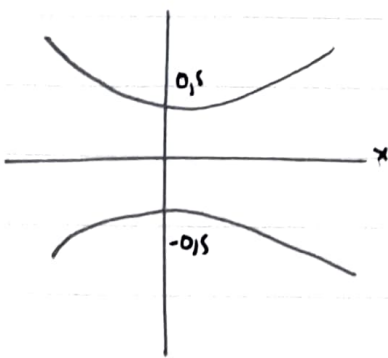


## Pop Quiz B

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① a.  $1 = 4y^2 - x^2$

$\rightarrow 1 = \frac{y^2}{\frac{1}{4}} - \frac{x^2}{1} \rightarrow \text{hiperbola}$



② ①.  $\lim_{(x,y) \rightarrow (0,0)} \frac{e^x - e^y}{e^x + e^y} = \frac{e^0 - e^0}{e^0 + e^0} = \frac{0}{1} = 0$

③  $D_u f(x,y) = \langle 2x \ln y + y^2, \frac{x^2}{y} + 2xy \rangle \cdot \frac{1}{\sqrt{2}} [1, 1]$   
 $= \frac{2x \ln y + y^2}{\sqrt{2}} + \frac{x^2 + 2xy^2}{y\sqrt{2}}$

~~$D_u f(x,y)$~~   $D_u f(-1, 2) = \frac{-2 \ln(2) + 4}{\sqrt{2}} + \frac{-7}{2\sqrt{2}}$

④ ①. bidang singgung

$z - z_0 = f_x(x_0, y_0)(x - x_0) + f_y(x_0, y_0)(y - y_0)$

$f_x(x,y) = 3x^2 \sin y + \frac{-\cos 2y}{x^2}$ ,  $f_y(x,y) = x^3 \cos y + \frac{2 \sin 2y}{x}$

$f_x(\frac{1}{2}, \pi) = -4$ ,  $f_y(\frac{1}{2}, \pi) = \frac{1}{8} \cdot -1 = -\frac{1}{8}$

$$z_1 = f\left(\frac{1}{2}, \pi\right) = \frac{1}{8} \cdot 0 + 2 = 2$$

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$$z - 2 = \left(x - \frac{1}{2}\right)(-4) + \left(-\frac{1}{8}\right)(y - \pi)$$

$$(5) (a) \quad \frac{dw}{dt} = \frac{dw}{dx} \frac{dx}{dt} + \frac{dw}{dy} \frac{dy}{dt} + \frac{dw}{dz} \frac{dz}{dt}$$

$$\frac{dw}{dx} = e^{\frac{\sqrt{y}}{x}} \quad \frac{dy}{dz} = x e^{\frac{\sqrt{y}}{x}} \cdot \frac{1}{2\sqrt{y}z} \quad \frac{dz}{dt} = x e^{\frac{\sqrt{y}}{x}} \cdot \frac{\sqrt{y}}{z^2}$$

$$\frac{dx}{dt} = \frac{1}{2\sqrt{t}} \quad \frac{dy}{dt} = \ln t + 1 \quad \frac{dz}{dt} = \cos t^2 \cdot 2t$$

$$\frac{dw}{dt} = \frac{e^{\frac{\sqrt{y}}{x}}}{2x} + \frac{x e^{\frac{\sqrt{y}}{x}} (\ln t + 1)}{2x\sqrt{y}(\ln t + 1)} + \frac{x e^{\frac{\sqrt{y}}{x}} (-\sqrt{y}) \cdot \cos t^2 \cdot 2t}{z^2}$$