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Other names

Pearson Edexcel
International
Advanced Level

Centre Number

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Candidate Number

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Core Mathematics C34

Advanced

Tuesday 17 January 2017 – Morning

Time: 2 hours 30 minutes

Paper Reference

WMA02/01

You must have:

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

1. Find an equation of the tangent to the curve

$$x^3 + 3x^2y + y^3 = 37$$

at the point $(1, 3)$. Give your answer in the form $ax + by + c = 0$, where a , b and c are integers.

(6)

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Question 1 continued

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Q1

(Total 6 marks)



(Total 7 marks)

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3. (a) Express $\frac{9 + 11x}{(1 - x)(3 + 2x)}$ in partial fractions. (3)

- (b) Hence, or otherwise, find the series expansion of

$$\frac{9 + 11x}{(1 - x)(3 + 2x)}, \quad |x| < 1$$

in ascending powers of x , up to and including the term in x^3 .
Give each coefficient as a simplified fraction.

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Question 3 continued



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Question 3 continued

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Q3

(Total 9 marks)



$$f(x) = \frac{4}{3x+5}, \quad x > 0$$

$$g(x) = \frac{1}{x}, \quad x > 0$$

- (a) state the range of f , (2)
- (b) find $f^{-1}(x)$, (3)
- (c) find $fg(x)$. (1)
- (d) Show that the equation $fg(x) = gf(x)$ has no real solutions. (4)

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Question 4 continued

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(Total 10 marks)



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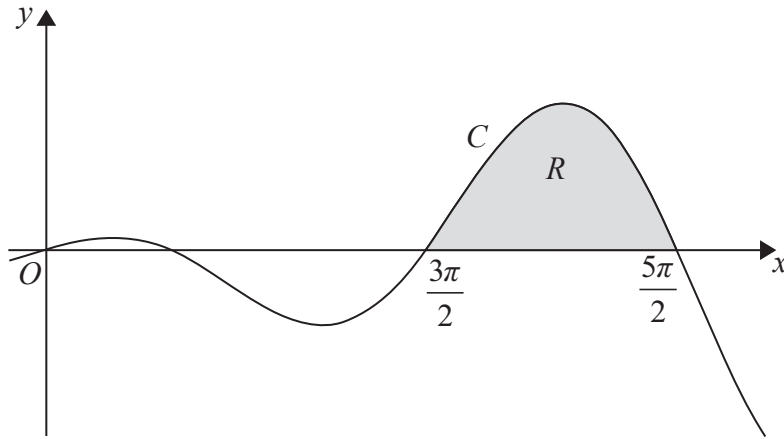


Figure 1

Figure 1 shows a sketch of part of the curve C with equation

$$y = x \cos x, \quad x \in \mathbb{R}$$

The finite region R , shown shaded in Figure 1, is bounded by the curve C and the x -axis for $\frac{3\pi}{2} \leq x \leq \frac{5\pi}{2}$

- (a) Complete the table below with the exact value of y corresponding to $x = \frac{7\pi}{4}$ and with the exact value of y corresponding to $x = \frac{9\pi}{4}$

x	$\frac{3\pi}{2}$	$\frac{7\pi}{4}$	2π	$\frac{9\pi}{4}$	$\frac{5\pi}{2}$
y	0		2π		0

(1)

- (b) Use the trapezium rule, with all five y values in the completed table, to find an approximate value for the area of R , giving your answer to 4 significant figures.

(3)

- (c) Find

$$\int x \cos x \, dx$$

(3)

- (d) Using your answer from part (c), find the exact area of the region R .

(2)



Question 5 continued

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Question 5 continued

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(Total 9 marks)

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6. (i) Differentiate $y = 5x^2 \ln 3x$, $x > 0$

(2)

- (ii) Given that

$$y = \frac{x}{\sin x + \cos x}, \quad -\frac{\pi}{4} < x < \frac{3\pi}{4}$$

show that

$$\frac{dy}{dx} = \frac{(1+x)\sin x + (1-x)\cos x}{1 + \sin 2x}, \quad -\frac{\pi}{4} < x < \frac{3\pi}{4}$$

(4)

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Question 6 continued

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Q6



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Question 7 continued

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Q7

(Total 7 marks)



8. (a) Using the trigonometric identity for $\tan(A + B)$, prove that

$$\tan 3x = \frac{3 \tan x - \tan^3 x}{1 - 3 \tan^2 x}, \quad x \neq (2n + 1)30^\circ, \quad n \in \mathbb{Z} \quad (4)$$

- (b) Hence solve, for $-30^\circ < x < 30^\circ$,

$$\tan 3x = 11 \tan x$$

(Solutions based entirely on graphical or numerical methods are not acceptable.) (5)

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Question 8 continued

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Question 8 continued

Lined area for writing the answer to Question 8.



