

# Mark Scheme (Results)

Summer 2017

Pearson Edexcel International A Level in Statistics S3 (WST03/01)



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# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### **EDEXCEL IAL MATHEMATICS**

# **General Instructions for Marking**

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{\phantom{a}}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

| Question<br>Number | Scheme   |                   |          |                |         |               |                |        |          |  | Marks            |         |
|--------------------|--|-------------------|----------|----------------|---------|---------------|----------------|--------|----------|--|------------------|---------|
| 1. (a)             | Parrot   | A                 | В        | С              | D       | E             | F              | G      | Н        |  |                  |         |
| , ,                | Rank Age   | 3                 | 6        | 2              | 1       | 7             | 8              | 4      | 5        |  |                  |         |
|                    | Rank Breed   | ler 5             | 6        | 4              | 1       | 8             | 7              | 2      | 3        |  | $M1 \rightarrow$ |         |
|                    | For finding the difference between each of the rank and evaluating $\mathring{a} d^2 = 4 + 0 + 4 + 0 + 1 + 1 + 4 + 4 = 18$   |                   |          |                |         |               |                |        |          |  | M1               |         |
|                    | $\mathring{\mathbf{a}} d^2 = 1$  |                   |          |                |         |               |                |        |          |  |                  |         |
|                    | For use of the correct formula with their $\overset{\circ}{\triangle} d^2$   |                   |          |                |         |               |                |        |          |  | dM1;             |         |
|                    | $r_{\rm S} = 1 - \frac{6(18)}{8(8^2 - 1)}$ ; = 0.78571429 For use of the correct formula with their $\frac{1}{2}a$ $\frac{1}{14}$ or awrt 0.786  |                   |          |                |         |               |                |        |          |  | A1               |         |
|                    |  |                   |          |                |         |               |                |        |          |  | T                | 5]      |
| (b)                | $H_0: \Gamma = 0, H_1: \Gamma > 0$ Both hypotheses stated correctly  |                   |          |                |         |               |                |        |          |  | B1               |         |
|                    | Critical Valu  | e = 0.833         | 3 or C   | R: $r_{\rm S}$ | ≥ 0.833 | 33            |                |        |          | Critical value of 0.8333   | B1               |         |
|                    | Since $r_S = 0.7857$ does not lie in the CR (or $0.7857 < 0.8333$ ), do not reject H <sub>0</sub> see notes  |                   |          |                |         |               |                |        |          |  | M1               |         |
|                    | <ul> <li>Either conclude that</li> <li>the <u>breeder does not</u> have the ability to correctly <u>order parrots</u> by age, after examining them.</li> <li>there is <u>insufficient evidence</u> that the <u>breeder</u> can correctly <u>order parrots</u> by age.</li> </ul> |                   |          |                |         |               |                |        |          |  | A1ft             |         |
|                    |  |                   |          |                |         |               |                |        |          |  | [4               | 4]<br>9 |
|                    |  |                   |          |                |         |               | Notes          |        |          |  |                  |         |
| (a)                | Attempt to rank for actual ages or breeder's estimates of ages. (At least 4 correct in either rowallow reverse rankings) Independent of 1st M1 but these must be ranks.  |                   |          |                |         |               |                |        |          |  |                  |         |
|                    | is dependent on $I^{st}$ M1 for use of $1 - \frac{6(18)}{3}$ with their $\mathring{\ominus} d^2$ .   |                   |          |                |         |               |                |        |          |  |                  |         |
| (b)                | $ \begin{array}{c c} 3^{\text{rd}} \text{ dM1} \\ 1^{\text{st}} \text{ B1} \end{array} $ Both hypotheses correct in terms of $\Gamma$ or $\Gamma_{\text{S}}$ .   |                   |          |                |         |               |                |        |          |  |                  |         |
|                    | 2 <sup>nd</sup> B1 Critical value of 0.8333  |                   |          |                |         |               |                |        |          |  |                  |         |
|                    | M1 F   | or a corre        | ct state | nent re        | lating  | their $r_{c}$ | $ r_{\rm c} <$ | 1) wit | th their | c.v. where their c.v. $< 1$  |                  |         |
|                    | A1ft For a contextualised comment which is accepting H <sub>0</sub> , which must mention "breeder", "order", "parrots", which conveys the idea that the breeder cannot order them correctly.  All previous marks in part (b) must have been scored to award this one.            |                   |          |                |         |               |                |        |          |  |                  |         |
|                    | Note Follow through their $r_S$ with 0.8333  |                   |          |                |         |               |                |        |          |  |                  |         |
|                    | Note Two-tailed test   |                   |          |                |         |               |                |        |          |  |                  |         |
|                    |  | pplying a o Award |          |                |         |               |                |        |          | $\begin{array}{l} \Delta 0 \\ \text{oy critical value}  r_s = (\pm) \end{array}$ | 0.881            |         |
|                    | the M  | the M1 mark only. |          |                |         |               |                |        |          |  |                  |         |

