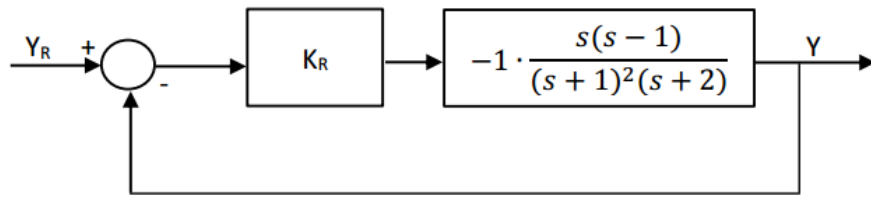


Za sistem prikazan na slici odrediti i predstaviti GMK ako je $K_R \leq 0$.



- **Prijenosna funkcija:**

$$G_o(s) = K \cdot \frac{s(s-1)}{(s+1)^2(s+2)}$$

-I KORAK :

$m=2$ ($m \Rightarrow$ broj nula prijenosne funkcije) $s_{N1}=0 \Rightarrow$ prva nula $s_{N2}=1 \Rightarrow$ druga nula

$n=3$ ($n \Rightarrow$ broj polova prijenosne funkcije)

$s_{P1}=-1 \Rightarrow$ prvi pol $s_{P2}=-1 \Rightarrow$ drugi pol $s_{P3}=-2 \Rightarrow$ treći pol

-II KORAK:

$\sigma \in (-\infty, -2] \cup \{-1\} \cup [0, 1]$ \Rightarrow tačke na realnoj osi koje pripadaju krivulji mjesta korijena

-III KORAK:

$\sigma_a = \frac{1}{n-m} \{ \sum_{v=1}^n \text{Re}(s_{Pv}) - \sum_{\mu=1}^m \text{Re}(s_{N\mu}) \}$ \Rightarrow tačka presjeka asimptota

$$\sigma_a = \frac{1}{1} (-1 - 1 - 2 - (0 + 1)) = -5$$

-IV KORAK:

$\alpha_k = \frac{180(2k+1)}{n-m}, k = 1, 2, \dots, n-m$ \Rightarrow ugao asimptote

$$\alpha_1 = \frac{180(2-1)}{1} = 180^\circ$$

-V KORAK :

$$\sum_{v=1}^n \frac{1}{s-s_{Pv}} = \sum_{\mu=1}^m \frac{1}{s-s_{N\mu}} \quad \Rightarrow \text{tačke grananja / tačke sjedinjenja}$$

$$\frac{1}{s} + \frac{1}{s-1} = \frac{1}{s+1} + \frac{1}{s+1} + \frac{1}{s+2}$$

$$(s^2 - 1)(s + 2) + (s^2 + s)(s + 2) = (2s^2 - 2s)(s + 2) + s(s^2 - 1)$$

$$s^3 + 2s^2 - s - 2 + s^3 + 2s^2 + s^2 + 2s = 2s^3 + 4s^2 - 2s^2 - 4s + s^3 - s$$

$$s^3 - 3s^2 - 6s + 2 = 0$$

$$s_1 = \sigma_{V1} = -1.5842 \quad \Rightarrow \text{ne pripada intervalu } (\sigma)$$

$$s_2 = \sigma_{V2} = 0.29428, \quad \Rightarrow \text{pripada intervalu - tačka sjedinjenja}$$

$$s_3 = \sigma_{V3} = 4.2899 \quad \Rightarrow \text{ne pripada intervalu } (\sigma)$$

-VI KORAK:

$$\varphi_{I,k}(s_{Pi}) = \frac{1}{r_{Pi}} \left(\sum_{\mu=1}^m < (s_{Pi} - s_{N\mu}) - \sum_{\substack{v=1 \\ v \neq i}}^n < (s_{Pi} - s_{N\mu}) + 180(2k - 1) \right), k = 1, \dots, r_{Pi}$$

$$\varphi_{U,k}(s_{Ni}) = \frac{1}{r_{Ni}} \left(\sum_{v=1}^n < (s_{Ni} - s_{Pv}) - \sum_{\substack{\mu=1 \\ \mu \neq i}}^m < (s_{Ni} - s_{Nv}) + 180(2k - 1) \right), k = 1, \dots, r_{Ni}$$

$$\varphi_{I,1}(s_{P1}) = \frac{1}{2} (180 + 180 - (0 + 0) + 180) = -90^\circ$$

$$\varphi_{I,2}(s_{P2}) = \frac{1}{2} (180 + 180 - (0 + 0) + 180 \cdot 3) = 90^\circ$$

$$\varphi_I(s_{P3}) = \frac{1}{1} (180 + 180 - (180 + 180) + 180) = 180^\circ$$

$$\varphi_U(s_{N1}) = \frac{1}{1} (0 + 0 + 0 - 180 + 180) = 0^\circ$$

$$\varphi_U(s_{N2}) = \frac{1}{1} (0 + 0 + 0 - 0 + 180) = 180^\circ$$

$$a_n=1$$

$$a_{n-1}=K+4$$

$$a_{n-2}=5-K$$

$$a_{n-3}=2$$

s^3	1	5-K
s^2	4+K	2
s^1	$-K^2 + K + 18$	0
s^0	0	0

$$4 + K = 0$$

$$K = -4$$

$$-K^2 + K + 18 = 0$$

$$K_1 = -3,77$$

$$K_2 = 4,77$$

$$W = \sqrt{\frac{2}{8,77}} = 0.47$$

```
G=tf([1 -1 0],[1 4 5 2]);
rlocus(G);
```

