Please check the examination de	etails below before ente	ering your candidate information	
Candidate surname		Other names	
Centre Number Cand	idate Number		
Pearson Edexcel Inter	rnational Ad	lvanced Level	
<b>Time</b> 1 hour 30 minutes	Paper reference	WFM01/0	1
Mathematics		0	•
	ad Cubaidiam	ne/ Adress and Lovel	
International Advanc	,	y/ Advanced Level	
Further Pure Mathem	atics F1		
You must have: Mathematical Formulae and St.	atistics Tables (Yell	low), calculator	arks

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use black ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
  - there may be more space than you need.
- You should show sufficient working to make your methods clear.
   Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

#### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ▶







1. Given that

$$\mathbf{A} = \begin{pmatrix} 2 & -1 & 3 \\ -2 & 3 & 0 \end{pmatrix} \quad \text{and} \quad \mathbf{B} = \begin{pmatrix} 1 & k \\ 0 & -3 \\ 2k & 2 \end{pmatrix}$$

where k is a non-zero constant,

(a) determine the matrix AB

**(2)** 

(b) determine the value of k for which  $det(\mathbf{AB}) = 0$ 

**(3)** 

Question 1 continued
(Total for Question 1 is 5 marks)
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## 2. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

Use the standard results for  $\sum_{r=1}^{n} r$  and  $\sum_{r=1}^{n} r^2$  to show that for all positive integers n

$$\sum_{r=1}^{n} (7r - 5)^{2} = \frac{n}{6} (7n + 1) (An + B)$$

where A and B are integers to be determined.

**(6)** 


Question 2 continued	
	Total for Question 2 is 6 marks)



# 3. In this question you must show all stages of your working. Solutions relying entirely on calculator technology are not acceptable.

$$f(z) = 4z^3 + pz^2 - 24z + 108$$

where p is a constant.

Given that -3 is a root of the equation f(z) = 0

(a) determine the value of p

**(2)** 

(b) using algebra, solve f(z) = 0 completely, giving the roots in simplest form,

**(4)** 

(c) determine the modulus of the complex roots of f(z) = 0

**(2)** 

(d) show the roots of f(z) = 0 on a single Argand diagram.

(2)



Question 3 continued	
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Question 3 continued	

Question 3 continued	
(Total fo	or Question 3 is 10 marks)



- (a) (i) Determine f'(x)
  - (ii) Explain why 0.25 cannot be used as an initial approximation for  $\alpha$  in the Newton-Raphson process.
  - (iii) Taking 0.15 as a first approximation to  $\alpha$  apply the Newton-Raphson process once to f(x) to obtain a second approximation to  $\alpha$  Give your answer to 3 decimal places.

**(5)** 

DO NOT WRITE IN THIS AREA

(b) Use linear interpolation once on the interval [0.15, 0.25] to find another approximation to  $\alpha$  Give your answer to 3 decimal places.

(3)



Question 4 continued



Question 4 continued

Question 4 continued	
	(Total for Orosit 4th 0
	(Total for Question 4 is 8 marks)



## 5. The quadratic equation

$$4x^2 + 3x + k = 0$$

where k is an integer, has roots  $\alpha$  and  $\beta$ 

- (a) Write down, in terms of k where appropriate, the value of  $\alpha + \beta$  and the value of  $\alpha\beta$  (2)
- (b) Determine, in simplest form in terms of k, the value of  $\frac{\alpha}{\beta^2} + \frac{\beta}{\alpha^2}$
- (c) Determine a quadratic equation which has roots

$$\frac{\alpha}{\beta^2}$$
 and  $\frac{\beta}{\alpha^2}$ 

giving your answer in the form  $px^2 + qx + r = 0$  where p, q and r are integer values in terms of k

**(3)** 

Question 5 continued



Question 5 continued	

Question 5 continued	
n	Cotal for Question 5 is 9 marks)
	(1000)



#### **6.** In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

The rectangular hyperbola H has equation xy = 20

The point  $P\left(2t\sqrt{a}, \frac{2\sqrt{a}}{t}\right)$ ,  $t \neq 0$ , where a is a constant, is a general point on H

(a) State the value of a

**(1)** 

(b) Show that the normal to H at the point P has equation

$$ty - t^3x - 2\sqrt{5}(1 - t^4) = 0$$
(4)

The points A and B lie on H

The point A has parameter t = c and the point B has parameter  $t = -\frac{1}{2c}$ , where c is a constant.

The normal to H at A meets H again at B

(c) Determine the possible values of c

**(4)** 

Question 6 continued



Question 6 continued

Question 6 continued	
	(Total for Question 6 is 9 marks)



7. (i)

$$\mathbf{P} = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

The matrix  ${\bf P}$  represents a geometrical transformation U

(a) Describe U fully as a single geometrical transformation.

**(2)** 

The transformation V, represented by the  $2 \times 2$  matrix  $\mathbf{Q}$ , is a rotation through 240° anticlockwise about the origin followed by an enlargement about (0, 0) with scale factor 6

(b) Determine the matrix Q, giving each entry in exact numerical form.

**(2)** 

Given that U followed by V is the transformation T, which is represented by the matrix  $\mathbf{R}$ 

(c) determine the matrix **R** 

**(2)** 

(ii) The transformation W is represented by the matrix

$$\begin{pmatrix} -2 & 2\sqrt{3} \\ 2\sqrt{3} & 2 \end{pmatrix}$$

Show that there is a real number  $\lambda$  for which W maps the point  $(\lambda, 1)$  onto the point  $(4\lambda, 4)$ , giving the exact value of  $\lambda$ 

**(5)** 

Question 7 continued



Question 7 continued	

Question 7 continued	
(Total for Question 7 is 11 ma	rks)



**8.** A parabola C has equation  $y^2 = 4ax$  where a is a positive constant.

The point S is the focus of C

The line  $l_1$  with equation y = k where k is a positive constant, intersects C at the point P

(a) Show that

$$PS = \frac{k^2 + 4a^2}{4a}$$
 (3)

The line  $l_2$  passes through P and intersects the directrix of C on the x-axis.

The line  $l_2$  intersects the y-axis at the point A

(b) Show that the y coordinate of A is 
$$\frac{4a^2k}{k^2 + 4a^2}$$
 (3)

The line  $l_1$  intersects the directrix of C at the point B

Given that the areas of triangles BPA and OSP, where O is the origin, satisfy the ratio

area 
$$BPA$$
: area  $OSP = 4k^2$ : 1

(c) determine the exact value of a





Question 8 continued



Question 8 continued	

Question 8 continued	
	Total for Question 8 is 11 marks)
	Total for Question o is 11 marks)



9.	Prove by induction that for all positive integers $r$ $\sum_{r=1}^{n} \log(2r-1)$		
	r=1	(2 m:)	(6)

Question 9 continued					



Question 9 continued				
	(Total for Question 9 is 6 marks)			
ТО	TAL FOR PAPER IS 75 MARKS			

