The stopping power of <u>hydrogen in</u> hafnium and the importance of relativistic 4f electrons

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The stopping power of protons through Hf foil has been studied both experimentally and theoretically. The measurements were performed at the Laboratory of Accelerators and X-Ray Diffraction in Lisbon, by using the transmission method on self-supporting stopping material. The overall uncertainty of around 5% was established over the protons energy range (0.6-2.5) MeV. The theoretical developments involved fully relativistic atomic structure calculations for Hf, which required the solution of the Dirac equation. The shell-wise local plasma approximation (SLPA) was used to describe the energy transferred to the bound 1s-4f electrons, and the outer four electrons were considered as a free electron gas (FEG). We found the relativistic description of the 4f-shell and the screening between 4f and 5p electrons are decisive around the stopping maximum. Present theoretical and experimental results are in very good agreement in the energy region of the new measurements. However, the present theoretical stopping cross sections show substantial differences with the most used semi-empirical models (SRIM2013 and ICRU-49) at intermediate to low energies. Our calculations suggest the stopping maximum higher and shifted to lower energies than these previous predictions. Future measurements below 100 keV would be decisive for a better knowledge around the maximum and below.

I. INTRODUCTION

For impact energies above a few keV/amu, mono-27 energetic charged particles penetrating a foil of any ma-28 terial lose their energy through a series of consecutive in-29 elastic collisions, mainly with target electrons [1, 2]. The ³⁰ information given by the energy loss process is essential 31 not only to have a better knowledge of the physics behind 32 the fundamental interactions, but also because it plays an 33 important role in many applied fields such as materials 24 science, nuclear physics, ionic implantation and radio- $_{35}$ therapy [2, 3]. Experimental data on ion mean energy $_{36}$ loss per unit path S(E) is of crucial relevance to check 37 the reliability of semi-empirical models and to determine $_{38}$ some key parameters [4-6]. The experimental data available is often rather scarce, which is troublesome when the $_{40}$ material under study corresponds to an element of low $_{\scriptscriptstyle 41}$ occurrence on the Earth's upper crust, such as hafnium. $_{\scriptscriptstyle 42}$ So far, only one experimental work has been pub- $_{\scriptscriptstyle 43}$ lished regarding the stopping power cross section of pure $_{\scriptscriptstyle 44}$ hafnium for protons [7], while more attention has been 45 recently given to studies involving hafnium oxide due to 46 its practical use [8-10][8-11]. It is well known that significant attention has been paid in recent years to transition

metal-oxides such as HfO₂ because of their potential as 48

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alternative gate dielectrics to replace SiO_2 for the future generation of nano-electronics with less than 45 nm gate length [12, 13]. Some important physical properties of the above mentioned metal-oxide films depend on its thickness, which is often measured by using Rutherford Backscattering Spectrometry [14, 15], a method that relies heavily on the determination of the stopping power of ion beams in the material of interest.

In this study, we report experimental stopping power cross sections over the incident energy range (0.6-2.5) MeV for protons crossing self-supported Hf thin-film by using the transmission method. We aim not only to upgrade stopping power data compilations [16, 17] but also to provide useful information about the processes governing the slowing down of protons in multi-electronic targets. In the rare earth metals, the 4f electrons play a relevant role in the stopping power, being the first shell of bound electrons below the conduction band. As already noted –[18], the free electron gas (FEG) shows unexpected behavior in these elements, which casts doubts on its proper description. In the case of Hf, we found the contribution of the 4f-shell decisive even at impact energies around the stopping maximum, as shown later.

The theoretical approach implemented in this work uses the shell-wise local plasma approximation (SLPA) [19] to describe the energy transferred to the bound 1s-4f electrons, and two different models for the FEG: in low energy region, the screened potential with

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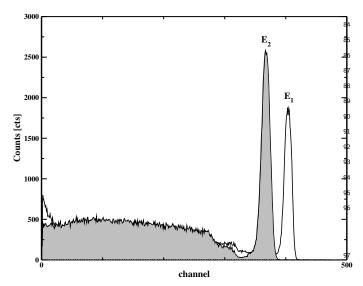


FIG. 1. RBS spectrum for $E_{\text{avg}} = 921.1$ keV protons on $_{99}$ hafnium sample which is subsequently used to determine the $_{100}$ energy loss in the foil.

