

cases	doc_1		doc_2		decision	id
	authors	<ul style="list-style-type: none">Manivel, Laurent	authors	<ul style="list-style-type: none">Laurent Manivel	DUPLICATES	904
	title	Configurations of lines and models of Lie algebras	title	Configurations of lines and models of Lie algebras		
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	urls	<ul style="list-style-type: none">http://arxiv.org/abs/math/0507118	urls	<ul style="list-style-type: none">https://archive.org/download/arxiv-math0507118/math0507118.pdf		
	id	id-7919433715303589922	id	id1796320959106989510		
	abstract	The automorphism groups of the 27 lines on the smooth cubic surface or the 28 bitangents to the general quartic plane curve are well-known to be closely related to the Weyl groups of E_6 and E_7 . We show how classical subconfigurations of lines, such as double-sixes, triple systems or Steiner sets, are easily constructed from certain models of the exceptional Lie algebras. For \mathfrak{e}_7 and \mathfrak{e}_8 we are lead to beautiful models graded over the octonions, which display these algebras as plane projective geometries of subalgebras. We also interpret the group of the bitangents as a group of transformations of the triangles in the Fano plane, and show how this allows to realize the isomorphism $\mathrm{PSL}(3, \mathbb{F}_2) \simeq \mathrm{PSL}(2, \mathbb{F}_7)$ in terms of harmonic cubes. Comment: 31 page	abstract	The automorphism groups of the 27 lines on the smooth cubic surface or the 28 bitangents to the general quartic plane curve are well-known to be closely related to the Weyl groups of E_6 and E_7 . We show how classical subconfigurations of lines, such as double-sixes, triple systems or Steiner sets, are easily constructed from certain models of the exceptional Lie algebras. For \mathfrak{e}_7 and \mathfrak{e}_8 we are lead to beautiful models graded over the octonions, which display these algebras as plane projective geometries of subalgebras. We also interpret the group of the bitangents as a group of transformations of the triangles in the Fano plane, and show how this allows to realize the isomorphism $\mathrm{PSL}(3, \mathbb{F}_2) \simeq \mathrm{PSL}(2, \mathbb{F}_7)$ in terms of harmonic cubes.		
	versions		versions			