

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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**Monday 14 January 2019**

Afternoon (Time: 1 hour 30 minutes)

Paper Reference **WFM01/01**

**Further Pure Mathematics F1**  
**Advanced/Advanced Subsidiary**

**You must have:**

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

### Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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**Pearson**

- (a) Find an equation of the line  $l$ .

(3)

(b) Find the coordinates of  $B$ .

(3)



**(Total 6 marks)**

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$$f(z) = z^3 - 2z^2 + 16z - 32$$

- (a) Show that  $f(2) = 0$  (1)
- (b) Use algebra to solve  $f(z) = 0$  completely. (3)
- (c) Show, on a single Argand diagram, all three roots of the equation  $f(z) = 0$  (2)

Q2

**(Total 6 marks)**

**Turn over**



3. (a) Use the standard results for  $\sum_{r=1}^n r$  and  $\sum_{r=1}^n r^2$  to show that, for all positive integers  $n$ ,

$$\sum_{r=1}^n (2r + 5)^2 = \frac{n}{3}[(an + b)^2 + c]$$

where  $a$ ,  $b$  and  $c$  are integers to be found.

(5)

- (b) Use the answer to part (a) to evaluate  $\sum_{r=0}^{100} (2r + 5)^2$

(2)

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### Question 3 continued

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Question 3 continued

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(Total 7 marks)

Q3

Box for marking the question.



$$f(x) = 2x^3 - \frac{7}{x^2} + 16, \quad x \neq 0$$

(a) Starting with the interval  $[-2, -1]$ , use interval bisection twice to find an interval of width 0.25 that contains  $\alpha$ .

(3)

(b) Taking 0.65 as a first approximation to  $\beta$ , apply the Newton-Raphson procedure once to  $f(x)$  to obtain a second approximation to  $\beta$ , giving your answer to 4 decimal places.

(4)

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Question 4 continued

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Q4

(Total 7 marks)



- The point  $P$ , on  $H$ , has coordinates  $\left(4p, \frac{4}{p}\right)$  where  $p$  is a non-zero constant.

- $$x + p^2y = 8p \tag{4}$$

(b) use algebra to find the coordinates of the two possible positions of  $P$ . (4)

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**Question 5 continued**

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Question 5 continued

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Question 5 continued

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Q5

(Total 8 marks)



- (b) find a quadratic equation that has roots  $\frac{2}{\alpha} - \beta$  and  $\frac{2}{\beta} - \alpha$  giving your answer in the form  $ax^2 + bx + c = 0$ , where  $a, b$  and  $c$  are integers to be found. (6)



Question 6 continued

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Question 6 continued

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**(Total 9 marks)**

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$$\mathbf{P} = \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix}$$

- $$\mathbf{P}^{35} = 2^k \begin{pmatrix} -1 & a \\ b & -1 \end{pmatrix}$$

(2)

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### Question 7 continued

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Question 7 continued

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(Total 9 marks)

Q7

Box for marking the question.



8. (i) Prove by induction that, for  $n \in \mathbb{Z}^+$

$$\begin{pmatrix} 5 & -8 \\ 2 & -3 \end{pmatrix}^n = \begin{pmatrix} 1+4n & -8n \\ 2n & 1-4n \end{pmatrix} \quad (5)$$

(ii) A sequence of positive numbers is defined by

$$\begin{aligned} u_1 &= 8, \quad u_2 = 40 \\ u_{n+2} &= 8u_{n+1} - 12u_n \quad n \geq 1 \end{aligned}$$

Prove by induction that, for  $n \in \mathbb{Z}^+$

$$u_n = 6^n + 2^n \quad (5)$$



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**(Total 10 marks)**

**Turn over**



9. The complex numbers  $z_1$  and  $z_2$  are given by

$$z_1 = -1 - i \text{ and } z_2 = 3 - 4i$$

(a) Find the argument of the complex number  $z_1 - z_2$ . Give your answer in radians to 3 decimal places.

(3)

(b) Find the complex number  $\frac{z_1}{z_2}$  in the form  $a + ib$ , where  $a$  and  $b$  are rational numbers.

(3)

(c) Find the modulus of  $\frac{z_1}{z_2}$ , giving your answer as a simplified surd.

(2)

(d) Find the values of the real constants  $p$  and  $q$  such that

$$\frac{p + iq - 8z_1}{p - iq - 8z_2} = 3i$$

(5)

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### Question 9 continued

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**Question 9 continued**

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Question 9 continued

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Q9

(Total 13 marks)

TOTAL FOR PAPER: 75 MARKS

END