| Question<br>Number |  |  | Sch                              | neme            |           |   | Marks                  |  |  |  |  |
|--------------------|--|--|----------------------------------|-----------------|-----------|---|------------------------|--|--|--|--|
| 2.                 | H <sub>0</sub> : There is no association between gender and (inspirational) message (independent) H <sub>1</sub> : There is an association between gender and (inspirational) message (dependent)  |  |                                  |                 |           |   |                        |  |  |  |  |
|                    |  | 1  |                                  |                 | 1         | Some attempt at   |                        |  |  |  |  |
|                    | Expected   | A  | В                                | C               | Total     |   | M1                     |  |  |  |  |
|                    | Male   | 27.106   | 41.373                           | 38.52           | 107       | (Grand Total)   |                        |  |  |  |  |
|                    | Female   | 29.893   | 45.626                           | 42.48           | 118       |   |                        |  |  |  |  |
|                    | Total  | 57   | 87                               | 81              | 225       |   | A1                     |  |  |  |  |
|                    |  |  |                                  |                 |           | At least 2 correct terms for  |                        |  |  |  |  |
|                    | Observed   | Expected   | $\frac{(O-E)^2}{E}$              | $\frac{O^2}{E}$ |           | $\frac{(O-E)^2}{E}$ or $\frac{O^2}{E}$ or correct                             | 13.61                  |  |  |  |  |
|                    | 25   | 27.11  | 0.1642                           | 23.0542         |           | expressions with their $E_i$ .  | dM1                    |  |  |  |  |
|                    | 37   | 41.37  | 0.4616                           | 33.0916         | 5         | Accept 2 sf accuracy  |                        |  |  |  |  |
|                    | 45   | 38.52  | 1.0901                           | 52.5701         | 1         | for the dM1 mark.   |                        |  |  |  |  |
|                    | 32   | 29.89  | 0.1489                           | 34.2589         |           | At least 5 correct  |                        |  |  |  |  |
|                    | 50   | 45.63  | 0.4185                           |                 |           | $\frac{(O-E)^2}{E}$ or $\frac{O^2}{E}$ terms to                               |                        |  |  |  |  |
|                    | 36   | 42.48  | 0.9885                           | 30.5085         |           | <b>=</b> -  | A1                     |  |  |  |  |
|                    |  | Totals   | 3.2718                           | 228.271         |           | either 1 dp or better. Allow truncation.                                      |                        |  |  |  |  |
|                    |  |  | l                                | I               |           | For applying either   |                        |  |  |  |  |
|                    | $X^2 = \mathring{\mathbf{a}} \frac{O}{O}$  | $\frac{-E)^2}{E}$ or   | $\mathring{a}\frac{O^2}{E} - 22$ | 25 ;= awrt 3    | 3.27      | $\mathring{a} \frac{(O-E)^2}{E} \text{ or } \mathring{a} \frac{O^2}{E} - 225$ | dM1                    |  |  |  |  |
|                    |  |  | _                                |                 |           | awrt <u>3.27</u>  | A1                     |  |  |  |  |
|                    | n = (2 - 1)(3  | n = (2 - 1)(3 - 1) = 2 $n = 2$   |                                  |                 |           |   |                        |  |  |  |  |
|                    |  | $10) = 4.605 \Rightarrow CR: X^2 \geqslant 4.605$ 4.605  |                                  |                 |           |   |                        |  |  |  |  |
|                    |  | [does not lie in the CR/not significant/Do not reject H <sub>0</sub> ]   |                                  |                 |           |   |                        |  |  |  |  |
|                    | Either conclude that  • there is insufficient evidence to support the headteacher's belief.  (There are independently a literated and the support of the sup |  |                                  |                 |           |   |                        |  |  |  |  |
|                    | • there is no association between <u>gender</u> and inspirational <u>message</u> . (They are independent)  |  |                                  |                 |           |   |                        |  |  |  |  |
|                    |  |  |                                  |                 |           |   |                        |  |  |  |  |
|                    | Notes  |  |                                  |                 |           |   |                        |  |  |  |  |
|                    | 1st B1 For both hypotheses. Must mention "gender" <i>and</i> "message" oe at least once. Use of "relationship" or "correlation" or "connection" or "link" is B0.   |  |                                  |                 |           |   |                        |  |  |  |  |
|                    | 1 <sup>st</sup> M1   | Can be implied by at least one correct $E_i$ to 1 d.p.   |                                  |                 |           |   |                        |  |  |  |  |
|                    | . 1  | I The state of the |                                  |                 |           |   |                        |  |  |  |  |
|                    |  |  |                                  |                 |           | t/trunc. 1.d.p. (may be implied by awr  | •                      |  |  |  |  |
|                    | and the  |  |                                  |                 |           |   | 3.27)                  |  |  |  |  |
|                    |  | Dependent on 2 <sup>nd</sup> M1 For applying either $\overset{\circ}{\bigcirc} \frac{(O-E)^2}{E}$ or $\overset{\circ}{\bigcirc} \frac{O^2}{E}$ - 225<br>If awrt 3.27 is seen (from a calculator) <b>without</b> the expected frequencies stated then award   |                                  |                 |           |   |                        |  |  |  |  |
|                    |  | special case   | M0A0M1A1                         | M1A1.           | ŕ         | -   |                        |  |  |  |  |
|                    | 2 <sup>nd</sup> B1   | $\bar{n} = 2$ . This   | mark can be                      | implied by a    | a correct | critical value of 4.605   |                        |  |  |  |  |
|                    |  | 4.605 or ft their $\nu$  |                                  |                 |           |   |                        |  |  |  |  |
|                    |  |  |                                  |                 |           | ntextualised conclusion which is accept                                       | oting H <sub>0</sub> . |  |  |  |  |
|                    |  | Must mention either "headteacher's belief" or "gender" <i>and</i> "message". Contradictory statements score A0. E.g. "significant, do not reject H <sub>0</sub> "  |                                  |                 |           |   |                        |  |  |  |  |
|                    |  | Condone "relationship" or "connection" here but <b>not</b> "correlation".  |                                  |                 |           |   |                        |  |  |  |  |
|                    |  | Hypotheses t   |                                  |                 |           |   |                        |  |  |  |  |

