Please check the examination details belo	ow before ente	ring your candidate information
Candidate surname		Other names
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Centre Number Candidate Nu	ımber	
Pearson Edexcel Interi	nation	al Advanced Level
Tuesday 30 May 202	23	
Afternoon (Time: 1 hour 30 minutes)	Paper reference	WFM01/01
Afternoon (Time: 1 hour 30 minutes) Mathematics	Paper reference	WFM01/01
Mathematics International Advanced Su	reference	□ •
Mathematics	reference	○ •
Mathematics International Advanced Su	reference	□ •
Mathematics International Advanced Su	reference	◊ •
Mathematics International Advanced Su	reference	◊ •

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ▶





1. Use the standard results for $\sum_{r=1}^{n} r^2$ and $\sum_{r=1}^{n} r^3$ to show that, for all positive integers n

$$\sum_{r=1}^{n} r^{2} (r+2) = \frac{1}{12} n(n+1) (an^{2} + bn + c)$$

where a, b and c are integers to be determined.

(4)

Question 1 continued
(Total for Quarties 1 is A morks)
(Total for Question 1 is 4 marks)



2.	In this question you must show all stages of your working.
	Solutions relying on calculator technology are not acceptable.

Given that x = 2 + 3i is a root of the equation

$$2x^4 - 8x^3 + 29x^2 - 12x + 39 = 0$$

(a) write down another complex root of this equation.

(1)

(b) Use algebra to determine the other 2 roots of the equation.

(4)

(c) Show all 4 roots on a single Argand diagram.

(2)

Question 2 continued



Question 2 continued

Question 2 continued	
	(Total for Question 2 is 7 marks)



3. The rectangular hyperbola H has Cartesian equation xy = 9

The point *P* with coordinates $\left(3t, \frac{3}{t}\right)$, where $t \neq 0$, lies on *H*

(a) Use calculus to determine an equation for the normal to H at the point PGive your answer in the form $ty - t^3x = f(t)$

(4)

Given that t = 2

(b) determine the coordinates of the point where the normal meets \boldsymbol{H} again.

Give your answer in simplest form.

(3)

Question 3 continued
(Total for Question 3 is 7 marks)
(10tai ioi Question 5 is / marks)



4. (i) $\mathbf{A} = \begin{pmatrix} -3 & 8 \\ -3 & k \end{pmatrix}$ where k is a constant

The transformation represented by A transforms triangle T to triangle T'

The area of triangle T' is three times the area of triangle T

Determine the possible values of k

(4)

(ii)
$$\mathbf{B} = \begin{pmatrix} a & -4 \\ 2 & 3 \end{pmatrix} \text{ and } \mathbf{BC} = \begin{pmatrix} 2 & 5 & 1 \\ 1 & 4 & 2 \end{pmatrix} \text{ where } a \text{ is a constant}$$

Determine, in terms of a, the matrix C

(4)



Question 4 continued



Question 4 continued

(Total for Question 4 is 8 marks)



$$f(x) = x^2 - 6x + 3$$

The equation f(x) = 0 has roots α and β

Without solving the equation,

(a) determine the value of

$$(\alpha^2+1)(\beta^2+1)$$

(4)

(b) find a quadratic equation which has roots

$$\frac{\alpha}{(\alpha^2+1)}$$
 and $\frac{\beta}{(\beta^2+1)}$

giving your answer in the form $px^2 + qx + r = 0$ where p, q and r are integers to be determined.

(6)



Question 5 continued



Question 5 continued

Question 5 continued	
	T-4-1 f O4' 5': 10
	Total for Question 5 is 10 marks)



6. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

$$z_1 = 3 + 2i$$
 $z_2 = 2 + 3i$ $z_3 = a + bi$ $a,b \in \mathbb{R}$

(a) Determine the exact value of
$$|z_1 + z_2|$$

(2)

Given that
$$w = \frac{z_2 z_3}{z_1}$$

(b) determine w in terms of a and b, giving your answer in the form x + iy, where $x, y \in \mathbb{R}$

(4)

Given also that
$$w = \frac{4}{13} + \frac{58}{13}i$$

(c) determine the value of a and the value of b

(2)

(d) determine arg w, giving your answer in radians to 4 significant figures.

(2)

Question 6 continued



Question 6 continued

Question 6 continued	
(Total for Question 6	is 10 marks)
(Total for Question o	15 IU IIIAI KSJ



- 7. $f(x) = x^{\frac{3}{2}} + x 3$
 - (a) Show that the equation f(x) = 0 has a root, α , in the interval [1, 2]

(2)

(b) Starting with the interval [1, 2], use interval bisection twice to show that α lies in the interval [1.25, 1.5]

(3)

- (c) (i) Determine f'(x)
 - (ii) Using 1.375 as a first approximation for α , apply the Newton-Raphson process once to f(x) to determine a second approximation for α , giving your answer to 3 decimal places.

(3)

(d) Use linear interpolation once on the interval [1.25, 1.5] to obtain a different approximation for α , giving your answer to 3 decimal places.

(3)

Question 7 continued



Question 7 continued

Question 7 continued	
	(Total for Question 7 is 11 marks)



- **8.** The point $P(2p^2, 4p)$ lies on the parabola with equation $y^2 = 8x$
 - (a) Show that the point $Q\left(\frac{2}{p^2}, \frac{-4}{p}\right)$, where $p \neq 0$, lies on the parabola.

(1)

(b) Show that the chord PQ passes through the focus of the parabola.

(4)

The tangent to the parabola at P and the tangent to the parabola at Q meet at the point R

(c) Determine, in simplest form, the coordinates of R

(8)

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Question 8 continued			

Question 8 continued

Question 8 continued	
	(Total for Question 8 is 13 marks)



9.	Prove, by induction, that for $n \in \mathbb{Z}$, $n \ge 2$					
	$4^n + 6n - 10$					
	is divisible by 18	(5)				

Question 9 continued			

Question 9 continued	
(Total for Question 9 is 5 marks)	
TOTAL FOR PAPER IS 75 MARKS	_

