
FINDING NEURONS IN A HAYSTACK: CASE STUDIES WITH SPARSE PROBING

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ABSTRACT

Despite rapid adoption and deployment of large language models (LLMs), the internal computations of these models remain opaque and poorly understood. In this work, we seek to understand how high-level human-interpretable features are represented within the internal neuron activations of LLMs. We train k -sparse linear classifiers (probes) on these internal activations to predict the presence of features in the input; by varying the value of k we study the sparsity of learned representations and how this varies with model scale. With $k = 1$, we localize individual neurons which are highly relevant for a particular feature, and perform a number of case studies to illustrate general properties of LLMs. In particular, we show that early layers make use of sparse combinations of neurons to represent many features in superposition, that middle layers have seemingly dedicated neurons to represent higher-level contextual features, and that increasing scale causes representational sparsity to increase on average, but there are multiple types of scaling dynamics. In all, we probe for over 100 unique features comprising 10 different categories in 7 different models spanning 70 million to 6.9 billion parameters.

1 Introduction

Neural networks are often conceptualized as being flexible “feature extractors” that learn to iteratively develop and refine suitable representations from raw inputs [1, 2]. This begs the question: what features are being represented and how? Probing is a standard technique used to study if and where a neural network represents a specific feature by training a simple classifier (a probe) on the internal activations of a model to predict a property of the input [3] (e.g., classifying the tense of a verb based on the activations of a specific layer). Because models are parameterized as a series of dense matrix multiplications and elementwise nonlinearities, a natural intuition is that features are represented as linear directions in activation space [4], and are iteratively combined to synthesize increasingly abstract features using linear combinations of previously computed features [5]. To zoom in on these dynamics in modern transformer language models, we propose *sparse probing*, where we constrain the probing classifier to use at most k neurons in its prediction, and probe for over 100 features to precisely localize relevant neurons and elucidate broader principles of how to study and interpret the rich structure within LLMs.

In the simplest case, one might hope there exists a 1:1 correspondence between features of the input and neurons in a network—that for the correct feature definition, a 1-sparse probe would be sufficient. Although the literature contains many examples of such seemingly *monosemantic neurons* [6, 7, 5, 8, 9, 10], an obvious problem arises when a network has to represent more features than it has neurons. To accomplish this, a model must employ some form of compression to embed n features in $d < n$ dimensions. While this *superposition* of features enables more representational power, it also causes loss-increasing “interference” between non-orthogonal features [4]. Recent work in toy models demonstrate that this tension manifests in a spectrum of representations: dedicated dimensions or neurons for the most prevalent and important features with increasing levels of superposition—and hence decreasing levels of sparsity—for the long tail of rarer or less important features [4, 11].

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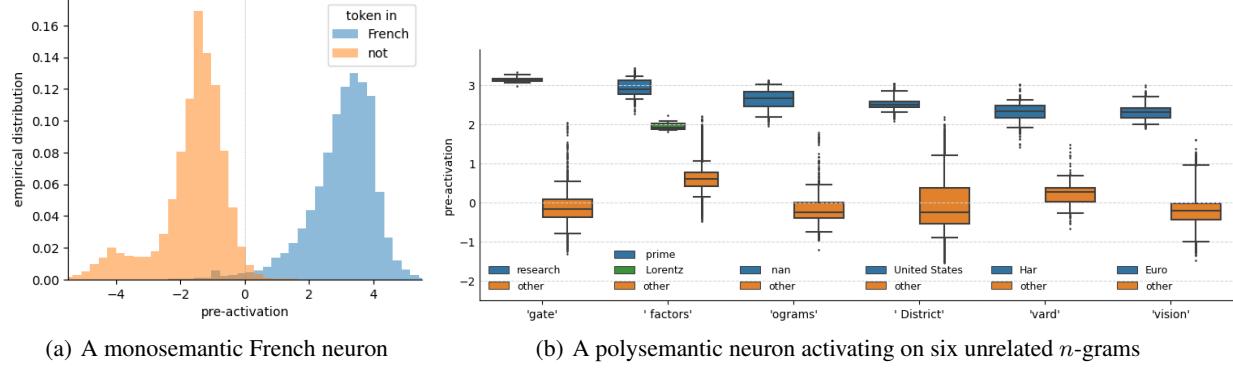


Figure 1: Neurons that respond to single features (left) can be understood independently, in contrast to polysemantic neurons (right) that activate for many unrelated features (in this case, the occurrence of specific multi-token spans).

As with any conceptual insight, these results raise more questions than they answer: To what extent do these observations transfer to full scale language models? What kinds of features do or do not appear in superposition? At what scale? How do we reliably find and verify such (feature, neuron) pairs? We leverage sparse probing to systematically study such questions, finding clean examples of both monosemantic neurons and superposition “in the wild.” Better understanding—and potentially resolving—superposition is on the critical path to ambitious full-model interpretability because a logical consequence of superposition is the presence of *polysemantic* neurons that activate for a large collection of seemingly unrelated stimuli (Figure 1) [10, 12]. Such tangled representations undermine our ability to decompose networks into independently meaningful and composable components, thwarting existing approaches to reverse-engineer networks [5].

In addition to being especially well suited to studying superposition, our sparse probing methodology addresses several shortcomings identified in the probing literature [3, 13, 14, 15]. By leveraging recent advances in optimal sparse prediction [16, 17], we are able to prove optimality of the k -sparse feature selection subproblem (for small k), addressing the conflation of ranking quality and classification quality raised in [13]. Second, by employing sparsity as an inductive bias, our probes maintain a strong simplicity prior and are more capable of precise localization of important neurons. This precision enables a more granular level of analysis illustrated throughout our case studies. Finally, the lack of capacity inhibits the probe from memorizing correlation patterns associated with the feature of interest [14], offering a more reliable signal of whether this feature is explicitly represented and used downstream [15].

In the first part of the paper, we outline several variants of sparse probing, discuss the various subtleties of applying sparse probing, and run a large number of probing experiments. In particular, we probe for over 100 unique features comprising 10 different categories in 7 different models spanning 2 orders of magnitude in parameter count (up to 6.9 billion). The majority of the paper then focuses on zooming-in [5] on specific examples of general phenomena in a series of more detailed case studies to demonstrate:

- There is a tremendous amount of interpretable structure within the neurons of LLMs, and sparse probing is an effective methodology to locate such neurons (even in superposition), but requires careful use and follow up analysis to draw rigorous conclusions.
- Many early layer neurons are in superposition, where features are represented as sparse linear combinations of polysemantic neurons, each of which activates for a large collection of unrelated n -grams and local patterns. Moreover, based on weight statistics and insights from toy models, we conclude that the first 25% of fully connected layers employ substantially more superposition than the rest.
- Higher-level contextual and linguistic features (e.g., `is_python_code`) are seemingly encoded by monosemantic neurons, predominantly in middle layers, though conclusive statements about monosemanticity remain methodologically out of reach.
- As models increase in size, representation sparsity increases on average, but different features obey different dynamics: some features with dedicated neurons emerge with scale, others split into finer grained features with scale, and many remain unchanged or appear somewhat randomly.

2 Related Work

Probing Originally introduced by [18], probing is a standard technique used to determine if models represent specific features or concepts [3]. For language models in particular, there exist many probing studies showing the rich linguistic representations learned by models [19, 20, 21], contributing to the broader field of “BERTology” [22]. Particularly relevant to our work are investigations on the role of individual neurons [7, 23, 24, 25] and the identification of sparsely represented features [26, 27]. While probing in general has a number of limitations [14, 28, 15, 29, 30], our work seeks to address, at least partially, the shortcomings most associated with probing individual neurons [13]. Methodologically, sparse probing is situated within the broader category of probing methods [31, 32, 33, 34], which itself is just one paradigm among other localization techniques [35, 36, 37, 38, 39, 40].

Mechanistic Interpretability Philosophically, our work is motivated by the growing field of mechanistic interpretability (MI) [5, 41, 42]. MI concerns itself with rigorously understanding the learned algorithms (circuits) utilized by neural networks [43, 44, 45, 46] in the hope of maintaining oversight and diagnosing failures of increasingly capable models [47]. Although research on reverse-engineering specific neurons in LLMs is limited, [48] proposed—and later refined [49]—the hypothesis that feed-forward layers function as key-value memories, responding to specific input features (keys) and updating the output vocabulary distribution accordingly [50].

Superposition Perhaps the most significant obstacle to interpreting neurons in LLMs, and consequently, the success of MI as a whole, is the phenomenon of superposition. As first observed by [51], superposition involves compressing multiple features into a smaller number of dimensions [4]. Recent research has investigated when superposition occurs [4, 11], how to design models to have less of it [52, 10], and how to extract features in spite of it [53]. Many of the underlying mathematical intuitions rely on prior work on compressed sensing [54]. Moreover, similar questions have been studied elsewhere in machine learning within the disentanglement literature [1, 55, 56].

Connections to Neuroscience In a promising demonstration of consilience, our previous discussion of superposition has striking analogues with coding theory from biological neuroscience—the study of how neurons in the brain map to sensory stimulus [57, 58, 59]. On one extreme, local coding theory posits the existence of “monosemantic” biological neurons which respond to a very specific stimulus (e.g., pictures of Jennifer Aniston [60]). Superposition is then analogous to sparse coding where a subset of neurons encode some feature about the input [58, 61]. Finally population coding theorizes the responses of a whole brain region are relevant, analogous to the computations of a full layer being required to compute or represent a feature [62, 63].

3 Sparse Probing

3.1 Preliminaries

Transformers We restrict our scope to transformer-based generative pre-trained (GPT) language models [64] that currently power the most capable AI systems [65]. Given an input sequence of tokens $x = [x_1, \dots, x_t] \in \mathcal{X}$ from the vocabulary, a model $\mathcal{M} : \mathcal{X} \rightarrow \mathcal{Y}$ outputs a probability distribution over the token vocabulary \mathcal{V} to predict the next token in the sequence. \mathcal{M} is parameterized by interleaving L multi-head attention (MHA) layers, and multi-layer perceptron (MLP) layers. The central object of the transformer is the residual stream, the sum of the output of all previous layers. Each MHA and MLP layer reads its input from the residual stream and writes its output by adding it to the stream. MHA layers are responsible for moving information between token positions, MLP layers apply pointwise nonlinearities to each token independently and therefore perform the majority of the feature extraction, and the residual stream acts as the communication channel between layers. In this study, we are primarily concerned with the MLP layers (accounting for $\approx \frac{2}{3}$ of total parameters). Ignoring the MHA layer, the value of the residual stream (also referred to as the hidden state) for token t at layer ℓ after applying the MLP is

$$h_t^{(\ell)} = h_t^{(\ell-1)} + W_{\text{proj}}^{(l)} \sigma \left(W_{fc}^{(l)} \gamma \left(h_t^{(\ell-1)} \right) + b_{fc}^{(l)} \right) + b_{\text{proj}}^{(l)}$$

where W_{proj} , W_{fc} , $b_{\text{proj}}^{(l)}$, $b_{fc}^{(l)}$ are learned weight matrices and biases, γ is a normalizing nonlinearity, and σ is a pointwise rectifying nonlinearity (in our case GeLU). For a more detailed mathematical explanation of the transformer architecture we refer the reader to [41].

Probing is a technique to localize where specific information resides in a model by training a simple classifier (a probe) to predict a labeled feature of the input using the internal activations of the model [3]. More formally, we require a tokenized text dataset $X \in \mathcal{V}^{n \times T}$ (where n is the number of sequences and T is the context length), and an associated

labeled dataset $D_{\text{probe}} = \{x_{jt}, z_{jt}\}$ which provides labels for a subset of the tokens (e.g., the tense of every verb). In our setting, we focus on the MLP neuron activations $a^{(\ell)} = \sigma(W_{fc}^{(l)} \gamma(h_t^{(l-1)}))$ —the set of representations immediately after the elementwise nonlinearity—and train a linear binary classifier $g_\ell(a_{jt}^{(\ell)}) = \hat{z}_{jt}$ to minimize a classification loss $\mathcal{L}(z_{jt}, \hat{z}_{jt})$ for each layer of the network.

Key Concepts We make frequent reference to the concept of a *feature*. The field has not yet settled on a consensus definition [4], but for our purposes, we mean an interpretable property of the input that would be recognizable to most humans. A *monosemantic* neuron, is a neuron which activates for exactly one feature, though this can also be subtle depending on what one is willing to count as one feature versus a composition of related features. In contrast, a *Polysemantic* neuron is a neuron which activates for multiple unrelated features. Polysemanticity is a consequence of *superposition*, the phenomena of representing n features with $d < n$ dimensions. We focus on applying sparse probing to the activations of the MLP layers because these activations form a *privileged basis* [41]. That is, because applying an elementwise nonlinearity breaks a rotational invariance of the representations, it is more likely that the basis dimensions (each neuron) are independently meaningful. Without a privileged basis, as in the residual stream, there is no reason for features to be basis aligned, and therefore no reason to expect sparsity (modulo optimization quirks [66]). Finally, superposition manifests differently in the residual stream than in the neuron activations because of this privileged basis; we discuss this further in A.3.

3.2 Sparse Feature Selection Methods

Rather than just localize a feature to a direction in a layer, we attempt to identify a single neuron or a sparse subset of neurons which fire if (and ideally only if) the feature is present in the input. This can be accomplished by training a k -sparse probe, a linear classifier with at most k non-zero coefficients. The problem becomes, which of the $\binom{d}{k}$ possible neuron subsets are most predictive? While this is an \mathcal{NP} -hard combinatorial optimization problem, there exists a number of fast heuristics and tractable optimal algorithms [67].

In probing, this is typically formalized as a ranking problem [13], where neurons are individually scored by some importance measure and then rank ordered to include the top k . Given a binary classification dataset, natural scoring rules that have been explored are the absolute difference between class means for each neuron [13], the mutual information between each neuron and the labels [68, 32, 33], or the absolute magnitude of the coefficients of a dense probe trained with l_1 regularization [27].

We propose two additional techniques: adaptive thresholding and optimal sparse probing (OSP). OSP leverages recent advantages in sparse prediction solution techniques to train a k -sparse classifier to provable optimality using a tractable cutting plane algorithm [17], though this is only feasible for smaller values of k . For larger ranges of k , we use adaptive thresholding to train a series of classifiers that iteratively decrease the value of k , where at each step t we retrain a probe to only use the top k_t neurons with highest coefficient magnitude from the previous k_{t-1} -sparse probe. For sake of computational efficiency, in both methods we perform an initial filtering step to take the top neurons with maximum mean difference.

For all methods, we retrain a logistic regression probe for the k neurons selected. Additionally, note that while we focus on classification, all of these methods have a straightforward generalization to continuous targets.

3.3 Probing in Practice

Constructing Probe Datasets Executing an informative probing experiment begins with designing a suitable probing dataset. To illustrate a common issue, take the case of probing for the `is_politician` feature. If the dataset just includes the names of people labeled as politicians or not, the trained probe will not be able to distinguish the model’s `is_politician` feature from the `is_political` feature which fires for all political content(e.g., “The Democratic Party”). On the other extreme, if the dataset contains just the names of politicians and random tokens, the probe won’t distinguish `is_politician` from `is_person` as very few random tokens concern non-politician people. In other words, there is a general tension in how to shape the negative examples in the dataset to create the most *conceptual separation* between the true feature of interest and all possible correlates.

Another issue arises when the feature of interest is a property of multiple tokens or a full sequence of tokens (e.g., `is_python_comment` or `is_french`). If the relevant neuron fires on every token in the feature sequence, one could just sample tokens randomly, but there might be more specific conditions on when a neuron fires that cannot be known a

*a priori*². A solution to this is to perform an elementwise aggregation (e.g., mean or max) of the activations over the token span of each occurrence of the feature. For example, for a dataset of sequences in many different languages, the input to our probe could be the average activation vector for each sequence, with the target being the language of the sequence. Unfortunately, this gives a somewhat weaker result, as this process is not able to distinguish the `is_french_noun` feature from the `is_french_verb` feature, and thus requires further analysis to interpret correctly.

There are additional subtleties having to do with feature granularity, rare features, and overlapping features [15] which we explore in Section 5.4. With all of these issues, the most appropriate recourse will depend on the researcher’s intent and the nature of the feature being probed for.

