

Write your name here

Surname

Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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# Further Pure Mathematics F3

**Advanced/Advanced Subsidiary**

Monday 22 June 2015 – Morning

**Time: 1 hour 30 minutes**

Paper Reference

**WFM03/01**

**You must have:**

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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**PEARSON**

1. Find the exact values of  $x$  for which

$$\cosh 2x - 7 \sinh x = 5$$

giving your answers as natural logarithms.

(7)



Q1

**(Total 7 marks)**









### Question 2 continued

**(Total 5 marks)**

Q2



3.

$$\mathbf{M} = \begin{pmatrix} 0 & 1 & 9 \\ 1 & 4 & k \\ 1 & 0 & -3 \end{pmatrix}, \text{ where } k \text{ is a constant.}$$

Given that  $\begin{pmatrix} 7 \\ 19 \\ 1 \end{pmatrix}$  is an eigenvector of the matrix  $\mathbf{M}$ ,

- (a) find the eigenvalue of  $\mathbf{M}$  corresponding to  $\begin{pmatrix} 7 \\ 19 \\ 1 \end{pmatrix}$ , (2)
- (b) show that  $k = -7$  (2)
- (c) find the other two eigenvalues of the matrix  $\mathbf{M}$ . (4)

The image of the vector  $\begin{pmatrix} p \\ q \\ r \end{pmatrix}$  under the transformation represented by  $\mathbf{M}$  is  $\begin{pmatrix} -6 \\ 21 \\ 5 \end{pmatrix}$ .

- (d) Find the values of the constants  $p$ ,  $q$  and  $r$ . (4)









**(Total 12 marks)**

**Q3**



4.

$$I_n = \int \cosh^n x \, dx, \quad n \geq 0$$

(a) Show that, for  $n \geq 2$

$$nI_n = \sinh x \cosh^{n-1} x + (n-1)I_{n-2} \quad (6)$$

(b) Hence find the exact value of

$$\int_0^{\ln 2} \cosh^5 x \, dx \quad (4)$$







**(Total 10 marks)**

## Q4

Given that  $L$  is a tangent to  $E$ ,

(a) show that

$$c^2 - 25m^2 = 9 \quad (4)$$

(b) find the equations of the tangents to  $E$  which pass through the point  $(3, 4)$ . (5)

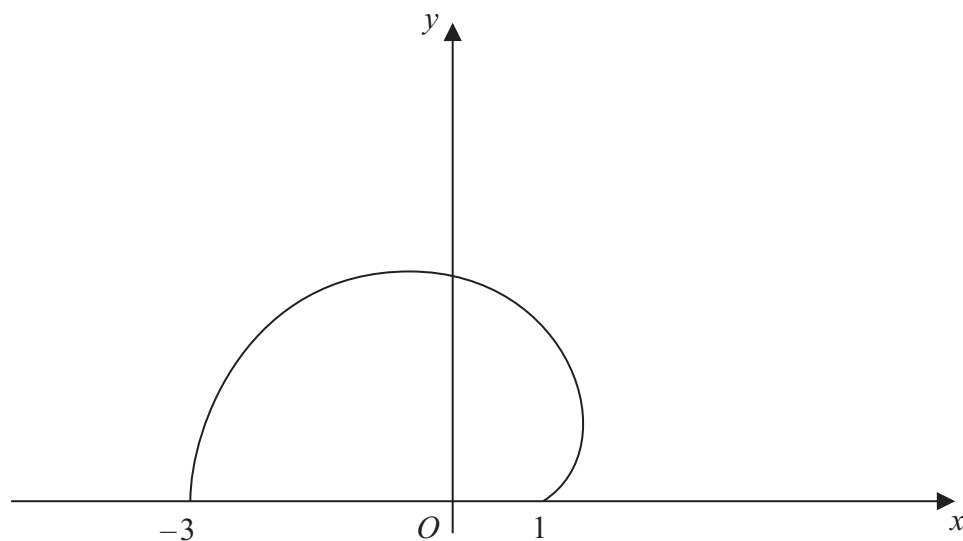












### Figure 1

Figure 1 shows the curve  $C$  with parametric equations

$$x = 2 \cos \theta - \cos 2\theta, y = 2 \sin \theta - \sin 2\theta, \quad 0 \leq \theta \leq \pi$$

(a) Show that

$$\left(\frac{dx}{d\theta}\right)^2 + \left(\frac{dy}{d\theta}\right)^2 = 8(1 - \cos\theta) \quad (5)$$

The curve  $C$  is rotated through  $2\pi$  radians about the  $x$ -axis.

(b) Find the area of the surface generated, giving your answer in the form  $k\pi$ , where  $k$  is a rational number.

(5)







**(Total 10 marks)**

**Q6**











**Q7**

where  $k$  is a constant to be determined.

(6)

$$\int_0^1 \frac{64x^2}{\sqrt{16x^2 + 9}} \, dx = p + q \ln 3$$

where  $p$  and  $q$  are rational numbers to be found.

(5)







**Question 8 continued**

**(Total 11 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**

