

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Pearson Edexcel
International
Advanced Level

Centre Number

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Candidate Number

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Tuesday 15 January 2019

Morning (Time: 2 hours 30 minutes)

Paper Reference **WMA02/01**

Core Mathematics C34
Advanced

You must have:

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

Question 1 continued

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Question 1 continued

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Question 1 continued

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Q1

(Total 12 marks)



$$\frac{3x^2 + 4x - 7}{(x+1)(x-3)} \equiv A + \frac{B}{x+1} + \frac{C}{x-3}$$

- (4)

- $$\frac{3x^2 + 4x - 7}{(x + 1)(x - 3)} \quad |x| < 1$$

Give each coefficient as a simplified fraction.

(6)

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Question 2 continued

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Question 2 continued

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Question 2 continued

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Q2

(Total 10 marks)



3. The function f is defined by

$$f: x \mapsto 2x^2 + 3kx + k^2 \quad x \in \mathbb{R}, -4k \leq x \leq 0$$

where k is a positive constant.

(a) Find, in terms of k , the range of f .

(4)

The function g is defined by

$$g: x \mapsto 2k - 3x \quad x \in \mathbb{R}$$

Given that $gf(-2) = -12$

(b) find the possible values of k .

(4)

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Question 3 continued

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Question 3 continued

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Question 3 continued

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(Total 8 marks)

Q3

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(5)

(6)

- (b) Hence find the coordinates of the points on C where $\frac{dy}{dx} = 0$

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 4 continued

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Question 4 continued

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Question 4 continued

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(Total 11 marks)

Q4



- (4)

(2)

(2)

Question 5 continued

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Question 5 continued

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Question 5 continued

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(Total 8 marks)

Q5



- The line l passes through the points A and B .

- (b) Find, in degrees, the acute angle between the line l and the line AC . (3)

The point D lies on the line l such that angle ACD is 90°

- (d) Find the exact area of triangle ADC , giving your answer as a fully simplified surd. (2)

Question 6 continued

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Question 6 continued

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Question 6 continued

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Q6

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Question 7 continued

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Question 7 continued

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Question 7 continued

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(Total 11 marks)

Q7



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(4)

- (4)

(5)

- (5)

Question 8 continued

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Question 8 continued

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Question 8 continued

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Q8

(Total 13 marks)



9.

(a) Find $\int x \sin 2x \, dx$ (3)

(b) Find $\int (x + \sin 2x)^2 \, dx$ (4)

