# The stopping power of <u>hydrogen in</u> hafnium and the importance of relativistic 4f electrons

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The stopping power of protons through Hf foil has been studied both experimentally and theoretically. The measurements were performed at the Laboratory of Accelerators and X-Ray Diffraction in Lisbon, by using the transmission method on self-supporting stopping material. The overall uncertainty of around 5% was established over the protons energy range (0.6-2.5) MeV. The theoretical developments involved fully relativistic atomic structure calculations for Hf, which required the solution of the Dirac equation. The shell-wise local plasma approximation (SLPA) was used to describe the energy transferred to the bound 1s-4f electrons, and the outer four electrons were considered as a free electron gas (FEG). We found the relativistic description of the 4f-shell and the screening between 4f and 5p electrons are to be decisive around the stopping maximum. Present theoretical and experimental results are in very good excellent agreement in the energy region of the new measurements. However, the present our theoretical stopping cross sections show substantial differences with the most used semi-empirical models (SRIM2013 and ICRU-49) at intermediate to low energies. Our calculations suggest the stopping maximum to be higher and shifted to lower energies than these previous predictions. Future measurements below 100 keV would be decisive necessary for a better knowledge understanding of the stopping power around the maximum and below.

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### I. INTRODUCTION

For impact energies above a few keV/amu, mono-26 energetic charged particles penetrating a foil of any ma-27 terial lose their energy through a series of consecutive in-28 elastic collisions, mainly with target electrons [1, 2]. The 29 information given by the energy loss process is essential 30 not only to have a better knowledge comprehension of the 31 physics behind the fundamental interactions —but also 32 because it plays an important a vital role in many applied 33 fields such as materials science, nuclear physics, ionic im-34 plantation, and radiotherapy [2, 3]. Experimental data 35 on ion mean energy loss per unit path S(E) is of crucial <sup>36</sup> relevance to check the reliability of semi-empirical mod- 37 els and to determine some key parameters [4–6]. The ex-38 perimental data available is often rather scarce, which is 39 troublesome when the material under study corresponds 40 to an element of low occurrence on the Earth's upper 41 crust, such as hafnium.

So far, only one experimental work has been pub-<sup>43</sup> lished regarding the stopping power cross section of pure <sup>44</sup> hafnium for protons [7], while more attention has been <sup>45</sup> recently given to studies involving hafnium oxide due to <sup>46</sup> its practical use [8–10][8–11]. It is well known that signif-<sup>47</sup>

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icant attention has been paid in recent years to transition metal-oxides such as HfO<sub>2</sub> because of their potential as alternative gate dielectrics to replace SiO<sub>2</sub> for the future generation of nano-electronics with less than 45 nm gate length [12, 13]. Some important physical properties of the above mentioned metal-oxide films depend on its their thickness, which is often measured by using Rutherford Backscattering Spectrometry [14, 15], a method that . This method relies heavily on the determination of the stopping power of ion beams in the material of interest.

In this study, we report experimental stopping power cross sections over the incident energy range (0.6-2.5)MeV for protons crossing self-supported Hf thin-film by using the transmission method. We aim not only to upgrade stopping power data compilations [16, 17] but also to provide useful information about the processes governing the slowing down of protons in multi-electronic targets. In the rare earth metals, the 4f electrons play a relevant an essential role in the stopping power, being since they belong to the first shell of bound electrons below the conduction band. As already noted -[18], the free electron gas (FEG) shows unexpected behavior in these elements, which casts doubts on its proper description. In the case of Hf, we found the contribution of the 4fshell to be decisive even at impact energies around the stopping maximum, as will be shown later.

The theoretical approach implemented in this work uses the shell-wise local plasma approximation

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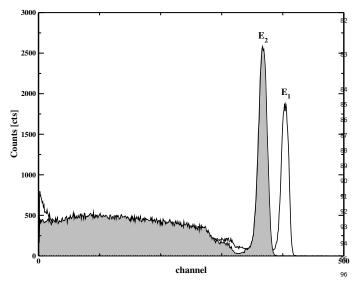


FIG. 1. RBS spectrum for  $E_{\text{avg}} = 921.1 \text{ keV}$  protons on the hafnium sample, which is subsequently used to determine the energy loss in the foil.

