

SOAL:

BAGIAN A (12.1)

⑤. Domain $f(x,y) = \sqrt{xy}$

maka $f: \mathbb{R} \rightarrow \mathbb{R}^+ \cup \{0\}$ domain $0 \leq xy < \infty$

atau $[0, \infty) \ni xy$

BAGIAN B (12.2)

⑨

$$f(x,y) = \frac{x}{(x+y)^2} = \frac{x}{x^2 + y^2 + 2xy} = x \cdot (x+y)^{-2}$$

division rule $\frac{d}{dx} \frac{u}{v} = \frac{u'v - v'u}{v^2}$

$$\frac{dF}{dx} = F_x(x,y) = \frac{(x+y)^2 - 2(x+y) \cdot x}{(x+y)^4} = \frac{x+y - 2x}{(x+y)^3} = \frac{y-x}{(x+y)^3}$$

$$\frac{dF}{dy} = F_y(x,y) = -2x \cdot (x+y)^{-3} = -\frac{2x}{(x+y)^3}$$

BAGIAN C (12.3)

$$\begin{aligned} \textcircled{3} \lim_{(x,y) \rightarrow (1,0)} \ln\left(\frac{1+y^2}{x^2+xy}\right) &= \lim_{(x,y) \rightarrow (1,0)} \ln \frac{1}{x} + \lim_{(x,y) \rightarrow (1,0)} \ln\left(\frac{1+y^2}{1+y}\right) \\ &= \lim_{(x,y) \rightarrow (1,0)} \ln \frac{1}{x} + \ln(1) \\ &= 0 \end{aligned}$$

BAGIAN D (12.4)

$$\textcircled{4} \nabla f(p) = f_x(p)i + f_y(p)j, \quad f(x,y) = \sin^2(x^2y)$$

$$\nabla f = \langle 3\sin^2(x^2y)\cos(x^2y)2xy, 3\sin^2(x^2y)\cos(x^2y)x^2 \rangle$$

BAGIAN E (12.5)

$$\textcircled{3} \nabla g(p,q) = \langle 4p^3 - 2q^3p, 3p^2q^2 \rangle$$

$$\nabla g(2,1) = \langle 28, 12 \rangle$$

$$v = \langle 1, 3 \rangle$$

$$D_v \nabla f(2,1) = 28 + 36 = 64 \quad \square$$

BAGIAN F (12.6)

$$\textcircled{3} \frac{dz}{dt} = \frac{dz}{dx} \cdot \frac{dx}{dt} + \frac{dz}{dy} \cdot \frac{dy}{dt}, \quad z = \arctan\left(\frac{y}{x}\right)$$

$$\frac{dz}{dx} = -\frac{y}{x^2+y^2}, \quad \frac{dz}{dy} = \frac{x}{y^2+x^2}$$

$$\frac{dx}{dt} = e^t, \quad \frac{dy}{dt} = e^t$$

$$\frac{dz}{dt} = \frac{xe^t}{y^2+x^2} - \frac{ye^t}{x^2+y^2} = \frac{x^2 - y^2}{x^2+y^2} \quad \square$$

BAGIAN G (12.7)

$$\textcircled{4} \text{ } F_x(x,y,z) = e^{xy} + xye^{xy}, \quad F_y(x,y,z) = x^2e^{xy}, \quad F_z = 0$$

$$\text{bidang singgung} \Rightarrow (z-2) \cdot 0 = (x-2) + 4(y)$$

$$\text{titik } (2,0,2) \quad 0 = 4y + x - 2 \quad \square$$