

Mark Scheme (Results)

January 2023

Pearson Edexcel International Advanced Level In Statistics S3 (WST03) Paper 01

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## **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### PEARSON EDEXCEL IAL MATHEMATICS

## **General Instructions for Marking**

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:

#### 'M' marks

These are marks given for a correct method or an attempt at a correct method. In Mechanics they are usually awarded for the application of some mechanical principle to produce an equation. e.g. resolving in a particular direction, taking moments about a point, applying a suvat equation, applying the conservation of momentum principle etc.

The following criteria are usually applied to the equation.

## To earn the M mark, the equation

- (i) should have the correct number of terms
- (ii) be dimensionally correct i.e. all the terms need to be dimensionally correct
- e.g. in a moments equation, every term must be a 'force x distance' term or 'mass x distance', if we allow them to cancel 'g' s.

For a resolution, all terms that need to be resolved (multiplied by sin or cos) must be resolved to earn the M mark.

M marks are sometimes dependent (DM) on previous M marks having been earned. e.g. when two simultaneous equations have been set up by, for example, resolving in two directions and there is then an M mark for solving the equations to find a particular quantity – this M mark is often dependent on the two previous M marks having been earned.

## 'A' marks

These are dependent accuracy (or sometimes answer) marks and can only be awarded if the previous M mark has been earned. E.g. M0 A1 is impossible.

## 'B' marks

These are independent accuracy marks where there is no method (e.g. often given for a comment or for a graph)

A few of the A and B marks may be f.t. – follow through – marks.

## 3. General Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:

  If all but one attempt is crossed out, mark the attempt which is NOT crossed out.

  If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

# **Special notes for marking Statistics exams (for AAs only)**

- Any correct method should gain credit. If you cannot see how to apply the mark scheme but believe the method to be correct then please send to review.
- For method marks, we generally allow or condone a slip or transcription error if these are seen in an expression. We do not, however, condone or allow these errors in accuracy marks.

Question		Scheme		Marks			
1 (a)(i)	Metl		Method 2	1/14/113			
	$[\overline{y} =$	$\left[\frac{847}{100}\right] = 8.47$	847+100×1000 [=100847]	M1			
	So $\bar{x}$	$\overline{\epsilon} = 1000 + \frac{847}{100} = 1008.47 *$	$\overline{x} = \frac{847 + 1000 \times 100}{100} = 1008.47$ *	A1*			
(ii)	$\left[ S_{x}^{2} \right]$	$\left[s_x^2\right] = \frac{101707510.1 - \frac{"100847"^2}{100}}{99}$	M1				
		= 64		A1			
				(4)			
(b)	$H_0$ :	$\mu_x = 1010$ $H_1: \mu_x \neq 1010$		B1			
	77	1010 7 1010		(1)			
(c)	$\frac{\overline{X} - 1010}{"8" / \sqrt{100}} = -1.9$ oe $\frac{\overline{X} - 1010}{"8" / \sqrt{100}} = 1.96$ oe						
		1008.432 $\bar{X} = 1011.568$ awr		A1			
	$\overline{X} \leqslant "1008.432"$ $\overline{X} \geqslant "1011.568"$						
				(4)			
(d)	1008.47 is not in the critical region						
	The machine does not need to be stopped /reset						
(e)	It is	reasonable since the sample size is	(reasonably) large	B1 (2)			
(0)	it is reasonable since the sample size is (reasonably) large						
	Notes						
(a)(i)	M1	For 8.47 or $\frac{847}{100}$ or $847 + 100 \times 1$	000 or $847 = \sum x - 100 \times 1000$ or 100847 seen				
	A1*	cso correct solution including $\overline{x} =$ y and must not be just $x \in E(X)$ , $\mu_x$	and=1008.47 allow alt notation for $\overline{x}$ but must refine an of $x$	fer to x not			
(ii)	M1	For a correct expression ft their 1008	47 Allow for answer of 1064				
	A1	Cao do not ISW Allow 64.00					
(b)	B1	Both hypotheses correct. Must be in t	terms of $\mu$ . (Allow $H_0: \mu_y = 10  H_1: \mu_y \neq 10$ )				
		Mark (c) and (d) together					
(c)	M1 For $\pm$ standardisation with 1010 and their sd. Allow equivalent eg. $1010 \pm n \times "8" / \sqrt{100}$ SC condone use of 1008.47 for 1010 or for $\bar{X}$						
	B1	For c.v. = $\pm 1.96$ or better seen (Calca one tail hypotheses in (b)	culator gives 1.95996) Condone 1.6449 or better if	they have			
	A1 For both limits 1008 or better and 1012 or better seen. (condone 1011from correct working)						
	A1	letters(condone $\mu$ ) Allow other notar	ir figures (not z value). Allow use of $<$ and $>$ also allow tion eg [1012, $\infty$ ], ( $\infty$ , 1008] allow [1012, $\infty$ ], [ $\infty$ ,	1008]			
(d)	d) If their CR if the final A mark in part (c) is awarded. For a correct comment compatible w CR. Must refer to $1008.47$ (allow mean of x) is in or out of their CR Allow writing in the form " $1008.432$ " $< 1008.47 < "1011.568$ " etc but if in middle it must ends. If no clear CR it is M0A0						
	dep on M1 awarded. Correct conclusion consistent with comparing 1008.47 with their CR( allow interval/ range etc). If it is in the CR they must say it needs to be reset/stopped. If it is not in the C it must say it does not need to be stopped/reset. (allow equivalent wording)						

