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Surname

Other names

Pearson Edexcel
International
Advanced Level

Centre Number

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Candidate Number

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Core Mathematics C12

Advanced Subsidiary

Tuesday 12 January 2016 – Morning

Time: 2 hours 30 minutes

Paper Reference

WMA01/01

You must have:

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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PEARSON

- $$u_{n+1} = 2u_n - 6, \quad n \geq 1$$

(a) find the value of u_3

(2)

(b) evaluate $\sum_{i=1}^4 u_i$

(3)

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Q1

(Total 5 marks)

Q1

Turn over



2. (i) Given that $\frac{49}{\sqrt{7}} = 7^a$, find the value of a . (2)

(ii) Show that $\frac{10}{\sqrt{18} - 4} = 15\sqrt{2} + 20$

You must show all stages of your working. (3)

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Q2

(Total 5 marks)

Q2

Turn over



3. Find, using calculus and showing each step of your working,

$$\int_1^4 \left(6x - 3 - \frac{2}{\sqrt{x}} \right) dx$$

(5)

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Q3

(Total 5 marks)

1

Turn over



4. The 4th term of an arithmetic sequence is 3 and the sum of the first 6 terms is 27

Find the first term and the common difference of this sequence.

(6)

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Question 4 continued

Handwriting practice area with 30 horizontal lines.

(Total 6 marks)

Q4



5. (a) Sketch the graph of $y = \sin 2x$, $0 \leq x \leq \frac{3\pi}{2}$

Show the coordinates of the points where your graph crosses the x -axis.

(2)

The table below gives corresponding values of x and y , for $y = \sin 2x$.
The values of y are rounded to 3 decimal places where necessary.

x	0	$\frac{\pi}{12}$	$\frac{\pi}{6}$	$\frac{\pi}{4}$
y	0	0.5	0.866	1

- (b) Use the trapezium rule with all the values of y from the table to find an approximate value for

$$\int_0^{\frac{\pi}{4}} \sin 2x \, dx$$

(3)

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Q5

(Total 5 marks)

Q5

Turn over



$$f(x) = x^3 + x^2 - 12x - 18$$

- (2)

- (2)

- (3)

[illegible]

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Question 6 continued

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Question 6 continued

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(Total 7 marks)

Q6



7. (a) Find the first 4 terms, in ascending powers of x , of the binomial expansion of $(1 + kx)^8$, where k is a non-zero constant. Give each term in its simplest form.

(4)

Given that the coefficient of x^3 in this expansion is 1512

- (b) find the value of k .

(3)

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Question 7 continued

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Question 7 continued

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(Total 7 marks)

Q7



8. (a) Given that $7 \sin x = 3 \cos x$, find the exact value of $\tan x$.

(1)

(b) Hence solve for $0 \leq \theta < 360^\circ$

$$7 \sin(2\theta + 30^\circ) = 3 \cos(2\theta + 30^\circ)$$

giving your answers to one decimal place.

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(5)

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Question 8 continued

Lined area for writing the answer to Question 8.

(Total 6 marks)

Q8

Mark box for Question 8.



- (1)

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Question 9 continued

Handwriting practice area with 25 horizontal lines.

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Q9

(Total 7 marks)

Turn over



(2)

(5)

- (3)

- (c) Use $\frac{d^2y}{dx^2}$ to determine the nature of this stationary point.



Question 10 continued

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[illegible]

Question 10 continued

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Q10

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(Total 10 marks)





Question 11 continued

Handwriting practice area with 25 horizontal lines.

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Question 11 continued

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Q11

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(Total 11 marks)



12.

$$f(x) = \frac{(4 + 3\sqrt{x})^2}{x}, \quad x > 0$$

- (a) Show that $f(x) = Ax^{-1} + Bx^k + C$, where A , B , C and k are constants to be determined.

(4)

- (b) Hence find $f'(x)$.

(2)

- (c) Find an equation of the tangent to the curve $y = f(x)$ at the point where $x = 4$

(4)

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Question 12 continued

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Question 12 continued

Q12

(Total 10 marks)



(a) Show that k satisfies the inequality

(b) Find the range of possible values for k . (4)

Question 13 continued

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Question 13 continued

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(Total 8 marks)

Q13



(4)

(4)

(4)

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Q14

(Total 8 marks)

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15. The points A and B have coordinates $(-8, -8)$ and $(12, 2)$ respectively.
 AB is the diameter of a circle C .

(a) Find an equation for the circle C .

(6)

The point $(4, 8)$ also lies on C .

(b) Find an equation of the tangent to C at the point $(4, 8)$, giving your
 answer in the form $ax + by + c = 0$

(4)

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Question 15 continued

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Question 15 continued

Handwriting practice area with 30 horizontal lines.

(Total 10 marks)

Q15

Two empty boxes for marking.



16.

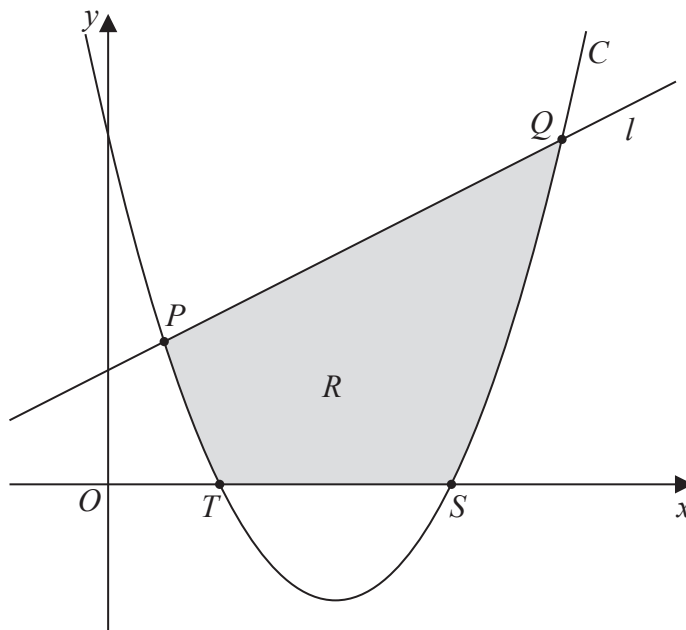


Figure 2

The straight line l with equation $y = \frac{1}{2}x + 1$ cuts the curve C , with equation $y = x^2 - 4x + 3$, at the points P and Q , as shown in Figure 2

- (a) Use algebra to find the coordinates of the points P and Q . (5)

The curve C crosses the x -axis at the points T and S .

- (b) Write down the coordinates of the points T and S . (2)

The finite region R is shown shaded in Figure 2. This region R is bounded by the line segment PQ , the line segment TS , and the arcs PT and SQ of the curve.

- (c) Use integration to find the exact area of the shaded region R . (8)



Question 16 continued

Handwriting practice area with 25 horizontal lines.

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Question 16 continued

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(Total 15 marks)

TOTAL FOR PAPER: 125 MARKS

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