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(SLPA) [19] to describe the energy transferred to the bound 1s-4f electrons , and two different models for the FEG:: in low energy region, the screened potential with cusp condition model (SPCC) [20], which is non-linear binary formalism; and the Mermin-Lindhard dielectric formalism (ML) [21], for energies around the stopping maximum and above. Our model requires the relativistic wave functions and binding energies of Hf, and considers 4 and considers four electrons per atom in the FEG [22]. Hf has the extra interest of Hafnium is particularly interesting since the filled 4f-subshell (with 14 electrons) as the main contribution is the main contributor below the FEG, causing the stopping cross sections to be very sensitive to a good description of this shell. The screening among the 4f and 5p electrons has been considered and found to play a major significant role within the SLPA calculations.

The experimental details and data are given in Sec-118 tion II, while the theoretical method is explained in119 Section III. Present theoretical and experimental val-120 ues are finally compared to the available experimental 121 values [7], the ICRU-49 calculations [27] and only 122 experimental values measured by Sirotinin et al. [7] 123 with the backscattering method, the theoretical results 124 by Grande and Schiwietz [23, 24], and by Sigmund and 125 Schinner [25], and also with the semi-empirical values 126 from the SRIM-2013 package [26] and the ICRU-49127 tabulation [27]. Conclusions and discussions are given 128 in Section V. All the present data can be found at the 129 Zenodo platform -[28].

#### II. EXPERIMENTAL ARRANGEMENTS

#### A. Accelerator and scattering Chamber

The procedure used in this work to obtain stopping power data is essentially the same as described in Ref. [29]. The present measurements were made at the IST/LATR (Laboratory of Accelerators and X-Ray Diffraction) in Lisbon. This facility uses a 2.5 MV Van de Graaff accelerator to deliver <sup>1</sup>H<sup>+</sup> primary ion beams through a series of electrostatic lenses and collimators onto a thin Au/SiO<sub>2</sub> sample, which is used as a scattering center. This sample was placed in the center of a-an RBS/C scattering chamber, where a high vacuum (pressure of  $\sim 10^{-6}$  Torr) was maintained during the measurements. The beam current on the sample was kept at around 5.0 nA to attain sufficient statistics in each particle spectrum. By using a beam spot of about 1.0 mm in diameter, a solid angle of 11.4 msr was attained. The overall energy resolution (FWHM) of the detection system was about 15 keV relative to 5.486 MeV alpha particles from a <sup>241</sup>Am source.

#### B. Target

The stopping material under analysis was a hafnium foil with a nominal thickness of 1.0  $\mu$ m and 99.95% purity, which was supplied by Lebow Company [30]. However, a more precise thickness value was achieved by measuring the energy loss of alpha particles coming from a calibrated (<sup>239</sup>Pu, <sup>241</sup>Am, <sup>244</sup>Cm) source. From the alpha spectra with and without the Hf foil interposed, the characteristic energy shift  $\delta E$  was measured and then combined with the stopping power for 5.486 MeV alphas on hafnium (55.69 eV/ $10^{15}$  at/cm<sup>2</sup>) found in Ref. [26] to obtain an areal density of  $(4.13 \pm 0.21) \times 10^{19}$  at/cm<sup>2</sup>, which corresponds to a thickness of  $0.920 \pm 0.046 \mu m$ .

#### C. Energy loss measurement

Once the beam impinges on the Au/SiO<sub>2</sub> sample, protons are back-scattered backscattered towards a Si surface barrier detector located at 140° relative to the initial beam direction. Fig. 1 shows two particle spectrawhere, where the ion energies  $E_2$  and  $E_1$  are associated to with a placed and removed hafnium sample, respectively. Both energy distributions were fitted by Gaussian functions to obtain the mean energy and width (FWHM) of the peaks -[31], and from the difference between these two peak positions in the spectrum, the total energy loss  $\Delta E = (E_1 - E_2)$  in the foil was calculated. As established in previous studies -[5, 29], the experimental stopping power cross sections  $\varepsilon(E)$  are determined at some mean energy  $E_{\rm avg}$  by measuring the ion energy losses  $\Delta E$  within the investigated Hf foil, which has a mean thick-

