

Write your name here

Surname

Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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# Further Pure Mathematics F1

**Advanced/Advanced Subsidiary**

Friday 20 May 2016 – Morning

**Time: 1 hour 30 minutes**

Paper Reference

**WFM01/01**

**You must have:**

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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**PEARSON**

1. Use the standard results for  $\sum_{r=1}^n r$  and for  $\sum_{r=1}^n r^3$  to show that, for all positive integers  $n$ ,

$$\sum_{r=1}^n r(r^2 - 3) = \frac{n}{4}(n+a)(n+b)(n+c)$$

where  $a$ ,  $b$  and  $c$  are integers to be found.

(4)

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Question 1 continued

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Q1

(Total 4 marks)



- Points  $A$  and  $B$  lie on the parabola  $P$ . The line  $AB$  is parallel to the directrix of  $P$  and cuts the  $x$ -axis at the midpoint of  $OS$ , where  $O$  is the origin.

- (b) Find the exact area of triangle  $ABS$ . (4)

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Question 2 continued

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Q2

(Total 5 marks)



$$f(x) = x^2 + \frac{3}{x} - 1, \quad x < 0$$

(a) Taking  $-1.5$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x)$  to find a second approximation to  $\alpha$ , giving your answer to 2 decimal places.

(5)

(2)

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Question 3 continued

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Q3

(Total 7 marks)



$$\mathbf{A} = \begin{pmatrix} k & 3 \\ -1 & k+2 \end{pmatrix}, \text{ where } k \text{ is a constant}$$

- (a) show that  $\det(\mathbf{A}) > 0$  for all real values of  $k$ , (3)
- (b) find  $\mathbf{A}^{-1}$  in terms of  $k$ . (2)





Question 4 continued

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(Total 5 marks)

Q4



5.

$$2z + z^* = \frac{3 + 4i}{7 + i}$$

Find  $z$ , giving your answer in the form  $a + bi$ , where  $a$  and  $b$  are real constants. You must show all your working.

(5)

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Question 5 continued

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Q5

(Total 5 marks)



- (a) Verify that, for  $t \neq 0$ , the point  $P\left(5t, \frac{5}{t}\right)$  is a general point on  $H$ . (1)

(b) Show that the normal to  $H$  at the point  $A$  has equation

$$8y - 2x - 75 = 0 \quad (5)$$

This normal at  $A$  meets  $H$  again at the point  $B$ .

- (c) Find the coordinates of  $B$ . (4)

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Question 6 continued

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Question 6 continued

Lined area for writing the answer to Question 6.



Question 6 continued

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Handwriting practice area with 30 horizontal lines.

Q6

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(Total 10 marks)



$$\mathbf{P} = \begin{pmatrix} \frac{5}{13} & -\frac{12}{13} \\ \frac{12}{13} & \frac{5}{13} \end{pmatrix}$$

- (d) Show that there is a value of  $k$  for which the transformation  $T$  maps each point on the straight line  $y = kx$  onto itself, and state the value of  $k$ . (4)

[illegible]



Question 7 continued

Handwriting practice area with 25 horizontal lines.

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Question 7 continued

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Handwriting practice area with horizontal lines.

Q7

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(Total 10 marks)



$$f(z) = z^4 + 6z^3 + 76z^2 + az + b$$

Given that  $-3 + 8i$  is a complex root of the equation  $f(z) = 0$

- (a) write down another complex root of this equation. (1)
- (b) Hence, or otherwise, find the other roots of the equation  $f(z) = 0$  (6)
- (c) Show on a single Argand diagram all four roots of the equation  $f(z) = 0$  (2)

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Question 8 continued

Handwriting practice area with 30 horizontal lines.

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Question 8 continued

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Q8

(Total 9 marks)



9. The quadratic equation

$$2x^2 + 4x - 3 = 0$$

has roots  $\alpha$  and  $\beta$ .

Without solving the quadratic equation,

(a) find the exact value of

(i)  $\alpha^2 + \beta^2$

(ii)  $\alpha^3 + \beta^3$

(5)

(b) Find a quadratic equation which has roots  $(\alpha^2 + \beta)$  and  $(\beta^2 + \alpha)$ , giving your answer in the form  $ax^2 + bx + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers.

(4)

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Question 9 continued

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Question 9 continued

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Q9

(Total 9 marks)



$$\begin{aligned} u_1 &= 5 \\ u_{n+1} &= 3u_n + 2, \quad n \geq 1 \end{aligned}$$
$$u_n = 2 \times (3)^n - 1 \quad (5)$$
$$\sum_{r=1}^n \frac{4r}{3^r} = 3 - \frac{(3+2n)}{3^n} \quad (6)$$
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Question 10 continued

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## This image shows a full page of blank, lined paper. It features approximately 28 horizontal blue or grey lines spaced evenly apart, typical of notebook paper. The lines extend across the entire width of the page, leaving small margins at the top and bottom. There are no vertical lines, text, or other markings on the page.

Question 10 continued

Handwriting practice area with 25 horizontal lines.

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**TOTAL FOR PAPER: 75 MARKS**

32

