

Please check the examination details below before entering your candidate information

Candidate surname		Other names	
Centre Number		Candidate Number	
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**Pearson Edexcel International Advanced Level**

**Friday 9 June 2023**

Afternoon (Time: 1 hour 30 minutes)

Paper reference **WMA14/01**

**Mathematics**

**International Advanced Level**

**Pure Mathematics P4**

**You must have:**  
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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1. (a) Find the first 4 terms of the binomial expansion, in ascending powers of  $x$ , of

$$\left(\frac{1}{4} - \frac{1}{2}x\right)^{-\frac{3}{2}} \quad |x| < \frac{1}{2}$$

giving each term in simplest form.

(5)

Given that

$$\left(\frac{1}{4} - \frac{1}{2}x\right)^n \left(\frac{1}{4} - \frac{1}{2}x\right)^{-\frac{3}{2}} = \left(\frac{1}{4} - \frac{1}{2}x\right)^{\frac{1}{2}}$$

- (b) write down the value of  $n$ .

(1)

- (c) Hence, or otherwise, find the first 3 terms of the binomial expansion, in ascending powers of  $x$ , of

$$\left(\frac{1}{4} - \frac{1}{2}x\right)^{\frac{1}{2}} \quad |x| < \frac{1}{2}$$

giving each term in simplest form.

(3)



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Question 1 continued

Lined area for writing the answer to Question 1.



Question 1 continued

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Question 1 continued

Handwriting practice area with horizontal lines.

(Total for Question 1 is 9 marks)



2.

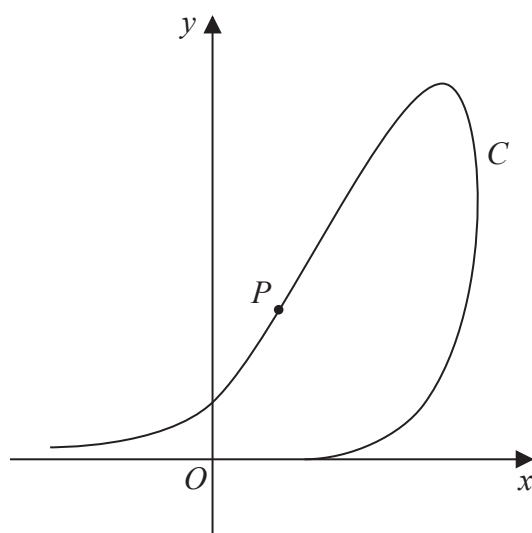


Figure 1

Figure 1 shows a sketch of part of the curve  $C$  with equation

$$2^x - 4xy + y^2 = 13 \quad y \geq 0$$

The point  $P$  lies on  $C$  and has  $x$  coordinate 2

- (a) Find the  $y$  coordinate of  $P$ .

(2)

- (b) Find  $\frac{dy}{dx}$  in terms of  $x$  and  $y$ .

(5)

The tangent to  $C$  at  $P$  crosses the  $x$ -axis at the point  $Q$ .

- (c) Find the  $x$  coordinate of  $Q$ , giving your answer in the form  $\frac{a \ln 2 + b}{c \ln 2 + d}$  where  $a, b, c$  and  $d$  are integers to be found.

(3)



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Question 2 continued

Lined area for writing the answer to Question 2.



Question 2 continued

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Question 2 continued

Handwriting practice area with horizontal lines.

(Total for Question 2 is 10 marks)



$$f(x) = \frac{8x - 5}{(2x - 1)(4x - 3)} \quad x > 1$$

(3)

(3)

$$\int_k^{3k} f(x) dx = \frac{1}{2} \ln 20$$

(5)

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Question 3 continued

Lined area for writing the answer to Question 3.



Question 3 continued

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Question 3 continued

Handwriting practice area with horizontal lines.

(Total for Question 3 is 11 marks)



4. Relative to a fixed origin  $O$ ,
- the point  $A$  has position vector  $4\mathbf{i} + 8\mathbf{j} + \mathbf{k}$
  - the point  $B$  has position vector  $5\mathbf{i} + 6\mathbf{j} + 3\mathbf{k}$
  - the point  $P$  has position vector  $2\mathbf{i} - 2\mathbf{j} + \mathbf{k}$

The straight line  $l$  passes through  $A$  and  $B$ .

- (a) Find a vector equation for  $l$ . (2)

The point  $C$  lies on  $l$  so that  $PC$  is perpendicular to  $l$ .

- (b) Find the coordinates of  $C$ . (4)

The point  $P'$  is the reflection of  $P$  in the line  $l$ .