| Question<br>Number | Scheme  |  | Marks     |  |  |  |  |
|--------------------|---|--|-----------|--|--|--|--|
| <b>3.</b> (a)      | $H_0: m = 30$ $H_1: m^{-1} 30$  |  | B1        |  |  |  |  |
|                    | $z = \frac{28.2 - 30}{\frac{8.5}{\sqrt{75}}}; = -1.833936$ $\pm \frac{28.2 - 30}{\frac{8.5}{\sqrt{75}}} \text{ or equivalent.}$   |  |           |  |  |  |  |
|                    | <b>,</b> , , ,  | awrt <u>-1.83</u>                            | A1        |  |  |  |  |
|                    | Two tailed c.v.'s $Z = \pm 1.6449$  |  |           |  |  |  |  |
|                    | or CR: $Z \le -1.6449$ or $Z \ge 1.6449$  |  | B1        |  |  |  |  |
|                    | or p-value = awrt 0.033 or awrt 0.034 < 0.05<br>[in the CR/significant/Reject H <sub>0</sub> /"[0.033, 0.034]" < 0.05   | 0.051  |           |  |  |  |  |
|                    | Conclude either   |  |           |  |  |  |  |
|                    | • that the mean age of gym customers is not 30  | ) years.                                     | A1        |  |  |  |  |
|                    | • that the manager's claim is not correct.  |  |           |  |  |  |  |
|                    |   |  | [5]       |  |  |  |  |
| (b)                | $\overline{X}$ is (approximately) <u>normally distributed</u>   |  | B1        |  |  |  |  |
| (a)                |   | 0 1 :  | [1]<br>B1 |  |  |  |  |
| (c)                | Assumed $s^2 = S^2$ or variance of sample = variance of population.   |  |           |  |  |  |  |
|                    |   |  | [1]       |  |  |  |  |
|                    |   | otes   |           |  |  |  |  |
| (a)                | Both hypotheses correct.  M1  Both hypotheses correct.  For standardising with 28.2, 30 and $\frac{8.5}{\sqrt{75}}$ (or awrt 0.981) [Allow use of $8.5 \times \sqrt{\frac{74}{75}}$ (= 2nd B1  Critical value of -1.6449 (compatible with sign of their test statistic) <b>or</b> a correct property of the correct property of |  |           |  |  |  |  |
|                    | comparison. Dependent on M1 scored for a correct contextualised comment which is rejecting $H_0$ which is based on their z-value and their critical value with compatible signs, where $1.64 \le  c.v.  \le 1.65$ Contradictory statements score final A0. E.g. "significant, do not reject $H_0$ ".  |  |           |  |  |  |  |
|                    | Alternative method for the "M1A1B1" marks: Let $\overline{X}_C$ be the critical value of the sample mean.   |  |           |  |  |  |  |
|                    | $-1.6449 = \frac{\overline{X}_C - 30}{\frac{8.5}{\sqrt{75}}}$ M1: For $\frac{c - 30}{\frac{8.5}{\sqrt{75}}}$ =  | - 1.6449 / -1.645 / -1.64 / -1.65            |           |  |  |  |  |
|                    | So $\overline{X}_C = 28.38883812$ A1: $\overline{X}_C = \text{awrt } 28$ B1: Critical value   |  |           |  |  |  |  |
| Note               | One tailed test SC: Applying a one-tailed test scores a maximum of B0M1A1B1A0 (Allow ±1.2816 to score the 2 <sup>nd</sup> B1)   |  |           |  |  |  |  |
| (b)                | Allow in words e.g "sample mean is normally distri  | buted"                                       |           |  |  |  |  |
| (c)                | B1   Also allow $s = S$ or standard deviation   | of sample = standard deviation of population | n.        |  |  |  |  |