	SC	If the CR in (c) is of the form "1008.432" $< \bar{X} <$ "1011.568" oe (not z values) then award M0A1 for concluding the machine does not need to be stopped/reset.
(e)	<b>B1</b>	Any suitable comment about the sample being large eg $n$ is large

Question			S	Scheme							Marks
	Athl	ete	A	В	C	D	E	F	G	Н	
2 (a)		k SBT	4	2	1	3	5	6	8	7	M1
_ (u)	FP	~	1	2	3	4	5	6	7	8	1,11
		=9+0+4+1-					1 2			U	M1
					10]					4.0.01	
	$r_s = 1$	- \frac{6("16")}{8(63)}	= 0.8095	)						awrt 0.81	dM1 A1 (4)
(1-)	H · a = 0 H · a > 0										
(b)	$H_0: \rho = 0$ , $H_1: \rho > 0$ Critical Value $r_s = 0.8333$ or CR: $r_s \ge 0.8333$										B1
							•.•			•	B1
		ot reject H <sub>0</sub> or no nce of a positive			does not	lie in th	e critica	region	or there	is no	M1
		is no evidence			rrelation	betwee	n seasoi	's best	time and	d finishing	4.1.0
		on for these ath	_								A1ft (4)
(c)	r = -	$\frac{0.225175}{0.1286875 \times 0.5}$	55275								M1
	1	0.12868/3×0.3 84428	03213							awrt 0.844	A1
	0.0	71120								uwit 0.011	(2)
(d)	Critical Value $r = 0.7887$ or CR: $r \ge 0.7887$							M1			
	so there is evidence of a positive correlation between season's best time and finishing									finishing	A1 ft
	time	for these athlete	S								(2)
					Note	es					Total 12
(a)	M1	attempt to rank	seasonal	best time			rect), Ma	y be impl	lied by \(\sum_{\text{inition}}\)	$\int d^2 = 16$	
_	N/1	Attempt to find	the diffe	rence bet	ween eac	h of the	ranks (a	t least 3 o	correct) a	nd evaluatin	$g \sum d^2$
	M1	May be implied	by awrt	0.81 NB	if no ran	ks for SE	T it is M	0			
	dM1	<b>dM1</b> dependent on 1 <sup>st</sup> M1. Using $1 - \frac{6\sum d^2}{8(63)}$ with their $\sum d^2$									
	A1	$\frac{17}{21}$ or awrt 0.8	31(0)								
	SC	for reverse rankings									
(1.)	D1								looks lik	e rho eg p).	Must be
(b)	<b>B1</b> both hypotheses correct. Must be in terms of $\rho$ (allow something that looks like rho eg $\rho$ attached to H <sub>0</sub> and H <sub>1</sub>							01/			
	B1	critical value of		Sign sl	hould ma	tch there	$H_1$ or $r_s$				
		correct statemen	nt compa	ring their	CV with	their $r_s$	- no con	text need	ed but do	not allow	
	M1	contradicting no	on contex	tual com	ments. If	no CV o	r test stat	istic give	en or the	test value  o	r  CV  > 1
	then it is M0								Conclusia	mayat === f- ::	
	A1ft correct conclusion in context for their value of $r_s$ from (a) and their stated CV. Conclusion positive correlation seasonal best or time and position							Conclusion	must reter		
		to <b>positive correlation</b> , <b>seasonal best</b> or <b>time</b> and <b>position</b> .  For use of two-tailed test:									
	SC	May score B0B			v 0.881.	.)					
(c)	M1	correct method									
	<b>A1</b> awrt 0.844										
(d)	M1	Critical value of	f 0.7887	Allow 0.3	8343 if h	vnothese	s are two	tailed in	(h)		