Evaluation and Interpretation To evaluate the performance of a probe, we compute the number of true positives (TP), false positives (FP), false negatives (FN), and true negatives (TN) of our binary classifier on an out-of-sample test set. We then calculate the precision (PR), recall (RE), and F1 score (F1):

$$PR = \frac{TP}{TP + FP} \quad RE = \frac{TP}{TP + FN} \quad F1 = \frac{2PR \times RE}{PR + RE}$$

We use the F1 score as our primary evaluation metrics to determine which neurons are most likely associated with the target feature given the asymmetric importance of the positive class³. Precision and recall give insight into how the selected neurons’ implicit feature granularity compares to the feature being probed for. Low precision and high recall indicates either selected neurons are highly polysemantic or the model represents a more general feature than is being probed for. High precision and low recall of the probing classifier may indicate that the identified submodule represents a more specific feature than the feature being probed for (e.g. `is_french_noun` instead of `is_french`). We can adjust our preference for classifiers with high precision or high recall by modifying the threshold of the classifier or by tuning the class weights in the probe loss function; a higher class weight for the positive class (assuming it has fewer samples than the negative class) will prioritize recall over precision.

4 Empirical Overview

Models We study EleutherAI’s Pythia suite of autoregressive transformer language models [70]⁴. These models are fairly standard GPT variants that utilize parallel attention and rotary positional encodings and were trained on The Pile [71]. In particular, we run experiments on the 7 models ranging from 70M to 6.9B parameters; full model hyperparameters are given in Table 1.

Data We study ten different feature collections: the natural language of Europarl documents, the programming language of github source files, the data source of documents from The Pile, the part-of-speech and grammatical dependency of individual tokens, morphological features of tokens (e.g., verb tense), plain text features of tokens (e.g., whitespace or capitalization), the presence of specific compound words, latex features in ArXiv documents, and a number of factual features associated with people (e.g., gender, occupation). Full descriptions of datasets, their construction process, and summary statistics are available in B.2. All categorical features are converted into separate one-versus-all binary features for over 100 total binary classification tasks.

Experiments For each combination of model, feature, layer, and sparse feature selection methods, we train probes for a range of values for k , and report classification performance on a held-out test set. We compare the feature selection methods in B.5 and illustrate the relationship between model size and sparsity in Figure 7. For neurons identified as being especially relevant, we save the activations over larger text data sets and perform further analyses described throughout Section 5. All code and data are available at <https://github.com/wesg52/sparse-probing-paper>.

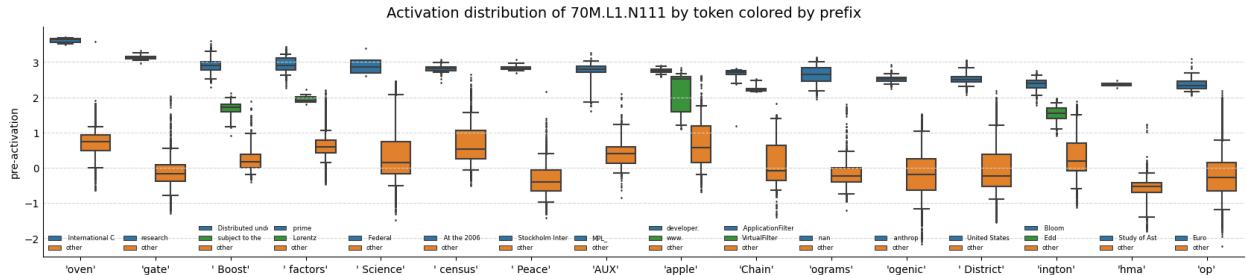
5 Case Studies

We conduct a series of more detailed case studies to carefully study the behavior of individual neurons, while also illustrating the challenges that pose barriers to further progress. Although we zoom in on very narrow examples, we found many neurons of the same category in our probing experiments, and believe these examples are representative of broader neuron families [5] that exist in all LLMs.

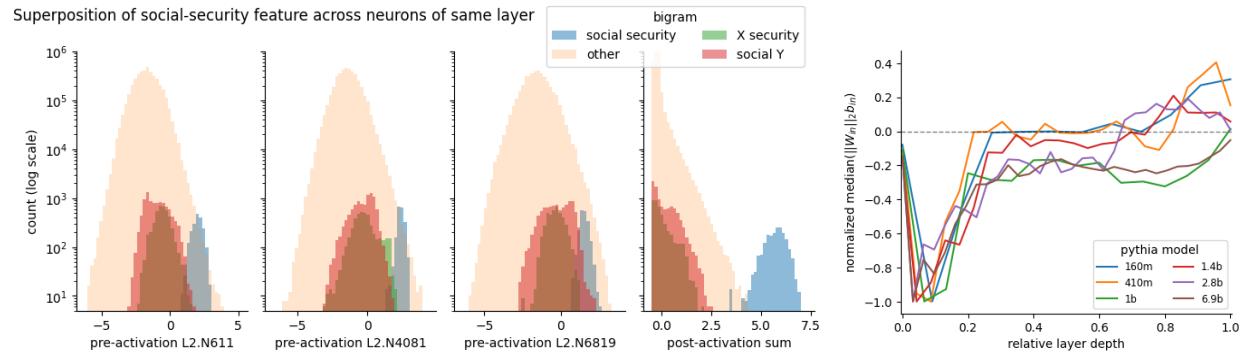
²As an example, in the case of factual recall, the results from [69] suggest that MLP neurons are especially important for the last token of a multi-token subject.

³We also measure Matthew’s Correlation Coefficient (MCC), a balanced accuracy metric, and the results are largely the same.

⁴<https://github.com/EleutherAI/pythia>; unfortunately, our experiments were performed with the V0 suite of models which have recently been updated.



(a) Activations of a single polysemantic neuron on different tokens when preceded by specific stimuli.



(b) Example of superposition in representing the compound word “social security.” (c) Evidence of superposition in early layers

Figure 2: Summary of our key results of superposition. Polysemantic neurons firing on many diverse stimuli (a) are necessary to implement superposition (b) to adequately represent many more possible n -grams than dimensions. The natural mechanism for implementing superposition in toy models leverages large weight norms and negative biases[4], which we observe to be most associated with early layers (c).

5.1 Superposition in the Wild: Compound Word Neurons

The token vocabulary is a fairly unnatural symbolic language to perform all of the linguistic and conceptual processing required of a language model. For instance, compound words like “social security” are treated as two separate tokens, despite meaning something very different when the tokens appear together versus apart. Moreover, quirks of spacing and capitalization frequently cause words to be broken up (e.g., despite “Harvard” being a single token, when not preceded by a space “Harvard” gets tokenized into “Har” and “vard”). Based on many such examples, [10] hypothesize that a primary function of the early layer neurons is to “de-tokenize” the raw tokens into a sequence of more useful abstractions. However, this *pseudo-vocabulary* might be extremely large (e.g., all common n -grams) making it a natural candidate for being represented in superposition. To investigate this, we probe for neurons which respond to 21 different compound words, where the first and second words mean something quite different when appearing separately versus together (e.g., “prime factors”).

After probing for neurons which activate for specific compound words XY while not firing on any bigrams of the form XZ or WY $\forall W, Z \in \mathcal{V}, Z \neq Y, W \neq X$ for each compound word we found *many* individual neurons which were almost perfectly discriminating. However, after inspecting the activations across a much wider text corpus, we observe these neurons activate for a huge variety of unrelated n -grams (see Figure 2(a)), a classic example of the well known phenomena of polysemy [5, 12, 10]. Superposition implies polysemy by the pigeonhole principle—if a layer of n neurons reacts to a set of $m \gg n$ features, then neurons must (on average) respond to more than one feature. This example also underscores the dangers of “interpretability illusions” caused by interpreting neurons using just the maximum activating dataset examples [72]. A researcher that just looked at the top 20 activating examples would be blind to all of the additional complexity of neuron 70M.L1.N111, with Figure 2(a) still only scratching the surface⁵. While inconvenient for interpretability researchers, polysemy is also problematic for the model, as it causes interference between

⁵This figure was generated with 300 million tokens from the Pile Test set but when run on 10 billion tokens of the Pile train set 16 of the top 20 dataset examples show the neuron activating on the “he” of German words starting with “Schönhe”. These maximum activating dataset examples can be viewed on Neuroscope[73]

different features [4]. That is, if 70M.L1.N111 fires, the model gets mixed signals that both the “prime **factors**” feature and the “International Coven” feature are present.

However, detecting n -grams in particular (and hence constructing the hypothesized pseudo-vocabulary), turns out to be a task particularly well suited for superposition (see A.2). In short, the model can take advantage of the fact that (for fixed n) exactly one possible n -gram out of $|\mathcal{V}|^n$ can occur at any time—that is, n -grams are mutually-exclusive binary features with respect to the current token of the input, despite coming from a massive set of possible features. While it would be impossible to dedicate a unique neuron to all possible n -grams, by leveraging the activations of multiple polysemantic neurons, each of which react to a bigram XY but with no other overlapping stimuli, the magnitude of the “true” feature gets boosted above all of the possible interfering features. As an example, in Figure 2(b), we show three neurons from the same layer which activate for the “social security” bigram while (mostly) not activating to bigrams with just one of the words (see the blue histograms being significantly to the right of the red and green histograms). However, because these neurons are polysemantic, there are many other inputs which cause them to activate, potentially even more so than the “social security” feature (see the orange histogram having a longer tail than the blue histograms). Despite this, by summing the activations across the three neurons, we achieve nearly perfect separation between the total activation magnitude of the “social security” feature and *all* other observed token combinations! We believe this to be first example of neuron superposition exhibited “in the wild” in real LLMs. We include examples for all 21 compounds words from layers 1-3 of Pythia 1B in Figures 9, 10, and 11, and further results on basis alignment in A.4 and Figures 13 and 14.

We believe that this computational motif—merging individual tokens into more semantically meaningful n -grams in the pseudo-vocabulary via a linear combination of massively polysemantic neurons—is one of the primary function of early layers. As a supporting line of evidence, we observe that a natural idealized model of n -gram recovery in superposition predicts a mechanistic fingerprint of superposition: the presence of large input weight norms and large negative input biases. We provide an idealised construction in Section C for how an arbitrary number of features can be compressed into two linear dimensions, similar to the construction in [4]. When we measure the product of the input weight norm and bias for each neuron in every layer and every model, we observe a striking difference in the early⁶ layers, exactly in line with our conceptual argument (see Figure 2(c) for a summary and Figure 8 for the full distributions).

We conclude by noting that, in another encouraging display of consilience, the phenomenon of different regions of the model employing different coding strategies for different functions bears resemblance to the diverse coding strategies employed by biological neural networks in different brain regions with different functional roles [74, 75, 76, 77]. We expect further research connecting local mechanisms to macroscopic structure to be particularly fruitful.

5.2 Context Neurons: a Monosemantic Neuron Family

Given the potential benefits of superposition, it is reasonable to ask if *any* features are represented monosemantically, and if so, why? We hypothesized that a likely candidate would be *context features*—high-level descriptions of all (or most) tokens within a sequence (e.g. `is_french` or `is_python_code`). Such features seem quite important, to the point that avoiding interference is worth a full neuron, while also being a higher-level property that may or may not be mutually exclusive or binary, making it harder to represent in superposition.

In particular, we probe on the language of natural language sequences from the Europarl dataset [78], the programming language of different Github source files, and the data subset of The Pile from which a sequence originated. We probe for these features using mean aggregation—training a classifier on the averaged activations over each sequence to predict the sequence label (e.g., `is_french` or `is_python`). Figure 3 depicts a sample of our results, illustrating the existence of highly specialized context neurons that activate approximately only when a token is in a specific context⁷ (with 21 additional examples in Figures 15, 16, and 17). To better understand the function of these neurons, for each token, we study the distribution of activations broken down by context (e.g., the activation of “return” in every programming language). Sorting by the largest differences (middle panel), we observe that one explanation for these neurons’ roles is token disambiguation. For example, many programming languages have a `return` keyword, but neuron 1B.L6.N3108 activates on `return` if and only if it is in the context of Go code.

To further support our interpretation and gain more insight into function, we conduct ablation experiments comparing the language modeling loss of the base model to the loss of the model with the identified neuron fixed to 0 for all tokens in every sequence (right panel). As anticipated, ablating the context neurons significantly degrades language modeling performance within the relevant context, while leaving other contexts virtually unaffected. The impact, however, heavily depends on the model size—in the 70M parameter model ($\approx 12k$ neurons), ablating a single neuron causes an average

⁶Pythia models use parallel attention so layer 0 is purely a function of the current token, hence not subject to the n -gram analysis.

⁷By recording the activation of every token, we eliminate the concern of finding an `is_french_noun` neuron instead of an `is_french` neuron.

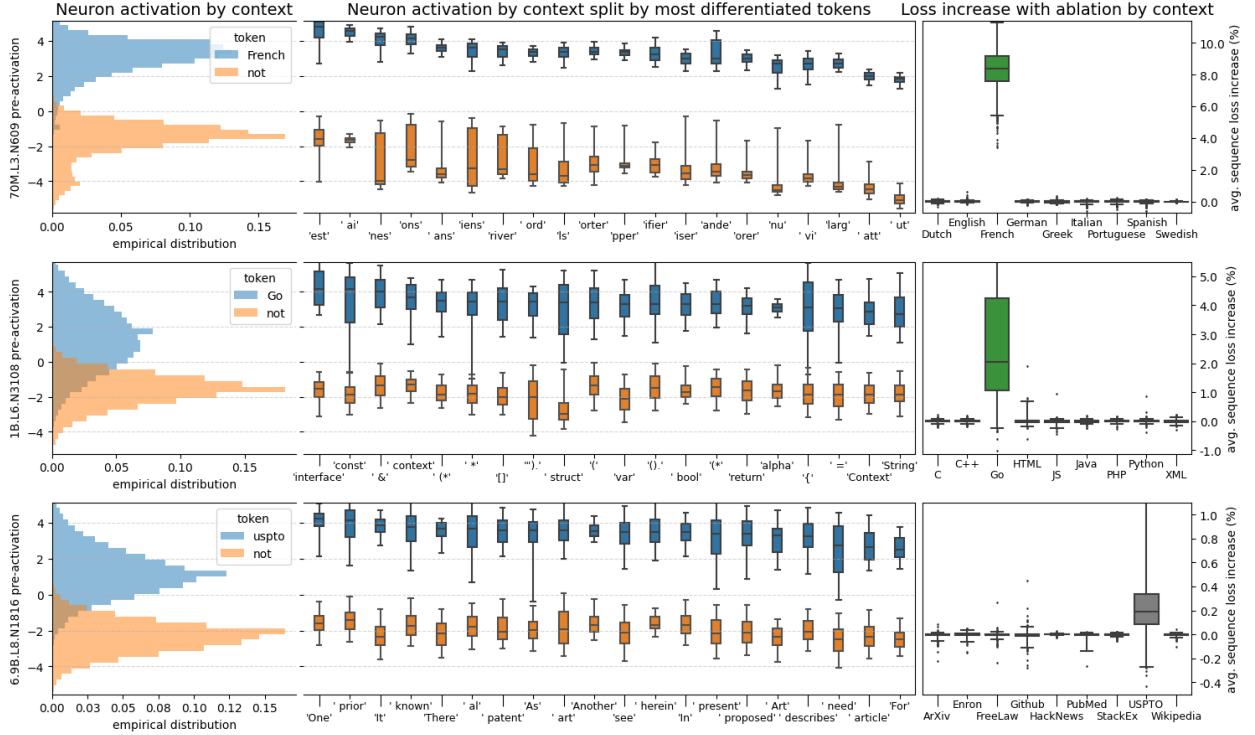


Figure 3: Analysis of individual context neurons that activate on tokens in French (top), in Go code (middle), and US Patent office documents (bottom). We show the distribution of activation when in and not in the target context (left) in addition to the tokens with average activation most distinguished by the neuron (middle). Finally we report the increase in sequence loss across contexts when the neuron is ablated (right).

loss increase of 8% per French sequence, while in the 6.9B model ($\approx 524k$ neurons), ablating one neuron results in only a 0.2% increase in loss.

While these neurons appear to be genuinely monosemantic, we emphasize that it is extremely difficult to prove this. Doing so requires answering thorny ontological questions (what *is* French?) and then efficiently searching through a dataset of billions of tokens to verify the neuron implements the answer. Moreover, the “true” feature the neuron responds to might be quite subtle. For instance, many of the code neurons do not fire when in a code comment, whereas the French neuron will fire in a non-French context on a French name or other token strongly associated to France⁸. In some sense, these exceptions prove the rule of the primary role of the neuron, but highlight the difficulty of mapping human features to the ontology of the network. Perhaps most challenging though, is ruling out the existence of very rare features the neuron also responds to. Sufficiently rare features will likely be undetectable from random samples or summary statistics—even when broken down by token—and therefore require manually⁹ examining max activating dataset examples in subdistributions where we don’t expect to find much French text.

