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Surname

Other names

Pearson Edexcel
International
Advanced Level

Centre Number

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Candidate Number

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Core Mathematics C34

Advanced

Monday 16 June 2014 – Morning

Time: 2 hours 30 minutes

Paper Reference

WMA02/01

You must have:

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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P 4 4 9 6 9 A 0 1 4 8

PEARSON

1.

$$f(x) = 2x^3 + x - 10$$

- (a) Show that the equation $f(x) = 0$ has a root α in the interval $[1.5, 2]$

(2)

The only real root of $f(x) = 0$ is α

The iterative formula

$$x_{n+1} = \left(5 - \frac{1}{2}x_n\right)^{\frac{1}{3}}, \quad x_0 = 1.5$$

can be used to find an approximate value for α .

- (b) Calculate x_1 , x_2 and x_3 , giving your answers to 4 decimal places.

(3)

- (c) By choosing a suitable interval, show that $\alpha = 1.6126$ correct to 4 decimal places.

(2)



(Total 7 marks)



(Total 6 marks)

Q2



4. Find

(a) $\int (2x + 3)^{12} dx$

(2)

(b) $\int \frac{5x}{4x^2 + 1} \, dx$

(2)

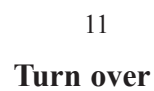


Q4

(5)

[illegible]

(Total 5 marks)





[illegible]

[illegible]

[illegible]

(Total 10 marks)

Q6



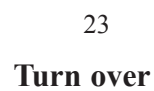
[illegible]

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This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

This image shows a full page of blank, lined paper. It features approximately 28 horizontal gray lines spaced evenly apart, typical of notebook paper. The lines extend across the entire width of the page, leaving small margins at the top and bottom. There are no vertical lines, text, or other markings present.

(Total 5 marks)



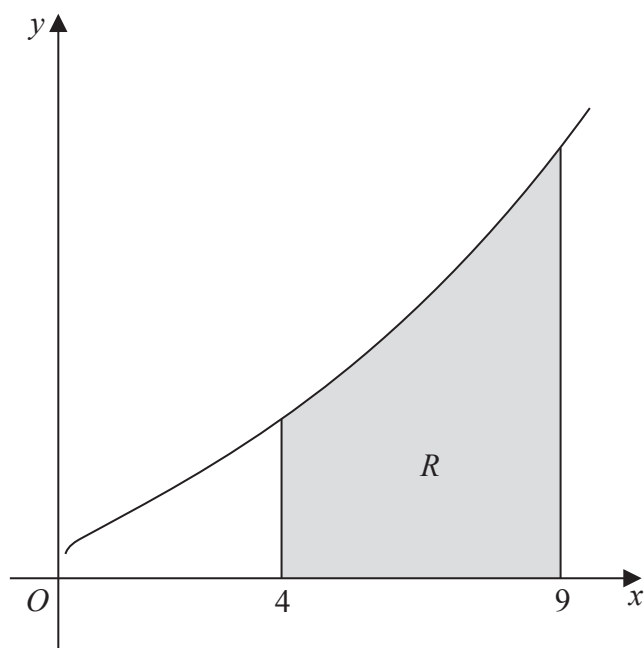


Figure 1 shows a sketch of part of the curve with equation $y = e^{\sqrt{x}}$, $x > 0$

(a) Use the trapezium rule, with 5 strips of equal width, to obtain an estimate for the area of R , giving your answer to 2 decimal places.

(4)

(b) Use the substitution $u = \sqrt{x}$ to find, by integrating, the exact value for the area of R . (7)

(7)



This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 9 continued

[illegible]

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(Total 11 marks)

Q9

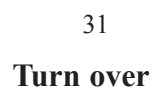




This image shows a full page of blank, lined paper. It features approximately 20 evenly spaced horizontal grey lines across its entire width, providing a guide for handwriting or typing. The paper itself is a clean, off-white color.

[illegible]

(Total 12 marks)



11.

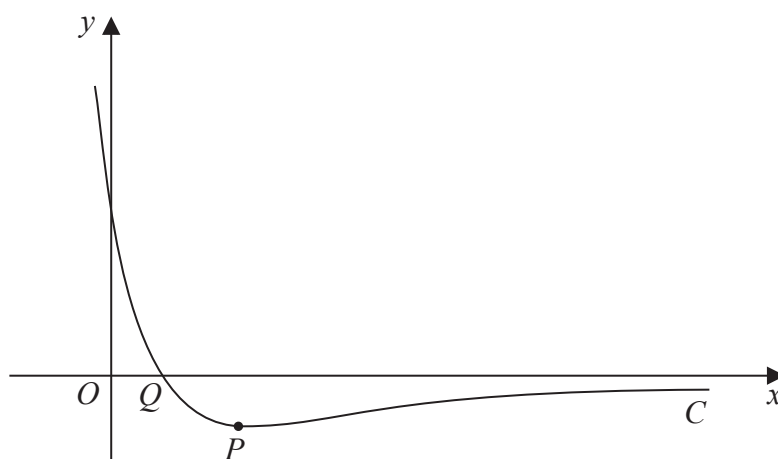


Figure 2

Figure 2 shows a sketch of part of the curve C with equation

$$y = e^{a-3x} - 3e^{-x}, \quad x \in \mathbb{R}$$

where a is a constant and $a > \ln 4$

The curve C has a turning point P and crosses the x -axis at the point Q as shown in Figure 2.