M1 must be awarded. A correct conclusion for their value of r from (c) Conclusion must refer to **A1ft positive correlation**, **seasonal best** or **time** and **finishing time**. Do not allow contradicting comments. if the |test value| or |CV| > 1 then it is M0

Question			Scheme		Marks			
	86×3	×300 1114×300						
3 (a)	120	or						
		and 278.5						
	21.0	and 276.5						
(1.)	H <sub>0</sub> : M	Making a claim and age are independent (not associated)						
(b)		Molving a claim and against not independent (agas sixted)						
		Observed	Expected	$\frac{(O-E)^2}{E}$				
		Observed Expected $\frac{(O-E)^2}{E}$ 14 "21.5" $\frac{(14-"21.5")^2}{"21.5"} = 2.6162$ 286 "278.5" $\frac{(286-"278.5")^2}{"278.5"} = 0.20197$						
		286	"278.5"	$\frac{(286 - "278.5")^2}{"278.5"} = 0.20197$				
	$\sum_{i=1}^{n}$	$\frac{(O-E)^2}{E} = 7.123 + $	- "2.616"+ "0.2019	1	M1			
		9.941		aw	vrt 9.94 A1			
	v = (2	(2-1)(3-1) = 2			B1			
	$\chi_2^2(0.$	$01) = 9.210 \implies C$	CR: $X^2 \ge 9.21[0]$		B1ft			
		e CR/significant/Reject H <sub>0</sub> ] There is sufficient evidence to suggest that making a is not independent of age.						
					(7)			
				otes	Total 9			
(a)	M1			eted value. Implied by one correct value.				
	A1		for both 21.5 and 278.5		. 1 . 1 . 22			
(b)	B1		eses correct. Must men "connection" is B0	tion claim and age at least once. Use of "	relationship" or			
	M1	A correct method for finding both contributions to the $\chi^2$ value or awrt 2.62 or awrt 0.202 Al						
	1411	truncated answers of 2.61 and 0.201 May be implied by awrt 9.94						
	M1	Adding their two	o values to 7.123 (may	be implied by a full $\chi^2$ calculation, with	at least 3 correct			
	1411	expressions or values. Do not ISW)						
	A1	awrt 9.94						
	B1	v = 2 This mark can be implied by a correct critical value of 9.21 or better						
	B1ft							
	dA1ft Independent of hypotheses but dependent on both M marks being awarded. We will ft their test statistic and CV only. A correct contextual conclusion compatible with their values, which has the words claim and age. eg if they have 11.345 and 9.94 they should say it is independent/ not associated. Do not allow contradicting statements.							
Full calcul				2	2			
(24-1)	$(4,33)^2$	$(176 - 185 67)^2$	$(48-50.17)^2$ (6)	$52-649.83)^2 (14-"21.5")^2 (286-$	_"278 5"\ <sup>2</sup>			

$$eg \frac{(24-14.33)^2}{14.33} + \frac{(176-185.67)^2}{185.67} + \frac{(48-50.17)^2}{50.17} + \frac{(652-649.83)^2}{649.83} + \frac{(14-"21.5")^2}{21.5} + \frac{(286-"278.5")^2}{278.5}$$

or awrt 6.52 + awrt 0.5 + awrt 0.09 + awrt 0.01 + awrt 2.62 + 0.20

or 
$$\frac{24^2}{14.33} + \frac{176^2}{185.67} + \frac{48^2}{50.17} + \frac{652^2}{649.83} + \frac{14^2}{"21.50"} + \frac{286^2}{"278.5"} - 1200$$

or awrt 40.19 + awrt 166.83 + awrt 45.92 + awrt 654.17 + awrt 9.116 + awrt 293.702 – 1200

