

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper

reference

WMA13/01

Mathematics

International Advanced Level

Pure Mathematics P3

You must have:

Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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Pearson

1. Find, using calculus, the x coordinate of the stationary point on the curve with equation

$$y = (2x + 5)e^{3x}$$

(4)

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Question 1 continued

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Q1

(Total 4 marks)



- $$8 \cos \theta = 3 \operatorname{cosec} \theta$$

$$\sin 2\theta = k$$

(3)

- $$8 \cos \theta = 3 \operatorname{cosec} \theta$$

(2)

Question 2 continued

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Q2

(Total 5 marks)



Question 3 continued

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Q3

(Total 6 marks)



Question 4 continued

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Q4

(Total 7 marks)



5.

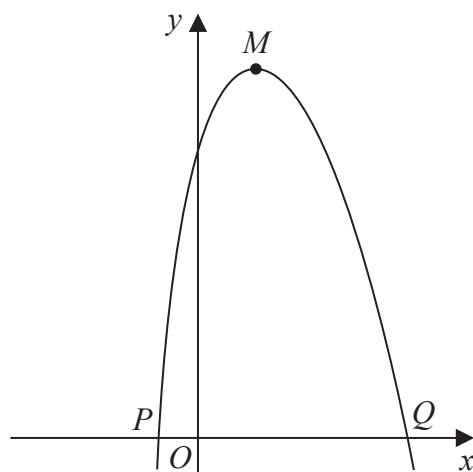


Figure 1

Figure 1 shows a sketch of part of the curve with equation

$$y = 6 \ln(2x + 3) - \frac{1}{2}x^2 + 4 \quad x > -\frac{3}{2}$$

The curve cuts the negative x -axis at the point P , as shown in Figure 1.

- (a) Show that the x coordinate of P lies in the interval $[-1.25, -1.2]$ (2)

The curve cuts the positive x -axis at the point Q , also shown in Figure 1.

Using the iterative formula

$$x_{n+1} = \sqrt{12 \ln(2x_n + 3) + 8} \quad \text{with } x_1 = 6$$

- (b) (i) find, to 4 decimal places, the value of x_2
 (ii) find, by continued iteration, the x coordinate of Q . Give your answer to 4 decimal places. (3)

The curve has a maximum turning point at M , as shown in Figure 1.

- (c) Using calculus and showing each stage of your working, find the x coordinate of M . (4)

Question 5 continued

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Question 5 continued

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Q5

(Total 9 marks)



$$f(x) = \frac{5x - 3}{x - 4} \quad x > 4$$

- (b) Find f^{-1} (3)

- (c) (i) Show that $\text{ff}(x) = \frac{ax + b}{x + c}$ where a , b and c are constants to be found.
- (ii) Deduce the range of ff .
- (5)**

Question 6 continued

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Question 6 continued

Lined area for writing the answer to Question 6.



Question 6 continued

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Q6

(Total 11 marks)



7.

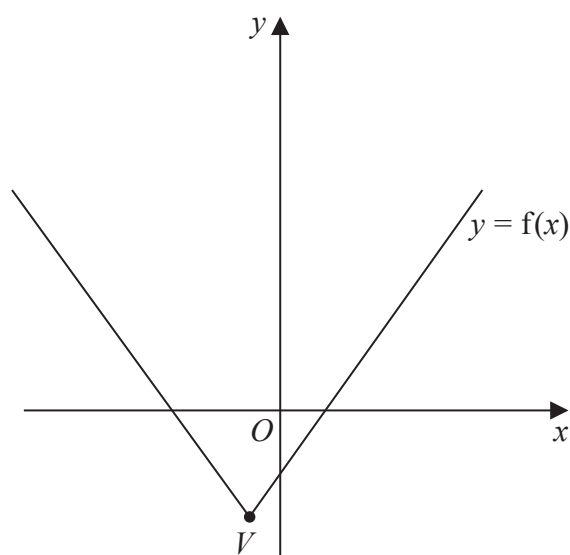


Figure 2

Figure 2 shows a sketch of part of the graph with equation $y = f(x)$, where

$$f(x) = \frac{1}{2}|2x + 7| - 10$$

(a) State the coordinates of the vertex, V , of the graph.

(2)

(b) Solve, using algebra,

$$\frac{1}{2}|2x + 7| - 10 \geq \frac{1}{3}x + 1$$

(4)

(c) Sketch the graph with equation

$$y = |f(x)|$$

stating the coordinates of the local maximum point and each local minimum point.

(4)

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Question 7 continued

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Lined area for writing the answer to Question 7.



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Question 7 continued

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Q7

(Total 10 marks)



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8. A dose of antibiotics is given to a patient.

The amount of the antibiotic, x milligrams, in the patient's bloodstream t hours after the dose was given, is found to satisfy the equation

$$\log_{10} x = 2.74 - 0.079t$$

- (a) Show that this equation can be written in the form

$$x = pq^{-t}$$

where p and q are constants to be found. Give the value of p to the nearest whole number and the value of q to 2 significant figures.

(4)

- (b) With reference to the equation in part (a), interpret the value of the constant p .

(1)

When a different dose of the antibiotic is given to another patient, the values of x and t satisfy the equation

$$x = 400 \times 1.4^{-t}$$

- (c) Use calculus to find, to 2 significant figures, the value of $\frac{dx}{dt}$ when $t = 5$

(3)



Question 8 continued

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Question 8 continued

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Question 8 continued

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Q8

(Total 8 marks)



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Question 9 continued

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Question 9 continued

Handwriting practice area with 25 horizontal lines.



Question 9 continued

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Q9

(Total 8 marks)



A Cartesian coordinate system with a horizontal x -axis and a vertical y -axis. The origin is labeled O . A curve, labeled C , passes through the origin. In the first quadrant, the curve is concave down and increases as x increases. In the third quadrant, the curve is concave up and decreases as x decreases, approaching the y -axis as a vertical asymptote.

Question 10 continued

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Q10

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