Please check the examination details belo	low before entering your candidate information		
Candidate surname	Other names		
Centre Number Candidate Nu	umbor		
Candidate No			
Pearson Edexcel Inter	national Advanced Level		
<b>Time</b> 1 hour 30 minutes	Paper reference WFM01/01		
Mathematics			
International Advanced Su	ubsidiary/Advanced Level		
Further Pure Mathematics F1			
	J		
(Variation to be accessed			
You must have:  Mathematical Formulae and Statistica	al Tables (Yellow), calculator		

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
  - there may be more space than you need.
- You should show sufficient working to make your methods clear.
   Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

## Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

## Advice

- Read each guestion carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.









1	A _	( 3	a
1.	$\mathbf{A} =$	_2	-2

where a is a non-zero constant and  $a \neq 3$ 

(a) Determine  $A^{-1}$  giving your answer in terms of a. (2)

Given that  $\mathbf{A} + \mathbf{A}^{-1} = \mathbf{I}$  where  $\mathbf{I}$  is the  $2 \times 2$  identity matrix,

(b) determine the value of a.

**(3)** 

Question 1 continued	blank
	01
	Q1
(Total 5 marks)	



- 2.  $f(x) = 7\sqrt{x} \frac{1}{2}x^3 \frac{5}{3x} \qquad x > 0$ 
  - (a) Show that the equation f(x) = 0 has a root,  $\alpha$ , in the interval [2.8, 2.9] (2)
  - (b) (i) Find f'(x).
    - (ii) Hence, using  $x_0 = 2.8$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to f(x) to calculate a second approximation to  $\alpha$ , giving your answer to 3 decimal places.

**(4)** 

(c) Use linear interpolation once on the interval [2.8, 2.9] to find another approximation to  $\alpha$ . Give your answer to 3 decimal places.

**(3)** 



Question 2 continued
Question 2 continued



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Question 2 continued	
	Q2
(Total 9 marks)	



**3.** The quadratic equation

$$2x^2 - 5x + 7 = 0$$

has roots  $\alpha$  and  $\beta$ 

Without solving the equation,

(a) write down the value of  $(\alpha + \beta)$  and the value of  $\alpha\beta$ 

**(1)** 

- (b) determine, giving each answer as a simplified fraction, the value of
  - (i)  $\alpha^2 + \beta^2$

(ii) 
$$\alpha^3 + \beta^3$$

**(4)** 

(c) find a quadratic equation that has roots

$$\frac{1}{\alpha^2 + \beta}$$
 and  $\frac{1}{\beta^2 + \alpha}$ 

giving your answer in the form  $px^2 + qx + r = 0$  where p, q and r are integers to be determined.

**(4)** 


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Question 3 continued	



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Question 3 continued		

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Question 3 continued	blank
Question 5 continued	
	<b>Q3</b>
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(Total 9 marks)	



l.	$f(z) = 2z^3 - z^2 + az + b$
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where a and b are integers.

The complex number -1 - 3i is a root of the equation f(z) = 0

(a) Write down another complex root of this equation.

**(1)** 

(b) Determine the value of a and the value of b.

**(4)** 

(c) Show all the roots of the equation f(z) = 0 on a single Argand diagram.

**(2)** 

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Question 4 continued	
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Question 4 continued	

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	Q4
(Total 7 marks)	



5. (a) Use the standard results for  $\sum_{r=1}^{n} r^3$ ,  $\sum_{r=1}^{n} r^2$  and  $\sum_{r=1}^{n} r$  to show that for all positive integers n,

$$\sum_{r=1}^{n} r(r-1)(r-3) = \frac{1}{12} n(n+1)(n-1)(3n-10)$$
(5)

(b) Hence show that

$$\sum_{r=n+1}^{2n+1} r(r-1)(r-3) = \frac{1}{12}n(n+1)(an^2 + bn + c)$$

where a, b and c are integers to be determined.

