

| M | Type | $X_p=(p-1)/2$ | $X_m=(M-1)/(2p)$ |
|------------|--------|------------------|--|
| 2^2-1 | | $0 = \{\}$ | $\{\}$ |
| 2^3-1 | $4k+3$ | $1 = \{\}$ | $\{\}$ |
| 2^5-1 | $4k+1$ | $2 = \{2\}$ | $\{3\}$ |
| 2^7-1 | $4k+3$ | $3 = \{3\}$ | $\{3^2\}$ |
| $2^{11}-1$ | $4k+3$ | $5 = \{5\}$ | $\{3*31\}$ |
| $2^{13}-1$ | $4k+1$ | $6 = \{2*3\}$ | $\{3^2*5*7\}$ |
| $2^{17}-1$ | $4k+1$ | $8 = \{2^3\}$ | $\{3*5*257\}$ |
| $2^{19}-1$ | $4k+3$ | $9 = \{3^2\}$ | $\{3^3*7*73\}$ |
| $2^{23}-1$ | $4k+3$ | $11 = \{11\}$ | $\{3*89*683\}$ |
| $2^{29}-1$ | $4k+1$ | $14 = \{2*7\}$ | $\{3*5*43*113*127\}$ |
| $2^{31}-1$ | $4k+3$ | $15 = \{3*5\}$ | $\{3^2*7*11*151*331\}$ |
| $2^{37}-1$ | $4k+1$ | $18 = \{2*3^2\}$ | $\{3^3*5*7*13*19*73*109\}$ |
| $2^{41}-1$ | $4k+1$ | $20 = \{2^2*5\}$ | $\{3*5^2*11*17*31*61681\}$ |
| $2^{43}-1$ | $4k+3$ | $21 = \{3*7\}$ | $\{3^2*7^2*127*337*5419\}$ |
| $2^{47}-1$ | $4k+3$ | $23 = \{23\}$ | $\{3*178481*2796203\}$ |
| $2^{53}-1$ | $4k+1$ | $26 = \{2*13\}$ | $\{3*5*157*1613*2731*8191\}$ |
| $2^{59}-1$ | $4k+3$ | $29 = \{29\}$ | $\{3*233*1103*2089*3033169\}$ |
| $2^{61}-1$ | $4k+1$ | $30 = \{2*3*5\}$ | $\{3^2*5^2*7*11*13*31*41*151*331*1321\}$ |
| $2^{67}-1$ | $4k+3$ | $33 = \{3*11\}$ | $\{3^2*7*23*89*683*20857*599479\}$ |

$$\begin{array}{l}
2^{71-1} \quad 4k+3 \quad 35 = \{5*7\} \quad \{3*11*31*43*127*281*86171*122921\} \\
\hline
2^{73-1} \quad 4k+1 \quad 36 = \{2^2*3^2\} \quad \{3^3*5*7*13*17*19*37*109*241*433*38737\} \\
\hline
2^{79-1} \quad 4k+3 \quad 39 = \{3*13\} \quad \{3^2*7*2731*8191*121369*22366891\} \\
\hline
2^{83-1} \quad 4k+3 \quad 41 = \{41\} \quad \{3*13367*164511353*8831418697\} \\
\hline
2^{89-1} \quad 4k+1 \quad 44 = \{2^2*11\} \quad \{3*5*17*23*353*397*683*2113*2931542417\} \\
\hline
2^{97-1} \quad 4k+1 \quad 48 = \{2^4*3\} \quad \{3^2*5*7*13*17*193*241*257*673*65537*22253377\} \\
\hline
2^{101-1} \quad 4k+1 \quad 50 = \{2*5^2\} \quad \{3*5^3*11*31*41*251*601*1801*4051*8101*268501\} \\
\hline
2^{103-1} \quad 4k+3 \quad 51 = \{3*17\} \quad \{3^2*7*307*2143*2857*6529*11119*43691*131071\} \\
\hline
2^{107-1} \quad 4k+3 \quad 53 = \{53\} \quad \{3*6361*69431*20394401*28059810762433\} \\
\hline
2^{109-1} \quad 4k+1 \quad 54 = \{2*3^3\} \quad \{3^4*5*7*13*19*37*73*87211*246241*262657*279073\} \\
\hline
2^{113-1} \quad 4k+1 \quad 56 = \{2^3*7\} \quad \{3*5*17*29*43*127*257*5153*15790321*54410972897\} \\
\hline
2^{127-1} \quad 4k+3 \quad 63 = \{3^2*7\} \quad \{3^3*7^2*19*43*73*337*5419*92737*649657*77158673929\} \\
\hline
2^{131-1} \quad 4k+3 \quad 65 = \{5*13\} \quad \{3*11*31*2731*8191*409891*7623851*145295143558111\} \\
\hline
2^{137-1} \quad 4k+1 \quad 68 = \{2^2*17\} \quad \{3*5*17^2*953*26317*43691*131071*354689*2879347902817\} \\
\hline
\end{array}$$