ness denoted by  $\Delta x$ . In this way, only when the energy<sub>183</sub> loss fraction  $\Delta E/E_{\rm avg}$  across the Hf foil is not exceeding<sub>184</sub> 20%, it is possible to define the stopping cross section by<sub>185</sub> –[32, 33]:

$$\varepsilon(E) = \frac{S(E)}{N} = -\frac{dE}{N dx} \approx -\frac{\Delta E}{N \Delta x},$$
 (1)

where N denotes the atomic number density (atoms<sub>191</sub> cm<sup>-3</sup>) of the material under study. When this condition<sub>192</sub> was not fulfilled, a small correction to the mean energies<sub>193</sub>  $E_{\text{avg}}$  was applied in order to account for the nonlinear non-linear dependence on ion energy of stopping powers<sub>195</sub>–[34, 35].

#### III. THEORETICAL METHOD

The energy loss of ions in metal targets responds to<sup>201</sup> different physical mechanisms, depending on the impact<sup>202</sup> ion velocity. At low velocities, the binary collisions are<sup>203</sup> responsible for the loss of energy by the ion. The main<sup>204</sup> contribution is the ionization of electrons of the metal<sup>205</sup> conduction band, which is well approximated by a free<sup>206</sup> electron gas (FEG) of Fermi velocity  $v_F$ . Above certain<sup>207</sup> velocity a particular velocity value (i.e.,  $v \ge 1.5 v_F$ ), not<sup>208</sup> only binary but also collective excitations (plasmons) are<sup>209</sup> possible occur [20]. Moreover, at high energies, also the<sup>210</sup> bound electrons contribute to the stopping power. The<sup>211</sup> method used in this work combines a FEG description for<sup>212</sup> the interaction with the valence (or conduction) electrons<sup>213</sup> as a FEG, and a different one for the interaction with the<sup>214</sup> bound electrons.

We used the SPCC model [20] to describe the stop-216 ping power of low velocity charged particles in the FEG.217 It is a non-perturbative binary collisional approximation, 218 thus valid at energies below that of plasmon excitations.219 The SPCC [20] is based on a screened central potential<sup>220</sup> with cusp condition of the electronic density close to the 221 projectile. This model proved to give a good descrip-222 tion of the induced electron density even for negative223 projectiles [20] -and reproduces the low velocity proton-224 antiproton differences in the stopping power (Barkas ef-225 fect). The SPCC formalism only depends on the Wigner-226 Seitz radio,  $r_S$ , which is a measure of the electronic den-<sub>227</sub> sity of the FEG. For metals of well-known  $r_S$ , the SPCC<sub>228</sub> describes correctly the low energy experimental stopping<sub>229</sub> data correctly [20], agreeing with the DFT results by<sub>230</sub> Echenique and coworkers [36, 37] at v = 0.

Hafnium  $(Z = 72, [Xe] 4f^{14} 6s^2 5d_{3/2}^1 5d_{5/2}^1)$ , belongs<sub>232</sub> to the first groups of transition metals, with 4-four elec-<sub>233</sub> trons as FEG (theoretical  $r_S = 2.14$  a.u.) and 1s-4f elec-<sub>234</sub> trons bound. We compared the computed  $r_S$  with the ex-<sub>235</sub> perimental value obtained from the measured energy loss<sub>236</sub> function by Lynch *et al.* [38]. The experimental plasmon<sub>237</sub> energy of Hf is  $\hbar\omega_P \approx 15.8$  eV, with a width at half<sub>238</sub> maximum  $\delta \approx 4.4 - \delta \approx 4.4$  eV, and  $r_S \approx 2.07 - r_S \approx 2.07$ <sub>239</sub> a.u. [38]. The difference of less than 5% between theo-<sub>240</sub>

retical and experimental  $r_S$  assess Hf as a canonical target [20].

Above certain impact velocity, the plasmon contribution is important essential (i.e., around and above the stopping maximum). An interesting value A value of interest for our analysis is the minimum impact velocity to excite plasmons,  $v_P$ . In the dielectric formalism, this value can be obtained as  $v_P \approx v_F [1 + (3\pi v_F)^{-1/2}]$  [39]. To describe the energy loss considering collective and binary excitation, we resort to the ML dielectric formalism –[21], which is a linear response, perturbative approximation, so it depends on the square of the ion charge. In this formalism, the response of target electrons to the ion passage is described through the quantum dielectric function, depending which depends on the characteristic  $r_S$  and  $\delta$  parameters of the FEG.