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cusp condition model (SPCC) [20], which is non-linear binary formalism; and the Mermin-Lindhard dielectric formalism (ML) [21], for energies around the stopping maximum and above. Our model requires the relativistic wave functions and binding energies of Hf, and considers 4 electrons per atom in the FEG [22]. Hf has the extra interest of the filled 4f-subshell (with 14 electrons) as the main contribution below the FEG, causing the stopping cross sections to be very sensitive to a good description of this shell. The screening among the 4f and 5p electrons has been considered and found to play a major role within the SLPA calculations.

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The experimental details and data are given in Sec-112 tion II, while the theoretical method is explained in 113 Section III. Present theoretical and experimental val-114 ues are finally compared to the available experimental 115 values [7], the ICRU-49 calculations [27] and only 116 experimental values by Sirotinin group [7] measured with 117 backscattering method, the theoretical results by Grande 118 and Schiwietz [23, 24], and by Sigmund and Schinner [25] 119 and also with the semi-empirical values from the SRIM-120 clusions and discussions are given in Section V. All the 122 present data can be found at the Zenodo platform -[28]. 123

II. EXPERIMENTAL ARRANGEMENTS

A. Accelerator and scattering Chamber

The procedure used in this work to obtain stop-¹²⁹ ping power data is essentially the same as described in Ref. [29]. The present measurements were made at₁₃₀ the IST/LATR (Laboratory of Accelerators and X-Ray₁₃₁ Diffraction) in Lisbon. This facility uses a 2.5 MV Van₁₃₂

de Graaff accelerator to deliver $^1\mathrm{H}^+$ primary ion beams through a series of electrostatic lenses and collimators onto a thin $\mathrm{Au/SiO_2}$ sample which is used as a scattering center. This sample was placed in the center of a RBS/C scattering chamber, where a high vacuum (pressure of $\sim 10^{-6}$ Torr) was maintained during the measurements. The beam current on the sample was kept at around 5.0 nA to attain sufficient statistics in each particle spectrum. By using a beam spot of about 1.0 mm in diameter, a solid angle of 11.4 msr was attained. The overall energy resolution (FWHM) of the detection system was about 15 keV relative to 5.486 MeV alpha particles from a $^{241}\mathrm{Am}$ source.

B. Target

The stopping material under analysis was a hafnium foil with nominal thickness of 1.0 μ m and 99.95% purity which was supplied by Lebow Company [30]. However, a more precise thickness value was achieved by measuring the energy loss of alpha particles coming from a calibrated (239 Pu, 241 Am, 244 Cm) source. From the alpha spectra with and without the Hf foil interposed, the characteristic energy shift δ E was measured and then combined with the stopping power for 5.486 MeV alphas on hafnium ($^{55.69}$ eV/ $^{10^{15}}$ at/cm²) found in Ref. [26] to obtain an areal density of $(^{4.13}\pm0.21)\times10^{19}$ at/cm² which corresponds to a thickness of $0.920\pm0.046\mu$ m.

C. Energy loss measurement

Once the beam impinges on the Au/SiO₂ sample, protons are back-scattered towards a Si surface barrier detector located at 140° relative to the initial beam direction. Fig. 1 shows two particle spectra where ion energies E_2 and E_1 are associated to a placed and removed hafnium sample, respectively. Both energy distributions were fitted by Gaussian functions to obtain the mean energy and width (FWHM) of the peaks -[31], and from the difference between these two peak positions in the spectrum, the total energy loss $\Delta E = (E_1 - E_2)$ in the foil was calculated. As established in previous studies -[5, 29], the experimental stopping power cross sections $\varepsilon(E)$ are determined at some mean energy E_{avg} by measuring the ion energy losses ΔE within the investigated Hf foil, which has a mean thickness denoted by Δx . In this way, only when the energy loss fraction $\Delta E/E_{\rm avg}$ across the Hf foil is not exceeding 20% it is possible to define the stopping cross section by -[32, 33]:

$$\varepsilon(E) = \frac{S(E)}{N} = -\frac{dE}{N dx} \approx -\frac{\Delta E}{N \Delta x},$$
 (1)

where N denotes the atomic number density (atoms cm⁻³) of the material under study. When this condition was not fulfilled, a small correction to the mean energies

 E_{avg} was applied in order to account for the nonlinear dependence on ion energy of stopping powers –[34, 35]. 189

