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Cases	id	id-2304232802484844568	id	id7616213243065729814		
cases	abstract	For any compact Lie group G and closed, smooth Riemannian manifold (X,g) of dimension d≥ 2, we extend a result due to Uhlenbeck (1985) that gives existence of a flat connection on a principal G-bundle over X supporting a connection with L^p-small curvature, when p>d/2, to the case of a connection with L^d/2-small curvature. We prove an optimal Lojasiewicz-Simon gradient inequality for abstract Morse-Bott functions on Banach manifolds, generalizing an earlier result due to the author and Maridakis in arXiv:1510.03817. We apply this result to prove the optimal Lojasiewicz-Simon gradient inequality for the self-dual Yang-Mills energy function near regular anti-self-dual connections over closed Riemannian four-manifolds and for the full Yang-Mills energy function over closed Riemannian manifolds of dimension d ≥ 2, when known to be Morse-Bott at a given Yang-Mills connection. We also prove the optimal Lojasiewicz-Simon gradient inequality by direct analysis near a given flat connection that is a regular point of the curvature map. We also prove the Morse-Bott property for irreducible Yang-Mills U(n) connections over Riemann surfaces and hence a new proof of the optimal Lojasiewicz-Simon gradient inequality for such critical points.	abstract	For any compact Lie group G, we prove that the Yang–Mills energy function obeys an optimal gradient inequality of Åojasiewicz–Simon type (exponent 1/2) near the critical set of flat connections on a principal Gbundle over a closed Riemannian manifold of dimension d≥ 2 and so its gradient flow converges at an exponential rate to that critical set. We establish this optimal Åojasiewicz–Simon gradient inequality by three different methods. Our first proof gives the most general result by direct analysis and relies on our extension of a theorem due to Uhlenbeck [86] that gives existence of a flat connection on a principal G-bundle supporting a connection with L^d/2 -small curvature, existence of a Coulomb gauge transformation, and W^1,p Sobolev distance estimates for p > 1. Our second proof proceeds by first establishing an optimal Åojasiewicz–Simon gradient inequality for abstract Morse–Bott functions on Banach manifolds, generalizing an earlier result due to the author and Maridakis [31, Theorem 4]. Our third proof establishes the optimal Åojasiewicz–Simon gradient inequality by direct analysis near a given flat connection that is a regular point of the curvature map. We prove similar results for the self-dual Yang–Mills energy function near regular anti-self-dual connections over closed Riemannian four-manifolds and for the full Yang–Mills energy function over closed Riemannian manifolds of dimension d≥ 2, when known to be Morse–Bott at a given Yang–Mills connection		3 732
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