

**Note:** Show all your operations in detail. The solutions that do not have enough details will be graded with zero points.

1. (P.396 Q.8) Consider the four  $3 \times 3$  linear systems having the same coefficient matrix:

$$\begin{array}{rcl} 2x_1 - 3x_2 + x_3 & = & 2 \\ x_1 + x_2 - x_3 & = & -1 \\ -x_1 + x_2 - 3x_3 & = & 0 \end{array} \qquad \begin{array}{rcl} 2x_1 - 3x_2 + x_3 & = & 6 \\ x_1 + x_2 - x_3 & = & 4 \\ -x_1 + x_2 - 3x_3 & = & 5 \end{array}$$

$$\begin{array}{rcl} 2x_1 - 3x_2 + x_3 & = & 0 \\ x_1 + x_2 - x_3 & = & 1 \\ -x_1 + x_2 - 3x_3 & = & -3 \end{array} \qquad \begin{array}{rcl} 2x_1 - 3x_2 + x_3 & = & -1 \\ x_1 + x_2 - x_3 & = & 0 \\ -x_1 + x_2 - 3x_3 & = & 0 \end{array}$$

- (a) Solve the linear systems by applying Gaussian elimination to the augmented matrix

$$\left[ \begin{array}{cccc|cccc} 2 & -3 & 1 & \vdots & 2 & 6 & 0 & -1 \\ 1 & 1 & -1 & \vdots & -1 & 4 & 1 & 0 \\ -1 & 1 & -3 & \vdots & 0 & 5 & -3 & 0 \end{array} \right].$$

- (b) Solve the linear systems by finding and multiplying by the inverse of

$$A = \begin{bmatrix} 2 & -3 & 1 \\ 1 & 1 & -1 \\ -1 & 1 & -3 \end{bmatrix}.$$

- (c) Which method requires more operations?