Quest	ion	Scheme					
4 (a	a)	$H_0$ : B(4, 0.5) is a suitable model	D1				
		$H_1: B(4, 0.5)$ is not a suitable model	B1				
		Expected frequencies 12.5, 50, 75, 50, 12.5	M1 A1				
		$(O-E)^2 (15-"12.5")^2 (10-"12.5")^2$					
		$\sum \frac{(O-E)^2}{E} = \frac{(15 - "12.5")^2}{"12.5"} + \dots + \frac{(10 - "12.5")^2}{"12.5"}$	) / (1				
		2 12.0	M1				
		or $\sum \frac{O^2}{E} - N = \frac{15^2}{"12.5"} + + \frac{10^2}{"12.5"} - 200$					
		= 10.84 (or 10.8)	A1				
		$\nu = 4$	B1				
		$\chi_4^2(0.05) = 9.488  \Rightarrow CR \geqslant 9.488$	B1				
		Sufficient evidence to say that the research students claim is not supported	A1ft				
			(8)				
(b)	)	$[0 \times 15 + ]1 \times 68 + 2 \times 69 + 3 \times 38 + 4 \times 10[= 360]$	M1				
		$\frac{360}{200\times4} = 0.45 *$	A1*				
		200×4					
(c)	\ \ \	H <sub>0</sub> : Binomial is a suitable model	(2)				
		·	B1				
	_	$H_1$ : Binomial is not a suitable model $v = 3$	D1				
	_		B1 B1ft				
	_	$\chi_3^2(0.05) = 7.815 \implies CR \geqslant 7.815$					
		No significant evidence to say that the binomial is not a reasonable model	B1ft				
1			(4)				
		Notes	(4) <b>Total 14</b>				
(a)	B1	Notes  Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)	Total 14				
(a)		Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial,	Total 14				
(a)	B1 M1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200[=12.5]$ or	Total 14				
(a)		Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)	Total 14				
(a)	M1 A1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200[=12.5]$ or $4 \times 0.5^4 \times 200[=50]$ or $6 \times 0.5^4 \times 200[=75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if need)	Total 14				
(a)	M1 A1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 [= 12.5]$ or $4 \times 0.5^4 \times 200 [= 50]$ or $6 \times 0.5^4 \times 200 [= 75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$	Total 14				
(a)	M1 A1 M1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 [= 12.5]$ or $4 \times 0.5^4 \times 200 [= 50]$ or $6 \times 0.5^4 \times 200 [= 75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8	Total 14				
(a)	M1 A1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 [= 12.5]$ or $4 \times 0.5^4 \times 200 [= 50]$ or $6 \times 0.5^4 \times 200 [= 75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$	Total 14				
(a)	M1 A1 M1 A1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 [= 12.5]$ or $4 \times 0.5^4 \times 200 [= 50]$ or $6 \times 0.5^4 \times 200 [= 75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8	Total 14				
(a)	M1 A1 M1 A1 B1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 [= 12.5]$ or $4 \times 0.5^4 \times 200 [= 50]$ or $6 \times 0.5^4 \times 200 [= 75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8 $v = 4$ This mark can be implied by a correct critical value of 9.488	Total 14				
(a)	M1 A1 M1 A1 B1 B1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 = 12.5$ or $4 \times 0.5^4 \times 200 = 50$ or $6 \times 0.5^4 \times 200 = 75$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8 $v = 4$ This mark can be implied by a correct critical value of 9.488  9.488 ft their degrees of freedom if given. For $v = 3$ it is 7.815  Dep on the $2^{\text{nd}}$ M1. independent of hypotheses. Need claim or student or binomial. ft their CV ar statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (	rotal 14  eded)  and their test (Allow in				
(a)	M1 A1 M1 A1 B1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200[=12.5]$ or $4 \times 0.5^4 \times 200[=50]$ or $6 \times 0.5^4 \times 200[=75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8 $v = 4$ This mark can be implied by a correct critical value of 9.488  9.488 If their degrees of freedom if given. For $v = 3$ it is 7.815  Dep on the $2^{nd}$ M1. independent of hypotheses. Need claim or student or binomial. If their CV are statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (terns of Binomial eg does not follow a binomial distribution) If their Test statistic > their CV the	eded) and their test (Allow in en must say				
	M1 A1 M1 A1 B1 B1 A1ft	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200[=12.5]$ or $4 \times 0.5^4 \times 200[=50]$ or $6 \times 0.5^4 \times 200[=75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8 $v = 4$ This mark can be implied by a correct critical value of 9.488  9.488 If their degrees of freedom if given. For $v = 3$ it is 7.815  Dep on the $2^{\text{nd}}$ M1. independent of hypotheses. Need claim or student or binomial. If their CV are statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (terns of Binomial eg does not follow a binomial distribution) If their Test statistic > their CV then ot supported (not binomial). If their Test statistic < their CV then must say supported (is binomial).	eded) and their test (Allow in en must say				
(a)	M1 A1 M1 A1 B1 B1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200[=12.5]$ or $4 \times 0.5^4 \times 200[=50]$ or $6 \times 0.5^4 \times 200[=75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8 $v = 4$ This mark can be implied by a correct critical value of 9.488  9.488 If their degrees of freedom if given. For $v = 3$ it is 7.815  Dep on the $2^{nd}$ M1. independent of hypotheses. Need claim or student or binomial. If their CV are statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (terns of Binomial eg does not follow a binomial distribution) If their Test statistic > their CV the	eded) and their test (Allow in en must say				
(b)	M1 A1 M1 A1 B1 B1 A1ft	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 [= 12.5]$ or $4 \times 0.5^4 \times 200 [= 50]$ or $6 \times 0.5^4 \times 200 [= 75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8 $v = 4$ This mark can be implied by a correct critical value of 9.488  9.488 If their degrees of freedom if given. For $v = 3$ it is 7.815  Dep on the $2^{nd}$ M1. independent of hypotheses. Need claim or student or binomial. If their CV at statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (terns of Binomial eg does not follow a binomial distribution) If their Test statistic > their CV the not supported (not binomial). If their Test statistic < their CV then must say supported (is binomial) accorrect method for finding the total number of girls. At least 3 non zero terms correct. useful figures $[0] + 68 + 138 + 114 + 40$ . Implied by 360 or 1.8  cso allow for 360/800 or 1.8/4 or 1.8 = 4 $p$	rotal 14  eded)  and their test (Allow in en must say mial)				
