

Mark Scheme (Results)

Summer 2021

Pearson Edexcel International Advanced Level In Statistics S2 Paper WST02/01

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL IAL MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer

Question Number		Scheme		Marks
	roughout the paper the candidates may use different letters to the ones given in the mark scheme			ne.
1. (a)	[$X \sim$ the number of pansy seeds that $X \sim B(20,0.05)$ or $Y \sim B(20,0.05)$	95)	umberthat <u>do</u> germinate]	B1
(i)	$P(X \le 4) - P(X \le 2) = 0.9974 - 0.92$	245 <u>or</u>		
	$\binom{20}{3}0.00$	$5^3 \times 0.95^{17} + {20 \choose 4} 0.05^4 \times 0.95^{10}$	b = 0.05958 + 0.01332	M1
	= 0.072909		awrt <u>0.0729</u>	A1
(ii)	$P(X \leq 1)$ or $P(Y \geq 19)$	$=20\times(0.95)^{19}(0.05)+(0.95)$	20	M1
	= 0.7358	= 0.735839	awrt <u>0.736</u>	A1 (5)
(b)	[Let $W = \text{no. of packets where } Y >$	181 $P(W-5) - ("0.7358)$	"\5	M1
, ,	Let W - no. or packets where I	= 0.21573	<i>'</i>	A1
		- 0.213/3	. awit <u>0.210</u>	(2)
	H 0.05 H > 0.05			
(c)	$H_0: p = 0.05$ $H_1: p > 0.05$			B1 (1)
				(1)
(d)	[V= no. of seeds that do not germinal	te $V \sim B(100, 0.05)$ approxim	nates to] $V \sim Po(5)$	M1A1
		CR for 1-tail in (c)	CR for 2-tail in (c)	
	$P(V \ge 8) = 1 - P(V \le 7)$ = 1 - 0.8666	$P(V \geqslant 9) = 0.0681$	$P(V \geqslant 10) = 0.0318$	M1
	= 1 - 0.8666	$P(V \geqslant 10) = 0.0318$	$P(V \geqslant 11) = 0.0137$	
	= 0.1334	CR $V \geqslant 10$ oe	$CR V \geqslant 11 \text{ oe}$	A1
	Accept H ₀ or not significant or 8 c			dM1
	Data consistent with <i>Spany</i> 's claim			Alcso
	or insufficient evidence that perce	ntage of seeds not germinatin	g is more than 5% (o.e.)	(6) Total 14
		Notes		
(a)	B1: writing or using $B(20,0.05)$ [A	Allow $Y \sim B(20, 0.95)$ if Y is clo	early defined]. Implied by 1 corn	rect prob.
(i)	M1: for $P(X \leq 4) - P(X \leq 2)$ and	one correct prob. or $P(X =$	(3) + P(X = 4) and 1 correct probability	
(ii)	M1: for $P(X \le 1)$ or $[20] \times (0.95)$	$^{19}(0.05)+(0.95)^{20}$ - condone i	missing 20	
(b)	M1: for $(their(a)(ii))^5$			
(c)	B1: both hypotheses correct with <i>p</i> of	or π		
(d)	1 st M1: for realising a Poisson appro 1 st A1: writing or using $V \sim Po(5)$ i.	e correct mean for the Poisson)A0
	2^{nd} M1: for writing or using $1-P(1)$			C.D.
	or writing $P(V \ge 10) = 0.03$. Implied by correct CR or properties of the properti		$P(V \ge 11) = 0.0137$ leading to	a CR.
			llow any letter but CR must mate	ch part(c)
	2nd A1 : for awrt 0.133 or $V \ge 10$ oe (e.g. $V > 9$) or $V \ge 11$ oe allow any letter but CR must match part(c) 3rd dM1 : dep on 2 nd M1. ft their CR or probability. A correct statement based on comparing 8 with their CR			- ' '
	or their prob with 0.05 or 0	0.025 [condone 0.866<0.95]— c	ontradicting non-contextual com	ments M0
	3 rd A1 cso: all previous marks must be awarded. A correct statement in context. Need Bold words . NB award M1A1 for a correct contextual statement on its own.			
		es or they are the wrong way a		
	Normal approximation: Award ma			
SC1	Sight of N(5 or 95, $\sqrt{4.75}^2$) M1A	1; probability awrt 0.125/6 M	[1A1; Correct contextual concl'	dM1A1
SC2	No approximation: Use of B(100,			
		•	,	

