

cases	doc_1		doc_2		decision	id
	authors	<ul style="list-style-type: none">Richard LÄ¶scherOlaf Steinbach			DUPLICATES	538
	title	Space-time finite element methods for distributed optimal control of the wave equation	authors	<ul style="list-style-type: none">Richard LÄ¶scherO. Steinbach		
	publication_date	2022-11-04 16:28:27+00:00	title	Space-time finite element methods for distributed optimal control of the wave equation		
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	journal	None	source	SupportedSources.SEMANTIC_SCHOLAR		
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	urls	<ul style="list-style-type: none">http://arxiv.org/pdf/2211.02562v1http://arxiv.org/abs/2211.02562v1http://arxiv.org/pdf/2211.02562v1	doi	10.48550/arXiv.2211.02562		
	id	id-6190312772397257232	urls	<ul style="list-style-type: none">https://www.semanticscholar.org/paper/8f2ae492665ca7604000e5311e22d2d667d30d47		
	abstract	We consider space-time tracking type distributed optimal control problems for the wave equation in the space-time domain $Q:=\Omega\times(0,T)\subset\{\mathbb{R}\}^{n+1}$, where the control is assumed to be in the energy space $[H_{\{0,0\}^{1,1}}(Q)]^*$, rather than in $L^2(Q)$ which is more common. While the latter ensures a unique state in the Sobolev space $H^{1,1}_{\{0,0\}}(Q)$, this does not define a solution isomorphism. Hence we use an appropriate state space XX such that the wave operator becomes an isomorphism from XX onto $[H_{\{0,0\}^{1,1}}(Q)]^*$. Using space-time finite element spaces of piecewise linear continuous basis functions on completely unstructured but shape regular simplicial meshes, we derive a priori estimates for the error $\ \widetilde{u}_{\varrho h}-\overline{u}_{L^2(Q)}\ $ between the computed space-time finite element solution $\widetilde{u}_{\varrho h}$ and the target function \overline{u} with respect to the regularization parameter ϱ , and the space-time finite element mesh-size h , depending on the regularity of the desired state \overline{u} . These estimates lead to the optimal choice $\varrho=h^2$ in order to define the regularization parameter ϱ for a given space-time finite element mesh size h , or to determine the required mesh size h when ϱ is a given constant representing the costs of the control. The theoretical results will be supported by numerical examples with targets of different regularities, including discontinuous targets. Furthermore, an adaptive space-time finite element scheme is proposed and numerically analyzed.	abstract	We consider space-time tracking type distributed optimal control problems for the wave equation in the space-time domain $Q:=\hat{\cdot},\check{\cdot}(0,T)\hat{\cdot},\check{\cdot}\mathbb{R}^{n+1}$, where the control is assumed to be in the energy space $[H^1_{\{0,0\}}(Q)]^*$, rather than in $L^2(Q)$ which is more common. While the latter ensures a unique state in the Sobolev space $H^{1,1}_{\{0,0\}}(Q)$, this does not deŕine a solution isomorphism. Hence we use an appropriate state space X such that the wave operator becomes an isomorphism from X onto $[H^1_{\{0,0\}}(Q)]^*$. Using space-time ŕnite element spaces of piecewise linear continuous basis functions on completely unstructured but shape regular simplicial meshes, we derive a priori estimates for the error (cid:107) (cid:101) u (cid:37) h $\hat{\cdot}$ u (cid:107) $L^2(Q)$ between the computed space-time ŕnite element solution (cid:101) u (cid:37) h and the target function u with respect to the regularization parameter (cid:37), and the space-time ŕnite element mesh-size h , depending on the regularity of the desired state u . These estimates lead to the optimal choice (cid:37) $=h^2$ in order to deŕine the regularization parameter (cid:37) for a given space-time ŕnite element mesh size h , or to determine the required mesh size h when (cid:37) is a given constant representing the costs of the control. The theoretical results will be supported by numerical examples with targets of diŕerent regularities, including discontinuous targets. Furthermore, an adaptive space-time ŕnite element scheme is proposed and numerically analyzed.		
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