For the stopping power due to bound electrons, the SLPA [19, 20] is employed. It is worth to mention mentioning that the only inputs for the SLPA are the space-dependent densities of each shell in the ground state, and their binding energies. Collective processes and screening among electrons are included. Hafnium Since hafnium is a relativistic target, therefore the wave functions and binding energies must be obtained by solving the manyelectron many-electron Dirac Hamiltonian. Details of these calculations and a table of binding energies have been published in Ref. [22], and the while Slater-type orbital expansions inare given in Ref. [40].

Too To assess the importance of the a fully relativistic description of bound electrons, Fig. 2shows—(a) non-relativistic [41] and our relativistic shows our binding energies,  $E_{nl\pm}$ , with  $\pm = j\pm 1/2$ ; and (b) the relative errors with respect to the non-relativistic values [41]; and experimental data on solid solid-state Hf [42] from, which is available only for 1s to  $4f_{\pm}$  subshells, as expected. We notice that not only the most inner shells require relativistic calculations, but also the outer 5p and 4f shells. Furthermore, this figure shows very clearly the disability of non-relativistic calculations to describe the experimental data, which surprisingly worsens from the inner to the outer shells.

From the comparison with the experimental values in Fig. 2 (a), it can be noted that the sign of the binding energy deviations is inverted for the outer 5s and 4f electrons, with the experimental binding energies being less bounded than our theoretical ones. Small differences for the outer shells are expected since the experimental values correspond to hafnium in solid-state, while our theoretical calculations correspond to the element in the gas phase.

More detail of the theoretical binding energies is given in Fig. 2 (b), where relative errors with respect to the experimental values are shown. This figure shows clearly that the relativistic corrections are critical to describing the atomic structure of hafnium, even for the outer shells. It turns out that the errors committed in the non-relativistic calculations of the inner shell orbitals propagate, through the Hartree-Fock approximation, to

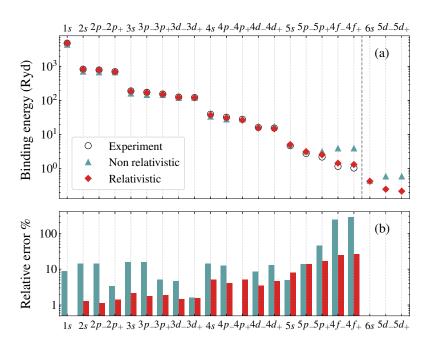


FIG. 2. (a) Binding energies of Hf. Non-relativistic and Present relativistic calculations and available non-relativistic [41] values are given with filled symbols. Experimental measurements for solids [42] are depicted with hollow open circles. (b) Corresponding relative errors with respect to experimental data.

the outer shells. The importance of fully relativistic<sup>271</sup> calculations for the outer shells has already been noted<sup>272</sup> for Au, Pb, Bi, and W [43].

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For the contribution of bound electrons to the total<sup>274</sup> stopping cross sections, the SLPA considers independent<sup>275</sup> contributions of each subshell. Our relativistic binding<sup>276</sup> energies present spin-orbit split. However, in total stop-<sup>277</sup> ping power, where the initial state of the excited elec-<sup>278</sup> tron is not measured, the quantum uncertainty in energy<sup>279</sup>  $\Delta E$  melts this split. The eriteria criterion  $\Delta E \Delta t \geq \hbar/2^{280}$  merges the energies  $E_{nl+} - E_{nl-}$  for sufficiently small<sup>281</sup> values of  $\Delta t$  (the collisional mean-time). In fact, at suf-<sup>282</sup> ficiently high impact velocity, we can expect all target<sup>283</sup> electrons to respond together to the ion passage [44, 45].<sup>284</sup> Following previous workworks [43], the collisional time<sup>285</sup> is estimated as  $\Delta t \approx \langle r_i \rangle/v$ , with  $\langle r_i \rangle$  and v being the<sup>286</sup> orbital mean radio and impact velocity, respectively.