	M1 A1 B1 A1ft M1 A1* B1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 [= 12.5]$ or $4 \times 0.5^4 \times 200 [= 50]$ or $6 \times 0.5^4 \times 200 [= 75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8 $v = 4$ This mark can be implied by a correct critical value of 9.488  9.488 If their degrees of freedom if given. For $v = 3$ it is 7.815  Dep on the $2^{\text{nd}}$ M1. independent of hypotheses. Need claim or student or binomial. If their CV at statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (terns of Binomial eg does not follow a binomial distribution) If their Test statistic > their CV then to supported (not binomial). If their Test statistic < their CV then must say supported (is binomial) a correct method for finding the total number of girls. At least 3 non zero terms correct. useful figures $[0] + 68 + 138 + 114 + 40$ . Implied by 360 or 1.8  cso allow for $360/800$ or $1.8/4$ or $1.8 = 4p$ Both hypotheses correct. Must mention binomial at least once. Condone inclusion of B(4,0.45)/Both	rotal 14  reded)  and their test (Allow in en must say mial)				
(b)	M1 A1 M1 B1 B1 A1ft M1 A1* B1 B1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200 [= 12.5]$ or $4 \times 0.5^4 \times 200 [= 50]$ or $6 \times 0.5^4 \times 200 [= 75]$ May be implied by correct answer 10.84 or 10.8  For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer 10.84 or 10.8  10.84 Allow 10.8 $v = 4$ This mark can be implied by a correct critical value of 9.488  9.488 ft their degrees of freedom if given. For $v = 3$ it is 7.815  Dep on the $2^{nd}$ M1. independent of hypotheses. Need claim or student or binomial. ft their CV at statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (terns of Binomial eg does not follow a binomial distribution) If their Test statistic > their CV then of Supported (not binomial). If their Test statistic < their CV then must say supported (is binonal A correct method for finding the total number of girls. At least 3 non zero terms correct. useful figures $[0] + 68 + 138 + 114 + 40$ . Implied by 360 or 1.8  cso allow for $360/800$ or $1.8/4$ or $1.8 = 4p$ Both hypotheses correct. Must mention binomial at least once. Condone inclusion of B(4,0.45)/B( $v = 3$ This mark can be implied by a correct critical value of 7.815 Condone (their $v$ in part(a) $v = 3$ This mark can be implied by a correct critical value of 7.815 Condone (their $v$ in part(a) $v = 3$ This mark can be implied by a correct critical value of 7.815 Condone (their $v$ in part(a) $v = 3$ This mark can be implied by a correct critical value of 7.815 Condone (their $v$ in part(a) $v = 3$ This mark can be implied by a correct critical v	rotal 14  reded)  and their test (Allow in en must say mial) (0.45,4)				
(b)	M1 A1 B1 B1 A1ft M1 B1 B1 B1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200[=12.5]$ or $4 \times 0.5^4 \times 200[=50]$ or $6 \times 0.5^4 \times 200[=75]$ May be implied by correct answer $10.84$ or $10.8$ For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer $10.84$ or $10.8$ $10.84$ Allow $10.8$ $v = 4$ This mark can be implied by a correct critical value of $9.488$ $9.488$ ft their degrees of freedom if given. For $v = 3$ it is $7.815$ Dep on the $2^{nd}$ M1. independent of hypotheses. Need claim or student or binomial. If their CV ar statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (terns of Binomial eg does not follow a binomial distribution) If their Test statistic $>$ their CV the not supported (not binomial). If their Test statistic $<$ their CV then must say supported (is binon A correct method for finding the total number of girls. At least 3 non zero terms correct. useful figures $[0] + 68 + 138 + 114 + 40$ . Implied by $360$ or $1.8$ cso allow for $360/800$ or $1.8/4$ or $1.8 = 4p$ Both hypotheses correct. Must mention binomial at least once. Condone inclusion of B(4,0.45)/Bi $v = 3$ This mark can be implied by a correct critical value of $7.815$ Condone (their $v$ in part(a) $-7.815$ ft their degrees of freedom if they have (their $v$ in part(a) $-1$ ).	rotal 14  reded)  and their test (Allow in en must say mial)  (0.45,4)  - 1)				
(b)	M1 A1 M1 B1 B1 A1ft M1 A1* B1 B1	Both hypotheses correct. Must mention B(4,0.5) at least once. (may be in words need Binomial, probability $(p) = 0.5$ and a reference to 4 children or $n = 4$ ) Condone B(0.5, 4)  For a correct method to find at least one expected frequency e.g. $0.5^4 \times 200[=12.5]$ or $4 \times 0.5^4 \times 200[=50]$ or $6 \times 0.5^4 \times 200[=75]$ May be implied by correct answer $10.84$ or $10.8$ For all 5 expected frequencies correct. These must be seen and cannot be implied.  For an attempt at the test statistic, at least 2 correct expressions/ values seen (include $-200$ if nee $\sum \frac{(O-E)^2}{E} = 0.5 + 6.48 + 0.48 + 2.88 + 0.5$ or $\sum \frac{O^2}{E} - N = 18 + 92.48 + 63.48 + 28.88 + 8 - 200$ May be implied by correct answer $10.84$ or $10.8$ $10.84$ Allow $10.8$ $v = 4$ This mark can be implied by a correct critical value of $9.488$ $9.488$ ft their degrees of freedom if given. For $v = 3$ it is $7.815$ Dep on the $2^{nd}$ M1. independent of hypotheses. Need claim or student or binomial. If their CV ar statistic only. A correct conclusion based on their test statistic value and their $\chi^2$ critical value (terns of Binomial eg does not follow a binomial distribution) If their Test statistic $>$ their CV the not supported (not binomial). If their Test statistic $<$ their CV then must say supported (is binon A correct method for finding the total number of girls. At least 3 non zero terms correct. useful figures $[0] + 68 + 138 + 114 + 40$ . Implied by $360$ or $1.8$ cso allow for $360/800$ or $1.8/4$ or $1.8 = 4p$ Both hypotheses correct. Must mention binomial at least once. Condone inclusion of B(4,0.45)/Bi $v = 3$ This mark can be implied by a correct critical value of $7.815$ Condone (their $v$ in part(a) $-7.815$ ft their degrees of freedom if they have (their $v$ in part(a) $-1$ ).	rotal 14  reded)  and their test (Allow in en must say mial)  (0.45,4)  - 1)				