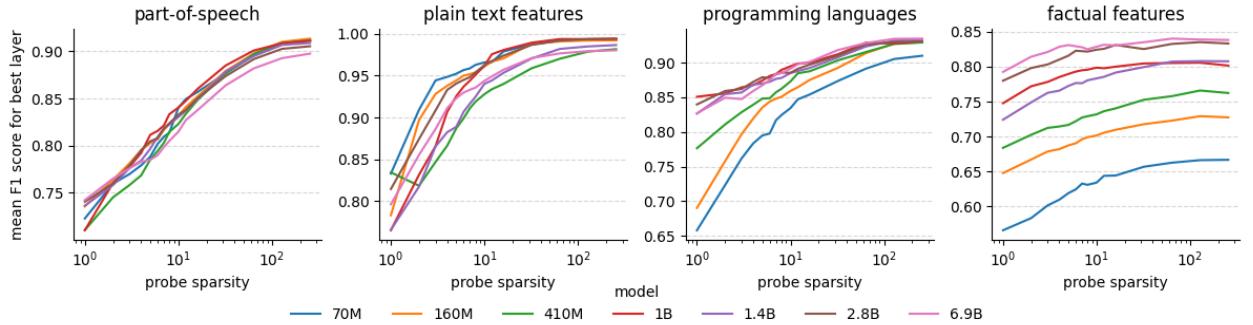
5.3 Effects of Scale: Quantization and Splitting

Given the importance of scale in LLMs, we turn our attention to studying the relationship between model size and the sparsity of representations, and the dynamics that drive this relationship. For all of our feature datasets described in B.2, we train a series of probes sweeping the value of k from 256 to 1 using adaptive thresholding. For sake of summarization, we report the maximum out-of-sample F1 value over the layers for each model, while averaging over the features within the collection (see Figure 4(a) for a sample and Figure 7 for full results with random baselines).

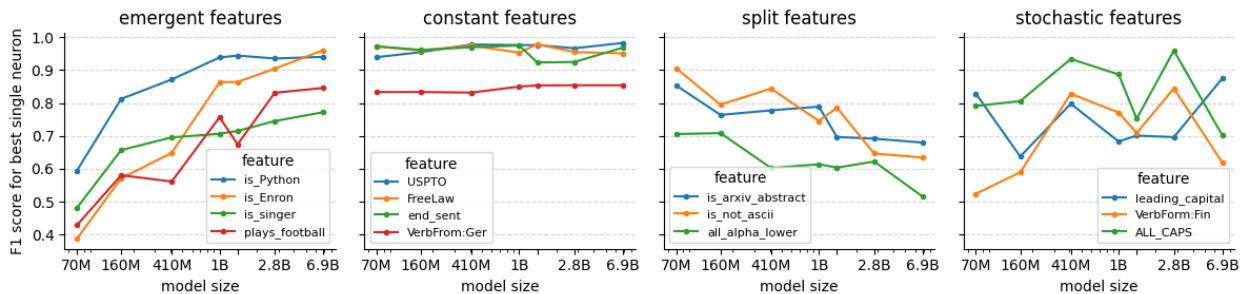
While some features appear to be more sparsely represented with scale (e.g., programming languages and factual features), we were surprised by how consistent others were (e.g., part-of-speech and compound words). In fact, for some of the simplest plain-text features, the smallest models seem to actually implement greater sparsity. When analyzing

⁸To further explore this, we encourage the reader to explore max activating dataset examples in Neuroscope[73]

⁹This is an area where we expect AI assisted interpretability to be particularly useful.



(a) Probe sparsity versus classification performance for different feature types and model sizes.



(b) Classification performance of most feature-aligned neuron by model size for different feature classes.

Figure 4: Summary of results on model scale. Representational sparsity increases on average with scale (top) but individual features obey different scaling dynamics (bottom).

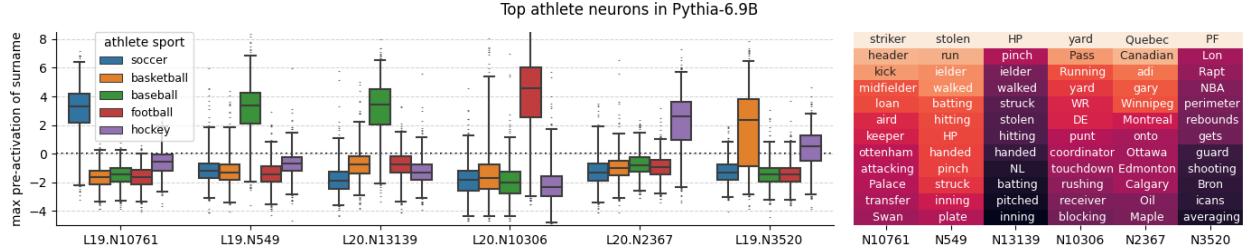
individual features on a per neuron basis, several general patterns become more apparent (Figure 4(b)). We believe there are two main dynamics driving these results: the quantization model of scaling [79] and neuron splitting [10].

In particular, the quantization hypothesis posits that there exists a natural ordering of features learned by a model with increasing scale based on how loss reducing they are, with larger models being able to learn a longer tail of increasingly rare features [79]. In our context, this suggests that features like part-of-speech or compound words are within the feature set learned by even small models, and are represented with very similar sparsity patterns. In contrast, factual features and some (but not all) contextual features only get represented by single neurons at sufficient scales. As a countervailing force, with increasing scale the model can dedicate multiple neurons to represent more granular features that was previously comprised one coarser feature. Consider the ALL_CAPS feature; while it would likely be advantageous to have dedicated circuitry for representing this feature in all models, a larger model might have dedicated neurons for all of the particular reasons a token might be in all capital letters (e.g., an abbreviation, a constant in python, shouting on the internet, etc.), eliminating the need to have just one more coarse grained representation. The result, as viewed from a probing experiment, is less sparsity, not more.

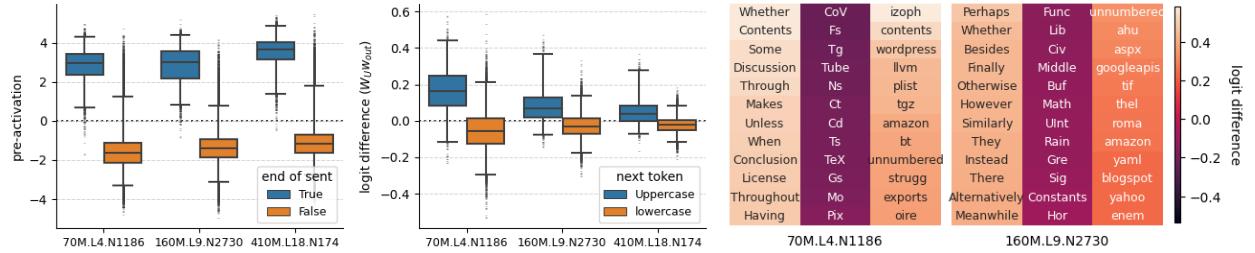
5.4 Refining and Verifying Interpretations

The result of a sparse probing experiment is a set of k neurons with a collection of classification performance metrics, usually for a range of values of k . We illustrate what conclusions might follow, simple techniques to refine and corroborate such conclusions, and confounding factors to be wary of.

One confounding factor is an ambiguity between superposition and *composition* [12]. If a (layer, feature) pair has a 1-sparse probe with poor accuracy and a k -sparse probe with high accuracy, it is tempting to take this as evidence of superposition, but it is also consistent with a feature being coarse or compositional—being either the union or intersection of multiple independent features. As an example, consider an *is_athlete* feature. Such a feature could either be represented by a single neuron, a superposition of polysemantic neurons, or as the union of neurons for specific types of athletes, as those shown in Figure 5(a). While we can distinguish a feature union from superposition by analyzing the activation cooccurrence (only one athlete type neuron activates for each athlete), this reasoning does not work for a true compositional feature. For example, we also found individual neurons which coded for a person’s gender and whether they are alive or not (Figure 20). It is likely more natural for a model to represent



(a) Neurons which activate for the names of specific types of athletes (left) turn out to be more general sport neurons when analyzing the top per-token average activations (right).



(b) End of sentence neurons: analyzing the effect on the output vocabulary can corroborate and refine neuron interpretations.

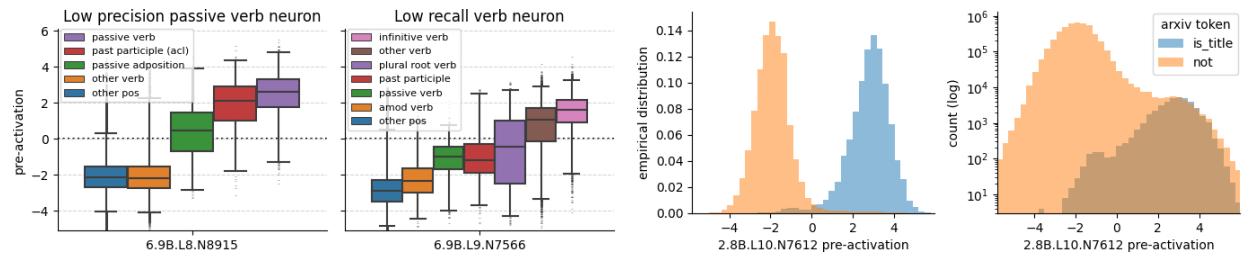


Figure 5: Examples of analyses used to refine and support neuron interpretations.

the `is_living_female_soccer_player` feature as simply a composition of three different neuron aligned-features `is_living`, `is_female`, and `plays_soccer`, which would nevertheless have low 1-sparse accuracy but high 3-sparse accuracy. Of course, this also assumes that these neurons are all in the same layer. However, models can, and almost certainly do, leverage superposition and composition across multiple layers, a subtlety which we blissfully ignore and leave for future work.

For the remaining discussion, we consider individual neurons identified by 1-sparse probes—how do we interpret such neurons? The most basic analysis is to simply inspect the maximum activating dataset examples [73], though this is subject to interpretability illusions [72]. A slightly more robust analysis involves computing the average activation for each token in the vocabulary. Doing so for our athlete neurons in Figure 5(a) reveals these neurons are perhaps better thought of as generalized sport neurons which activate for all tokens generally having to do with a particular sport, including the names of athletes (with the notable exception of the hockey neuron which appears to be a Canadian neuron).

In addition to analyzing a neuron via the input, one can also gain insight by analyzing the output; in particular, one can compute a neuron’s effect on the output logits by simply considering the product of the unembedding matrix and the neuron output weight [50]. Doing so for neurons which always activate on punctuation ending a sentence, we find that the output probability of most uppercase tokens gets increased while the probability of most lowercase tokens gets decreased (Figure 5(b)). Inspecting specific examples is often constructive; for instance, the highest increasing lowercase tokens are words like “amazon” or “wordpress,” indicating such neurons are also useful in constructing URLs. For uppercase tokens, those with the highest increase in probability correspond to words like “Finally” or “However” while the most decreased tokens are those representing atomic elements, proper nouns, or CamelCase strings.

Most of the neurons discussed thus far have had excellent overall classification performance; what happens if there does not exist such a crisp fit? As discussed in Section 3.3, classification performance can be further decomposed into precision (sensitive to false positives) and recall (sensitive false negatives). In our context, high recall and low precision with respect to a specific feature potentially suggests that a neuron represents a less granular feature than the feature manifest in the probe dataset¹⁰; low recall and high precision suggest a neuron represents a more specific feature. As an example, Figure 5(c) depicts the activations for a high-recall-low-precision neuron identified when probing for `is_passive_verb` and a low-recall-high-precision neuron identified when probing for `is_verb` in Pythia 6.9B. When we analyzed these neurons in more detail, we find that in addition to activating on all occurrences of passive verbs, L8.N8915 also activates on adjacent adposition tokens, and past participles when in an adnominal clause. Almost symmetrically, L9.N7566 activates on most verbs, especially infinitive verbs, but not passive verbs, adjectival modifiers, plural root verbs, or past participles in certain dependency roles. These examples illustrate the more general point that it should not be assumed that a model will learn to represent features in an ontology convenient or familiar to humans.

Of course, precision and recall are only defined with respect to the labels of a probing dataset, which may themselves contain imbalances or spurious correlations that confound the results. Perhaps most common, especially when constructing a dataset from scratch, is the problem of asymmetric sampling and rare features. Consider a probing dataset for an `is_arxiv_paper_title` feature (Figure 5(d)). Without a more specific hypothesis on the relevant negative examples, one is likely to simply sample random non-title tokens (or at least weight all non-title examples the same). However, when the space of negatives is large (e.g., all non-title tokens), at a distribution level, all rare features get drowned out. Hence, when looking at summary or distributional statistics, the results can look impressive (Figure 5(d); the neuron had $F1 > 0.95$ for `is_title`), but when looking at raw counts (Figure 5(d) right) one observes that the `is_title` feature actually explains less than half of the activations. Though, upon inspection, we find that the rest of the activations are for *section titles*!

6 Discussion

6.1 Strengths and Weaknesses of Sparse Probing

The primary use case of sparse probing is to quickly and precisely localize neurons relevant to a specific feature or concept, while naturally accounting for superposition and composition. The speed and precision of recovery is in contrast to gradient based [38] and causal intervention based methods [69], which are too slow or coarse-grained to be used for features requiring precise localization within large models. The feature specificity contrasts with sparse autoencoding based methods which aim to recover *all* features stored in the model, but in an unsupervised manner and without attributing semantic meaning to each feature [53]. Having probes with optimality guarantees further addresses the pitfall raised by [13] regarding the conflation of classification quality and ranking quality when analyzing individual neurons with probes. Moreover, sparse probes are designed to be of minimum capacity, mitigating the concern that the probe is powerful enough to construct its own representation to learn the task [14]. While probing requires a supervised dataset, once constructed, it can be reused for interpreting any model (modulo features regarding tokenization), enabling investigation into the universality of learned circuits [5, 46] and the natural abstractions hypothesis [80]. By design, sparse probing is particularly well suited for studying superposition, and can be used to automatically test the effect of architectural changes on the frequency of polysemy and superposition, as opposed to relying on human evaluations as in [10].

However, sparse probing also inherits many of the weaknesses of the general probing paradigm [14, 28, 15, 29, 30]. In short, the results from a probing experiment just do not allow for drawing especially strong conclusions without more detailed secondary analysis on the identified neurons. Probing offers limited insight into causation, and is highly sensitive to implementation details, anomalies, misspecifications, and spurious correlations within the probing dataset. For interpretability specifically, sparse probes cannot detect features built up over multiple layers or easily distinguish between features in superposition versus features represented as the union of multiple independent and more granular features [12]. In seeking the sparsest classifier, sparse probing may also fail to select important neurons that are redundant within the probing dataset, requiring the use of iterative pruning to enumerate all important neurons. Multi-token features require special processing, often in the form of aggregations that can further weaken the specificity of the result. Finally, depending on how much representations change with scale [79], larger models may utilize more specific features [10], hampering the transferability of datasets between different model scales.

¹⁰It is also consistent with superposition. Indeed, all of the compound word neurons had higher recall than precision.

6.2 Strengths and Weaknesses of Empirical Findings

In light of the limitations of probing, we attempted to corroborate every case study with independent evidence, including theoretical predictions, ablations, and vocabulary analyses. We find our evidence compelling, although not always conclusive. In particular, we believe we have provided the clearest evidence to date of superposition, monosemantic neurons, and polysemantic neurons in full scale language models. Furthermore, by demonstrating this behavior in seven different models spanning two orders of magnitude in size while exploring over a hundred features, we believe our basic insights are likely to be general and to transfer to current frontier models like GPT-4.

However, much of our analysis is *ad hoc*, tailored to the specific feature being investigated, and requires substantial researcher effort to draw conclusions. While we explored models of varying size, they were all from the same model family and trained with the same data. We think it is unlikely our results are specific to the implementation details of the Pythia model suite, but we do not rule this out. Additionally, the largest model we studied is 6.9 billion parameters which is still more than order-of-magnitude off the frontier. Given the emergent abilities of LLMs with scale [81], it is possible our analysis misses a key dynamic underlying the success of the largest models. Moreover, our results are restricted to binary features and categorical features converted to binary features, and we are not confident that our insights will cleanly transfer to continuous features or cleverly encoded categorical features.

