

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

--	--	--	--	--

--	--	--	--

## Pearson Edexcel International Advanced Level

**Time** 1 hour 30 minutes

**Paper**

**reference**

**WFM03/01**

### Mathematics

**International Advanced Subsidiary/Advanced Level  
Further Pure Mathematics F3**

**You must have:**

Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

#### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

#### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

#### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

P71102A

©2022 Pearson Education Ltd.

L:1/1/



Pearson



Question 1 continued

Handwriting practice area with 30 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Question 1 continued

Lined area for writing the answer to Question 1.



Question 1 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Q1

(Total 8 marks)





Question 2 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**DO NOT WRITE IN THIS AREA**

**DO NOT WRITE IN THIS AREA**

**DO NOT WRITE IN THIS AREA**

P 7 1 1 0 2 A 0 8 3 6





Question 2 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Q2

(Total 8 marks)





Question 3 continued

Handwriting practice area with 30 horizontal lines.

DO NOT WRITE IN THIS AREA



**DO NOT WRITE IN THIS AREA**

Question 3 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Q3

(Total 9 marks)



4.

$$\mathbf{M} = \begin{pmatrix} 6 & k & 2 \\ k & 5 & 0 \\ 2 & 0 & 7 \end{pmatrix}$$

where  $k$  is a constant.

Given that 3 is an eigenvalue of  $\mathbf{M}$ ,

(a) determine the possible values of  $k$ .

(3)

Given that  $k < 0$

(b) determine the other eigenvalues of  $\mathbf{M}$ .

(3)

(c) Determine a normalised eigenvector corresponding to the eigenvalue 3

(3)



Question 4 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Lined area for writing the answer to Question 4.



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Question 4 continued

Lined area for writing the answer to Question 4.





Question 4 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Q4

(Total 9 marks)



5. Determine

$$(i) \int \frac{1}{\sqrt{x^2 - 3x + 5}} dx \quad (3)$$

$$(ii) \int \frac{1}{\sqrt{63 + 4x - 4x^2}} dx \quad (4)$$

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 5 continued

Handwriting practice area with 25 horizontal lines.

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Question 5 continued

Lined area for writing the answer to Question 5.



Question 5 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Q5

(Total 7 marks)



P 7 1 1 0 2 A 0 2 1 3 6



Question 6 continued

Handwriting practice area with 25 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Question 6 continued

Lined area for writing the answer to Question 6.





Question 6 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Q6

--	--

(Total 10 marks)



P 7 1 1 0 2 A 0 2 5 3 6

$$\frac{x-3}{4} = \frac{y-5}{-2} = \frac{z-4}{7}$$
$$2x + 4y - z = 1$$

(a) Determine the coordinates of  $P$  (3)

(b) Determine, to one decimal place, the value of  $\theta$  (3)

(c) determine a vector equation for  $l_2$  (5)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

**Question 7 continued**

**DO NOT WRITE IN THIS AREA**

**DO NOT WRITE IN THIS AREA**

**DO NOT WRITE IN THIS AREA**



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Question 7 continued

Lined area for writing the answer to Question 7.



Question 7 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Q7

--	--

(Total 11 marks)



P 7 1 1 0 2 A 0 2 9 3 6

(2)

$$\frac{x^2}{9} + \frac{y^2}{4} = 1$$

- (a) Determine the eccentricity of  $E$
- (b) Hence, for this ellipse, determine
  - (i) the coordinates of the foci,
  - (ii) the equations of the directrices.

(3)

(3)

- (c) Using calculus, show that an equation for  $l_1$  is

$$2x \cos \theta + 3y \sin \theta = 6$$

The line  $l_2$  passes through the origin and is perpendicular to  $l_1$

The line  $l_1$  intersects the line  $l_2$  at the point  $Q$

- (d) Determine the coordinates of  $Q$
- (e) Show that, as  $\theta$  varies, the point  $Q$  lies on the curve with equation

$$(x^2 + y^2)^2 = \alpha x^2 + \beta y^2$$

where  $\alpha$  and  $\beta$  are constants to be determined.

Question 8 continued

Handwriting practice area with 25 horizontal lines.

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Question 8 continued

Lined area for writing the answer to Question 8.





Question 8 continued

Handwriting practice area with 25 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Question 8 continued

Lined area for writing the answer to Question 8.



Question 8 continued

Handwriting practice area with 25 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**DO NOT WRITE IN THIS AREA**

**DO NOT WRITE IN THIS AREA**

**DO NOT WRITE IN THIS AREA**

--	--

**TOTAL FOR PAPER: 75 MARKS**

36