| Question<br>Number |   |                       |                                 | Scheme                    |                                 |  |  | Mai        | rks           |
|--------------------|---|-----------------------|---------------------------------|---------------------------|---------------------------------|--|--|------------|---------------|
| <b>4.</b> (a)      | $\widehat{\lambda} = \frac{0(3)}{2}$  | ) + 1(13) +           | + 2(14) + 3(                    | $\frac{(15) + 4(10)}{80}$ | 0+5(8)+6(8)+                    | -7(6)+8(3) $=$                           | $\frac{280}{80}$ = 3.5*                            | B1cso      | *             |
|                    |   |                       |                                 |                           |                                 |  |  |            | [1]           |
| (b)                | $r = 80 - \frac{e^{-3.5}(3.5)^3}{3!} = 17.26283752$ or $r = 80 - (0.5366 - 0.3208) = 17.264$                  |                       |                                 |                           |                                 |  |  |            |               |
|                    |   |                       |                                 |                           | 15.10 + 10.57                   | + 6.17 + 3.08) {                         | = 2.14 or 2.13716}                                 | M1         |               |
|                    | or $s = 8$  | 0 (1 - 0              | ).9733) {=                      | 2.136}                    |                                 |  |  |            |               |
|                    | r=1   | 7.26 (2dp             | s = 2.14                        | (2dp)                     | At least one                    |  | rt17.26 or $s = \text{awrt} 2.14$                  | A1         |               |
|                    |   |                       |                                 |                           |                                 | Both awrt $r =$                          | 17.26 and awrt $s = 2.14$                          | A1         | [2]           |
| (c)                | •   |                       | oution is a soution is no       |                           |                                 |  |  | B1         | [3]           |
|                    | l   | 1                     |                                 |                           | <u> </u>                        |  |  |            |               |
|                    | #   | $O_{i}$               | $E_{_i}$                        | Comb                      | Comb                            | $\frac{(O_i - E_i)^2}{E_i}$              | $\frac{O_i^2}{E_i}$                                |            |               |
|                    | calls   | $\mathcal{O}_i$       | $\boldsymbol{L}_{i}$            | $O_{_i}$                  | $E_{_{i}}$                      | $E_{_i}$                                 | $E_{i}$  |            |               |
|                    | 0   | 3                     | 2.42                            | 16                        | 10.88                           | 2.4094                                   | 23.5294  | M1         |               |
|                    | 2   | 13<br>14              | 8.46<br>14.80                   | 14                        | 14.80                           | 0.0432                                   | 13.2432  | 1V11       |               |
|                    | $\frac{2}{3}$   | 15                    | 17.26                           | 15                        | 17.26                           | 0.2959                                   | 13.0359  |            |               |
|                    | 4   | 10                    | 15.10                           | 10                        | 15.10                           | 1.7225                                   | 6.6225   |            |               |
|                    | 5   | 8                     | 10.57                           | 8                         | 10.57                           | 0.6249                                   | 6.0549   | M1         |               |
|                    | 6   | 8                     | 6.17                            | 8                         | 6.17                            | 0.5428                                   | 10.3728  |            |               |
|                    | 7<br>≥8   | 6 3                   | 3.08<br>2.14                    | 9                         | 5.22                            | 2.7372                                   | 15.5172  |            |               |
|                    |   | Totals 8.3759 88.3759 |                                 |                           |                                 |  |  |            |               |
|                    |   |                       |                                 |                           |                                 |  |  |            |               |
|                    | _   | H                     | $\frac{a}{a}$ or $\mathring{a}$ | $\frac{O^2}{E} - 80;$     | = awrt 8.38                     |  | awrt <u><b>8.38</b></u> or awrt <u><b>8.39</b></u> | A1         |               |
|                    | <i>n</i> = 7 - 1  | - 1 = 5               |                                 |                           |                                 |  |  | B1ft       |               |
|                    | $\chi_5^2(0.05)$  | = 11.070              | $\Rightarrow$ CR: 2             | $X^2 \geqslant 11.07$     | 0                               |  |  | B1ft       |               |
|                    | Inot in th  | e CR/not              | significant                     | /Do not reio              | ect Hol                         |  |  |            |               |
|                    | [not in the CR/not significant/Do not reject H <sub>0</sub> ]  Poisson distribution is a suitable model. (oe) |                       |                                 |                           |                                 |  |  |            |               |
|                    | 1 0100011   | 41541104110           | <u> </u>                        |                           | (0.0)                           |  |  | A1         | [7]           |
|                    |   |                       |                                 |                           |                                 |  |  |            | 11            |
| ( )                | D1 *  | A . 1                 |                                 | 1 ,                       | Not                             |  | . 2.5*   |            |               |
| (a)<br>(c)         | B1cso*  | l l                   |                                 |                           |                                 | vide by 80 to ach                        | neve 3.5°<br>nce. Inclusion of 3.5 for             | / in ic 1  | st <b>P</b> O |
| (c)                | 1 <sup>st</sup> M1  |                       |                                 |                           |                                 | s at both ends [ft                       |  | / 111 15 1 | В             |
|                    | 2 <sup>nd</sup> M1  |                       |                                 |                           |                                 |  | ions/values (to awrt/trun                          | cated 2    | d.p.)         |
|                    | 1 <sup>st</sup> A1  | awrt                  | 8.38 or awr                     | t 8.39 (Thi               | s implies the b                 | oth M1 marks)                            | `  |            | . ,           |
|                    | 2 <sup>nd</sup> B1ft  |                       |                                 |                           | _                               |  | btract 2 from their $n$ .                          |            |               |
|                    | 3 <sup>rd</sup> B1ft  |                       |                                 |                           |                                 |  | r n. (May see 9.488, 12.5                          | 592, 14.   | 067)          |
|                    | 2 <sup>nd</sup> A1  |                       |                                 |                           |                                 | onclusion which                          |  |            |               |
|                    | Note<br>Note  |                       |                                 |                           |                                 | hey are stated the<br>'significant, do n | e wrong way round.                                 |            |               |
|                    | Note<br>Note  |                       |                                 |                           | ore Au. E.g.<br>(3.5) in conclu |  | or reject H <sub>0</sub>                           |            |               |
|                    | 11016   | Conu                  | one the me                      |                           | (J.J) III COIICI                |  |  |            |               |