Theoretical total stopping cross sections of protons in  $^{288}$  hafnium adding FEG and bound 1s-4f contributions, as  $^{289}$  mentioned in the inset. The vertical grey dashed-line  $^{290}$  indicates the energy above which plasmon excitation is  $^{291}$  possible. The SLPA total stopping values for 1s-4f292 bound electrons with and without 5p-4f screening are  $^{293}$  displayed with solid and dotted lines, respectively.

The SLPA calculates the contribution of each subshell of bound electrons to the total stopping cross sections. We In the case of hafnium, we found that for every subshell of Hf, at the impact energy at which this sub-shell began to contribute electrons, the spin-orbit split was unresolved. Then is unresolved in the energy region this 300

sub-shell contributes. Therefore, the nl-electrons should be considered together, responding to the ion passage as a single gas of electrons with density  $\delta_{nl}(r)$  and  $\frac{1}{8}$ mean binding energy  $E_{nl}$ . This feature is important vital within the SLPA calculations because it accounts for the screening among electrons of the *same* binding energy. For example, the  $4f_{-}$  and  $4f_{+}$  of Hf can only be resolved for impact energies E < 0.05 keV, but the contribution of 4f to the total stopping is negligible for E < 40 keV. Moreover, the 5p and 4f electrons of Hf are very close in energy ( $\Delta E_{5p-4f} \approx 1$  a.u. [22]), and they react together for at impact energies E > 40 keV (inter-shell screening). As already mentioned, at higher energies, inter-shell screening is possible for other subshells (i.e., 4p-4d for impact energies above 0.9 MeV), but its weight in the total stopping is minor for deeper shells.

Finally, in all our calculations [20], we assumed the projectile to be proton and not neutral hydrogen. When an ion moves inside a metal, the FEG screens the nucleus, so the binding energies will be smaller than outside the metal, and this effect is more critical at low impact velocities v. In the case of hydrogen, the difference is drastic, i.e., for H inside Hf (rs=2.07), the 1s-bound state is almost null at v<2 [39]. It is worth to mention that this assumption agrees with Ziegler SRIM code [26] but differs from CasP code [23], that predicts neutral hydrogen at very low velocities.

In Fig. 3, we display the present theoretical stopping cross section of Hf for protons using the relativistic wave functions and binding energies, but with and without the

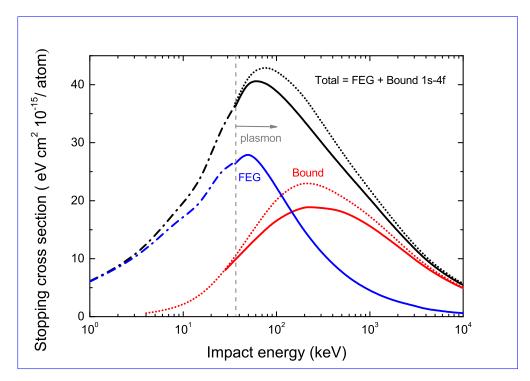


FIG. 3. Stopping power (color online) Theoretical stopping cross section sections of hafnium for protons in hafnium. Symbols: solid circles Blue dash-dotted-line, present values the non-perturbative SPCC for the FEG; open circles, previous data [7]. Curves: Black blue solid-line, present full theoretical ML results for the FEG (includes plasmon excitation); red solid and dotted-lines, the SLPA results for bound electrons with 4f-and without 5p-4f screening; violet dashed line, values from ICRU 49 [27] respectively. Black curves, total stopping adding the FEG and green dotted line bound 1s-4f contributions: dash-dotted-line, SRIM-2013 [26]SPCC (FEG) + SLPA (bound); solid-line, ML (FEG) + SLPA (bound) with 4f-5p screening; dotted-line, ML (FEG) + SLPA (bound) without 4f-5p screening. The vertical grey dashed-line indicates the energy of 37 keV above which plasmon excitation is possible.