Question		Scheme	Marks						
5 (a)		$: \mu_A = \mu_B$	B1						
3 (u)		$: \mu_A > \mu_B$ oe							
	CO	$se = \sqrt{\frac{17.8^2}{50} + \frac{18.4^2}{40}}$							
		<u> </u>	M1						
	7 =	<u>+ 1377 – 1368</u>							
		$17.8^2 \cdot 18.4^2$	M1						
	$z = \pm \frac{1377 - 1368}{\sqrt{\frac{17.8^2}{50} + \frac{18.4^2}{40}}}$								
	$=\pm 2.339$ awrt $\pm 2.34$								
	On	e tailed c.v. $ Z  = 2.3263$ or CR: $Z \le -2.3263$ or $Z \ge 2.3263$	B1						
	In	CR/Significant/Reject H <sub>0</sub>	dM1						
	Su	fficient evidence to support that the mean $\underline{\text{vield}}$ from plants using fertiliser $\underline{A}$ is	A1ft						
	gre	eater than the mean <u>yield</u> from plants using fertiliser <u>B</u>							
ALT	fi.,	ding the CI can get D1M1M1A0D1M1A1 unless test statistic given	(7)						
ALI	1111	ding the CI can get B1M1M1A0B1M1A1 unless test statistic given							
	aw	ard M1 for $z = \pm \frac{D}{\sqrt{\frac{17.8^2}{50} + \frac{18.4^2}{40}}}$ dep on first M1 where $2.3 \le z \le 2.4$							
		$\sqrt{\frac{17.8}{50} + \frac{18.4}{40}}$							
		by be implied by $ D  = 8.949$							
(b)		pected profit per plant							
	Α.	$3 \times 1 \ 377 - \frac{75}{}$ $R: 3 \times 1 \ 368 - \frac{50}{}$	M1						
		$\frac{3 \times 1.377 - \frac{75}{50}}{82.62(1)} B: 3 \times 1.368 - \frac{50}{40}$							
	<i>A</i> :	£2.63(1) B: £2.85(4)	Al						
	Cla	aire should use fertiliser B	dA1 (3)						
		Notes	Total 10						
(a)	<b>B</b> 1	Both hypotheses correct. Allow equivalent hypotheses. Must be in terms of $\mu$ If A and B not use the degree of $\mu$ If A a	used the						
` '		letter must be defined  For a correct attempt to find the se or se <sup>2</sup> Condone slip in sample sizes May be implied by							
	M1	se = awrt 3.85 or se <sup>2</sup> = awrt 14.8. Allow for a $p$ -value of 0.0096 or awrt 0.0097							
	M1	For an attempt to find z value. Allow slip in sample sizes and/or use of 17.8 and 18. 4 rather the same $\frac{1}{2}$ and $\frac{1}{2}$	han 17.8 <sup>2</sup>						
	<b>A1</b>	and 18. $4^2$ Allow for a <i>p</i> -value of 0.0096 or awrt 0.0097 awrt = $\pm 2.34$ Allow for a <i>p</i> -value of 0.0096 or awrt 0.0097							
	B1	$\pm$ 2.3263 or better seen (Calculator gives 2.3263479) must be compatible with their test star	tistic						
	DI	dep on previous dM1 awarded, ft their test statistic and CV only. A correct statement compat							
	dM1	their test statistic and CV only - need not be contextual but do not allow contradicting non co							
		comments.  ft their z value and CR only. A correct contextual statement compatible with their test statistic	and CV						
.	A1ft	with context of yield (at least once) and A and B	anu CV						
		NB id they give a <i>p</i> -value of awrt 0.0096/7 they could get B1M1dM1A1B0dM1A1							
	A correct method to find the profit per $n$ plants or $m$ kg for either fertiliser $A$ or fertiliser $B$								
(b)	<b>M1</b> $n(3\times1.377-75/50)$ or $n(3\times1.368-50/40)$ or $m(3-75/50\times1.377)$ or $m(3-50/(40\times1.368))$								
		where $n$ and $m \neq 0$ Implied by one correct value for $A$ or $B$							
		must have 2 values which can be compared. ie using same $n$ or $m$ . Profit per $n$ plant £2.63(1) $n$ and							
	£2.85(4) n or profit per m kg awrt £1.91 m and awrt £2.09 m (2dp) or cost per m kg awrt £1. awrt £0.91 m or number plants per £1, awrt $0.38$ y and awrt $0.35$ y								
	dA1								
		Useful numbers ( $n = 50$ gives profit 131.55, 142.7) or ( $n = 40$ gives profits105.24 and 114.16) gain M1A							

