

Mark Scheme (Results)

January 2019

Pearson Edexcel International Advanced Level In Statistics S2 (WST02/01)

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement.
 All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL IAL MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper or ag- answer given
- Cord... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread

however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. Ignore wrong working or incorrect statements following a correct answer.

Question Number	Scheme	Marks
1. (a)	Any one response in context from: Each person <u>turns up</u> independently/randomly of others oe Probability/proportion/percentage of not <u>turning up</u> remains constant (5%) oe	B1
(b) (i) (ii)	$X \sim B(50, 0.05)$ $[P(X=0) =] 0.076944$ awrt $\underline{0.0769}$ $P(X=1) = 0.2794 - 0.0769 = 0.20248$ awrt $\underline{0.202/0.203}$	(1) B1 M1A1
(c)	Let $T = \text{total earnings for a journey}$ $\begin{array}{ c c c c c c c c c c c c c c c c c c c$	(3) M1
	$E(T) = 880 \times \text{``}0.0769\text{''} + 940 \times \text{``}0.2025\text{''} + 1000 \times (1 - (\text{``}0.0769 + 0.2025\text{''}))$ =£978.62 awrt (£) <u>979</u>	dM1 A1 (3)
	Alternative Let $S = possible pay out$ $ \begin{array}{c cccc} S & 60 & 120 \\ \hline P(S = s) & "0.2025" & "0.0769" \end{array} $	Alternative M1
	$E(T) = 1000 - (120 \times "0.0769" + 60 \times "0.2025")$ =£978.62 awrt (£) <u>979</u>	dM1 A1 [7 marks]
(a)	Notes Must be in context containing the words in bold. Allow turning up rather than not turni	ng up and vice
(b) (ii)	versa. M1 for correct use of tables or for correct use of formula $50(0.05)(0.95)^{49}$ Allow $P(X \le 1) - P(X = 0)$ oe written of used	
(c)	1^{st} M1 for identifying the 3 possible total earnings 880, 940, 1000 oe 2^{nd} dM1 for a correct ft expression for E(T) eg 880 × 'their b(i)' + 940 × 'their b(ii)' + 1000 × (1 – ('their b(i) + their b(ii))	
	Alternative: 1^{st} M1 for identifying the 2 possible pay outs 120 and 60 oe 2^{nd} dM1 for a correct ft expression for E(T) Eg $1000 - (120 \times \text{their b(i)} + 60 \times \text{their b(ii)})$	
	Eg	

Question Number	Scheme	Marks
2. (a)	$[X \sim \text{Po}(2)]$ $P(X < 5) = P(X \le 4)$ = 0.947346 awrt <u>0.947</u>	M1 A1
(b)	$Y \sim Po(6)$	B1 (2)
	$e^{-6} \frac{6^n}{(n)!} = e^{-6} \frac{6^{n+1}}{(n+1)!} \rightarrow (n+1) = 6$ or $P(Y=4) = 0.13385$ P(Y=5) = 0.16062 P(Y=6) = 0.16062	M1
	$\underline{n=5}$	A1 (3)
(c)	$[D \sim Po(9)]$ $P(c \le D \le 12) = P(D \le 12) - P(D \le c - 1) \text{ or } P(X \le d) = 0.8758 - 0.8546$	M1
	$0.8546 = 0.8758 - P(D \le c - 1)$ = 0.0212 $P(D \le c - 1) = 0.0212$ $P(X \le 3) = 0.0212$ c - 1 = 3	dM1
	$\frac{c-1-3}{c=4}$ $\underline{c=4}$	A1
(d)	$P(X=2) = 0.27067$ $W \sim B(6, \text{ awrt } 0.27067)$ $P(W=4) = {}^{6}C_{4}("0.27067")^{4}(1 - "0.27067")^{2}$ $= 0.0428$ awrt <u>0.043</u>	(3) B1 B1ft M1 A1
		[12 marks]
(a)	Notes M1 for writing or using $P(X \le 4)$ If answer is incorrect this must be shown	
. ,	 B1 for writing or using Po(6) M1 for a correct expressions for P(Y = n) and P(Y = n + 1) using their value of λ or foliast 2 of the given probabilities for Po(6) only correct to 3sf. A1 must be only one value of n given. If more than one value of n is given working n to award the B1 and M1, 5 on its own gains B1M1A1 	
(c)	1 st M1 for the expression $P(D \le 12) - P(D \le c - 1)$ oe Condone $P(D \le 12) - P(D \le 12)$	c) allow any

letters.