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5p-4f screening. We added show the FEG and the bound 320 electron contributions as explained aboves eparately and 321 the total stopping as the addition of both of them. The minimum energy for plasmon excitation was estimated to at approximately 37 keV. We used the non-perturbative<sub>323</sub> SPCC model for impact energies  $E \leq 37$  keV, and the<sub>324</sub> perturbative ML calculation above this energy. Clearly, 325 considering value. Bound 1s-4f electrons (relativistic<sub>326</sub> wave functions and binding energies) are calculated<sub>327</sub> with the SLPA and shown separately in Fig. 3 with 328 and without the 4f-5p screening. Below  $\sim 40$  keV, the difference between both calculations is negligible. 330 Considering 5p-4f electrons as a single group of 20 electrons with screening among them gives lower stopping values than the addition of the separate 5p and 4f contributions. Notice that this shell correction can only be considered within a many electron model be considered naturally within a many-electron model, such as the 336 SLPA.

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## IV. ANALYSIS OF THE RESULTS AND DISCUSSION

The present data and theoretical results are displayed in Table I, and Fig. 4. As can be seen in Table Iobserved, an overall relative uncertainty of around 5% was achieved for the experimental stopping power values, which are mainly due to the uncertainty in the hafnium foil thickness.

In Fig. 4 . we have good synthesizes the results of the present work. The agreement between the present theoretical results and the new measurements displayed in Table I is excellent. Present measurements using the transmission method are in good agreement with the previous data by Sirotinin [7], which were measured in backscattering geometry. Our theoretical approach also agrees with previous the data by Sirotinin [7], except for the lowest energy measurement at 80 keV. It is interesting that We have also included in this figure the theoretical curves from the CasP5.2 code by Grande and Schiwietz [23, 24] and from the DPASS code by Sigmund and Schinner [25] , both available online. Furthermore, we incorporated the semi-empirical results from SRIM-2013 [26] and the ICRU49 tables [27]. Interestingly, our full theoretical

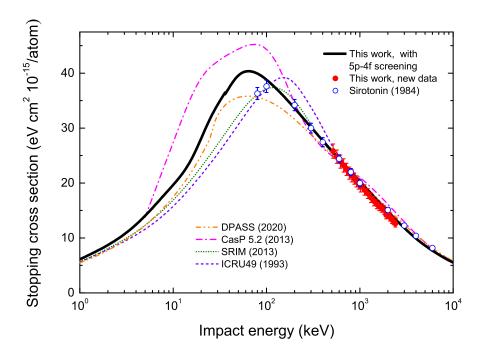


FIG. 4. (color online) Stopping power cross section of hafnium for protons. Symbols: solid circles, present values; open circles, previous data [7]. Curves: Black solid-line, present full theoretical results with 4f-5p screening; pink dash-dot line, theoretical CasP5.2 [23, 24] values; orange dash-double-dot line, theoretical DPASS [25] results; green dotted-line, semi-empirical SRIM-2013 [26]; violet dashed-line, ICRU49 [27] tabulated values.

TABLE I. Stopping power values  $S_{\overline{exp}_{oexp}}$  of hafnium for protons measured in this work.  $\Delta E/E$  values are also shown.