Question	Scheme						
6 (a)	$\overline{x} = \frac{8}{3}$	$\frac{06.4}{36} = ]22.4$	B1				
	"22.4" $\pm$ 2.3263 $\times \frac{0.4}{\sqrt{36}}$						
	(22.24, 22.55) awrt (22.2, 22.6)						
	NB answers which are awrt (22.2, 22.6) gain full marks						
	F		(4)				
(b)	[The Central Limit Theorem is not required as] the original population is <b>normally</b> distributed						
	22.5:		(1)				
(c)		within the confidence interval	B1 ft				
	So no r	reason to doubt the manufacturers claim	dB1 ft				
			(2)				
(d)	$\overline{Y} \sim N$	$\left(850, \left(\frac{5}{\sqrt{10}}\right)^2\right)$	B1				
	$P(\overline{Y} < 848) = P\left(Z < \frac{848 - 850}{\frac{5}{\sqrt{10}}}\right) = [P(Z < -1.26)]$						
		= 0.1038 (Calculator gives $0.10295$ ) awrt $0.103 / 0.104$	A1 (3)				
ALT	N(8500	250)	B1				
	`	$848) = P\left(Z < \frac{8480 - 8500}{\sqrt{250}}\right) = [P(Z < -1.26)]$	M1				
		= 0.1038	A1				
(a)	D1	Notes For 22.4	Total 10				
(a)	B1						
	M1	For use of $\overline{x} \pm z$ value $\times \frac{\sigma}{\sqrt{n}}$ with $1.2 < z < 2.6$					
	B1	For z value = $2.3263$ or better seen (Calculator gives $2.3263479$ )					
	A1	awrt (22.2, 22.6) This does not imply the B1					
(b)	B1	For reference to the data is modelled by <b>normal distribution</b>					
(c)	B1 ft ft their CI For a comment on whether 22.5 (or it) is or is not in their CI allow eg range for CI Allow "22.24" < 22.5 < " 22.6" Answer must be compatible with their CI						
	dB1 ft	Dependent on B1 ft. For a correct comment ft their CI eg claim is correct oe					
(d)	for $\overline{Y} \sim N(850,)$ or $\overline{Y} < \frac{848 - 850}{5}$ Must have $\overline{Y}$ or $N\left(850, \left(\frac{5}{\sqrt{10}}\right)^2\right)$ or $N(850,2.5)$ seen used or $N(8500,250)$ seen or used. Both implied by a correct standardisation.						
	M1	For $\pm$ (a correct standardisation) implied by a correct answer					
	A1	awrt 0.103 to 0.104					
	•	·					