2nd dM1 for correct substitution of 0.8758 (awrt 0.876) and 0.8546 leading to $P(D \le c - 1) = a$ probability. Condone $P(D \le c) = a$ probability allow any letters

For an awrt 0.043 from correct working award full marks.

1st B1 for awrt 0.271 seen

 2^{nd} B1ft Follow through their P(X=2) but you must see either B(6, "0.27067...") or working of the form $("0.27067...")^4(1 - "0.27067...")^2$. Condone missing 6C_4

NB If P(X = 2) is not stated and 0.271 is not seen do not ft.

M1 ${}^{6}C_{4} p^{4}(1-p)^{2}$ or $P(W \le 4) - P(W \le 3)$ or 0.9932... 0.9504... written

Question Number	Scheme	Marks
	P(3 < X < 7) = F(7) - F(3) [= 0.7 - 0.2] <u>0.5</u>	M1 A1 (2)
(b)	$a = \frac{0.4 - 0}{4 - 2}$ $b = \frac{0}{6 - 4}$ $c = \frac{1 - 0.4}{8 - 6}$ $\underline{a = 0.2}$ $\underline{b = 0}$ $\underline{c = 0.3}$	M1 A1 A1
(c)	$E(X) = \int_{2}^{4} 0.2 x dx \left[+ \int_{4}^{6} 0 x dx \right] + \int_{6}^{8} 0.3 x dx$	(3) M1
	$E(X) = \left[\frac{0.2x^2}{2}\right]_2^4 + \left[\frac{0.3x^2}{2}\right]_6^8$	A1ft
	$= \underline{5.4}$	A1 (3)
	Alternative E(X) = $3 \times p + 7 \times 2 \times$ "their c" or $3 \times 2 \times$ "their a"+ $7 \times p$ where $0 = 3 \times"0.4"+ 7 \times"0.6"= 5.4$	Alternative M1 A1ft A1
		[8 marks]
(a)	Notes M1 for writing or using $F(7) - F(3)$ Implied by answer 0.5	
(b)	M1 for attempt to find the gradient of at least 1 line segment (may be implied by either a or c correct) 1st A1 two values correct 2nd A1 all three values correct	
(c)	M1 for a correct expression for $\int xf(x) dx$ (ignore limits) using their a, b and c (Cond	done a , b and c
	as a function of x) and an attempt to integrate $(x^n \to x^{n+1})$. No need to see $\int_4^6 "0"x \ dx$ in	f b = 0
	otherwise it must be present A1ft correct integration with correct limits (ft their constants a, b and c from part (b)) A1 5.4 oe	
	Alternative M1 must have 3, 7 and one half correct ft their values for a/c . A1ft $3\times2\times$ "their a "+ $7\times2\times$ "their c " A1 5.4 oe	