| Question<br>Number | Scheme  | Marks  |
|--------------------|---|--------|
| <b>5.</b> (a)      | Label beginners $1-452$ , intermediates $1-251$ , professionals $1-97$  | M1     |
|                    | <u>Use random numbers</u> to select a   | M1     |
|                    | Simple random sample of <u>28 beginners</u> , <u>16 intermediates</u> and <u>6 professionals</u> .  | A1     |
| (b)                | Any one of  | [3]    |
| (0)                | • Enables estimation of statistics/sampling errors for each strata.   | B1     |
|                    | Reduces variability.  | DI     |
|                    | <ul> <li>More representative of the population/reflects population structure</li> </ul>   | [1]    |
| (c)                | $H_0: m_1 - m_B = 3$ $H_1: m_1 - m_B > 3$   | B1; B1 |
| (4)                | s.e. = $\sqrt{\frac{38.1}{60} + \frac{57.3}{80}} $ {= 1.162432794}  | M1     |
|                    | 36.9 - 31.7 - 3   | dM1;   |
|                    | $z = \frac{36.9 - 31.7 - 3}{"1.1624}$ ; = 1.89258 awrt 1.89   | A1     |
|                    | One tailed c.v. $Z = 1.6449$ or $CR : Z \ge 1.6449$ or p-value = awrt $0.029 < 0.05$  | B1     |
|                    | [in the CR/significant/Reject H <sub>0</sub> /"0.029" < 0.05]   |        |
|                    | <ul> <li>Conclude either that the</li> <li>mean score of intermediates is more than 3 greater than the mean score of beginners. (oe)</li> <li>manager's belief is correct.</li> </ul> | A1     |
|                    |   | [7]    |
|                    |   | 11     |
|                    | Alternative method for "2 <sup>nd</sup> M1, 1 <sup>st</sup> A1, 3 <sup>rd</sup> B1" marks: Let $D = \overline{x}_I - \overline{x}_B$  |        |
|                    | $1.6449 = \frac{D-3}{1.1624}$ dependent upon the 1 <sup>st</sup> M1 for $\frac{D-3}{\text{their "1.1624"}} = 1.6449/1.645/1.64/1.65$  | dM1:   |
|                    | So, $D = 4.912$ $D = \text{awrt } 4.91 \text{ and } D_{\text{obs}} = 5.2$   | A1     |
|                    | $D_{\text{obs}} = 36.9 - 31.7 = 5.2$ [1.64, 1.65]   | B1     |
|                    |   |        |