6.3 Implications

For interpretability researchers, our results support the conclusion that superposition is important for the success of models. Hence, attempts to remove it [10] are likely either hiding it or are unlikely to be competitive, but that the highest leverage interventions are perhaps best aimed at the early layers. For AI ethicists and legal scholars, our study of factual neurons point to an important avenue of further inquiry—understanding how neurons encoding protected attributes compute this feature and affect downstream predictions of the model. For AI alignment scholars, our work highlights the potential of identifying safety-critical features and perhaps even manually intervening in computations to enhance our ability to steer models. While none of the features we probed for were especially critical, the Pile subset context neurons could be considered a precursor for situational awareness [47, 82].

6.4 Future Directions

We only scratched the surface of possible applications and experiments involving sparse probing. Scientifically, further understanding superposition—and how to cope with it—seems central to making progress on the ambitious version of mechanistic interpretability. As outlined in [4], this requires either designing architectures which do not use superposition or to take features out of superposition using a sparse coding like technique—both of which can be assisted with automatic sparse probing as a form of validation. While not explored here, it would also be possible to apply sparse probing to predicting properties of the *output* (e.g. `next_token_is_verb`), as opposed to properties of the input, to better understand the neurons most implicated in making specific types of predictions. With neurons identified in each experiment, it would be potentially insightful to also track how these neurons develop and change through time [83] as well as more carefully analyze how the set of neurons change with scale [79], which is naturally enabled by the Pythia suite’s [70] checkpoints. In particular, sparse probing (or similar) is well suited to study neuron splitting in more detail by training probes to predict the value of a less granular neuron from the sum of a sparse set of more granular neurons.

Our primary motivation however, is in ensuring the development of safe AI systems. To further this goal, we envision the development of a large library of probing datasets—potentially with AI assistance—that capture features of particular relevance to bias, fairness, safety, and high-stakes decision making. In addition to automating evaluations of new models, having large and diverse supervised datasets will enable better evaluations of the next generation of unsupervised interpretability techniques [53, 84] that will be needed to keep pace with AI progress.

7 Conclusion

Guided by sparse probing, we have found some of the cleanest examples of monosemantics, polysemantics, and superposition in language models “in the wild,” and contributed practical guidance and conceptual clarification for how to interpret neurons in greater detail. More than any specific technical contribution, we hope to contribute to the general sense that ambitious interpretability *is* possible—that LLMs have a tremendous amount of rich structure that can and should be understood by humans. We believe this is most productively accomplished with an empirical approach more reminiscent of the natural sciences, such as biology or neuroscience, than the traditional experimental loop of ML. While such research can be hard to finish, it is easy to start, so we encourage the curious researcher to just start looking! It is the dignified thing to do.

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Author Contributions

Wes Gurnee proposed, led, and executed most of the research in addition to writing the paper. **Neel Nanda** advised on most of the technical and methodological aspects of the research, helped interpret and red-team results, shaped the main narrative of the paper, and made substantial revisions. **Matthew Pauly** implemented the initial activations infrastructure, and led the development of the wikidata feature datasets and the factual feature experiments. **Katherine Harvey** assisted with the literature review, performed deeper investigations into the monosemanticity of context neurons, and made the data tables. **Dmitrii Troitski** assisted with investigating the role of early layer neurons, enumerating many additional concrete examples of polysemanticity. **Dimitris Bertsimas** inspired, supported, and advised the investigation in addition to editing the paper.

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A Frequently Asked Questions

A.1 Why expect ambitious interpretability to be possible or worthwhile?

Although gradient descent has no reason or incentive to learn representations scrutable to humans, the same could be said of all the biological structures “learned” by natural selection. The form and function of such structures were no doubt similarly incomprehensible to early pioneers in molecular biology, genetics, and neuroscience, exhibiting an emergent complexity that seemed irreducible. However, rather than claiming cells, genes, or brains were “uninterpretable,” entire scientific disciplines emerged which have made great strides in understanding the core principles in sufficient detail to enable intervening, engineering, and controlling biological systems. We believe artificial neural networks can be fully interpreted—even reverse-engineered—but doing so requires a comparable amount of effort as interpreting biological ones. In many ways, this emerging *artificial neuroscience* is unusually amenable to the scientific method: it is possible to run arbitrary counterfactual experiments, iteration times are rapid, resource requirements are minimal, all with full observability and measurement precision equal to floating point machine precision. While ambitious, we think such an effort is paramount for addressing issues in the alignment and control of increasingly capable AI systems.

A.2 Why are mutually exclusive features easier to represent in superposition?

The phenomena of superposition arises because models can decrease loss by representing more features, yet having non-orthogonal features introduces interference which increases loss. This creates a pareto-frontier trading off the two for each feature and each model, and this determines the representations a model learns. Crucially, interference between two features A and B decomposes into two conceptually different forms of interference^[87]: alternating interference where A is present, B is not present (or vice versa), and the model needs to tell that A is present and B is not, and simultaneous interference where A and B are present, but the model needs to tell that A and B are both present, but that, for example A is not present at twice strength. To understand the difference, let's consider the case where A and B are binary features corresponding to different directions of unit norm.

Alternating interference is fundamentally about distinguishing high activations (feature A is on) from low activations (feature B is on, feature A is off, but its direction is not the same as feature A's direction), which is fairly straightforward with GELUs and softmaxes. But simultaneous interference is fundamentally about treating medium activations (feature A is on, feature B is off) as the same as high activations (feature A is on and feature B is on) but different from low activations (feature A is off and feature B is on, or both are off). This is much harder to do with GELUs or softmaxes.

In practice, models seem to avoid superposition with high simultaneous interference (e.g., correlated features), but tolerate high alternating interference (e.g., anti-correlated features). Notably, [4] observed that independent features occurring with probability p engage in more superposition when p is lower - the probability of alternating interference is linear in p while simultaneous is quadratic in p , so for rare features simultaneous interference is a non-issue.

Mutually exclusive features like n -grams are an extreme case where simultaneous interference can never occur, and so are well suited to superposition.

A.3 What is the difference between residual stream and neuron superposition?

Residual stream superposition, also sometimes called bottleneck or linear superposition, is fundamentally about compression. That is, mapping a high dimensional space to a low dimension space such that the model can recover the compressed features at a later point in the network. This also implies that the model has already computed the feature, and the superposition is just for the purposes of storage. In contrast, neuron superposition *is* about computation. If there exist more features than neurons that must be potentially computed, then each individual neuron must (on average) be involved in the computation of many features.

A.4 How can you conclude you found superposition as opposed to simply non-basis aligned features?

We think that our findings of superposition rest on two sub-claims: (1) that there exist more features than neurons to represent them and (2) that the neuron basis is meaningful, such that superposition is implemented as a sparse combination of neurons.

We think claim (1) is clearly true, given the extremely long tail of features in internet text in addition to all the possible meaningful n -grams and other repeated patterns that model would clearly want to memorize. As an example, just take the case of people's names. There are likely more people that GPT-3 knows about than it has neurons. A first and last name gets split into at least two tokens, but with most surnames being tokenized further. We think it would be impossible to fit all of the possible features of these people as just linear combinations of the token embeddings, therefore requiring some nonlinearity to detect the presence of a sequence of tokens corresponding to a name, and adding back the appropriate information about this person.

To further support claim (2), we run an experiment on the compound words dataset comparing the classification performance of the top 50 individual neurons in a layer to the top 50 dimensions in a random basis. In particular, for both the standard neuron basis, and the activation dataset when multiplied by a random $d \times d$ Gaussian matrix, we train 1-sparse probes for the 100 neurons with the largest class mean difference, and report the out of sample F1-score for the top 50 (averaged over 5 such random bases). Our results in Figure 13, clearly demonstrates that individual neurons are more predictive than random linear combinations of neurons, which implies that the neuron basis is meaningful.

Although there are usually 1-5 neurons with notably higher F1 score than the rest, the full top 50 neurons still maintain high F1 scores. This seems consistent with results from Section 8 of [4], where there exists a main neuron per feature, with a longer tail of less important neurons. Intuitively, just achieving linear separability is unlikely to be sufficient for overcoming interference. To minimize interference models likely want to maximize the separation between potentially interfering features, implying that the potential number of neurons in superposition may be much higher than the minimal number required to achieve near perfect classification performance. For a rough approximation, in Figure 14, we measure the logistic test loss, rather than F1 score, of k -sparse probes for a range of values of k . Again, we see that probes trained in the neuron basis generally have lower loss than those trained in a random basis. Perhaps more interestingly, there appears to be two regimes governing the loss with respect to sparsity, one with power law scaling, and then a kink with no returns to using additional neurons. It is plausible this kink gives an indication of the "true" sparsity used to implement features in superposition.

Finally, we note that these results likely understate the basis alignment, because they are with respect to an "easy" classification task: just distinguishing bigrams XY from bigrams XZ or WY rather than all possible n -grams, and that there likely exist many confounding contextual correlates that improve the performance of the random basis dimensions. Designing more careful experiments to untangle these different effects is an important area for future work.

A.5 Which sparse probing method should I use?

It depends. If your experiments must be extremely fast or scalable, then simply doing maximum mean difference is likely best. If you are less runtime sensitive and want to sweep over a large range of k then adaptive thresholding is most appropriate. Finally, if you require any sort of formal guarantees then you should use optimal sparse probing, with the caveat that this requires potentially substantial compute time.

A.6 Why think of features as directions?

The intuition behind this is that the primary capability of models is doing linear algebra—addition and matrix multiplication, which further breaks down into addition, scalar multiplication, and projecting onto specific directions. Given these capabilities, it is especially natural for a model to represent features as directions: if a later layer wants to access a feature it can project onto that feature's direction, a neuron can easily access and combine multiple features, features can vary independently, and the component in that feature direction represents the strength of that feature.

A.7 What are possible conceptual models for what MLP layers are actually doing?

Perhaps the main model, as hypothesized and studied in [48], is that of a key-value store (note that the key and value terms here are unrelated to those used in the attention layers). A key-value store can be used in tasks such as memorization and factual recall, where the model wants to look up a fact, such as the location of the Eiffel Tower. If the residual stream contains both the features "Eiffel" and "Tower," then a neuron's key could be the sum of both of those features, and the value could be the feature indicating that the current token is in Paris.

The non-linearity of the MLP might serve several possible roles, such as thresholding, where only if the "Eiffel" and "Tower" features are present, do we conclude that it is in Paris. Additionally, some form of translation or memory management could be necessary, where it would not be in the model's interests to produce the "is in Paris" feature earlier on for fear of causing interference. Another possible role is that of activation range management. More broadly, neurons seem well-suited to representing Boolean functions such as AND, which is inherent in studying simple structures such as bigrams and trigrams. An AND can be implemented by stating that if the features A and B are both present with size 1, then only if their sum is present with size 2 does the neuron fire, and otherwise it is set to zero.

Another role that neurons might play is that of disambiguation. There are certain tokens which occur in very different contexts, but where the same token arises, such as "Die" in English corresponding to "death," "dice," or "Die" as a common token in languages such as German or Dutch or Afrikaans. Neurons that disambiguate "Die" have been observed in the literature [10]. In some sense, this can be thought of as having a more general "this is in Dutch" neuron producing an "is in Dutch" feature, and having the neuron having the "Die in Dutch" feature be the linear combination of the "is in Dutch" feature and the "Die" token is present feature.

One interesting application of neurons in transformers that does not occur with simpler models such as convolutional networks is neurons engaging with and enhancing the function of attention heads. Models with a single attention-only layer can exhibit functions such as skip trigrams, but where this has bugs [41], a neuron could be used to fix this. They could also compose with important attention head circuits, such as induction heads, to help clarify edge cases. Induction heads detect and continue repeated text, but if a token arises in multiple different contexts in the prior text with different subsequent tokens, we may want the induction heads to not activate at all. This is easier done with clarifying neurons than with an attention-focused circuit.

A.8 Did you train your probes on pre-GELU or post-GELU activations?

We train our probes on the post-GELU neuron activations (ie $\text{GELU}(W_{in}x)$) because there's a linear map from these to residual stream, so linear combinations of them are meaningful to the network, in a way that pre-GELU linear combinations are not. We often choose to plot histograms of pre-GELU activations for individual neurons for clarity, to better show the negative range, and to avoid an enormous spike around zero from all highly negative activations.

A.9 Did you have any negative results?

Yes. We had two types of feature datasets which did not appear to be sparsely represented: falsehoods in the counterfactual dataset or the occurrence of particular suffixes and prefixes, though both attained fairly high accuracy with a dense probe. For prefixes and suffixes, since these are purely a property of single tokens, we believe these aren't likely to get dedicated neuron representation since the feature already exists within the token embedding.

For counterfactual, a dataset of true and false factual completions, we hypothesized there might exist some dedicated "falsehood" neuron. However, sparse probes performed quite poorly, while increasing k continued to yield performance gains until about $k = 1024$ where we achieved 90% accuracy on the best layer. Our interpretation of this is that the probe is picking up some pattern of confusion or dissonance, associated with an unexpected completion, rather than a true falsehood or truth feature.

Our last negative result was in attempting to causally implicate the factual neurons. That is, run ablations that degrade the performance of few shot prompting based classification of people's gender, occupation, and whether they are alive or not. However, ablating individual neurons seemed to have very limited effect, indicating that either the "fact" was computed previously, and these neurons

are simply responding to this fact, or that there is some amount of ensembling or redundancy [88] that is robust to the deletion of a single neuron.

B Experimental Details

B.1 Models

We study the Pythia model suited [70] which was trained on The Pile [71], with each model trained for the same number of steps with an identical data ordering. These models follow a fairly standard architecture, but use parallel attention and rotary positional embeddings. See Table 1 for the architectural parameters of each model studied.

Model	n_{layers}	d_{model}	n_{heads}	d_{head}	Total Number of Neurons
Pythia 70M	6	512	8	64	12288
Pythia 160M	12	768	12	64	36864
Pythia 410M	24	1024	16	64	98304
Pythia 1B	16	2048	8	256	131072
Pythia 1.4B	24	2048	16	128	196608
Pythia 2.8B	32	2560	32	80	327680
Pythia 6.9B	32	4096	32	128	524288

Table 1: Hyperparameters of Pythia models studied.

B.2 Datasets

Table 2 contains summary statistics of all of our probing datasets in addition to the full list of features in each. We briefly describe the design, preprocessing, and motivation of each one.

Dataset	Sequences	n_{ctx}	Non-pad tokens	Source	Pos ratio	Total Features
part-of-speech	1438	512	281044	EWT	0.20	16
dependencies	1438	512	281044	EWT	0.20	29
morphology	1438	512	281044	EWT	0.20	22
code language	5397	512	2757867	pile-github	0.11	9
natural language	28084	512	14350924	pile-europarl	0.11	9
text features	10000	256	2248714	pile-test-all	0.26	11
data subset	8413	512	4299043	pile-test-all	0.11	9
compound words	167959	24	4031016	pile-test-all	0.20	21
latex	4486	1024	4589178	pile-arxiv	0.26	14
wikidata sex or gender	6000	128	688085	pile-test-all	0.50	2
wikidata is alive	6000	128	688179	pile-test-all	0.50	2
wikidata occupation	6000	128	677512	pile-test-all	0.17	6
wikidata athlete	5000	128	575350	pile-test-all	0.20	5
wikidata political party	3000	128	337755	pile-test-all	0.50	2

Table 2: Summary statistics of probing datasets studied.

Natural Language We used both the raw text and the labels from the EuroParl subset of the pile, which contain a large number of parliamentary proceedings in many different languages. Many documents were quite a bit longer than our context length, so for each, we took a random contiguous sequence from the document. This choice was also made to minimize any context clues from the beginning of the document about the country speaking. For probing, we performed mean-aggregation. That is, computing the activation for all non-padding tokens in the sequence and using the average neuron activations as the representation for the sequence to be used for probing. One problem with this dataset is that all of the sequences are similarly styled, and about similar topics, hence our probes could be picking up on a particular style or topic feature rather than a true language feature.

Data Subset Similar to the above, we randomly selected several thousand sequences from each data subset of the Pile test set, where the labels were implied. We also used the same random sub-sequencing and mean aggregation.