Quest Numb		Scheme		Marks		
-	()	$H_{0:} p = 0.35$ $H_{1:} p > 0.35$			B1	
		Probability 1	oute		CR route	
		$P(X \ge 11) = 1 - P(X \le 10)$	(a) [= 1 – 0.9468]	$P(X \le 11)$	= 0.9804	M1
				$P(X \ge 12)$	= 0.0196	
		=0.0532		$CR: X \ge 1$		A1
		Do not Reject H ₀ or not si	gnificant or 11 do	es not lie in th	ne CR	dM1
		Hadi's belief is not suppor	ted or			Alcso
		the <u>proportion</u> of customer	rs paying by credit	card is not gr	reater than 35%.	
						(5)
	(b)	$X \sim B(20, 0.35)$				
		[E(X) =] 7				B1
		S.D. = $\sqrt{20 \times 0.35 \times 0.65}$ [$=\sqrt{4.55}=2.133$.]		B1
		"7" + 2 × "2.133" 11 - 11 < 11.266	"7" < 2 × 2.133…	$\frac{11-"7"}{\sqrt{"4.55"}}$	11 - 2 × "2.133…"	M1
		11 < 11.266	4 < 4.266	1.875 < 2	6.734 < 7	Alcso
		ı		l	I	(4)
						[9 marks]
		Notes		I.		
	(a) B1 both hypotheses correct (may use p or π). Must have H_0 and H_1 1^{st} M1 for writing or using $1 - P(X \le 10)$ or if leading to a CR allow $P(X \le 11) = \text{awrt } 0.93$ (condone 0.98) or $P(X \ge 12) = \text{awrt } 0.0196$ (may be implied by awrt 0.0532 or correct for 0.0532 or CR: $X \ge 12$ oe					
		NB M1 A1 for 0.9468 < 0.9	5			
		2 nd M1 Dependent on the 1		./	I I CD	
			ent i.e. not significa ir probability/CR ar		ust have a Critical regio	n not just a
		Do not allow non-c	ontextual conflicting			
		May be implied by a correct 2 nd A1cso fully correct solution	on and correct conte	extual statemen		juired and in a
		correct statement. eg Allow The (proportion/percentage/r	_			er/is
		35%(0.35)/ remains the same	e) or there is insuffic			
	(b)	pay by credit card has increa $1^{st} B1 E(X) = 7$	sed			
	. ,	2 nd B1 for a correct express M1 for using 'mean' + 2			ir mean" < 2 × 'standar	d deviation'
		or $\frac{11 - \text{"their E}(X)\text{"}}{\text{UTL in all Beta Interpolation}}$ If E(X)			ii iiicaii 🔨 2 ^ Staiidai	u deviation
		"I heir sa"		icii ailow		
		5 < E(X) < 10 and A1cso for comparison with		awrt (11.3 or 4.	.27 or 1.88 or 6.43) oe a	nd no errors
		seen			·	

Question Number	Scheme	Marks	
5. (a)(i)	(b-2a)-a = 1 $b-(b-2a) = 2$		
<i>(u)</i> (1)	$\frac{(b-2a)-a}{b-a} = \frac{1}{3} \qquad \frac{b-(b-2a)}{b-a} = \frac{2}{3}$	M1	
	3(b-3a) = (b-a) $6a = 2(b-a)$		
	b = 4a or $b = 4a$		
	$_{\mathrm{E}(V)}$ $a+4a$ $5a_{*}$ $_{\mathrm{E}(V)}$ $a+4a$ $5a_{*}$	M1A1cso	
	$E(X) = \frac{a+4a}{2} = \frac{5a}{2}$ * $E(X) = \frac{a+4a}{2} = \frac{5a}{2}$ *	(3)	
(ii)	[P(X > b - 4a) = P(X > 0) =] 1	B1	
		(1)	
(b)(i)	$\frac{(c-3)^2}{12} = 3c - 9$	M1	
	$\frac{12}{12}$ = 3c = 9		
	$c^2 - 42c + 117 = 0 \rightarrow (c - 3)(c - 39) = 0$	M1	
	c = 39	A1	
		(3)	
(ii)	P(2Y-7<20-Y)=P(Y<9)	M1	
	$\frac{9-3}{'39'-3} = \frac{1}{6}$ awrt 0.167	A1ft A1	
	39-3 6	(3)	
(;;;)	$E(Y^2) = Var(Y) + [E(Y)]^2 = (3('39') - 9) + (\frac{'39' + 3}{2})^2$	M1 A1ft	
(111)	$L(1) \text{val}(1) \mid L(1) \mid (3(3)) \mid (3) \mid (2)$	MITAIII	
	$E(Y^2) = \underline{549}$	A1 (3)	
		[13 marks]	
	Notes	[]	
(a)(i)	1^{st} M1 for a correct probability equation = $\frac{1}{3}$ (or a correct probability equation = $\frac{2}{3}$) in t	$\frac{1}{1}$ erms of a and b	
	2^{nd} M1 for use of E(X) = $\frac{a+'4a'}{2}$ oe		
	Alcso correct solution with no errors seen.		
(b)(i)	1 st M1 for $\frac{(c-3)^2}{12} = 3c - 9$		
	_		
	2^{nd} M1 for rearranging correctly to form 3TQ = 0 and attempt to solve or $\frac{c-3}{12}$ = 3 oe		
	For attempt at factorising it must give two of the terms when multiplied out		
	For using the formula allow 1 slip if the correct formula is written down otherwise no For completing the square allow one sign error.	errors	
	A1 If more than one value is given and $c = 39$ is not clearly selected then A0. Allow [3,39]	
(ii)	M1 for rearranging to (or using) $P(Y < 9)$		
	1 st A1ft for a correct probability expression ft their '39'. If (i) is incorrect we must see	a correct	
	expression eg $\frac{9-3}{"39"-3}$ or $\frac{6}{"36"}$ to ft		
(iii)	1201	_	
	M1 for writing or using $E(Y^2) = Var(Y) + [E(Y)]^2$ (must be $E(Y^2) = \int_{3}^{39} \frac{1}{39^3 - 3} y^2 dy$	with $y^2 \rightarrow y^3$	
	condone different letter. If c is incorrect, they must show where $Var(Y)$ and $E(Y)$		
	A1ft correct (follow through) expression for $E(Y^2)$ allow $\frac{1}{^{1}39'-3}\left[\frac{y^3}{3}\right]_3^{^{1}39'}$		
	The sense (tensor anomaly expression for $E(1)$ and $\frac{1}{3}$		