$\mathrm{E}_{\overline{avg}}$ ayg $_{\sim}$	$S_{\overline{exp}}_{\overline{exp}}$	$\Delta E/E$	Eavg avg	$S_{\overline{exp}}_{-\exp_{\sim}}$	$\Delta E/E$	Eavg avg	$S_{\overline{exp}}_{-\exp_{\sim}}$
keV	$eV/(10^{15} at/cm^2)$	<del>%_</del> %	keV	$eV/(10^{15} at/cm^2)$	<del>%_</del> %_	keV	$eV/(10^{15} \text{ at/cm}^2)$
<del>516,6</del> - <u>516.6</u>	$\frac{25.8}{25.8}$ $\pm \frac{1.3}{1.3}$	20,5-20.5	<del>1170,3</del> - <u>1170.3</u>	$18,25$ $18.25$ $\pm 0,91$ $0.91$	6,4-6.4	<del>1813,4</del> – <u>1813.4</u>	$15,10$ $15.10$ $\pm 0,76$ $0.76$
$\underline{567,8}\underline{567.8}$	$\frac{24.8}{24.8}$ $\pm \frac{1.2}{1.2}$	17,9 $17.9$	<del>1220,0</del> - <u>1220.0</u>	$18,08 - 18.08 \pm 0,90 - 0.90$	<del>6,1</del> - <u>6.1</u>	1862,7	$14,79$ $14.79$ $\pm 0,74$ $0.74$
$\underline{618,8}\underline{618.8}$	$23.9 - 23.9 \pm 1.2 - 1.2$	<del>15,8</del> - <u>15.8</u>	1269,6-1269.6	$17.57 - 17.57 \pm 0.88 - 0.88$	<del>5,7</del> <u>5.7</u>	<del>1912,0</del> - <u>1912.0</u>	$14,21$ - $14.21$ $\pm 0,71$ - $0.71$
669,6-669.6	$23,2$ $23.2$ $\pm 1,2$ $1.2$	<del>14,2</del> - <u>14.2</u>	<del>1319,2</del> -1319.2	$17.32 \pm 0.87$	<del>5,4</del> - <u>5.4</u>	<del>1961,2</del> - <u>1961.2</u>	$14,46$ $14.46$ $\pm 0,72$ $0.72$
720,1-720.1	$\frac{22,5}{22.5}$ $\pm \frac{1,1}{1.1}$	$\underbrace{12,8}_{-12.8}$	1368,8-1368.8	$17,15$ $17.15$ $\pm 0,86$ $0.86$	<del>5,1</del> - <u>5.1</u>	2010,4-2010.4	$14,34$ $14.34$ $\pm 0,72$ $0.72$
770,5 $770.5$	$21.8 - 21.8 \pm 1.1 - 1.1$	<del>11,6</del> - <u>11.6</u>	<del>1418,3</del> - <u>1418.3</u>	$16,69 - 16.69 \pm 0,83 - 0.83$	4,8 4.8	<del>2059,6</del> - <u>2059.6</u>	$13.76 - 13.76 \pm 0.69 - 0.69$
$820,8 \underbrace{820.8}_{0$	$21.3 \pm 1.1 \pm 1.1$	$\underbrace{10,7}_{-10.7}$	<del>1467,8</del> - <u>1467.8</u>	$16,43$ $16.43$ $\pm 0,82$ $0.82$	4,6-4.6	<del>2108,8</del> <u>2108.8</u>	$\frac{13,78-13.78}{13.78} \pm \frac{0,69-0.69}{10.00}$
<del>871,0</del> <u>871.0</u>	$20.8 - 20.8 \pm 1.0 - 1.0$	$9.8_{-9.8}$		$16.13 - 16.13 \pm 0.81 - 0.81$			$\frac{13,70}{13.70} \pm \frac{0,69}{0.69} = 0.69$
921,1 - 921.1	$20.3 - 20.3 \pm 1.0 - 1.0$	$9,1$ $\stackrel{9}{\sim}$ $\stackrel{1}{\sim}$	<del>1566,7</del> - <u>1566.7</u>	$16.04 \pm 0.80 \pm 0.80$			$43,33$ $\pm 0,67$ $0.67$
971,1  971.1	$\frac{19.9-19.9}{10.0} \pm \frac{1.0-1.0}{10.0}$	$8,4$ $\overset{8}{\sim}$ $\overset{4}{\sim}$	<del>1616,0</del> - <u>1616.0</u>	$15,77$ $15.77$ $\pm 0,79$ $0.79$	4,0-4.0	<del>2256,4</del> <u>2256.4</u>	$\frac{13,27}{13.27} \pm \frac{0,66}{0.66} \pm \frac{0.66}{0.66}$
1021,0 $1021.0$	$\underline{19,33},\underline{19.33},\pm 0,97,\underline{0.97}$	<del>7,8</del> -7.8	<del>1665,4</del> - <u>1665.4</u>	$15,51$ $15.51$ $\pm 0,78$ $0.78$	<del>3,8</del> <u>3.8</u>	<del>2305,5</del> <u>2305.5</u>	$13.07 - 13.07 \pm 0.65 - 0.65$
<del>1070,8</del> <u>1070.8</u>	$\frac{19,03}{19.03}$ $\pm \frac{0,95}{0.95}$	$\frac{7,3}{2}$ .3	<del>1714,8</del> <u>1714.8</u>	$15,46$ $15.46$ $\pm 0,77$ $0.77$	<del>3,7</del> <u>3.7</u>	<del>2354,7</del> <u>2354.7</u>	$12.91 - 12.91 \pm 0.65 - 0.65$
<del>1120,6</del> - <u>1120.6</u>	$18,73$ $18.73$ $\pm 0,94$ $0.94$	6,9 $6.9$	$ \frac{1764,1}{1764,1}$	$14.93 - 14.93 \pm 0.75 - 0.75$	<del>3,5</del> _3.5	<del>2403,8</del> <u>2403.8</u>	$\frac{12,61}{12.61} \pm \frac{0,63}{0.63} \pm \frac{0.63}{0.63}$