Programming Languages For our programming language dataset, we took all of the github subset from the Pile test set. We then used a code recognition package to classify the type of code, and only include the source files with a prediction of over 90%

Dataset	Features
part of speech	AUX, ADP, VERB, ADJ, X, CCONJ, PROPN, NOUN, INTJ, SYM, PRON, DET, SCONJ, ADV, PUNC, NUM
dependencies	aux:pass, acl:relcl, nsubj, xcomp, flat, cc, mark, acl, ccomp, appos, root, nmod:poss, aux, amod, nsubj:pass, obj, obl, det, advmod, punct, parataxis, conj, case, list, advcl, cop, compound, nummod, nmod
morphology	eos_True, Person_2, Gender_Fem, VerbForm_Inf, PronType_Dem, Gender_Masc, first_eos_True, Gender_Neut, VerbForm_Part, NumType_Card, PronType_Int, PronType_Prs, Person_3, Tense_Past, Number_Plur, PronType_Art, Voice_Pass, PronType_Rel, VerbForm_Ger, Mood_Imp, Person_1, VerbForm_Fin
code language	Python, XML, Java, C++, HTML, C, Go, PHP, JavaScript
natural language	Swedish, Portuguese, German, English, French, Spanish, Greek, Italian, Dutch
text features	leading_capital, no_leading_space_and_loweralpha, all_digits, is_not_ascii, has_leading_space, contains_all_whitespace, all_capitals, is_not_alphanumeric, contains_whitespace, contains_capital, contains_digit
data subset	github, pubmed_abstracts, stack_exchange, wikipedia, freelaw, hackernews, arxiv, enron, uspto
compound words	mental-health, magnetic-field, trial-court, control-group, human-rights, north-america, clinical-trials, high-school, third-party, public-health, cell-lines, living-room, second-derivative, credit-card, social-media, prime-factors, federal-government, social-security, blood-pressure, gene-expression, side-effects
latex	is_superscript, is_inline_math, is_title, is_subscript, is_reference, is_denominator, is_author, is_numerator, is_display_math, is_math, is_abstract, is_frac
wikidata sex or gender	is_female, is_male
wikidata is alive	true, false
wikidata occupation	is_actor, is_athlete, is_journalist, is_politician, is_researcher, is_singer
wikidata athlete	is_american_football_player, is_association_football_player, is_baseball_player, is_basketball_player, is_ice_hockey_player
wikidata political party	is_democratic_party, is_republican_party

Table 3: All feature within the feature collections.

confidence. A challenge with code is that it includes many tokens which aren’t code (licenses, copywrite, comments, etc.). As a very coarse cleaning attempt, we ignore the first 50 tokens in the sequence when applying mean aggregation, to avoid beginning of file boilerplate. However, for some languages like HTML or XML that likely contain substantial plain text, this does little to help (and hence we see the lowest accuracy on HTML and XML).

Compound Words For our compound words dataset, we computed the top thousand alphabetical bigrams XY over the pile test set. We then filtered for bigrams where $P(X = x|Y = y)$ and $P(Y = y|X = x)$ were below 0.3 to make the prediction task less trivial. We then manually filtered to bigrams with the property that the first and second word together means something quite distinct from either word separately. For the probing dataset, we then included 2000 short (24 tokens) sequences from The pile ending with the bigram XY, 4000 examples ending with XW, W \neq Y, and 4000 examples ending with ZY, Z \neq X. We then probe on the activations of the last token of every sequence.

Latex Features For our latex feature dataset, we included the first 1024 tokens of all documents from the ArXiV subset of the Pile test set which contained at least 1024 tokens. We mostly relied on regular expressions to extract features, though used a simple finite state machine to parse the math text. For each of the features involving any sort of “containment,” (which is most of them), we used the policy that all tokens within the containment counted as being part of the feature, but any tokens defining the containment for not. For instance for `is_subscript`, the `_{} token is not included, but anything within the braces is. For our positive class, we randomly sample tokens from the set of all positive tokens. For features with a natural complement (e.g., is_numerator and is_denominator) we make the negative class be occupied by half of tokens within the complement, and half random tokens.`

Text Features For our plain-text feature dataset, we similarly extracted features using regular expressions, but just applied to the raw token strings. Therefore, for our text features, a feature could be correctly predicted simply by partitioning the tokens into two classes, with no additional context. We sampled tokens randomly from a subset of the Pile test set.

Linguistic Features For our linguistic features, we use the text and labels from the well known Penn Treebank Corpus. The dataset is provided at a sentence level, so we first merge sentences from the same documents, and then perform a token alignment and character mapping to adapt the dataset labels to the specific tokenization of the Pythia models. For features that apply to all tokens (like part-of-speech or dependency relations), we have no restrictions on the tokens sampled for the negative class. For features

restricted to tokens of specific types (e.g. verb tense), we restrict the negative examples to be from the same token class (e.g. only verbs).

Wikidata Features To create a Wikidata feature dataset for a specific property (e.g. gender, occupation), we search through a JSON dump of all Wikidata entities and compile a table containing the names and relevant property value for each person with data on the chosen property. When there are multiple Wikidata entities with the same name, we choose the entity with more total Wikidata properties defined as a heuristic for relevance. We then search the text of the test set of The Pile for instances of these names and filter out all examples with names that occur only once in the dataset. We tokenize each matching string and truncate to 128 tokens such that the tokenized name is at the end (if there are sufficient preceding tokens, otherwise we pad the tokenized string to length 128). We further filter the tokenized examples to ensure that each name occurs no more than three times in each feature dataset. This helps us find general knowledge neurons that aren't overly impacted by individual people. Then when probing, we consider only the activations for the tokens of the surname for each example to reduce the effect of correlations between first names and certain properties (such as gender).

B.3 Feature Selection Methods

Throughout, assume we have a dataset of token activations for n tokens and d neurons $X \in \mathbb{R}^{n \times d}$, and a vector of labels $y = \{-1, 1\}^n$. We refer to the set of tokens in the positive class P and the set of tokens in the negative class N . Below we describe the different feature selection methods in more detail. With the exception of optimal sparse probing and adaptive thresholding, we can think of these approaches as scoring algorithms that can be used to rank the different neurons by importance. Then, to get a k sparse classifier, in all cases one just selects the k neurons with highest score s .

Mean Difference The score is given by the average mean difference between classes for each neuron. That is, for neuron i we have $s_i = \frac{1}{|P|} \sum_{j \in P} X_{ij} - \frac{1}{|N|} \sum_{j \in N} X_{ij}$.

Mutual Information We use the algorithm presented by [68], to compute the mutual information between continuous data (in this case each neuron independently) and a discrete target relying on a nearest-neighbor approximation. The score for each neuron is then just the estimated mutual information.

L_1 regularized We train a dense logistic regression probe on the activations with L_1 regularization. The score for each neuron is the absolute value of the corresponding coefficient of the dense probe.

F-statistic We utilize a one-way ANOVA test to evaluate the relationship between the continuous data of each neuron independently and a discrete target. The F-statistic is calculated by partitioning the total variability into between-group and within-group components, represented by sum of squares between groups (SSB) and sum of squares within groups (SSW), respectively. The ratio of the mean square between groups (MSB) to the mean square within groups (MSW) is computed as the F-statistic. A higher F-statistic indicates a larger discrepancy between group means and is used as the score for each neuron.

Optimal Sparse Probing We train a cardinality-constrained support vector machine (SVM) with hinge-loss trained to provable optimality using the cutting planes technique as described in [17]. The selected coefficients are simply those selected by the classifier.

Adaptive Thresholding Starting from $k = d_{mlp}$ (or some large k on a filtered set of neurons from a different heuristic), we train a series of logistic regression probes with elasticnet regularization (that is combined l_1 and l_2 regularization). Given a schedule for reducing k , at each step t , we take the $k_t < k_{t-1}$ neurons with highest absolute coefficient magnitude and retrain a logistic regression probe on these neurons. This process enables us to sweep through many values of k while leveraging past computation to achieve better feature selection.

B.4 Experimental Procedure

Here we provide additional details on the experimental procedure regarding both the feature selection experiments and the sparsity with scale experiments within Section 4.

Perhaps most significantly, for all experiments we preceded probe training with a heuristic filtering step, where we only trained probes on the top 1024 neurons, as judged by mean difference, for each combination of layer, feature, and model. This was done for computational reasons, as computing the mutual information, training dense probes, and optimal sparse probing methods are very expensive to run on hundreds of features for many layers containing in excess of 10,000 neurons. For optimal sparse probing, we only used the top 50, and set a timeout of 60 seconds.

All classifiers were trained with balanced class weights to account for class imbalances in the dataset. Finally, we selected hyperparameters using a small subset of feature and model combinations, and then used the best performing hyperparameters for all other experiments, as doing separate tuning for every trial would be too computationally expensive.

Method	Sparsity								Runtime (s)
	1	2	3	4	5	6	7	8	
Random	0.573	0.629	0.663	0.690	0.712	0.729	0.743	0.755	0.257
MMD	0.832	0.857	0.867	0.874	0.880	0.884	0.887	0.890	0.292
FS	0.832	0.856	0.867	0.874	0.880	0.884	0.887	0.890	0.303
LR	0.818	0.853	0.871	0.882	0.890	0.897	0.902	0.906	7.796
MI	0.831	0.851	0.863	0.869	0.876	0.880	0.884	0.886	32.241
OSP	0.831	0.861	0.876	0.884	0.891	0.896	0.899	0.902	53.028

Table 4: Comparison of sparse feature selection methods. Results are for the out-of-sample F1 score averaged for the best scoring layer for each combination of model and feature.

B.5 Feature Selection Results

For each combination of model, feature, and layer described above, we train a sparse probe for values of $k = 1, \dots, 8$ using the features selected by the aforementioned subset selection methods. In Table 4, we report the out-of-sample F1 score of each method averaged across models and features, and for the maximum across layers since features tend to be only represented in specific layers.

While our results are averaging over many trials, several points stand out. The top methods are always within 1% of each other, with no method strictly dominating the others. Although OSP comes with optimality guarantees, we set a one minute timeout, which is frequently reached especially for larger values of k . Moreover, this provable optimality is with respect to the specific level of l_2 regularization which often needs to be turned fairly high to speed up convergence [17]. Nevertheless, it is impressive that such fast and simple heuristics as the mean difference are comparable to far more sophisticated approaches, with even random neurons containing substantial information of the target task. This suggests that perhaps the best design is a two-stage approach where very fast heuristics are used to find relevant neurons and layers, and optimal methods are used to improve and verify the solution.

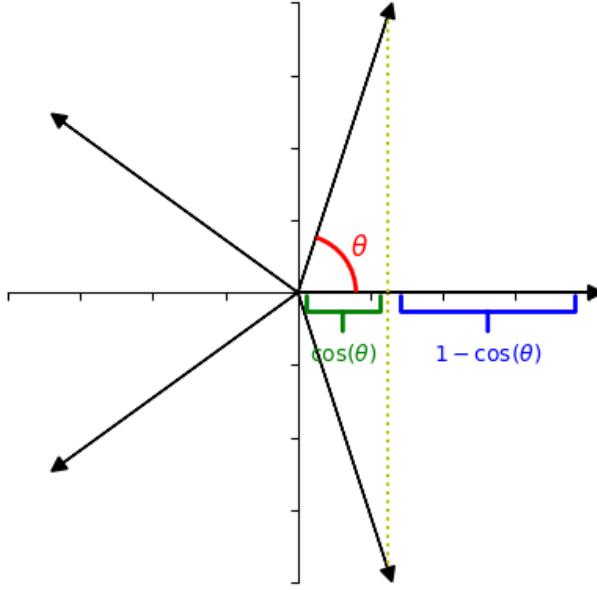


Figure 6: Superposition intuition for representing 5 features in 2 dimensions.

C Superposition Construction

Consider a set of n binary and mutually exclusive features (i.e., one-hot vectors like n -grams), that we want to embed in two dimensions, and later losslessly recover. Specifically, given a one hot vector $x \in \mathbb{R}^n$, we seek a $W \in \mathbb{R}^{n \times 2}$ such that

$$x = \text{ReLU}(WW^T x + b)$$

where $\text{ReLU}(x) = \max(x, 0)$. By embedding each point to be equally spaced around a circle of radius α (i.e., $w_i = \alpha \cos(2\pi i/n), \alpha \sin(2\pi i/n)$), we get that

$$(WW^T e_i)_j = \alpha^2 \cos\left(2\pi \frac{|i-j|}{n}\right)$$

where $\alpha = \|w_i\|_2$. To recover the initial one-hot representation, we require

$$\alpha^2 \left(1 - \cos\left(\frac{2\pi}{n}\right)\right) = 1 \quad \text{and} \quad b = -\alpha^2 \cos\left(\frac{2\pi}{n}\right)$$

Analyzing our proxy metric, $b\|w\|_2 = \frac{\cos(2\pi/n)}{(\cos(2\pi/n)-1)}$ monotonically decreases for n with $n > 2$.

Note that this construction refers to residual stream superposition and *not* neuron superposition since we are assuming we have exactly as many neurons as features. However, we expect the same basic motif to clean up interference to hold for the case with fewer neurons than features. Moreover, it is plausible increased levels of residual stream superposition is associated with increased levels of neuron superposition. Hence we believe this construction, and therefore the presence of large weight norms and negative biases, to be suggestive evidence of neuron superposition.

See [4] for a far more extensive set of experiments and results on related topics.

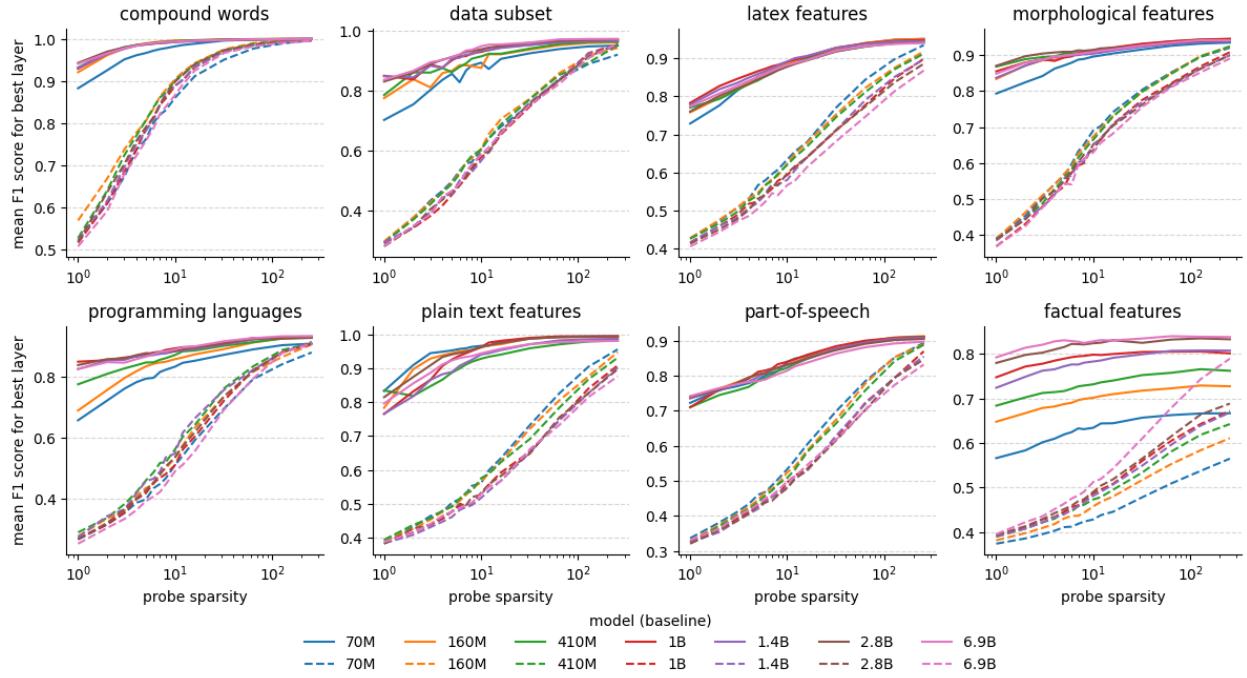


Figure 7: Difference between a k -sparse classifier using sparse features selection versus a random baseline. Specifically, the F1 score of training a classifier with k coefficients on the full $n \times d$ activation dataset when multiplied by a random $d \times k$ orthogonal matrix.