(a) Find, in terms of a , the coordinates of the point P . (6)

(b) Find, in terms of a , the x coordinate of the point Q . (3)

(c) Sketch the curve with equation

$$y = |e^{a-3x} - 3e^{-x}|, \quad x \in \mathbb{R}, \quad a > \ln 4$$

Show on your sketch the exact coordinates, in terms of a , of the points at which the curve meets or cuts the coordinate axes.

(3)



[illegible]

[illegible]

Question 11 continued

Q11

(Total 12 marks)



12.

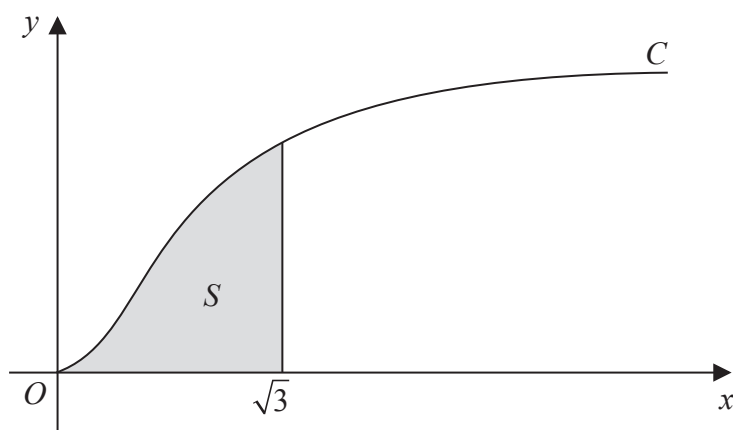


Figure 3

Figure 3 shows a sketch of part of the curve C with parametric equations

$$x = \tan t, \quad y = 2\sin^2 t, \quad 0 \leq t < \frac{\pi}{2}$$

The finite region S , shown shaded in Figure 3, is bounded by the curve C , the line $x = \sqrt{3}$ and the x -axis. This shaded region is rotated through 2π radians about the x -axis to form a solid of revolution.

- (a) Show that the volume of the solid of revolution formed is given by

$$4\pi \int_0^{\frac{\pi}{3}} (\tan^2 t - \sin^2 t) dt \quad (6)$$

- (b) Hence use integration to find the exact value for this volume.

(6)



[illegible]

[illegible]

(Total 12 marks)



13. (a) Express $2 \sin \theta + \cos \theta$ in the form $R \sin (\theta + \alpha)$, where R and α are constants, $R > 0$ and $0 < \alpha < 90^\circ$. Give your value of α to 2 decimal places. (3)

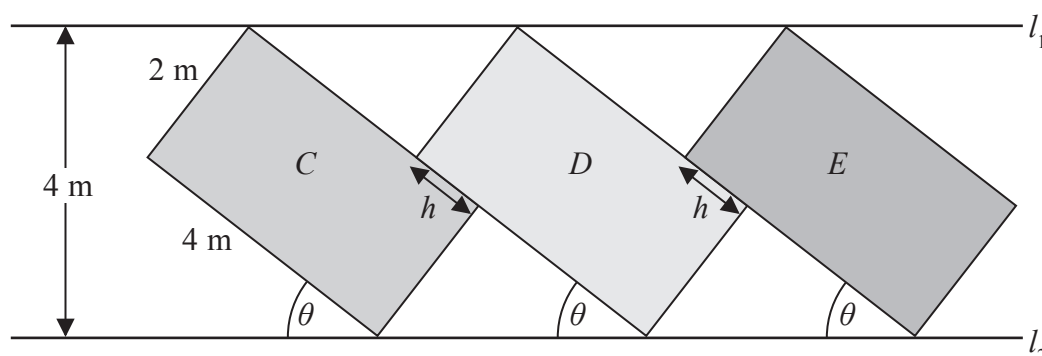


Figure 4

Figure 4 shows the design for a logo that is to be displayed on the side of a large building. The logo consists of three rectangles, C , D and E , each of which is in contact with two horizontal parallel lines l_1 and l_2 . Rectangle D touches rectangles C and E as shown in Figure 4.

Rectangles C , D and E each have length 4 m and width 2 m. The acute angle θ between the line l_2 and the longer edge of each rectangle is shown in Figure 4.

Given that l_1 and l_2 are 4 m apart,

- (b) show that

$$2 \sin \theta + \cos \theta = 2 \quad (2)$$

Given also that $0 < \theta < 45^\circ$,

- (c) solve the equation

$$2 \sin \theta + \cos \theta = 2$$

giving the value of θ to 1 decimal place. (3)

Rectangles C and D and rectangles D and E touch for a distance h m as shown in Figure 4.

Using your answer to part (c), or otherwise,

- (d) find the value of h , giving your answer to 2 significant figures. (3)



[illegible]

[illegible]

(Total 11 marks)



[illegible]

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Question 14 continued

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(Total 14 marks)

Q14

TOTAL FOR PAPER: 125 MARKS

END

