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		title	Legendre Memory Units: Continuous-Time Representation in Recurrent Neural Networks	
		publication_date	2019-12-01 00:00:00	
	A T7 11	source	SupportedSources.PAPERS_WITH_CODE	
	Aaron Voelker     Ivana Kajic	journal		
auth	• Chris Eliasmith	volume		
	Cin is Eliasiniui	doi		
titl	Legendre Memory Units: Continuous-Time Representation in Recurrent Neural Networks		http://papers.nips.cc/paper/9689-legendre-memo units-continuous-time-representation-in-recurren	
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ases	https://web.archive.org/web/20220308032320/https://proceedings.neurips.cc/paper/2019/file/952285b9b7e7a1be5aa7849f32ffff05-Paper.pdf	that dynamically maintains information across lon time using relatively few resources. The Legendre (LMU) is mathematically derived to orthogonalize time history doing so by solving \$d\$ coupled or differential equations~(ODEs), whose phase space onto sliding windows of time via the Legendre pol degree \$d - 1\$. Backpropagation across LMUs out equivalently-sized LSTMs on a chaotic time-series task, improves memory capacity by two orders of significantly reduces training and inference times. efficiently handle temporal dependencies spanning \$100\text{,}000\$ time-steps, converge rapidly, and internal state-variables to learn complex functions windows of time exceeding state-of-the-art performation of the network's disposition to learn scale-invariant for independently of step size. Backpropagation throus solver allows each layer to adapt its internal time-step the network to learn task-relevant time-scales. We that LMU memory cells can be implemented using recurrently-connected Poisson spiking neurons, \$\text{\text{h}} \text{\text{b}} \text{\text{the and memory, with error scaling as \$\text{\text{mand memory}} \text{\text{the error scaling as \$\text{\text{mand memory}}}	(LMU) is mathematically derived to orthogonalize its continuous-	ws of v Unit~ inuous- maps s up to s on de, and an v g long among ue to
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abstr	We propose a novel memory cell for recurrent neural networks that dynamically maintains information across long windows of time using relatively few resources. The Legendre Memory Unit (LMU) is mathematically derived to orthogonalize its continuous-time history -doing so by solving d coupled ordinary differential equations (ODEs), whose phase space linearly maps onto sliding windows of time via the Legendre polynomials up to degree d â° 1. Backpropagation across LMUs outperforms equivalently-sized LSTMs on a chaotic time-series prediction task, improves memory capacity by two orders of magnitude, and significantly reduces training and inference times. LMUs can efficiently handle temporal dependencies spanning 100,000 time-steps, converge rapidly, and use few internal state-variables to learn complex functions spanning long windows of time -exceeding state-of-the-art performance among RNNs on permuted sequential MNIST. These results are due to the network's disposition to learn scale-invariant features independently of step size. Backpropagation through the ODE solver allows each layer to adapt its internal time-step, enabling the network to learn task-relevant time-scales. We demonstrate that LMU memory cells can be implemented using m recurrently-connected Poisson spiking neurons, O(m) time and memory, with error scaling as O(d/ â°s m). We discuss implementations of LMUs on analog and digital neuromorphic hardware.		onto sliding windows of time via the Legendre polynomials up to degree \$d - 1\$. Backpropagation across LMUs outperforms equivalently-sized LSTMs on a chaotic time-series prediction task, improves memory capacity by two orders of magnitude, and significantly reduces training and inference times. LMUs can efficiently handle temporal dependencies spanning \$100\text{,}000\$ time-steps, converge rapidly, and use few internal state-variables to learn complex functions spanning long windows of time exceeding state-of-the-art performance among RNNs on permuted sequential MNIST. These results are due to	
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