Yesterday - Tomorrow Data

Aldo Solari



Yesterday

- From AS, Chapter 3
- Yesterday we observed n = 30 observations

$$(x_1, y_1), (x_2, y_2), \ldots, (x_n, y_n)$$

These data are artificially generated by the model

$$Y = f(x) + error$$

where f(x) is a unspecified smooth and regular function

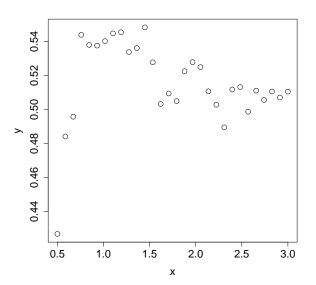
• We wish to obtain a model

$$\hat{y} = \hat{f}(x)$$

that allows us to predict y as new observations of x become available, say tomorrow



yesterday **data**





Mean squared error

• The MSE for the yesterday data (training data) is given by

$$MSE_{Tr} = \frac{1}{n} \sum_{i=1}^{n} [y_i - \hat{f}(x_i)]^2$$

We would like to have a good performance

$$MSE_{Te} = \frac{1}{m} \sum_{i=1}^{m} [y_i^* - \hat{f}(x_i^*)]^2$$

on tomorrow data (test data)

$$(x_1^*, y_1^*), (x_2^*, y_2^*), \dots, (x_m^*, y_m^*)$$

but y_1^*, \ldots, y_m^* are not available



Goal

- Training data: n = 30
- Test data: m = n with $x_i^* = x_i$ for i = 1, ..., 30
- You are not allowed to use the test data y_1^*, \ldots, y_{30}^*
- Restrict attention to polynomial regression models

$$Y = \beta_0 + \beta_1 X + \beta_2 X^2 + \ldots + \beta_d X^d + \varepsilon$$

for
$$d \in \{0, 1, ..., n-1\}$$

ullet Find the degree d that minimize $\mathbb{E}(\mathrm{MSE}_{\mathrm{Te}})$



```
# import data
load("yesterday.Rdata")
test = data.frame(x=train$x)
# plot training data
plot( y ~ x , train)
# 2nd-degree polynomial regression fit
fit <- lm( y ~ poly(x, degree=2), train)
yhat <- predict(fit, newdata=test)</pre>
lines( yhat ~x, train)
# MSE.tr
MSE.tr <- mean( (train$y - yhat)^2)
```



2nd-degree polynomial regression fit

