

Write your name here

Surname

Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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# Further Pure Mathematics F1

**Advanced/Advanced Subsidiary**

Thursday 14 May 2015 – Morning

**Time: 1 hour 30 minutes**

Paper Reference

**WFM01/01**

**You must have:**

Mathematical Formulae and Statistical Tables (Blue)

Total Marks

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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**PEARSON**



**(Total 5 marks)**

**Q1**

3

**Turn over**



2. Use the standard results for  $\sum_{r=1}^n r$  and for  $\sum_{r=1}^n r^2$  to show that

$$\sum_{r=1}^n (3r-2)^2 = \frac{n}{2}(an^2 + bn + c)$$

where  $a$ ,  $b$  and  $c$  are integers to be found.

(5)



### Question 2 continued

**(Total 5 marks)**

Q2

[illegible]



Q3

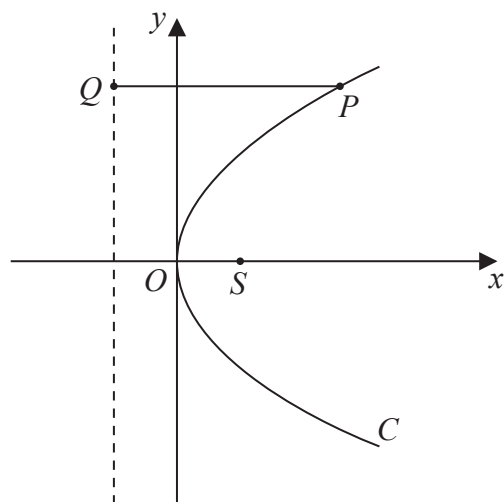


Figure 1 shows a sketch of the parabola  $C$  with equation  $y^2 = 4ax$ , where  $a$  is a positive constant. The point  $S$  is the focus of  $C$  and the point  $Q$  lies on the directrix of  $C$ . The point  $P$  lies on  $C$  where  $y > 0$  and the line segment  $QP$  is parallel to the  $x$ -axis.

(a) write down the length of  $PQ$ .

(1)

find

(b) the value of  $a$ ,

(2)

(c) the area of triangle  $PSQ$ .

(3)

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Q4









This image shows a full page of blank, lined paper. It features approximately 28 horizontal gray lines spaced evenly across the page, typical of standard notebook paper. The lines are thin and light gray, set against a plain white background. There is no handwriting or other markings on the page.

**Q6**

7.

$z = -3k - 2ki$ , where  $k$  is a real, positive constant.

- (a) Find the modulus and the argument of  $z$ , giving the argument in radians to 2 decimal places and giving the modulus as an exact answer in terms of  $k$ .

(3)

- (b) Express in the form  $a + ib$ , where  $a$  and  $b$  are real and are given in terms of  $k$  where necessary,

(i)  $\frac{4}{z+3k}$

(ii)  $z^2$

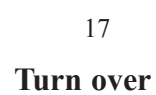
(5)

- (c) Given that  $k = 1$ , plot the points  $A, B, C$  and  $D$  representing  $z, z^*, \frac{4}{z + 3k}$  and  $z^2$  respectively on a single Argand diagram.

(3)

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[illegible]

**(Total 11 marks)**

**Q7**



**8.**

$\mathbf{P} = \begin{pmatrix} 3a & -4a \\ 4a & 3a \end{pmatrix}$ , where  $a$  is a constant and  $a > 0$

- (a) Find the matrix  $\mathbf{P}^{-1}$  in terms of  $a$ .

(3)

The matrix  $\mathbf{P}$  represents the transformation  $U$  which transforms a triangle  $T_1$  onto the triangle  $T_2$ .

The triangle  $T_7$  has vertices at the points  $(-3a, -4a)$ ,  $(6a, 8a)$ , and  $(-20a, 15a)$ .

- (b) Find the coordinates of the vertices of  $T_1$ .

(3)

- (c) Hence, or otherwise, find the area of triangle  $T$ , in terms of  $a$ .

(3)

The transformation  $V$ , represented by the  $2 \times 2$  matrix  $\mathbf{Q}$ , is a rotation through an angle  $\alpha$  **clockwise** about the origin, where  $\tan \alpha = \frac{4}{3}$  and  $0 < \alpha < \frac{\pi}{2}$

- (d) Write down the matrix  $\mathbf{Q}$ , giving each element as an exact value.

(2)

The transformation  $U$  followed by the transformation  $V$  is the transformation  $W$ . The matrix  $\mathbf{R}$  represents the transformation  $W$ .

- (e) Find the matrix  $\mathbf{R}$ .

(2)

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[illegible]

[illegible]

**(Total 13 marks)**

**Q8**



9. (i) Prove by induction that, for  $n \in \mathbb{Z}^+$ ,

$$\sum_{r=1}^n r^2(2r-1) = \frac{1}{6}n(n+1)(3n^2+n-1) \quad (6)$$

(ii) Prove by induction that, for  $n \in \mathbb{Z}^+$ ,

$$\begin{pmatrix} 7 & -12 \\ 3 & -5 \end{pmatrix}^n = \begin{pmatrix} 6n+1 & -12n \\ 3n & 1-6n \end{pmatrix} \quad (6)$$







**Question 9 continued**

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