D Additional Results

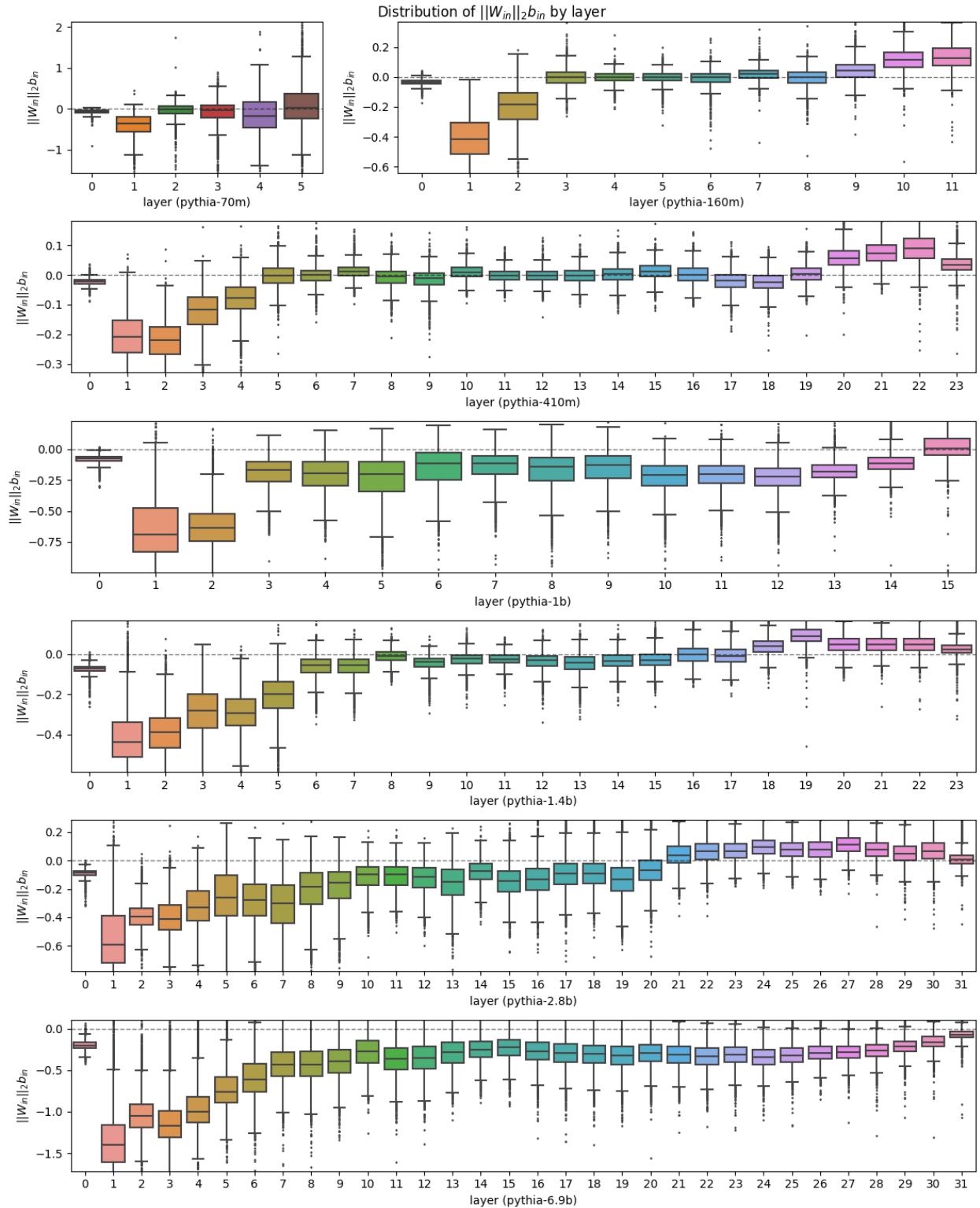


Figure 8: Distribution of input weight norms and biases for all Pythia models studied.

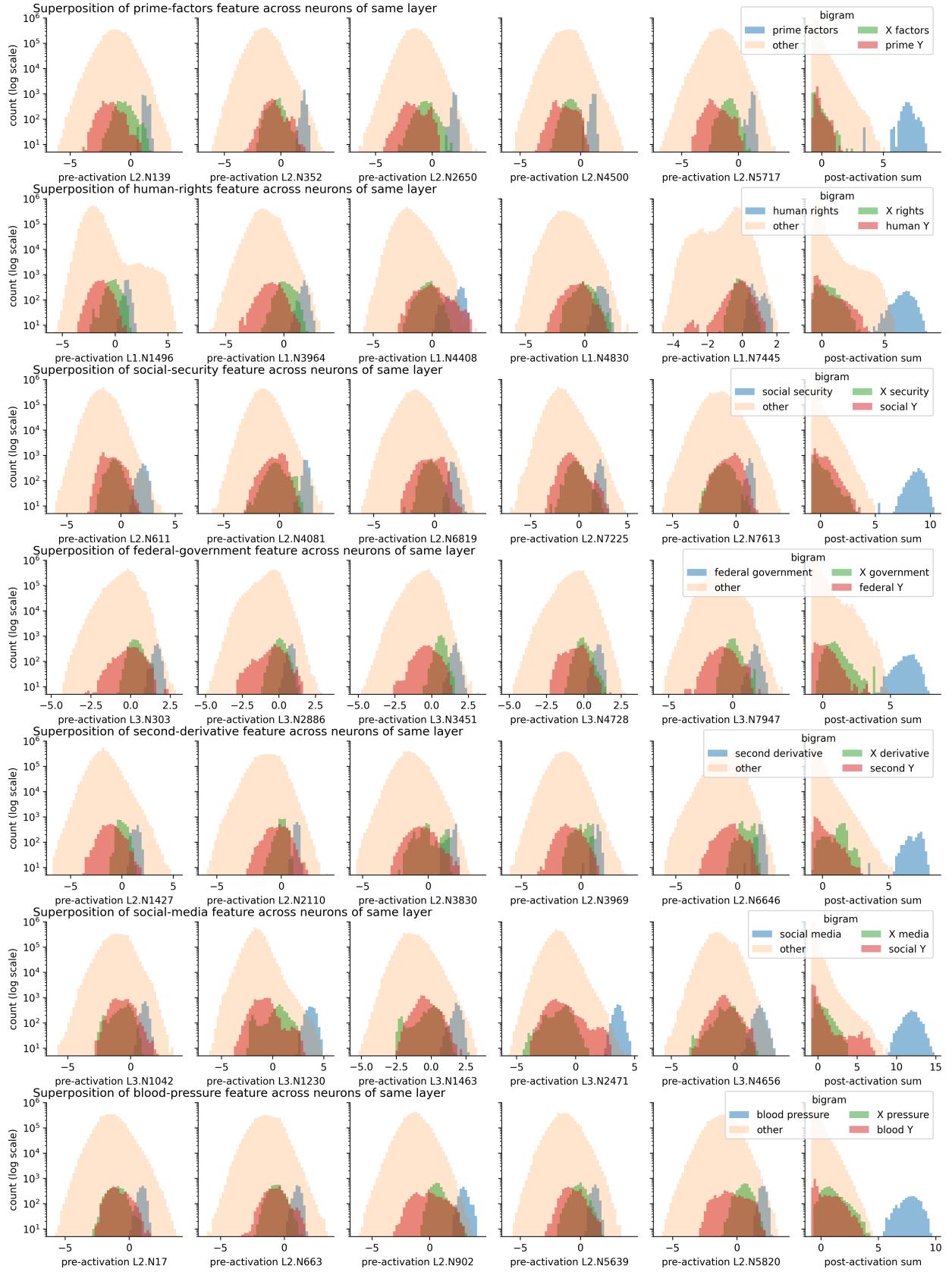


Figure 9: More examples of superposition of compound words in Pythia-1B

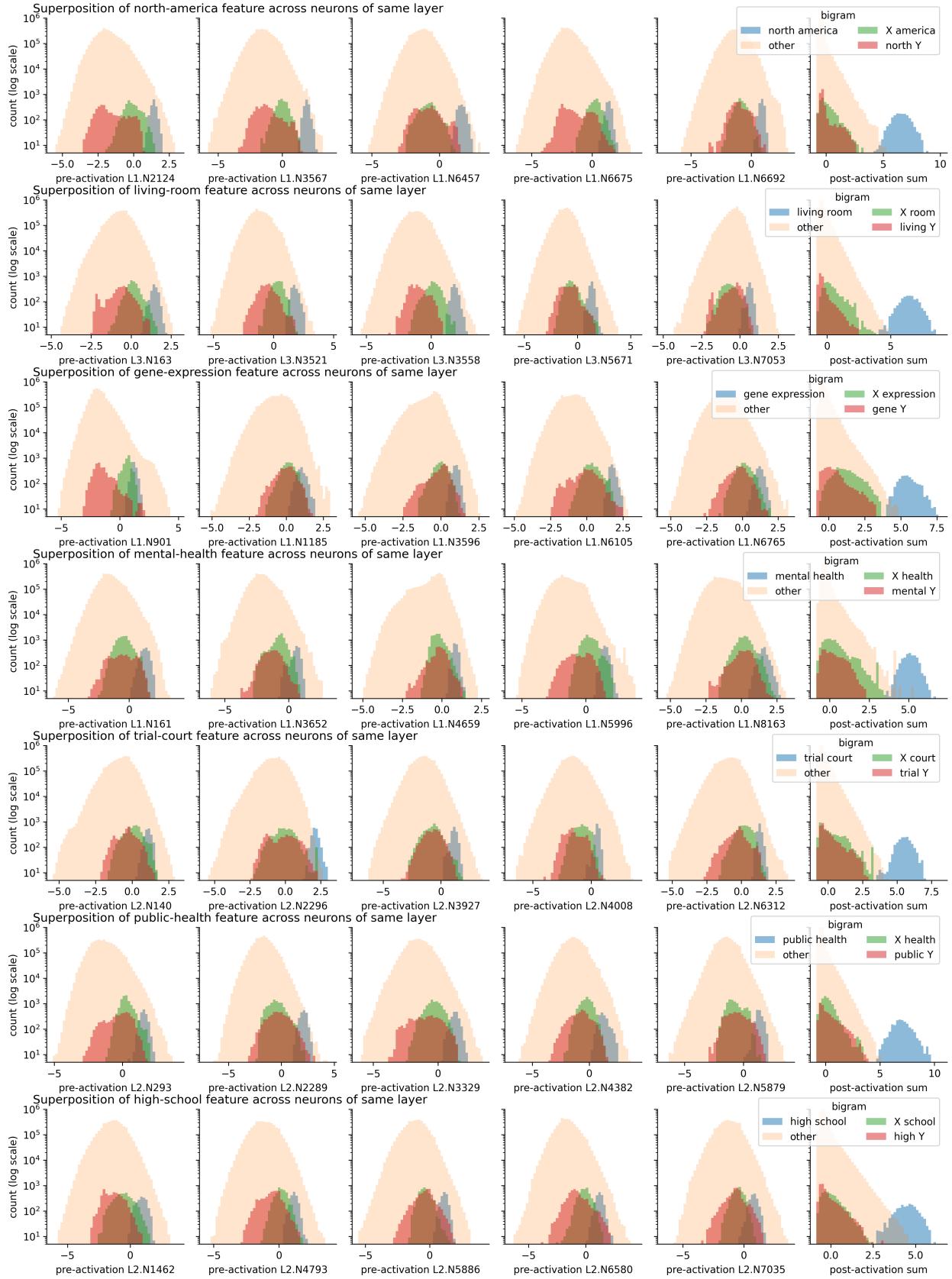


Figure 10: More examples of superposition of compound words in Pythia-1B

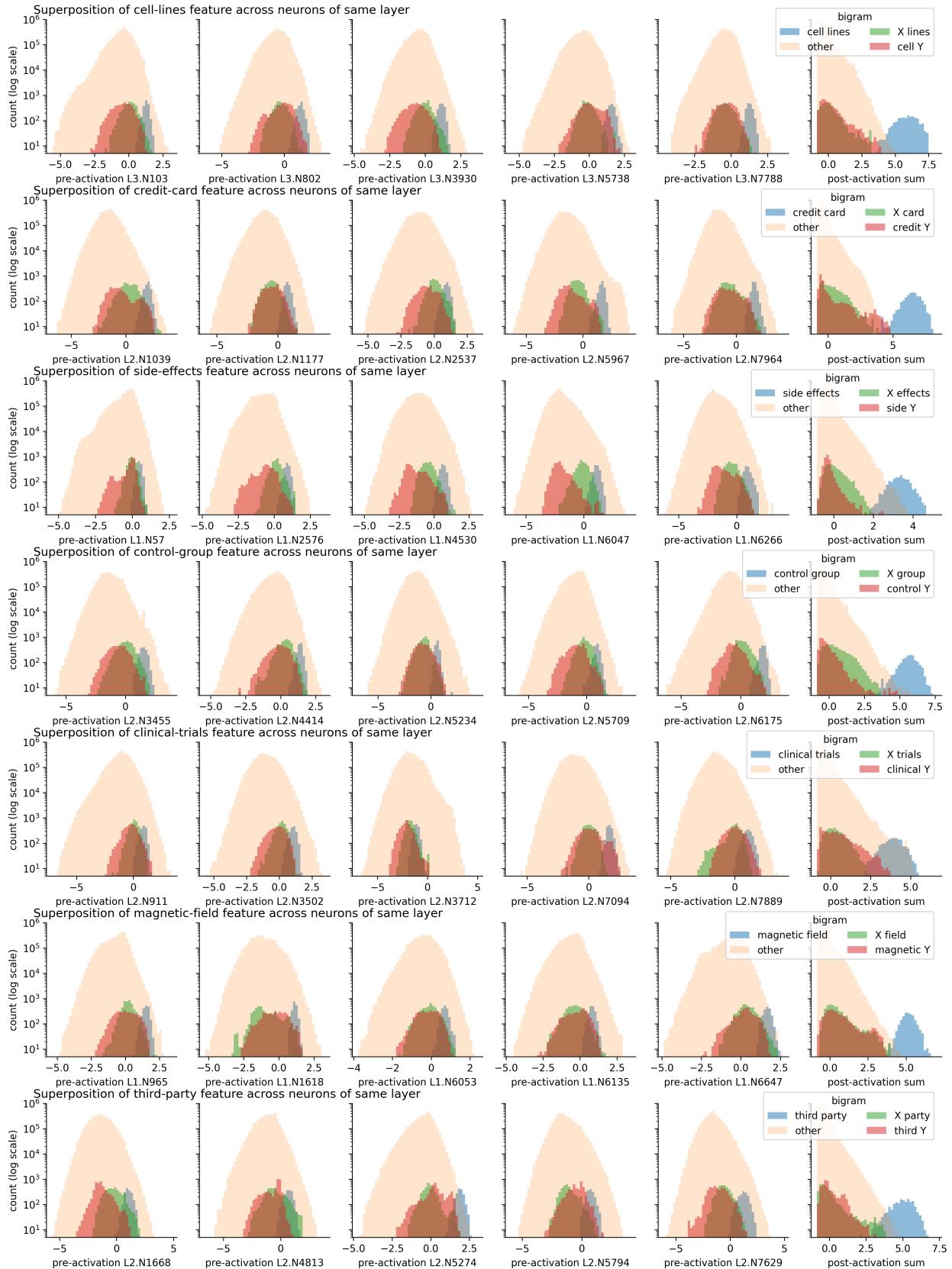


Figure 11: More examples of superposition of compound words in Pythia-1B

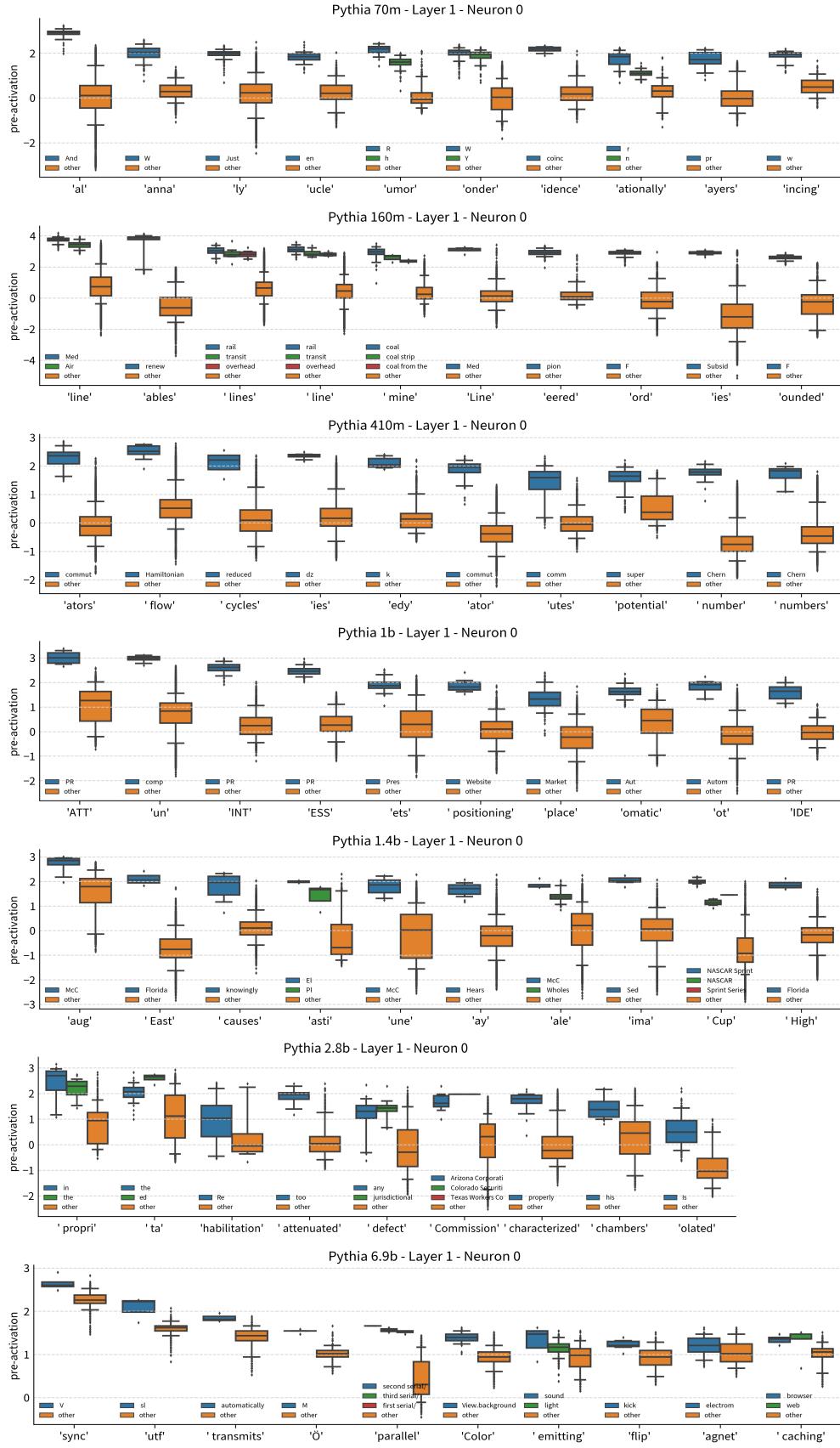


Figure 12: More examples of n -gram polysemy in layer 1 neuron 0 of all Pythia models studied.