|     |                     | Notes  |  |  |  |  |  |  |
|-----|---------------------|--|--|--|--|--|--|--|
| (a) | 1st M1              | for a suitable numbered/labelled list for each ability level   |  |  |  |  |  |  |
|     | 2 <sup>nd</sup> M1  | for use of random numbers/sample to select beginners, intermediates and professionals.                         |  |  |  |  |  |  |
|     | A1                  | (dependent on either the 1 <sup>st</sup> or the 2 <sup>nd</sup> M1 mark)                                       |  |  |  |  |  |  |
|     |                     | For <u>28 beginners</u> , <u>16 intermediates</u> and <u>6 professionals</u> .                                 |  |  |  |  |  |  |
| (c) | 1st B1              | $H_0: m_I - m_B = 3 \text{ oe}$  |  |  |  |  |  |  |
|     | 2 <sup>nd</sup> B1  | $H_1: m_I - m_B > 3 \text{ oe}$  |  |  |  |  |  |  |
|     | Note                | If $m_1, m_2$ used then it must be clear which one refers to intermediates/beginners.                          |  |  |  |  |  |  |
|     | 1 <sup>st</sup> M1  | s.e. = $\sqrt{\frac{38.1}{60} + \frac{57.3}{80}}$ . May be implied by s.e. = awrt 1.16                         |  |  |  |  |  |  |
|     |                     | Condone minor slips e.g. $\sqrt{\frac{38.1}{80} + \frac{57.3}{60}}$  |  |  |  |  |  |  |
|     | 2 <sup>nd</sup> dM1 | Dependent upon the 1 <sup>st</sup> M1. (follow through their s.e. if 1 <sup>st</sup> M1 mark has been awarded) |  |  |  |  |  |  |
|     | 1 <sup>st</sup> A1  | awrt 1.89  |  |  |  |  |  |  |
|     | 3 <sup>rd</sup> B1  | $1.64 \le  C.V.  \le 1.65$ (compatible sign with their test statistic) or a correct probability comparison.    |  |  |  |  |  |  |
|     | 2 <sup>nd</sup> A1  | Dep. on all M1 and B1 marks scored for contextualised comment which is rejecting $H_0$ .                       |  |  |  |  |  |  |

| Question<br>Number |  | Scheme  |   | Ma | rks |  |  |  |
|--------------------|--|---|---|----|-----|--|--|--|
| <b>6.</b> (a)      | $\overline{x} = 230.5$   | 5; 95% confidence limits for <i>m</i> are         |   |    |     |  |  |  |
|                    | 230.5  | $5 \pm 1.96 \cdot \frac{1.2}{\sqrt{5}}$           | their $\overline{x} \pm z = \frac{1.2}{\sqrt{5}}$ | M1 |     |  |  |  |
|                    |  | ······································            | z = 1.96  | B1 |     |  |  |  |
|                    | =(229.44)  | 4815, 231.55185) = awrt(229.4, 231.6)             | At least one end-point is correct.                | A1 |     |  |  |  |
|                    | (,   |   | Both end-points are correct.                      | A1 |     |  |  |  |
|                    |  |   |   |    |     |  |  |  |
| (b)                | { Let $X =$ number of confidence intervals that <b>don't contain</b> $m$ }                 |   |   |    |     |  |  |  |
|                    | ${So X \sim} B(20,0.05)$   |   |   |    |     |  |  |  |
|                    | ${P(X>3)}=1-P(X \le 3) \text{ or } 1-0.9841$   |   |   |    |     |  |  |  |
|                    | = 0.0159 awrt <u><b>0.0159</b></u>   |   |   |    |     |  |  |  |
|                    |  |   |   |    | [3] |  |  |  |
|                    |  |   |   |    | 7   |  |  |  |
|                    |  | Note  | es  |    |     |  |  |  |
| (b)                | M1   | Writing or using either $X \sim B(20, 0.05)$ or Y | $V \sim B(20, 0.95)$                              |    |     |  |  |  |
|                    | 1st A1 $1-P(X \le 3)$ or $1-0.9841$ or $P(Y \le 16)$ . Can be implied by the final answer. |   |   |    |     |  |  |  |
|                    | 2nd A1   | awrt 0.0159                                       | •   |    |     |  |  |  |
|                    |  |   |   |    |     |  |  |  |
|                    |  |   |   |    |     |  |  |  |
|                    |  |   |   |    |     |  |  |  |
|                    |  |   |   |    |     |  |  |  |