(3	)





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Question 5 continued	



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Question 5 continued	

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	Q5
(Total 8 marks)	
(Total o marks)	



**6.** The curve H has equation

$$xy = a^2$$
  $x > 0$ 

where a is a positive constant.

The line with equation y = kx, where k is a positive constant, intersects H at the point P

(a) Use calculus to determine, in terms of a and k, an equation for the tangent to H at P

The tangent to H at P meets the x-axis at the point A and meets the y-axis at the point B

(b) Determine the coordinates of A and the coordinates of B, giving your answers in terms of a and k

**(2)** 

(c) Hence show that the area of triangle AOB, where O is the origin, is independent of k

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Question 6 continued	



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Question 6 continued	

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	Q6
(Total 8 marks)	



- 7. In part (i), the elements of each matrix should be expressed in exact numerical form.
  - (i) (a) Write down the  $2 \times 2$  matrix that represents a rotation of  $210^{\circ}$  anticlockwise about the origin.

**(1)** 

(b) Write down the  $2 \times 2$  matrix that represents a stretch parallel to the y-axis with scale factor 5

**(1)** 

The transformation T is a rotation of 210° anticlockwise about the origin followed by a stretch parallel to the y-axis with scale factor 5

(c) Determine the  $2 \times 2$  matrix that represents T

**(2)** 

(ii)

$$\mathbf{M} = \begin{pmatrix} k & k+3 \\ -5 & 1-k \end{pmatrix} \quad \text{where } k \text{ is a constant}$$

(a) Find det M, giving your answer in simplest form in terms of k.

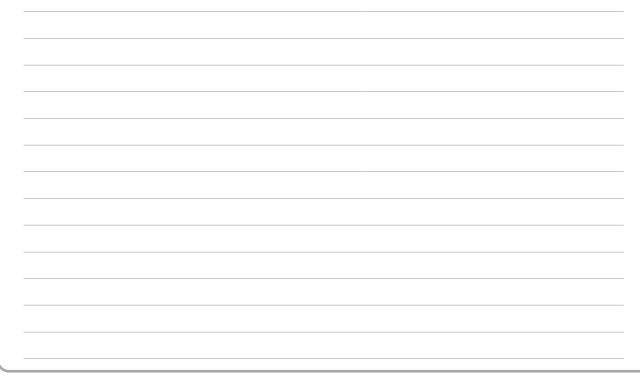
**(2)** 

A closed shape R is transformed to a closed shape R' by the transformation represented by the matrix M.

Given that the area of R is 2 square units and that the area of R' is 16k square units,

(b) determine the possible values of k.

(3)



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Question 7 continued	

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	<b>Q7</b>
(Total 9 marks)	
(Total 7 marks)	



**8.** The parabola C has equation  $y^2 = 20x$ 

The point P on C has coordinates  $(5p^2, 10p)$  where p is a non-zero constant.

(a) Use calculus to show that the tangent to C at P has equation

$$py - x = 5p^2 \tag{3}$$

The tangent to C at P meets the y-axis at the point A.

(b) Write down the coordinates of A.

**(1)** 

The point S is the focus of C.

(c) Write down the coordinates of S.

**(1)** 

The straight line  $l_1$  passes through A and S.

The straight line  $l_2$  passes through O and P, where O is the origin.

Given that  $l_1$  and  $l_2$  intersect at the point B,

(d) show that the coordinates of B satisfy the equation

$$2x^2 + v^2 = 10x$$

**(5)** 



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Question 8 continued	



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Question 8 continued

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Question 8 continued	
	Q8
(Total 10 marks)	



9. (i) A sequence of numbers is defined by

$$u_1 = 0$$
  $u_2 = -6$ 

$$u_{n+2} = 5u_{n+1} - 6u_n \quad n \geqslant 1$$

Prove by induction that, for  $n \in \mathbb{Z}^+$ 

$$u_n = 3 \times 2^n - 2 \times 3^n$$

(ii) Prove by induction that, for all positive integers n,

$$f(n) = 3^{3n-2} + 2^{4n-1}$$

is divisible by 11



**(5)** 



Question 9 continued	bla
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