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Surname

Other names

Pearson Edexcel
International
Advanced Level

Centre Number

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Candidate Number

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Core Mathematics C34

Advanced

Tuesday 19 June 2018 – Afternoon

Time: 2 hours 30 minutes

Paper Reference

WMA02/01

You must have:

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

1. (i) Find

$$\int \frac{2x^2 + 5x + 1}{x^2} dx, \quad x > 0$$

(3)

(ii) Find

$$\int x \cos 2x \, dx$$

(3)

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Question 1 continued

Handwriting practice area with 30 horizontal lines.

(Total 6 marks)

Q1

Mark box



$$x = \frac{3}{2}t - 5, \quad y = 4 - \frac{6}{t} \quad t \neq 0$$

- (b) Show that a cartesian equation of C can be expressed in the form

$$y = \frac{ax + b}{x + 5} \quad x \neq k$$

(4)

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Question 2 continued

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Question 2 continued

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(Total 7 marks)

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Question 3 continued

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(Total 7 marks)

Q3



- (2)

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Question 4 continued

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Q4

(Total 10 marks)

Turn over



- $$g : x \rightarrow \ln(3x - 1), \quad x \in \mathbb{R}, x > \frac{1}{3}$$

- (3)

- (2)

- (2)

(5)

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Question 5 continued

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Question 5 continued

Lined area for writing the answer to Question 5.



Question 5 continued

Handwriting practice area with 30 horizontal lines.

Q5

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(Total 12 marks)

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- (3)

- (4)

(4)

Question 6 continued

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Question 6 continued

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(Total 11 marks)



A diagram of a hemispherical bowl. The bowl is partially filled with water, which is shaded grey. The water surface is a horizontal circle. A vertical double-headed arrow indicates the height of the water surface from the bottom of the bowl, labeled h cm.

Figure 1 shows a hemispherical bowl.

When the height of the water is h cm, the volume of water V cm³ is given by

$$V = \frac{1}{3} \pi h^2 (90 - h), \quad 0 \leq h \leq 30$$

Give your answer to 2 significant figures.

(5)



(Total 5 marks)

Q7

Turn over



- $$l_1 : \mathbf{r} = \begin{pmatrix} 1 \\ -3 \\ 2 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}, \quad l_2 : \mathbf{r} = \begin{pmatrix} 6 \\ 4 \\ 1 \end{pmatrix} + \mu \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}$$

(a) Show that l_1 and l_2 do not meet.

(4)

(b) Find the acute angle between the line segment PQ and l_1 , giving your answer in degrees to 2 decimal places.

(5)

- (2)

Question 8 continued

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Question 8 continued

Lined area for writing the answer to Question 8.



(Total 11 marks)

Turn over



9.

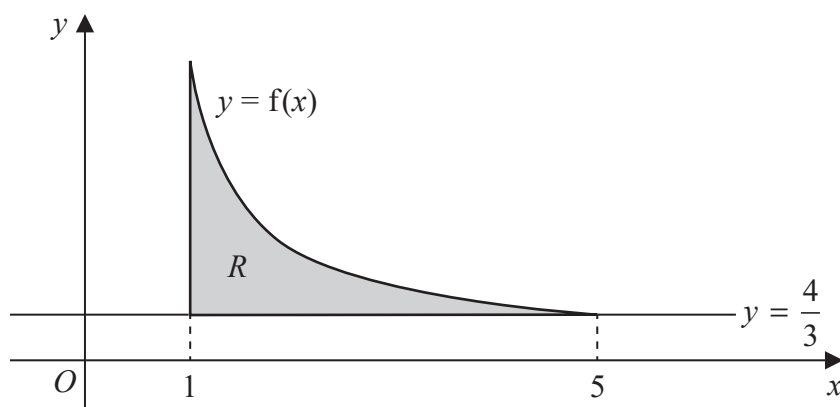


Figure 2

- (a) Find

$$\int \frac{1}{(2x-1)^2} dx$$

(2)

Figure 2 shows a sketch of the curve with equation $y = f(x)$ where

$$f(x) = \frac{12}{(2x-1)} \quad 1 \leq x \leq 5$$

The finite region R , shown shaded in Figure 2, is bounded by the line with equation $x = 1$, the curve with equation $y = f(x)$ and the line with equation $y = \frac{4}{3}$.

