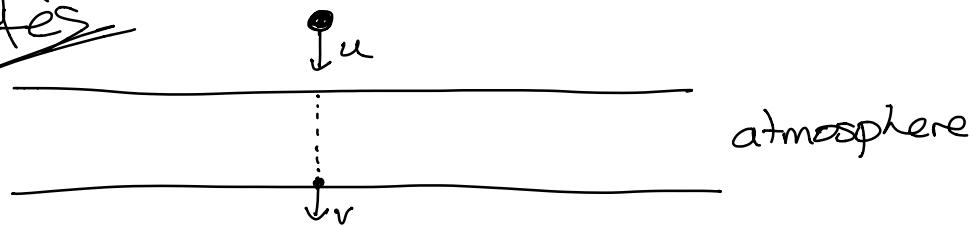


Rough Notes



FBD



$$F_{\text{net}} = \underbrace{F_g}_{mg} - \underbrace{F_a}_{kv^2} = ma.$$

Simplist case  $\rightarrow$  assume  $g$  is constant  
 $\rightarrow$  assume  $P, T$  etc atm- constant

$$\text{Drag equation: } F_a = C_d \rho \frac{v^2 A}{2}$$

$$F_a = -kv^2$$

+↓

$$\therefore mg - kv^2 = ma$$

$$mg - kv^2 = m \frac{dv}{dt}$$

$$\frac{dv}{dt} = g - \frac{k}{m} v^2$$

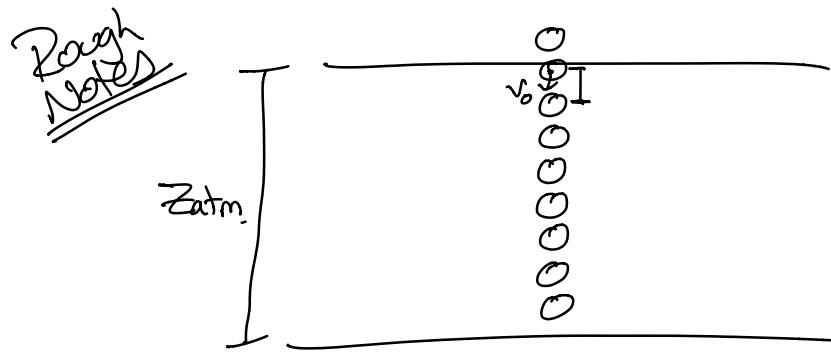
differential equation:

$$\frac{dv}{dt} = g - \frac{C_d \rho A}{2m} v^2$$

$$a = \frac{\Delta v}{\Delta t}$$

① Differentiation

② ~~Numerical integration~~



$$\Delta r = \left[ g - \left( \frac{C_d \rho A}{\sum m} \right) v^2 \right] \Delta t.$$

$$\Delta z = v \Delta t$$

$$\text{at } t=0 \quad z=0 \quad u=v$$

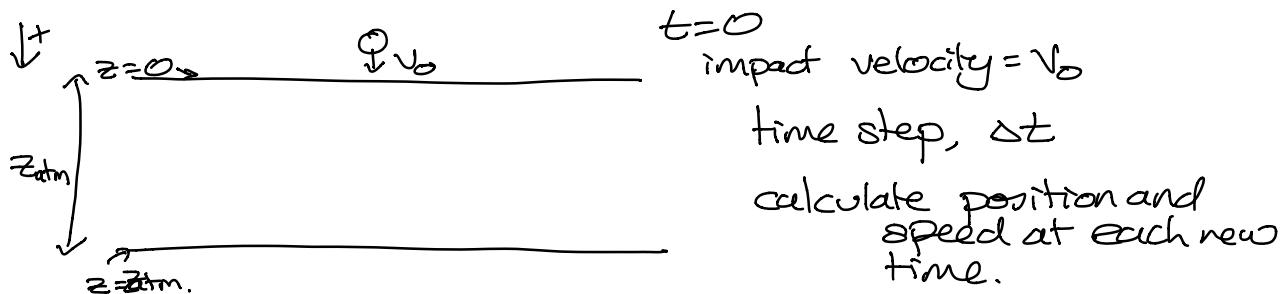
$$\text{at } t=\Delta t \quad z_1 = z_0 + v_0 \Delta t$$

$$v_1 = v_0 + \left[ g - \frac{C_d \rho A}{\sum m} v_0^2 \right] \Delta t$$

loop until  $z = z_{\text{atmosphere}}$ .