| Question<br>Number | Scheme  | Marks |
|--------------------|---|-------|
| 7. (a)             | $A = \frac{X_1 + X_2 + X_3 + Y_1 + Y_2}{5},  X \sim N(30, 4.5^2),  Y \sim N(20, 3.5^2);  X,  Y \text{ are independent.}$                            |       |
|                    | $E(A) = \frac{3(30) + 2(20)}{5}$ or $Var(A) = \frac{3(4.5)^2 + 2(3.5)^2}{25}$ A correct method for finding $E(A)$ or $Var(A)$                       | M1    |
|                    | E(A) = 26 or $Var(A) = 3.41$ At least one of either $E(A) = 26$ or $Var(A) = 3.41$  | A1    |
|                    | Both $E(A) = 26$ and $Var(A) = 3.41$  | A1    |
|                    | $\{\text{So } A \sim N(26, 3.41)\}$   |       |
|                    | $\left\{ P(A < 24) = \right\}  P\left(Z < \frac{24 - 26}{\sqrt{3.41}}\right)$ Standardising (±) with their mean and their standard deviation        | M1    |
|                    | and their standard deviation $\sqrt{3.41}$  | 1011  |
|                    | = P(Z < -1.08306)   |       |
|                    | = 1 - 0.8599  | M1    |
|                    | = 0.1401 (or 0.139391) <u>0.14</u> or awrt <u>0.140</u> or awrt <u>0.139</u>  | A1    |
|                    |   | [6]   |
| (b)                | $W \sim N(m, 2.8^2)$ ; $P(W - X < 4) = 0.1$ W, X are independent.   |       |
|                    | $\left\{ E(W - X) = E(W) - E(X) = m - 30 \right\} \triangleright E(W - X) = m - 30$ $E(W - X) = m - 30$   | B1    |
|                    | $\left\{ \text{Var}(W - X) = \right\} 2.8^2 + 4.5^2 \left\{ = 28.09 \right\}$ $2.8^2 + 4.5^2$   | M1    |
|                    | {So W - X N(m-30, 28.09)}   |       |
|                    | $\left\{ P(W - X < 4) = 0.1 \right\} \implies P\left( Z < \frac{4 - (m - 30)}{\sqrt{2.8^2 + 4.5^2}} \right) = 0.1$                                  |       |
|                    | Standardising $(\pm)$ with their mean which is in terms of $m$  |       |
|                    | 4 - (m - 30) and their standard deviation and setting the result equal to   | M1    |
|                    | $\frac{4 - (m - 30)}{\sqrt{2.8^2 + 4.5^2}} = k \ (= -1.2816)$ k, where  k  is in the interval [1.28, 1.29].   |       |
|                    | $\pm 1.2816$ or awrt $\pm 1.2816$   | B1    |
|                    | Correct equation . See notes  | A1    |
|                    | $\{ m = 34 + 1.2816(5.3) \triangleright \} $ $m = 40.792 (= 40.784 \text{ from using } -1.28) $ awrt <u>40.8</u>                                    | A1    |
|                    |   | [6]   |
|                    | NT /  | 12    |
| (a)                | Notes  3 <sup>rd</sup> M1 For a probability tail compatible with 24 and their mean  |       |
| (4)                |   |       |
| (b)                | 2 <sup>nd</sup> M1 Allow $\pm \frac{4 - \text{their } E(W - X)}{\sqrt{\text{their } Var(W - X)}} = k$ , where $ k $ is in the interval [1.28, 1.29] |       |
|                    | 2 <sup>nd</sup> B1 For either -1.2816 or 1.2816   |       |
|                    | 1st A1 E.g. Allow $\frac{4 - (m - 30)}{\sqrt{2.8^2 + 4.5^2}} = [-1.29, -1.28]$ or $\frac{(m - 30) - 4}{\sqrt{2.8^2 + 4.5^2}} = [1.28, 1.29]$        |       |

