5. (a)	$k = \frac{2}{35}$	$k = \frac{2}{35}$				B1		
	х	1	2	3	4	5	3.61	
	P(X=x) $P(X=x)$	$\frac{3}{35}$	$\frac{5}{35}$ or $\frac{1}{7}$		$\frac{9}{35}$	$\frac{11}{35}$	M1 A1	(3)
	P(X=x)	0.08571	0.14285	0.2	0.25714	0.31428	\	
(b)	$\frac{5}{35} + \frac{7}{35} = \frac{1}{3}$	$\frac{2}{5}$					M1 A1f	
		2 5	-	0 11	r 7		(	(2)
(c)	-			$\frac{9}{35} + 5 \times \frac{11}{35}$			M1	
	$E(X^{2}) = 1 \times \frac{3}{35} + 4 \times \frac{5}{35} + 9 \times \frac{7}{35} + 16 \times \frac{9}{35} + 25 \times \frac{11}{35} = \left[\frac{101}{7}\right]$					M1		
	Var $(X) = \frac{101}{7} - \left(\frac{25}{7}\right)^2$ ; $= \frac{82}{49}$ (allow 1.67~1.674)					M1; A1	-	
	$Var(12-7X) = 7^2 \times \frac{82}{49}$ ; = 82				M1; A1	:		
							(	(6)
(d)	$4X \le  Y  \text{ when } X = 1, 4 \text{ or } 5,$ so probability = " $\frac{3}{35}$ "+" $\frac{9}{35}$ "+" $\frac{11}{35}$ "					M1;A11	ft	
	$=\frac{23}{35}$					A1 (	(3)	
					`	,		
	Notes				Total 14	4		
(a)	B1 may be implied by a correct probability							
	M1 need $x$ values each with a prob and at least one correct prob.(Allow probs in terms of $k$ )					<i>k</i> )		
	A1 all values correct – accept decimals 3sf or better							

- **(b)** M1 "their P(X=2)" + "their P(X=3)"
  - ft providing < 1 Allow answer in [0.3428, 0.343] or 6kA1ft

(c)  $\int_{-\infty}^{\infty} |x|^{1} dx = \int_{-\infty}^{\infty} |x|^{2} dx =$ 

- $2^{\text{nd}} \text{ M1} \quad \text{using } \sum x^2 P(X = x) \quad \text{or} \quad \frac{101}{7} \quad \text{or} \quad \frac{505}{2} k \quad \text{or} \quad \sum y^2 P(Y = y) \qquad (\geqslant 4 \text{ correct terms or ft})$   $3^{\text{rd}} \text{ M1} \quad \text{using } \text{Var}(X) = \text{E}(X^2) [\text{ E}(X)]^2 \qquad \text{or} \quad \text{Var}(Y) = \text{E}(Y^2) [\text{ E}(Y)]^2$
- or  $Var(Y) = E(Y^2) [E(Y)]^2$
- 1<sup>st</sup> A1 for a correct answer (allow 3sf)
- <u>or</u> for  $E(Y^2) = 251$

 $4^{th}$  M1  $49 \times Var(X)$ 

<u>or</u> correct distribution for *Y* (ft probs from *X*)

- 2<sup>nd</sup> A1 for 82 only
- for X = 1, 4 or 5 [ or Y = 5, -16, -23] and at least one correct ft probability. (d) M1

their " $\frac{3}{35}$ "; + their " $\frac{9}{35}$ " + their " $\frac{11}{35}$ " providing sum is <1 (allow in terms of k) A1ft

**A**1 cao (allow  $\frac{23}{2}k$ )

Dist of Y

$y^2$	25	4	81	256	529
У	5	-2	<b>-9</b>	- 16	-23
P(X=x)	$\frac{3}{35}$	$\frac{5}{35}$ or $\frac{1}{7}$	$\frac{7}{35}$ or $\frac{1}{5}$	$\frac{9}{35}$	11/35

 $\mathbf{F}(x) = \mathbf{f}(x)$  Get  $k = \frac{2}{85}$  Can award: (a) 0/3 (b) M1A1ft (c) M4A0 (d) M1A1ftA0