The region R is rotated through 2π radians about the x -axis to form a solid of revolution.

- (b) Find the exact value of the volume of the solid generated, giving your answer in its simplest form.

(6)



Question 9 continued

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(Total 8 marks)

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10. The curve C satisfies the equation

$$xe^{5-2y} - y = 0 \quad x > 0, \quad y > 0$$

The point P with coordinates $(2e^{-1}, 2)$ lies on C .

The tangent to C at P cuts the x -axis at the point A and cuts the y -axis at the point B .

Given that O is the origin, find the exact area of triangle OAB , giving your answer in its simplest form.

(7)

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Question 10 continued

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Question 10 continued

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Q10

(Total 7 marks)



(a) By writing $\sec \theta$ as $\frac{1}{\cos \theta}$, show that when $x = 3 \sec \theta$,

Figure 3 shows a sketch of part of the curve C with equation

$$y = \frac{\sqrt{x^2 - 9}}{x} \quad x \geq 3$$

(b) Use the substitution $x = 3 \sec \theta$ to find the exact value of the area of R .
[Solutions based entirely on graphical or numerical methods are not acceptable.] (7)

Question 11 continued

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12. (a) Show that

$$\cot x - \tan x \equiv 2 \cot 2x, \quad x \neq 90n^\circ, n \in \mathbb{Z} \quad (4)$$

(b) Hence, or otherwise, solve, for $0 \leq \theta < 180^\circ$

$$5 + \cot(\theta - 15^\circ) - \tan(\theta - 15^\circ) = 0$$

giving your answers to one decimal place.

[Solutions based entirely on graphical or numerical methods are not acceptable.] (5)

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Question 12 continued

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(Total 9 marks)



Question 13 continued

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Question 13 continued

Q13

(Total 11 marks)



14. Given that

$$y = \frac{(x^2 - 4)^{\frac{1}{2}}}{x^3} \quad x > 2$$

(a) show that

$$\frac{dy}{dx} = \frac{Ax^2 + 12}{x^4(x^2 - 4)^{\frac{1}{2}}} \quad x > 2$$

where A is a constant to be found.

(6)

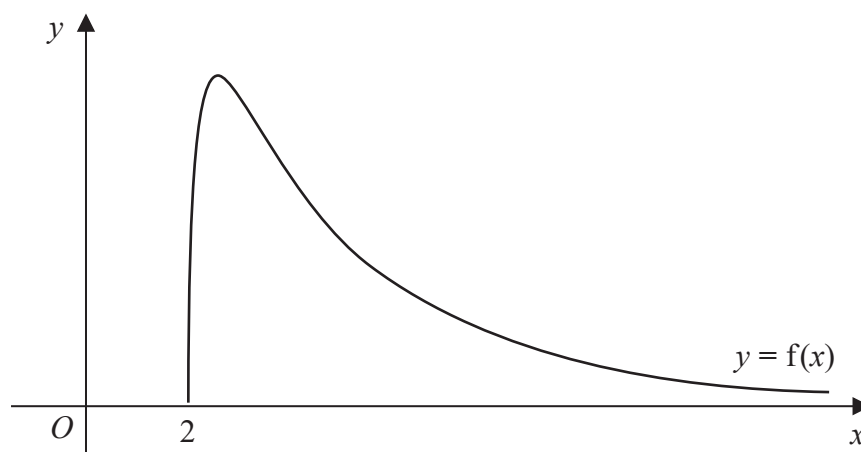


Figure 4

Figure 4 shows a sketch of part of the curve with equation $y = f(x)$ where

$$f(x) = \frac{24(x^2 - 4)^{\frac{1}{2}}}{x^3} \quad x > 2$$

(b) Use your answer to part (a) to find the range of f .

(5)

(c) State a reason why f^{-1} does not exist.

(1)

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Question 14 continued

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Question 14 continued

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Q14

Question 14 continued

Lined area for writing the answer to Question 14.

(Total 12 marks)

TOTAL FOR PAPER: 125 MARKS

END