Question Number	Scheme	Marks
6. i.(a)	n is large and p is small	B1 (1)
(b)	$[X \sim B(3000, 0.0025) \rightarrow] Y \sim Po(7.5)$ $P(Y > 7) = 1 - P(Y \le 7) = 1 - 0.5246 = 0.47536$ awrt 0.475	B1 M1 A1 (3)
ii.(a)	A list/database/register of all employees	B1 (1)
(b)	The probability distribution of the number of employees that cycle to work [from all possible samples of 150]	B1
(c)	$D \sim N(60, 36)$ $P(C \le \alpha) = P(Z \le z) = 0.0668$ $\frac{\alpha - 60''}{6''} = -1.5 \text{ or } \frac{60'' - \alpha}{6''} = 1.5$	(1) B1 M1 B1
	"6" $= 1.5$ or "6" $= 1.5$ $\underline{\alpha} = 51$	A1cao (4)
(d)	$P\left(Z \le \frac{"51" - "60" + 0.5}{"6"}\right)$ $= P(Z \le -1.42) = 1 - 0.9222$	M1
	= 0.0778/0.0782 awrt <u>0.078</u>	A1 (2) [12 marks]
	Notes	•
(a) i. (b) ii (a) (b) (c)	n is bigger then 10 and $p < 0.25B1 for writing or using Po(7.5)M1 for writing or using 1 - P(Y \le 7) oeB1 must be all employeesB1 Allow number of employees that cycle to work and their associated probabilities$	