curve differs from SRIM-2013 for impact energies be- $_{350}$  low 100 keV. We obtain a stopping maximum around $_{351}$   $40 \times 10^{-15}$  of approximately  $40 \times 10^{-15}$  eV cm $^2$ /atom $_{352}$  at 65 keV. Instead, following the up-to-now only set of  $_{353}$  data  $_{-[7]}$ , SRIM-2013 suggests a lower stopping maxi- $_{354}$  mum at an impact energy of 115 kevkeV. The stopping  $_{355}$ 

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maximum is a susceptible region for any full theoretical description without parameters, and this is quite visible in a linear-scale plot like Fig. 4. However, the impact energy for the maximum seems to agree between our curve and DPASS, although it is 10% below. Instead, CasP a maximum value of the stopping power 10% above

our value and a completely different shape at lower<sup>390</sup> energies. It is worth mentioning that similar theoretical<sup>391</sup> our model gives similar results using the experimental<sup>392</sup> value  $r_S = 2.07$  a.u. instead of the theoretical rather<sup>393</sup> than the theoretical one  $r_S = 2.14$  a.u.give., with the<sup>394</sup> stopping maximum at the same impact energy but 4%<sup>395</sup> higher.

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Future experiments for impact energies below 100 keV<sub>397</sub> would be important essential to complete this study on<sub>398</sub> the stopping of Hf for protons. In the energy region<sub>399</sub> 80 – 500 keV, only the measurements by Sirotinin's<sub>400</sub> group [7] from 1984 are available. SRIM-2013 includes<sub>401</sub> these values in the code fitting, so it does not represent a<sub>402</sub> test for this data. Undoubtedly, new measurements are<sub>403</sub> needed in three specific energy regions: below 500 keV, <sub>404</sub> around the stopping maximum (i.e., 50 – 200 keV), and<sub>405</sub> at low impact energies.

#### V. CONCLUSION

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In this work, we have used the transmission method<sup>411</sup> to experimentally determine stopping power cross sec-412 tion values for (0.6-2.5) MeV protons incident on self-413 supporting Hf foils with an overall uncertainty of around 5%. Additionally, we calculated values extracted from the theoretical framework that involved the relativis-414 tic wave functions and binding energies of Hf , and considered 4-and considered four electrons per atom in<sub>415</sub> the free electron gas. The shell-wise local plasma approx-416 imation was employed to describe the energy transferred 417 to the bound 1s-4f electrons, and two different models<sub>418</sub> for the FEG: the screened potential with cusp condition419 (SPCC model) for energies below that of the plasmon ex-420 citation, and the Mermin-Lindhard dielectric formalism, 421 for energies around the stopping maximum and above.422 Present theoretical stopping cross sections cover an ex-423 tensive energy range from 1 keV/ $\frac{10 \text{ meV}}{\text{amu}}$  to 10 MeV/amu.

At high impact energies, the new stopping measurements are in good agreement with our theoretical results, with previous experimental data and semi-empirical values by SRIM-2013 and ICRU-49. However, we call the attention that around the stopping maximum and at lower impact energies, the difference between our full-theoretical results and SRIM is substantial. We compare our theoretical results with two other models given by the DPASS and CasP5.2 codes. Differences can be noted at intermediate to low impact energies, but they also support a stopping maximum at lower energy than SRIM predictions.

To the best of our knowledge, these are the first theoretical calculations of stopping in Hf taking into account the atomic relativistic effects to take into account relativistic effects in the atomic structure and screening among electrons in a consistent way, from very low to high impact energies. Future experiments for impact energies below 100 keV would be important to complete this study. around the stopping maximum and in the low energy region would be essential to have a better understanding of the stopping of protons in hafnium.

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