Question Number	Scheme	Marks
2. (a)	[$X =$ number of faults in 4 m ² so $X \sim Po(3)$]	
	$P(X=5) = P(X \le 5) - P(X \le 4) [= 0.9161 - 0.8153]$ or $\frac{e^{-3}3^5}{5!}$ (allow λ instead of 3)	M1
		A1
		(2)
(b)	[Y = number of faults in 6 m ² so] $Y \sim Po(4.5)$ and $P(Y > 5) = 1 - P(Y \le 5)$ [= 1 - 0.7029]	M1
	= 0.2971 or (calc) 0.29706956 awrt 0.297	A1
		(2)
(c)		B1ft
	Faults occur independently/ randomly	B1 (2)
(d)	$F = \text{number of faults in a small rug}$ $F \sim \text{Po}(0.9)$	
(u)	$e^{-"0.9"}n \times 80 + (1 - e^{-"0.9"})n \times 60 \ge 4000$ or $(awrt 0.407)n \times 80 + (awrt 0.593)n \times 60 \ge 4000$	B1 M1
	$n \geqslant \frac{4000}{20e^{-"0.9"} + 60} = 58.71\dots$	M1
	$n = \underline{59}$	A1 (4)
		(4)
(e)	$H_0: \lambda = 9$ $H_1: \lambda > 9$ $R \sim Po("0.9" \times 10)$ and $[P(R \ge 13)] = 1 - P(R \le 12)$ $[= 1 - 0.8758]$	B1
	$P(R \le 13) = 0.9261$ or $P(R \ge 14) = 0.0739$ or $P(R \le 14) = 0.9585$ or $P(R \ge 15) = 0.0739$	M1
	0.0415	
	[$P(R \ge 13)$] = 0.1242 awrt 0.124 or CR $R \ge 15$ (oe) so insufficient evidence to reject H_0 /not significant/ not in critical region	A1 M1
	There is insufficient evidence that the rate at which faults occur is higher for Rhiannon	A1
		(5) Total 15
	Notes	1
(a)	M1: for using or writing $P(X \le 5) - P(X \le 4)$ or $\frac{e^{-\lambda} \lambda^5}{5!}$ (Accept letter λ or any value of	· \(\lambda \)
(b)	M1: writing or using Po(4.5) and sight of $[P(Y > 5)] = 1 - P(Y \le 5)$ Implied by sight of $1 - 0.7$	
(a)		
(c)	2 nd B1: for a comment about faults occurring randomly/independently or Poisson has "no men	iory
(d)	B1: writing or using Po(0.9) May be implied by sight of 0.407 or 0.593 1st M1: for $e^{-\lambda} n \times 80 + (1 - e^{-\lambda}) n \times 60 > 4000$ any value for λ . Allow = 4000	
	2^{nd} M1: for solving their equation leading to a positive value of n . Allow any value of λ and all	$low n = \dots$
	A1: for an answer of 59 only	
(e)	B1: both hypotheses correct with λ or μ . Allow 3 or 0.75 or 0.9 instead of 9	
	1st M1: for writing or using Po("9") and writing or using $1 - P(R \le 12)$ (implied by $1 - 0.8758$ $P(R \le 13) = 0.9261$, $P(R \ge 14) = 0.0739$, $P(R \le 14) = 0.9585$, $P(R \ge 15) = 0.0415$ lead :	
	CR	
	 1st A1: for probability = awrt 0.124 or CR of R ≥ 15 oe e.g. R > 14 2nd M1: for a correct conclusion based on their prob & 0.05 or their CR & 13. Assume correct h Do not allow contradicting conclusions 	ypotheses.
	2 nd A1: dep on both Ms for a correct contextual comment including the words in bold.	