- (c) Find the coordinates of  $P'$  (2)

- (d) Hence find  $|\overrightarrow{PP'}|$ , giving your answer as a simplified surd. (2)



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Question 4 continued

Lined area for writing the answer to Question 4.



Question 4 continued

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Question 4 continued

Lined area for writing answers.

(Total for Question 4 is 10 marks)



5. (i) Find

$$\int x^2 e^x dx$$

(4)

(ii) Use the substitution  $u = \sqrt{1 - 3x}$  to show that

$$\int \frac{27x}{\sqrt{1 - 3x}} dx = -2(1 - 3x)^{\frac{1}{2}}(Ax + B) + k$$

where  $A$  and  $B$  are integers to be found and  $k$  is an arbitrary constant.

(6)



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Question 5 continued

Lined area for writing the answer to Question 5.



Question 5 continued

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Question 5 continued

Lined area for writing the answer to Question 5.

(Total for Question 5 is 10 marks)



6.

**In this question you must show all stages of your working.****Solutions relying entirely on calculator technology are not acceptable.**

The temperature,  $\theta^{\circ}\text{C}$ , of a car engine,  $t$  minutes after the engine is turned off, is modelled by the differential equation

$$\frac{d\theta}{dt} = -k(\theta - 15)^2$$

where  $k$  is a constant.

Given that the temperature of the car engine

- is  $85^{\circ}\text{C}$  at the instant the engine is turned off
- is  $40^{\circ}\text{C}$  exactly 10 minutes after the engine is turned off

(a) solve the differential equation to show that, according to the model

$$\theta = \frac{at + b}{ct + d}$$

where  $a$ ,  $b$ ,  $c$  and  $d$  are integers to be found.

(7)

(b) Hence find, according to the model, the time taken for the temperature of the car engine to reach  $20^{\circ}\text{C}$ . Give your answer to the nearest minute.

(2)



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Question 6 continued

Lined area for writing the answer to Question 6.



Question 6 continued

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Question 6 continued

Lined area for writing answers.

(Total for Question 6 is 9 marks)



7. Use proof by contradiction to prove that  $\sqrt{7}$  is irrational.

(You may assume that if  $k$  is an integer and  $k^2$  is a multiple of 7 then  $k$  is a multiple of 7) (4)



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Question 7 continued

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(Total for Question 7 is 4 marks)



8.

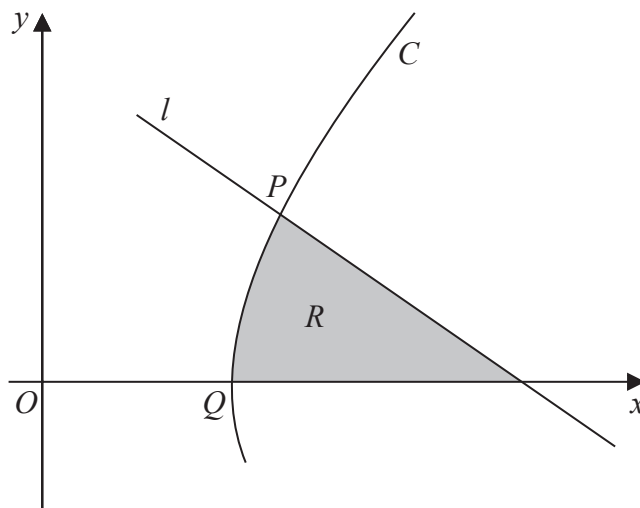


Figure 2

Figure 2 shows a sketch of part of the curve  $C$  with parametric equations

$$x = t + \frac{1}{t} \quad y = t - \frac{1}{t} \quad t > 0.7$$

The curve  $C$  intersects the  $x$ -axis at the point  $Q$ .

- (a) Find the  $x$  coordinate of  $Q$ .

(1)

The line  $l$  is the normal to  $C$  at the point  $P$  as shown in Figure 2.

Given that  $t = 2$  at  $P$

- (b) write down the coordinates of  $P$

(1)

- (c) Using calculus, show that an equation of  $l$  is

$$3x + 5y = 15$$

(3)

The region,  $R$ , shown shaded in Figure 2 is bounded by the curve  $C$ , the line  $l$  and the  $x$ -axis.

- (d) Using algebraic integration, find the exact volume of the solid of revolution formed when the region  $R$  is rotated through  $2\pi$  radians about the  $x$ -axis.

(7)

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Question 8 continued

Lined area for writing the answer to Question 8.



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Question 8 continued

Lined area for writing the answer to Question 8.



**Question 8 continued**

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**(Total for Question 8 is 12 marks)**

**TOTAL FOR PAPER IS 75 MARKS**