Question		Scheme	Marks						
7 (a)	Let $P = t$	time to serve a customer at a standard checkout							
	$Q = P_1 +$	$[Q \sim] N(720,1200)$	B1						
	$P(Q < 660) = P\left(Z < \pm \frac{660 - "720"}{"\sqrt{1200"}}\right) [= P(Z < -1.732)]$								
	= 0.0418 (Calculator gives 0.04163) <u>awrt 0.041 / 0.042</u>								
A T 7T	for the B1 M1								
ALT									
	B1 for	$[Q \sim] N\left(12, \frac{1}{3}\right)$							
	M1 for	$P(Q < 11) = P\left(Z < \pm \frac{11 - "12"}{\sqrt{"\frac{1}{3}"}}\right) [= P(Z < -1.732)]$							
		$(\sqrt{3})$							
(b)	Assume	the time taken to serve customers is independent	B1 (1)						
(c)	P - time	to serve a customer at an express checkout	(1)						
		$(S_1)^2 + (R_1 + R_2)^2 + (R$	M1 A1						
			1411 741						
	P(S>0)	$= P\left(Z > \pm \frac{0-20}{\sqrt{1648}}\right) \left[= P\left(Z > -0.492\right)\right]$	M1						
		9 (Calculator gives 0.6888) <u>awrt 0.688 / 0.689</u>	A1						
ALT		M1A1M1							
	M1 for 1	$N\left(\frac{1}{2}\right)$							
		(3,)							
		$I\left(\frac{1}{3},\frac{103}{225}\right)$							
	M1 C	$0 - \frac{1}{3}$							
	MI for ±	M1 for $\pm \frac{0 - \frac{1}{3}}{\sqrt{103/225}}$ "							
		V /225	(4)						
		Notes	(4) <b>Total 8</b>						
			100010						
(a)	B1	For N(720,1200) or N $\left(12,\frac{1}{3}\right)$ Maybe awarded if used in standardisation							
	M1	For standardising using 660, their mean ≠ 240 or 4 and their standard deviation ≠ 20 or	3						
	A 1	distribution given the mean and sd must be correct in the standardisation. Allow $\pm$ stand							
(1)	A1	awrt 0.041 or awrt 0.042	1 )						
(b)	B1	A correct assumption. Must have context of customers or time and independence(allow	v random)						
(c)	M1	For N( $\pm 20$ ,) or N $\left(\frac{1}{3}$ ,) maybe awarded in standardisation							
	A1	For N(±20, 1648) or N $\left(\frac{1}{3}, \frac{103}{225}\right)$ maybe awarded if used in standardisation							
	M1	For standardising using 0 and mean of $\pm 20$ or $\pm 1/3$ and their standard deviation. The	0 may be						
	A1	implied by having just the mean on the numerator Allow $\pm$ stand awrt 0.688 to 0.689							