Question Number	Scheme	Marks
3. (a)	12/25 - 6/25 -	M1
	0 1 2 4 9	A1 (2)
(b)	$\frac{d\left(\frac{3}{50}(4y^2 - y^3)\right)}{dy} = \frac{3}{50}(8y - 3y^2)$	M1
	$\frac{3}{50}(8y-3y^2)=0$; $y=\frac{8}{3}$ oe	M1; A1
(c)	$\frac{1}{2}$ $c^{2}(6, c^{2}, 6, c^{2})$ $c^{4}(12, c^{2}, 3, c^{2})$	(3)
	$E(Y^{2}) = \int_{1}^{2} \left(\frac{6}{25} y^{3} - \frac{6}{25} y^{2} \right) dy + \int_{2}^{4} \left(\frac{12}{50} y^{4} - \frac{3}{50} y^{5} \right) dy$	M1
	$= \left[\frac{6}{100}y^4 - \frac{6}{75}y^3\right]_1^2 + \left[\frac{12}{250}y^5 - \frac{3}{300}y^6\right]_2^4$	A1
	$= \left[\left(\frac{8}{25} \right) - \left(-\frac{1}{50} \right) \right] + \left[\left(\frac{1024}{125} \right) - \left(\frac{112}{125} \right) \right] ; \qquad = \frac{1909}{250} \text{or} 7.636 \text{or} 7.64$	dM1; A1
(d)	$Var(Y) = "\frac{1909}{1}" - 2.696^2$	(4) M1
	$Var(Y) = \frac{1909}{250} - 2.696^{2}$ $= 0.367584$ awrt <u>0.368</u>	A1
(a)	1 ((2)
(6)	$\int_{1}^{1} \frac{1}{2} (y-1) \times \frac{6}{25} (y-1) = 0.1 \underline{\text{or}} \int_{1}^{x} \frac{6}{25} (y-1) dy = 0.1$	M1
	$\frac{1}{2}(y-1) \times \frac{6}{25}(y-1) = 0.1 \underline{\text{or}} \int_{1}^{x} \frac{6}{25}(y-1) dy = 0.1$ $\frac{1}{2}(y-1) \times \frac{6}{25}(y-1) = 0.1 \underline{\text{or}} \frac{6}{25} \left[\left(\frac{x^{2}}{2} - x \right) + \frac{1}{2} \right] = 0.1 \underline{\text{or}} \frac{6}{50}(x-1)^{2} = 0.1$	A1
	$(y-1)^2 = \frac{5}{6} \text{ or } y = 1 \pm \sqrt{\frac{5}{6}}$; $y = 1.9128$ awrt <u>1.91</u>	dM1; A1
		(4) Total 15
	Notes	•

- M1: the two parts must be the right shape and not joined. Ignore labels and condone if it goes below x axis (a) A1: for 6/25, 12/25, 1, 2 and 4 and must not go beyond 4 or < 1 [Can allow "freehand" straight line]
- 1st M1: for attempting to differentiate $v^n \rightarrow v^{n-1}$ for n = 2 or 3 2nd M1: for equating their differential ($\neq f(y)$) to zero and an attempt at solving so must reach y = ...for $\frac{8}{3}$ oe and allow awrt 2.67 If y = 0 is seen it must be rejected.
- 1st M1: for using $\int y^2 f(y)$ for both parts, and an attempt at integration (some $y^n \to y^{n+1}$) Ignore limits. 1st A1: for correct integration for both parts. Ignore limits. 2nd dM1: dep on 1st M1 for adding the 2 parts together and substituting the correct limits in to each part. 2nd A1: allow 7.64 or 7.636 You will need to check that they have used algebraic integration.
- **M1:** for "their part(c)" -2.696^{2} **A1:** for awrt 0.368 (d)
- 1st M1: allow $\frac{1}{2}t \times \frac{6}{25}(t-1) = 0.1$ or $\int_1^x \frac{6}{25}(y-1) dy = 0.1$ and some integration and sub' of 1 and x 1st A1: for a correct equation in any form

2nd dM1: dependent on 1st M1 for a correct method for solving their equation. Implied by correct answer. 2nd A1: for awrt 1.91 (second solution should be rejected)