III. THEORETICAL METHOD

The energy loss of ions in metal targets responds to ¹⁹⁴ different physical mechanisms, depending on the impact ¹⁹⁵ ion velocity. At low velocities, the binary collisions are ¹⁹⁶ responsible for the loss of energy by the ion. The main ¹⁹⁷ contribution is the ionization of electrons of the metal ¹⁹⁸ conduction band, which is well approximated by a free ¹⁹⁹ electron gas (FEG) of Fermi velocity v_F . Above cer-²⁰⁰ tain velocity (i.e. $v \geq 1.5 v_F$), not only binary but also²⁰¹ collective excitations (plasmons) are possible occur [20]. ²⁰² Moreover, at high energies, also the bound electrons con-²⁰³ tribute to the stopping power. The method used in this ²⁰⁴ work combines a description for the interaction with the ²⁰⁵ valence (or conduction) electrons as a FEG, and a differ-²⁰⁶ ent one for the interaction with the bound electrons.

We used the SPCC model [20] to describe the stop-208 ping power of low velocity charged particles in the FEG.²⁰⁹ It is a non-perturbative binary collisional approximation,²¹⁰ thus valid at energies below that of plasmon excitations.²¹¹ The SPCC [20] is based on a screened central potential²¹² with cusp condition of the electronic density close to the²¹³ projectile. This model proved to give a good descrip-214 tion of the induced electron density even for negative215 projectiles [20], and reproduces the low velocity proton-216 antiproton differences in the stopping power (Barkas ef-217 fect). The SPCC formalism only depends on the Wigner-218 Seitz radio, r_S , which is a measure of the electronic den-219 sity of the FEG. For metals of well-known r_S , the SPCC₂₂₀ describes correctly the low energy experimental stopping²²¹ data [20], agreeing with the DFT results by Echenique222 and coworkers [36, 37] at v = 0.

Hafnium $(Z=72, [\text{Xe}] \ 4f^{14} \ 6s^2 \ 5d^1_{3/2} \ 5d^1_{5/2})$, belongs₂₂₄ to the first groups of transition metals, with 4-four elec-²²⁵ trons as FEG (theoretical $r_S=2.14$ a.u.) and 1s-4f²²⁶ electrons bound. We compared the computed r_S with²²⁷ the experimental value obtained from measured energy²²⁸ loss function by Lynch et al -[38]. The experimental²²⁹ plasmon energy of Hf is $\hbar\omega_P\approx 15.8$ eV, with a width²³⁰ at half maximum $\delta\approx 4.4$ eV, and $r_S\approx 2.07$ a.u. -[38].²³¹ The difference of less than 5% between theoretical and²³² experimental r_S assess Hf as a canonical target [20].

Above certain impact velocity, the plasmon contribu-234 tion is important (i.e. around and above the stopping-235 maximum). An interesting value for our analysis is the-236 minimum impact velocity to excite plasmons, v_P . In-237 the dielectric formalism, this value can be obtained as-238 $v_P \approx v_F [1 + (3\pi v_F)^{-1/2}]$ [39]. To describe the energy-239 loss considering collective and binary excitation, we re-240 sort to the ML dielectric formalism -[21], which is a linear-241 response, perturbative approximation, so it depends on-242 the square of the ion charge. In this formalism, the re-243 sponse of target electrons to the ion passage is described-244 through the quantum dielectric function, depending on-245

the characteristic r_S and δ parameters of the FEG.

For the stopping power due to bound electrons, the SLPA [19, 20] is employed. It is worth to mention mentioning that the only inputs for the SLPA are the space-dependent densities of each shell in the ground state, and their binding energies. Collective processes and screening among electrons are included. Hafnium Since hafnium is a relativistic target, therefore the wave functions and binding energies must be obtained by solving the manyelectron many-electron Dirac Hamiltonian. Details of these calculations and a table of binding energies have been published in Ref. [22], and the while Slater-type orbital expansions in are given in Ref. [40].

Too To assess the importance of the a fully relativistic description of bound electrons, Fig. 2shows—(a) non-relativistic [41] and our relativistic shows our binding energies, $E_{nl\pm}$, with $\pm = j\pm 1/2$; and (b) the relative errors with respect to the non-relativistic values [41]; and the experimental data on solid Hf [42]from—, which is available only for 1s to $4f_{\pm}$ subshells, as expected. We notice that not only the most inner shells require relativistic calculations, but also the outer 5p and 4f shells. Furthermore, this figure shows very clearly the disability of non-relativistic calculations to describe the experimental data, which surprisingly worsens from the inner to the outer shells.