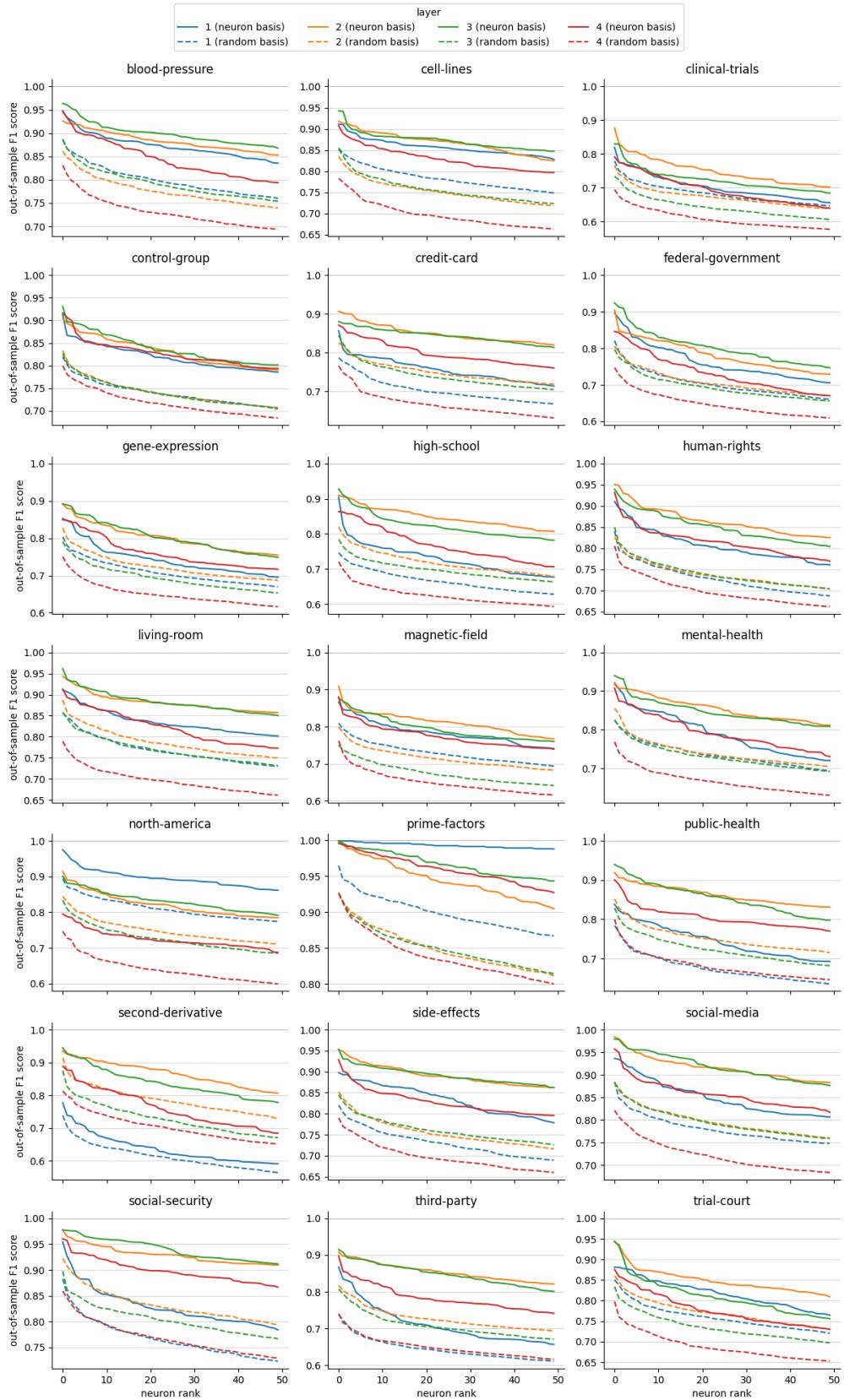


Figure 13: Demonstration of neuron basis alignment in early layers of Pythia-1B. Compares the compound-word classification performance of the top 50 neurons for layers 1-4 in the standard neuron basis, as opposed to a random basis (the post-activation dataset multiplied by a random Gaussian $d \times d$ matrix).

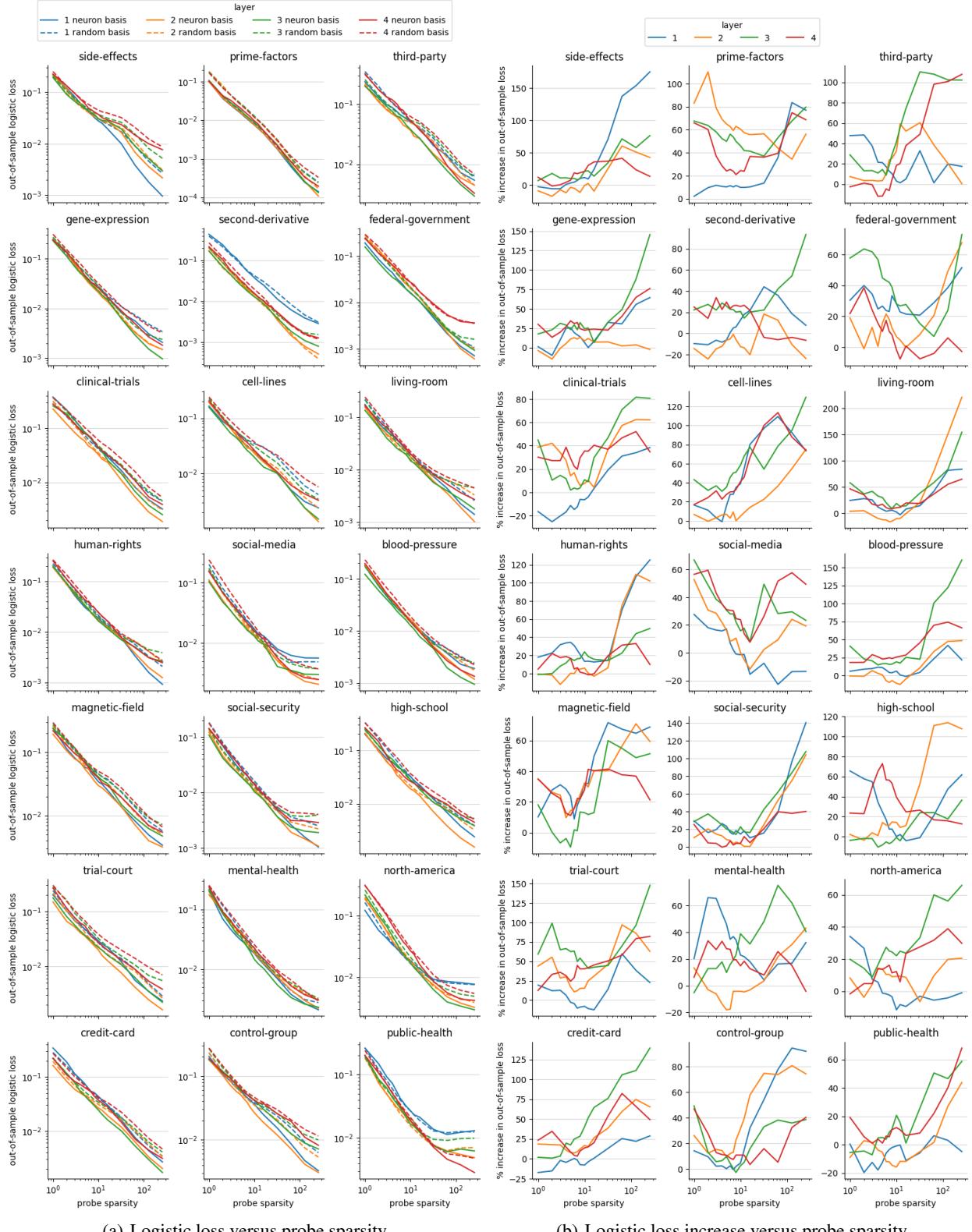


Figure 14: Logistic loss for classifying the occurrence of a particular compound word in layers 1-4 of Pythia-1B (in both the neuron basis and the average of random bases) undergo power law scaling until hitting a break point (left). In general, probes in the neuron basis achieve lower overall loss, further suggesting the neuron basis is meaningful (right).

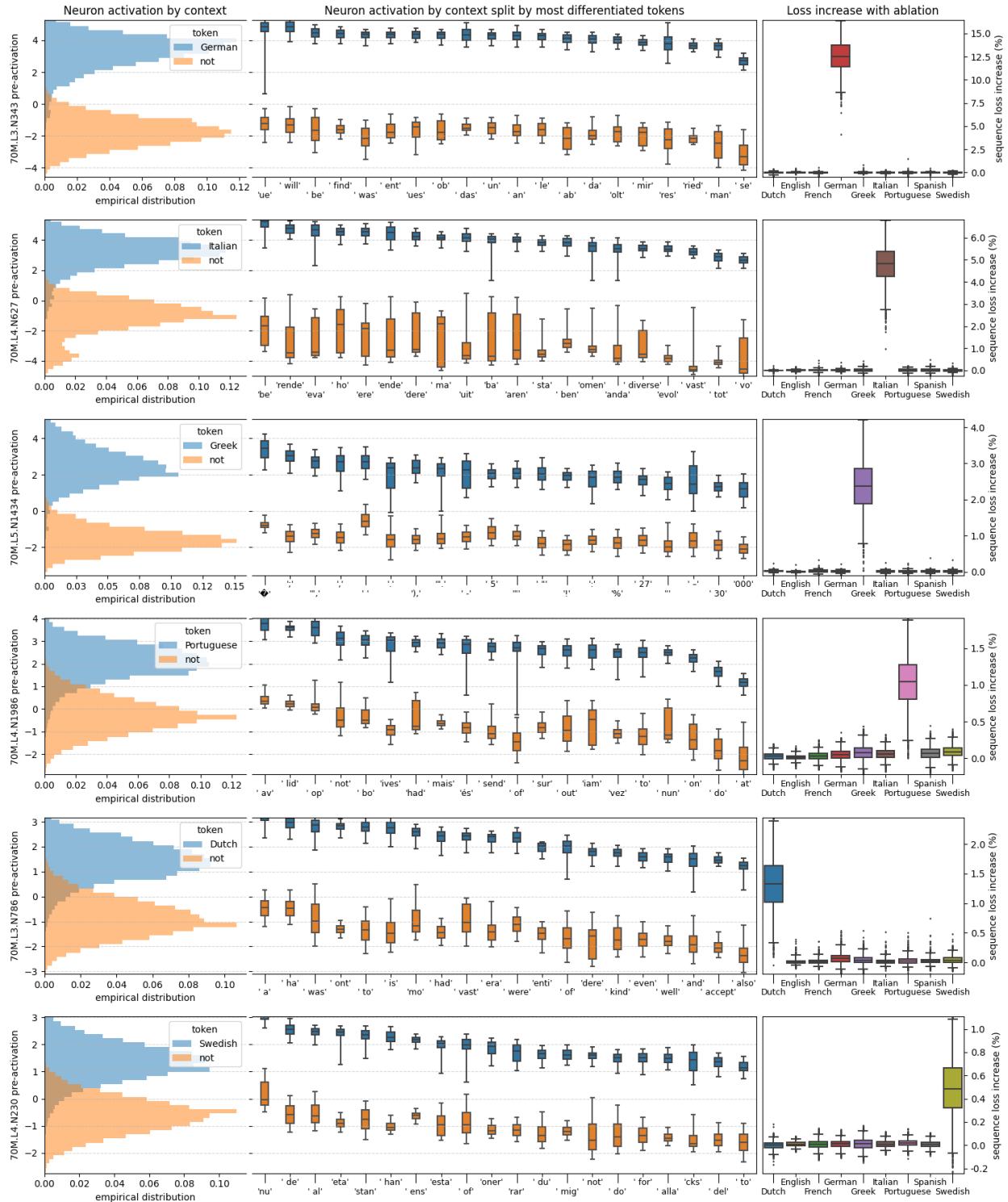


Figure 15: Monosemantic language context neurons in Pythia-70M.

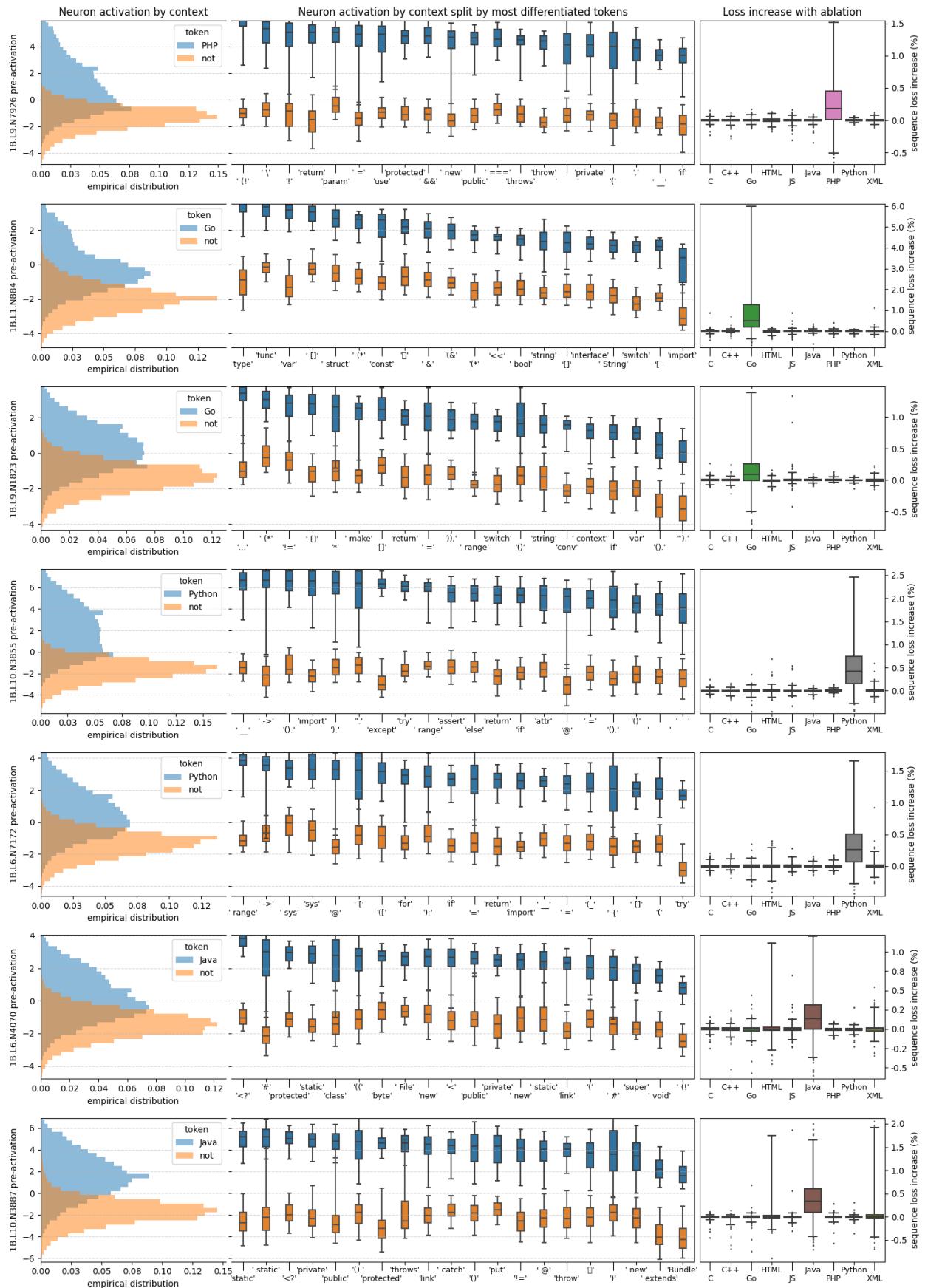


Figure 16: Monosemantic code context neurons in Pythia-1B.