Question Number	Scheme	Marks		
4.	[A = the number on the ball] $P(A=1) = \frac{2}{9}$ $P(A=2) = \frac{1}{3}$ $P(A=5) = \frac{4}{9}$	B1		
(i)	Possible samples with a range of 4 are: $(1,1,5)$ $(1,2,5)$ $(1,5,5)$	M1		
	$(1,1,5) \frac{2}{9} \times \frac{2}{9} \times \frac{4}{9} \times 3 = \frac{16}{243} \qquad \underline{\text{or}} \qquad (1,5,5) \frac{2}{9} \times \frac{4}{9} \times \frac{4}{9} \times 3 = \frac{32}{243}$	M1		
	$(1,2,5)$ $\frac{2}{9} \times \frac{1}{3} \times \frac{4}{9} \times 6 = \frac{16}{81}$	M1		
	$P(B=4) = \frac{16}{243} + \frac{32}{243} + \frac{16}{81} = \frac{32}{81}$	A1		
(ii)	$P(B=0) = \left(\frac{2}{9}\right)^{3} + \left(\frac{1}{3}\right)^{3} + \left(\frac{4}{9}\right)^{3} = \frac{11}{81}$	M1		
	$P(B=1) = 3 \times \frac{2}{9} \times \left(\frac{1}{3}\right)^{2} + 3 \times \frac{1}{3} \times \left(\frac{2}{9}\right)^{2} = \frac{10}{81} \text{ or } P(B=3) = 3 \times \frac{1}{3} \times \left(\frac{4}{9}\right)^{2} + 3 \times \frac{4}{9} \times \left(\frac{1}{3}\right)^{2} = \frac{28}{81}$	M1		
	$1 - \frac{11}{81} - \frac{10}{81} - \frac{32}{81} = \frac{28}{81} \qquad \underline{\text{or}} 1 - \frac{11}{81} - \frac{28}{81} - \frac{32}{81} = \frac{10}{81}$	M1		
	b 0 1 3 4	B1		
	P(B=b)	A1		
		(10) Total 10		
	Notes			
(2)				
(i)				
	2nd M1: for $p \times p \times q \times 3$ or $p \times q \times q \times 3$ where p and q are probabilities with $(p+q) < 1$ 3rd M1: for $p \times q \times r \times 6$ where p , q and r are probabilities with $(p+q+r) = 1$			
	A1: for $\frac{32}{81}$ or awrt 0.395 [Calc: 0.3950617]			
(ii)	1st M1: for $p^3 + q^3 + r^3$ (for their p, q and r)			
	2nd M1: for $3 \times p \times (q)^2 + 3 \times q \times (p)^2$ or $3 \times q \times (r)^2 + 3 \times r \times (q)^2$ (for their p, q and r)			
	3rd M1: for use of all probabilities of $P(B=b)$ adding to 1 [Must have 3, 4 or 5 values for b]			
	B1: for ranges $0, 1, 3$ and 4 with none omitted and no extras. Allow extras if assigned proba-	ability of 0		
	A1: for a fully correct probability distribution.			
SC A0 in (i)	If A0 scored in (i) <u>and</u> all other marks scored in (ii) <u>and</u> correct prob's for 2 values of b: award A	Al in (ii)		

Question Number	Scheme	Marks
5 (a)(i)	If $y = 0$ then $1 - (\alpha + \beta y^2) = 0$ $\therefore \alpha = 1$ *	B1cso
(ii)	If $y = 5$ then $1 - (\alpha + \beta y^2) = 1$	
	$1+25\beta=0 \therefore \beta=-\frac{1}{25} \qquad *$	B1cso (2)
(b)	$F(y) = \frac{1}{25}y^2$ so $f(y) = \frac{dF(y)}{dy} = \frac{2}{25}y$	(2) M1
	$ \therefore [f(y)] = \begin{cases} \frac{2}{25}y & 0 \le y \le 5\\ 0 & \text{otherwise} \end{cases} $	A1
		(2)
(c)	$\left[P\left(R > \frac{11}{5}\right) = P\left(Y > \frac{5}{3}\right) = 1 - \frac{1}{25} \times \left(\frac{5}{3}\right)^2 = \frac{8}{9} \text{ oe} \right]$	B1
	$\frac{3d - \frac{11}{5}}{3d - d} = \frac{8}{9}$ oe $\frac{11}{5} - d = \frac{1}{9}$ oe	M1
	$d = \frac{9}{5} \text{oe}$	A1
	p(y 11) 121	(3)
(d)	$P\left(Y < \frac{11}{5}\right) = \frac{121}{625}$ or 0.1936	B1
	[Let $G =$ the number of spins with distance < 2.2 m]	
	$\left[P(G \geqslant 5) = \right]$	
	$\left[\left(\frac{1}{9} \right)^{3} \times \left(\frac{121}{625} \right)^{3} + 3 \times \left(\frac{1}{9} \right)^{2} \times \left(\frac{8}{9} \right) \times \left(\frac{121}{625} \right)^{3} + 3 \times \left(\frac{1}{9} \right)^{3} \times \left(\frac{121}{625} \right)^{2} \times \left(\frac{504}{625} \right) \right]$	M1, M1
	= $0.000\ 373226$ awrt $0.000\ 373$	A1
		(4)
	Notes	Total 11
H	- 10000	