| Question<br>Number |   | Scheme   | Mark     | ís . |  |  |  |  |  |
|--------------------|---|--|----------|------|--|--|--|--|--|
| 8.                 | X follows                                     | s a continuous unform distribution over $\left[2 + 3, 22 + 9\right]$ ; $Y = \frac{2\overline{X}}{3} + k$   |          |      |  |  |  |  |  |
| (a)                | $\left\{ \mathrm{E}(\overline{X}) = \right\}$ | $m = \frac{2a + 9 + a + 3}{2}$   | M1       |      |  |  |  |  |  |
|                    |   | $= \frac{3a}{2} + 6 \text{ or } \frac{3a+12}{2} + \frac{1}{2} = \frac{3a}{2} + \frac{1}{2} = $ | A1       |      |  |  |  |  |  |
| (b)                | bias {=                                       | bias $\left\{ = \frac{3a}{2} + 6 - a \right\} = \frac{1}{2}a + 6$ or $\frac{a+12}{2}$ (allow ±)  |          |      |  |  |  |  |  |
| (c)                |   | $\frac{2}{3}E(\bar{X}) + k = 2 \Rightarrow \frac{2}{3}\left(\frac{3a}{2} + 6\right) + k = 2$   | M1       | [1]  |  |  |  |  |  |
| (c)                | (   | $\frac{3}{3} \stackrel{\text{L}(\Lambda) + k - a}{\longrightarrow} \frac{3}{3} \frac{3}{2} \stackrel{\text{+} 0}{\longrightarrow} + k - a}{k = a} \stackrel{\text{L}(\Lambda) + k - a}{\longrightarrow} \frac{k = -4}{3}$  | A1       |      |  |  |  |  |  |
|                    |   |  |          | [2]  |  |  |  |  |  |
| (d)                | ( 3   | $\overline{X} - 4 \Rightarrow \hat{a} = \frac{2}{3}(7.8) - 4 = 1.2$  | M1       |      |  |  |  |  |  |
|                    | Max valu                                      | $e = 2(1.2) + 9$ $= 11.4 \text{ or } 11\frac{2}{5} \text{ or } \frac{57}{5}$   | M1<br>A1 |      |  |  |  |  |  |
|                    |   | $\frac{11.4 \text{ of } 11\frac{1}{5} \text{ of } \frac{1}{5}}{5}$   | A1       | [3]  |  |  |  |  |  |
|                    |   | Notes  |          | 8    |  |  |  |  |  |
| (a)                | M1  | Using the formula $\left(\frac{b+a}{2}\right)$ or obtaining $\frac{3a+12}{2}$ or $\frac{3a}{2}+6$  |          |      |  |  |  |  |  |
|                    | A1  | $\frac{3a}{2} + 6$ or $\frac{3a+12}{2}$ and <sup>1</sup> a.  |          |      |  |  |  |  |  |
| (b)                | B1ft  | bias = $\pm \left(\frac{1}{2}a + 6\right)$ or $\pm \left(\frac{a+12}{2}\right)$ or ft their $\mu$ provided $\mu \neq \alpha$   |          |      |  |  |  |  |  |
| (c)                | M1  | Sets $\frac{2}{3}$ (their E( $\overline{X}$ )) + $k = a$ . This mark can be implied.   |          |      |  |  |  |  |  |
|                    | A1  | k = -4. Note that $k = -4$ with no working is M1 (implied) A1.   |          |      |  |  |  |  |  |
| (d)                | 1 <sup>st</sup> M1                            | An attempt to use the sample data given to find $\frac{2}{3}\bar{x}$ + "their $k$ ".   |          |      |  |  |  |  |  |
|                    |   | Allow full expression for $\bar{x}$ or $\frac{\sum x}{n}$ . (Note that from the data $\bar{x} = 7.8$ )   |          |      |  |  |  |  |  |
|                    | 2 <sup>nd</sup> M1                            | 2 "their $a$ " + 9 where their $a$ is a function of the sample mean – which has been for applying $\frac{\sum x}{x}$ from the data values given in the question.   | ound by  |      |  |  |  |  |  |
|                    | A1  | $\frac{-1}{n}$ 11.4 cao  |          |      |  |  |  |  |  |
|                    | Note  | 2(10.6) + 9 = 30.2 is M0M0A0   |          |      |  |  |  |  |  |