

PS04-03

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Consider grammar G :

$$S \rightarrow ABS|AB$$

$$A \rightarrow aA|a$$

$$B \rightarrow bA.$$

a. Are the following strings in $L(G)$?

- i. $abaab \notin L(G)$. This is because the only terminal in G is a .
- ii. $aaaaba \ S \rightarrow AB \rightarrow aAB \rightarrow aaAB \rightarrow aaaAB \rightarrow aaaaB \rightarrow aaaabA \rightarrow aaaaba$.
- iii. $aabbaa \notin L(G)$. This is because a b is always followed by an a (rule S). If there are two b s in a string in this language, there are always at least 2 a s in between.
- iv. $abaaba \ S \rightarrow ABS \rightarrow aBS \rightarrow abAS \rightarrow abaS \rightarrow abaAB \rightarrow abaaB \rightarrow abaabA \rightarrow abaaba$.

b. $G = \langle V, \Sigma, R, S \rangle$,

$$L(G) = \{w \in \Sigma^* : S \Rightarrow^* w\}$$

$$L(G) = \{a^{i_1}ba^{j_1} \cdot \dots \cdot a^{i_n}ba^{j_n} : i, j, n > 0\}$$