From the comparison with the experimental values in Fig. 2 (a), it can be noted that the sign of the binding energy deviations is inverted for the outer 5s and 4f electrons, with the experimental binding energies being less bounded than our theoretical ones. Small differences for the outer shells are expected since the experimental values correspond to hafnium in solid-state, while our theoretical calculations correspond to the element in the gas phase.

For more detail, Fig. 2 (b) shows the relative errors with respect to the experimental values. This figure shows clearly that the relativistic corrections are very important to describe the atomic structure of hafnium, even for the outer shells. It turns out that the errors committed in the non-relativistic calculations of the inner shell orbitals propagate, through the Hartree-Fock approximation, to the outer shells. The importance of fully relativistic calculations for the outer shells has already been noted for Au, Pb and Bi and W [43].

For the contribution of bound electrons to the total stopping cross sections, the SLPA considers independent contributions of each subshell. Our relativistic binding energies present spin-orbit split. However, in total stopping power, where the initial state of the excited electron is not measured, the quantum uncertainty in energy ΔE melts this split. The criteria $\Delta E \Delta t \geq \hbar/2$ merges the energies $E_{nl+} - E_{nl-}$ for sufficiently small values of Δt (the collisional mean-time). In fact, at sufficiently high impact velocity, we can expect all target electrons to respond together to the ion passage [44, 45]. Following previous workworks [43], the collisional time is estimated as $\Delta t \approx \langle r_i \rangle / v$, with $\langle r_i \rangle$ and v being the orbital mean

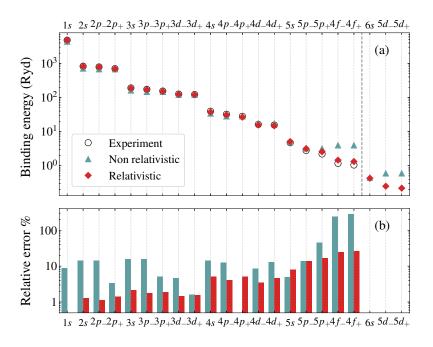


FIG. 2. (a) Binding energies of Hf. Non-relativistic and Present relativistic calculations and available non-relativistic [41] values are given with filled symbols. Experimental measurements for solids [42] are depicted with hollow open circles. (b) Corresponding relative errors respect to experimental data.

radio and impact velocity, respectively.

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Theoretical total stopping cross sections of protons in hafnium adding FEG and bound 1s-4f contributions, as mentioned in the inset. The vertical grey dashed-line indicates the energy above which plasmon excitation is possible. The SLPA total stopping values for 1s-4f282 bound electrons with and without 5p-4f screening are displayed with solid and dotted lines, respectively.

The SLPA calculates the contribution of each subshell²⁸⁵ of bound electrons to the total stopping cross sections.286 We In the case of hafnium, we found that for every subshell of Hf, at the impact energy at which this sub-shell₂₈₇ began to contribute electrons, the spin-orbit split was 288 unresolved. Then is unresolved in the energy region this 289 sub-shell contributes. Therefore, the nl-electrons should₂₉₀ be considered together, responding to the ion passage as₂₉₁ a single gas of electrons with density $\delta_{nl}(r)$ and a mean₂₉₂ binding energy E_{nl} . This feature is important within the₂₉₃ SLPA calculations because it accounts for the screening₂₉₄ among electrons of the same binding energy. For ex-295 ample, the $4f_{-}$ and $4f_{+}$ of Hf can only be resolved for₂₉₆ impact energies E < 0.05 keV, but the contribution of₂₉₇ 4f to the total stopping is negligible for $E < 40 \text{ keV}_{.298}$ Moreover, the 5p and 4f electrons of Hf are very close₂₉₉ in energy ($\Delta E_{5p-4f} \approx 1$ a.u. [22]) and they react to-300 gether for impact energies E > 40 keV (inter-shell screen-301 ing). As already mentioned, at higher energies inter-shell₃₀₂ screening is possible for other subshells (i.e. 4p-4d for₃₀₃) impact energies above 0.9 MeV), but its weight in the₃₀₄ total stopping is minor for deeper shells.