## Meteorite shooting through the atmosphere.

- Start  $\rightarrow$  asteroid velocity perpendicular to Earth's surface
- $\rightarrow$  constant density atmosphere of a given thickness
- $\rightarrow$  assume acceleration due to gravity is constant
- $\rightarrow$  assume asteroid size and mass constant
- $\rightarrow$  assume drag coefficient is constant



$$\text{Forces: grav: } F_g = mg \quad \downarrow \therefore +\text{ve.}$$

$$\text{air resistance: } F_d = \frac{C_d \rho A}{2} v^2 \quad \uparrow \therefore -\text{ve.}$$

$$F_{\text{net}} = mg - \frac{C_d \rho A}{2} v^2$$

$$\text{N}^{\circ}\text{l}'s 2^{\text{nd}}: ma = mg - \frac{C_d \rho A}{2} v^2$$

$$a = \frac{\Delta v}{\Delta t} \quad \frac{d}{dt} \frac{\Delta v}{\Delta t} = mg - \frac{C_d \rho A}{2m} v^2$$

$$\Delta v = \left( g - \frac{C_d \rho A}{2m} v^2 \right) \Delta t$$

Position  $\rightarrow$  assume <sup>close enough</sup> constant acceleration within  $\Delta t$

$$\text{const. ac. eq: } s = ut + \frac{1}{2}at^2$$

$$\Delta z = v \Delta t + \frac{1}{2} \left( g - \frac{C_d \rho A}{2m} v^2 \right) \Delta t^2$$

## Base Simulation:

Initial cond:  $v = v_0$   
 $z = z_0$   
 $t = 0$

end when  $z > z_{\text{atm}}$ .

$$z_1 = z_0 + \Delta z$$

$$z_1 = z_0 + v_0 \Delta t + \frac{1}{2} \left( g - \frac{C_D \rho A}{2m} v_0^2 \right) \Delta t^2.$$

$$v_1 = v_0 + \Delta v$$

$$v_1 = v_0 + \left( g - \frac{C_D \rho A}{2m} v_0^2 \right) \Delta t$$

output  $\Rightarrow$  final  $v$ .

Possible variations:

- initial speed
- $z_{\text{atm}}$
- $\rightarrow \rho$  (or  $\rho(z)$ )
- $\rightarrow g$  (or  $g(z)$ )
- $\rightarrow C_D$
- $\rightarrow m$
- $\rightarrow A$

] $\rightarrow$  think about ablation  $\rightarrow$  how asteroid "burns up" through atmosphere,

Concerns  $\rightarrow$  error analysis needed \*

Alec research: Find initial values to use:

asteroid:  $v_0, m, A$

atmosphere:  $z_{\text{atm}}, \rho \leftarrow$  constant density model,  
 $g = 9.81 \text{ ms}^{-2}$

drag coefficient ??

Things to explore:

- atmosphere models - const. den, isothermal, adiabatic, real ....
- $g$  as a function of position  $\leftarrow$  is it worth it?
- asteroid impacts  $\rightarrow$  initial vel & asteroid properties.

June 11<sup>th</sup>

→ Base simulation good

- add radius as variable ← will be changing in loop
- recalculate  $k$  within <sup>while</sup> loop
- also plot  $\sqrt{t}$

→ Complications:

① Add  $g$  as dependant on  $z$ .

$$g = \frac{F}{m} = \frac{GM}{R^2} \quad \begin{array}{l} \rightarrow \text{radius of Earth} = R_{\text{Earth}} \\ \rightarrow R = R_{\text{Earth}} + z \end{array}$$

\* Switch  $z = \text{altitude}$

- start as  $z = \text{thickness}$
- loop becomes  $z > 0$
- $z = \dots$

\* Acceleration =  $\frac{GM_{\text{Earth}}}{R^2}$  ← while in loop

→ print acceleration → check when  $z=0$   $acc = 9.81$   
 $z > 0$   $acc < 9.81$   
(expect  $acc \approx 9.6$  at top)

② Ablation of meteorites \*

→ look into how people do this  
e.g. model as pure iron

In while loop:

- calculate change in GPE
- change in KE

→ Find thermal energy  $Q = \Delta E_p - \Delta E_k$

easier way?  
 $Q \rightarrow \text{mass loss}$

$$\rightarrow \text{use } Q = \underbrace{mc\Delta T + mL}_{n}$$

the thermal energy will heat and sublime (?)