**All in k** | Can award: (a) B0M1A0 (b) 2/2 in (c) M4A0 (d) M1A1ftA1

**Reverse** Y May see Y = 12 - 7(6 - X) used: in (c) can score M3 A0 probably zero in (d)

Question Number	Scl	Marks		
6. (a)	$P(L > 4.3) = P\left(Z > \frac{4.3 - 4.1}{0.125}\right)$	M1		
	$= P(Z > 1.6)  \underline{\text{or}}  1 - P(Z)$ = 0.0548	M1 A1 (3)		
(b)	P(3.9 < L < 4.3) = P(Z < 1.6) - P(Z < 0.9452 - 0.0548)	(-1.6) or $2(P(Z<1.6)-0.5)= 2(0.9452-0.5)$	D1aga	
	= 0.8904	= 0.8904	B1cso (1)	
(c)	Number of unusable bolts = $(1-0.89) \times 500$ [= 55]	$\frac{\text{Alternative}}{\text{E(value of a bolt)}} = 0.89 \times 9 + 0.11 \times 1$	M1oe	
	Value of bolts = "445"×9+"55"×1 profit = "445"×9+"55"×1 $-500$ ×5	E(profit per bolt)= $0.89 \times 9 + 0.11 \times 1 - 5$ Profit = "3.12"×500	M1oe M1oe	
	Profit from bolts = 1560 pence	Profit from bolts = 1560 pence	A1 (4)	
(d)	$\frac{4.198 - \mu}{\sigma} = 1.96$ or $4.198 - 4.065 - \mu$	$-\mu = 1.96\sigma$ <b>oe</b>	M1A1	
	$\frac{4.065 - \mu}{\sigma} = -0.7$ or $4.065 -$	$\mu = -0.7\sigma$ oe	A1	
	$0.133 = 2.66\sigma$ $\sigma = 0.05$ (or awrt 0.0500) $\mu = 4.1$ (or awrt 4.10)		M1 A1 A1 (6)	
(e)	The mean the same but the st. dev. dec	A1 (6) B1ft dB1ft		
	So the profit will increase  NB Use of + 0.7 in (c) $\rightarrow \mu = 3.99, \sigma$	(2) <b>Total 16</b>		
		otes		
. ,	$1^{\text{st}}$ M1 standardising. Allow use of $0$ $2^{\text{nd}}$ M1 $1-p$ $p > 0.8$ A1 awrt $0.0548$	.1252		
<b>(b)</b>	B1cso sight of 0.8904 or better (calc:	0.8904014212) or a correct subtraction	l	
, ,	$1^{\text{st}}  \text{M1}  (1 - \text{"0.89"}) \times 500  \text{or}  0.89 \times 9 + 0.11 \times 1$ $2^{\text{nd}}  \text{M1}  \text{"445"} \times 9 + \text{"55"}  \text{or}  0.89 \times 9 + 0.11 \times 1 - 5$ $3^{\text{rd}}  \text{M1}  \text{method for the profit}  \text{or}  \text{their}  \text{"3.12"} \times 500$ A1 for awrt £15.60 or 1560 pence(p) [need units]  SC think 55 scrap loses 1p $1^{\text{st}}  \text{M1}  \text{for sight of 55}$ B1 for answer of awrt 1450 p  Score as: M1M0M0A1			
	1 <sup>st</sup> M1 Forming either equation – must have z value but allow $\pm$ z where $ z  > 0.6$ 1 <sup>st</sup> A1 correct equation $4.198 - \mu = 1.96\sigma$ - any form (or allow $z = \text{awrt } 1.960$ ) 2 <sup>nd</sup> A1 correct equation $4.065 - \mu = -0.7\sigma$ - any form (or allow $z = \text{awrt } -0.700$ ) 2 <sup>nd</sup> M1 eliminating $\mu$ or $\sigma$ (method seen leading to equation in 1 variable) 3 <sup>rd</sup> A1 0.05 (or awrt 0.0500) 4 <sup>th</sup> A1 4.1 (or awrt 4.10 dep on 1 <sup>st</sup> or 2 <sup>nd</sup> A1)			
(e)	NB Candidate who assumes $\mu = 4.1$ 1 <sup>st</sup> B1ft if $\mu = 4.1$ then ft $\sigma$ ; if $\mu < 3.9$ If they have $\mu = 4.1$ in part (d) then 2 <sup>nd</sup> dB1ft therefore profit will increase			