Finally, in all our calculations [20] we assumed the 306

projectile to be proton and not neutral hydrogen. When an ion moves inside a metal, the FEG screens the nucleus, so the binding energies will be smaller than outside the metal, and this effect is more important a low impact velocities v. In the case of hydrogen the difference is drastic, i.e. for H inside Hf (rs=2.07), the 1s-bound state is almost null at v<2 [39]. It is worth to mention that this assumption agrees with Ziegler SRIM code [26], but differs from CasP code [23] that predicts neutral hydrogen at very low velocities.

In Fig. 3, we display the present theoretical stopping cross section of Hf for protons using the relativistic wave functions and binding energies, but with and without the 5p-4f screening. We added show separately the FEG and the bound electron contributions as explained above and the total stopping as the addition of both of them. The minimum energy for plasmon excitation was estimated to $37 \sim 37$ keV. We used the non-perturbative SPCC model for impact energies $E \leq 37$ keV, and the perturbative ML calculation above this energy. Bound 1s-4f electrons (relativistic wave functions and binding energies) are calculated with the SLPA and shown separately in Fig. 3 with and without the 4f-5p screening. Below $\sim 40 \text{ keV}$ the difference between both calculations is negligible. Clearly, considering 5p-4f electrons as a single group of 20 electrons with screening among them gives lower stopping values than the addition of the separate 5p and 4fcontributions. Notice that this shell correction can only be considered be considered naturally within a many electron model such as the SLPA.

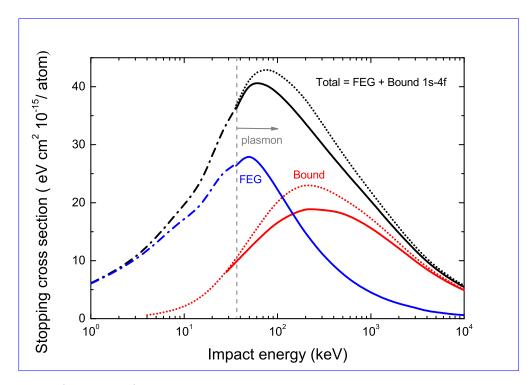


FIG. 3. Stopping power (colour online) Theoretical stopping cross section sections of hafnium for protons in hafnium. Symbols solid circles Blue dash-dotted-line, present values the non-perturbative SPCC for the FEG; open circles, previous data [7]. Curves: Black-blue solid-line, present full theoretical ML results for the FEG (includes plasmon excitation); red solid and dotted-lines, the SLPA results for bound electrons with 4f-and without 5p-4f screening; violet dashed-line, values from ICRU-49 [27] respectively. Black curves, total stopping adding the FEG and green dotted linebound 1s-4f contributions: dash-dotted-line, SRIM-2013 [26]SPCC (FEG) + SLPA (bound); solid-line, ML (FEG) + SLPA (bound) without 4f-5p screening. The vertical grey dashed-line indicates the energy of 37 keV above which plasmon excitation is possible.

IV. ANALYSIS OF THE RESULTS AND DISCUSSION

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The present data and theoretical results are is dis-³³⁴ played in Table I, and Fig. 4. As can be seen in ³³⁵ Table Iobserved, an overall relative uncertainty of around ³³⁶ 5% was achieved for the experimental stopping power ³³⁷ values, which are mainly due to the uncertainty in the ³³⁸ hafnium foil thickness.

In Fig. 4, we have good synthesizes the results of the 340 present work. The agreement between the present theo-341 retical results and the $\underline{\underline{new}}$ measurements displayed in Ta-342 ble I is clear. Present measurements using transmission $^{343}\,$ method are in good agreement with the previous data³⁴⁴ by Sirotinin [7], measured in backscattering geometry.345 Our theoretical approach also agrees with previous the 346 data by Sirotinin [7], except for the lowest energy mea-347 surement at 80 keV. We have also included in this figure₃₄₈ the theoretical curves from the CasP5.2 code by Grande349 and Schiwietz [23, 24] and from the DPASS code by 350 Sigmund and Schinner [25], both available online; also₃₅₁ the semi-empirical results from SRIM-2013 [26] and the352 ICRU49 tables [27]. It is interesting that our full theo-353 retical curve differs from SRIM-2013 for impact energies₃₅₄ below 100 keV. We obtain a stopping maximum around₃₅₅ 40×10^{-15} eV cm²/atom at 65 keV. Instead, following the up-to-now only set of data -[7], SRIM-2013 suggests a lower stopping maximum at impact energy of 115 kevkeV. The stopping maximum is a very sensitive region for any full theoretical description, with no parameters at all, and this is quite visible in a linear-scale plot like Fig. 4. However, the impact energy for the maximum seem to agree between our curve and DPASS, although is 10% below. Instead, CasP predicts a stopping maximum 10% above our value and a completely different shape at lower energies. It is worth mentioning that similar theoretical our model gives similar results using the experimental $r_S = 2.07$ a.u. instead of the theoretical $r_S = 2.14$ a.u. give with the stopping maximum at the same impact energy but 4% higher.