Question Number	Scheme	Marks
7. (a)	$\int_{-3}^{0} c(x+3) dx + \int_{0}^{3} \frac{5}{36} (3-x) dx \text{or} \text{area of triangle} = \frac{3 \times 3c}{2} + \frac{3 \times \frac{5}{36} (3)}{2}$	M1
	$c(-\frac{9}{2}+9)+\frac{5}{8}=1$ oe $\frac{3\times 3c}{2}+\frac{5}{8}=1$ oe	dM1
	$c = \frac{1}{12} *$ Alternative	A1cso (3)
	Alternative $\left[\int c(x+3) \right] = c \left(\frac{x^2}{2} + 3x \right) + d \text{ and } \left[\int \frac{5}{36} (3-x) \right] = \frac{5}{36} \left(3x - \frac{x^2}{2} \right) + e$	M1
	Using $F(-3) = 0$ and $F(3) = 1$ and $d = e$	dM1
	$c = \frac{1}{12}$ *	A1 cso
(b)(i)	A correct sketch of $f(x)$ with straight line positive gradient from $-3 \le x < 0$ and straight line negative gradient from $0 \le x \le 3$, LHS below RHS at y axis Correct labels: -3 and 3 on x -axis and $\frac{1}{4}$ and $\frac{5}{12}$ oe on y -axis	B1 B1
(ii)	Highest point [at $f(0)$, so $X = 0$ is the mode] oe	B1
. ,		(3)
(c)	$\int_{-3}^{x} \frac{1}{12}(t+3) dt$ or $\int_{-3}^{1} \frac{1}{12}(x+3) dx$ with $+c$ and $F(-3) = 0$	M1
	$\int_{-3}^{x} \frac{1}{12}(t+3) dt \qquad \text{or} \qquad \int_{\frac{1}{12}}^{1} (x+3) dx \text{with } + c \text{ and } F(-3) = 0$ $\int_{-3}^{0} \frac{1}{12}(t+3) dt + \int_{0}^{x} \frac{5}{36}(3-t) dt \qquad \text{or} \qquad \int_{\frac{5}{36}}^{5} (3-x) dx \text{with } + d \text{ and } F(3) = 1$ $\begin{cases} 0 & x < -3 \end{cases} \qquad \begin{cases} 0 & \end{cases}$	
	$ \begin{cases} 0 & x < -3 \\ \frac{1}{24}x^2 + \frac{1}{4}x + \frac{3}{8} & -3 \le x < 0 \end{cases} $ or $F(x) = \begin{cases} 0 \\ \frac{1}{24}(x+3)^2 \end{cases}$	B1
	$F(x) = \begin{cases} 0 & x < -3 \\ \frac{1}{24}x^2 + \frac{1}{4}x + \frac{3}{8} & -3 \le x < 0 \\ \frac{5}{12}x - \frac{5}{72}x^2 + \frac{3}{8} & 0 \le x \le 3 \\ 1 & x > 3 \end{cases} $ or $F(x) = \begin{cases} 0 \\ \frac{1}{24}(x+3)^2 \\ 1 - \frac{5}{72}(3-x)^2 \\ 1 \end{cases}$	A1 A1 (4)
(d)	$[P(X>d \mid X>0) =] \frac{1-F(d)}{1-F(0)} = \frac{2}{5} \text{ oe}$	M1
	$1 - F(d) = \frac{2}{5} \times \frac{5}{8} \left[= \frac{1}{4} \right] \text{ oe}$	A1
	Using cdf or area of triangle $1 - \left(\frac{5}{12}d - \frac{5}{72}d^2 + \frac{3}{8} \right) = \frac{2}{5} \times \frac{5}{8}$ or $\frac{(3-d)\frac{5}{36}(3-d)}{2} = \frac{2}{5} \times \frac{5}{8}$ oe	dM1
	$d = \text{awrt } \underline{1.10}$	A1
		(4) [14 marks]
	Notes	
(a)	M1 for correct integrals added, including limits, or area of triangle. Condone missing Do not accept $c(0+3)=5/36(3-0)$ dM1 for equating to 1 and attempting to solve	dx
(b)(ii)	A1 cso for $c = \frac{1}{12}$ with no incorrect working seen B1: oe eg Maximum value. Condone highest probability	
(c)	M1 for attempting to integrate first line of pdf with correct limits $\underline{\mathbf{or}} + c$ and $F(-3) = 0$ $\underline{\mathbf{or}}$ for attempting to integrate second line of pdf with correct limits $+F(0)$ $\underline{\mathbf{or}}$ +	

(d)	NB Allow use of $F(0) = \frac{3}{8}$ instead of either $F(-3) = 0$ or $F(3) = 1$ B1 1 st and 4 th line correct. Allow one of range to be otherwise, \leq instead of \leq and \geq instead of $>$ 1 st A1 correct 2 nd line with limits. Allow \leq instead of \leq and vice versa 2 nd A1 correct 3 rd line with limits. Allow \leq instead of \leq and vice versa 1 st M1 for a correct probability expression, allow $\frac{P(X > d)}{P(X > 0)} = \frac{2}{5}$ oe implied by A1. Do not allow $P(X > d) \cap P(X > 0)$ for $P(X > d)$ 1 st A1 for $1 - F(d) = \frac{2}{5} \times \frac{5}{8}$ or $1 - P(x < d) = \frac{2}{5} \times \frac{5}{8} [= \frac{1}{4}]$ or $F(d) = \frac{3}{4}$ or $P(x > d) = \frac{1}{4}$ oe 2 nd dM1 previous M1 awarded. For $1 - F(d) = 1$ their $P(X > d)$ for their cdf oe and attempting to solve leading to a value for d .
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