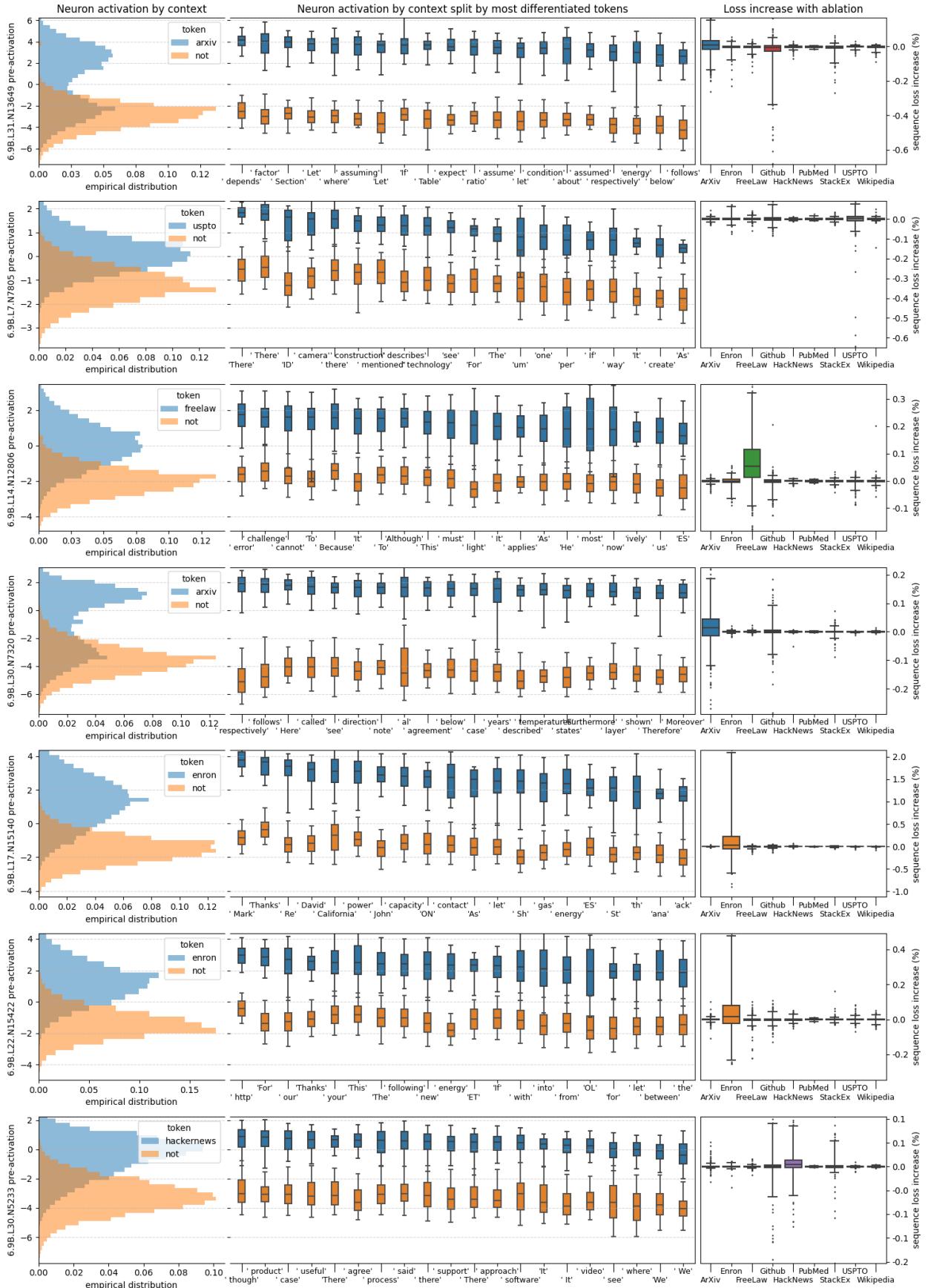


Figure 17: Monosemantic distribution identification context neurons in Pythia-6.9B.

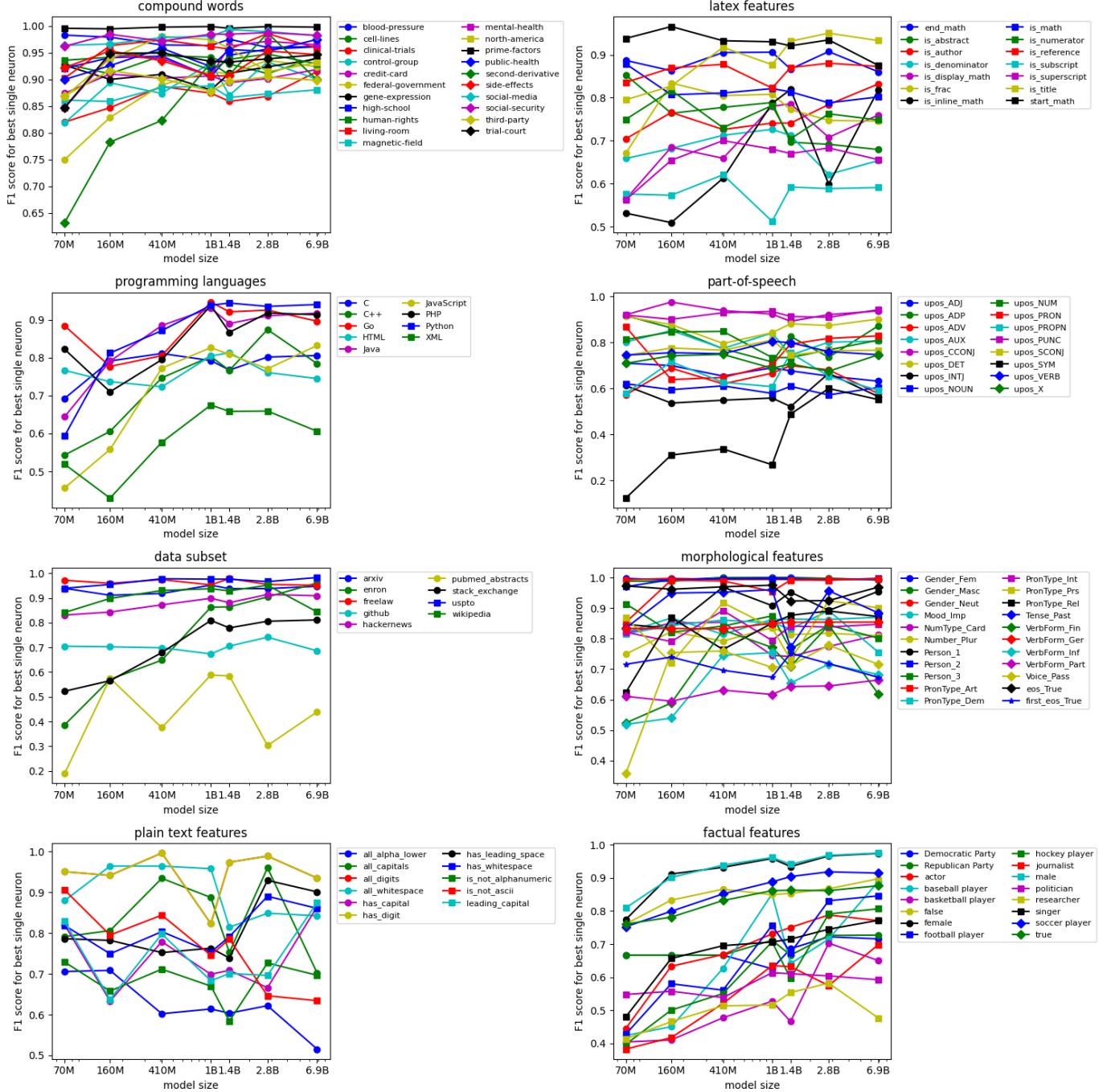


Figure 18: The single neuron with highest F1 classification performance for each feature by model size.

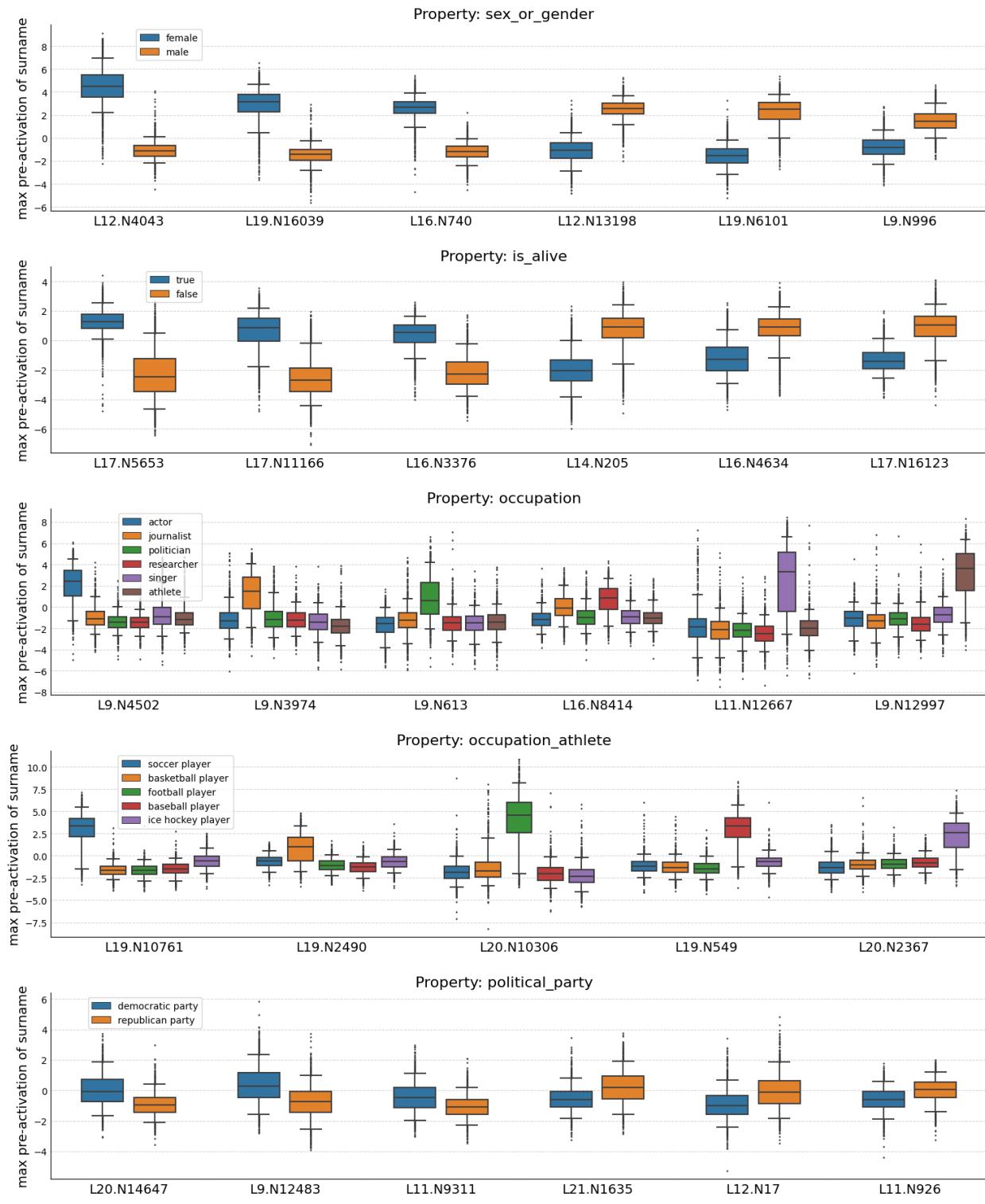


Figure 19: Top neurons in Pythia-6.9B for each category of factual neuron.

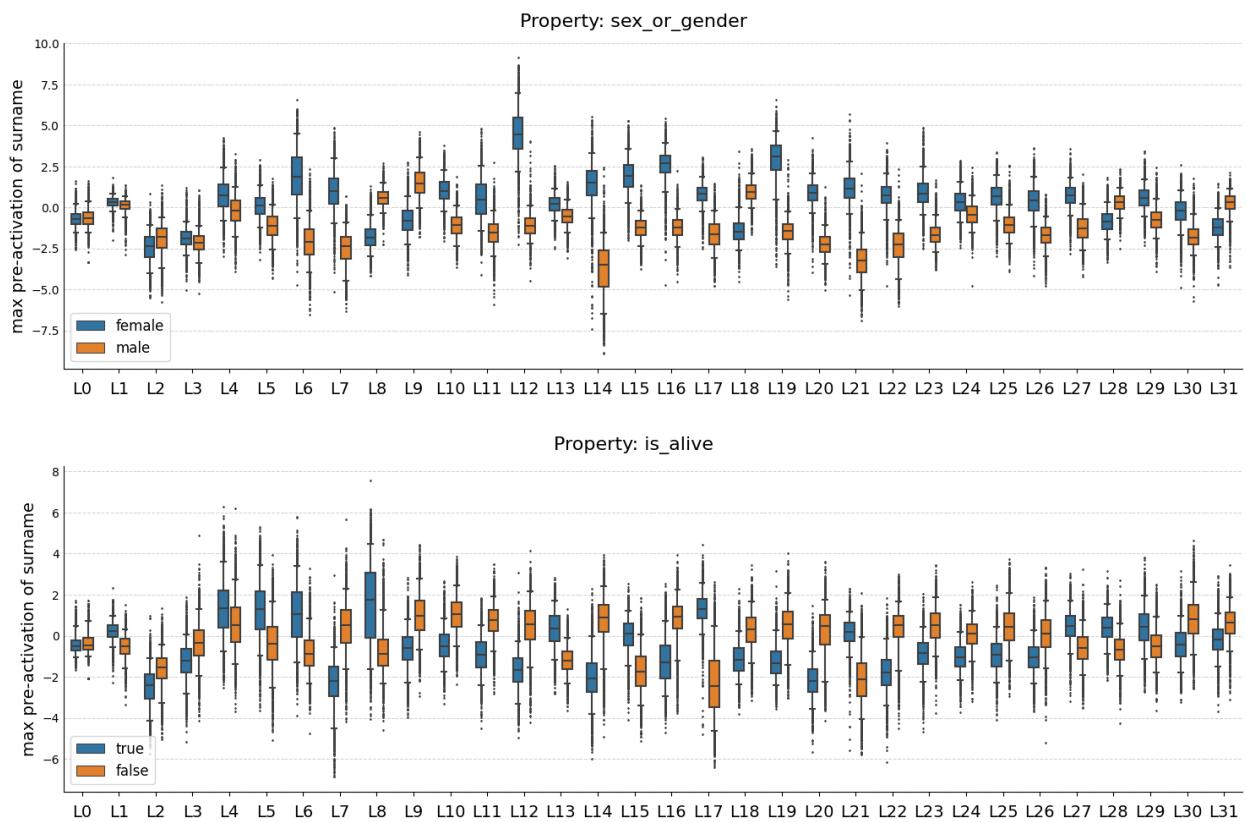


Figure 20: Top neuron for each layer in Pythia-6.9B for the `sex_or_gender` and `is_alive` feature categories.