Future experiments for impact energies below 100 keV would be important to complete this study on the stopping of Hf for protons. In the energy region 80-500 keV only the measurements by Sirotinin group [7] in 1984 are available. SRIM-2013 clearly includes these values in the adjust of the code, so it does not represent a test for this data. Undoubtedly, new measurements are needed in three specific energy regions: below 500 keV, around the stopping maximum (i.e. 50-200 keV) and at low impact energies.

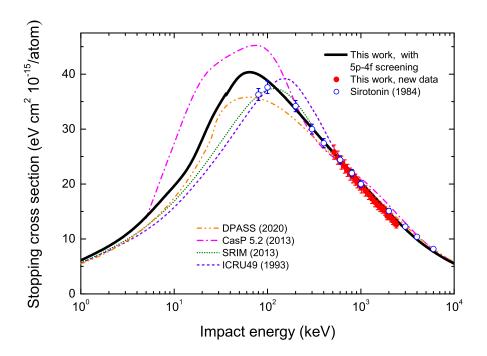


FIG. 4. (colour online) Stopping power cross section of hafnium for protons. Symbols: solid circles, present values; open circles, previous data [7]. Curves: Black solid-line, present full theoretical results with 4f-5p screening; pink dash-dot line, theoretical CasP5.2 [23, 24] values; orange dash-double-dot line, theoretical DPASS [25] results; green dotted-line, semi-empirical SRIM-2013 [26]; violet dashed-line, ICRU49 [27] tabulated values.

TABLE I. Stopping power values $S_{exp,exp}$ of hafnium for protons measured in this work. $\Delta E/E$ values are also shown.