(Total 9 marks)



Diagram not
drawn to scale

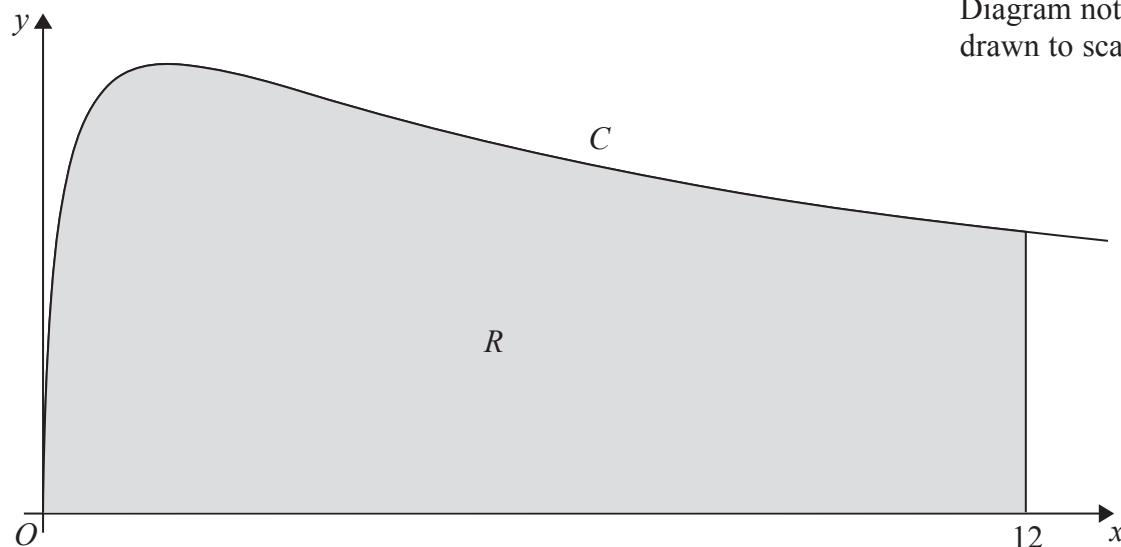


Figure 3

- (a) By using the substitution $u = 2x + 3$, show that

$$\int_0^{12} \frac{x}{(2x+3)^2} dx = \frac{1}{2} \ln 3 - \frac{2}{9} \quad (7)$$

The curve C has equation

$$y = \frac{9\sqrt{x}}{(2x+3)}, \quad x > 0$$

The finite region R , shown shaded in Figure 3, is bounded by the curve C , the x -axis and the line with equation $x = 12$. The region R is rotated through 2π radians about the x -axis to form a solid of revolution.

- (b) Use the result of part (a) to find the exact value of the volume of the solid generated. (2)



Question 9 continued

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Question 9 continued

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Q9

(Total 9 marks)



- $$N = \frac{300}{3 + 17e^{-0.2t}} \quad t \in \mathbb{R}, \quad t \geq 0$$

Using the model,

- (b) find the number of insects when $t = 10$,
- (2)**

- (d) Find, by differentiating, the rate, measured in insects per week, at which the number of insects is increasing when $t = 5$. Give your answer to the nearest whole number. **(3)**

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Question 10 continued

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Question 10 continued

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Q10

(Total 10 marks)



- Give the exact value of R , and give the value of α , in radians, to 4 significant figures. (3)

- $$70 \sin x - 24 \cos x = 37$$

$$y = \frac{7000}{31 + (35 \sin x - 12 \cos x)^2}, \quad x > 0$$

- (ii) the smallest value of x , $x > 0$, at which this minimum value occurs.

Question 11 continued

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Question 11 continued

Handwriting practice area with 25 horizontal lines.



Question 11 continued

Handwriting practice area with 30 horizontal lines.

Q11

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Question 12 continued

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Question 12 continued

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(Total 9 marks)



13.

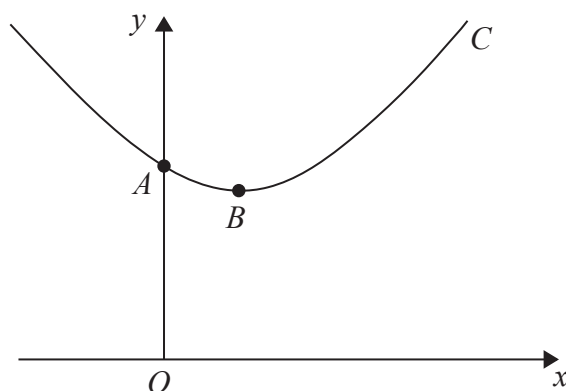


Figure 4

The curve C shown in Figure 4 has parametric equations

$$x = 1 + \sqrt{3} \tan \theta, \quad y = 5 \sec \theta, \quad -\frac{\pi}{2} < \theta < \frac{\pi}{2}$$

The curve C crosses the y -axis at A and has a minimum turning point at B , as shown in Figure 4.

(a) Find the exact coordinates of A . (3)

(b) Show that $\frac{dy}{dx} = \lambda \sin \theta$, giving the exact value of the constant λ . (4)

(c) Find the coordinates of B . (2)

(d) Show that the cartesian equation for the curve C can be written in the form

$$y = k\sqrt{(x^2 - 2x + 4)}$$

where k is a simplified surd to be found. (3)

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Question 13 continued

Q13

(Total 12 marks)



P 4 8 3 2 5 A 0 4 5 4 8

Given that

(c) find the area of the parallelogram $ABCD$. (2)

(d) Use your answer to part (c) to find the area of the trapezium $ABCE$. (2)

Question 14 continued

Handwriting practice area with 25 horizontal lines.

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Question 14 continued

Lined area for writing the answer to Question 14.

(Total 11 marks)

TOTAL FOR PAPER: 125 MARKS

END