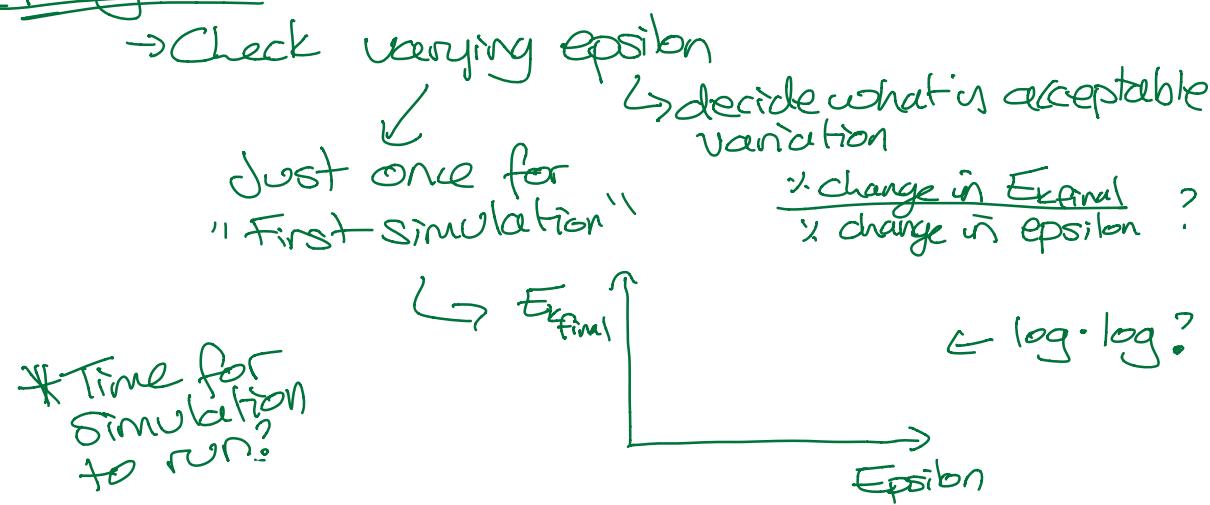
$\rightarrow$  find a mass loss each step  
 $\rightarrow$  recalculate radius  
 MASS  
 K  
 etc...  
 $\therefore$  First simulation (w/ g & ablation)

Then the actual investigation:

Vary:  
 - Initial radius  
 - Initial speed  
 - density ] kinetic energy at top of atmosphere.

Dependant  $\rightarrow$  kinetic energy of meteorite immediately before impact.

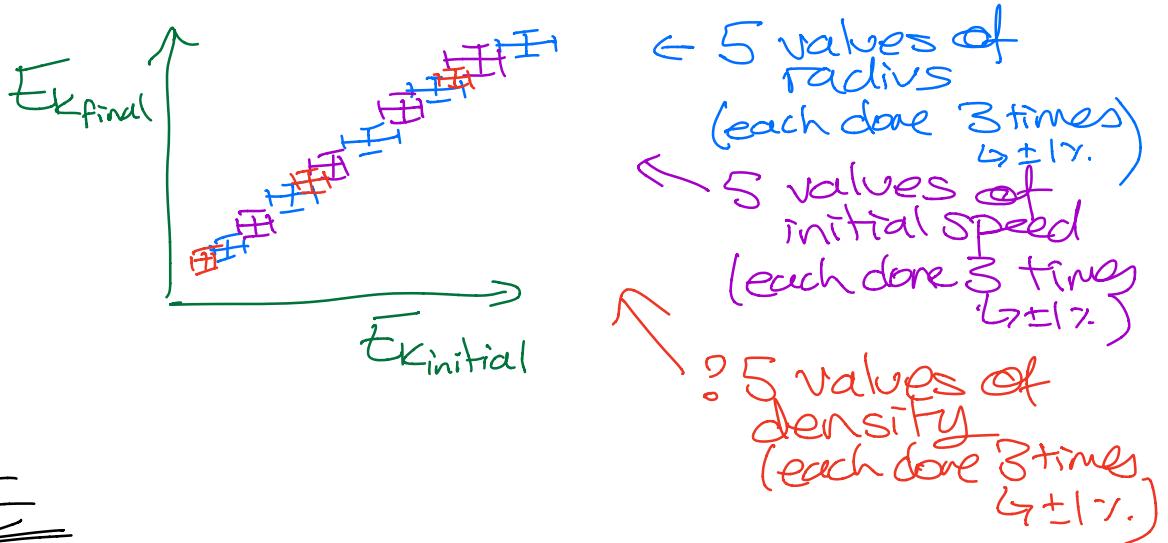
## Analysis.



\* Trying to get to error bars?

\* Alternative  $\rightarrow$  When running do 3 sims for each

$\left[ \begin{array}{l} \rightarrow +1\% \text{ of IV} \\ \rightarrow -1\% \text{ of IV} \end{array} \right] \rightarrow$  find short on  $E_{\text{final}}$ .



EE

## Background/Intro

- \* Sudbury context ← Why we care about  $E_{k\text{final}}$
- \* Vocab - asteroid : meteorite : meteor

## Base simulation

- \* Math for  $z \neq v$
- \* Simulation ( $\leftarrow$  brief)  $\leftarrow$  time step  $\leftarrow$  loop ] samples of code?

## First simulation

- \* Math for ablation ]  $\Rightarrow$  samples of code

- \* Results  $\leftarrow$  compare to base.

## Investigation

- vary  $r, v, \rho$
- results

→ analysis

### Conclusion & evaluation

- What you found + why care
- What could be better
- further work.