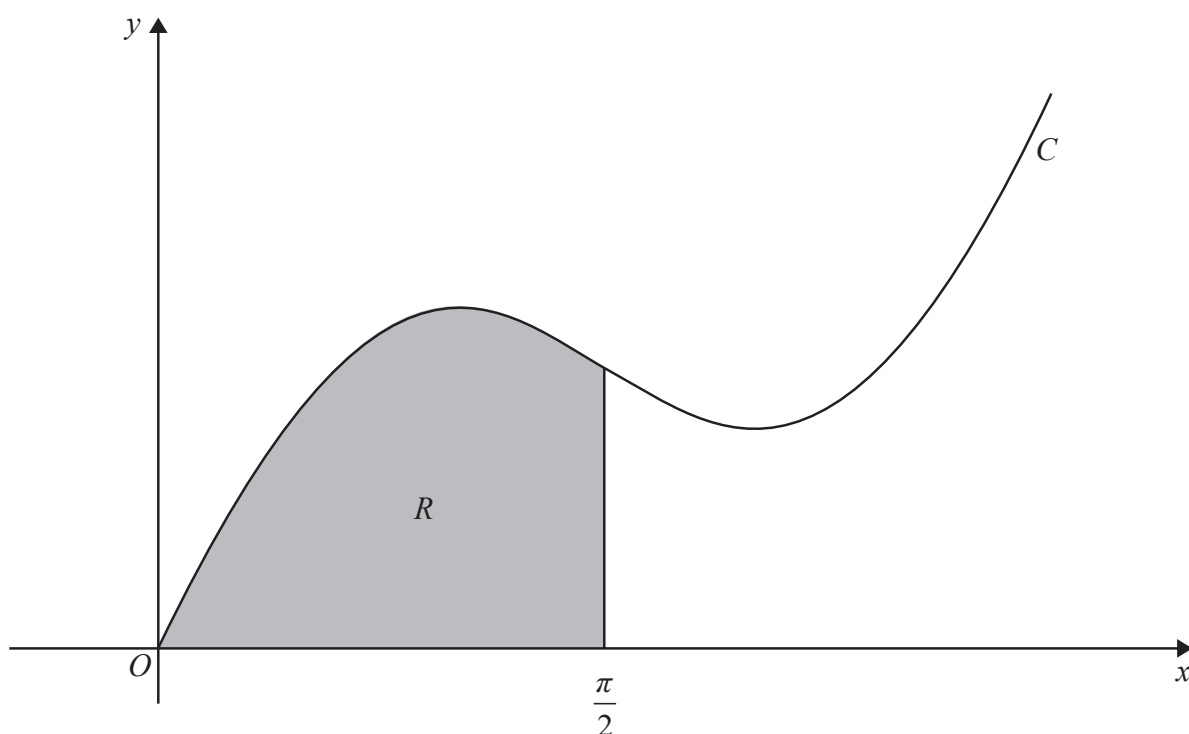


Figure 2

Figure 2 shows a sketch of part of the curve C with equation $y = x + \sin 2x$.

The region R , shown shaded in Figure 2, is bounded by C , the x -axis and the line with equation $x = \frac{\pi}{2}$

The region R is rotated through 2π radians about the x -axis to form a solid of revolution.

(c) Find the exact value for the volume of this solid, giving your answer as a single, simplified fraction. (3)



Question 9 continued

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Question 9 continued

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Question 9 continued

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Q9

(Total 10 marks)



10.

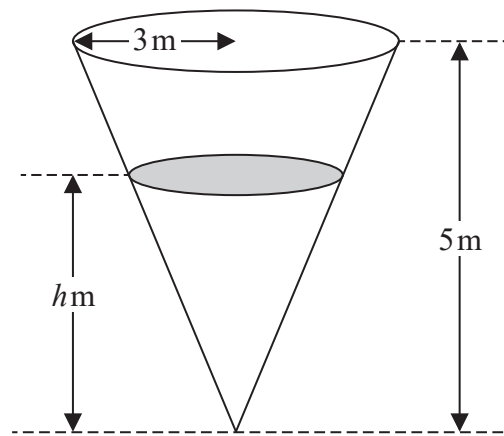


Diagram not
drawn to scale

Figure 3

Figure 3 shows a container in the shape of an inverted right circular cone which contains some water.

The cone has an internal radius of 3 m and a vertical height of 5 m as shown in Figure 3.

At time t seconds, the height of the water is h metres, the volume of the water is $V \text{ m}^3$ and water is leaking from a hole in the bottom of the container at a constant rate of $0.02 \text{ m}^3 \text{ s}^{-1}$

[The volume of a cone of radius r and height h is $\frac{1}{3} \pi r^2 h$.]

(a) Show that, while the water is leaking,

$$h^2 \frac{dh}{dt} = -\frac{1}{k\pi}$$

where k is a constant to be found.

(5)

Given that the container is initially full of water,

(b) express h in terms of t .

(3)

(c) Find the time taken for the container to empty, giving your answer to the nearest minute.

(2)

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Question 10 continued

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Question 10 continued

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Q10



11. (a) Given that $0 \leq f(x) \leq \pi$, sketch the graph of $y = f(x)$ where

$$f(x) = \arccos(x - 1), \quad 0 \leq x \leq 2 \quad (2)$$

The equation $\arccos(x - 1) - \tan x = 0$ has a single root α .

- (b) Show that $0.9 < \alpha < 1.1$ (2)

The iteration formula

$$x_{n+1} = \arctan(\arccos(x_n - 1))$$

can be used to find an approximation for α .

- (c) Taking $x_0 = 1.1$ find, to 3 decimal places, the values of x_1 and x_2 (2)

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(Total 6 marks)

Q11

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12. Given that k is a positive constant,

(a) sketch the graph with equation

$$y = 2|x| - k$$

Show on your sketch the coordinates of each point at which the graph crosses the x -axis and the y -axis.

(2)

(b) Find, in terms of k , the values of x for which

$$2|x| - k = \frac{1}{2}x + \frac{1}{4}k$$

(3)

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Question 12 continued

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Question 12 continued

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Question 12 continued

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(Total 5 marks)

Q12



- $$N = \frac{240}{1 + ke^{-\frac{t}{16}}}$$

$$\frac{dN}{dt} = \frac{1}{p}N - \frac{1}{q}N^2$$

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Question 13 continued

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Question 13 continued

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TOTAL FOR PAPER: 125 MARKS

END