$E_{\overline{avg}}$	avg_	$S_{\overline{exp}}_{\overline{exp}}$	$\Delta \mathrm{E}/\mathrm{E}$	$\mathbb{E}_{\overline{avg}}$ avg \sim	$S_{\overline{exp}}_{-exp_{\sim}}$	$\Delta \mathrm{E}/\mathrm{E}$	$E_{\overline{avg}}$ avg \sim	$S_{\overline{exp}}_{-exp}$
ke		$eV/(10^{15} at/cm$	²) % <u>%</u>	keV	$eV/(10^{15} at/cm^2)$	%_ ‰_	keV	$eV/(10^{15} at/cm^2)$
516,6	516.6	$\frac{25.8}{25.8}$ $\pm \frac{1.3}{1}$	20,5 $20,5$	1170,3 <u>1170.3</u>	$18,25$ 18.25 $\pm 0,91$ 0.91	6,4	1813,4 - <u>1813.4</u>	$15,10$ 15.10 $\pm 0,76$ 0.7
567,8	567.8	$24.8 - 24.8 \pm 1.2 - 1$	2.2 17.9 17.9	1220,0 - <u>1220.0</u>	$18,08-18.08 \pm 0,90-0.90$	6,1-6.1	1862,7 - <u>1862.7</u>	$14,79$ 14.79 $\pm 0,74$ 0.7
618,8	518.8	$23.9 - 23.9 \pm 1.2 - 1$	<u>2</u> 15,8 – <u>15.8</u>	1269,6 – <u>1269.6</u>	$17.57 17.57 \pm 0.88 0.88$	5,7 <u>5.7</u>	1912,0 _1912.0	$14,21$ 14.21 $\pm 0,71$ 0.7
669,6	569.6	$23,2$ 23.2 $\pm 1,2$	$\underbrace{.2}_{2}$ $\underbrace{14.2}_{2}$	1319,2 1319.2	$17.32 17.32 \pm 0.87 0.87$	5,4 <u>5.4</u>	1961,2 1961.2	$14,46$ 14.46 $\pm 0,72$ 0.7
720,1	720.1	$\frac{22,5}{22.5}$ $\pm \frac{1,1}{2}$	$\underbrace{.1}_{}$ $\underbrace{12.8}_{}$	1368,8 <u>1368.8</u>	$\pm \frac{17,15}{17.15} \pm \frac{0,86}{0.86} \pm \frac{0.86}{0.86}$	5,1 − <u>5.1</u>	2010,4-2010.4	$14,34$ 14.34 $\pm 0,72$ 0.7
770,5	770.5	21,8 21.8 ± 1,1 1	$\underbrace{.1}_{1}$ $\underbrace{11,6}_{-11.6}$	1418,3 <u>1418.3</u>	$16,69$ 16.69 $\pm 0,83$ 0.83	4,8 4.8	2059,6 -2059.6	$13.76 13.76 \pm 0.69 0.6$
820,8	820.8	$21,3$ 21.3 $\pm 1,1$	$\underbrace{.1}_{1}$ $\underbrace{10,7}_{-10.7}$	1467,8 <u>1467.8</u>	$16,43$ 16.43 $\pm 0,82$ 0.82	4,6-4.6	2108,8 <u>2108.8</u>	$13.78 - 13.78 \pm 0.69 - 0.69$
871,0	871.0	$20.8 - 20.8 \pm 1.0 - 1$	0 <u>9,8</u> —9.8	1517,2 1517.2	$16,13$ 16.13 $\pm 0,81$ 0.81	4,4-4.4	2158,0 <u>2158.0</u>	$13,70$ 13.70 $\pm 0,69$ 0.6
921,1	921.1	$20.3 \pm 1.0 $			$16,04$ 16.04 $\pm 0,80$ 0.80			
971,1	971.1	$19.9 - 19.9 \pm 1.0 - 1$	<u>8,4−8.4</u>		$15,77$ 15.77 $\pm 0,79$ 0.79			
1021,0	1021.0	$19,33-19.33 \pm 0,97$	0.97 7,8 7.8	1665,4-1665.4	$15,51$ 15.51 $\pm 0,78$ 0.78	3,8 − <u>3.8</u>	2305,5 <u>2305.5</u>	$13.07 \pm 0.65 \pm 0.65$
1070,8	1070.8	$19.03 - 19.03 \pm 0.95$	0.95 7,3 7.3	1714,8 <u>1714.8</u>	$15,46$ 15.46 $\pm 0,77$ 0.77	3,7 <u>3.7</u>	2354,7 <u>2354.7</u>	$12.91 - 12.91 \pm 0.65 - 0.6$
1120,6	1120.6	$18,73$ 18.73 ± 0.94			$14.93 \pm 0.75 = 0.75$			

V. CONCLUSION

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In this work, we have used the transmission method 363 to experimentally determine stopping power cross section values for (0.6-2.5) MeV protons incident on self-supporting Hf foils with an overall uncertainty of around

5%. Additionally, we calculated values extracted from the theoretical framework that involved the relativistic wave functions and binding energies of Hf, and considered 4-four electrons per atom in the free electron gas. The shell-wise local plasma approximation was employed to describe the energy transferred to the bound 1s-4f elec-

trons, and two different models for the FEG: the screened₃₈₈ potential with cusp condition (SPCC model) for energies₃₈₉ below that of the plasmon excitation, and the Mermin-₃₉₀ Lindhard dielectric formalism, for energies around the₃₉₁ stopping maximum and above. Present theoretical stop-₃₉₂ ping cross sections cover an extensive energy range from₃₉₃ 1 keV/amu-10 meVMeV/amu.

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At high impact energies, the new stopping measurements are in good agreement with our theoretical results, with previous experimental data and semi-empirical values by SRIM-2013 and ICRU-49. However, we call the attention that around the stopping maximum and at lower impact energies the difference between our full-396 theoretical results and SRIM is substantial. We compare our theoretical results with other two models given by 398 the DPASS and CasP5.2 codes. Differences can be noted 399 at intermediate to low impact energies, but they also 400 support an stopping maximum at lower energy than 401 SRIM predictions.

To the best of our knowledge, these are the first theo-403 retical calculations of stopping in Hf taking into account 404

the atomic relativistic effect and the screening among electrons in a consistent way from very low to high impact energies. Future experiments for impact energies below 100 keV around the stopping maximum and in the low energy region would be important to complete this study. have a more complete understanding of the stopping of protons in hafnium.

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