- (a) (i) B1: for stating or using the fact that when y = 0 then $\alpha + \beta y^2 = 1$
 - (ii) B1: for stating or using that when y = 5 then $\alpha + \beta y^2 = 0$ and setting up the equation leading to $\beta = -\frac{1}{25}$
 - **(b)** M1: for differentiating. Implied by $\pm \frac{2}{"25"}y$ can ft their value of β

A1: for a fully correct f(y) defined for the whole range.

(c) B1: for using F(y) and $\frac{5}{3}$ to find $P(Y > \frac{5}{3})$. Allow $\frac{8}{9}$ or any exact equivalent.

M1: for LHS = p where 0

A1: for $\frac{9}{5}$ or any exact equivalent e.g. 1.8

(d) B1: for $\frac{121}{625}$ or awrt 0.194 This mark could be implied by a correct answer.

1st M1: for $p^3q^3 + np^2(1-p)q^3 + np^3q^2(1-q)$ where p and q are probabilities and n is an integer > 0

2nd M1: for $p^3q^3 + 3p^2(1-p)q^3 + 3p^3q^2(1-q)$ where p and q are probabilities.

A1: for awrt 0.000 373

Question Number	Scheme	Marks
6. (i)	z = 1.25	B1
	$\frac{187.5 - \mu}{\sigma} = 1.25$	M1 M1 A1
	$187.5 - \mu = 1.25\sigma$	
	$\mu = 225 p$	M1
	$\sigma = \sqrt{225 p(1-p)}$	M1
	$(187.5 - 225p)^{2} = (1.25)^{2} \times 225p(1-p) \underline{\text{or}} (150 - 180p)^{2} = 225p(1-p) \text{(o.e.)}$	M1
	e.g. $900(5-6p)^2 = 225(p-p^2) \Rightarrow 4(25-60p+36p^2) = p-p^2$	A1*
	Leading to $145 p^2 - 241 p + 100 = 0 *$	Al
(ii)	$\left[(29p - 25)(5p - 4) = 0 \Rightarrow \right] \qquad p = 0.8 \underline{\text{or}} p = \frac{25}{29} \text{ (accept: } 0.862(0689))$	M1
	[$p = $] <u>0.8</u> because 0.862 gives a mean greater than 188 (oe)	A1
		(10) Total 10
	Notes	1000110
(i)	B1: for 1.25 or better (calculator gives: 1.25027)	
	1 st M1: for attempting to use a continuity correction i.e. for sight of 188 ± 0.5	
	2nd M1: for standardising using μ and σ or np and $\sqrt{np(1-p)}$ (Condone letter n or any integ	ger > 0
	1 st A1: for a correct equation with compatible signs, allow 1.250 If using a value for <i>n</i> it must 3 rd M1: for $\mu = 225p$ seen at any stage in the working.	st be 225
	4th M1: for $\sigma = \sqrt{225p(1-p)}$ seen at any stage in the working. Must be for σ not $\sigma^2 = 225p(1-p)$	1 – <i>p</i>)
	5 th M1: for squaring to get a quadratic equation in p	
	2 nd A1*: dep on all previous Ms and use of 1.25 (with correct sign) for at least 1 correct interme	diate step
(ii)	from a correct quadratic equation e.g one of those in scheme for 5^{th} M1 for solving the quadratic correctly–leading to $p = \dots$ or implied by 0.8 or awrt 0.862	2
	A1: for 0.8 and a correct reason to eliminate 0.862	